

# Modeling Plasma Wake Field Accelerator

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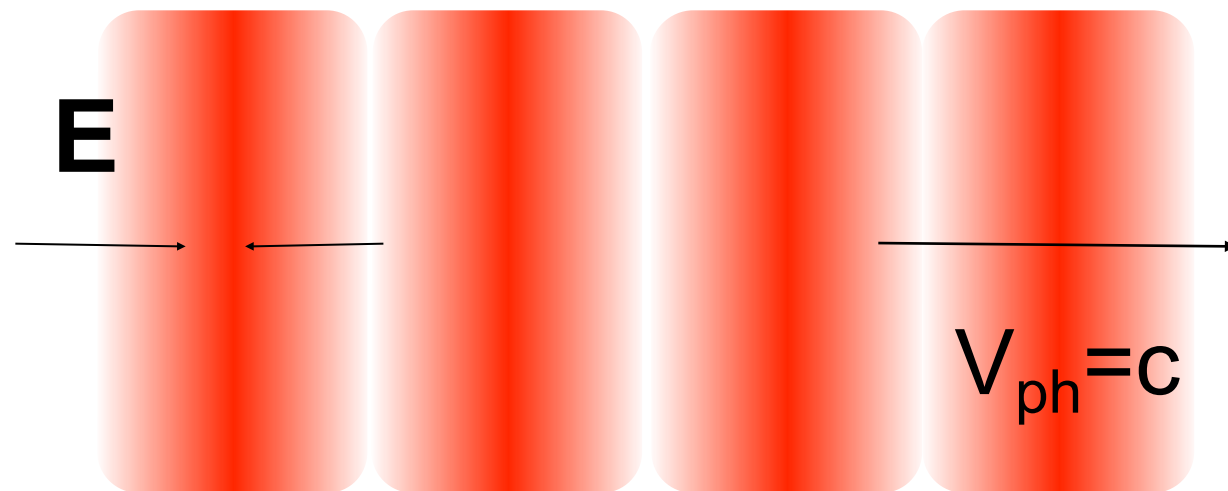


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1-D plasma density wave



## Gauss' Law

$$\nabla \cdot E \sim ik_p E = -4\pi en_1$$

$$k_p = \omega_p / V_{ph} \approx \omega_p / c$$

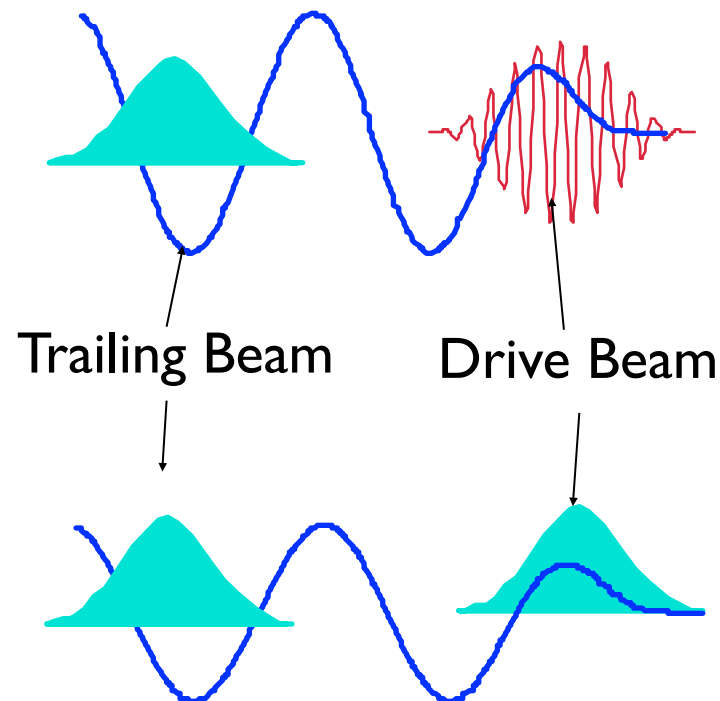
$$n_1 \sim n_o$$

$$\Rightarrow eE \sim 4\pi en_o e^2 c / \omega_p = mc\omega_p$$

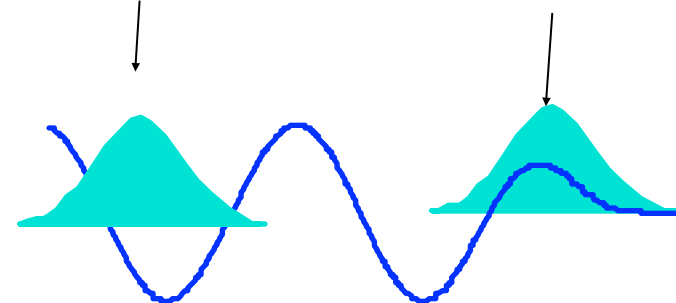
$$\text{or } eE \sim \sqrt{\frac{n_o}{10^{16} \text{ cm}^{-3}}} \underline{10 \text{ GeV/m}}$$

