



July 31 - August 5

## ADVANCED ACCELERATOR CONCEPTS

July 31 - August 5  
2016  
Gaylord National Convention Center, National Harbor, MD



# Comparison of the injection between boosted frame and lab frame simulations

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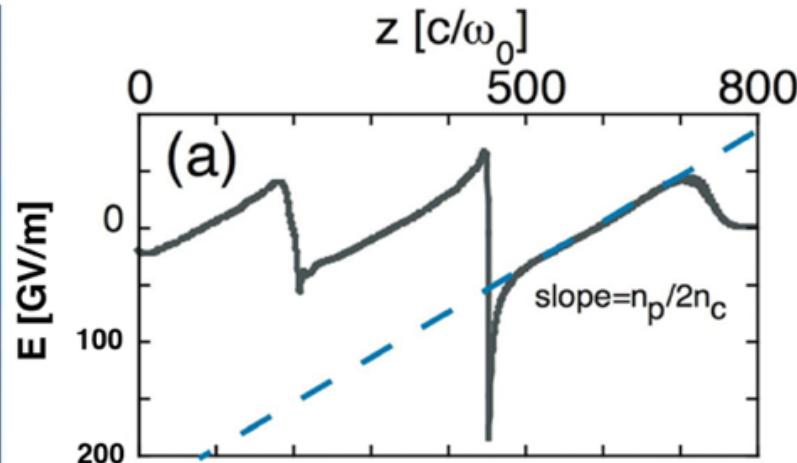
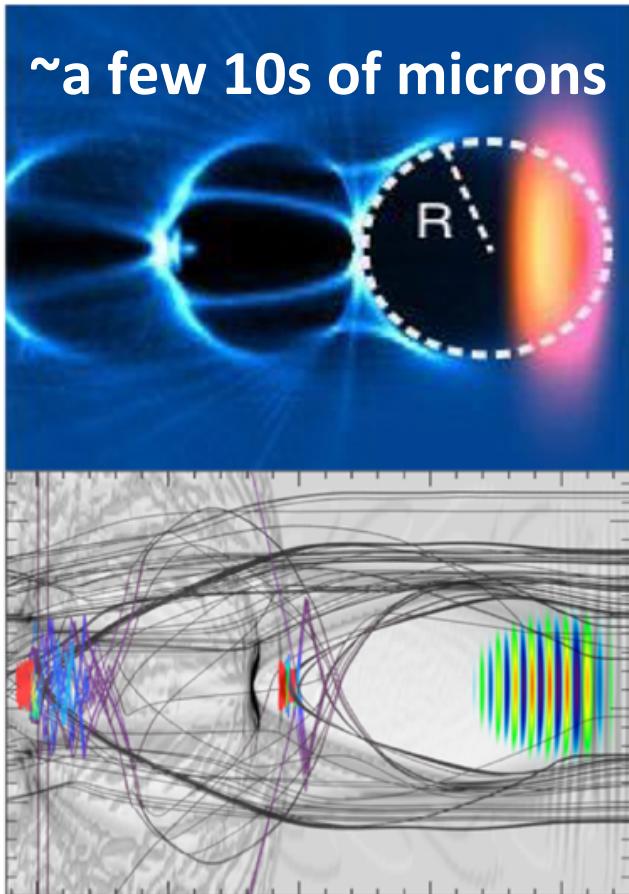
Aug 2th, 2016

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<http://picksc.idre.ucla.edu/>

PICK<sup>SC</sup>

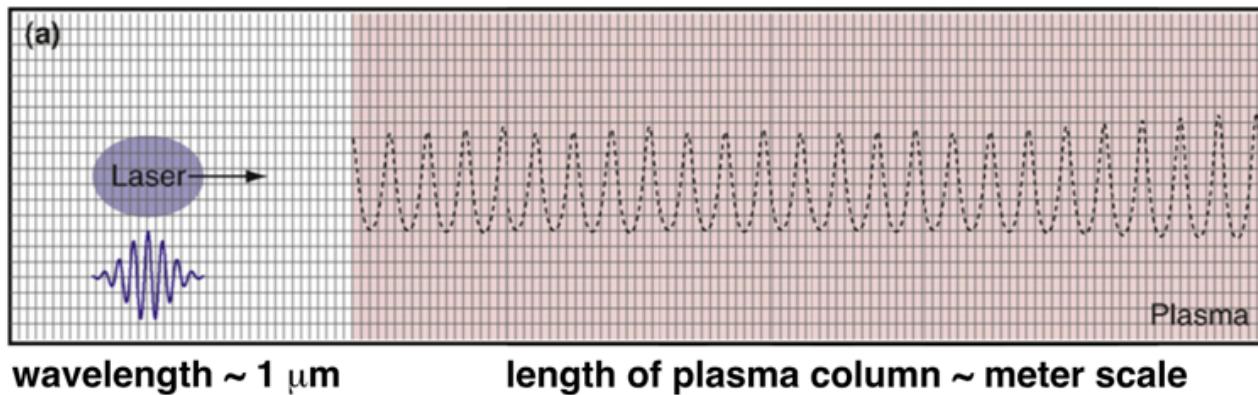
# Simulation in LWFA



- plasma density highly modulated
- acceleration field highly nonlinear
- particle trajectories highly irregular

We rely on Particle-in-cell simulations to give us vision on the physics in LWFA.

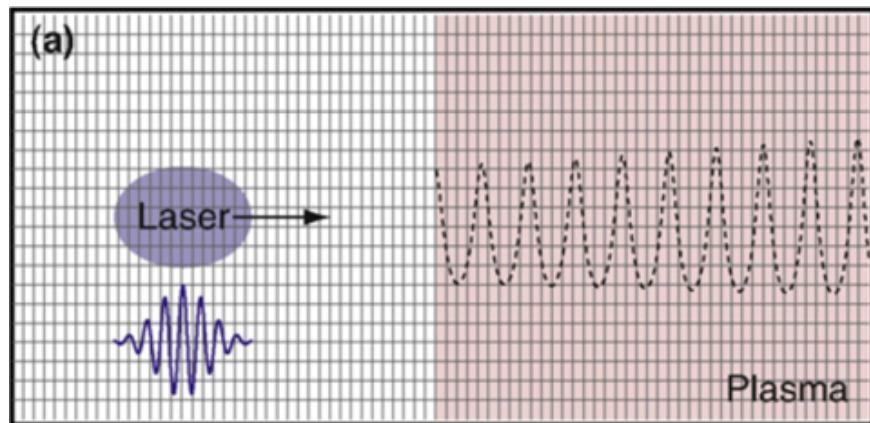
# Lorentz boosted frame simulation of LWFA



Beam energy	plasma column length	CPU-hours
1 GeV	0.09 m	$\sim$ 1 million
10 GeV	0.28 m	$\sim$ 100 million
100 GeV	9.00 m	$\sim$ 10 billion

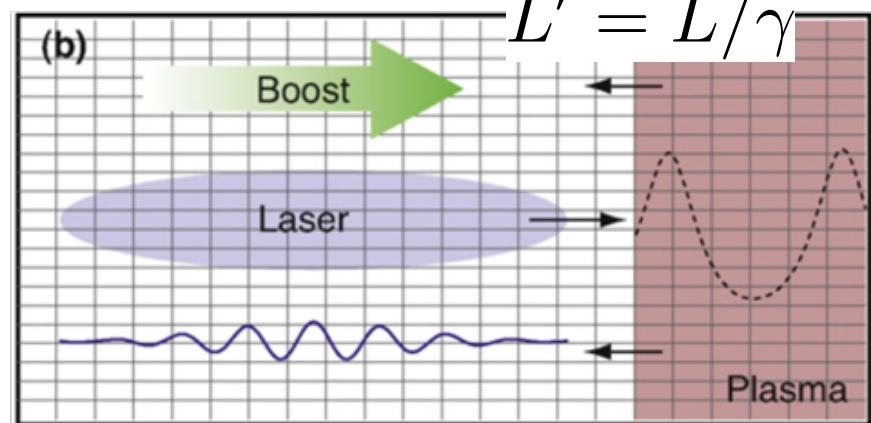
- Quasi-Static Approximation + Ponderomotive Guiding Center
- Full PIC + Guiding Center
- **Lorentz boosted frame**

