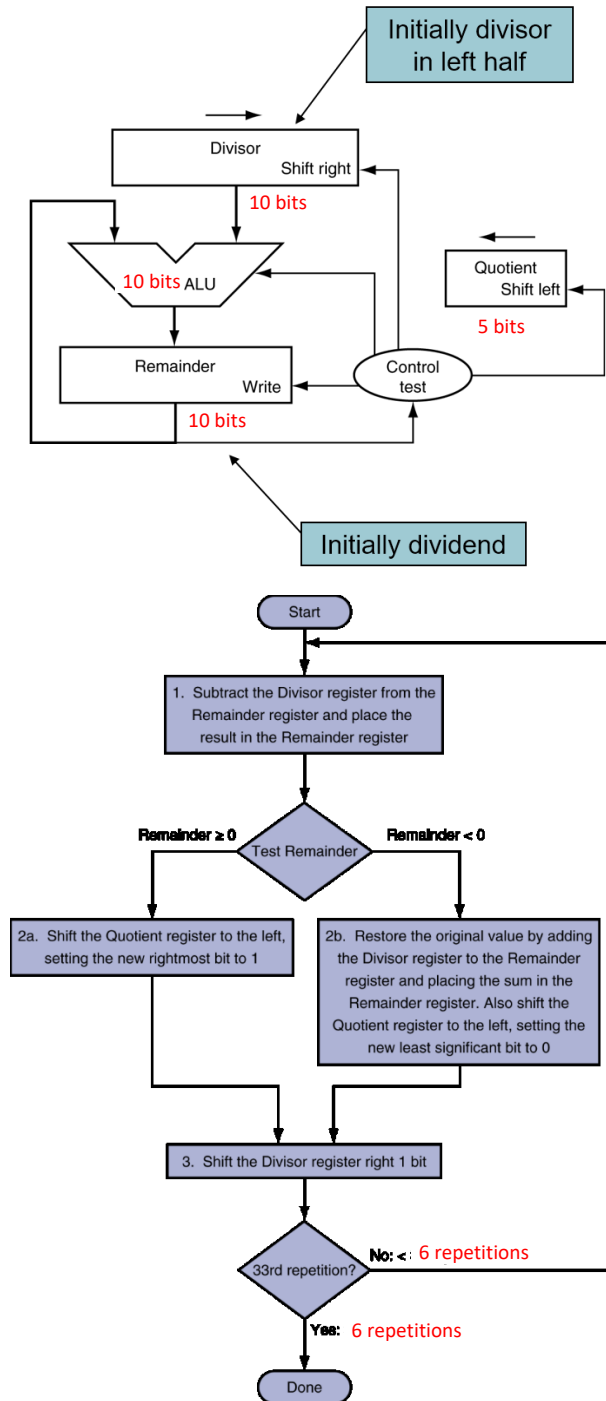


HW#8 (CSC 390): SOLUTION

Q1. The following Circuit performs the division of two 32-bit unsigned binary numbers and produces the Quotient and Remainder in the respective registers. Figure 1 shows the three steps division algorithm that the circuit performs to produce the result. Suppose, you are assigned to design a 5-bit division circuit that will perform the division of the two 5-bit unsigned numbers $A=(11011)_2$ and $B=(00101)_2$ and produce the Quotient and Remainder of the division. Draw the necessary hardware and show the results produced in each iteration of your algorithm. Hints: see figure 3.10 (page 192) of our text book.



Iteration	Step	Quotient	Divisor	Remainder
0	Initial Value	00000	0010100000	0000011011
1	1: Rem = Rem - Div	00000	0010100000	1101111011
	2b : Rem < 0 => +Div, sll Q, Q0 = 0	00000	0010100000	0000011011
	3: Shift Div right	00000	0001010000	0000011011
2	1: Rem = Rem - Div	00000	0001010000	1111001011
	2b : Rem < 0 => +Div, sll Q, Q0 = 0	00000	0001010000	0000011011
	3: Shift Div right	00000	0000101000	0000011011
3	1: Rem = Rem - Div	00000	0000101000	1111110011
	2b : Rem < 0 => +Div, sll Q, Q0 = 0	00000	0000101000	0000011011
	3: Shift Div right	00000	0000010100	0000011011
4	1: Rem = Rem - Div	00000	0000010100	0000000111
	2a : Rem ≥ 0 => sll Q, Q0 = 1	00001	0000010100	0000000111
	3: Shift Div right	00001	0000001010	0000000111
5	1: Rem = Rem - Div	00001	0000001010	1111111101
	2b : Rem < 0 => +Div, sll Q, Q0 = 0	00010	0000001010	0000000111
	3: Shift Div right	00010	0000000101	0000000111
6	1: Rem = Rem - Div	00010	0000000101	0000000010
	2a : Rem ≥ 0 => sll Q, Q0 = 1	00101	0000000101	0000000010
	3: Shift Div right	00101	0000000010	0000000010

