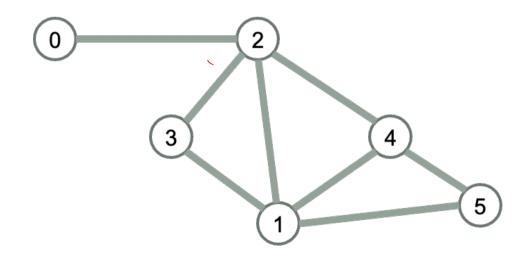
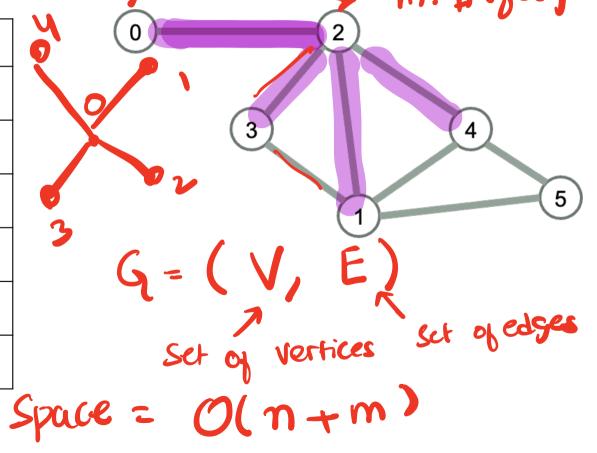
GRAPH SEARCH



Review: Adjacency list representation of graph

esentation of graph	N: # of neaple
	m: # gedges

Vertex	adjList
0	2
1	2,3,4,5
2	0/1/3/4
3	1,2
4	1,2,5
5	1,4



O(n)

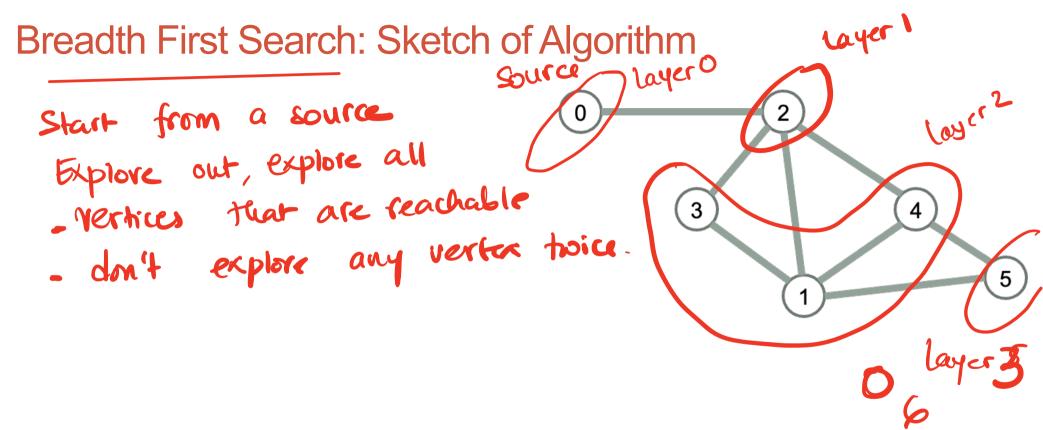
Which of these functions did you implement from last lecture's handout?

```
class graph{
  public:
    graph(int n = 0) \{ // n \text{ is the number of vertices } \}
       adjList = vector<list<int>>(n);
    void addEdge(int from, int to);
    bool hasEdge(int i, int j) const;
    vector<bool> bfs(int source) const;
    bool is ValidPath(const vector<int> & path) const; // returns true if the input path exists
    bool isReachable(int source, int dest) const; // returns true if a path exists from source to dest
  private:
     vector<list<int>> adiList;
```

E: All of them!

};

Link to hand out: https://bit.ly/CS24F23GraphsHandout



- In general, a search algorithm would explore (or "visit") from a source vertex
 all the vertices reachable ,
 - never exploring out from the same vertex twice
- How does the BFS algorithm ensure this?

BFS Traverse: Time Complexity (express in terms of n, m)

```
Input: Graph G = (V, E), source vertex s, Let n = |V|, m = |E|
 Start at source s; O(1)
 Mark all the vertices as "not visited" o(n)
 Mark s as visited 0(1)
 push s into a queue (1)
 while the queue is not empty: (n times)
                                                  What is the time complexity of BFS?
                                                  A. O(n)
   - pop the vertex u from the front of the queue
                                                  B. O(m)
      for each of u's neighbor (v)
                                                  C.O(n + m)
       - If v has not yet been visited (v):
                                                   D. O(n^2)
Mark v as visited the number Push v in the queue
                                                   E. None of the above O(n.m)
- How many times does the while loop run? n times
```

- How many times do we check if a vertex has been visited?

