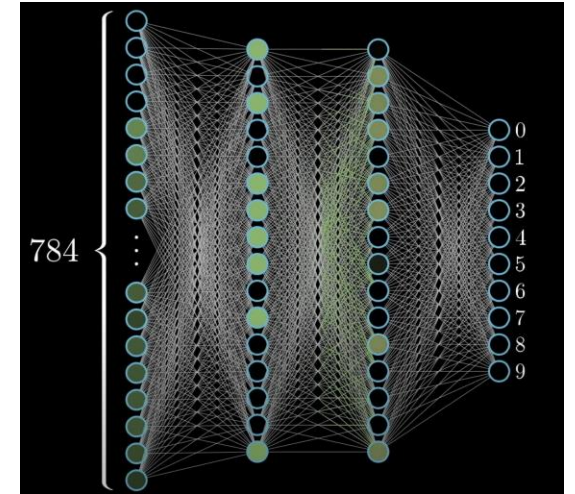


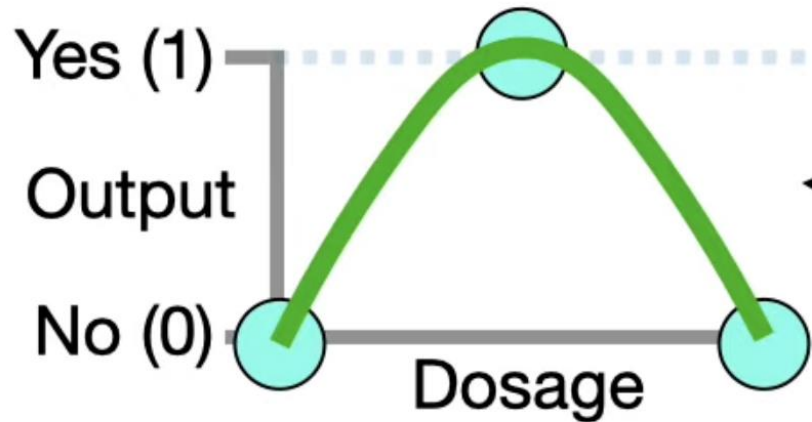
Link to handout: <https://bit.ly/NN-DFS-Backprop>



PA03: DFS BACKPROP

COMPLEXITY ANALYSIS OF OF GRAPH SEARCH

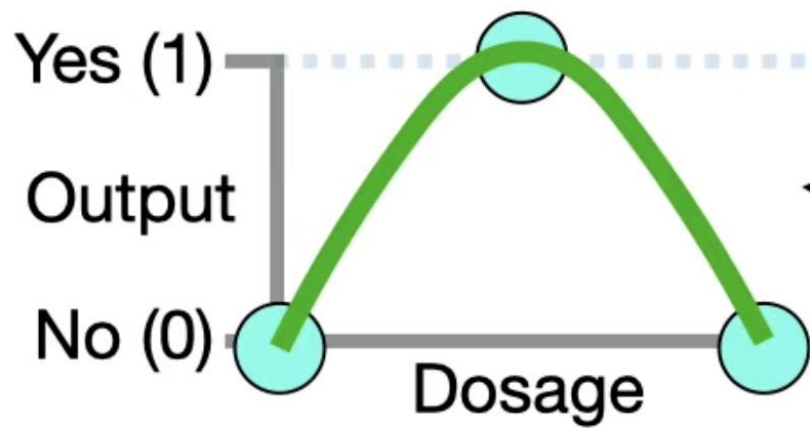
Neural Net to predict effectiveness of a drug



Draw the neural network that was used to predict whether a drug's dosage is effective against a virus.