# Lorentz boosted frame simulation of LWFA



$\sim$  micro meter

$\sim$  centimeter



laser wavelength stretch

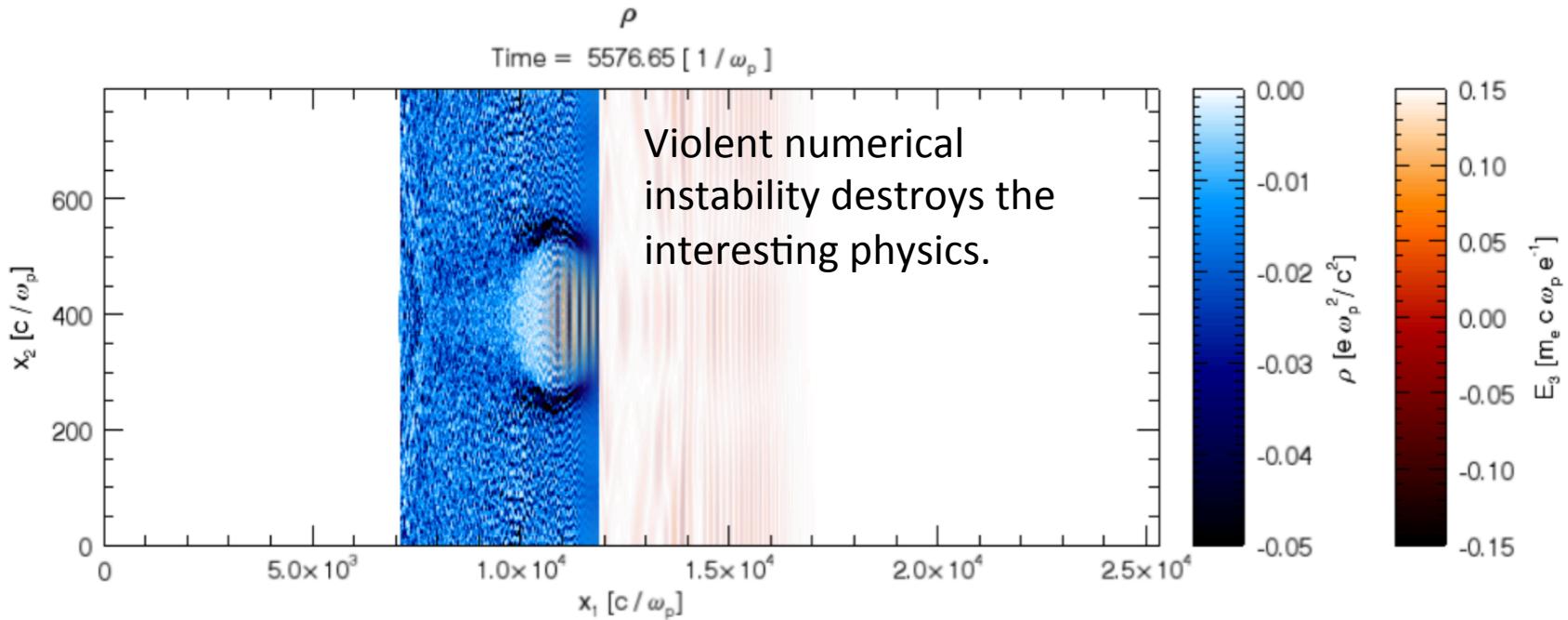
$$\lambda' = \gamma(1 + \beta)\lambda$$

Speed up from Boosted frame:  $\gamma^2$

W. Mori, et. al., NSF Proposal (1992).

J.-L. Vay, Phys. Rev. Lett., 98, 130405 (2007).

# Numerical instability in relativistically drifting plasma

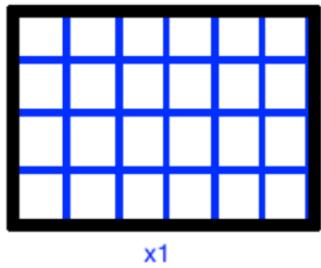


B. B. Godfrey and J.-L. Vay, J. Comp. Phys. 248 (2013) 33. And other papers from Godfrey and Vay.

X. Xu, P. Yu, et. al., Comp. Phys. Comm., 184 (2013) 2503. And other paper from Xu and Yu.

# Hybrid Yee-FFT solver

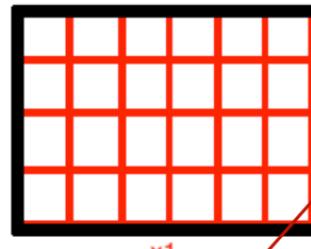
OSIRIS: FDTD solver



$$[k_1] = \frac{\sin(k_1 \Delta x_1 / 2)}{\Delta x_1 / 2}$$

$$[k_2] = \frac{\sin(k_2 \Delta x_2 / 2)}{\Delta x_2 / 2}$$

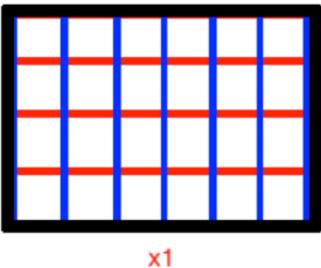
UPIC-EMMA: spectral solver



$$[k_1] = k_1$$

$$[k_2] = k_2$$

Hybrid solver



$$[k_2] = \frac{\sin(k_2 \Delta x_2 / 2)}{\Delta x_2 / 2}$$

$$[k_1] = k_1$$

$$\frac{\partial}{\partial x_1} \quad \frac{\partial}{\partial x_2}$$

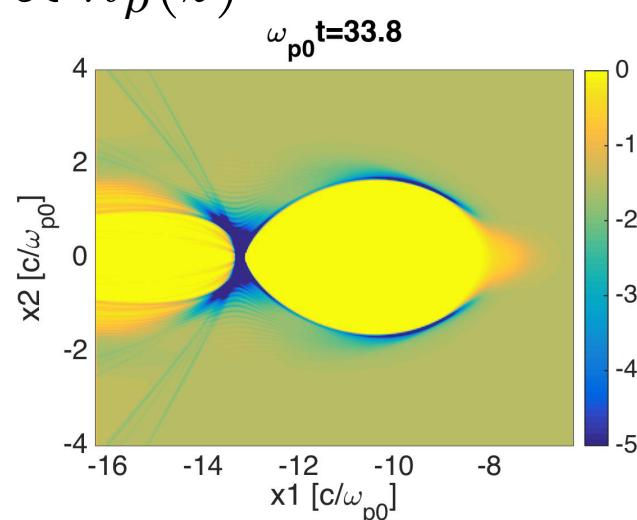
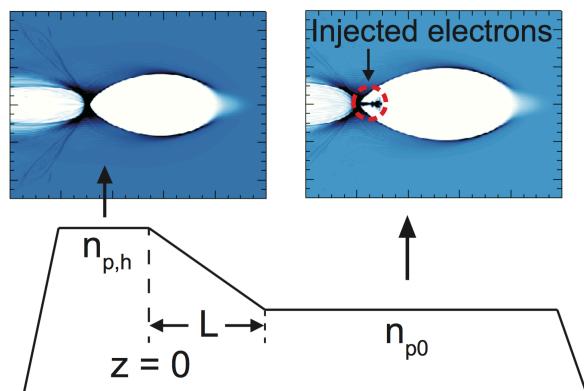
Current correction

$$\tilde{j}_1^{n+\frac{1}{2}} = \frac{\sin k_1 \Delta x_1 / 2}{k_1 \Delta x_1 / 2} j_1^{n+\frac{1}{2}}$$

this idea can be extended to quasi-3d geometry.

