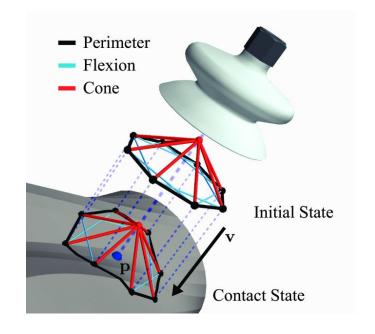
# **EECS 106B/206B**Robotic Manipulation and Interaction

Prof. Ruzena Bajcsy



## Intro to grasping





### Types of Grippers



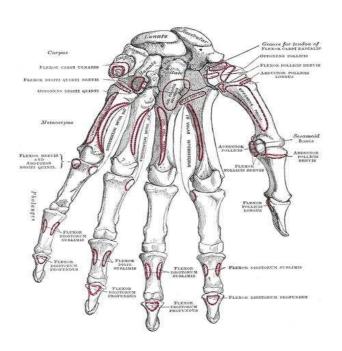




Multi-Finger



#### Hand Function



#### Hand function:

- Interface with external world
- Hand operation:
  - Grasping
  - Dextrous manipulation
  - Fine manipulation
- Exploration

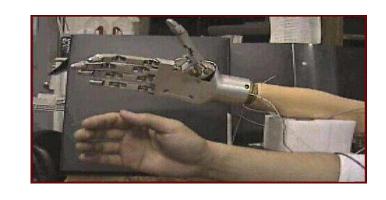
#### History of Hand Design

Prosthetic devices (1509)

Dextrous end-effectors

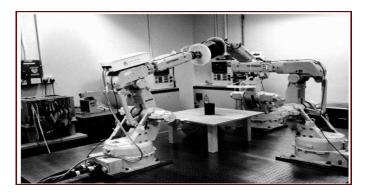
Multiple manipulator/agents coordination

Human hand study





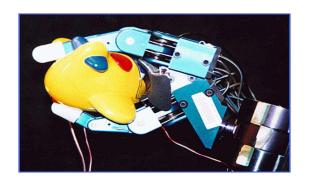




#### Hand Design Issues

- Mechanical systems
- Sensor/actuators
- Control hardware

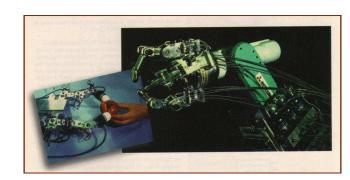
### **Example Hand Prototypes**



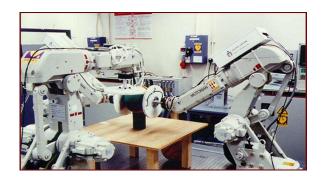
Salisbury



**Utah-MIT** 



Toshiba



**HKUST** 



DLR



Micro/Nano

#### **Grasp Planning**

A **contact** between a finger and an object can be described as a mapping between forces exerted by the finger at the point of contact and the resultant wrenches at some reference point on the object.

Imagine the 3 point contacts (in Figure A) to be the fingertips of a hand grasping an object, this arrangement will be referred to as a grasp.

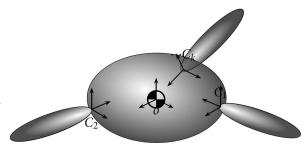


Figure A

#### **Grasp Planning**

Desirable Properties of a Grasp

- Ability to resist external forces
- Ability to dexterously manipulate the object

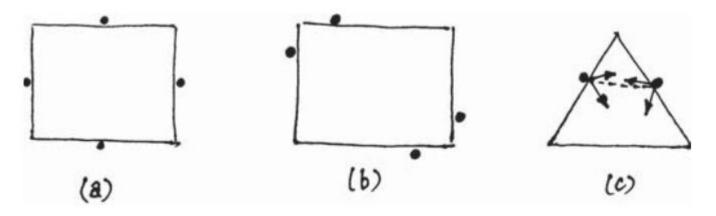
#### Assumptions for this lecture:

