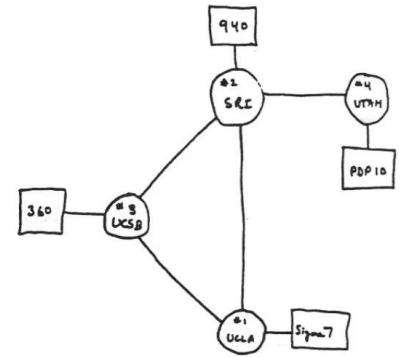
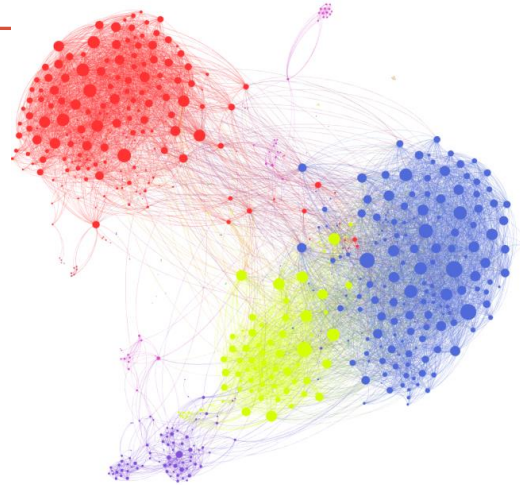
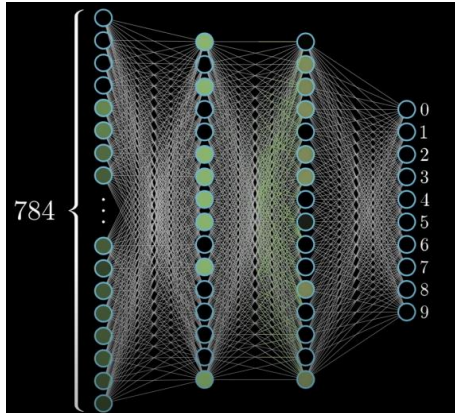


Handout: <https://bit.ly/GraphSearch-BFS-DFS>

# GRAPH SEARCH – BFS & DFS

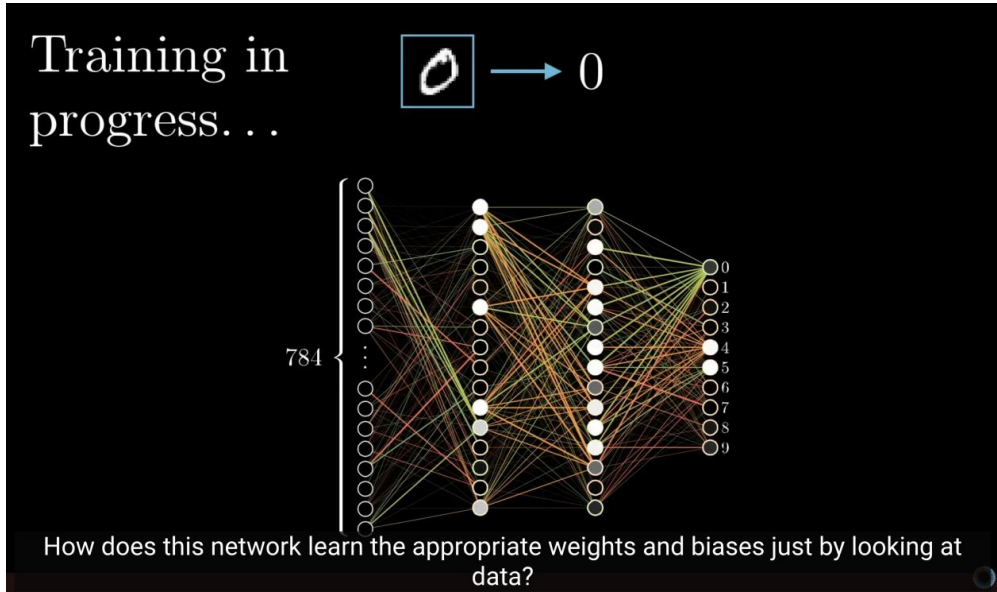


THE ARPA NETWORK

DEC 1969

4 NODES

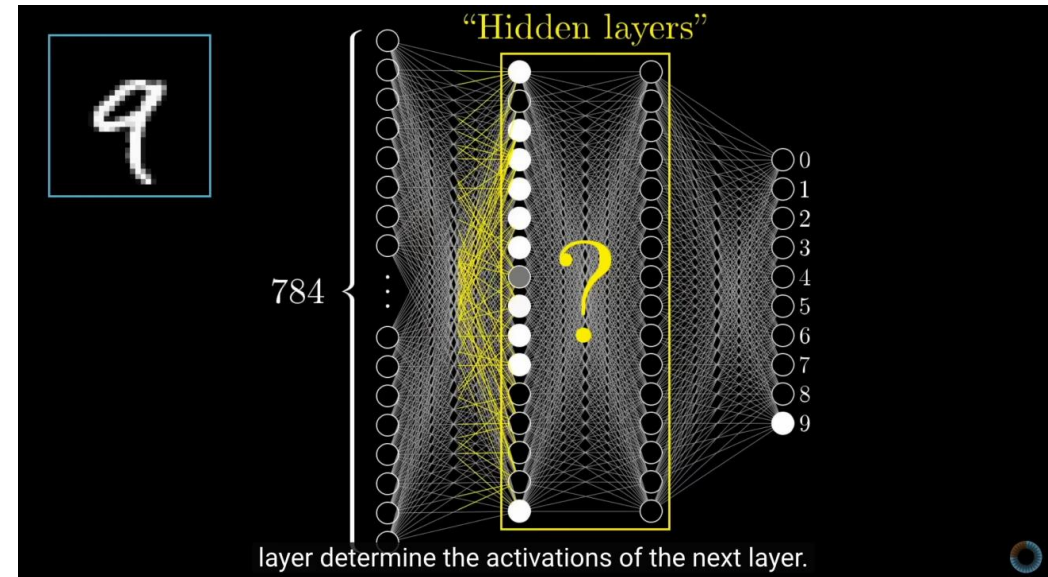
# How does information flow in a Neural Network ?



## Training

Learn network parameters  
(all the weights and biases)

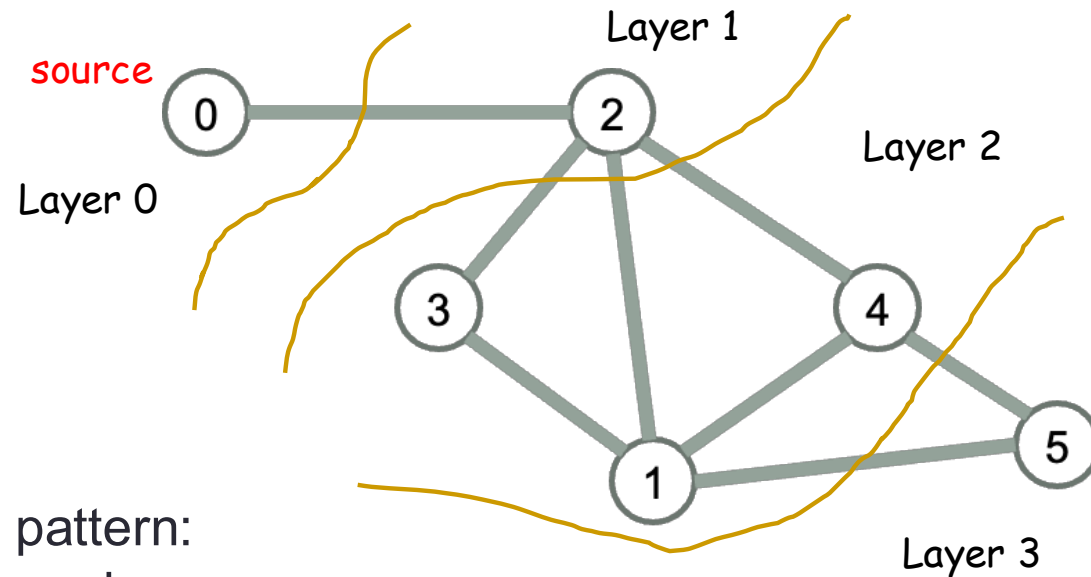
Credits: [3Blue1Brown](#)