# Density Downramp injection - Introduction

- “Accordion effect”<sup>1</sup>:  $\lambda_{wake} \propto n_p(z)^{-1/2}$



- S. Bulanov<sup>2</sup> et al. (1998), and H. Suk<sup>3</sup> et al. (2001) studied the injection process using 1D analysis.
- Beam brightness from 3D PIC simulations:
  - We (2013) showed an injected electrons beam with  $10^{19}$  A/m<sup>2</sup>/rad<sup>2</sup>;
  - J. Grebenyuk et al. (2014)@ $0.35 \times 10^{17}$  A/m<sup>2</sup>/rad<sup>2</sup>.

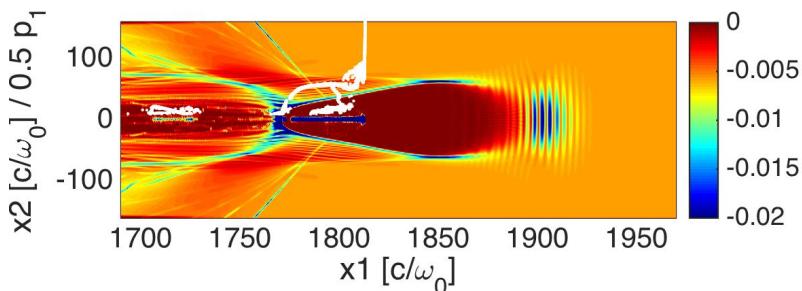
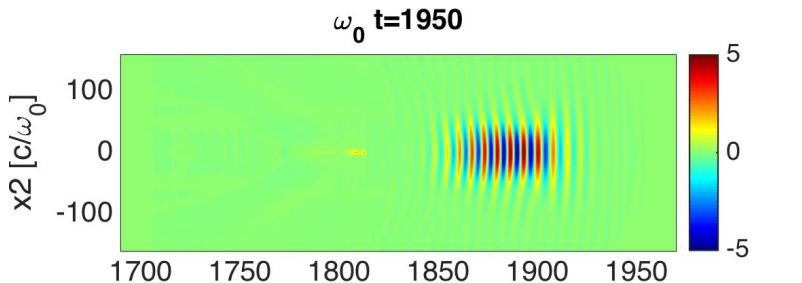
<sup>1</sup>T. Katsouleas, Phys. Rev. A 33, 2056 (1986); <sup>2</sup>S. Bulanov, et al., Phys. Rev. E 58, R5257 (1998); <sup>3</sup>H. Suk, et al., Phys. Rev. Lett. 86, 1011 (2001); <sup>4</sup>FACET-II Proposal v6 (2013); <sup>5</sup>J. Grebenyuk et al., NIMA 740, 246 (2014).

# Simulation setup (Hybrid Solver)

- Laser: LP,  $a_0=4$ , polynomial ( $\tau_{\text{rise}}=\tau_{\text{fall}}=25.4$  fs,  $\tau_{\text{flat}}=0$  fs), Gaussian ( $w_0=4.8$  microns)
- Plasma:  $n_{p0}=10^{19}$  cm $^{-3}$

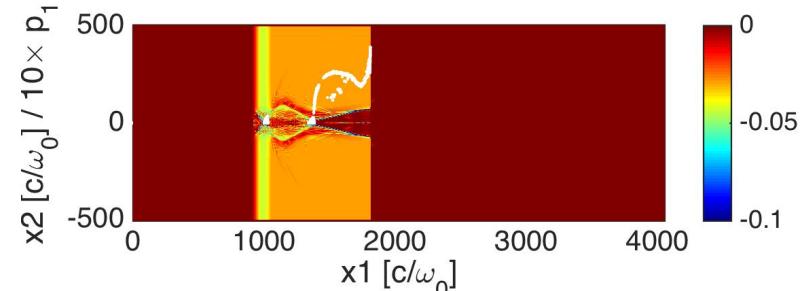
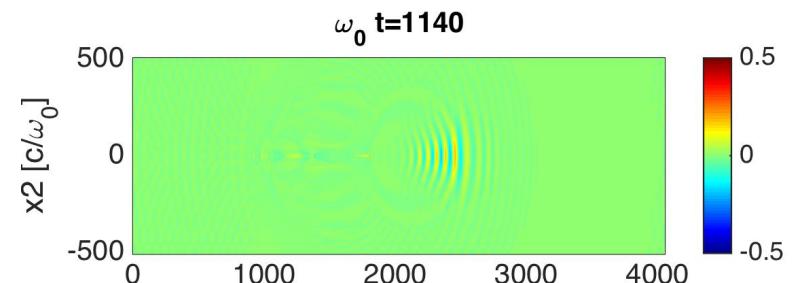
- lab frame

$$dx=[0.2, 2, 2], dt=0.05$$



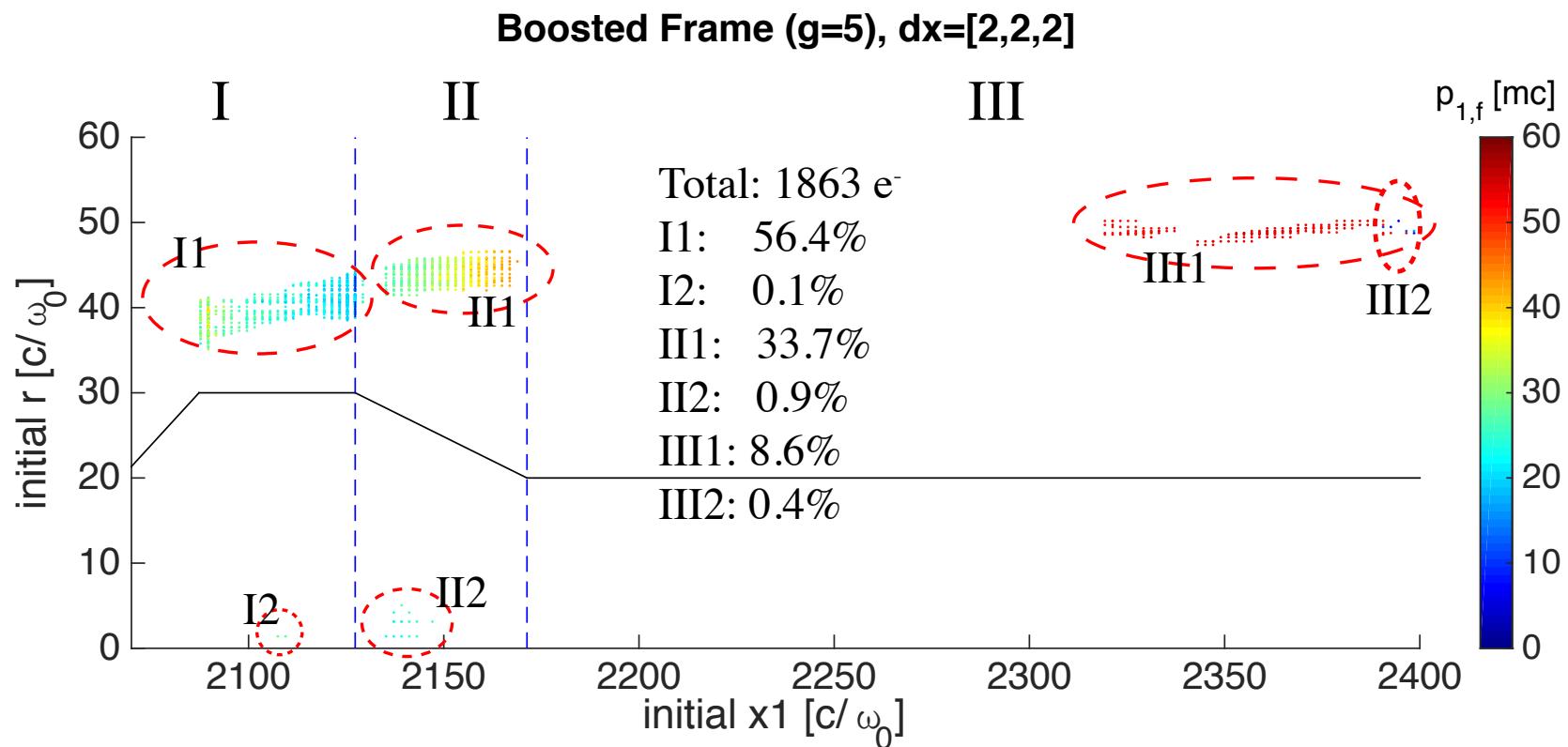
- boosted frame ( $Y_b=5$ )

