Brain-Inspired Artificial Intelligence 1: Introduction to Reinforcement Learning

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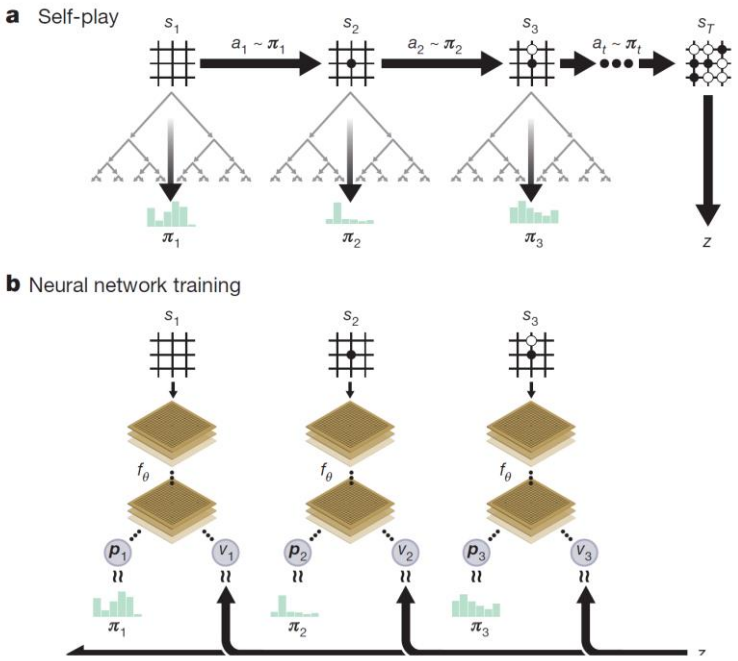
Reinforcement learning in games

AlphaGo Zero (Silver et al., 2017)
board game, Go
RL from scratch
4.9 millions of self-play

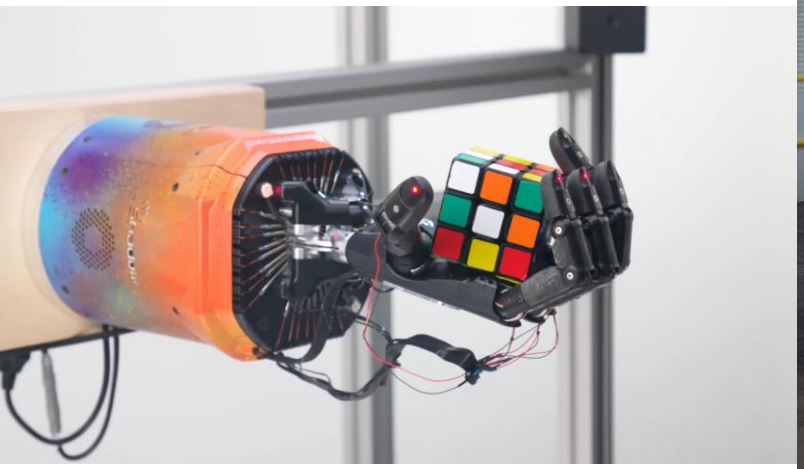


AlphaStar (Vinyals et al., 2019)
multiagent real-time strategy game
RL + supervised learning
200 years

Gran Turismo Sophy (Wurman et al., 2022)
racing game
RL with shaped rewards
1,000 PlayStation 4

Reinforcement learning in robotics

OpenAI (Akkaya et al., 2019)
manipulating Rubik's cube
RL + domain randomization
2.8 GWh of electricity

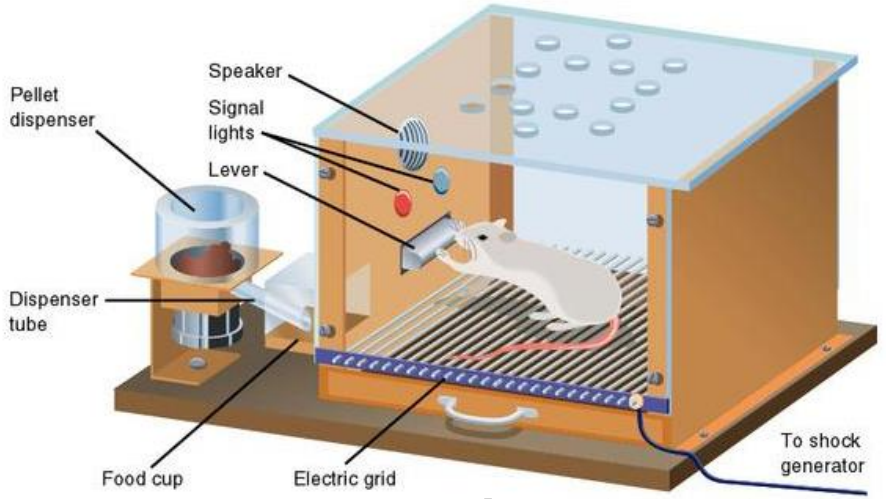


MT-Opt (Kalashnikov et al., 2021)
grasping
RL (+ supervised learning)
7 robots, 9600 robot hours

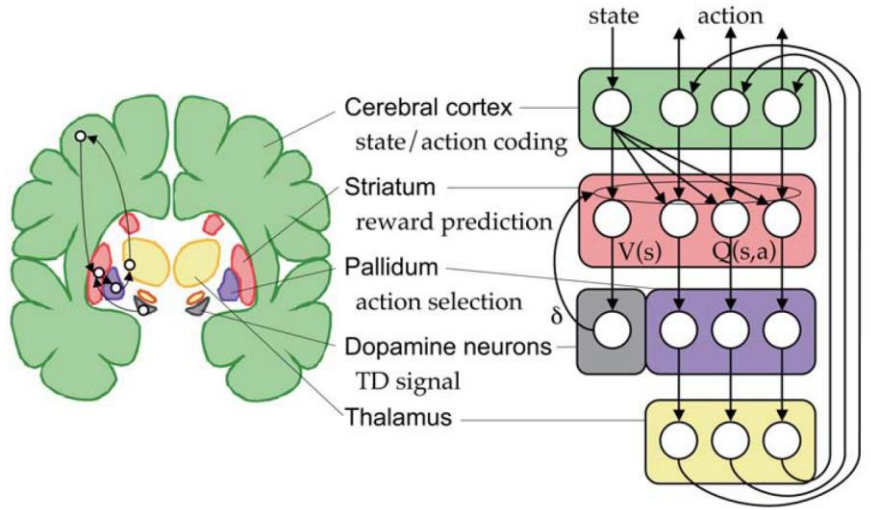
DDPP (Tsurumine et al., 2019)
folding a T-shirt
SL + RL with shaped rewards
192 demonstrations

What is Reinforcement Learning (RL)?

- RL is a computational framework to find an optimal policy (controller) by trial and error
- Inspired from psychology
  - Thorndike's law of effect
  - Skinner's principle of reinforcement
- Computational model of decision making of human/animal

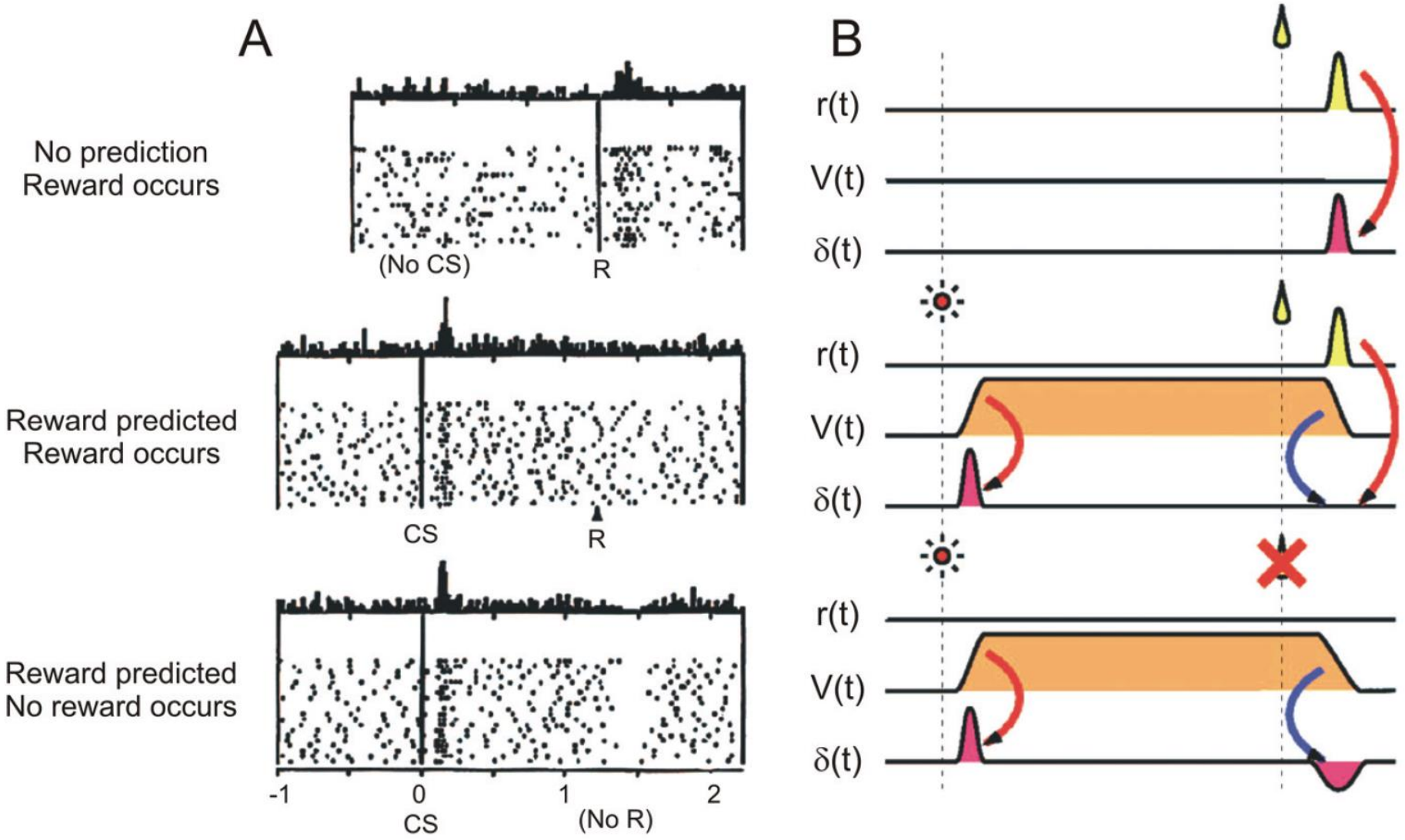


[Simply Psychology]



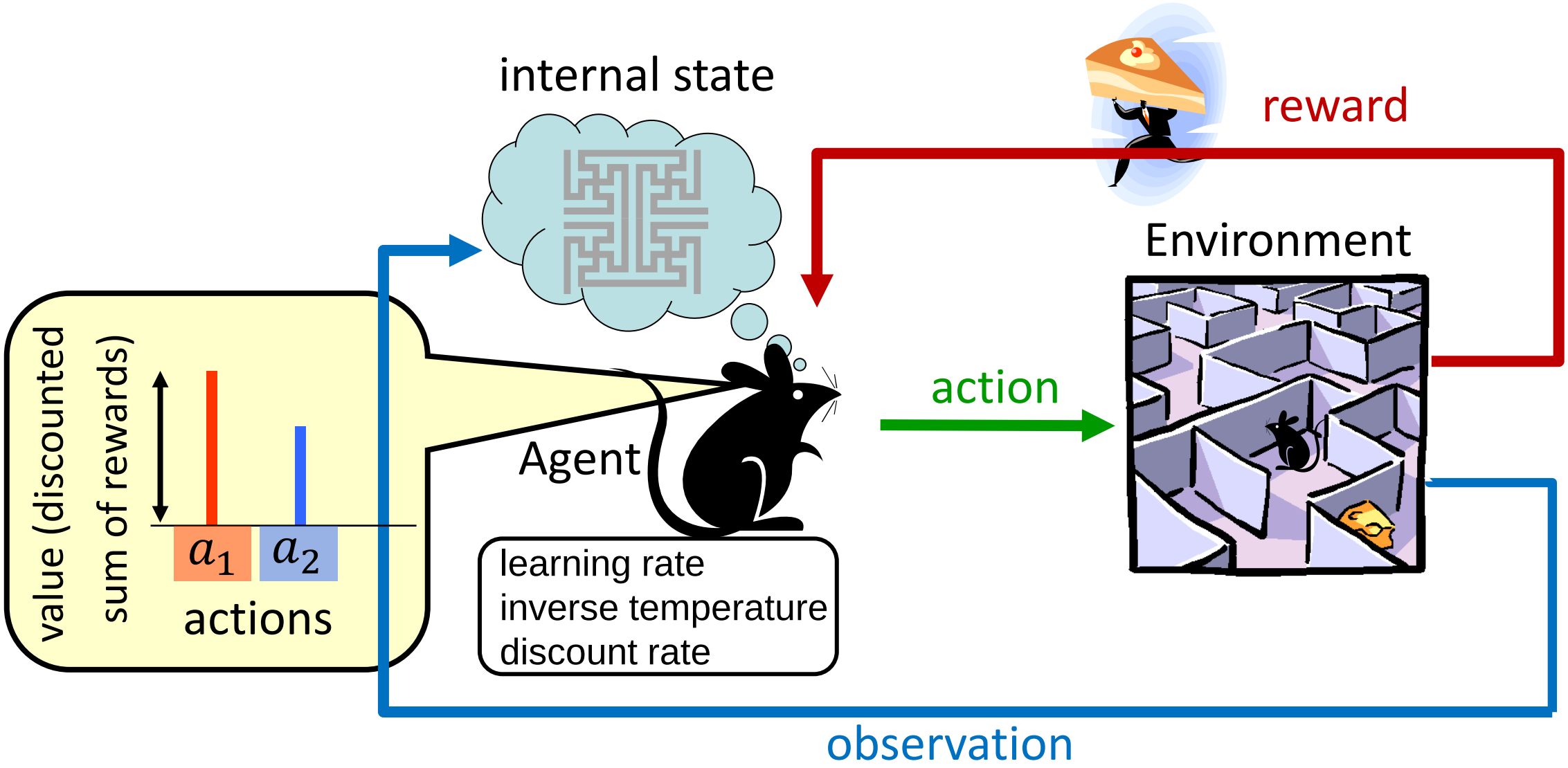
K. Doya (2007). Reinforcement learning: Computational theory and biological mechanisms. HFSP Journal, vol. 1, no. 1, pp. 30–40.

Dopamine neurons code Temporal Difference error



W.P. Schultz, P. Dayan, P.R. Montague (1997). A Neural Substrate of Prediction and Reward. Science 275, no. 5306: 1593–99.