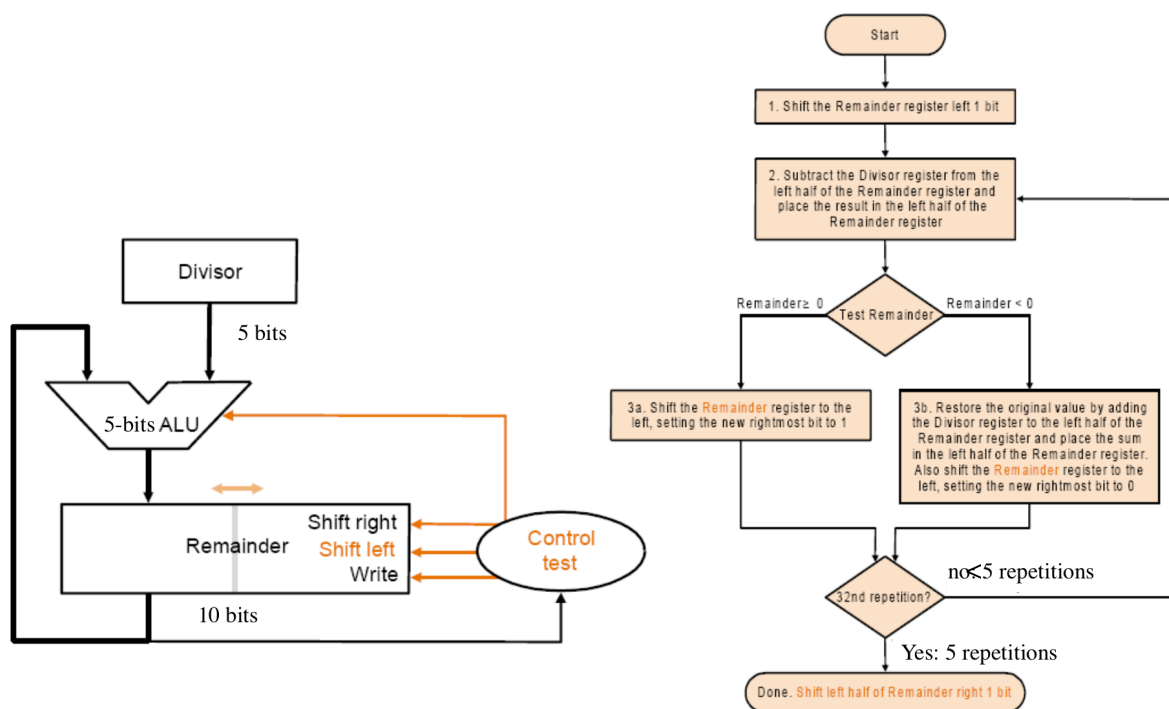
$A=(11011)_2 \rightarrow 27$; $B=(00101)_2 = 5$; $A/B = 27/5 \rightarrow$

Quotient = 5 \rightarrow **000101** and

Remainder = 2 \rightarrow **00010**

Q2.

Iteration	Divisor	Hardware design	
		Step	Remainder
0	00101	Initial value	00000 11011
		Shift remainder left by 1	00001 10110
1	00101	Remainder = remainder -division	11100 10110
		Remainder < 0 => +division, shift left; r0 = 0	00011 01100
2	00101	Remainder = remainder -division	11110 01100
		Remainder < 0 => +division, shift left; r0 = 0	00110 11000
3	00101	Remainder = remainder -division	00001 11000
		Remainder > 0 => shift left; r0 = 1	00011 10001
4	00101	Remainder = remainder -division	11110 10001
		Remainder < 0 => +division, shift left; r0 = 0	00111 00010
5	00101	Remainder = remainder -division	00010 00010
		Remainder > 0 => shift left; r0 = 1	00100 00101
Done	00101	Shift "left half of remainder" right by 1	00010 00101



Quotient: 00101

Remainder 00010

Q3.

$$\bullet (6.725)_{10} = 110.101110011001100110011_2 = 1.10101110011001100110011_2 \times 2^2$$

So, we represent $(6.725)_{10}$ as

$$(-1)^0 \times (1 + 10101110011001100110011_2) \times (2)^2$$

$$S = 0$$

$$\text{fraction} = 10101110011001100110011$$

$$\text{exponent} = 2 + \text{bias} = 2 + 127 = 129_{10} = 10000001_2$$

=> Floating point format:

$$0100\ 0000\ 1101\ 0111\ 0011\ 0011\ 0011\ 0011_2 = \mathbf{40d73333}_{16}$$

$$\bullet -0.3125_{10} = 0.0101_2 = 1.01_2 \times 2^{-2}$$

So, we represent -0.3125_{10} as

$$(-1)^{-1} \times (1 + 0.01_2) \times 2^{-2}$$

$$S = 1$$

$$\text{fraction} = 010000000000000000000000$$

$$\text{exponent} = -2 + \text{bias} = -2 + 127 = 125_{10} = 01111101_2$$

=> Floating point format:

$$1011\ 1110\ 1010\ 0000\ 0000\ 0000\ 0000\ 0000_2 = \mathbf{BEA00000}_{16}$$

Address	Value (+0)	Value (+4)	Value (+8)	Value (+c)	Value (+10)	Value (+14)	Value (+18)	Value (+1c)
0x10010000	0x40d73333	0xbea00000	0x00000000	0x00000000	0x00000000	0x00000000	0x00000000	0x00000000