$$dx=[2, 2, 2], dt=0.6$$



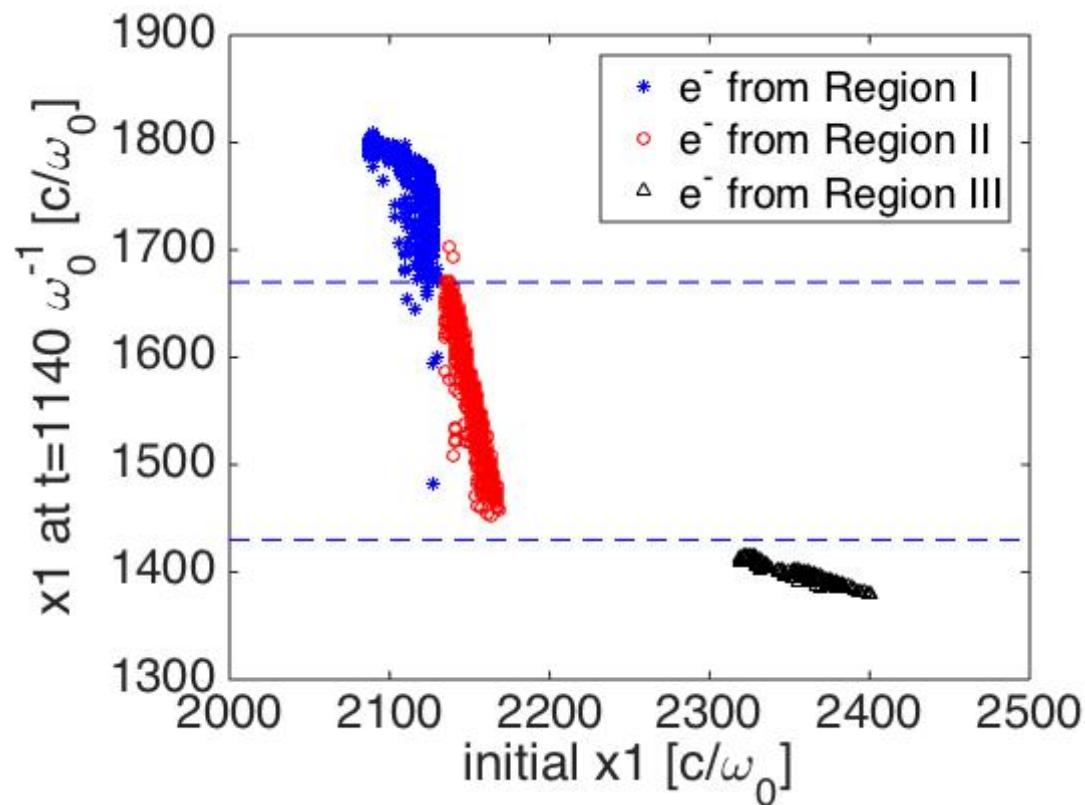
# Boosted Frame Results

- Initial positions of the injected electrons



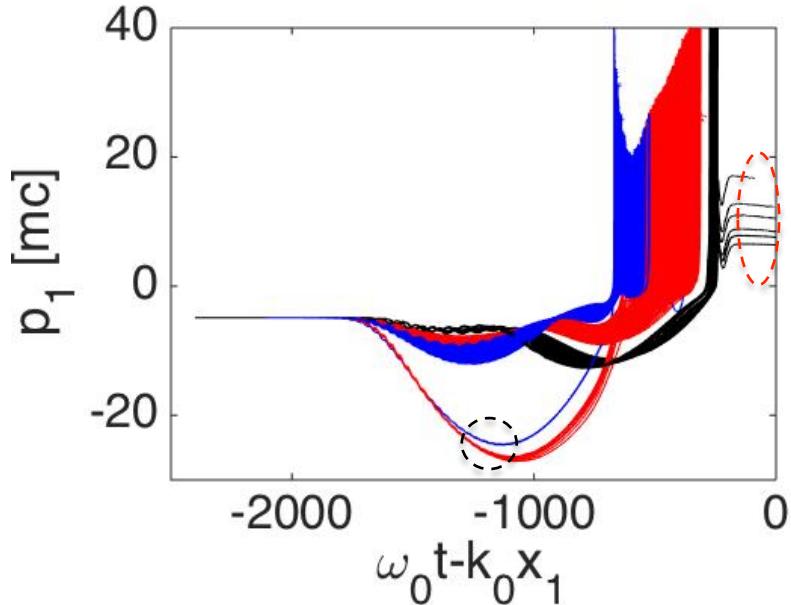
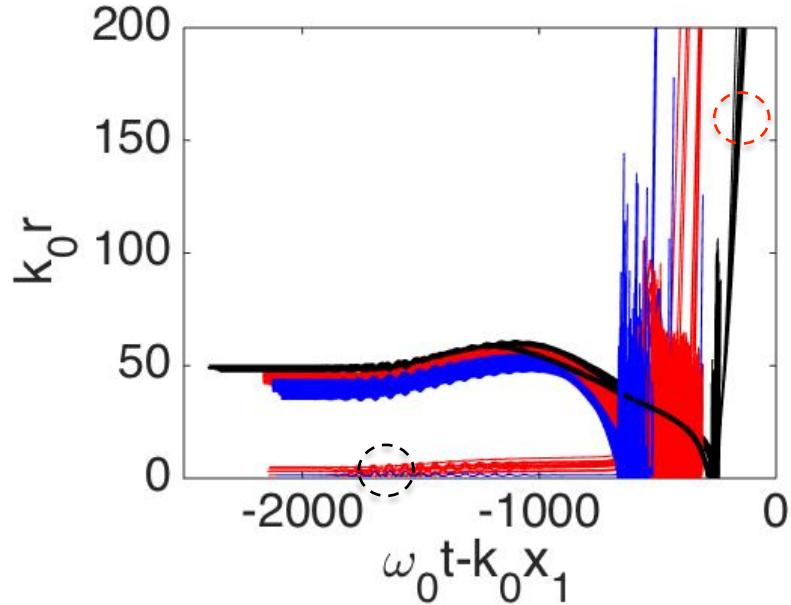
# Boosted Frame Results

