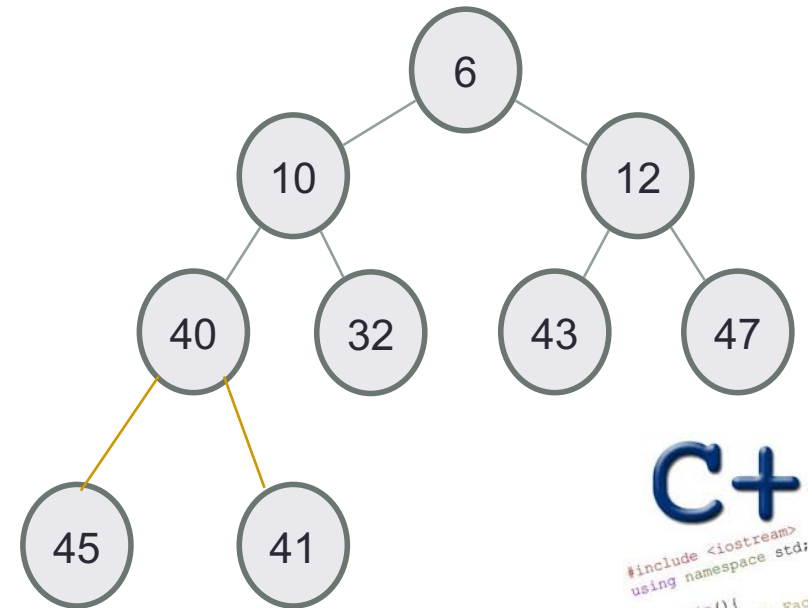
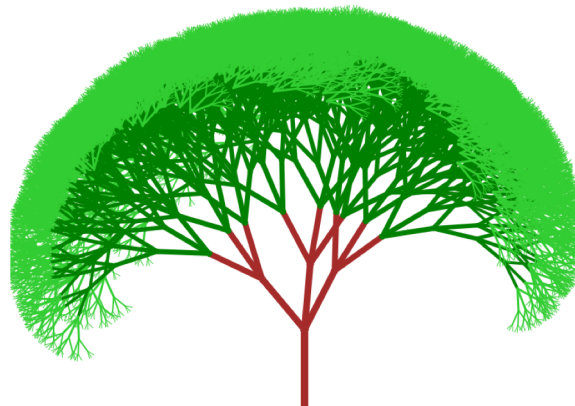


MORE ON RECURSION



Problem Solving with Computers-I



C++

```
#include <iostream>
using namespace std;

int main(){
    cout<<"Hola Facebook!";
    return 0;
}
```

**COMPUTER SCIENCE
UNDERGRADUATE AFFAIRS
COMMITTEE
*PRESENTS***



Speed Advising

Date: Friday, December 6, 2019

Location: 1132 Harold Frank Hall

Time: 10:00 AM - 1:00 PM

Refreshments will be provided

Final Exam: Monday 12/09, noon-3:00p,
Embarcadero Hall

Final Exam Review Session:

Day: Friday (12/06)
Time: 5:00p - 7:00p
Location: Phelps 3536

Thinking recursively !

```
int fac(int N) {  
    if (N <= 1) } Base case  
        return 1;  
  
    else{  
        int rest = fac(N-1) ; } Recursive case  
        return rest * N;  
    }
```

Human: Base case and 1 step

Computer: Everything else

Thinking recursively !

```
int fac(int N) {  
    if (N <= 1)  
        return 1;  
  
    else  
        return fac(N-1) * N;  
}
```

} Base case

} Recursive case
(shorter version)

Human: Base case and 1 step

Computer: Everything else

Behind the curtain...

```
int fac(int N) {  
    → if (N <= 1)  
        return 1;  
    else  
        return N * fac(N-1) ;  
}
```

```
cout<<fac(1) ;
```

Result: 1

The base case !