Interaction between Agent and Environment

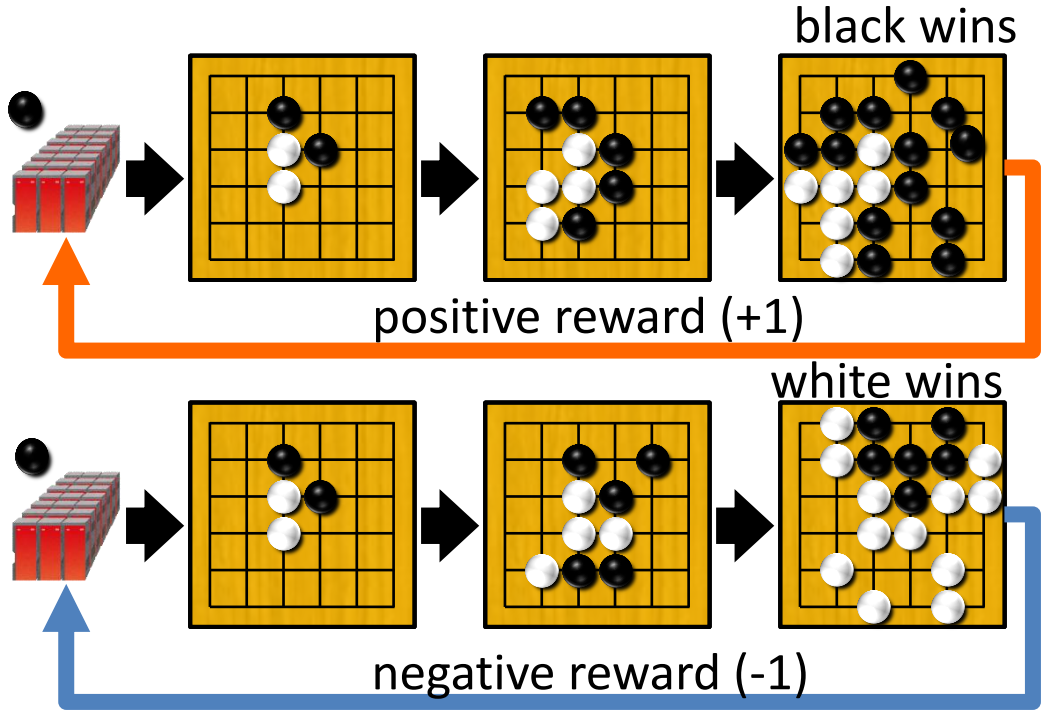


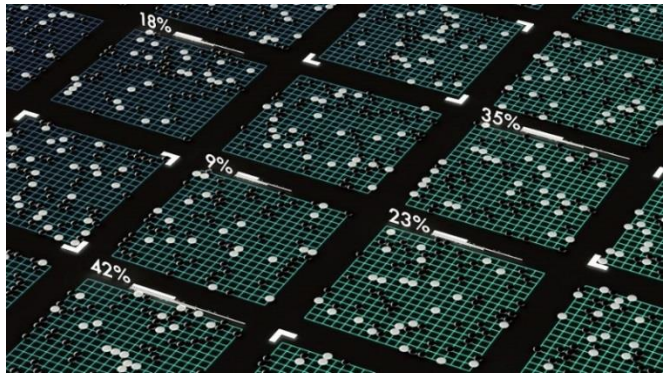
What is Reward?

- In the case of Go
  - positive reward for winning
  - negative reward for losing
  - zero otherwise

⇒ very sparse reward

- AlphaGo Zero, which does not use a record of a game of go, needs **4.9 million** games of self-play

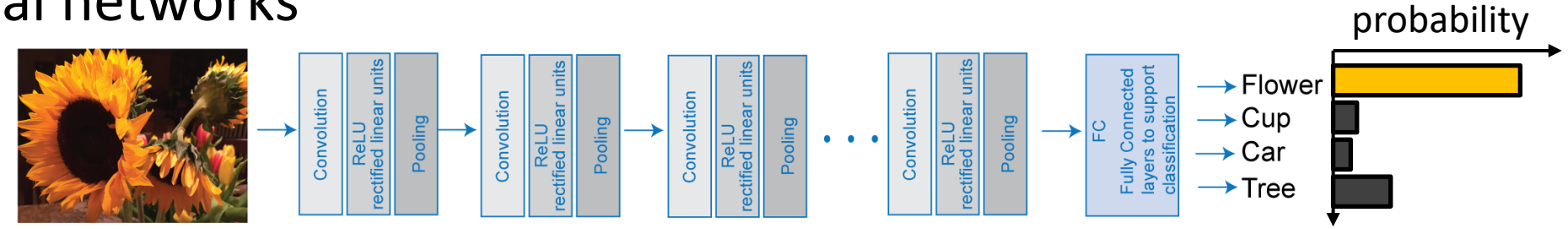




Difference between Deep Learning and (Deep) Reinforcement Learning

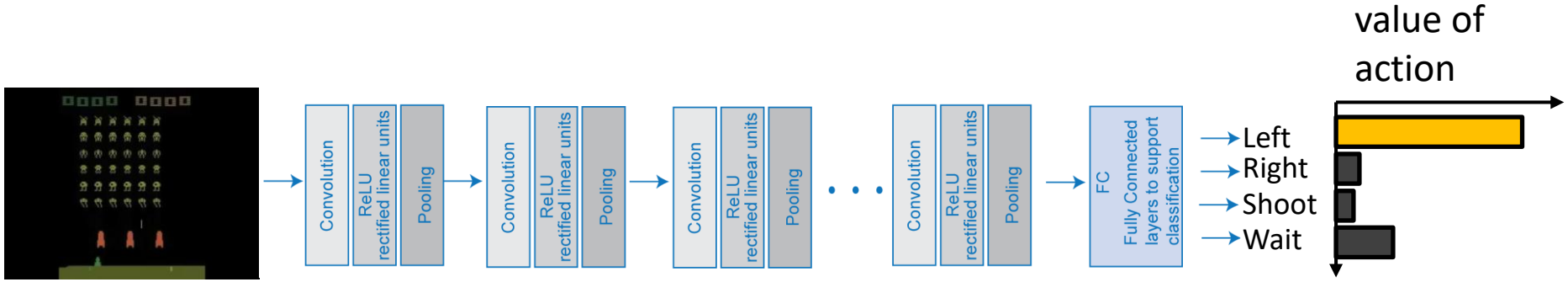
- Deep Learning for Classification

  Take input data and predict a category for that data by using multilayer neural networks



- Deep Reinforcement Learning

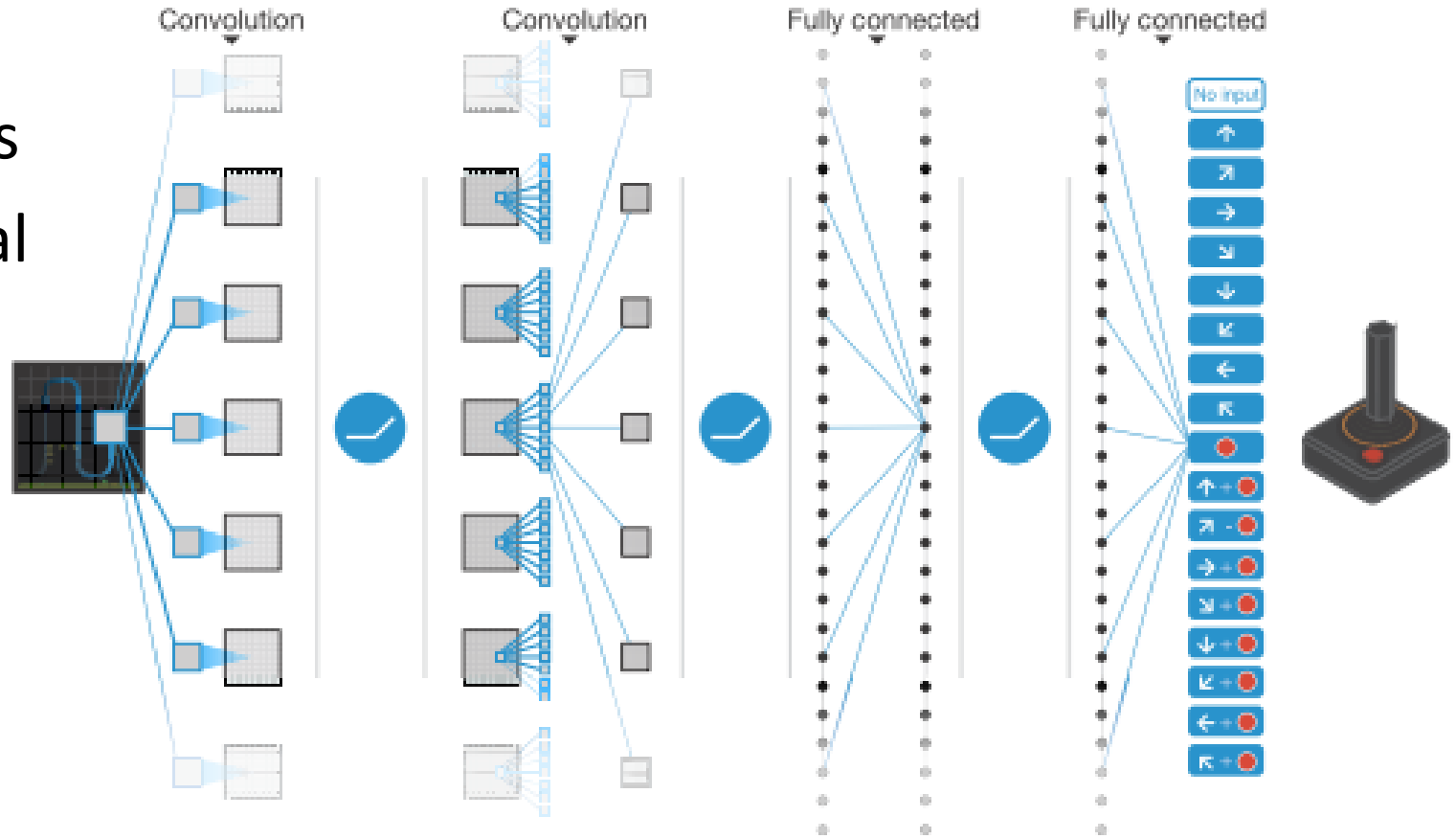
  Find a policy that maximizes the sum of rewards by trial and error



RECENT STUDIES ON REINFORCEMENT LEARNING

Deep Q Networks (DQN), playing ATARI 2600 games

- Learned a mapping from a sequence of game screens to the value of action
- Performed at a level that is comparable to professional human game testers



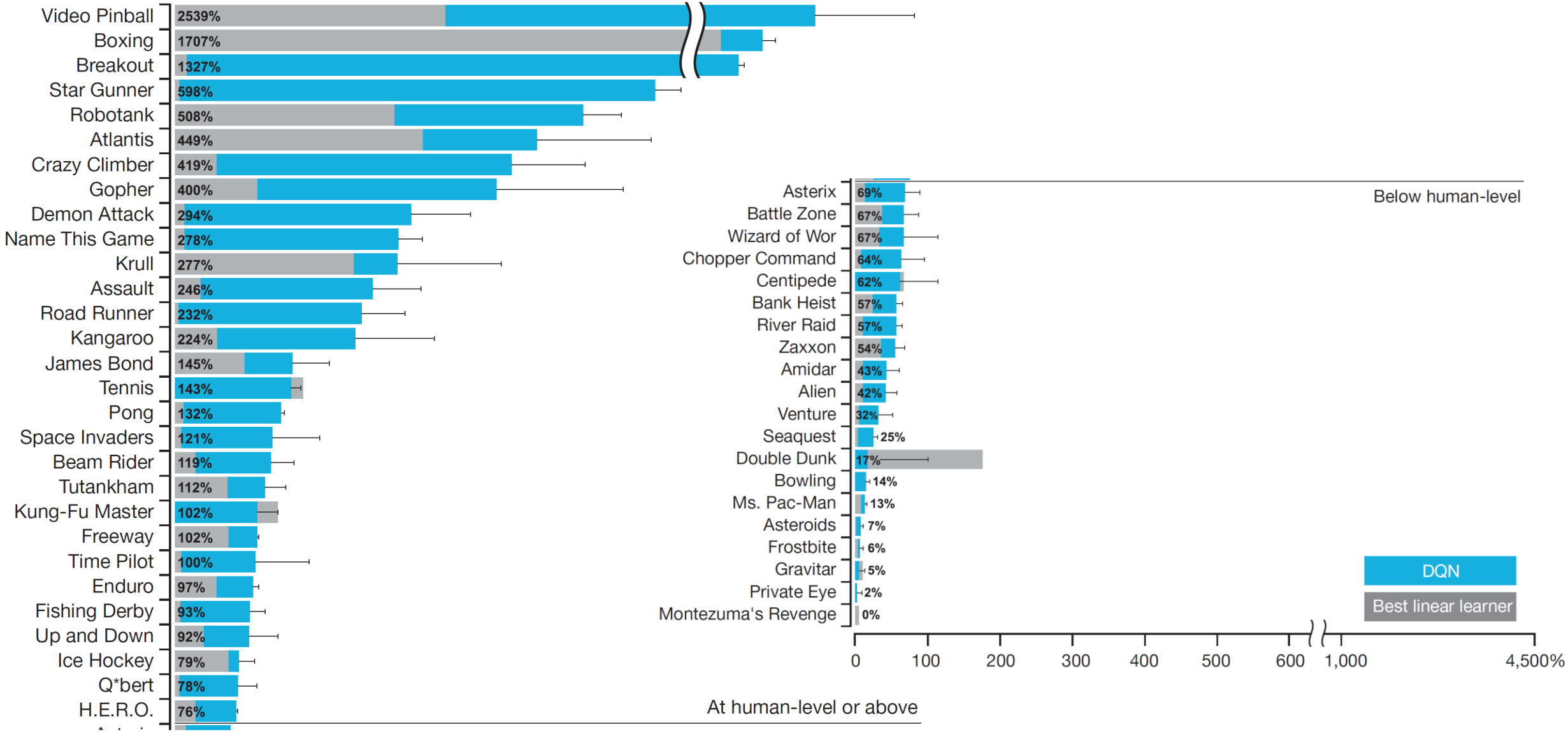
V. Mnih et al. (2015). Human-level control through deep reinforcement learning. Nature, vol. 518, no. 7540, pp. 529–533.

What is the Atari 2600 games?

- Home video console released in 1977
- 210 x 160 color video at 60 Hz
- Pac-Man (‘82) sold 7.7 million copies

from Wikipedia

Performance of DQN



V. Mnih et al. (2015). Human-level control through deep reinforcement learning. Nature, vol. 518, no. 7540, pp. 529–533.

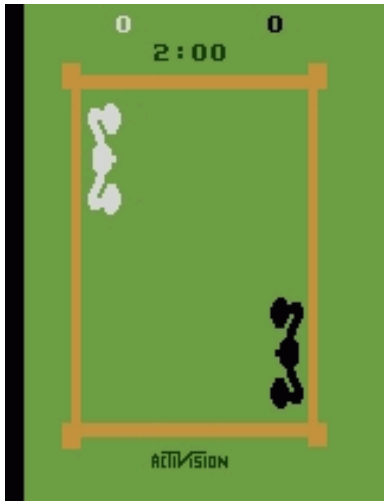
Examples of the Atari 2600 games

Better than human

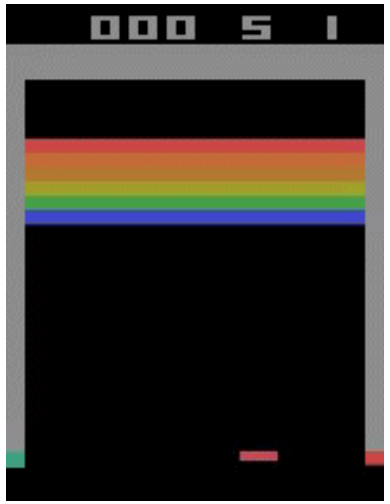
- Reactive games

Worse than human

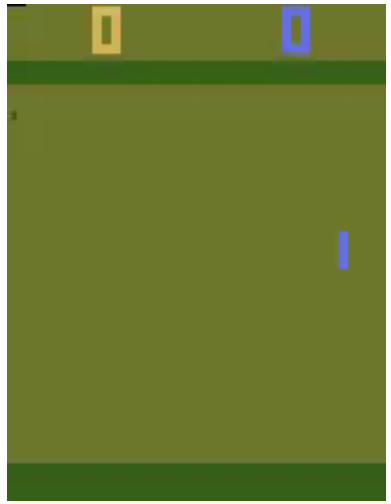
- Games demanding more temporally extended planning strategies



