

Lecture 1: Logistics and Review of Rigid Body Motion

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1.1 Goals

Prepare to do research in future

- Primary Areas: nonlinear control, path planning, mobile robotics, grasping, soft robotics
- Secondary Areas: legged robotics, active safety, HRI
- Not Covered: learning, estimation, SLAM, vision, mechatronics

General Research Skills: reading papers (a lot), presenting work (at least three), and writing reports (for all four projects)

1.2 Logistics

Prerequisites

- 106A
- EE128
- Lin Alg
- Python and MatLab
- Curiosity
- Interest in experimental work

Staff emails on course website

Piazza for fastest response

Lectures: T/Th 3:30-5 pm

No exams :D

HWs are biweekly

Five slip days, max two for one hw

Must scribe at least one lecture

Paper presentation: one in lab (same as one hw), slide or word based, twenty minutes

Projects: four total, 40-60 hours, groups of three, at least one who took 106A and one with controls experience

Can reserve robot three hours at a time and can only make new reservation when current expires else five percent deduction from project grade

Project due dates on website

Proj 1: trajectory tracking with control on baxter/sawyer

Proj 2: path planning with turtlebots

Proj 3: grasping with baxter/sawyer

Proj 4: soft robotics

Final Proj:

- proposal due 3/20 and presentations will be on friday of RRR week
- should be research projects applying multiple parts of the course material including some sensingm planning, and actuation

Graduate students have more expectations that undergrads can do for extra credit

Disc

- W 2:00pm-3:00pm 237 Cory, Valmik and Amay
- W 4:00pm-5:00pm 293 Cory, Valmik and Amay

OH

- Prof. Bajcsy: Weds 11-12, Thursday 1-2 (SDH 719)
- Prof. Sastry: Tuesday 1:15-2:30 (Cory 333B)
- Tiffany: Tuesday 11-12 (Cory 111)
- Amay: Monday 4-5 (Cory 111)
- Jun: Monday 5-6 (Cory 111)
- Valmik: Tuesday 12-1, Wednesday 5-6 (Cory 111)

Labs

- Thursday 5-8pm Cory 111, Tiffany
- Friday 11am-2pm Cory 111, Amay
- Friday 2-5pm Cory 111, Jun

Should be 1.5-2 hours most days, rest will be OH

1.3 Announcements

- Look at website
- Join Piazza and Gradescope
- Disc 1 tomorrow
- Lab 0 in lab sec this week
- HW 1 assigned tomorrow
- Project 1a released this week and will be discussed during lab section

1.4 Expectations

- Emphasis on collaboration and exploration
- Ask a lot of questions
- It's okay to be confused
- Expect to work hard

1.5 Rotational Matrices

will rotate any vector q about some axis w by an angle
represented as linear transformations

$$R: R^3 \rightarrow R^3$$

$$q_A = R_{AB}q_B$$

1.6 Linear Transformations

$$T_{AA} : A \rightarrow A$$

Left Multiplication: Change output frame $R_{BA}T_{AA} : A \rightarrow B$

Right Multiplication: Change input frame $T_{AA}R_{BA} : B \rightarrow A$

Change both input and output frames: $R_{BA}T_{AA}R_{BA}^{-1} : B \rightarrow B$

1.7 Groups

Rotations as a Group

$SO(n)$ are a group of special orthogonal matrices under matrix multiplication which can represent any rotation

Properties of Rotation Matrices:

$$R^{-1} = R^T$$

$$\det(R) = +1$$

Properties of Groups:

$$\text{Closure} : \exists P, Q \in SO(n) \rightarrow PQ \in SO(n)$$

$$\text{Associativity} : \exists A, B, C \in SO(n) (AB)C = A(BC)$$

$$\text{Identity} : \exists I \in SO(n) \text{ s.t. } AI = IA = A \forall A \in SO(n)$$

$$\text{Inverse} : \forall A \in SO(n) \exists A^{-1} \in SO(n) \text{ s.t. } AA^{-1} = I$$

1.8 Lie Group

Rotations as a Lie Group

$SO(n)$ is a continuous, smooth group which means that it has a tangent space

$SO(n)$ at any point can define a tangent or derivative space

1.9 Lie Algebra

$$so(n) = \{S \in R^{n \times n} : S^T = -S\}$$

example: $so(2)$ and $so(3)$

1.10 Exponential Map

elements in lie algebra are essentially velocities moving at some velocity \hat{w} for a time T to find any element in the group

$$\dot{R}(t) = \hat{w}R(t)$$

From $t = 0$ to T :

$$e^{\hat{w}T} R(0) = e^{\hat{w}T}$$

1.11 Practice Problem

$SO(2)$'s lie group is a circle while a line tangent to the circle would be its lie algebra or $so(2)$

1.12 More Rotations

Other Parameterizations of Rotations:

Using Euler angles: $R = R_x R_y R_z$

Axis Angle same as exponential

Unit Quaternions:

also a Lie Group

rotations correspond to 2 quaternions

computationally efficient

1.13 Velocities

Rotational Velocities

When we take the derivative of a rotation, we get a tangent plane of \mathbf{R} at its current value, not $\mathfrak{so}(n)$

$$q_a = R_{ab}q_b$$

$$\frac{d}{dt}q_a = \dot{R}q_b$$

$$\dot{R} : q_b \rightarrow \dot{q}_a$$

1.14 Use Lie Groups for Rotational Velocities

Represent Rotational Velocities with $\mathrm{SO}(n)$

body velocity:

$$\hat{w}_{AB}^b = R_{AB}^{-1} \dot{R}_{AB}$$

$$= R_{BA} \dot{R}_{AB}$$

$$= \dot{R}_{BB}$$

spatial velocity

$$\hat{w}_{AB}^b = \dot{R}_{AB} R_{AB}^{-1}$$

$$= \dot{R}_{AB} R_{BA}$$

$$= \dot{R}_{AA}$$