~1000 times larger  
than the conventional  
accelerators

## Nonlinear Process



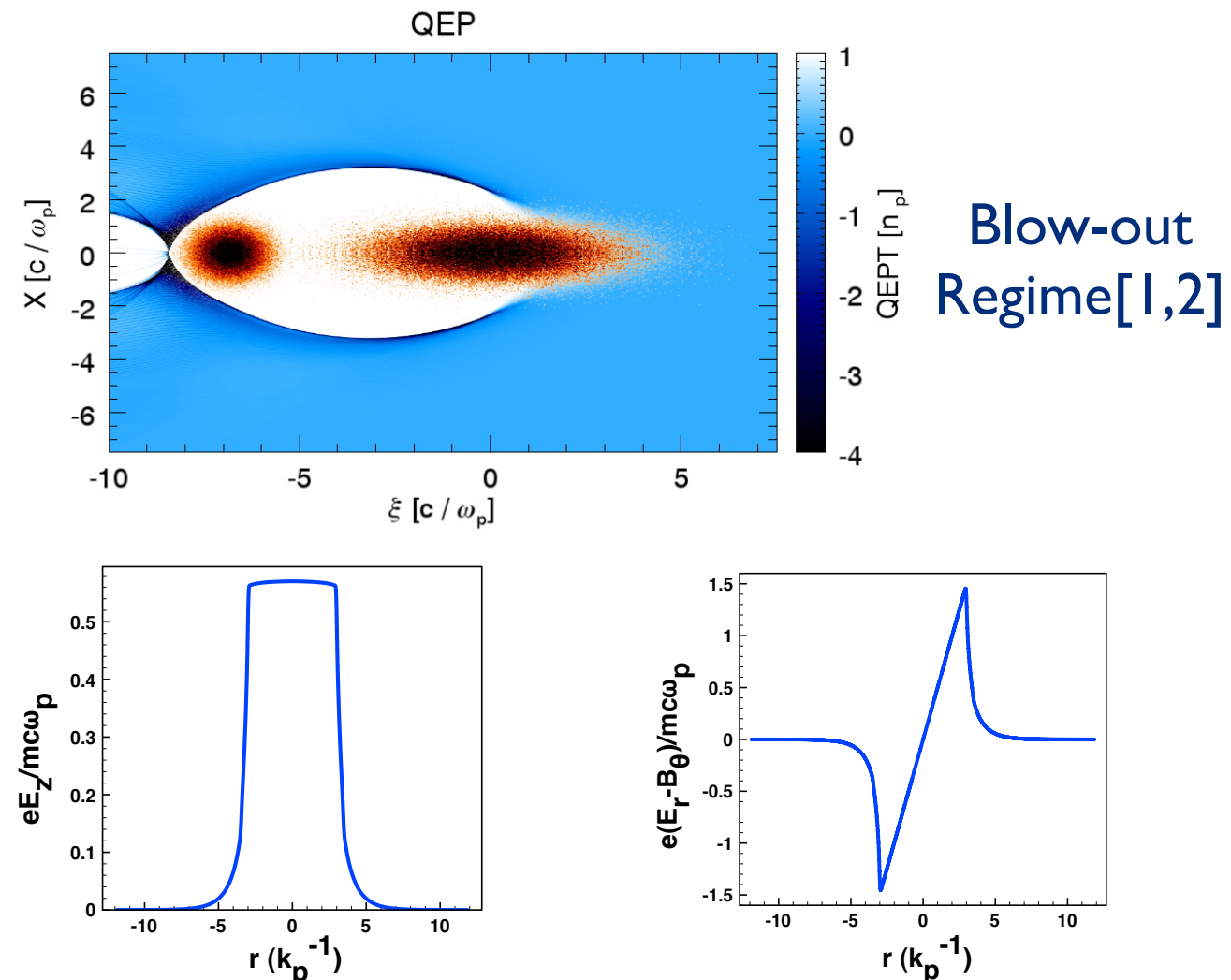
LWFA\*



PWFA\*

- Wake: phase velocity = driver velocity ( $V_g$  or  $V_{\text{beam}}$ )

LWFA: Tajima and Dawson 1979  
PWFA: Chen, Dawson et al., 1985



\*J. B. Rosenzweig, et. al., Phys. Rev. A 44, R6189 (1991)

\*W. Lu, et. al., Phys. Rev. Lett. 96, 165002 (2006)



# UCLA

## Plasma Based Accelerator Research is at the Forefront of Science



Plasma simulation has greatly impacted on PBA research.