Behind the curtain...

```
int fac(int N) {  
    if (N <= 1)  
        return 1;  
    else  
        return N * fac(N-1) ;  
}  
  
fac(5)
```

Behind the curtain...

```
int fac(int N) {  
    if (N <= 1)  
        return 1;  
    else  
        return N * fac(N-1) ;  
}
```

fac(5)
└──────────┘
5 * fac(4)


```
int fac(int N) {
```

```
    if (N <= 1)  
        return 1;
```

```
    else  
        return N * fac(N-1);
```

```
}
```

Behind the curtain...

fac(5)

5 * fac(4)

4 * fac(3)

```
int fac(int N) {
```

```
    if (N <= 1)  
        return 1;
```

```
    else  
        return N * fac(N-1);
```

```
}
```

Behind the curtain...

fac(5)

5 * fac(4)

4 * fac(3)

3 * fac(2)

```
int fac(int N) {
```

```
    if (N <= 1)  
        return 1;
```

```
    else  
        return N * fac(N-1);
```

```
}
```

Behind the curtain...

fac(5)

5 * fac(4)

4 * fac(3)

3 * fac(2)

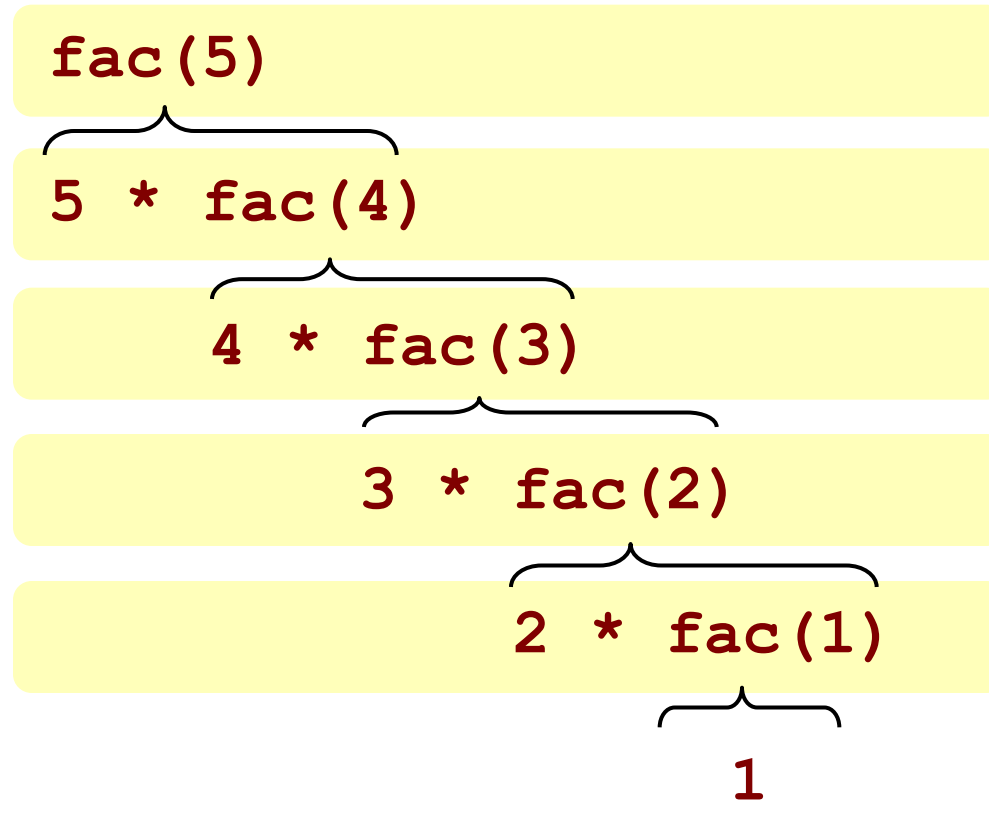
2 * fac(1)

```
int fac(int N) {  
    if (N <= 1)  
        return 1;  
    else  
        return N * fac(N-1);  
}
```

Behind the curtain...