## Evaluation/Prediction

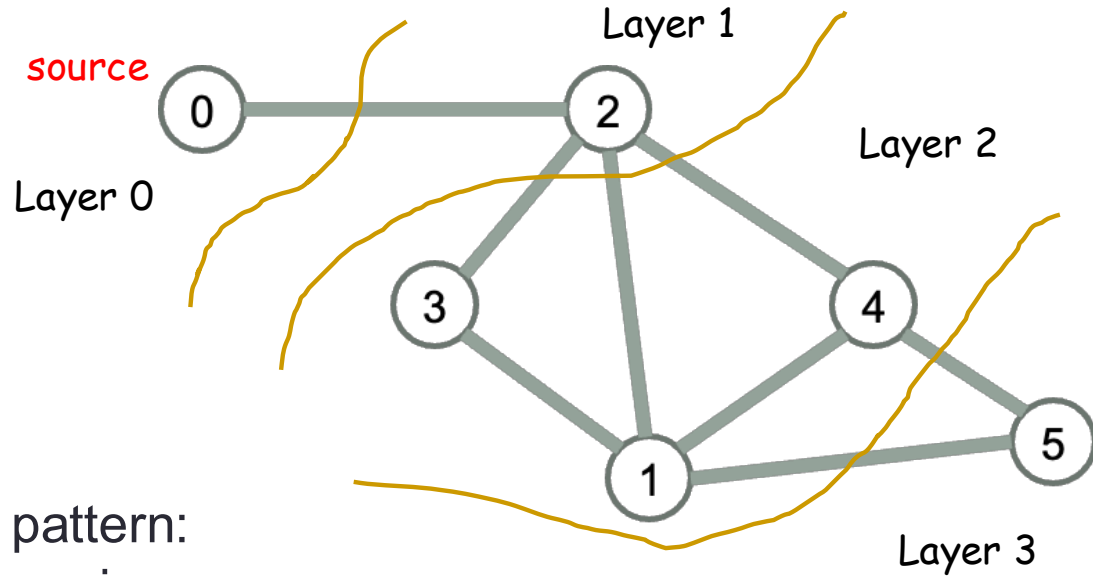
Activations in one layer determine  
activations in the next layer

# Breadth First Traversal: Sketch of Algorithm



Explore the graph in a wave (layered) pattern: explore all the vertices reachable from a given vertex before exploring their neighbors.

# Breadth First Traversal: Sketch of Algorithm



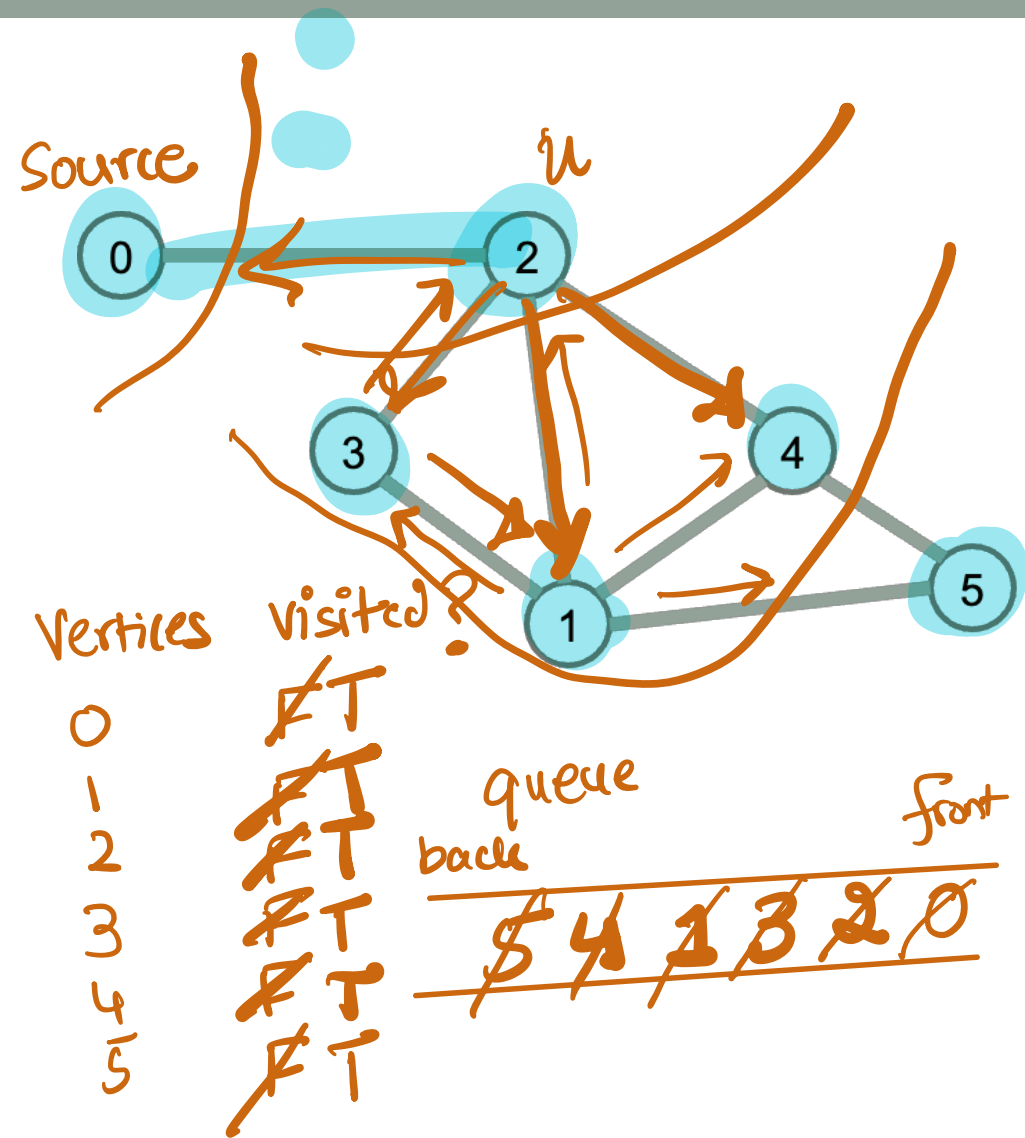
Explore the graph in a wave (layered) pattern:  
explore all the vertices reachable from a given  
vertex before exploring their neighbors.

- In general, a search algorithm would explore (or “visit”) from a source vertex
  - all the vertices reachable ,
  - never exploring out from the same vertex twice
- How does the Breadth First Search/Traversal algorithm ensure this?

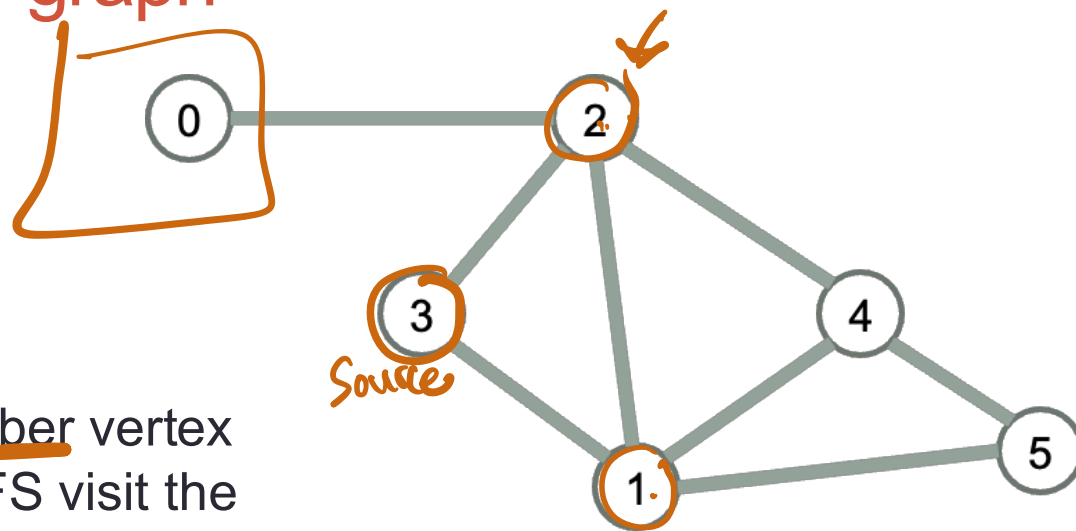
# Breadth First Algorithm

- Algo exploreBFS (Graph G, vertex  $s$ ):
- Mark all the vertices as "not visited"
  - Mark  $s$  as visited
  - push  $s$  into a queue
  - while the queue is not empty:
    - pop the vertex  $u$  from the front of the queue
    - for each of  $u$ 's neighbor ( $v$ )
      - If  $v$  has not yet been visited:
        - Mark  $v$  as visited
        - Push  $v$  in the queue