Beam Particles:  $10^8 \sim 10^9$

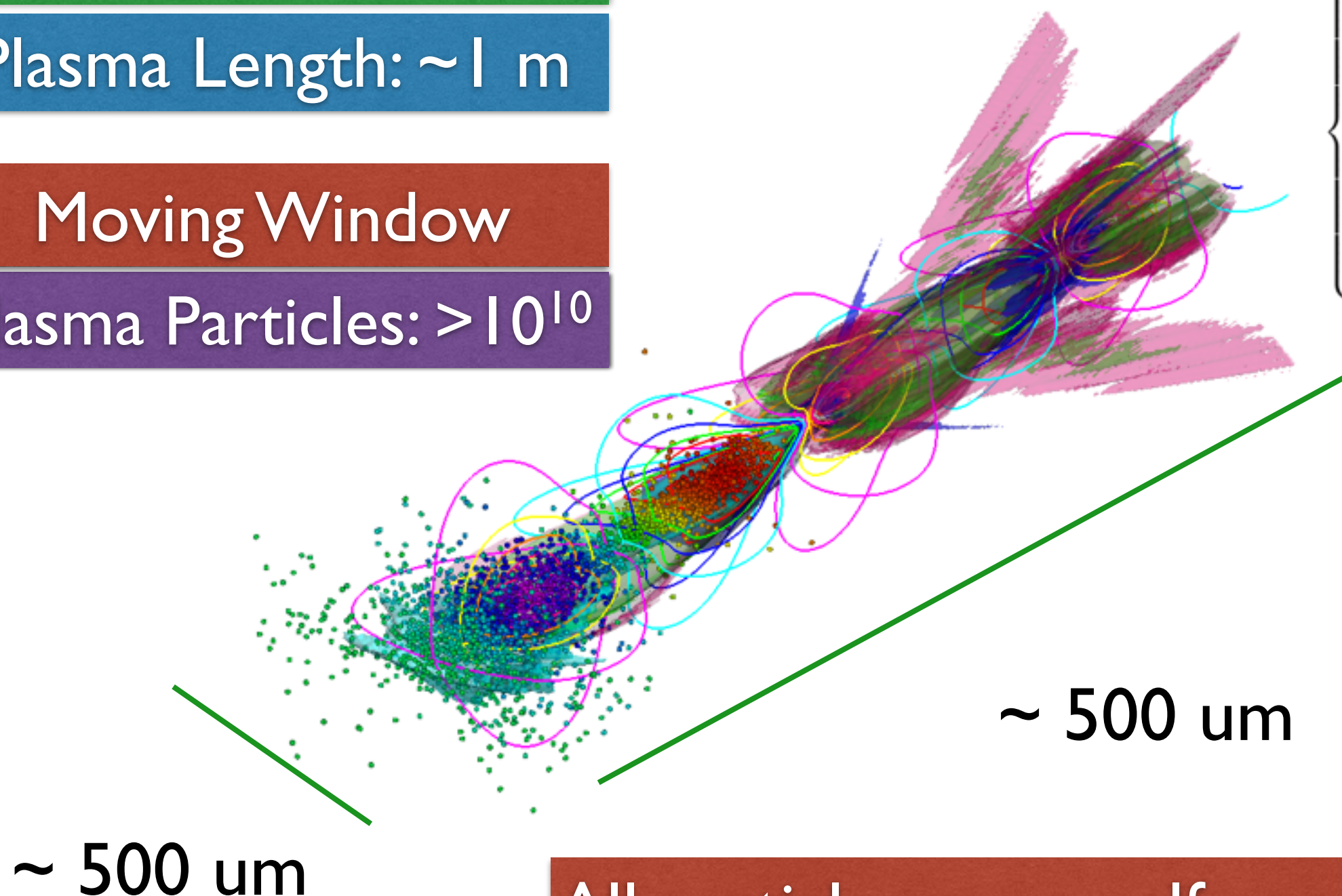
Plasma Length:  $\sim 1$  m

Moving Window

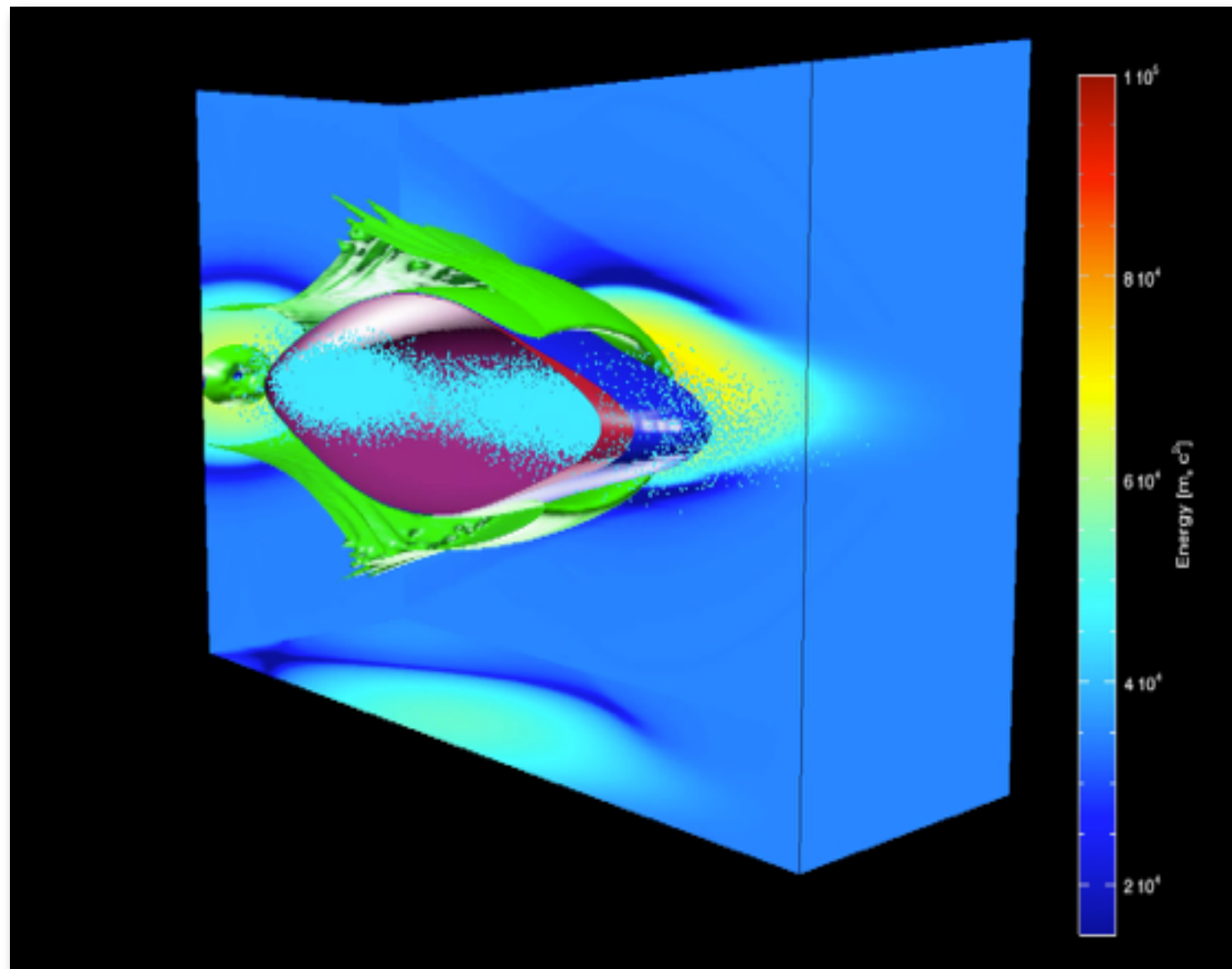
Plasma Particles:  $> 10^{10}$

Maxwell's Eqns

$$\begin{cases} \nabla \times \vec{E} = -\frac{\partial \vec{B}}{\partial t} \\ \nabla \times \vec{B} = \frac{\partial \vec{E}}{\partial t} + \vec{J} \\ \nabla \cdot \vec{E} = \rho \\ \nabla \cdot \vec{B} = 0 \end{cases}$$



