

HW#2 (CSC390)-SOLUTION

1.11

1.11.1 $\text{CPI} = \text{clock rate} \times \text{CPU time} / \text{instr. count}$

$$\text{clock rate} = 1 / \text{cycle time} = 3 \text{ GHz}$$

$$\text{CPI}(\text{bzip2}) = 3 \times 10^9 \times 750 / (2389 \times 10^9) = 0.94$$

1.11.2 $\text{SPEC ratio} = \text{ref. time} / \text{execution time}$

$$\text{SPEC ratio}(\text{bzip2}) = 9650 / 750 = 12.86$$

1.11.3. $\text{CPU time} = \text{No. instr.} \times \text{CPI} / \text{clock rate}$

If CPI and clock rate do not change, the CPU time increase is equal to the increase in the of number of instructions, that is 10%.

1.11.4 $\text{CPU time}(\text{before}) = \text{No. instr.} \times \text{CPI} / \text{clock rate}$

$$\text{CPU time}(\text{after}) = 1.1 \times \text{No. instr.} \times 1.05 \times \text{CPI} / \text{clock rate}$$

$\text{CPU time}(\text{after}) / \text{CPU time}(\text{before}) = 1.1 \times 1.05 = 1.155$. Thus, CPU time is increased by 15.5%.

1.11.5 $\text{SPECratio} = \text{reference time} / \text{CPU time}$

$\text{SPECratio}(\text{after}) / \text{SPECratio}(\text{before}) = \text{CPU time}(\text{before}) / \text{CPU time}(\text{after}) = 1 / 1.155 = 0.86$. The SPECratio is decreased by 14%.

1.11.6 $\text{CPI} = (\text{CPU time} \times \text{clock rate}) / \text{No. instr.}$

$$\text{CPI} = 700 \times 4 \times 10^9 / (0.85 \times 2389 \times 10^9) = 1.37$$

1.11.7 $\text{Clock rate ratio} = 4 \text{ GHz} / 3 \text{ GHz} = 1.33$

$$\text{CPI @ 4 GHz} = 1.37, \text{CPI @ 3 GHz} = 0.94, \text{ratio} = 1.45$$

They are different because, although the number of instructions has been reduced by 15%, the CPU time has been reduced by a lower percentage.

1.11.8 $700 / 750 = 0.933$. CPU time reduction: 6.7%

1.11.9 $\text{No. instr.} = \text{CPU time} \times \text{clock rate} / \text{CPI}$

$$\text{No. instr.} = 960 \times 0.9 \times 4 \times 10^9 / 1.61 = 2146 \times 10^9$$

1.11.10 $\text{Clock rate} = \text{No. instr.} \times \text{CPI} / \text{CPU time}$.

$$\text{Clock rate}_{\text{new}} = \text{No. instr.} \times \text{CPI} / 0.9 \times \text{CPU time} = 1 / 0.9 \text{ clock rate}_{\text{old}} = 3.33 \text{ GHz}$$

1.11.11 $\text{Clock rate} = \text{No. instr.} \times \text{CPI} / \text{CPU time}$.

$$\text{Clock rate}_{\text{new}} = \text{No. instr.} \times 0.85 \times \text{CPI} / 0.80 \text{ CPU time} = 0.85 / 0.80, \text{clock rate}_{\text{old}} = 3.18 \text{ GHz}$$

1.13

1.13.1 $T_{fp} = 70 \times 0.8 = 56$ s. $T_{new} = 56 + 85 + 55 + 40 = 236$ s. Reduction: 5.6%

1.13.2 $T_{new} = 250 \times 0.8 = 200$ s, $T_{fp} + T_{l/s} + T_{branch} = 165$ s, $T_{int} = 35$ s. Reduction time INT: 58.8%

1.13.3 $T_{new} = 250 \times 0.8 = 200$ s, $T_{fp} + T_{int} + T_{l/s} = 210$ s. NO

1.14

1.14.1 Clock cycles = $CPI_{fp} \times \text{No. FP instr.} + CPI_{int} \times \text{No. INT instr.} + CPI_{l/s} \times \text{No. L/S instr.} + CPI_{branch} \times \text{No. branch instr.}$

$$T_{CPU} = \text{clock cycles} / \text{clock rate} = \text{clock cycles} / 2 \times 10^9$$

$$\text{clock cycles} = 512 \times 10^6; T_{CPU} = 0.256 \text{ s}$$

To have the number of clock cycles by improving the CPI of FP instructions:

$$CPI_{improved\ fp} \times \text{No. FP instr.} + CPI_{int} \times \text{No. INT instr.} + CPI_{l/s} \times \text{No. L/S instr.} + CPI_{branch} \times \text{No. branch instr.} = \text{clock cycles} / 2$$

$$CPI_{improved\ fp} = (\text{clock cycles} / 2 - (CPI_{int} \times \text{No. INT instr.} + CPI_{l/s} \times \text{No. L/S instr.} + CPI_{branch} \times \text{No. branch instr.})) / \text{No. FP instr.}$$

$$CPI_{improved\ fp} = (256 - 462) / 50 < 0 \Rightarrow \text{not possible}$$

1.14.2 Using the clock cycle data from a.

To have the number of clock cycles improving the CPI of L/S instructions:

$$CPI_{fp} \times \text{No. FP instr.} + CPI_{int} \times \text{No. INT instr.} + CPI_{improved\ l/s} \times \text{No. L/S instr.} + CPI_{branch} \times \text{No. branch instr.} = \text{clock cycles} / 2$$

$$CPI_{improved\ l/s} = (\text{clock cycles} / 2 - (CPI_{fp} \times \text{No. FP instr.} + CPI_{int} \times \text{No. INT instr.} + CPI_{branch} \times \text{No. branch instr.})) / \text{No. L/S instr.}$$

$$CPI_{improved\ l/s} = (256 - 198) / 80 = 0.725$$

1.14.3 Clock cycles = $CPI_{fp} \times \text{No. FP instr.} + CPI_{int} \times \text{No. INT instr.} + CPI_{l/s} \times \text{No. L/S instr.} + CPI_{branch} \times \text{No. branch instr.}$

$$T_{CPU} = \text{clock cycles} / \text{clock rate} = \text{clock cycles} / 2 \times 10^9$$

$$CPI_{int} = 0.6 \times 1 = 0.6; CPI_{fp} = 0.6 \times 1 = 0.6; CPI_{l/s} = 0.7 \times 4 = 2.8; CPI_{branch} = 0.7 \times 2 = 1.4$$

$$T_{CPU} (\text{before improv.}) = 0.256 \text{ s}; T_{CPU} (\text{after improv.}) = 0.171 \text{ s}$$