0 2 3 1 4 5



## Trace BFS for the example graph

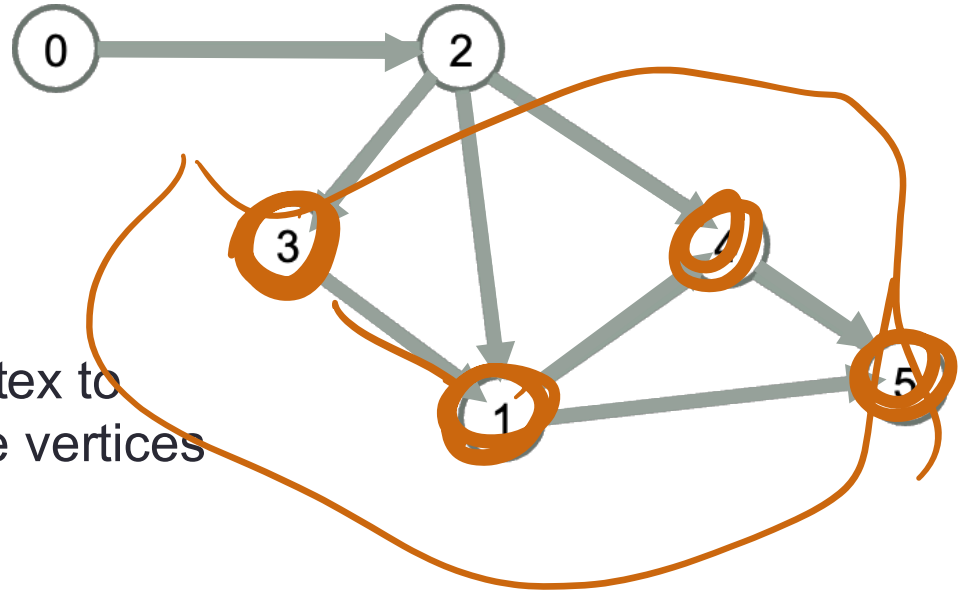


Assume BFS chooses the lower number vertex to explore first, in what order does BFS visit the nodes in this graph starting at **source vertex 3**.

- A. 0, 1, 2, 3, 4, 5
- B. 0, 1, 3, 2, 4, 5
- C. 3, 2, 0, 1, 4, 5 X
- D. 3, 1, 2, 0, 4, 5
- ☒ E. Something else

3, 2, 1, 0, 4, 5  
3, 1, 2, 4, 5, 0

## Trace BFS (different source vertex)



**What if edges were directed as shown?**

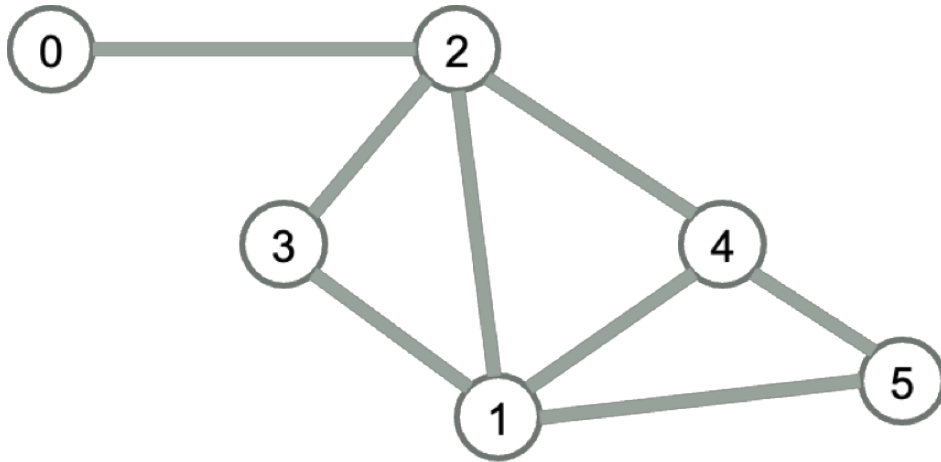
Assume BFS chooses the lower number vertex to explore first, in what order does BFS visit the vertices in this graph starting at **source vertex 3**.

- A. 0, 1, 2, 3, 4, 5
- B. 0, 1, 3, 2, 4, 5
- C. 3, 2, 0, 1, 4, 5
- D. 3, 1, 2, 0, 4, 5
- ☒ E. Something else

# Graph search: general approach

Keep track of all areas discovered

While there is an unexplored path, follow path



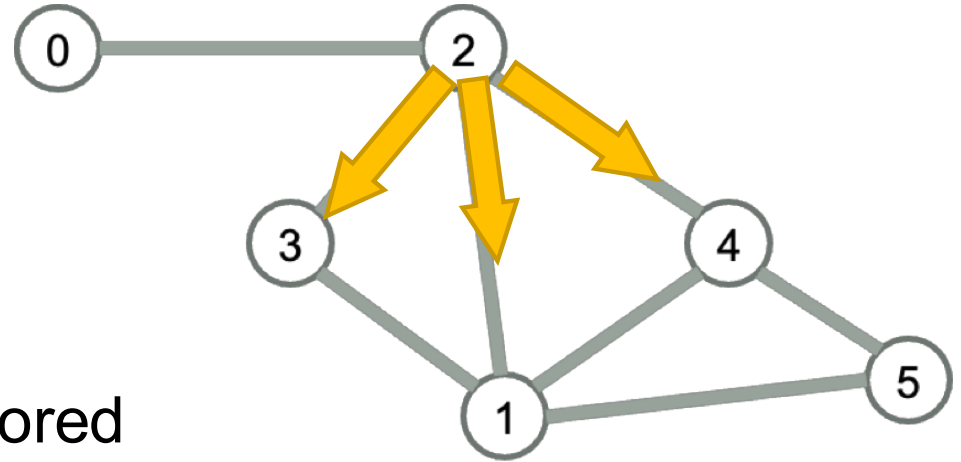


# Systematize the Search with DFS

**Depth-First Search** explores a graph by following one branch as far as it can go before backtracking. It uses a stack (explicit or via recursion) to remember where to return.

Need to keep track of:

- Which vertices discovered
- Which edges have yet to be explored



# Explore – Depth First

**exploreDFS**(v)

v.visited  $\leftarrow$  true

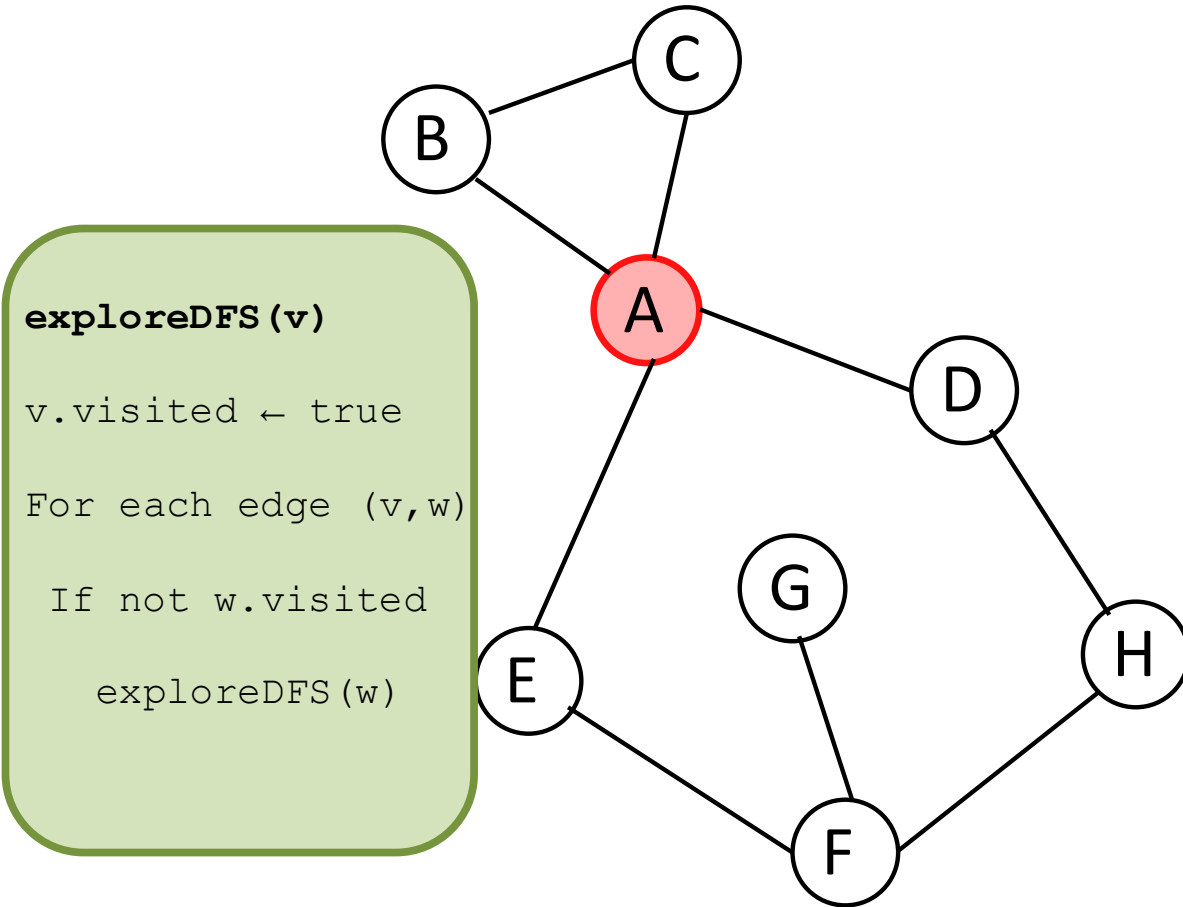
For each edge (v,w)