- Initial positions of the injected electrons



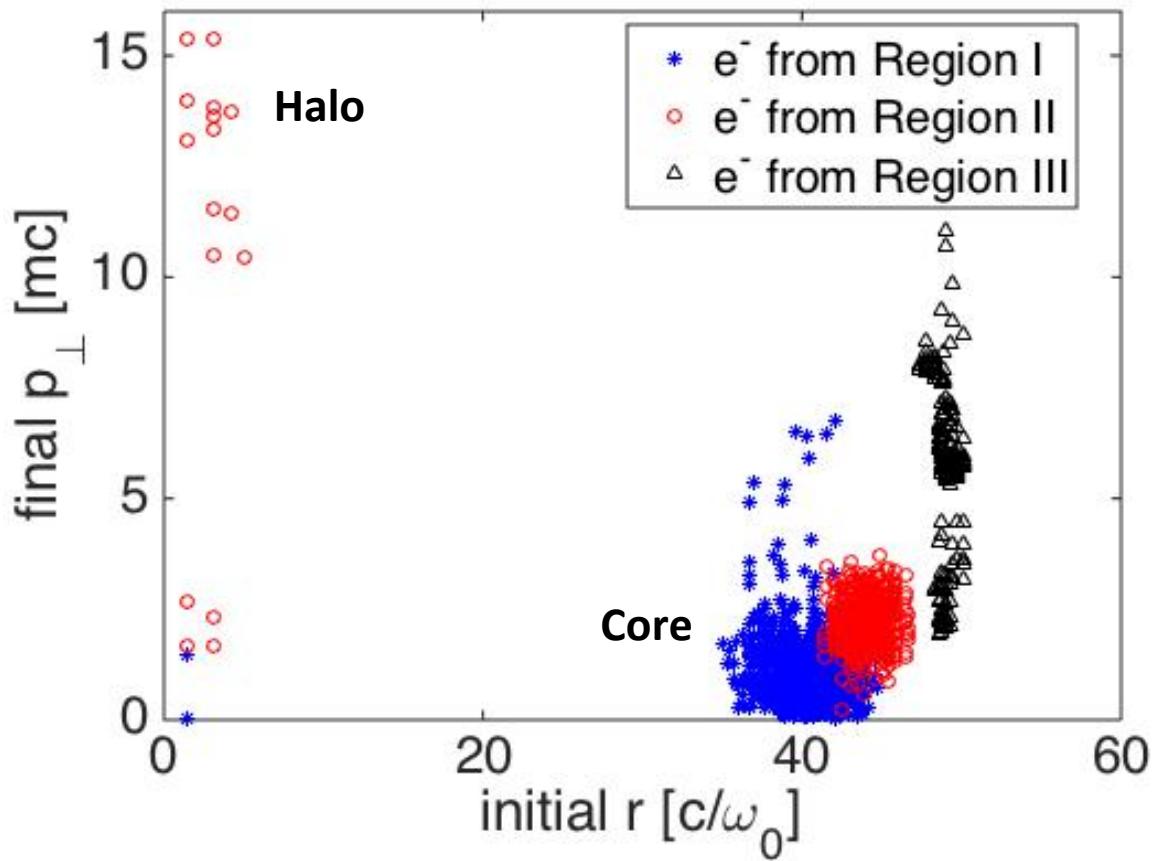
# Boosted Frame Results (cont'd)

- Trajectories of the injected particles



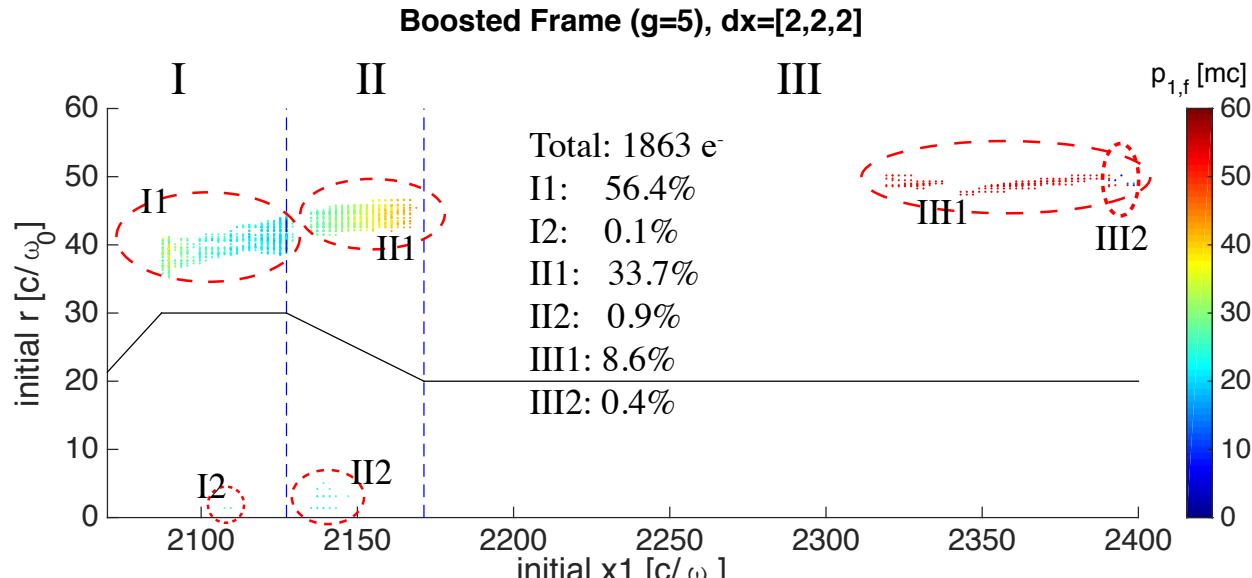
# Boosted Frame Results (cont'd)

- The relation between  $p_{\text{perp}}$  and the initial  $r$

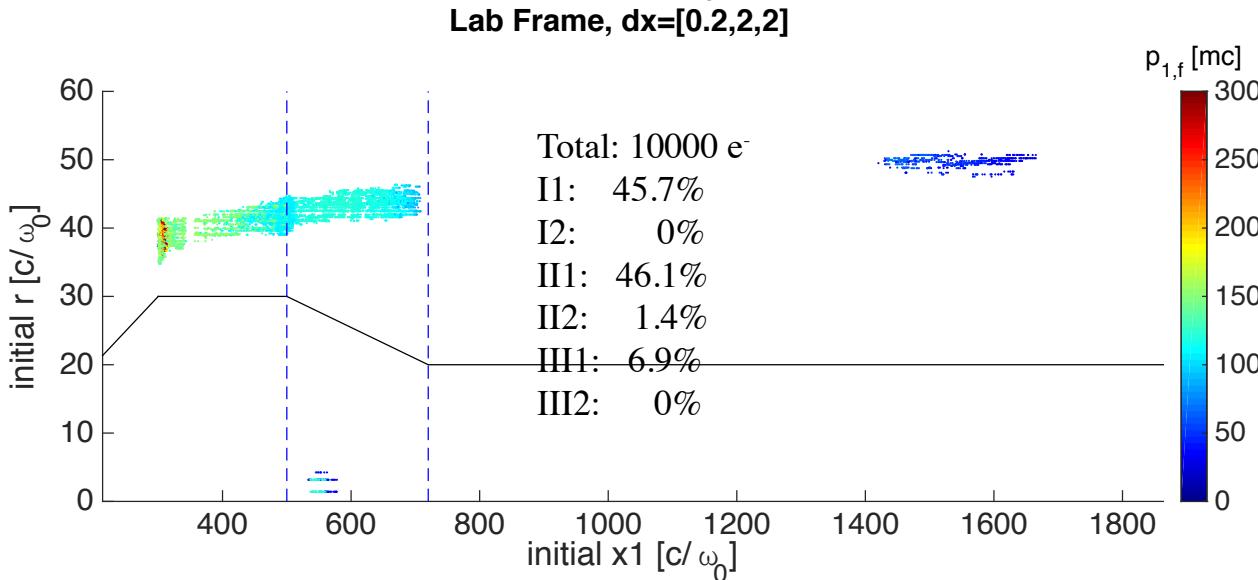


The unique and the importance of the transverse motion we revealed before in self-injections.