Boxing
1,707 %

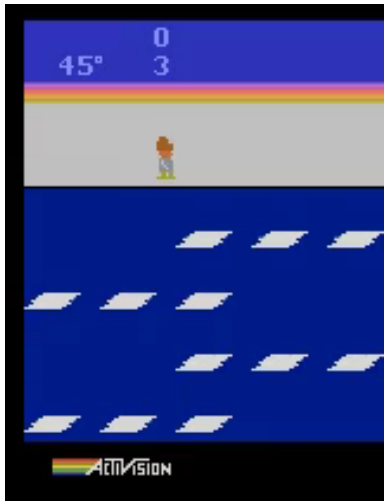


Breakout
1,327 %

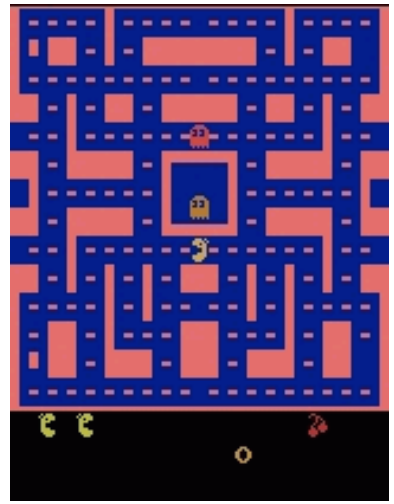


Pong
132 %

Seaquest
25 %



Frostbite
6 %



Ms. Pac-Man
13 %

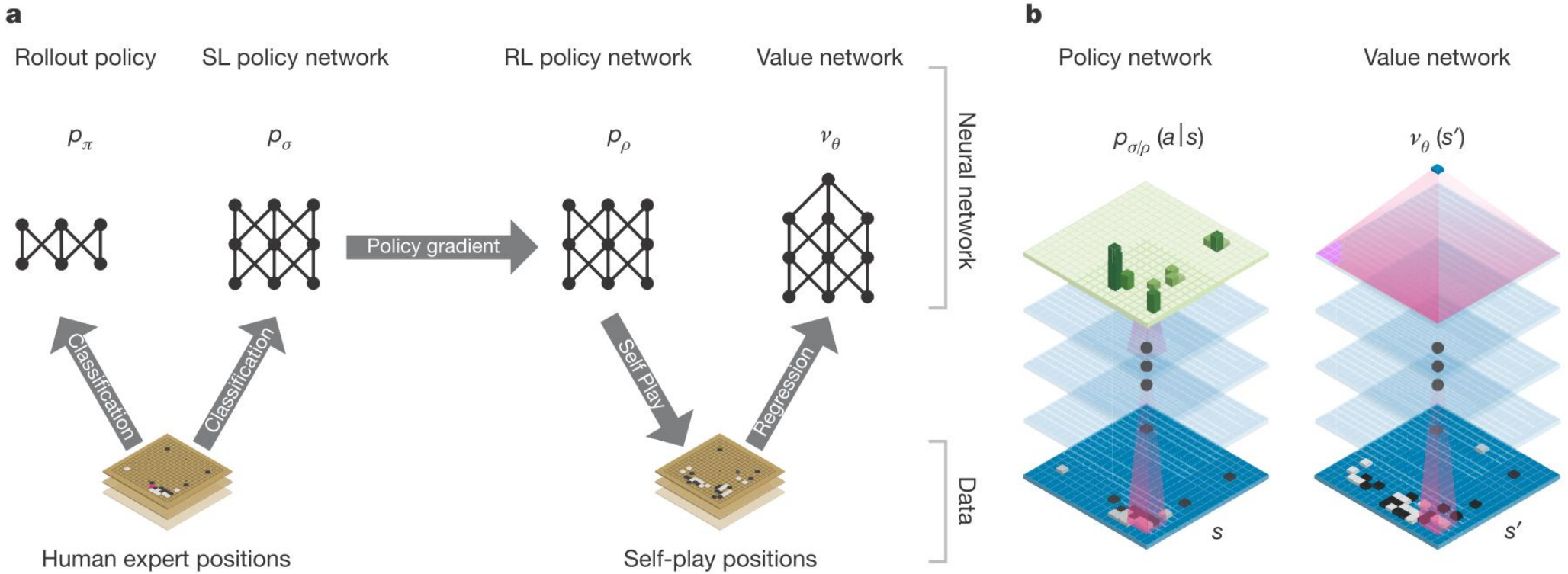
V. Mnih et al. (2015). Human-level control through deep reinforcement learning. Nature, vol. 518, no. 7540, pp. 529–533.

AlphaGo

- Outperform the human-champion

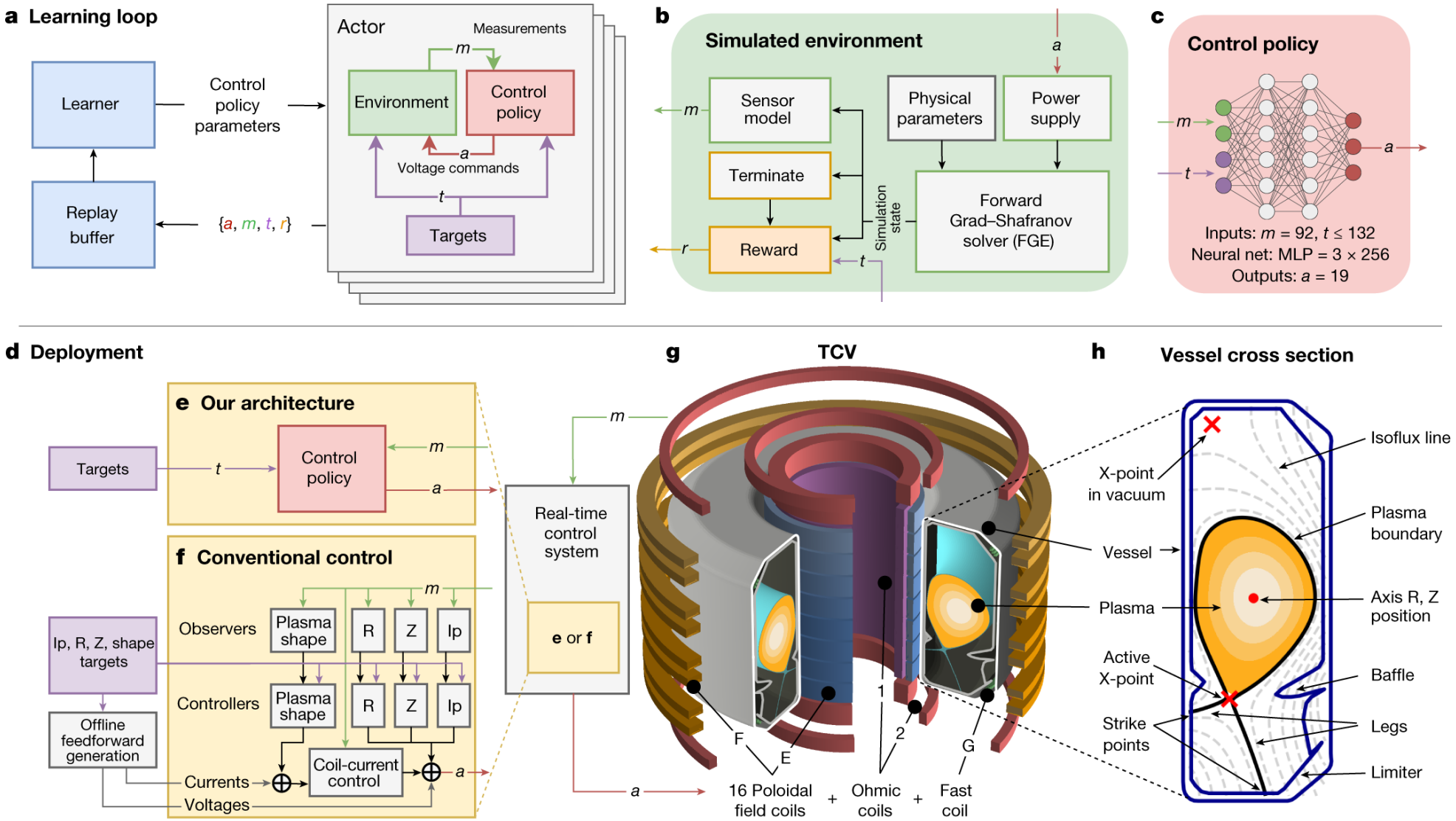
Go ratings

Rank	Name	♂♀	Flag	Elo
1	Ke Jie	♂		3615
2	Google AlphaGo			3585
3	Park Jungwhan	♂		3569
4	Iyama Yuta	♂		3532
5	Lee Sedol	♂		3519



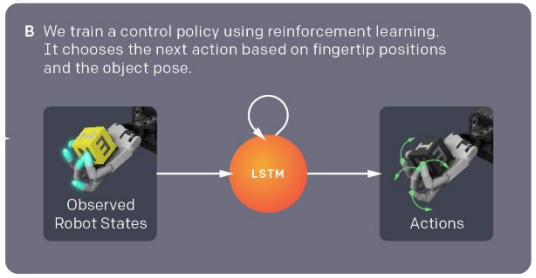
D. Silver et al. (2016). Mastering the game of Go with deep neural networks and tree search. Nature, vol. 529, no. 7587, pp. 484–489.

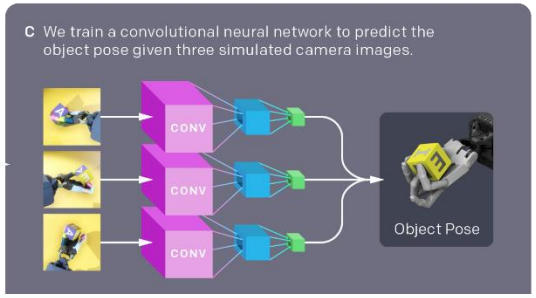
Magnetic control of tokamak plasmas

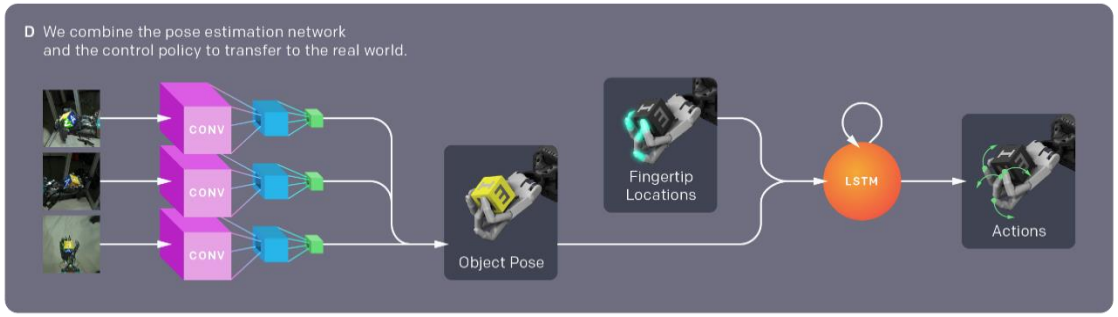


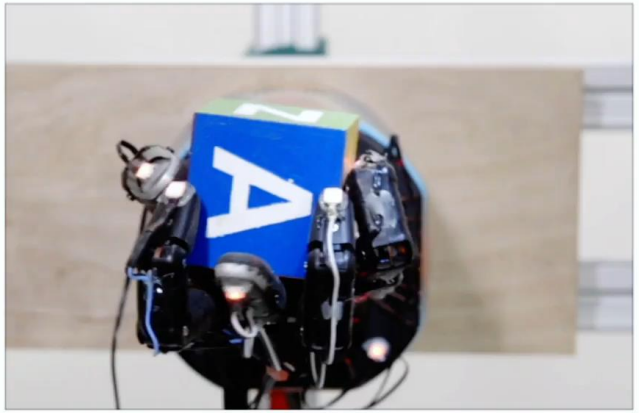
J. Degrave et al. (2022). Magnetic control of tokamak plasmas through deep reinforcement learning. Nature, vol. 602, no. 7897, pp. 414-419.

In-hand manipulation

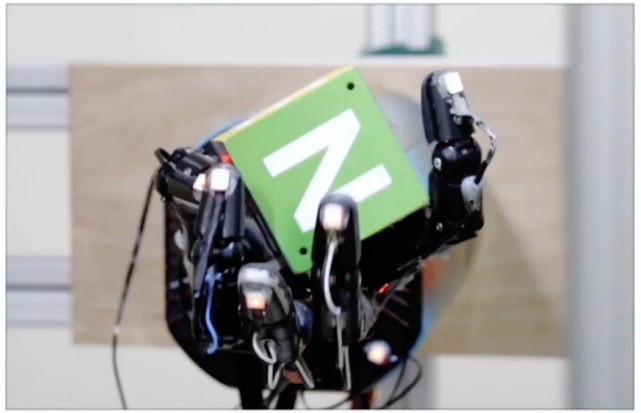




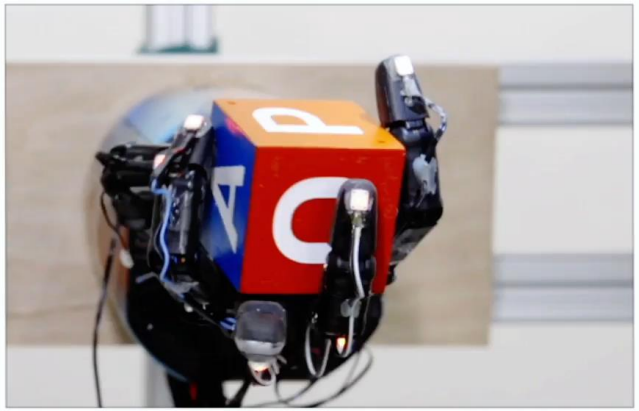




FINGER PIVOTING



SLIDING



FINGER GAITING

OpenAI: M. Andrychowicz, et al. (2020). Learning dexterous in-hand manipulation. The International Journal of Robotics Research. Vol. 39, no. 1, pages 3-20.

Tax Collections Optimizers

- Optimally managing the tax collection processes at financial institutions

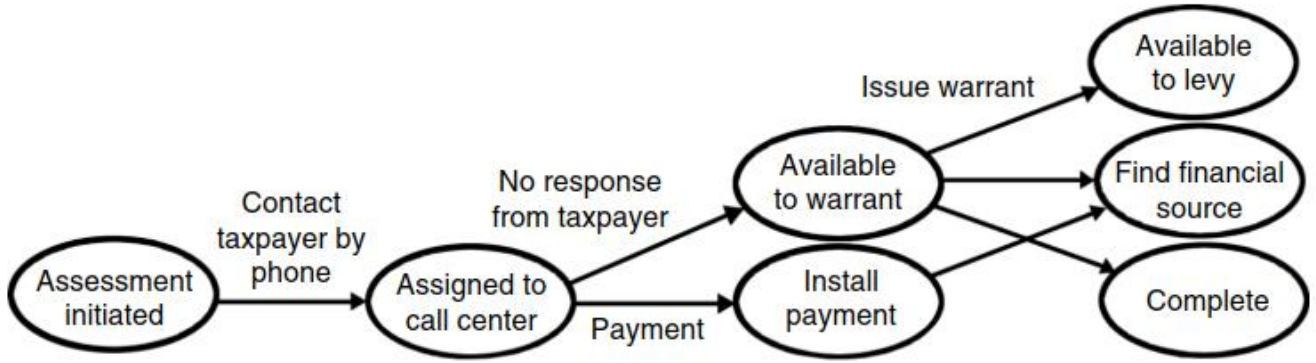
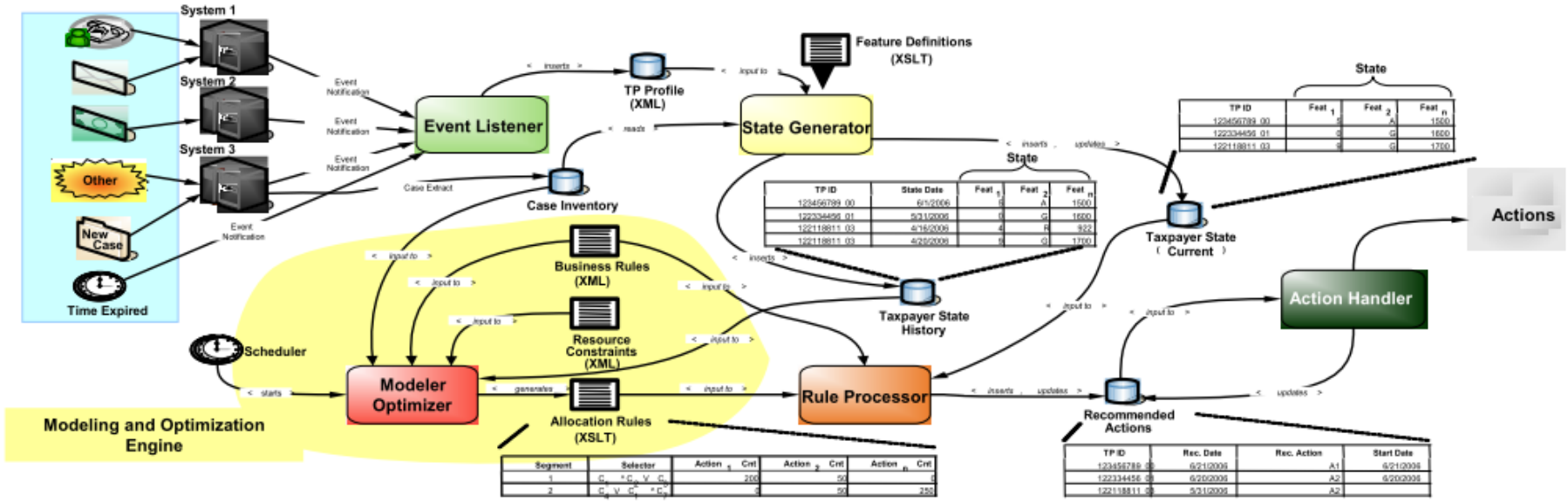


Figure 1: The graphic illustrates an MDP formulation of the collections process.