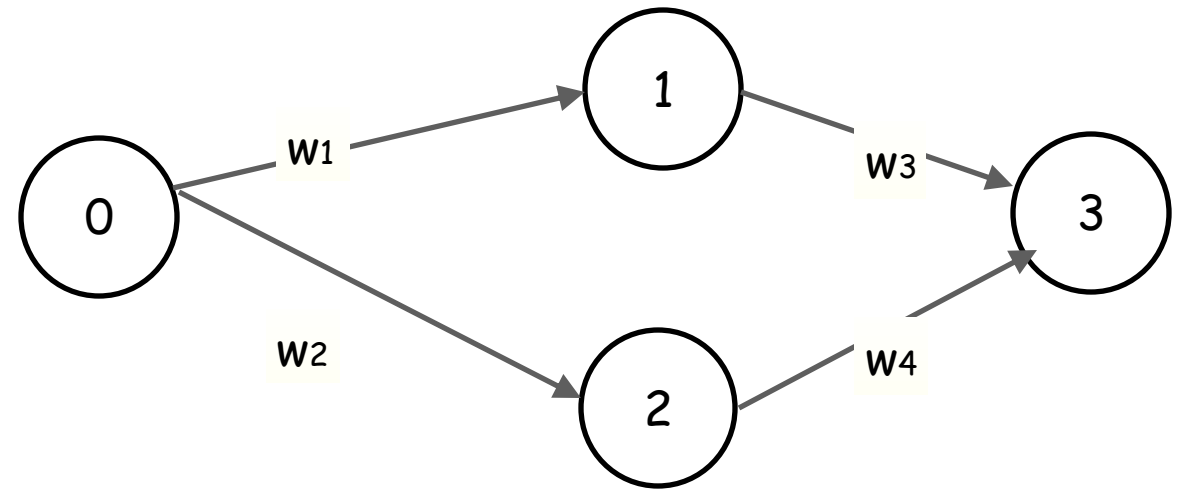
How many parameters does the NN have?

What is “training” the neural net?

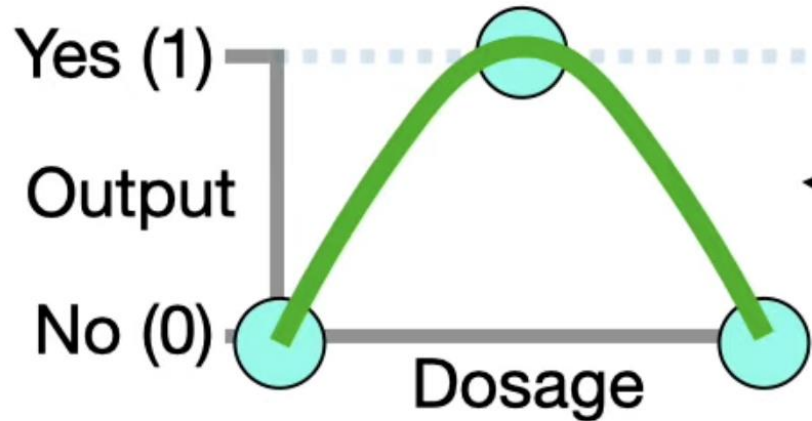


Training a neural net means adjusting its parameters (weights and biases) so it learns to map inputs to the correct outputs.