    If not w.visited

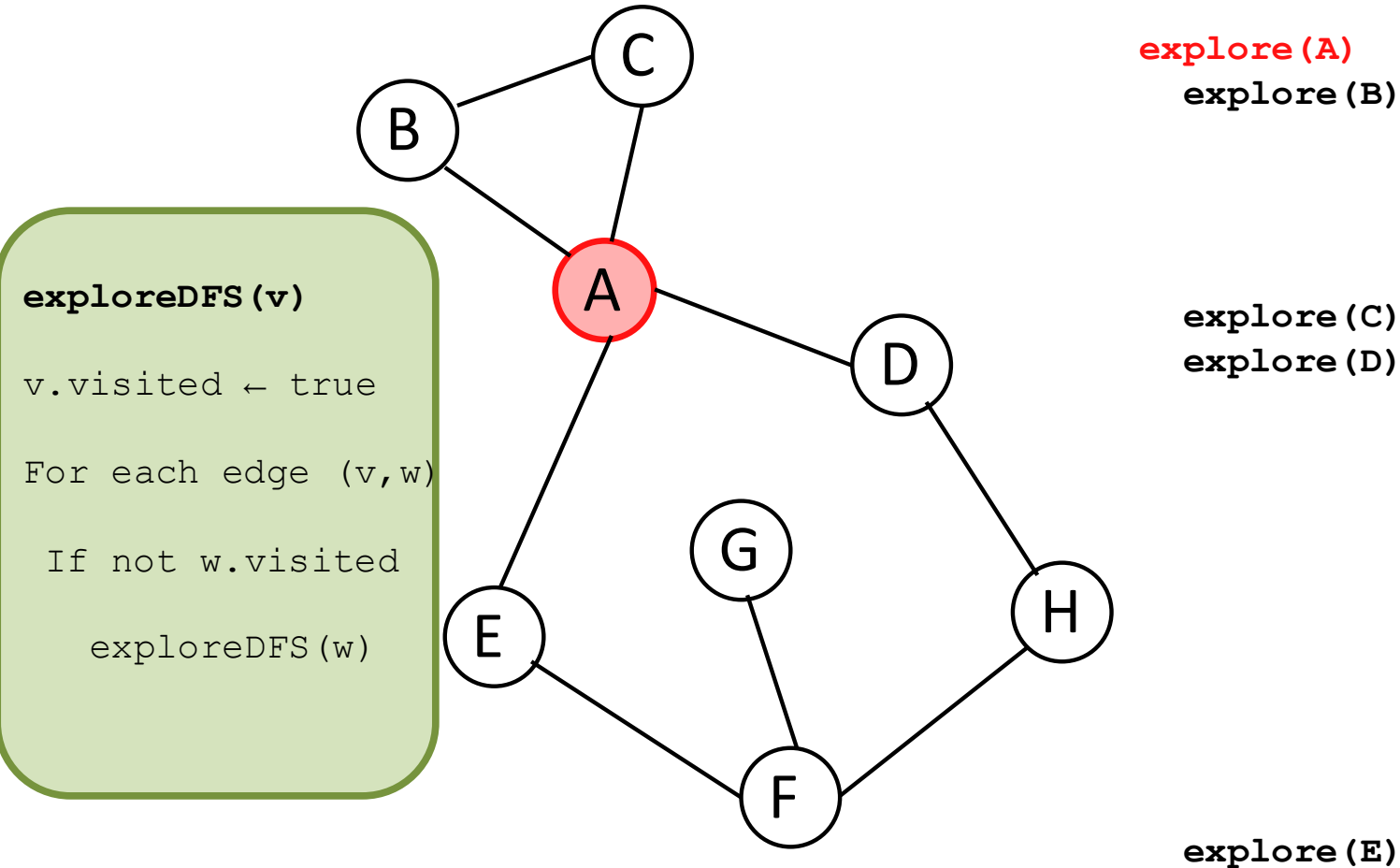
        exploreDFS(w)

# Explore (Depth First): Example

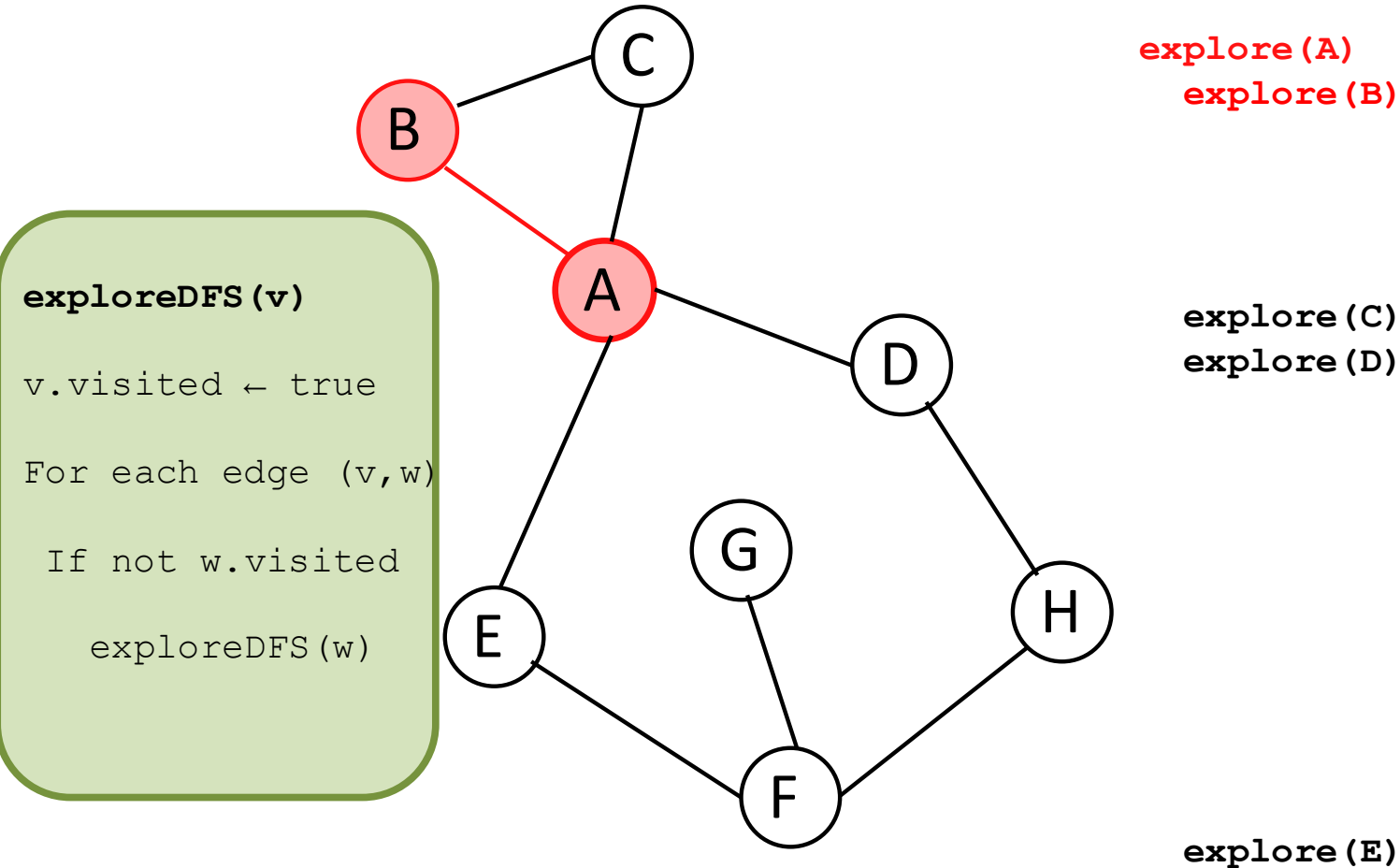
explore(A)