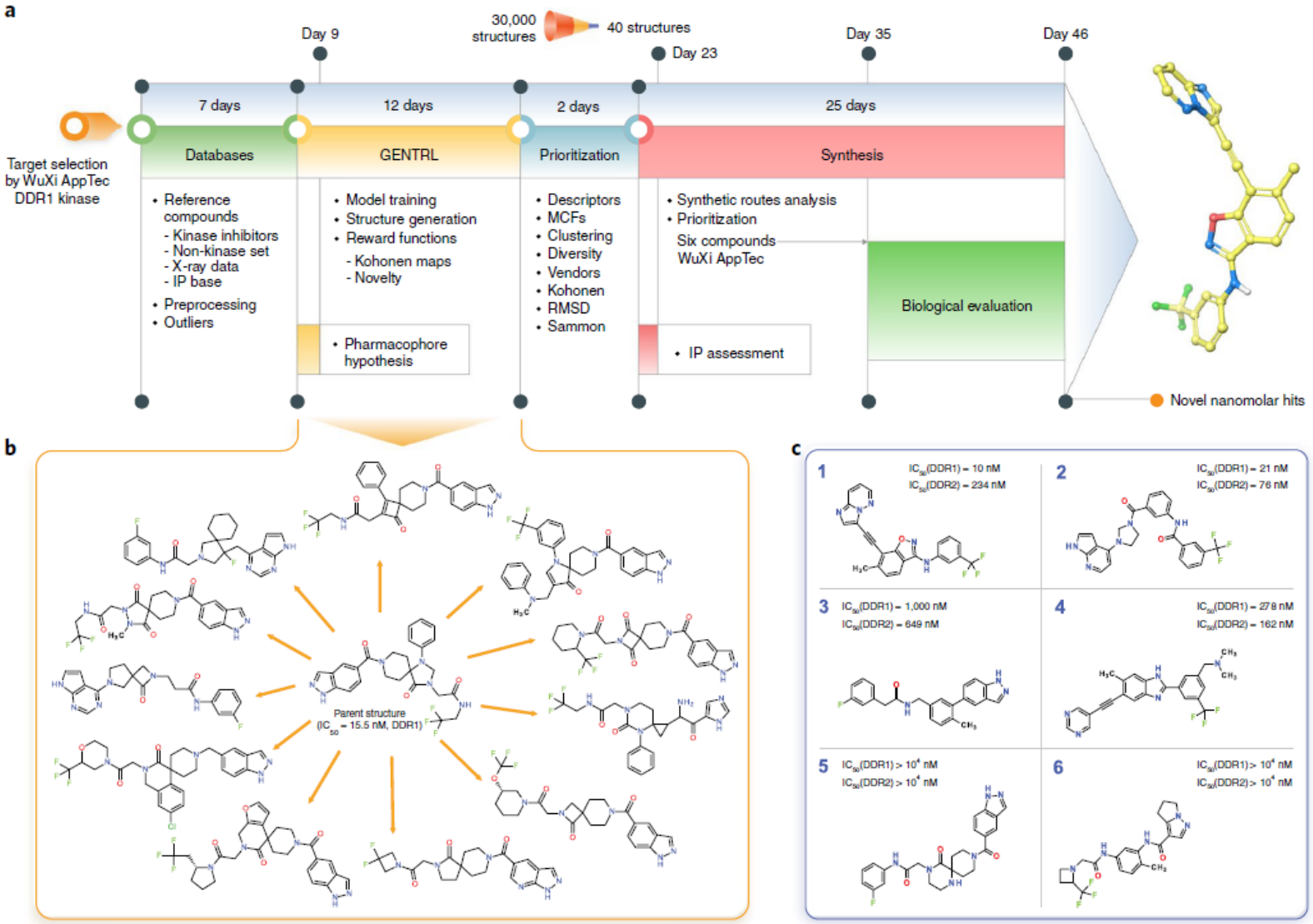
- Use actually in New York State Department of Finance



N. Abe, et al. (2010). Optimizing debt collections using constrained reinforcement learning. In Proc. of the 16th ACM SIGKDD, pp. 75-84.

G. Miller, et al. (2012). Tax collection optimization for New York State. Interfaces, 42(1), 74-84, 2012.

Rapid identification of potent DDR1 kinase inhibitors

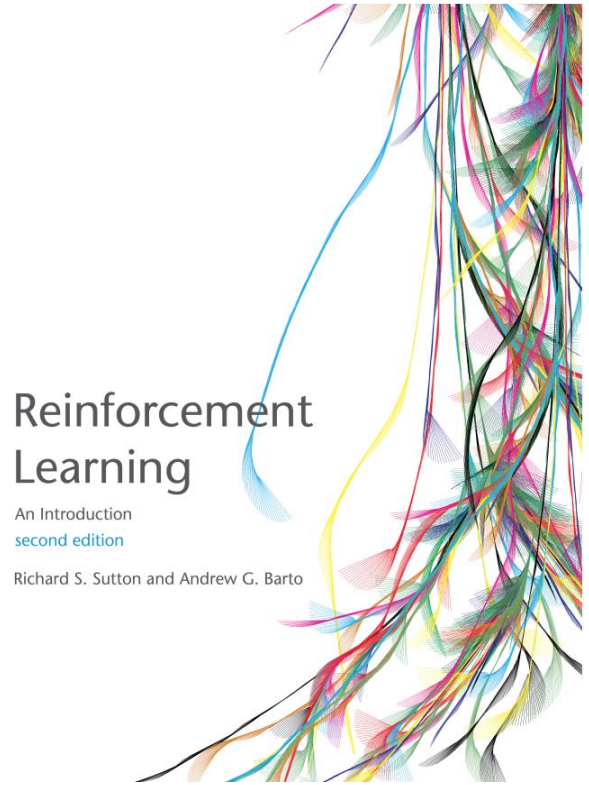


A. Zhavoronkov, et al. (2019). Deep learning enables rapid identification of potent DDR1 kinase inhibitors. Nature Biotechnology. Vol 37, no. 9, pages 1038-1040.

RECOMMENDED TEXTBOOKS

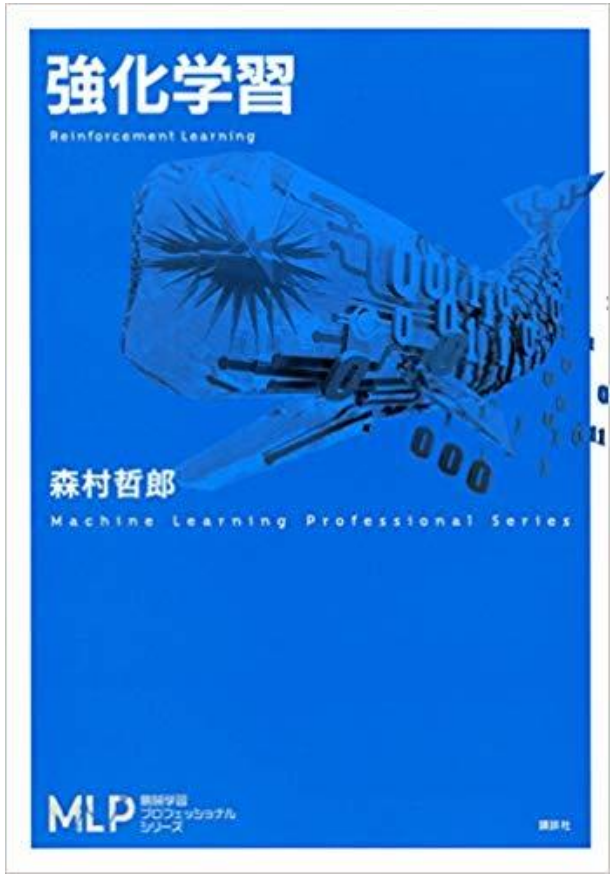
R.S. Sutton and A.G. Barto. (2018). Reinforcement learning: An introduction. MIT Press.

- First edition (1998), and Japanese translation (2000), and Second edition (2018).
- Must-read for researchers



森村哲郎 (2019). 機械学習プロフェッショナルシリーズ 強化学習

- Official page
- Theoretical introduction to reinforcement learning with discrete states and actions
- One chapter describes recent topics such as distributional RL and deep RL

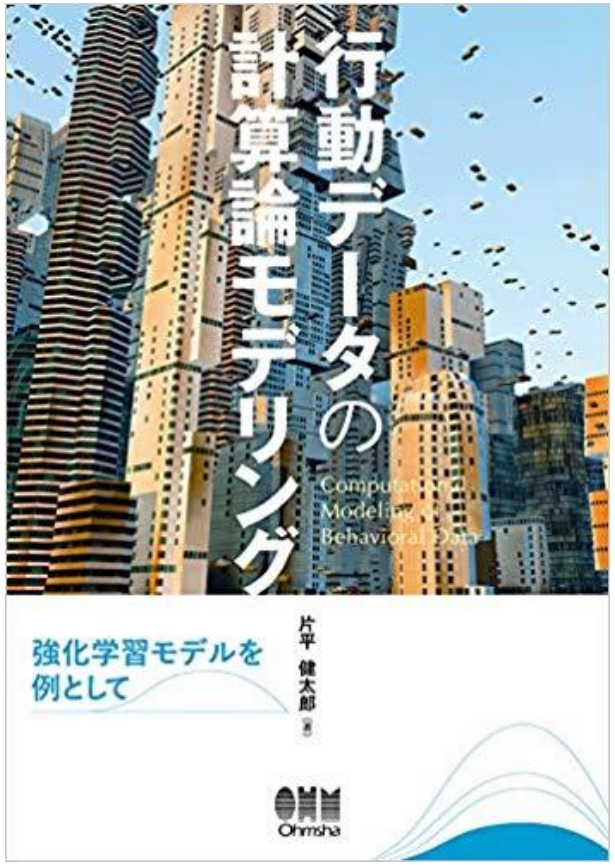


牧野貴樹、澁谷長史(編) (2016) これからの強化学習. 森北出版

- Official page
- Overview of modern reinforcement learning such as policy search methods, deep RL, and inverse RL

片平 健太郎 (2018).行動データの計算論モデリング: 強化学習モデルを例としてオーム社

- Official page
- R and Stan scripts are available
- Computational modeling of behavioral data based on reinforcement learning



Other books

- 伊藤真 (2021). 「強化学習」を学びたい人が最初に読む本. 日経BP.
- 久保隆宏 (2019). Pythonで学ぶ強化学習 [改訂第2版] 入門から実践まで. 講談社.
- 斎藤康毅 (2022).ゼロから作るDeep Learning 4 —強化学習編. オライリージャパン.
- Szepesvári, C. (2010). Algorithms for reinforcement learning. Morgan & Claypool.
  - 翻訳: 小山田 創哲 訳者代表 (2017). 速習 強化学習アルゴリズム. 共立出版.

Report

- Please select one topic and write your report

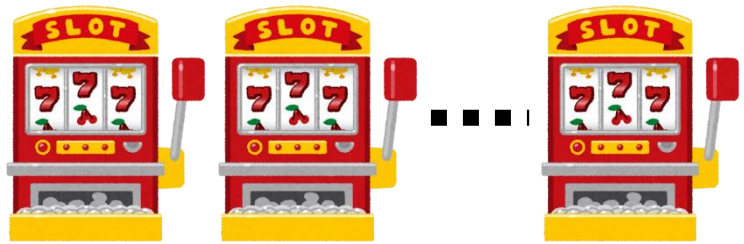
1. Consider the application of reinforcement learning

2. How can we reduce the training data and time?

REINFORCEMENT LEARNING FOR BANDIT PROBLEMS

Multi-Armed Bandit Problem

- There exist k gambling machines
- Each machine has a different unknown probability distribution for rewards
  - Action: select a gambling machine

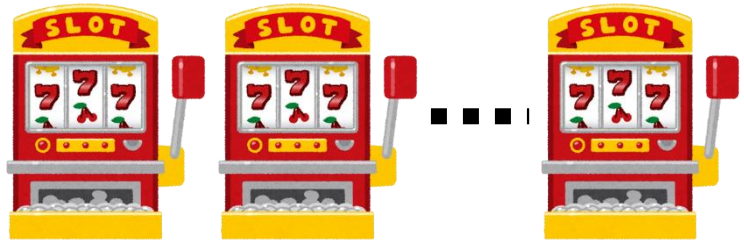


0 1 $k-1$

- The goal is to maximize the rewards obtained by successively playing gamble machines (the ‘arms’ of the bandits)

Components: Action and Policy

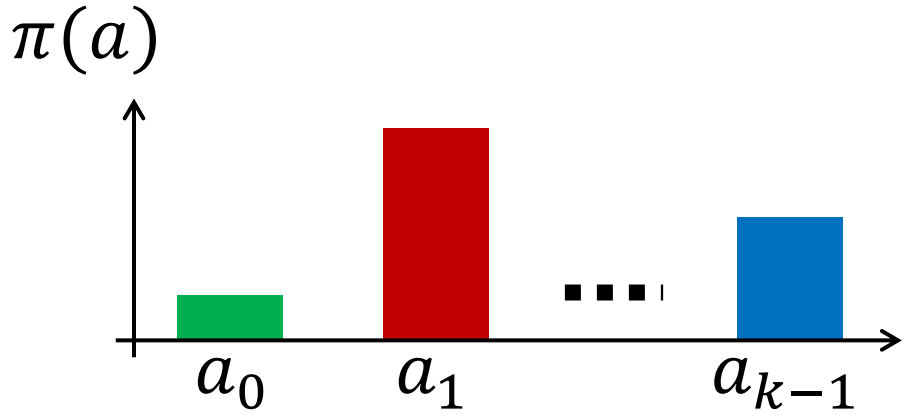
- (Discrete) Action
  - Choosing one gambling machine in the bandit problems
  - If there exist k machines, it is convenient to define a set of actions by $\mathcal{A} = \{a_0, a_1, \ldots, a_{k-1}\}$