Show the neural net different example inputs and outputs

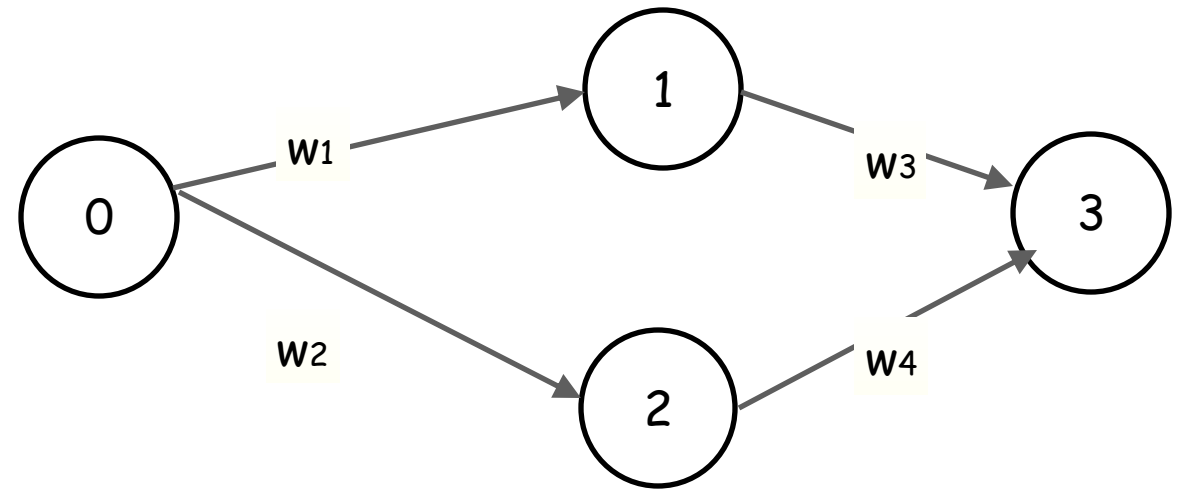


Backpropagation = smart feedback

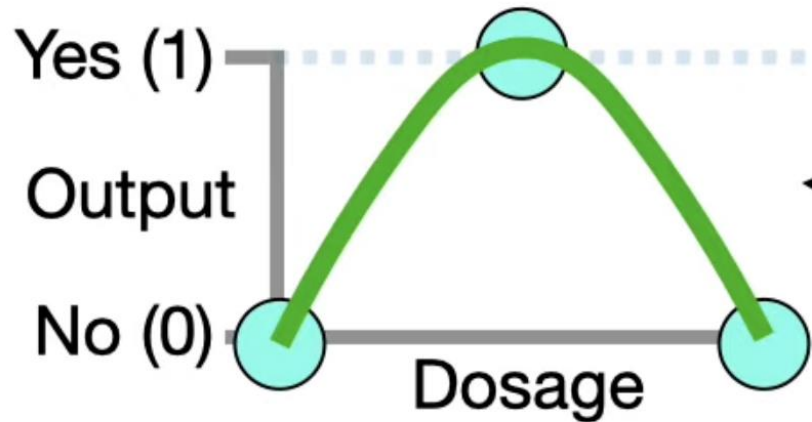


Backprop: Guiding feedback that tells each weight and bias how to slightly nudge to reduce the error.

In PA03, that feedback is abstracted into a call to `contribute(node, y, p)`



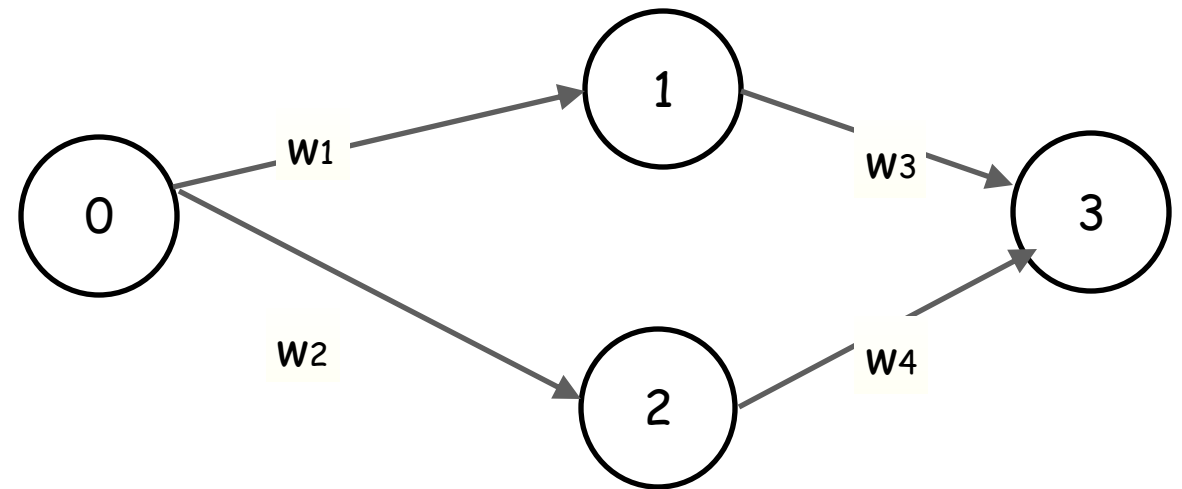
Backpropagation: PA03 contribute()