All particles move self-consistently



3D or 2D r-z with  
moving window

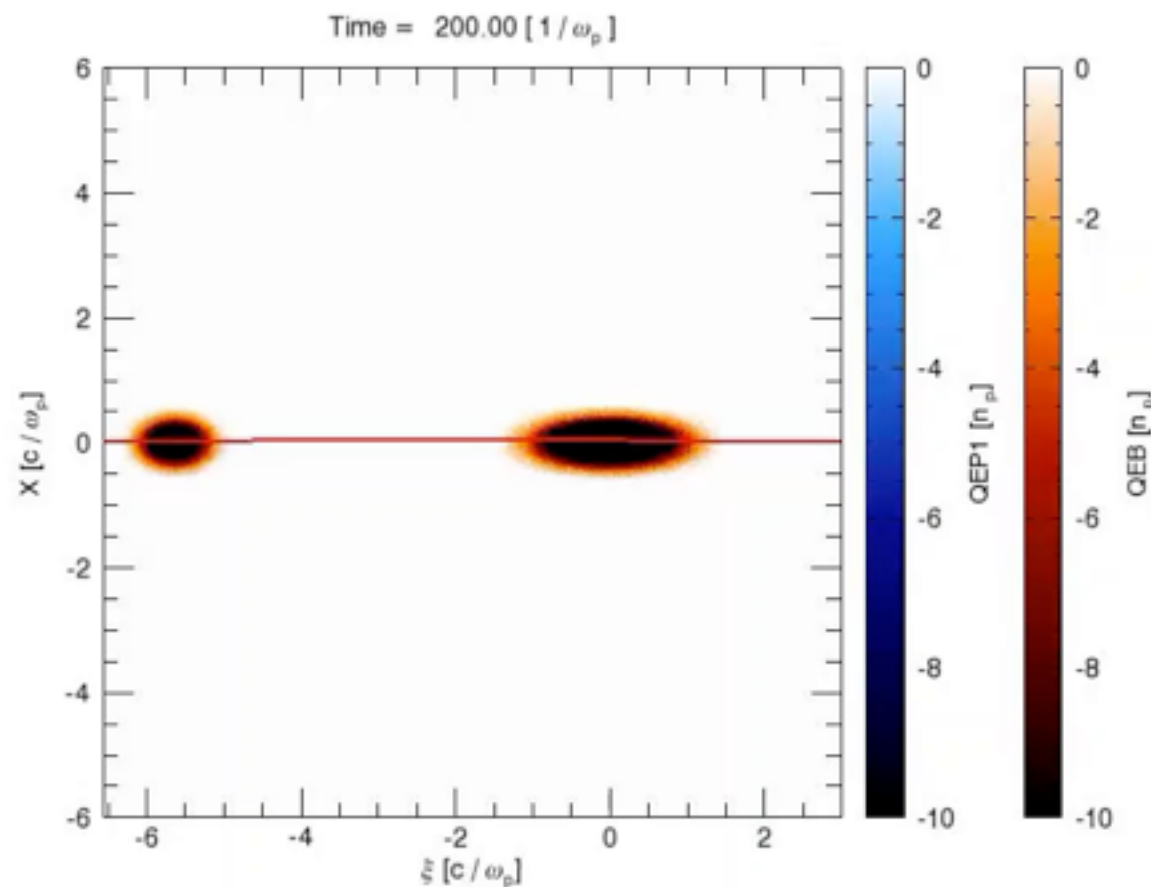
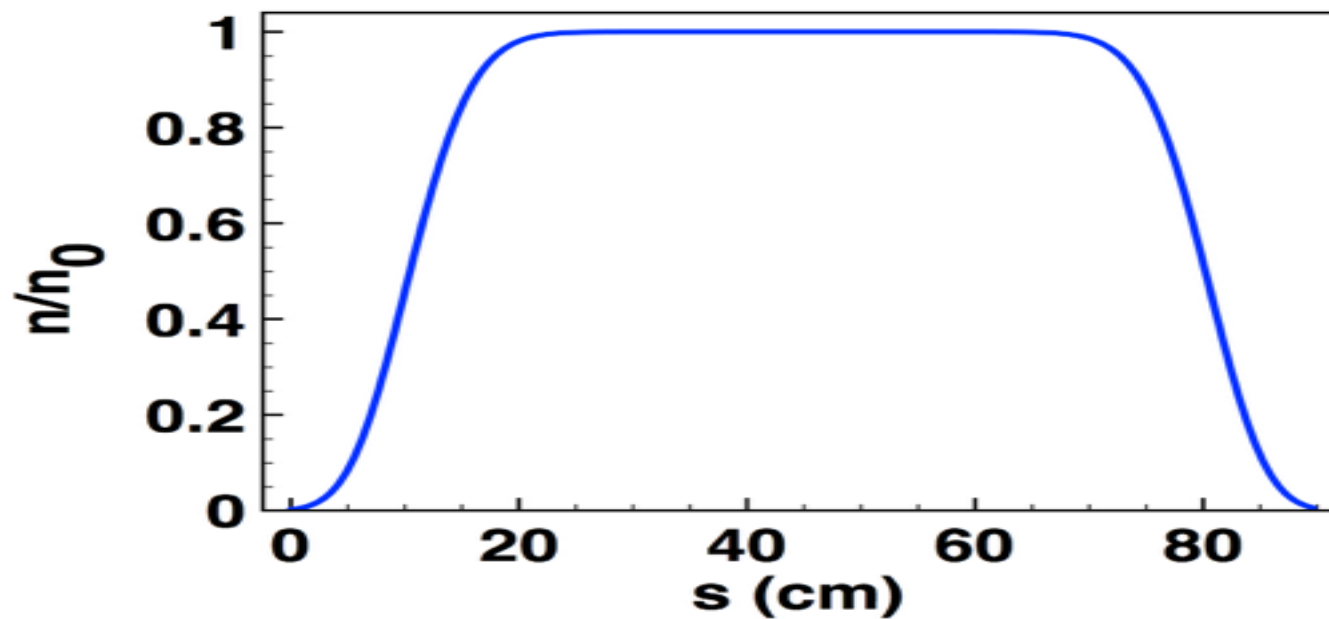
Box Size:  
Large Enough to  
minimize the boundary  
effects.

Cell Size: Resolve the plasma wave length.