0 1 $k-1$

- Policy (learned by the agent)
  - $\pi(a)$: probability to select an action a
  - $\pi(a) \geq 0, \forall a \in \mathcal{A}$

$$\sum_{a \in \mathcal{A}} \pi(a) = 1 \Rightarrow k-1 \text{ free parameters}$$

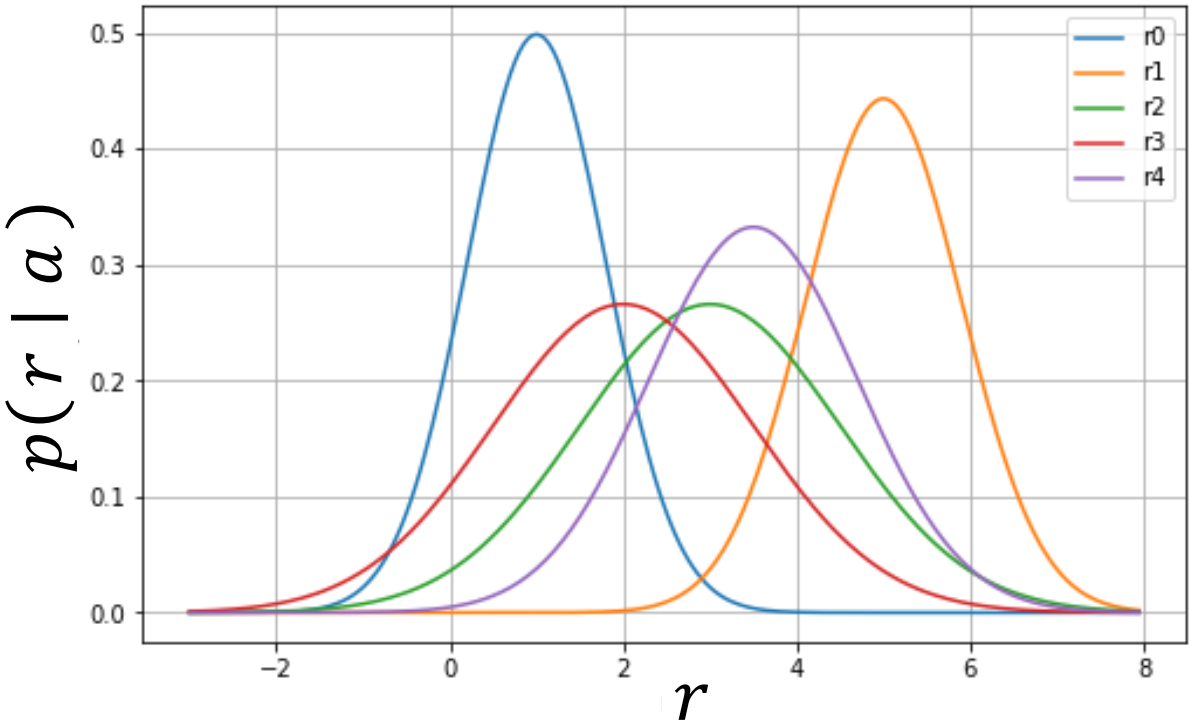


Components: Reward

- Usually unknown to a learning agent
  - When the agent executes an action a_t at time t, it receives a scalar feedback called reward

$$R_t \sim p(r \mid a_t)$$

  - For example, $p(r \mid a)$ is modeled by a Gaussian distribution with the mean $\mu(a)$ and the standard deviation $\sigma(a)$



$$p(r \mid a) = \frac{1}{\sqrt{2\pi}\sigma(a)} \exp\left(-\frac{\left(r-\mu(a)\right)^2}{2\sigma(a)^2}\right)$$

Goal of the Learning Agent

- Find a policy π that maximizes the expected reward

$$J(\pi) \triangleq \mathbb{E}_{\pi}[R] = \int rp(r \mid \pi)\mathrm{d}r$$

- $p(r \mid \pi)$ is a probability density function

$$p(r \mid \pi) \triangleq \sum_{a} p(r \mid a)\pi(a)$$

- To simplify notations, we often write the objective function as follows in this lecture

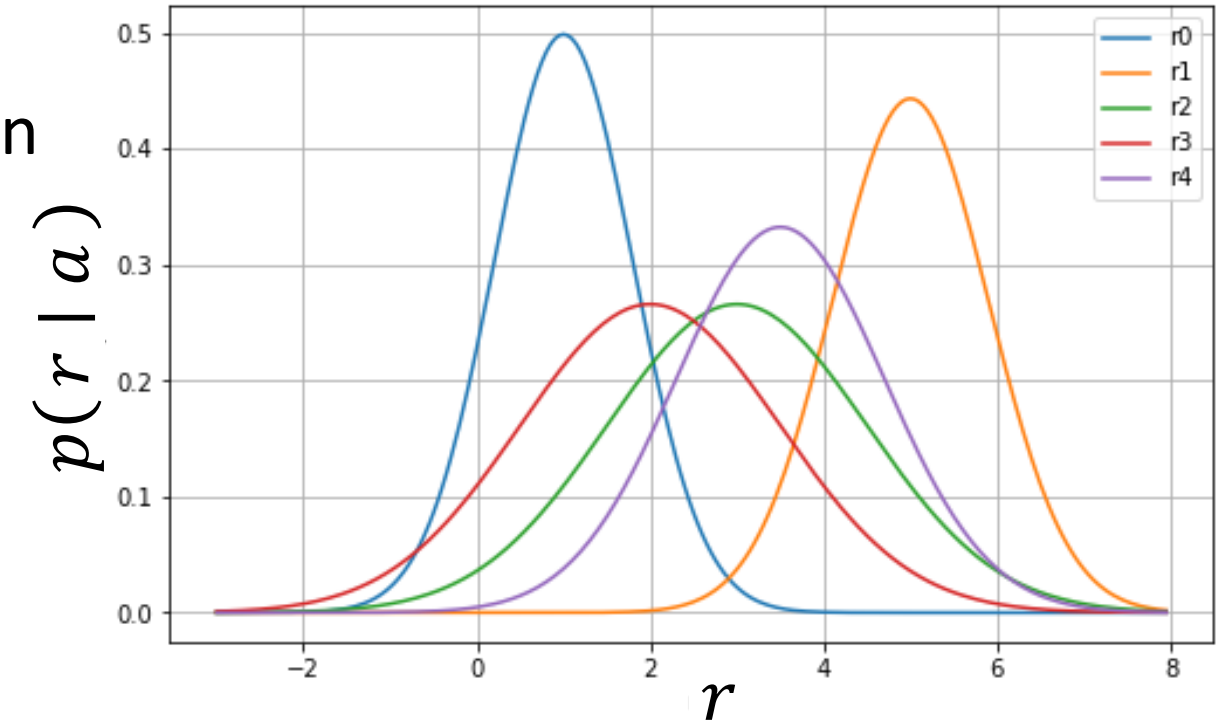
$$J(\pi) = \sum_{r,a} rp(r \mid a)\pi(a)$$

Example

- The rewards of the machine are determined by a Gaussian distribution where

  mean
  {1, 5, 3, 2, 3.5}

  standard deviation
  {0.8, 0.9, 1.5, 1.5, 1.2}

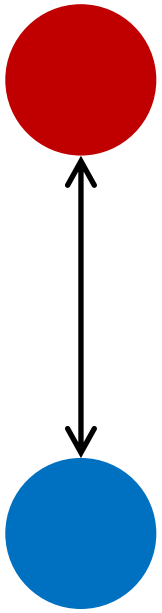


- The optimal action is to select the machine “1” because it has the highest mean value

- A learning agent does not know these distributions

REINFORCEMENT LEARNING FOR BANDIT PROBLEMS
-- VALUE-BASED APPROACH --

Two RL Approaches



Value-based approach

- Compute expected rewards for every action
- Select an action according to the expected rewards

Policy-based approach

- Compute a gradient of an expected reward under a parametric stochastic policy
- Update a policy by a stochastic gradient ascent

Value-based approach

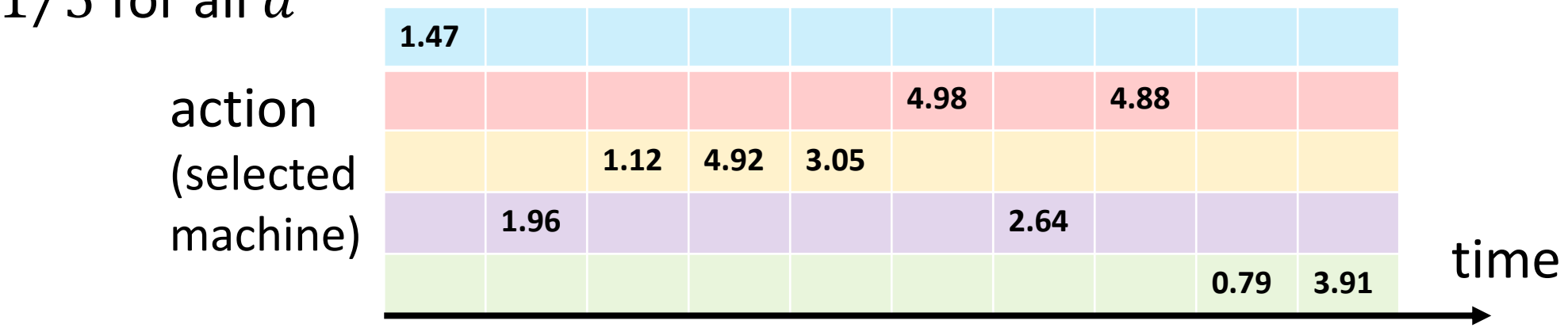
- We want to know the expected values of actions

$$Q^*(a) \triangleq \mathbb{E}_{r \sim p(\cdot|a)}[r \mid a_t = a] = \int r p(r \mid a)\, \mathrm{d}r$$

  - Can't compute $Q^*(a)$ analytically because $p(r \mid a)$ is unknown

- In order to estimate $Q^*(a)$, we need to gather samples by playing

- Suppose that an agent gets the following sequence of rewards based on $\pi(a) = 1/5$ for all a



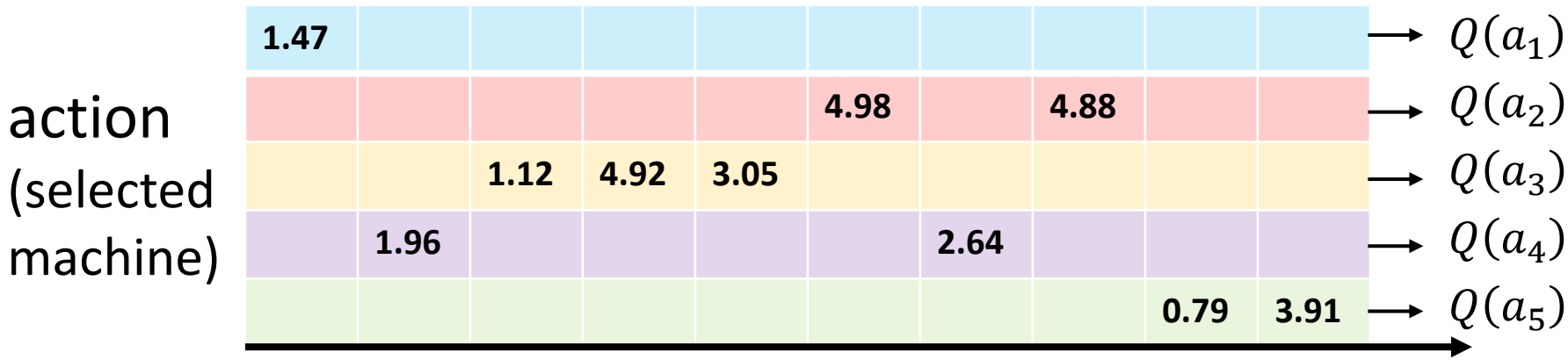
Value-based Approach

- Estimate by averaging the rewards actually received:

$$Q_t(a) = \frac{\text{sum of rewards when } a \text{ taken prior to } t}{\text{number of times } a \text{ taken prior to } t}$$

where $Q_t(a)$ is an array estimate of $Q(a)$ at time t

- Example $$Q_4(a_2) = \frac{1.12 + 4.92 + 3.05}{3} = 3.03$$

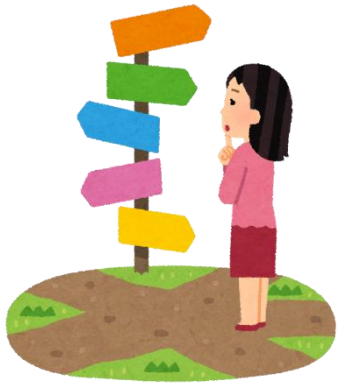


Greedy Policy

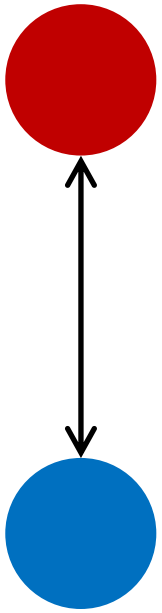
- If Q_t is sufficiently accurate, it is enough to select an action greedily
  - always choose the action with current best expected reward

$$a_t = \underset{a}{\operatorname{argmax}}\, Q_t(a)$$

- However, a learning agent does not have a correct Q at the beginning of learning
- So, the agent should gather information by trial and error to estimate Q efficiently
- How should the agent select actions during learning?



Action Selection Strategies during Learning

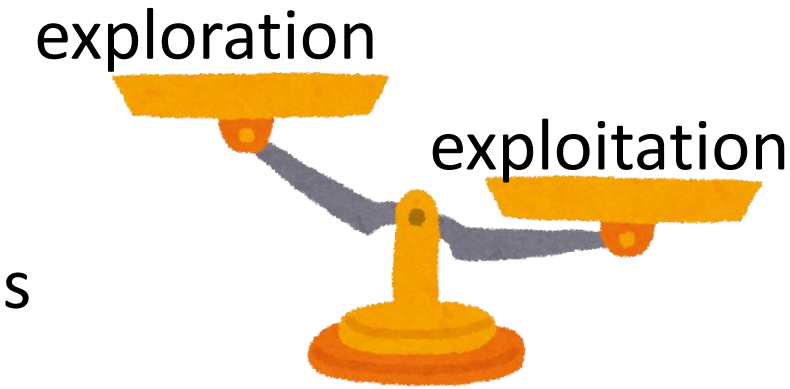


Exploitation

- Use known information to act
- E.g., go to the best restaurant I know

Exploration

- Find more information about machines
- E.g., try a new restaurant



- An RL agent faces the exploration-exploitation dilemma at every time step

ε-greedy policy

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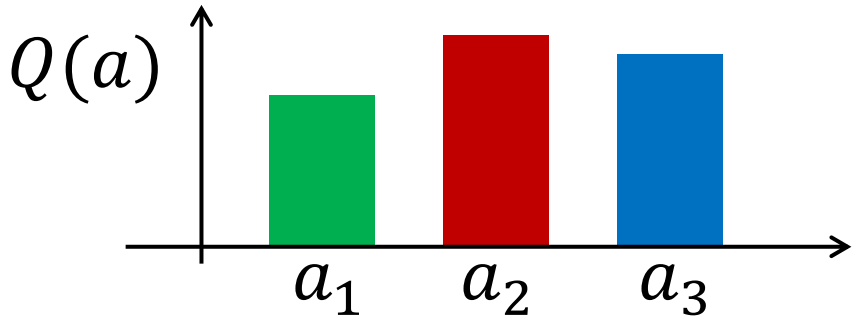
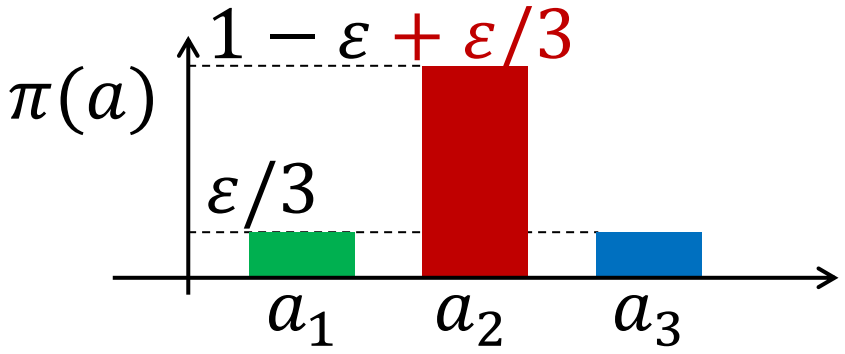
- Choose the action with current best expected reward with probability $1 - \varepsilon$
- Choose another action randomly with probability ε/k

$$\pi(a) = \begin{cases} \varepsilon/k + 1 - \varepsilon & \text{if } a = \underset{a'}{\operatorname{argmax}}\, Q(a') \\ \varepsilon/k & \text{otherwise} \end{cases}$$

