

## Answers

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Programming Languages: Java, Scala, Python,  
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### Question 3:

$\text{nullable}([c_1, c_2, \dots, c_n])$	$\stackrel{\text{def}}{=}$	<u>false</u>
$\text{nullable}(r^+)$	$\stackrel{\text{def}}{=}$	<u><math>\text{nullable}(r \cdot r^+)</math></u>
$\text{nullable}(r^?)$	$\stackrel{\text{def}}{=}$	<u>true</u>
$\text{nullable}(r_1 \& r_2)$	$\stackrel{\text{def}}{=}$	<u><math>\text{nullable}(r_1) \&amp; \text{nullable}(r_2)</math></u>
$\text{nullable}(r^{\{n\}})$	$\stackrel{\text{def}}{=}$	<u>if <math>n == 0</math> true</u> <u>else <math>\text{nullable}(r \cdot r^{\{n-1\}})</math></u>
$\text{nullable}(r^{\{-m\}})$	$\stackrel{\text{def}}{=}$	<u>if <math>m \geq 0</math> true</u> <u>else false</u>
$\text{nullable}(r^{\{n.. \}})$	$\stackrel{\text{def}}{=}$	<u>if <math>n == 0</math> true</u> <u>else <math>\text{nullable}(r \cdot r^{\{n-1.. \}})</math></u>
$\text{nullable}(r^{\{n..m\}})$	$\stackrel{\text{def}}{=}$	<u>if <math>n == 0</math> true</u> <u>else false</u>
$\text{nullable}(\sim r)$	$\stackrel{\text{def}}{=}$	<u><math>! (\text{nullable}(r))</math></u>

$der\ c([c_1, c_2, \dots, c_n]) \stackrel{def}{=} \text{if } [c_1, \dots, c_n].contains(c) \mid \text{else } 0$   
 $der\ c(r^+) \stackrel{def}{=} (der\ (c, r)) \{1..\}$   
 $der\ c(r^?) \stackrel{def}{=} der\ (c, r) + 1$   
 $der\ c(r_1 \& r_2) \stackrel{def}{=} (der\ c\ r_1) \& (der\ c\ r_2)$   
 $der\ c(r^{\{n\}}) \stackrel{def}{=} \text{if } n == 0 \mid 0$   
 $\text{else } der\ (c, r) \cdot r^{\{n-1\}}$   
 $der\ c(r^{\{..m\}}) \stackrel{def}{=} \text{if } m == 0 \mid 0$   
 $\text{else } (der\ (c, r) \cdot r^{\{n-1\}}) + 1$   
 $der\ c(r^{\{n.. \}}) \stackrel{def}{=} \text{if } n == 0 \mid 1$   
 $\text{else } (der\ c\ r) \cdot r^{\{n-1..\}}$   
 $der\ c(r^{\{n..m\}}) \stackrel{def}{=} \text{if } n == 0 \&\& m == 0 \mid 0$   
 $\text{else if } n > 0 \mid (der\ c\ r) \cdot r^{\{n-1..m-1\}}$   
 $\text{else } (der\ c\ r) \cdot r^{\{n..m-1\}}$   
 $der\ c(\sim r) \stackrel{def}{=} \sim (der\ c\ r)$

#### Question 4:

$nullable(CFUN(f)) \stackrel{def}{=} \text{false}$

$der\ c(CFUN(f)) \stackrel{def}{=} \text{if } f(c) \mid$   
 $\text{else } 0$

$c \stackrel{def}{=} CFUN((-) \Rightarrow \_ == c)$

$[c_1, c_2, \dots, c_n] \stackrel{def}{=} CFUN((c) \Rightarrow [c_1..c_n].contains(c))$

$ALL \stackrel{def}{=} CFUN((-) \Rightarrow \text{true})$

Question 5 ('mathematical' notation):

$$\left( \left( [a-z 0-9 _ . - ]^* \cdot " . " \right) \cdot [a-z . ] \{ 2 .. 6 \} \right) + [a-z . ] \{ 0 .. 4 \}$$

Question 6:

1) ☒ Yes / No    2) ☒ Yes / No    3) Yes / ☒ No    4) ☒ Yes / No

Question 7:

	$r_1$	$r_2$
1.	yes	yes
2.	no	no
3.	no	yes