# Comparisons of Boosted and Lab

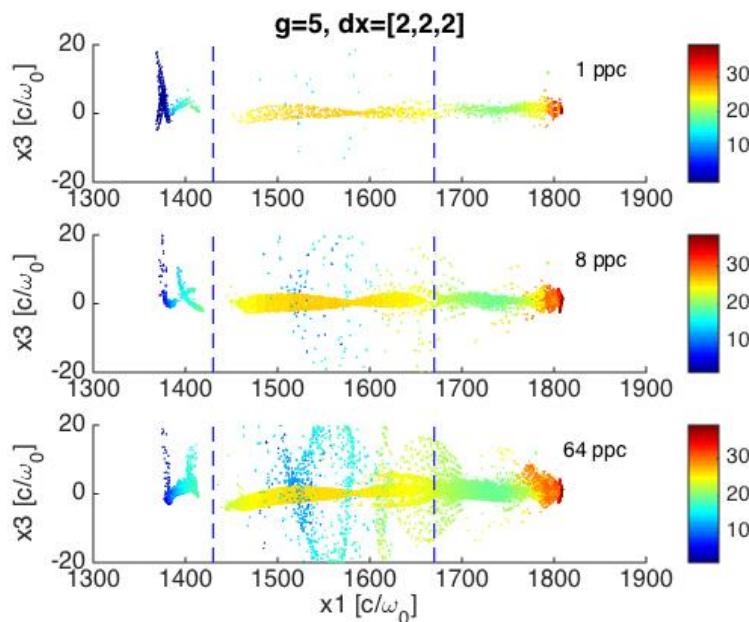
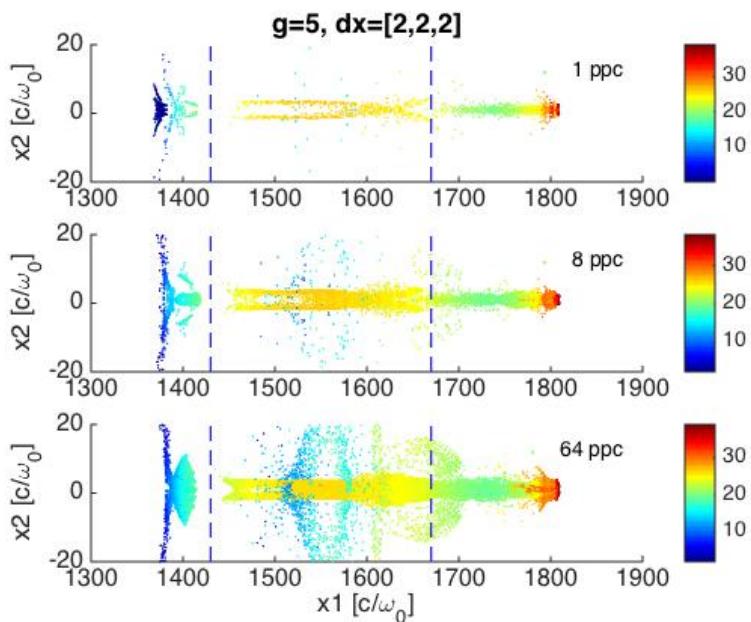


Looks Similar!



# Comparisons of Boosted and Lab (cont'd)

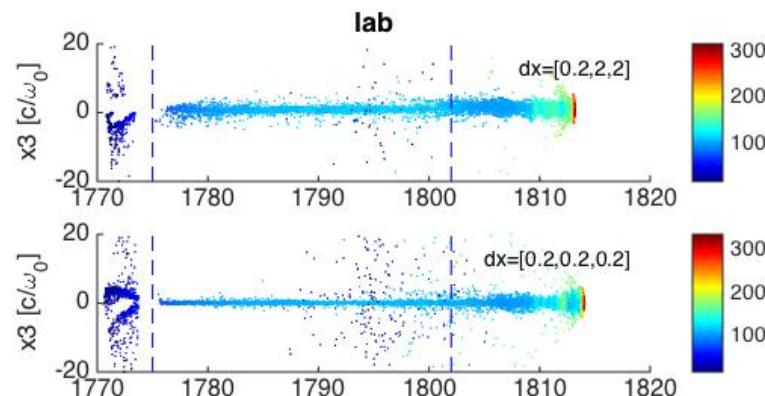
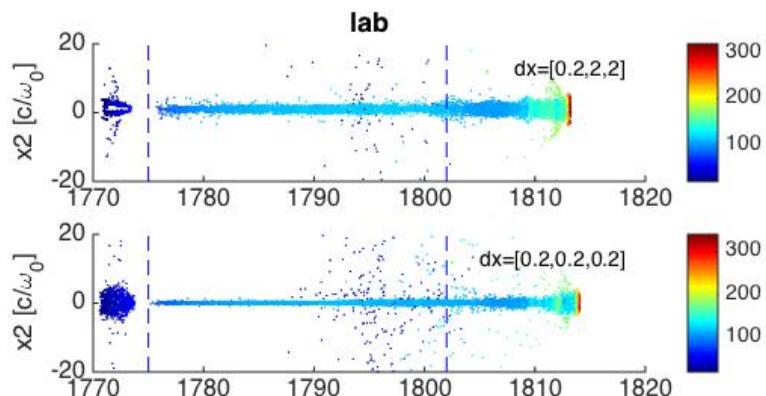
- Increasing the ppc in Boosted Frame Simulations



E. N. Nerush and I. Yu. Kostyukov, *Carrier-Envelope Phase Effects in Plasma-Based Electron Acceleration with Few-Cycle Laser Pulses*, PRL 103, 035001 (2009).

# Comparisons of Boosted and Lab (cont'd)

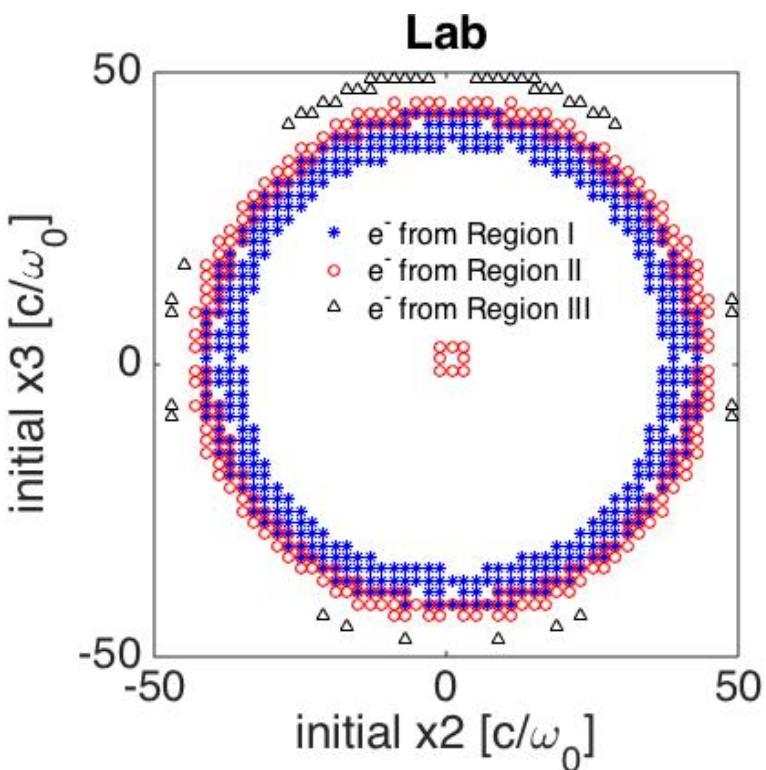
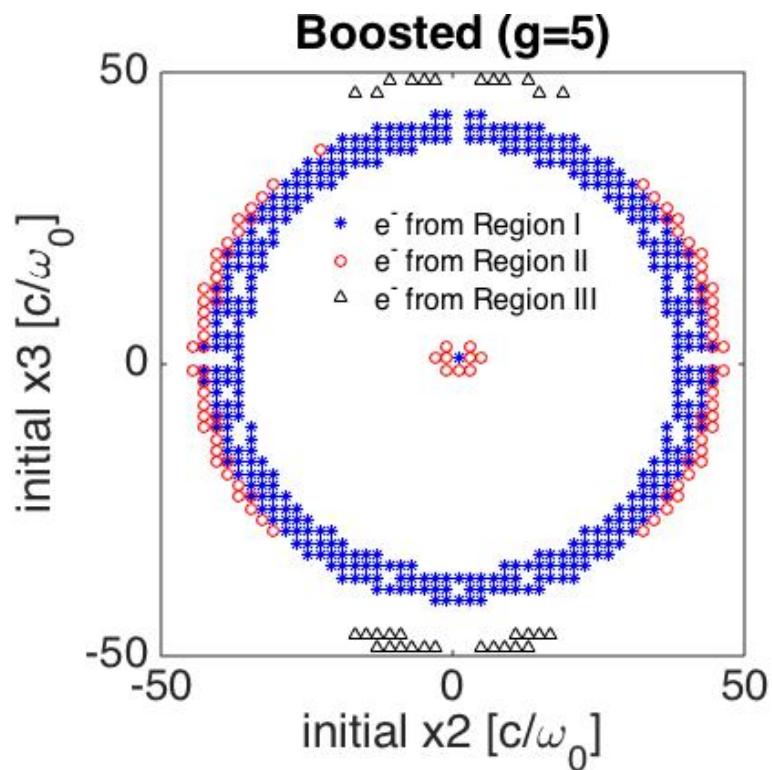
- Lab Frames Results



Less ‘Hosing’ phenomena is observed in the lab frame simulations.

