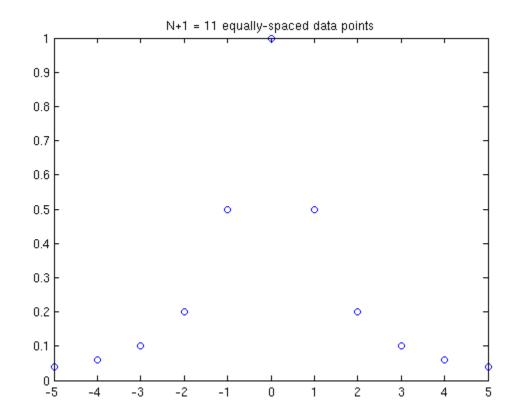
Lab 4

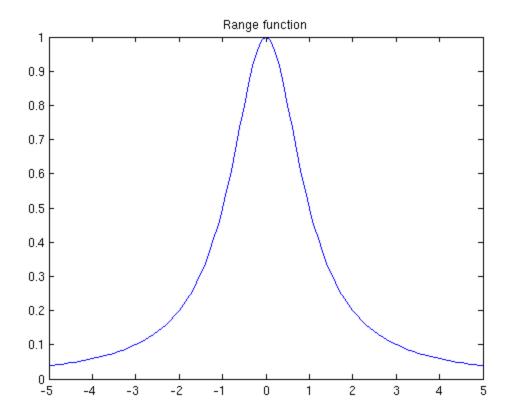
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Problem 1

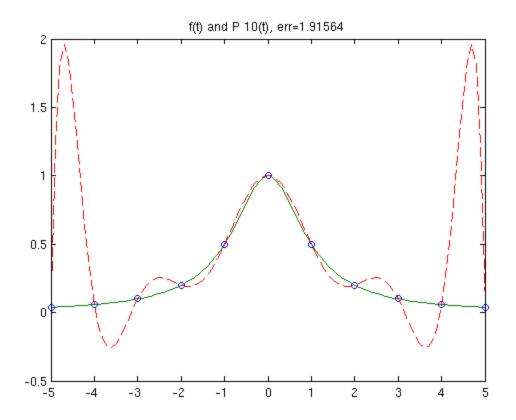
```
N = 10;
x = linspace(-5,5,N+1);
f = inline('1./(1+x.*x)','x');
y = f(x);
plot(x, y, 'o');
title('N+1 = 11 equally-spaced data points');
t = [-5:.1:5];
figure;
plot(t, f(t), '-');
title('Range function');
```





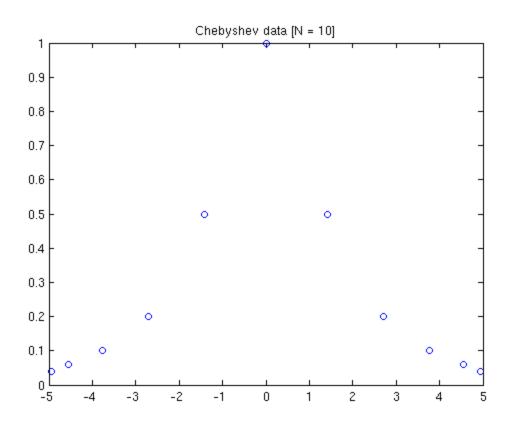
Problem 2

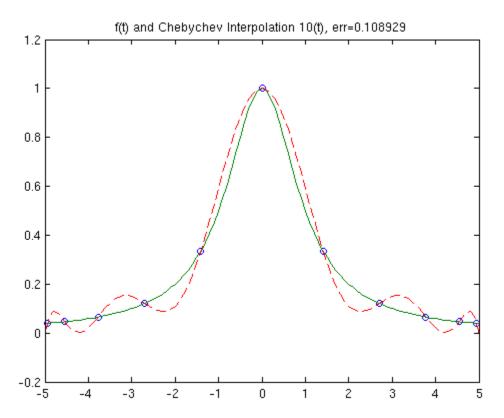
```
PN = polyfit(x,y,N);
v = polyval(PN,t);
err = norm(f(t)-v,inf);
figure;
plot(x,y,'o',t,f(t),'-',t,v,'--')
title(sprintf('f(t) and P {10}(t), err=%g',err))
```