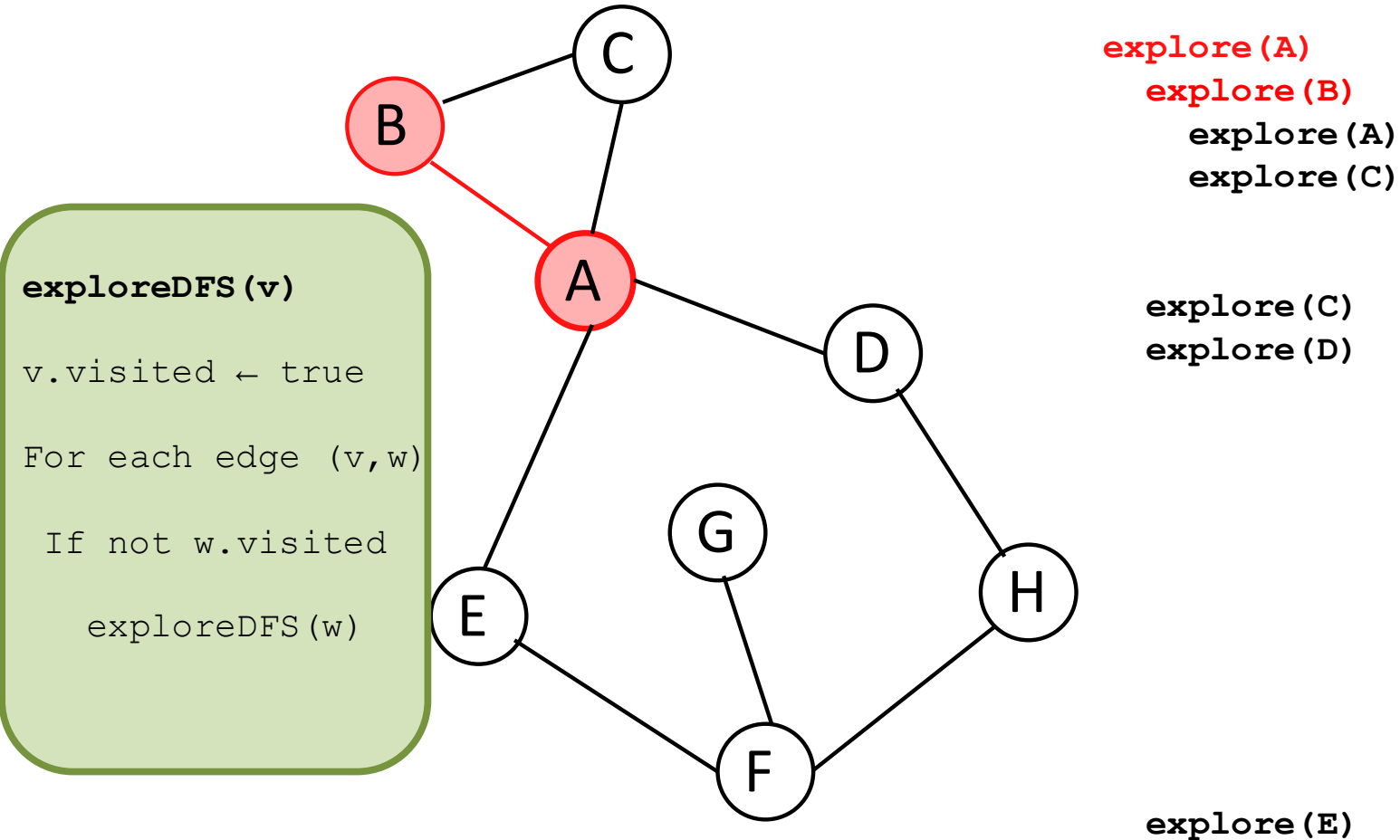
# Explore (Depth First): Example



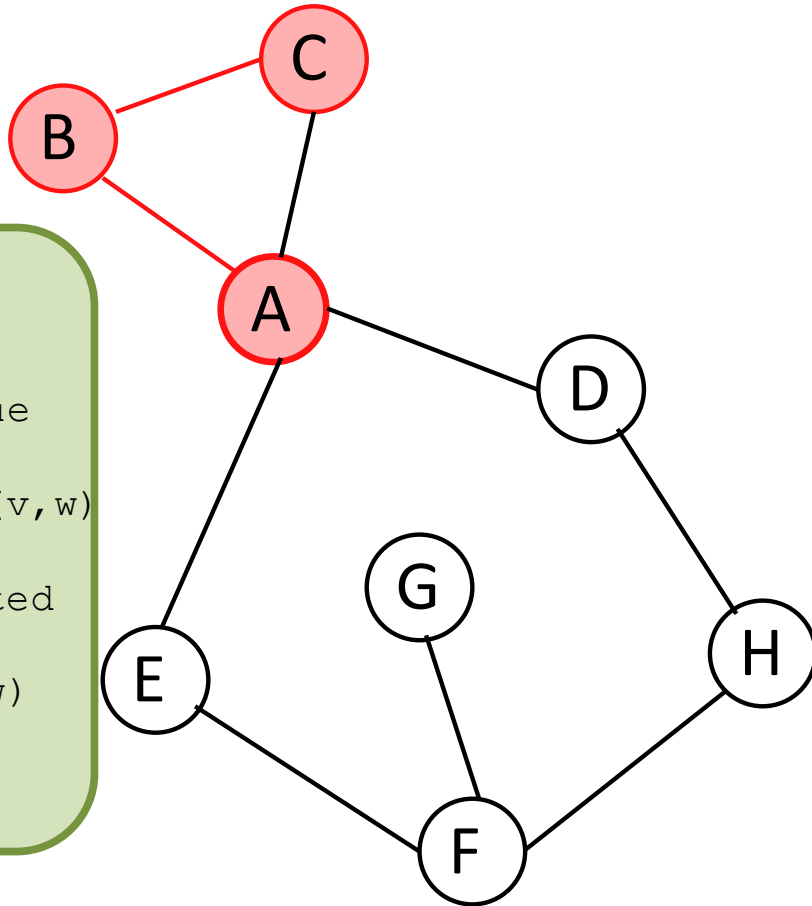
# Explore (Depth First): Example



# Explore (Depth First): Example



# Explore (Depth First): Example



**explore(A)**  
**explore(B)**  
explore(A)  
**explore(C)**

**explore(C)**  
**explore(D)**

**explore(E)**

**exploreDFS(v)**

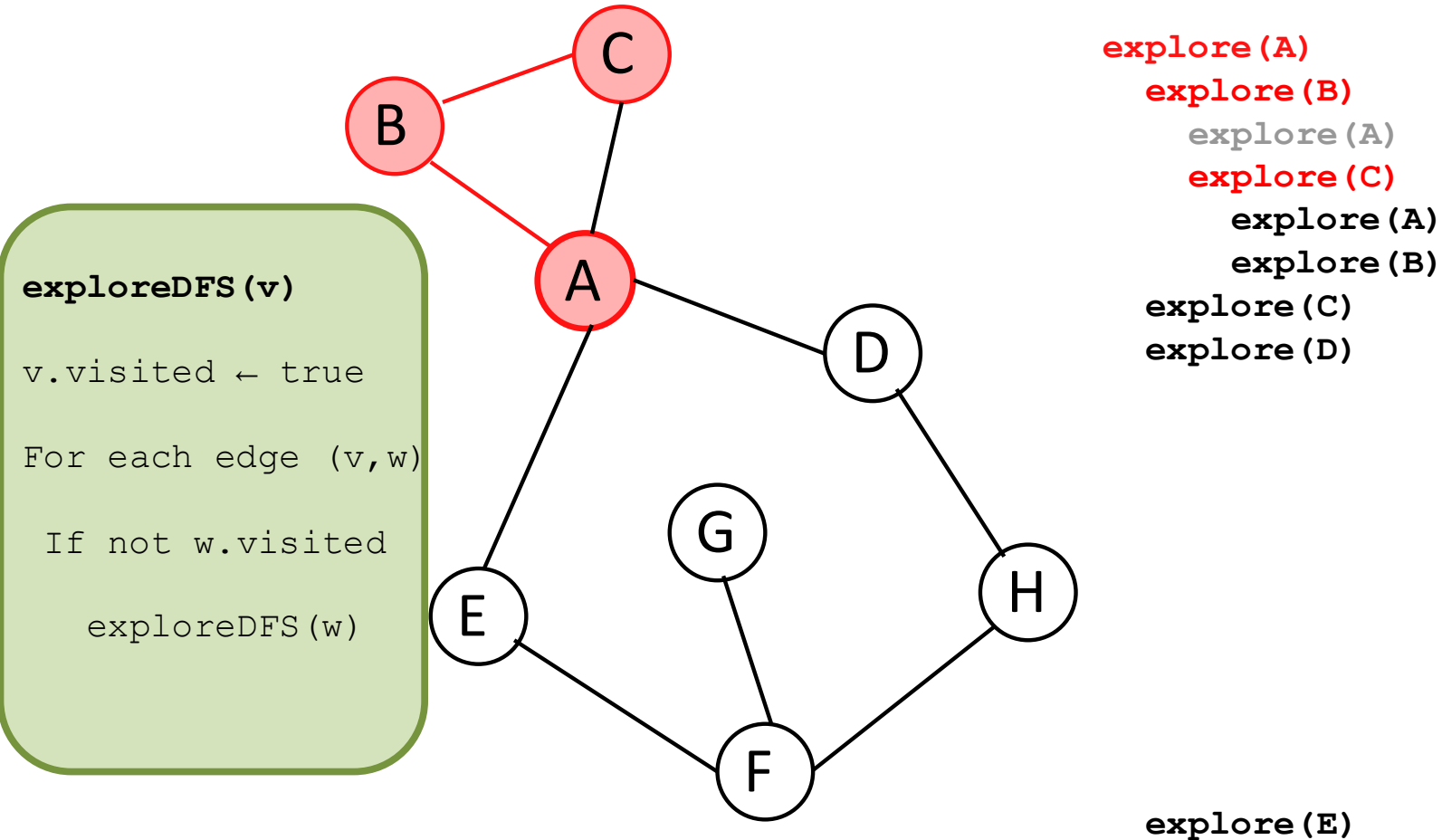
`v.visited ← true`

`For each edge (v,w)`

`If not w.visited`

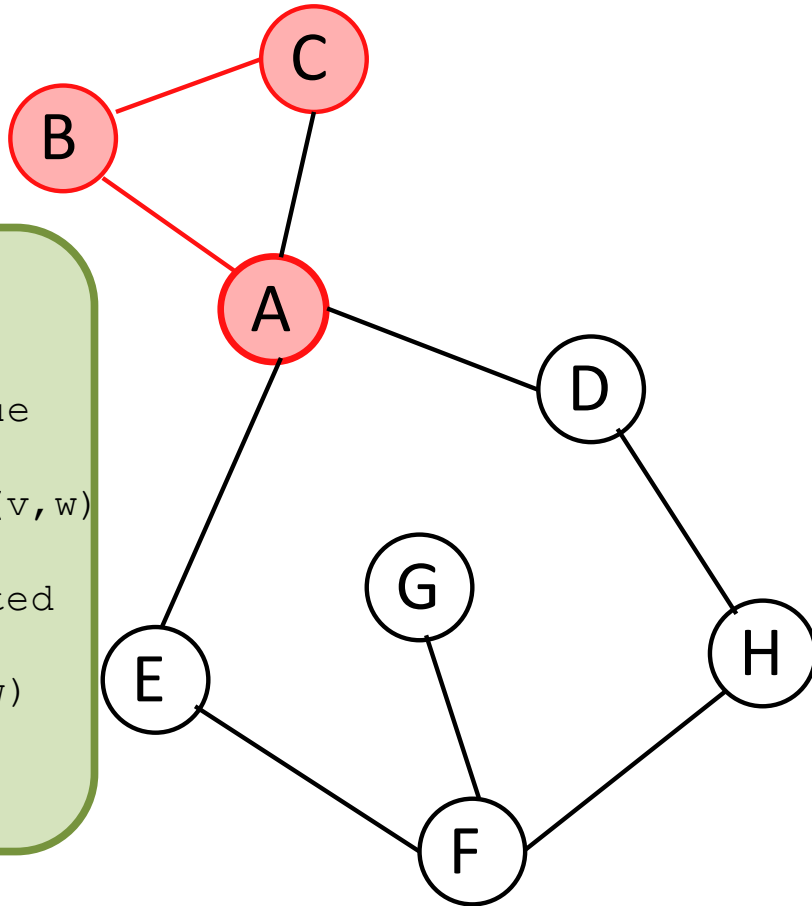