- Object is a rigid body
- Accurate models of the finger and object are given

#### Problems with Grasping

- Perceiving and identifying objects
- Designing end effectors
- Grasp planning (will the grasp work?)
  - Shape
  - Density
  - Material
- Grasp execution (how do we know it worked?)
  - Applying forces
  - Manipulating objects
  - Regrasping

#### 2D Contact Models

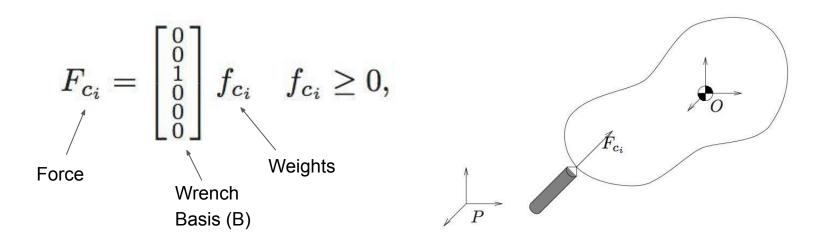


a&b) A planar rigid body constrained by four frictionless point contact

c) A rigid body constrained by two point contacts with friction. Gravity acts downward

#### **Finger Contacts**

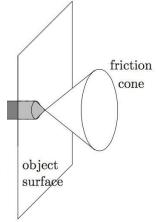
How do we measure the effect of a multifingered grasp?

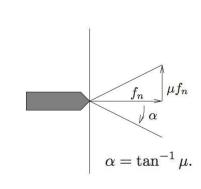


$$F_{c_i} = B_{c_i} f_{c_i}$$
  $f_{c_i} \in FC_{c_i}$ .

#### **Grasps with Friction**

$$FC_{c_i} = \{ f \in \mathbb{R}^3 : \sqrt{f_1^2 + f_2^2} \le \mu f_3, f_3 \ge 0 \}.$$





side view

#### **Torsional Friction**

$$FC_{c_i} = \{ f \in \mathbb{R}^4 : \sqrt{f_1^2 + f_2^2} \le \mu f_3, f_3 \ge 0, |f_4| \le \gamma f_3 \},$$

### Multiple Fingers: Grasp Maps

Having multiple fingers means we should use the world frame, rather than individual contact frames. So we use the Adjoint:

$$F_o = \operatorname{Ad}_{g_{oc_i}^{-1}}^T F_{c_i} = \begin{bmatrix} R_{oc_i} & 0 \\ \widehat{p}_{oc_i} R_{oc_i} & R_{oc_i} \end{bmatrix} B_{c_i} f_{c_i}, \qquad f_{c_i} \in FC_{c_i}.$$

First, we define a contact map G:

$$G_i := \operatorname{Ad}_{g_{oc_i}^{-1}}^T B_{c_i}.$$

This maps the contact basis to a wrench in the world frame.

#### Combining multiple fingers

The net force on the object is:

$$F_o = G_1 f_{c_1} + \cdots + G_k f_{c_k} = \begin{bmatrix} G_1 & \cdots & G_k \end{bmatrix} \begin{bmatrix} f_{c_1} \\ \vdots \\ f_{c_k} \end{bmatrix}$$

We can redefine the array  $\begin{bmatrix} G_1 & \cdots & G_k \end{bmatrix}$  as a new mapping:

$$G = \begin{bmatrix} \operatorname{Ad}_{g_{oc_1}^{-1}}^T B_{c_1} & \cdots & \operatorname{Ad}_{g_{oc_k}^{-1}}^T B_{c_k} \end{bmatrix} \qquad F_o = Gf_c \qquad f_c \in FC$$

This is the grasp map, which maps an entire hand to a wrench in the world frame.