Problem 3

```
K = N+1;
a = -5;
b = 5;
xcheb = zeros(1,K);
for i=1:K
    xcheb(i)=(a+b)/2 + (b-a)/2 * cos((i-.5)*pi/K);
end
plot(xcheb, y, 'o');
title('Chebyshev data [N = 10]');
ycheb = f(xcheb);
PNcheb = polyfit(xcheb,ycheb,N);
vcheb = polyval(PNcheb,t);
cheberr = norm(f(t)-vcheb,inf);
figure;
plot(xcheb, ycheb, 'o', t, f(t), '-', t, vcheb, '--');
title(sprintf('f(t) and Chebychev Interpolation {10}(t), err=%g',cheberr))
```





The polynomial interpolation provided by matlabs polyfit finds the coefficients of a p(x) that fit a vector of X points. The interpolation that happens in Problem 2 uses N equally spaced points (shown in Figure 1) and yeilds a polynomial that interpolates the points but also has a lot of error at the ends of the interval (in this case near -5 and 5). The Chebychev polynomial in problem 3 uses X values generated using the equation $\frac{(a+b)}{2} + \frac{(b-a)}{2} \cdot \frac{cos((i-.5)*pi/K)}{2}$. You can see in Figure 3 that the x values used in the Chebychev polynomial are bunched up near the ends of the interval (-5 to 5). The high error at the ends of the polynomial in Problem 2 is an example of Runge's phenomenom. The chebyshev points help mitigate the error poblem by using a least squares method to ensure a minimum maximum error.

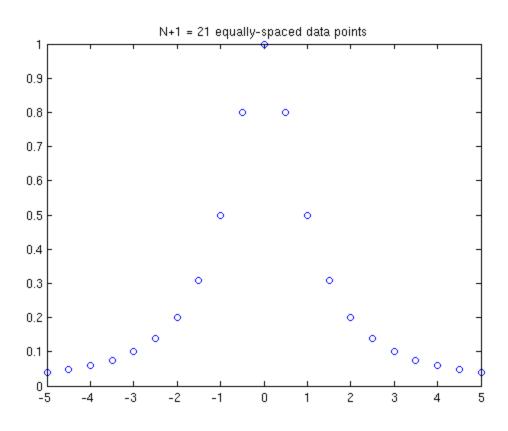
Problem 4

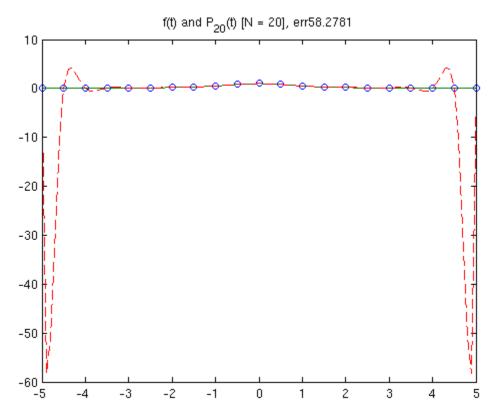
As the number of nodes increases, the error in an interpolating polynomial with equally spaced X values becomes exteremely bad at the end of it's interval. In contrast, the polynomial using chebyshev points get's more and more accurate.

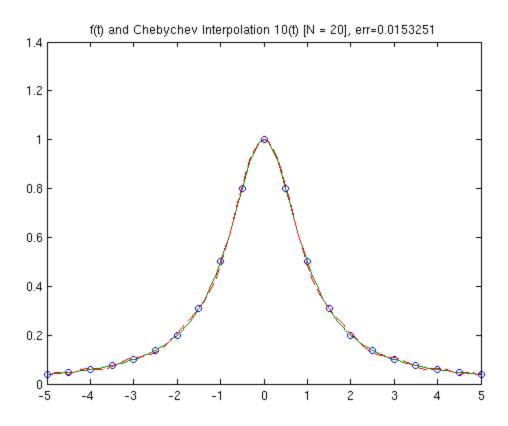
Here are the cases when N = 20 and N = 50 and then 50.