`exploreDFS(w)`

# Explore (Depth First): Example





# Explore (Depth First): Example



```
explore(A)
  explore(B)
    explore(A)
  explore(C)
    explore(A)
    explore(B)
  explore(D)
```

```
explore(E)
```

**exploreDFS(v)**

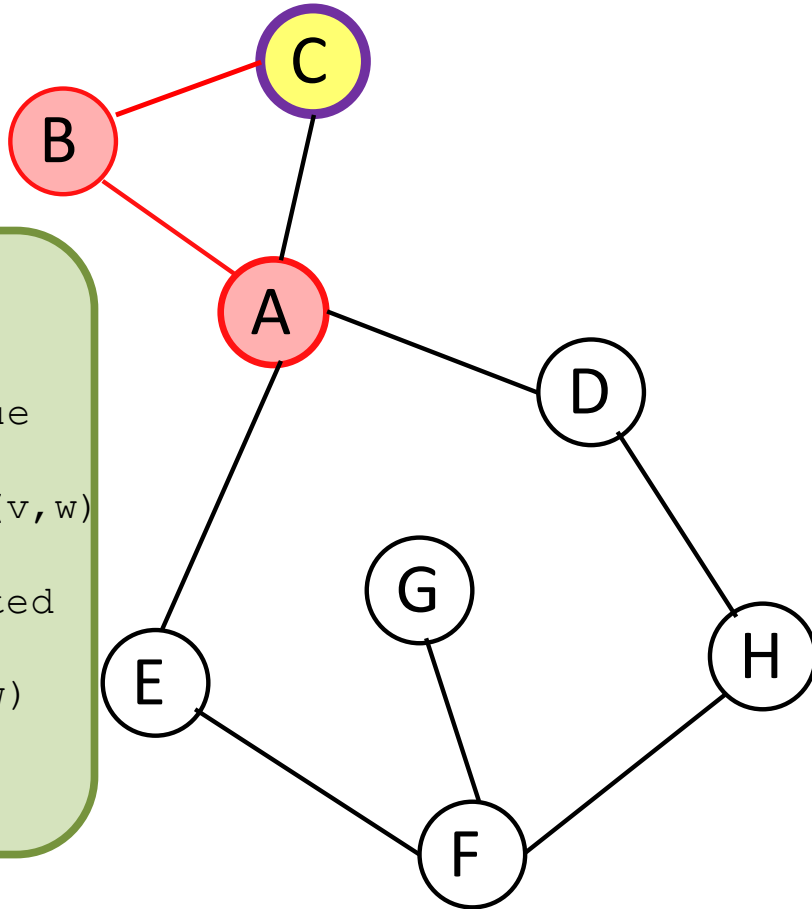
`v.visited ← true`

For each edge (v,w)

  If not w.visited

    exploreDFS(w)

# Explore (Depth First): Example



```
explore(A)
  explore(B)
    explore(A)
      explore(C)
        explore(A)
          explore(B)
```

Dead end!