# Comparisons of Boosted and Lab (cont'd)

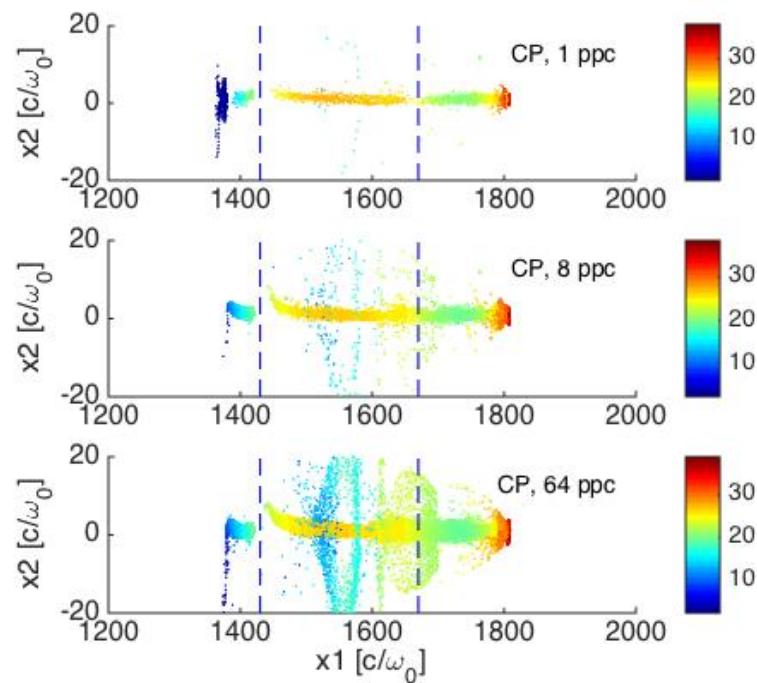
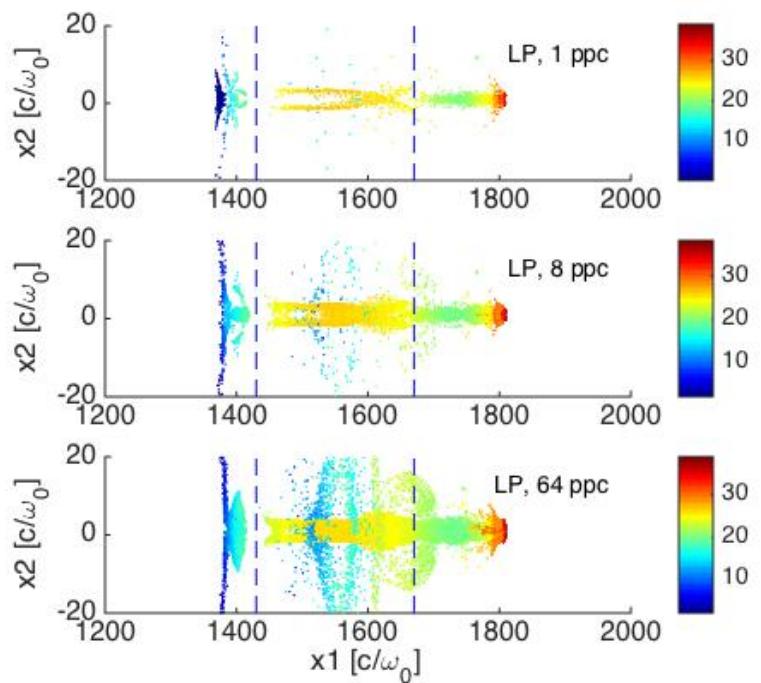
- Initial transverse positions



# Comparisons of Boosted and Lab (cont'd)

- LP  $\rightarrow$  CP

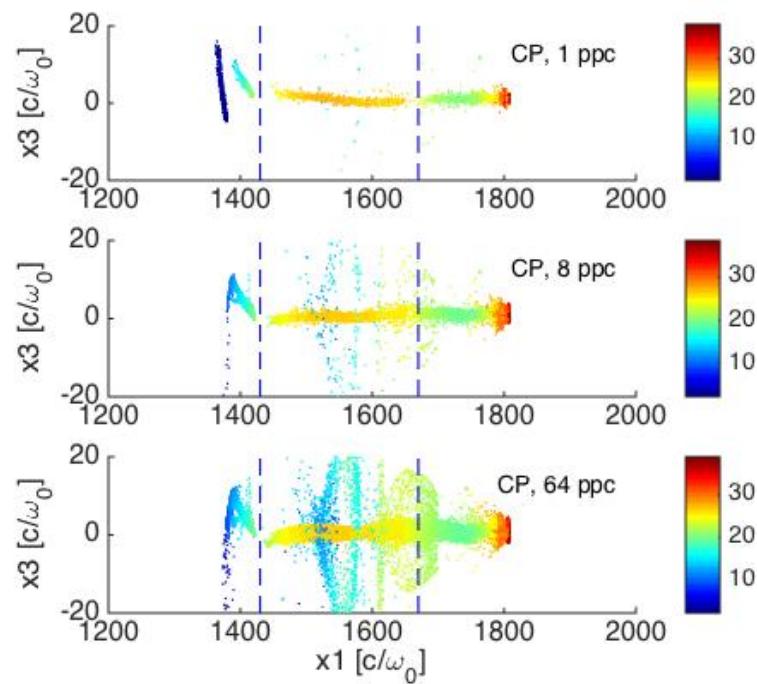
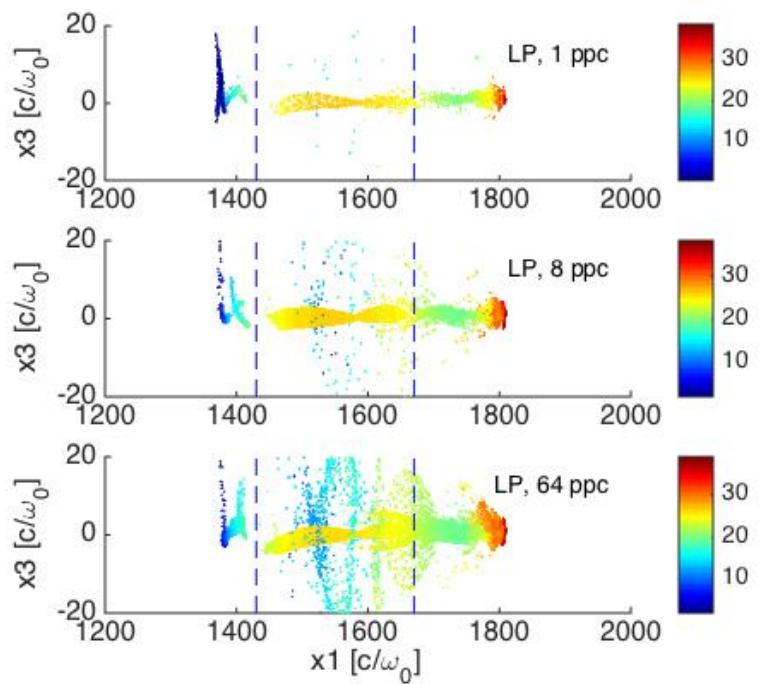
x1-x2 plane