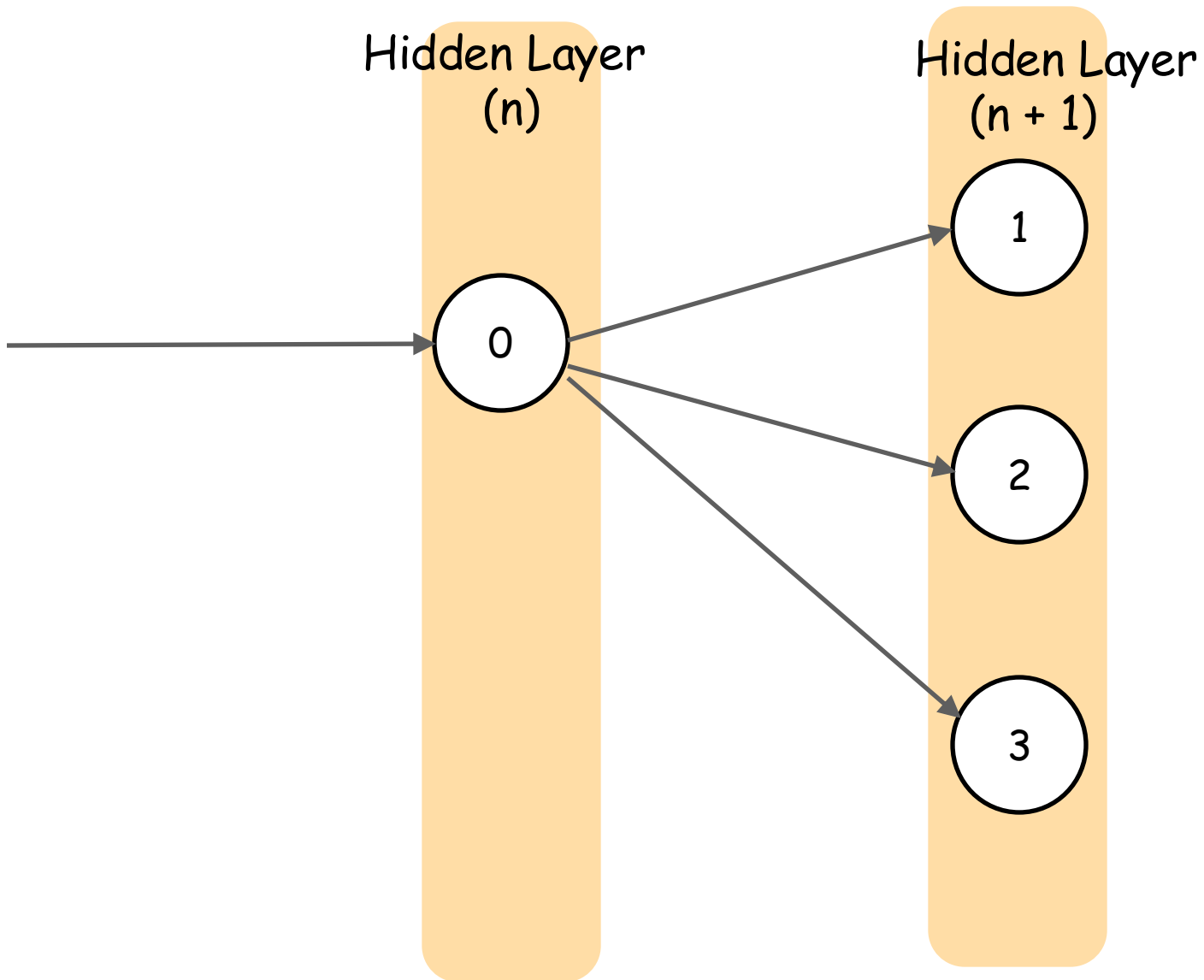
Node 3's contribution = Nudge to node 3's bias

Contributions in one layer are used to compute the contributions in the previous layer

Node 3's outgoing contribution is used to compute the contributions of which nodes?