#### **Force Closure**

If a grasp can resist any applied wrench, we say that such a grasp is Force-closure. Formally,

#### Definition 5.2. Force-closure grasp

A grasp is a force-closure grasp if given any external wrench  $F_e \in \mathbb{R}^p$  applied to the object, there exist contact forces  $f_c \in FC$  such that

$$Gf_c = -F_e$$
.

A grasp is force-closure if and only if G is surjective and there exists a vector of contact forces  $f_N \in \mathcal{N}(G)$  such that  $f_N \in \text{int}(FC)$ .

*Proof.* (Sufficiency) Choose  $F_o \in \mathbb{R}^p$  and let  $f'_c$  be any vector such that  $F_o = Gf'_c$ . Since G is surjective, such an  $f'_c$  must exist. We will show that there exists an  $\alpha$  such that  $f'_c + \alpha f_N \in \text{int}(FC)$ . Notice that

that there exists an 
$$\alpha$$
 such that  $f'_c + \alpha f_N \in \operatorname{int}(FC)$ . Notice that 
$$\lim_{\alpha \to \infty} \frac{f'_c + \alpha f_N}{\alpha} = f_N \in \operatorname{int}(FC);$$

therefore, there exists  $\alpha'$  sufficiently large such that

Proposition 5.2. Necessity of internal forces

$$\frac{f_c' + \alpha' f_N}{\alpha'} \in \operatorname{int}(FC) \subset FC.$$

$$\frac{\sigma C}{\alpha'} \in \operatorname{int}(F'C) \subset F'C.$$
 From the properties of the friction cone it follows that

From the properties of the friction cone, it follows that

 $f_c := f'_c + \alpha' f_N \in \text{int}(FC)$ 

and  $Gf_c = Gf'_a = F_a$ .

#### **Force Closure**

Proposition 5.3. Convexity conditions for force-closure grasps Consider a fixed contact grasp which contains only frictionless point contacts. Let  $G \in \mathbb{R}^{p \times m}$  be the associated grasp matrix and let  $\{G_i\}$  denote the columns of G. The following statements are equivalent:

- 1. The grasp is force-closure.
- 2. The columns of G positively span  $\mathbb{R}^p$ .
- 3. The convex hull of  $\{G_i\}$  contains a neighborhood of the origin.
- 4. There does not exist a vector  $v \in \mathbb{R}^p$ ,  $v \neq 0$ , such that for  $i = 1, \ldots, m, v \cdot G_i \geq 0$ .

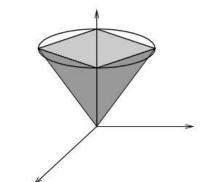
#### Limitations of Force Closure

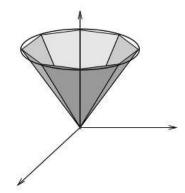
- Assumes you can move fingers in any direction
- Assumes you can exert as much as infinite force
- Sometimes it's better to execute suboptimal grasps

# Approximating the Friction Cone

Why would you do this?

$$f_i = \begin{bmatrix} \mu \cos \frac{2\pi i}{n} \\ \mu \sin \frac{2\pi i}{n} \\ 1 \end{bmatrix}$$



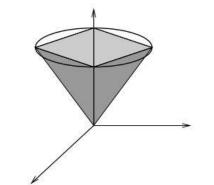


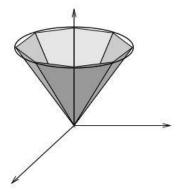
# Approximating the Friction Cone

Why would you do this?

You can simplify the constraints to a **Positive** linear combination of facet vectors

$$f_i = \begin{bmatrix} \mu \cos \frac{2\pi i}{n} \\ \mu \sin \frac{2\pi i}{n} \\ 1 \end{bmatrix}$$





#### Sources

MLS Ch 3

Chapter 5 Lecture Notes for A Mathematical Introduction to Robotic Manipulation by Z.X. Li and Y.Q. Wu