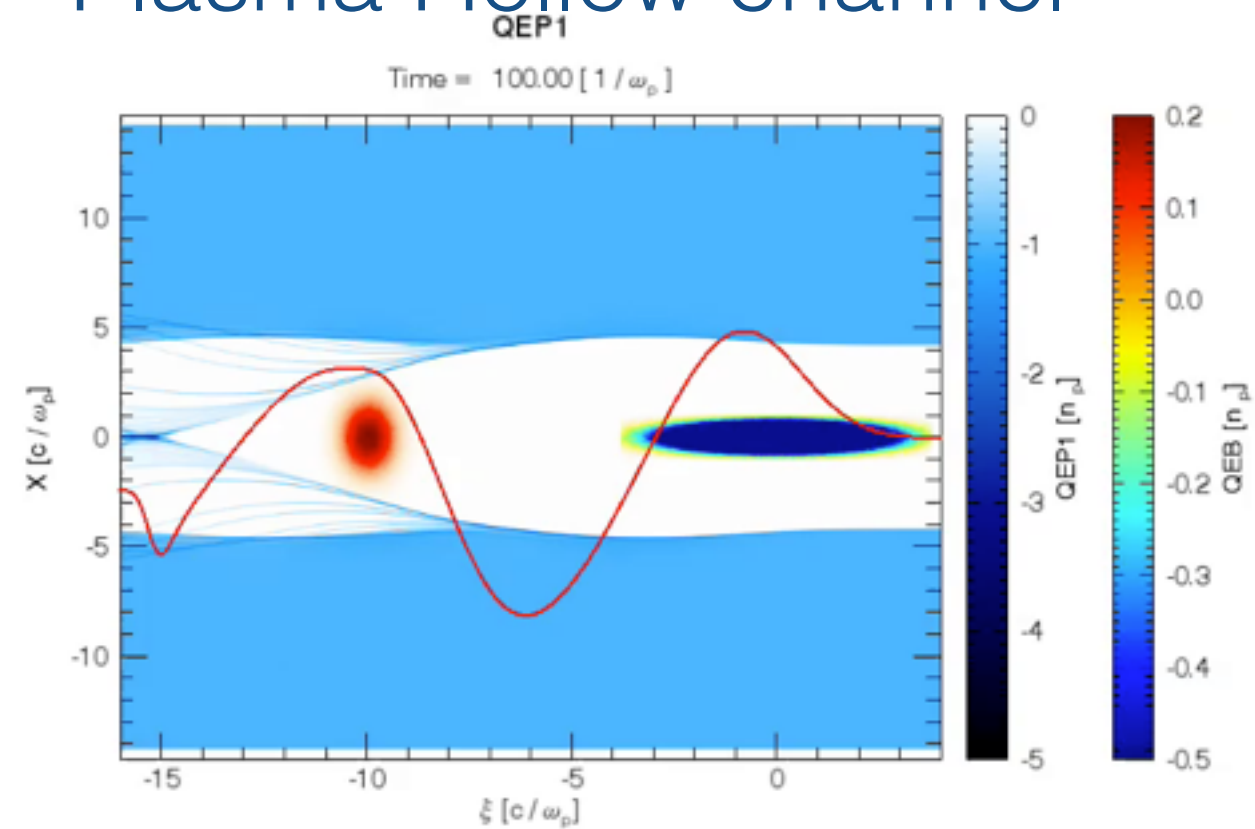
$$\leq 0.05 k_p^{-1}$$



## Plasma Density Profile

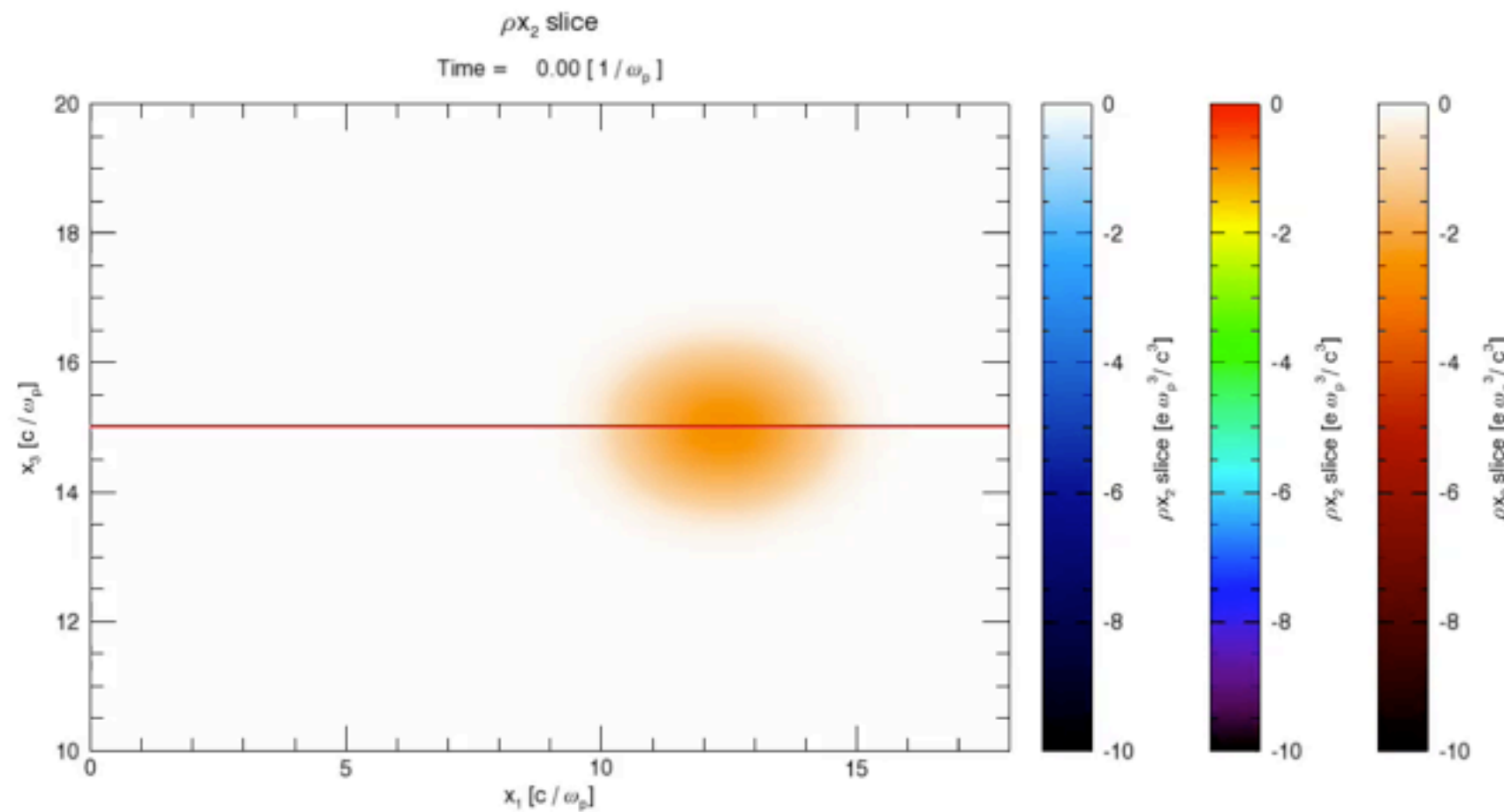


## Plasma Hollow channel



Define the density profile using math function.

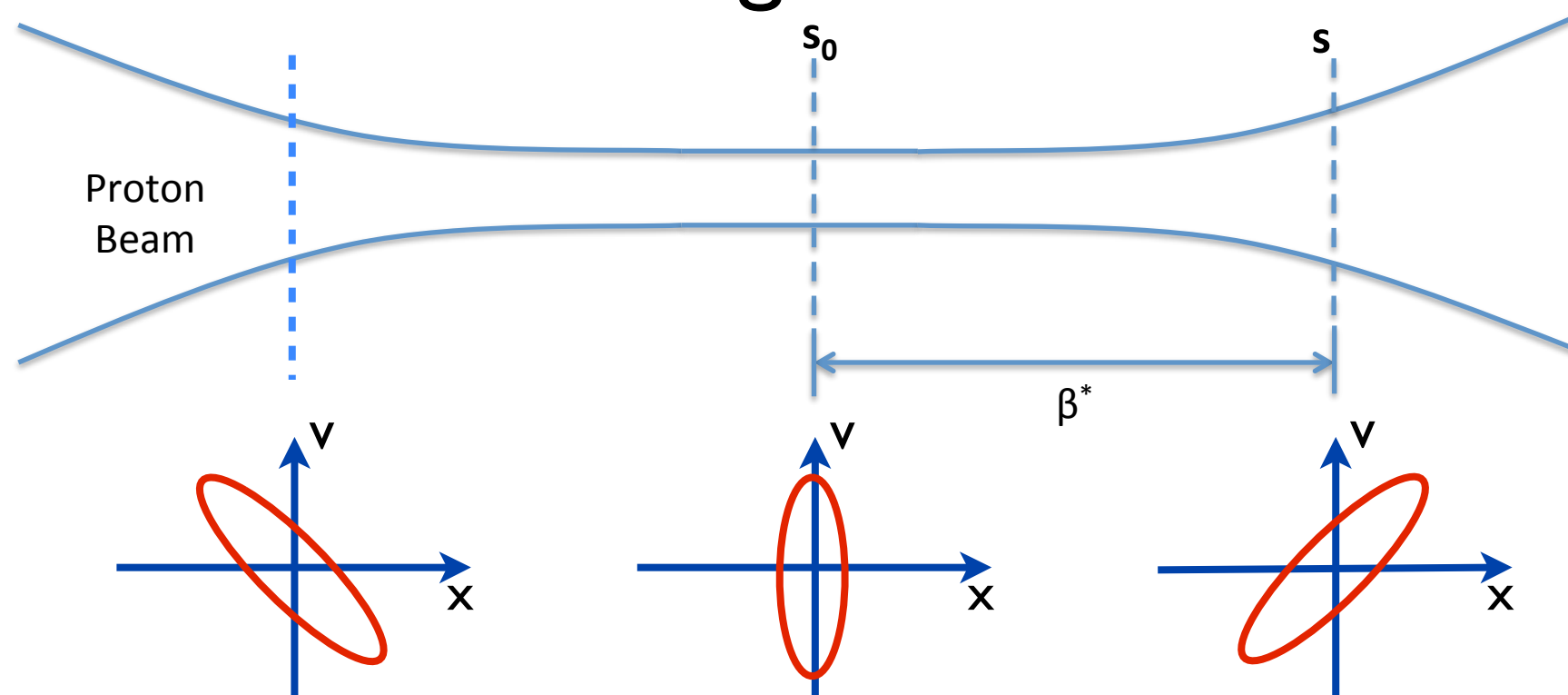
## Field Ionized Plasma



Neutral Species



## The focal length of the beam



$$\beta^* = \gamma \frac{\sigma_r^2}{\epsilon_N}$$

$$\sigma_r = \sigma_{r0} \sqrt{1 + (s - s_0)^2 / \beta^{*2}}$$

Twiss Parameter:

$$\gamma x'^2 + 2\alpha x x' + \beta x^2 = \epsilon$$

In the Vacuum:  $\gamma = \frac{1}{\beta^*}, \quad \beta = \beta^*(1 + \alpha^2), \quad \alpha = -\frac{s - s_0}{\beta^*}$