Backpropagation: Order of operations for one node



Backprop using DFS (you need to implement)

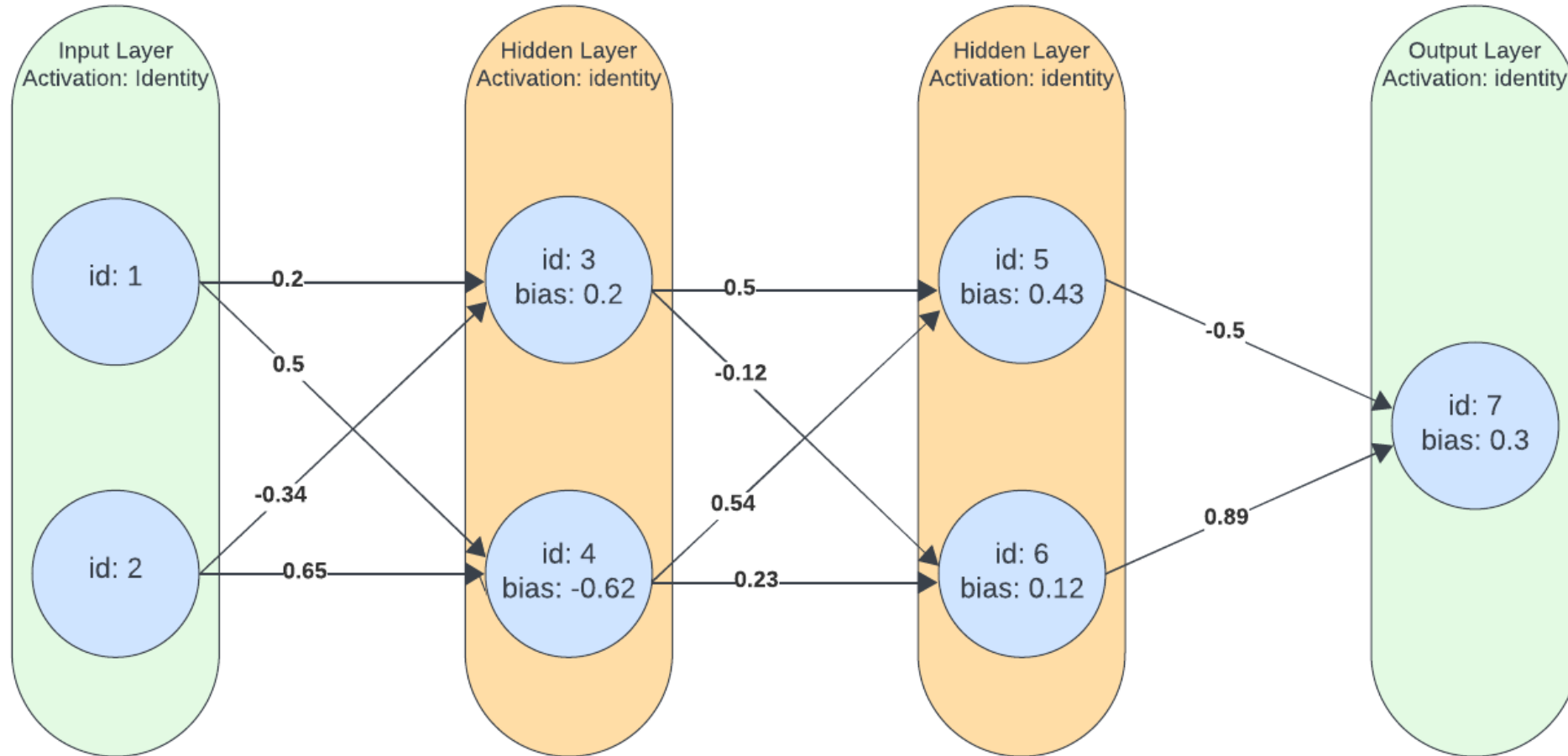
```
contribute(int nodeId,  
           const double& y,  
           const double& p)
```