# Comparisons of Boosted and Lab (cont'd)

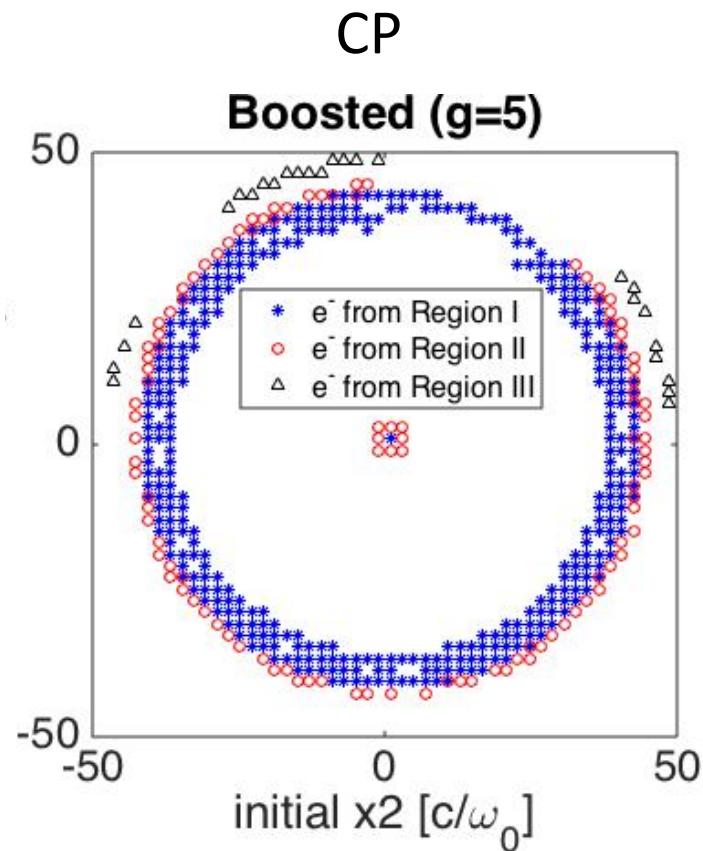
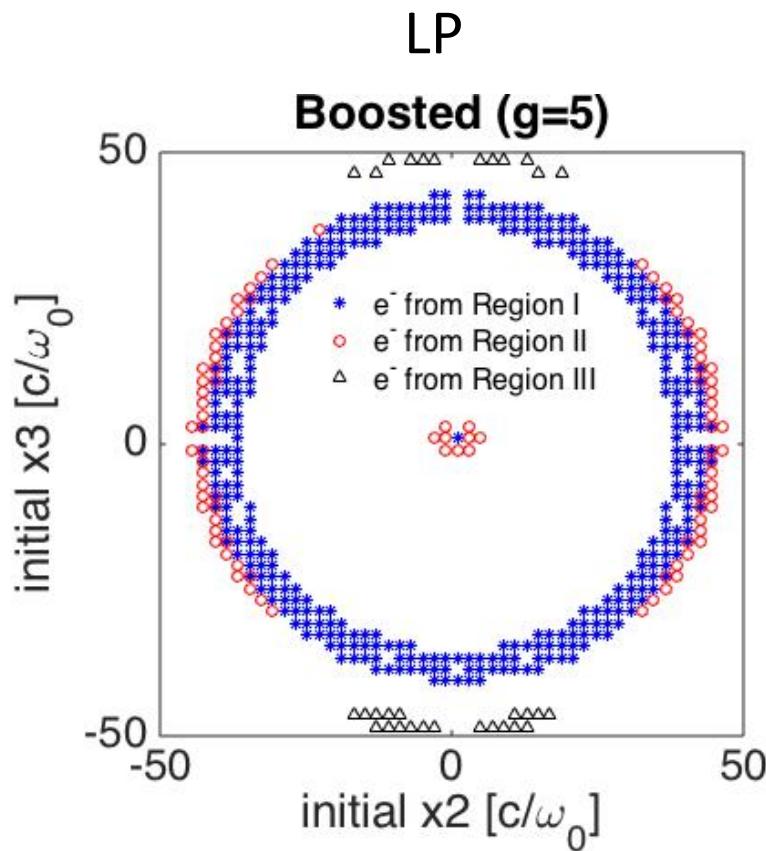
- LP  $\rightarrow$  CP

x1-x3 plane



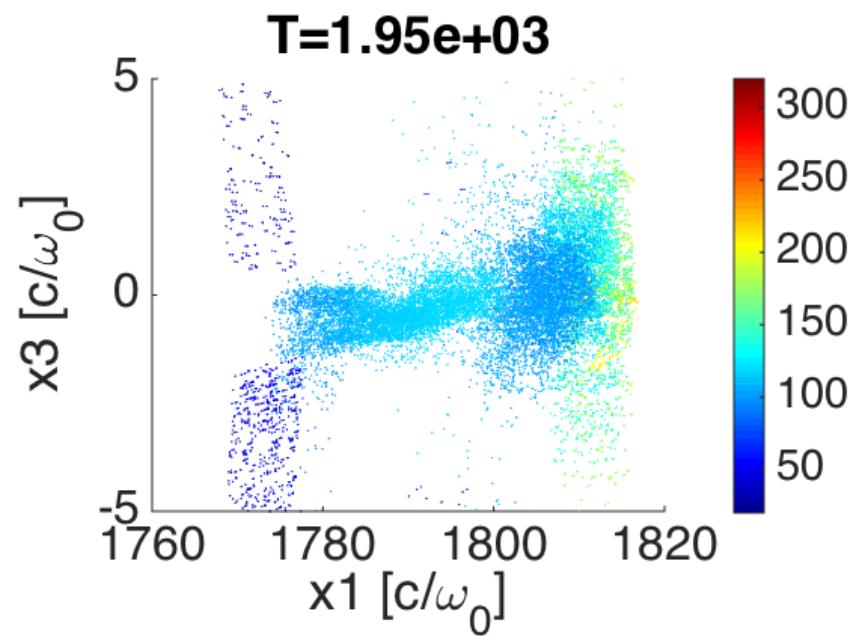
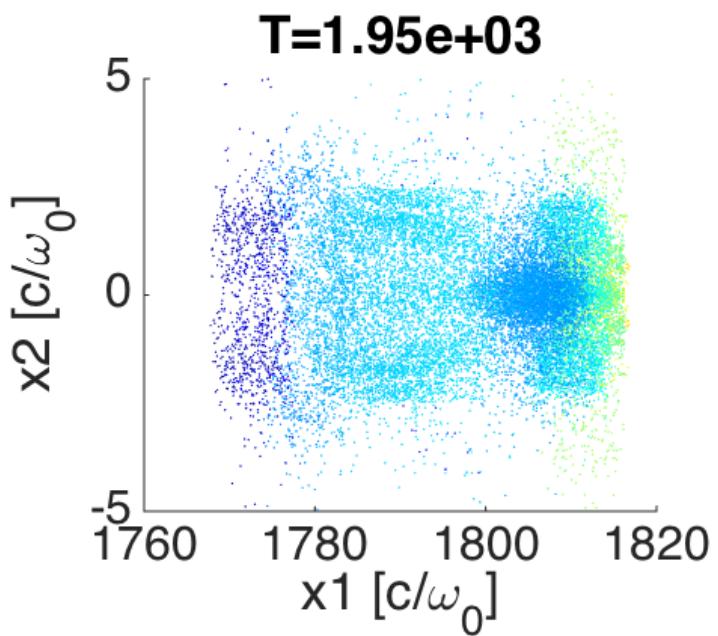
# Comparisons of Boosted and Lab (cont'd)

- LP  $\rightarrow$  CP: initial transverse positions



# Comparisons of Boosted and Lab (cont'd)

- Back to Lab: Boosted g=5, LP, 8 ppc



- Thanks!