- Exploration insensitive to relative performance levels





$\varepsilon = 1$ —time→ $\varepsilon = 0$

(exploration) (exploitation)

Boltzmann policy

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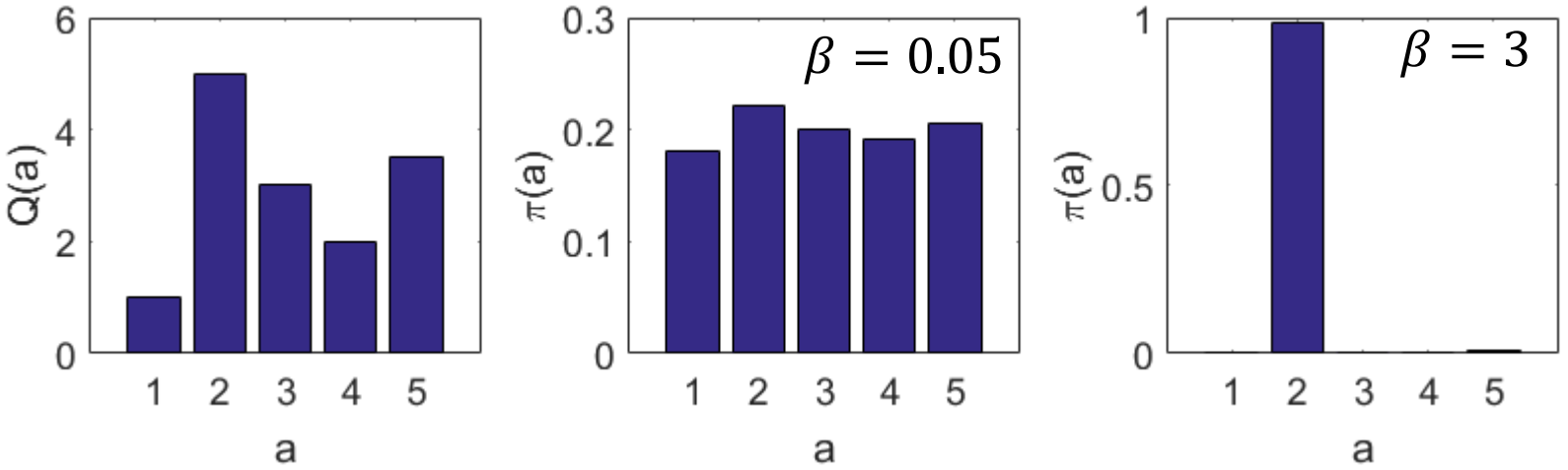
- The policy is calculated from the value

$$\pi(a) = \frac{\exp\big(\beta Q(a)\big)}{\sum_{a' \in \mathcal{A}} \exp\big(\beta Q(a')\big)}$$

where β is an inverse temperature

  - $\beta = 0$: pure exploration (random policy)
  - $\beta \to \infty$: pure exploitation (greedy policy)

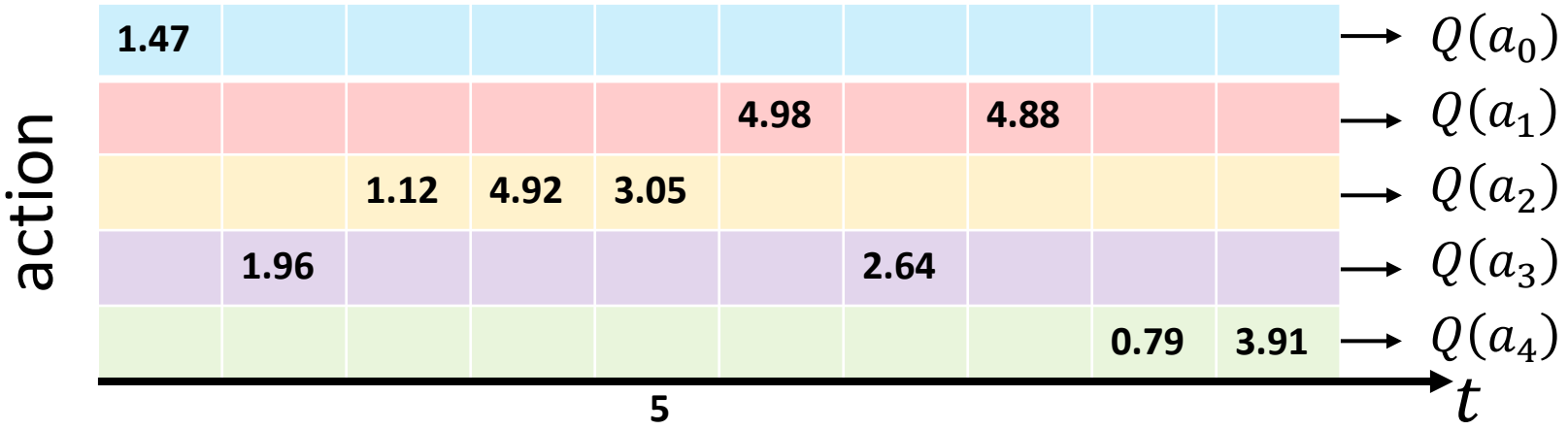


$\beta = 0 \xrightarrow{\text{time}} \beta = \infty$

(exploration) (exploitation)

Estimation of Q

- Let $R^n(a)$ and $Q^n(a)$ denote the reward received after the n-th selection of a and the estimate of its action value after it has been selected $n-1$ times



- $R^1(a_2) = 1.12,\ Q^1(a_2) \triangleq R^1(a_2) = 1.12$
- $R^2(a_2) = 4.92,\ Q^2(a_2) = \left(R^1(a_2) + R^2(a_2)\right)/2 = 3.02$
- $R^3(a_2) = 3.05,\ Q^3(a_2) = (R^1(a_2) + R^2(a_2) + R^3(a_2))/3 = 3.03$

Incremental Estimation of Q

$$Q^n(a) = \frac{1}{n}\sum_{i=1}^{n} R^i(a) = \frac{1}{n}\left(R^n(a) + \sum_{i=1}^{n-1} R^i(a)\right)$$

$$= \frac{1}{n}\left(R^n(a) + (n-1)\frac{1}{n-1}\sum_{i=1}^{n-1} R^i(a)\right)$$

$$= \frac{1}{n}\left(R^n(a) + (n-1)Q^{n-1}(a)\right)$$

$$= Q^{n-1}(a) + \frac{1}{n}\left[R^n(a) - Q^{n-1}(a)\right]$$

Interpretation of the update rule

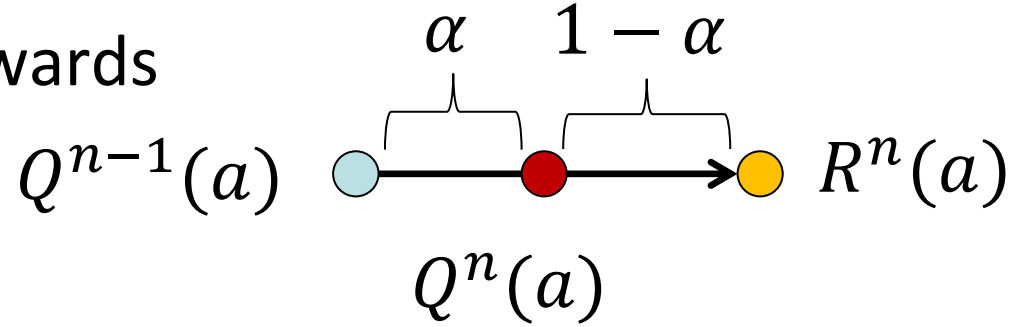
- $$Q^n(a) = Q^{n-1}(a) + \frac{1}{n}[R^n(a) - Q^{n-1}(a)]$$

  new estimate — target — old estimate

- $\delta \triangleq R^n(a) - Q^{n-1}(a)$ represents the error for the old estimate
- $\alpha \triangleq 1/n$ is a learning rate

$$Q^n(a) = (1-\alpha)Q^{n-1}(a) + \alpha R^n(a)$$

- Online update rule for estimating rewards



A simple bandit algorithm

Initialize, for $a = 0$ to $k - 1$:

$$Q(a) \leftarrow 0, N(a) \leftarrow 0$$

Loop forever:

$$A \leftarrow \begin{cases} \arg\max_a Q(a) & \text{with probability } 1 - \varepsilon \quad \text{(breaking ties randomly)} \\ \text{a random action} & \text{with probability } \varepsilon \end{cases}$$

$$R \leftarrow \text{bandit}(A)$$

$$N(A) \leftarrow N(A) + 1 \qquad Q(A) \leftarrow Q(A) + \frac{1}{N(A)}[R - Q(A)]$$

Performance of ε-greedy policy (ε=0.1)

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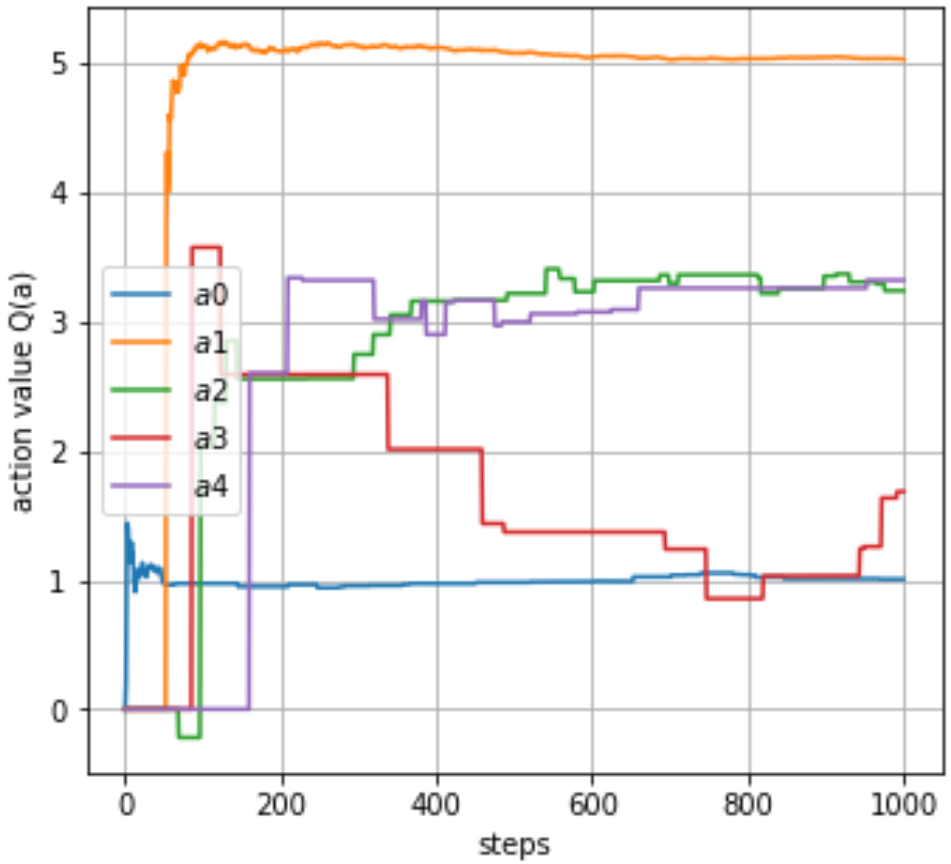
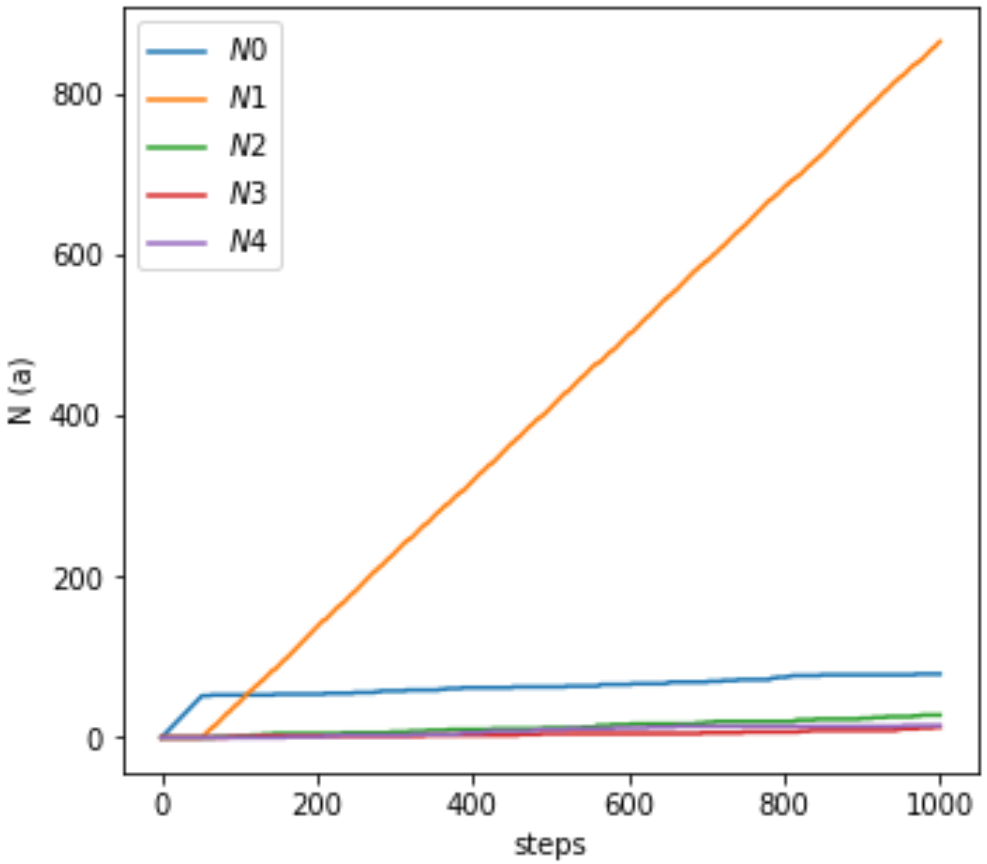
- Found the optimal action (a1) successfully





Performance of Boltzmann policy (β=1)