Helper visit functions that do the math for you:

```
visitContributeNeighbor(  
    Connection& c,  
    double& incomingContribution,  
    double& outgoingContribution)
```

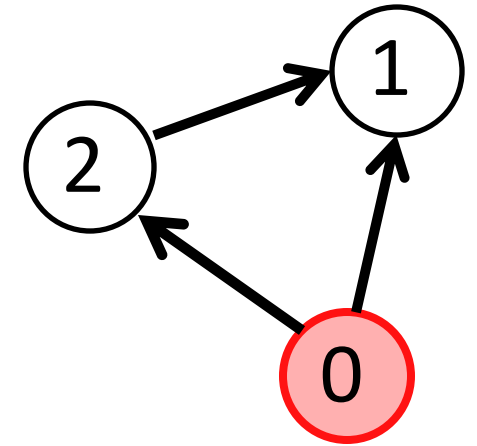
```
visitContributeNode(  
    int vId,  
    double& outgoingContribution)
```

PA03: Backpropagation data flow



Trace the order in which **contribute(...)**, **visitContributeNode (...)**, and **visitContributeNeighbor(...)** are called. For each node, write down: when it's visited, what contributions it receives, and when those are passed on to others.

BFS: Running Time Complexity



Algo exploreBFS (Graph G , vertex s):

- Mark all the vertices as “not visited”
- Mark s as visited
- push s into a queue
- while the queue is not empty:
 - pop the vertex u from the front of the queue
 - for each of u 's neighbor (v)
 - If v has not yet been visited:
 - Mark v as visited
 - Push v in the queue

n : number of vertices

m : number of edges

How many times does the while loop run?

A. n

B. m

C. $n + m$

D. nm

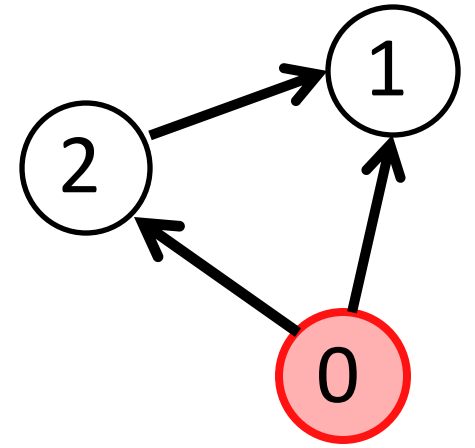
E. None of the above

BFS: Running Time Complexity

Algo exploreBFS (Graph G , vertex s):

For each iteration of the while loop, the for loop runs a variable number of times. How should we proceed to analyze the Big-O running time?

- while the queue is not empty:
 - pop the vertex u from the front of the queue
 - for each of u 's neighbor (v):
 - If v has not yet been visited:
 - Mark v as visited
 - Push v in the queue