What should happen next?

```
explore(E)
```

**exploreDFS(v)**

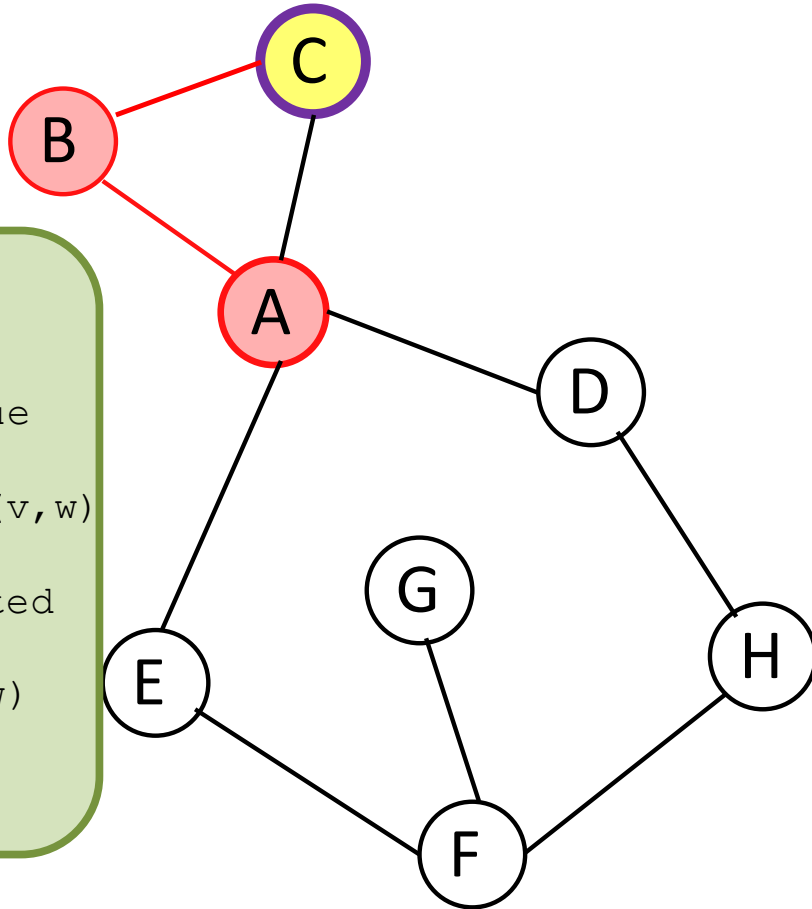
`v.visited ← true`

For each edge (v,w)

If not w.visited

`exploreDFS(w)`

# Explore (Depth First): Example



```
explore(A)
  explore(B)
    explore(A)
    explore(C)
      explore(A)
      explore(B)
    explore(C)
    explore(D)
```

Dead end!

What should happen next?

Go back to vertex B

Explore any unexplored  
neighbors of B

**exploreDFS(v)**

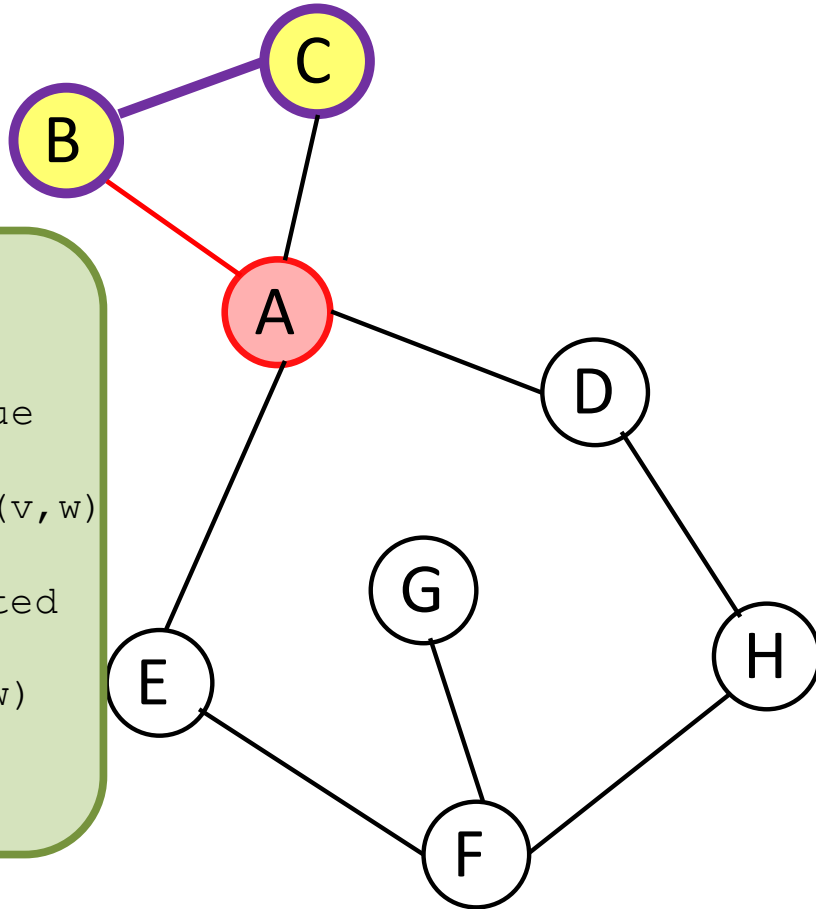
`v.visited ← true`

For each edge (v,w)

If not w.visited

`exploreDFS(w)`

# Explore (Depth First): Example



```
explore(A)
  explore(B)
    explore(A)
    explore(C)
      explore(A)
      explore(B)
    explore(C)
    explore(D)
```

**Backtracking!**

**Go back to A  
Explore unexplored  
neighbors of A**

```
explore(E)
```

**exploreDFS(v)**

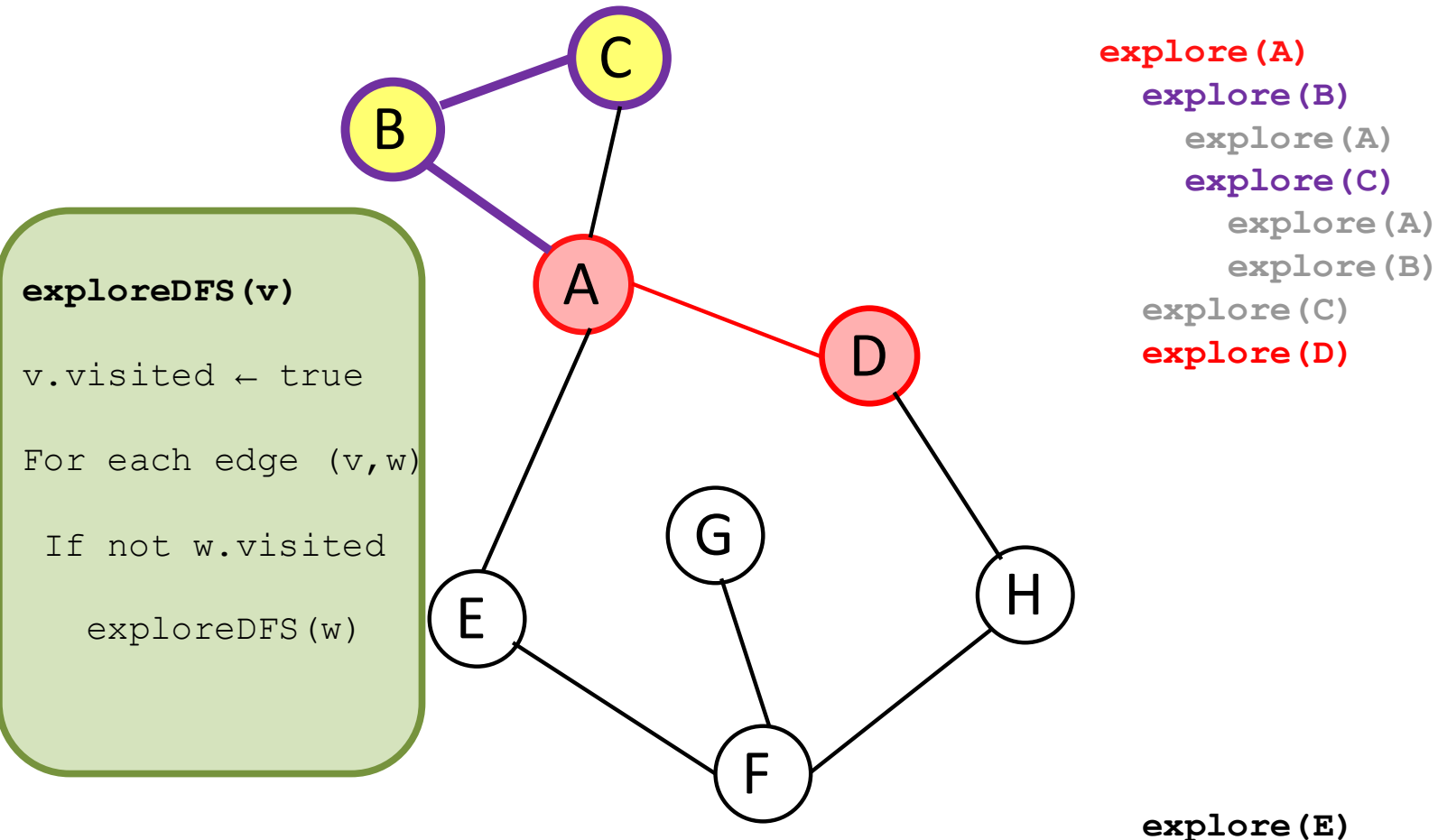
`v.visited ← true`

For each edge (v,w)