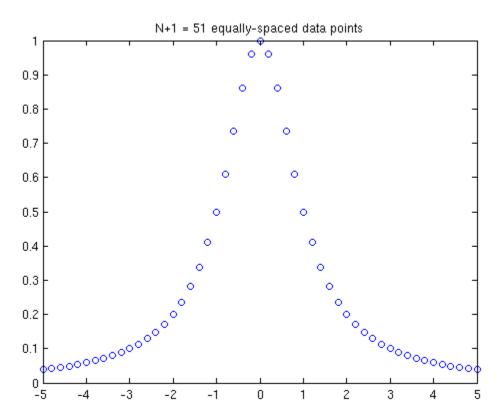
```
N = 20;
x = linspace(-5, 5, N+1);
f = inline('1./(1+x.*x)', 'x');
y = f(x);
figure;
plot(x,y,'o');
title('N+1 = 21 equally-spaced data points');
t = [-5:.1:5];
PN = polyfit(x,y,N);
v = polyval(PN,t);
err = norm(f(t)-v, inf);
figure;
plot(x,y,'o',t,f(t),'-',t,v,'--');
title(sprintf('f(t) and P_{20}(t) [N = 20], err g', err));
K = N+1;
a = -5;
b = 5;
xcheb = zeros(1,K);
for i=1:K
    xcheb(i)=(a+b)/2 + (b-a)/2 * cos((i-.5)*pi/K);
end
ycheb = f(xcheb);
PNcheb = polyfit(xcheb,ycheb,N);
vcheb = polyval(PNcheb,t);
cheberr = norm(f(t)-vcheb,inf);
figure;
plot(x,y,'o',t,f(t),'-',t,vcheb,'--')
title(sprintf('f(t) and Chebychev Interpolation \{10\}(t) [N = 20], err=%g',cheberr)
% N = 50
N = 50;
```

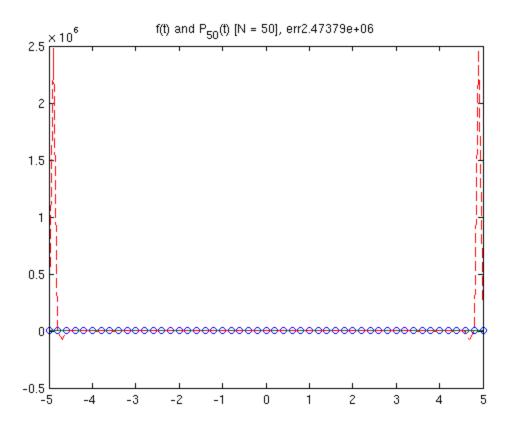
```
x = linspace(-5,5,N+1);
f = inline('1./(1+x.*x)', 'x');
y = f(x);
figure;
plot(x,y,'o');
title('N+1 = 51 equally-spaced data points');
t = [-5:.1:5];
PN = polyfit(x,y,N);
v = polyval(PN,t);
err = norm(f(t)-v, inf);
figure;
plot(x,y,'o',t,f(t),'-',t,v,'--');
title(sprintf('f(t) and P_{50}(t) [N = 50], err g', err));
K = N+1;
a = -5;
b = 5;
xcheb = zeros(1, K-1);
for i=1:K
    xcheb(i)=(a+b)/2 + (b-a)/2 * cos((i-.5)*pi/K);
end
ycheb = f(xcheb);
PNcheb = polyfit(xcheb,ycheb,N);
vcheb = polyval(PNcheb,t);
cheberr = norm(f(t)-vcheb,inf);
figure;
plot(x,y,'o',t,f(t),'-',t,vcheb,'--')
title(sprintf('f(t)) and Chebychev Interpolation \{10\}(t) [N = 50], err= g', cheberr)
        Warning: Polynomial is badly conditioned. Add points with distinct X
                 values, reduce the degree of the polynomial, or try centering
                 and scaling as described in HELP POLYFIT.
        Warning: Polynomial is badly conditioned. Add points with distinct X
                 values, reduce the degree of the polynomial, or try centering
                 and scaling as described in HELP POLYFIT.
        Warning: Polynomial is badly conditioned. Add points with distinct X
                 values, reduce the degree of the polynomial, or try centering
                 and scaling as described in HELP POLYFIT.
        Warning: Polynomial is badly conditioned. Add points with distinct X
                 values, reduce the degree of the polynomial, or try centering
                 and scaling as described in HELP POLYFIT.
```











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