A. Bound the maximum number of times the for loop runs **per iteration** of the while loop

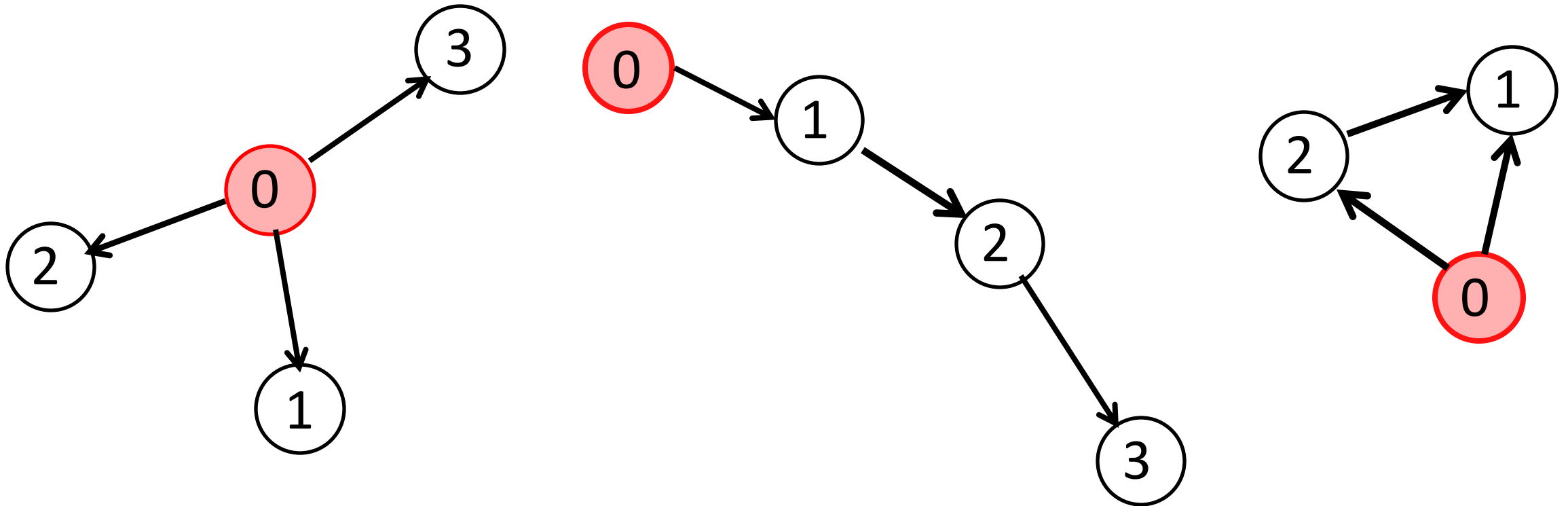
B. Compute the total number of times the for loop runs over **the entire run of exploreBFS**

C. Cannot compute Big-O because running time depends on two parameters (n, m)

BFS: Running Time Complexity

(A) The total number of times the for loop runs over **the entire run of exploreBFS**

(B) The total number of times each neighbor (u) is checked for all vertices over **the entire run of exploreBFS**



BFS: Time Complexity

Algo exploreBFS (Graph G , vertex s):

- Mark all the vertices as “not visited”
- Mark s as visited
- push s into a queue
- while the queue is not empty:
 - pop the vertex u from the front of the queue
 - for each of u 's neighbor (v)
 - If v has not yet been visited:
 - Mark v as visited
 - Push v in the queue

n : number of vertices
 m : number of edges

What is the time complexity of exploreBFS?

- A. $O(n)$
- B. $O(m)$
- C. $O(n + m)$
- D. $O(nm)$
- E. None of the above

BFS Traverse: Space Complexity

Algo exploreBFS (Graph G , vertex s):

- Mark all the vertices as “not visited”
- Mark s as visited
- push s into a queue
- while the queue is not empty:
 - pop the vertex u from the front of the queue
 - for each of u 's neighbor (v)
 - If v has not yet been visited:
 - Mark v as visited
 - Push v in the queue

n : number of vertices
 m : number of edges

What is the Big -O
auxiliary space
complexity of
exploreBFS?

- A. $O(n)$
- B. $O(m)$
- C. $O(n + m)$
- D. $O(n^2)$
- E. None of the above

- Auxiliary Space complexity: Additional space usage (not including input and output)

exploreDFS: Time Complexity

```
exploreDFS(v)
```

```
    v.visited ← true
```

```
    For each edge (v, w):
```

```
        If not w.visited
```

```
            exploreDFS(w)
```

n: number of vertices
m: number of edges

What is the time complexity of exploreDFS?

- A. $O(n)$
- B. $O(m)$
- C. $O(n + m)$
- D. $O(n^2)$
- E. None of the above

exploreDFS: Space Complexity

```
exploreDFS (v)

    v.visited ← true

    For each edge (v,w)

        If not w.visited

            exploreDFS (w)
```

n: number of vertices
m: number of edges

What is the worst-case space complexity of exploreDFS?

- A. $O(n)$
- B. $O(m)$
- C. $O(n + m)$
- D. $O(n^2 + n.m)$
- E. None of the above