BFS Traverse: Time Complexity (express in terms of n, m)

```
Input: Graph G = (V, E), source vertex s, Let n = |V|, m = |E|
Start at source s:
                                          (0)
Mark all the vertices as "not visited"
Mark s as visited
push s into a queue
                                                   O(n) for the whole program
while the queue is not empty:
     - If v has not yet been visited (v): O(m) is run time for the Mark v as visited

• Push v in the queue
 - pop the vertex u from the front of the queue
  - for each of u's neighbor(v)

    Mark v as visited
```

- How many times does the while loop run?
- How many times do we check if a vertex has been visited?

BFS Traverse: Space Complexity (express in terms of n, m)

Input: Graph G = (V, E), source vertex s, Let n = |V|, m = |E| Start at source s; Mark all the vertices as "not visited" Mark s as visited push s into a queue while the queue is not empty: - pop the vertex u from the front of the queue

- for each of *u*'s neighbor (v)
 - If v has not yet been visited (v):
 - Mark v as visited
 - Push *v* in the queue



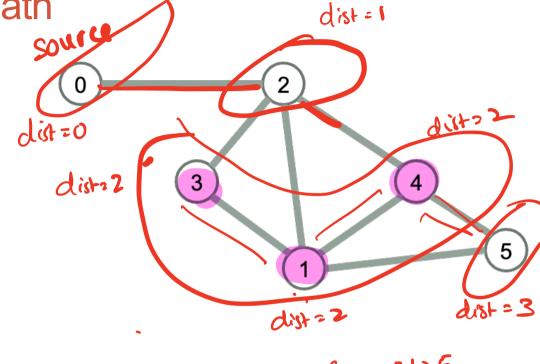
What is the space complexity of BFS?

- B. O(m)
- C. O(n + m)
- D. O(n²)
- E. None of the above

- Space complexity: Peak (additional) space usage expressed as big O

Application of BFS: shortest path

			1
Vertex	dist	prev	adjList
0 (source)	0		2
1	2	2	2, 3, 4, 5
2	1	(0)	0, 1, 3, 4
3	2	2	1, 2
4	2	(2)	1, 2, 5
5	3	4	1, 4
$\Omega \setminus A$			45



dist(5): Shortest distance from 0+35 Shortest path: 0,2,4,5

Goal. Compute dist(v): fewest number of edges from the path from vertex s to v

BFS Shortest Path

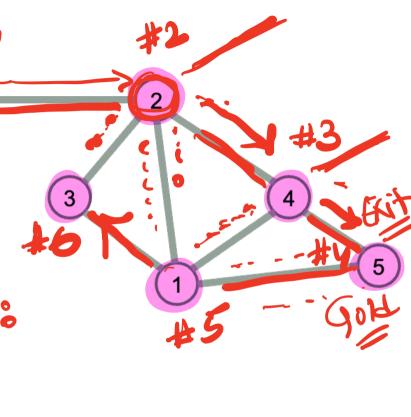
```
Input: Graph G = (V, E), source vertex s, Let n = |V|, m = |E|
Start at source s;
Mark all the vertices as "not visited", dist(i) = \begin{cases} 0 \\ 0 \end{cases}, otherwise
Mark s as visited
push s into a queue in thicking the previous vector. Is all -1 while the queue is not empty:
```

- pop the vertex *u* from the front of the queue
 - for each of *u*'s neighbor (v)
 - If v has not yet been visited (v):
 - Mark v as visited
 - Push v in the queue dist (v) = 1 + dist(u)Per (v) = u

- Modify BFS to compute the shortest path from source s to all other vertices

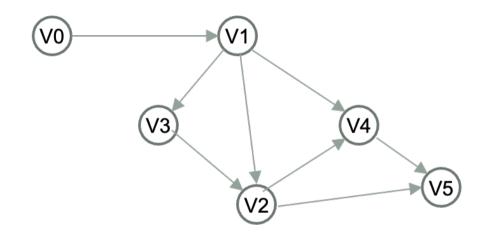
Depth First Search

Search as far down a single path as possible, backtrack as needed



Depth First Search

Search as far down a single path as possible, backtrack as needed



Assuming DFS chooses the lower number node to explore first, in what order does DFS visit the nodes in this graph?

A. V0, V1, V2, V3, V4, V5

B. V0, V1, V3, V4, V2, V5

C) V0, V1, V3, V2, V4, V5

D. V0, V1, V2, V4, V5, V3

Work to complete your handout

```
class graph{
  public:
    graph(int n = 0) \{ // n \text{ is the number of vertices } \}
       adiList = vector<list<int>>(n):
    void addEdge(int from, int to);
    bool hasEdge(int i, int j) const;
    vector<book> bfs(int source) const;
    bool is ValidPath(const vector<int> & path) const; // returns true if the input path exists
    bool isReachable(int source, int dest) const; // returns true if a path exists from source to dest
    // (New!) Implement a variation of BFS to compute the shortest path from a
              source vertex to all vertices reachable from it
    // (New!) Implement depth-first search
   private:
    vector<list<int>> adiList;
                                             Link to hand out: https://bit.ly/CS24-Graph-SearchHandout
```