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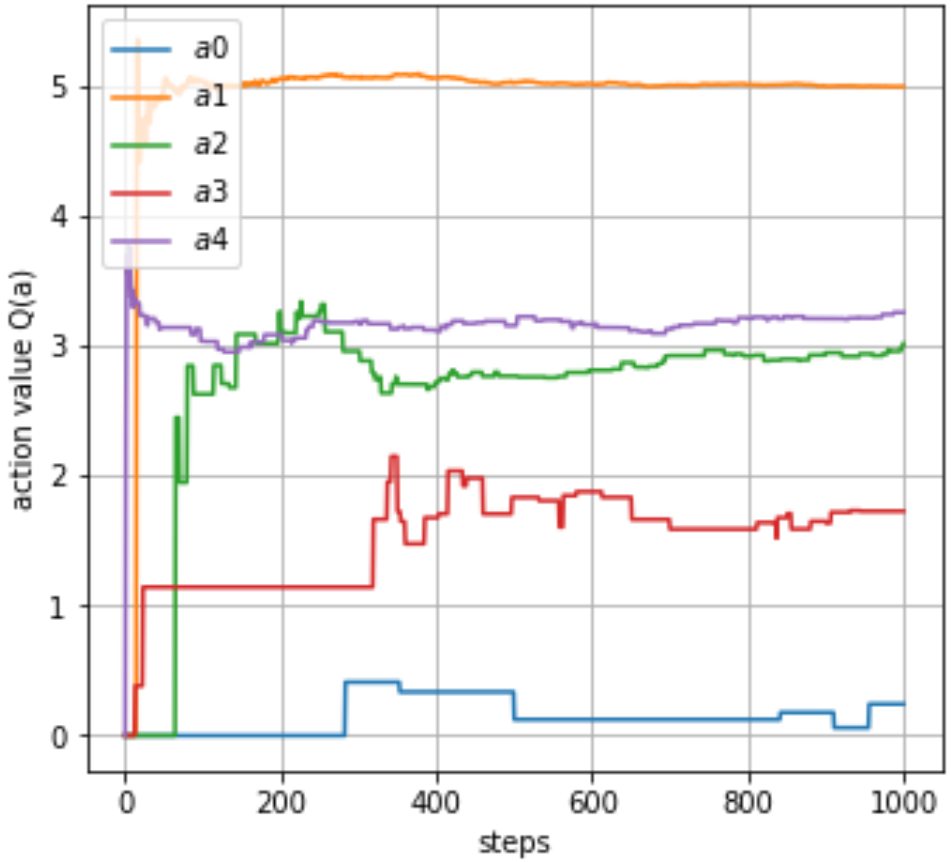
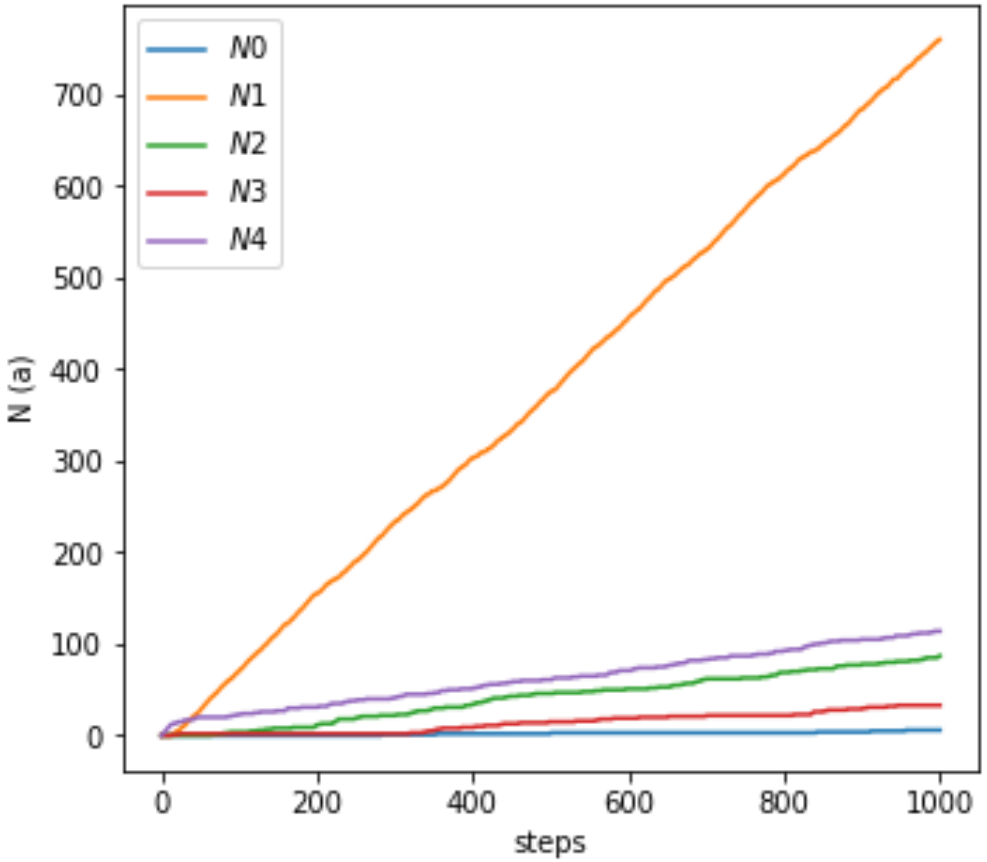
- Found the optimal action (a1) successfully





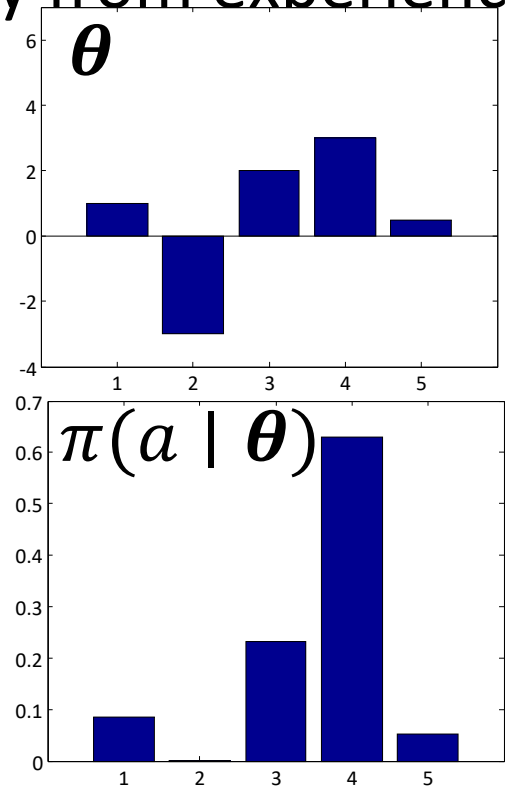
REINFORCEMENT LEARNING FOR BANDIT PROBLEMS
-- POLICY-BASED APPROACH --

Policy-based approach

- So far, we explicitly estimate action values from experiences, and they are used to derive a policy
- Next, we consider how to learn the policy directly from experiences
- One way is to parameterize the policy by the Boltzmann distribution
- The Boltzmann policy is given by

$$\pi(a_i \mid \boldsymbol{\theta}) = \frac{\exp(\theta_i)}{\sum_{j=1}^{k} \exp(\theta_j)}$$

where $\boldsymbol{\theta} = [\theta_1, \theta_2, \ldots, \theta_k]^\top$



Policy-based approach

- The expected reward is

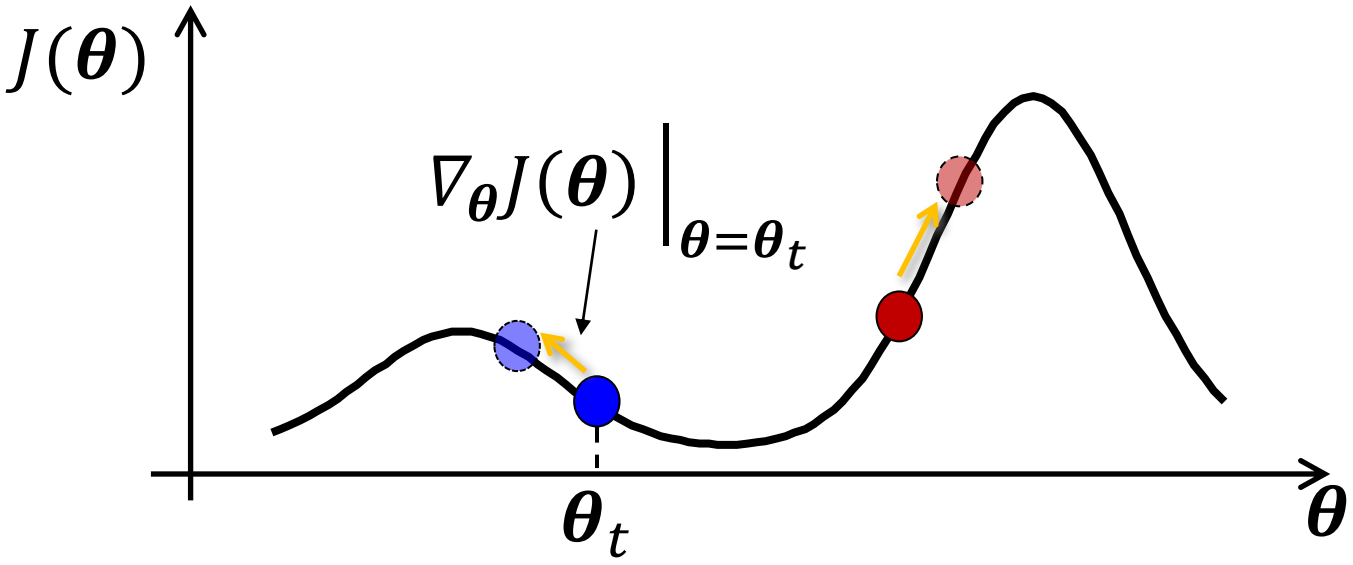
$$J(\boldsymbol{\theta}) = \mathbb{E}_{\pi}[R] = \sum_{r,a} rp(r \mid a)\pi(a \mid \boldsymbol{\theta})$$

- The goal is to find $\boldsymbol{\theta}$ that maximizes $J(\boldsymbol{\theta})$

- Use a gradient ascent method to maximize $J(\boldsymbol{\theta})$ with respect to $\boldsymbol{\theta}$

$$\boldsymbol{\theta} \leftarrow \boldsymbol{\theta} + \alpha \nabla_{\boldsymbol{\theta}} J(\boldsymbol{\theta})$$

where α is a positive step-size parameter



Gradient of function

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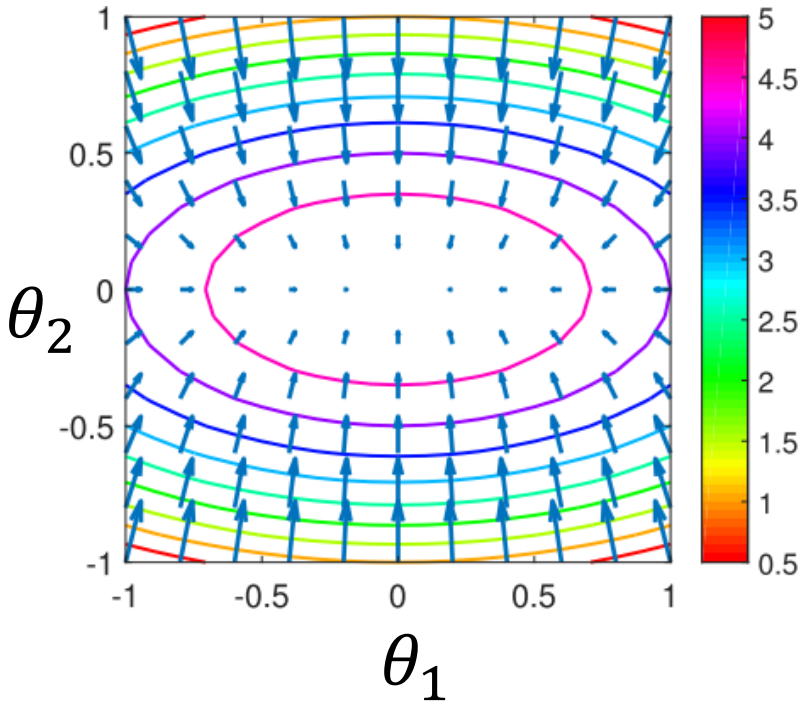
- $\boldsymbol{\theta} = [\theta_1, \theta_2, \ldots, \theta_k]^\top$: k-dimensional vector
- $J(\boldsymbol{\theta})$: $\mathbb{R}^k \to \mathbb{R}$: differentiable scalar function
- $\nabla_{\boldsymbol{\theta}} J$: $\mathbb{R}^k \to \mathbb{R}^k$: its gradient

$$\nabla_{\boldsymbol{\theta}} J(\boldsymbol{\theta}) = \nabla_{\boldsymbol{\theta}} J(\theta_1, \ldots, \theta_k) = \begin{bmatrix} \partial J/\partial \theta_1 \\ \vdots \\ \partial J/\partial \theta_k \end{bmatrix} = \frac{\partial J}{\partial \boldsymbol{\theta}}$$



$$J(\boldsymbol{\theta}) = -\theta_1^2 - 4\theta_2^2 + 5$$

$$\nabla_{\boldsymbol{\theta}} J(\boldsymbol{\theta}) = \begin{bmatrix} -2\theta_1 \\ -8\theta_2 \end{bmatrix}$$

Gradient ascent optimization

- Find a local optimal solution

Initialize

$n \leftarrow 0$

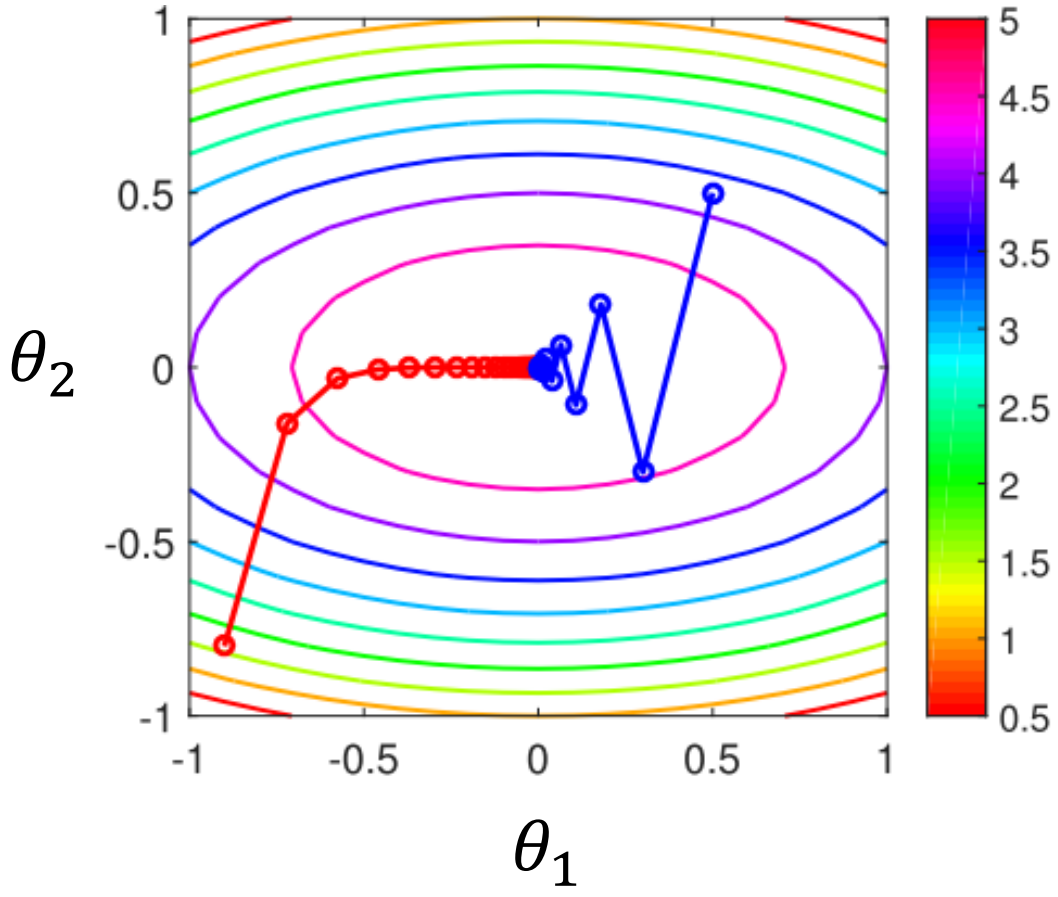
Repeat:

$n \leftarrow n + 1$

$\boldsymbol{\theta}^n \leftarrow \boldsymbol{\theta}^{n-1} + \alpha \nabla_{\boldsymbol{\theta}} J(\boldsymbol{\theta})$

until stopping_criterion($\boldsymbol{\theta}^n, \boldsymbol{\theta}^{n-1}, \epsilon$)

return $\boldsymbol{\theta}^n$



Calculate $\nabla_{\boldsymbol{\theta}} J(\boldsymbol{\theta})$

- $\nabla_{\boldsymbol{\theta}} J(\boldsymbol{\theta}) = \frac{\partial}{\partial \boldsymbol{\theta}} \left[\sum_{r,a} r p(r \mid a) \pi(a \mid \boldsymbol{\theta}) \right]$

$$= \sum_{r,a} r p(r \mid a) \frac{\partial \pi(a \mid \boldsymbol{\theta})}{\partial \boldsymbol{\theta}}$$

$$= \sum_{r,a} r p(r \mid a) \pi(a \mid \boldsymbol{\theta}) \frac{\partial \ln \pi(a \mid \boldsymbol{\theta})}{\partial \boldsymbol{\theta}}$$

$$= \mathbb{E}_{\pi} \left[R \frac{\partial \ln \pi(a \mid \boldsymbol{\theta})}{\partial \boldsymbol{\theta}} \right]$$