Beam Density:  $n_b = n_{b0} \exp\left(-\frac{r^2}{2\sigma_r^2}\right) \exp\left(-\frac{z^2}{2\sigma_z^2}\right)$

Transverse Phase Space:  $\sim \exp\left(-\frac{x^2}{2\sigma_{x0}^2}\right) \exp\left(-\frac{v^2}{2\sigma_{v0}^2}\right)$

Transverse Phase Space  
at  $s^* = z - z_0$ :  $\sim \exp\left(-\frac{(x - vs^*/c)^2}{2\sigma_{x0}^2}\right) \exp\left(-\frac{v^2}{2\sigma_{v0}^2}\right)$

$$\sim \exp\left[-\frac{x^2}{2\sigma_{x0}^2(1 + s^{*2}/\beta^{*2})}\right] \exp\left[-\frac{\left(v - \frac{s^*cx}{\beta^{*2} + s^{*2}}\right)^2}{2\sigma_{v0}^2/(1 + s^{*2}/\beta^{*2})}\right]$$

$$\bar{\sigma}_x = \sigma_{x0} \sqrt{1 + s^{*2}/\beta^{*2}}$$

$$\bar{\sigma}_v = \sigma_{v0} / \sqrt{1 + s^{*2}/\beta^{*2}}$$

Good for Osiris Initialization!



Boundary Condition

Conducting

Interpolation Order

1st

MPI or Shared Memory

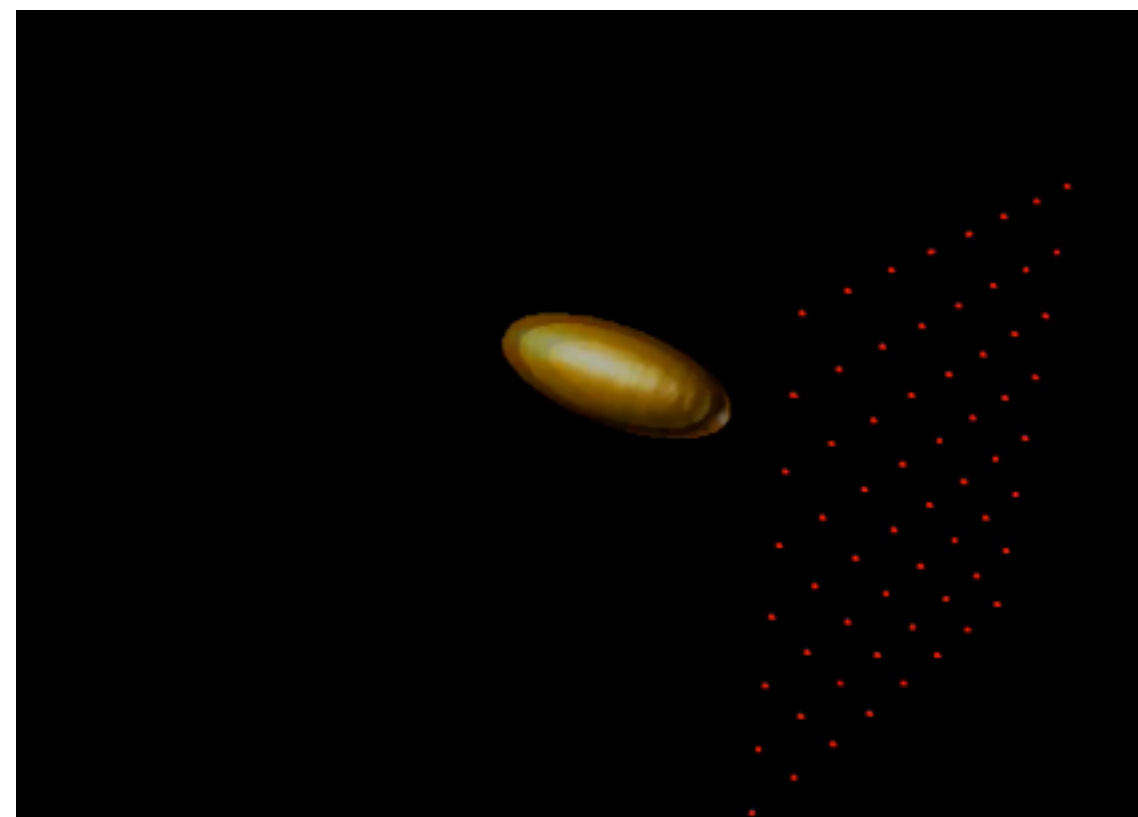
MPI + OpenMP



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Fortran 2003  
Object Oriented

Fortran 77  
Fortran 90



Github QuickPIC-OpenSource