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- Model the problem as a graph! Puddles are the nodes, moats the edges.
- They can meet at some puddle if the graph is connected
 - Start BFS or DFS at any node and check if all nodes were visited.

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 - Nodes can be in the queue at most degree times
 - Broken: mark as visited when popping, check for visited when looking at neighbors
 - Nodes are processed multiple times, which can amplify arbitrarily

Problem: In a 2-colorable graph, which color has a higher weight.

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- Runtime $\mathcal{O}(n+m)$

Problem: Given a chess board output the shortest path from a knight to the black king.

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- Alternatively run a BFS from every white knight at once

Problem: Find any topological sorting of a DAG

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- there's also a DFS-based algorithm

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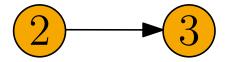
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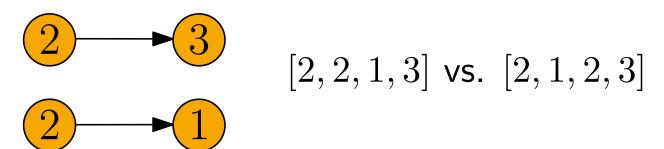
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Problem: Find the minimum battery capacity to reach 75% of the *other* cities

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- Now do a binary search to find the minimum needed capacity