Calculate $\partial \ln \pi(\boldsymbol{a} \mid \boldsymbol{\theta}) / \partial \boldsymbol{\theta}$ (1/2)

- $\pi(a_i \mid \boldsymbol{\theta}) = \dfrac{\exp(\theta_i)}{\sum_{j=0}^{k-1} \exp(\theta_j)}$
- $\dfrac{\partial \pi(a_i \mid \boldsymbol{\theta})}{\partial \theta_i} = \dfrac{\exp(\theta_i) \sum_{j=0}^{k-1} \exp(\theta_j) - (\exp(\theta_i))^2}{\left(\sum_{j=0}^{k-1} \exp(\theta_j)\right)^2}$

$$= \frac{\exp(\theta_i)}{\sum_{j=0}^{k-1} \exp(\theta_j)} - \left(\frac{\exp(\theta_i)}{\sum_{j=0}^{k-1} \exp(\theta_j)}\right)^2 = \pi(a_i \mid \boldsymbol{\theta})\left(1 - \pi(a_i \mid \boldsymbol{\theta})\right)$$

- $\dfrac{\partial \ln \pi(a_i \mid \boldsymbol{\theta})}{\partial \theta_i} = \dfrac{1}{\pi(a_i \mid \boldsymbol{\theta})} \dfrac{\partial \pi(a_i \mid \boldsymbol{\theta})}{\partial \theta_i} = 1 - \pi(a_i \mid \boldsymbol{\theta})$

Calculate $\partial \ln \pi(\boldsymbol{a} \mid \boldsymbol{\theta}) / \partial \boldsymbol{\theta}$ (2/2)

- $$\frac{\partial \pi(a_i \mid \boldsymbol{\theta})}{\partial \theta_j} = -\frac{\exp(\theta_i)\exp(\theta_j)}{\left(\sum_{j=0}^{k-1}\exp(\theta_j)\right)^2} = -\pi(a_i \mid \boldsymbol{\theta})\pi(a_j \mid \boldsymbol{\theta})$$

- $$\frac{\partial \ln \pi(a_i \mid \boldsymbol{\theta})}{\partial \theta_j} = \frac{1}{\pi(a_i \mid \boldsymbol{\theta})}\frac{\partial \pi(a_i \mid \boldsymbol{\theta})}{\partial \theta_j} = -\pi(a_j \mid \boldsymbol{\theta})$$

Implementation

- Compute the gradient from experiences

$$\nabla_{\boldsymbol{\theta}} J(\boldsymbol{\theta}) = \mathbb{E}_{\pi}[R \nabla_{\boldsymbol{\theta}} \ln \pi(a \mid \boldsymbol{\theta})]$$

- Use the stochastic gradient method

1. Sample action: $a \sim \pi(a \mid \boldsymbol{\theta})$
2. Receive the reward r from the environment: $r \sim p(r \mid a)$
3. Update θ by the stochastic gradient ascent

$$\boldsymbol{\theta} \leftarrow \boldsymbol{\theta} + \alpha r \frac{\partial \ln \pi(a \mid \boldsymbol{\theta})}{\partial \boldsymbol{\theta}}$$

Variance reduction

- Although we can estimate policy gradient, it has a large variance in general
- We can further reduce the variance by subtracting a baseline

$$\mathbb{E}_\pi\left[(R-b)\frac{\partial \ln \pi(a \mid \boldsymbol{\theta})}{\partial \boldsymbol{\theta}}\right]$$

$$= \underbrace{\mathbb{E}_\pi\left[R\frac{\partial \ln \pi(A \mid \boldsymbol{\theta})}{\partial \boldsymbol{\theta}}\right]}_{J(\boldsymbol{\theta})} + b\underbrace{\mathbb{E}_\pi\left[\frac{\partial \ln \pi(a \mid \boldsymbol{\theta})}{\partial \boldsymbol{\theta}}\right]}_{=0}$$

Proof sketch

- We want to prove $\mathbb{E}_\pi\left[\frac{\partial \ln \pi(a \mid \boldsymbol{\theta})}{\partial \boldsymbol{\theta}}\right] = \mathbf{0}$

- $$\mathbb{E}_\pi\left[\frac{\partial \ln \pi(a \mid \boldsymbol{\theta})}{\partial \boldsymbol{\theta}}\right] = \sum_{r,a} p(r \mid a)\,\pi(a \mid \boldsymbol{\theta})\,\frac{\partial \ln \pi(a \mid \boldsymbol{\theta})}{\partial \boldsymbol{\theta}}$$

  $$= \sum_{r,a} p(r \mid a)\,\frac{\partial \pi(a \mid \boldsymbol{\theta})}{\partial \boldsymbol{\theta}} = \frac{\partial}{\partial \boldsymbol{\theta}}\Big[\underbrace{\sum_{r,a} p(r \mid a)\pi(a \mid \boldsymbol{\theta})}_{p(r,a \mid \boldsymbol{\theta})}\Big]$$

  $$= \frac{\partial}{\partial \boldsymbol{\theta}}[1] = \mathbf{0}$$

Performance without variance reduction

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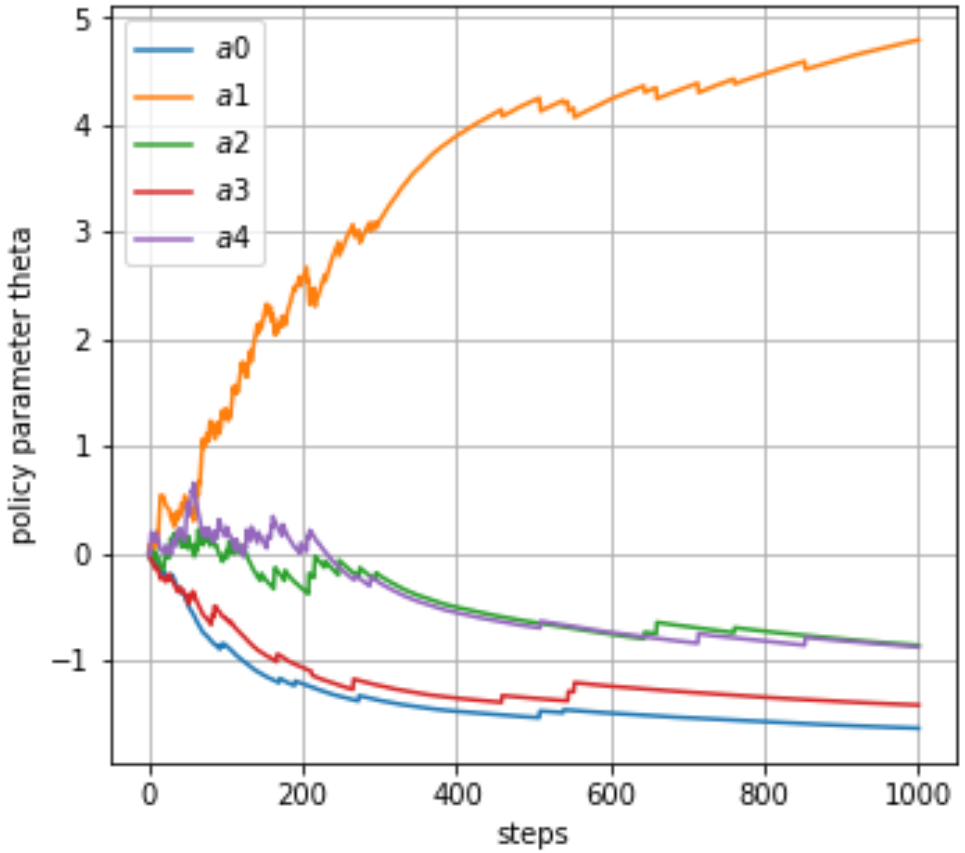

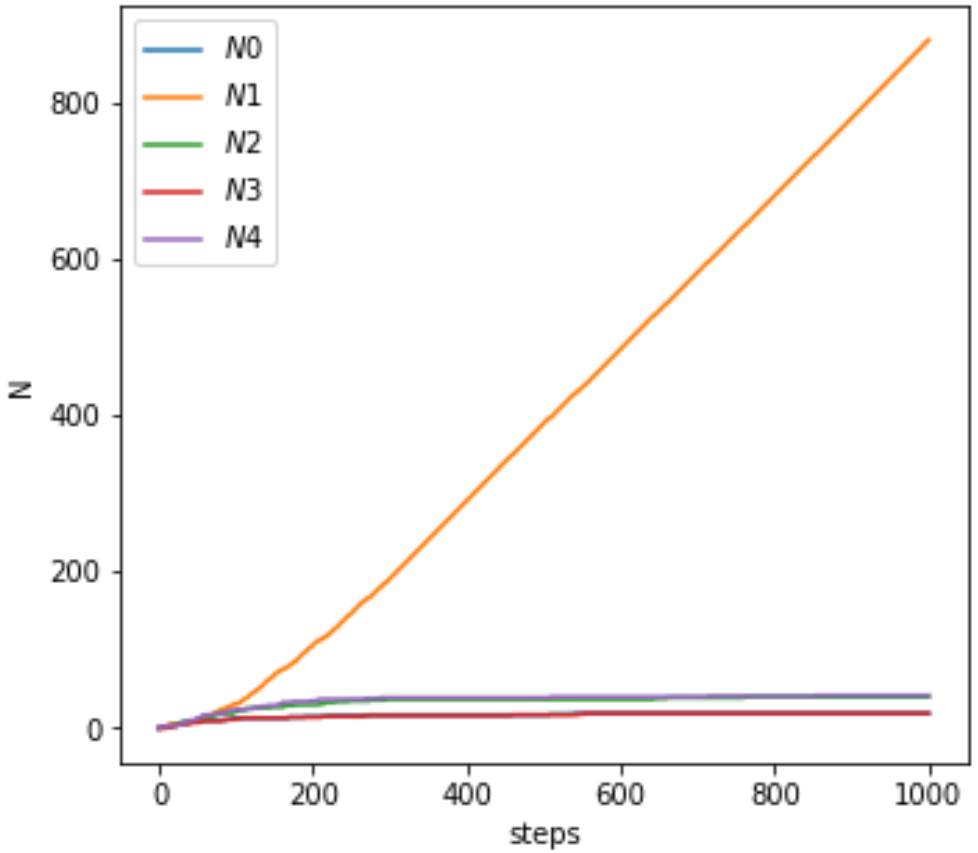

Performance with variance reduction

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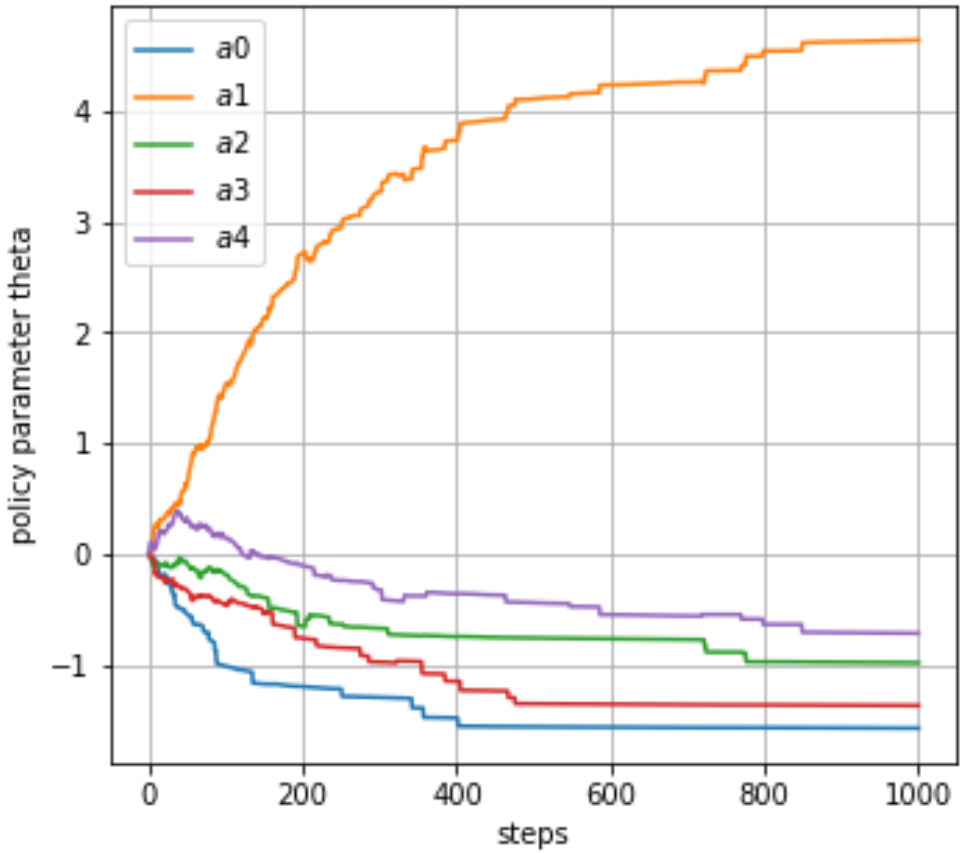

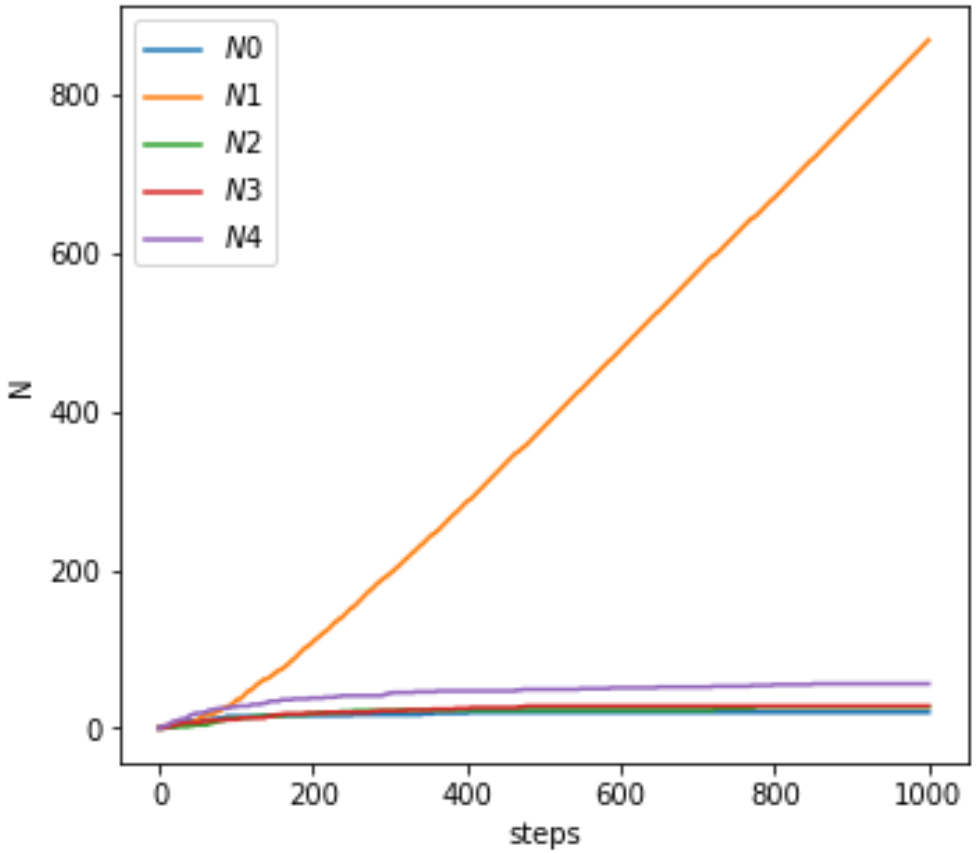

Summary

- Introduction to reinforcement learning
- Bandit problem
  - Action, Reward, Value
- Value-based approach: Learn the action-value function and derive the policy ➡ Indirect approach
- Policy-based approach: Learn the policy by the gradient ascent method of the objective function with respect to the policy parameters

  ➡ Direct approach