"The Stack"

Remembers all of
the individual calls
to **fac**



```
int fac(int N) {
```

```
    if (N <= 1)  
        return 1;
```

```
    else  
        return N * fac(N-1);
```

```
}
```

Behind the curtain...

fac(5)

5 * fac(4)

4 * fac(3)

3 * fac(2)

2 * 1

```
int fac(int N) {
```

```
    if (N <= 1)  
        return 1;
```

```
    else  
        return N * fac(N-1);
```

```
}
```

Behind the curtain...

fac(5)

5 * fac(4)

4 * fac(3)

3 * 2

```
int fac(int N) {
```

```
    if (N <= 1)  
        return 1;
```

```
    else  
        return N * fac(N-1);
```

```
}
```

Behind the curtain...

fac(5)

5 * fac(4)

4 * 6

Behind the curtain...

```
int fac(int N) {  
    if (N <= 1)  
        return 1;  
    else  
        return N * fac(N-1) ;  
}
```

fac(5)
└──────────┘
5 * 24

Behind the curtain...

```
int fac(int N) {  
    if (N <= 1)  
        return 1;  
    else  
        return N * fac(N-1) ;  
}
```

fac(5)

Result: 120

Binary Search: Efficient search in a sorted array

- **Binary search.** Given `value` and sorted array `v[]`, find index `i` such that `v[i] == value`, or return `-1` indicating that no such index exists.
- **Invariant.** Algorithm maintains `v[lo] ≤ value ≤ v[hi]`.
- **Ex.** Binary search for 33.

[illegible]

Binary Search

- Ex. Binary search for 33.

6	13	14	25	33	43	51	53	64	72	84	93	95	96	97
0	1	2	3	4	5	6	7	8	9	10	11	12	13	14
↑							↑							↑
lo							mid							hi

Binary Search

- Ex. Binary search for 33.

6	13	14	25	33	43	51	53	64	72	84	93	95	96	97
0	1	2	3	4	5	6	7	8	9	10	11	12	13	14
↑						↑								
lo						hi								

Binary Search

- Ex. Binary search for 33.

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↑			↑			↑								
lo			mid			hi								

Binary Search

- Ex. Binary search for 33.

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				↑		↑								
				lo		hi								

Binary Search

- Ex. Binary search for 33.

6	13	14	25	33	43	51	53	64	72	84	93	95	96	97
0	1	2	3	4	5	6	7	8	9	10	11	12	13	14
				↑	↑	↑								
				lo	mid	hi								

Write the recursive implementation of Binary search

```
int binarySearch(int v[], int value, int lo, int hi);
```

Which of the following is a valid base case?

```
int binarySearch(int v[], int value, int lo, int hi){
```

A:

```
    if(hi<=lo){  
        return -1;  
    }
```

B:

```
    int mid = (lo + hi)/2;  
    if(v[mid] == value){  
        return mid;  
    }
```

C: Both A and B

Fill in the blanks

```
int binarySearch(int v[], int value, int lo, int hi){  
    if(hi < lo)  
        return -1;  
    int mid = (lo + hi)/2;  
    if(v[mid] == value)  
        return mid;  
    if(v[mid] < value){  
        binarySearch(v, value, _____, hi);  
    }  
}
```

A: lo
B: mid - 1
C: mid
D: mid + 1
E: hi

Searching a linked list

Given a linked list, implement a recursive search function

- Return true if a given value is present in the linked list
- Otherwise return false

Recursive function to free nodes in a linked list

Given a linked list, implement a recursive function to delete all the nodes in the linked list

Is this a correct implementation?

A: Yes

B: No

```
int binarySearch(int v[], int value, int lo, int hi){
    if(hi<lo)
        return -1;
    int mid = (lo + hi)/2;
    if(v[mid] == value)
        return mid;
    if(v[mid] < value){
        binarySearch(v, value, mid + 1, hi);
    }else{
        binarySearch(v, value, lo, mid - 1);
    }
}
```