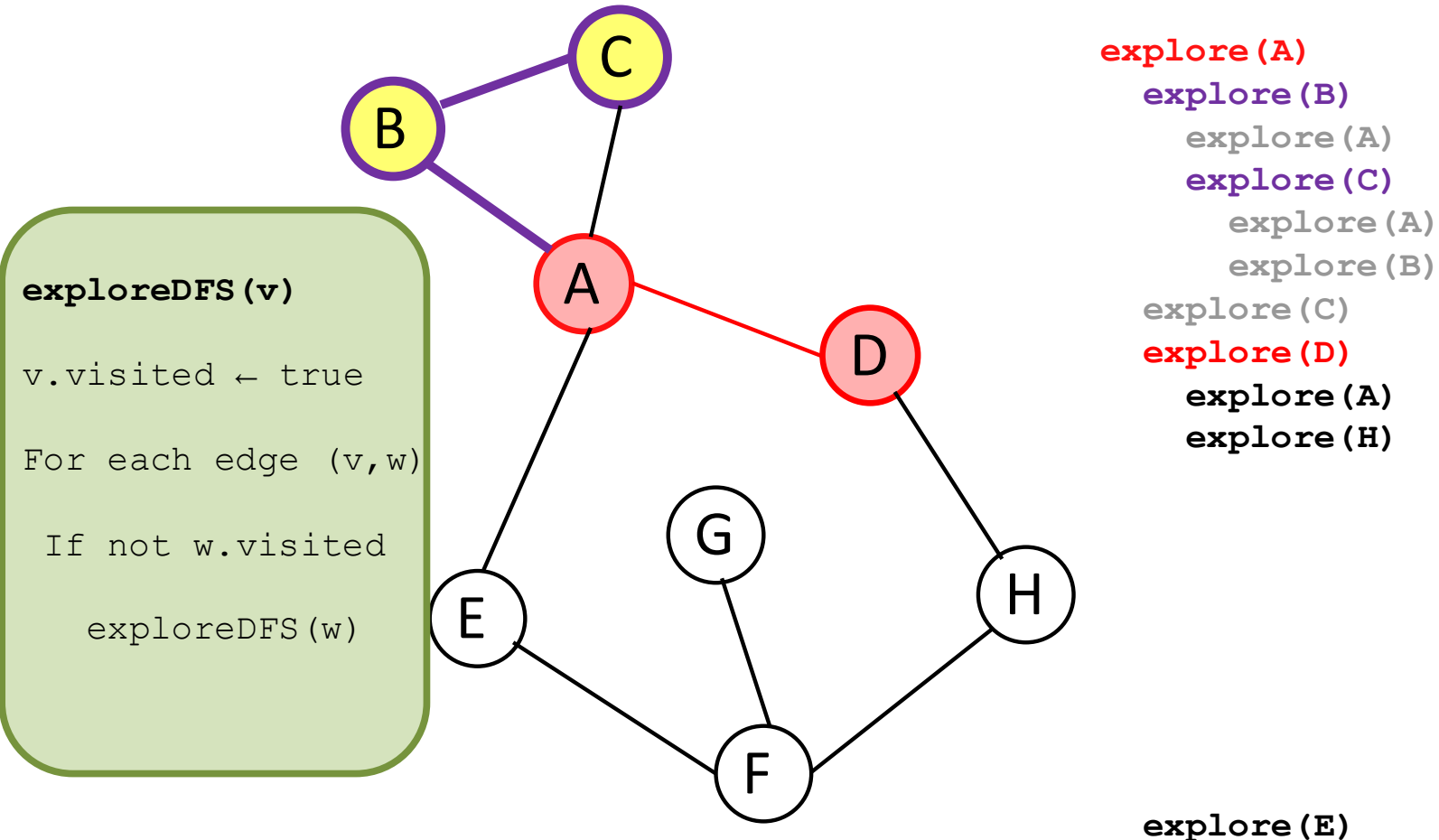
If not w.visited

`exploreDFS(w)`

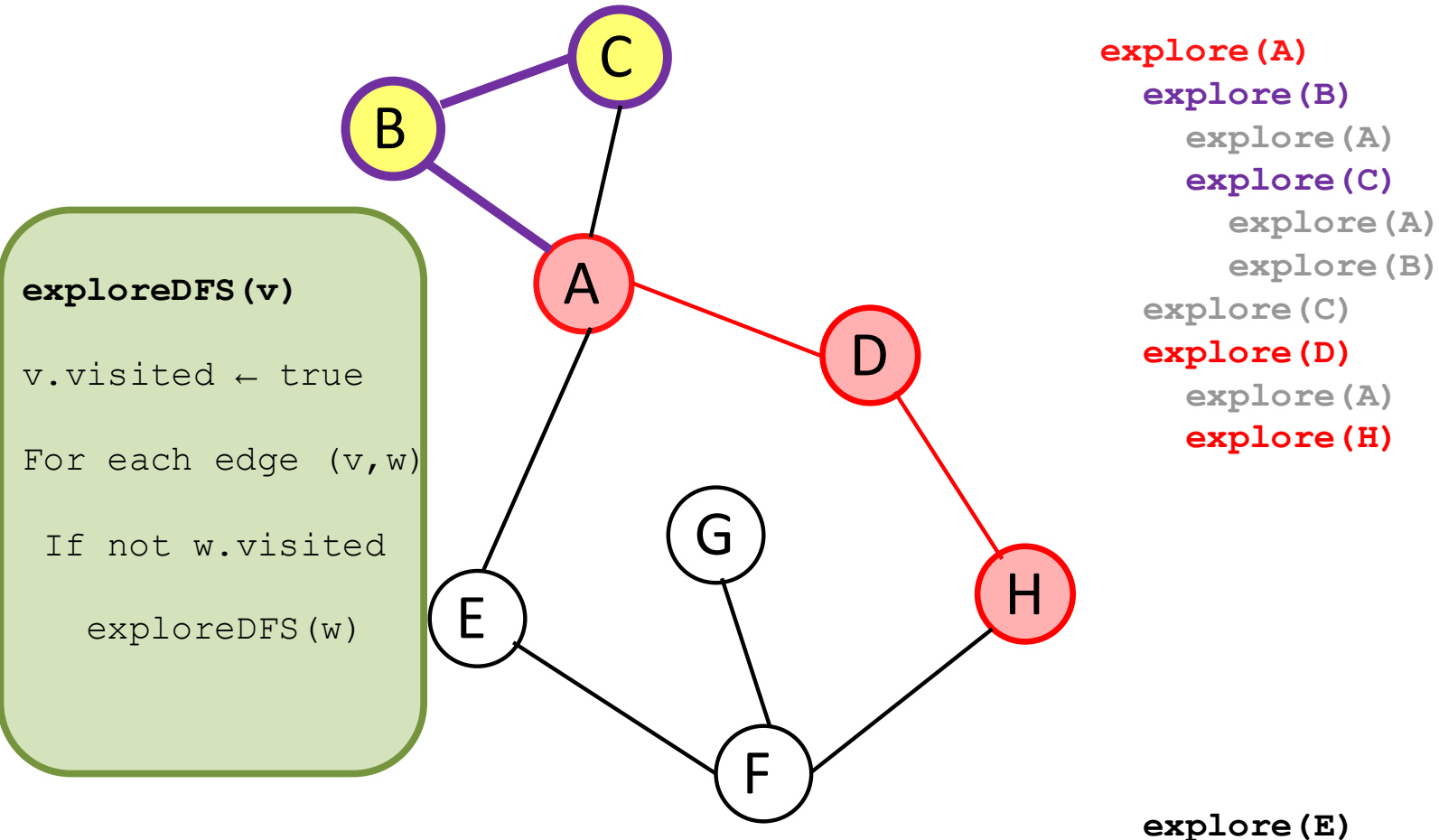
# Explore (Depth First): Example



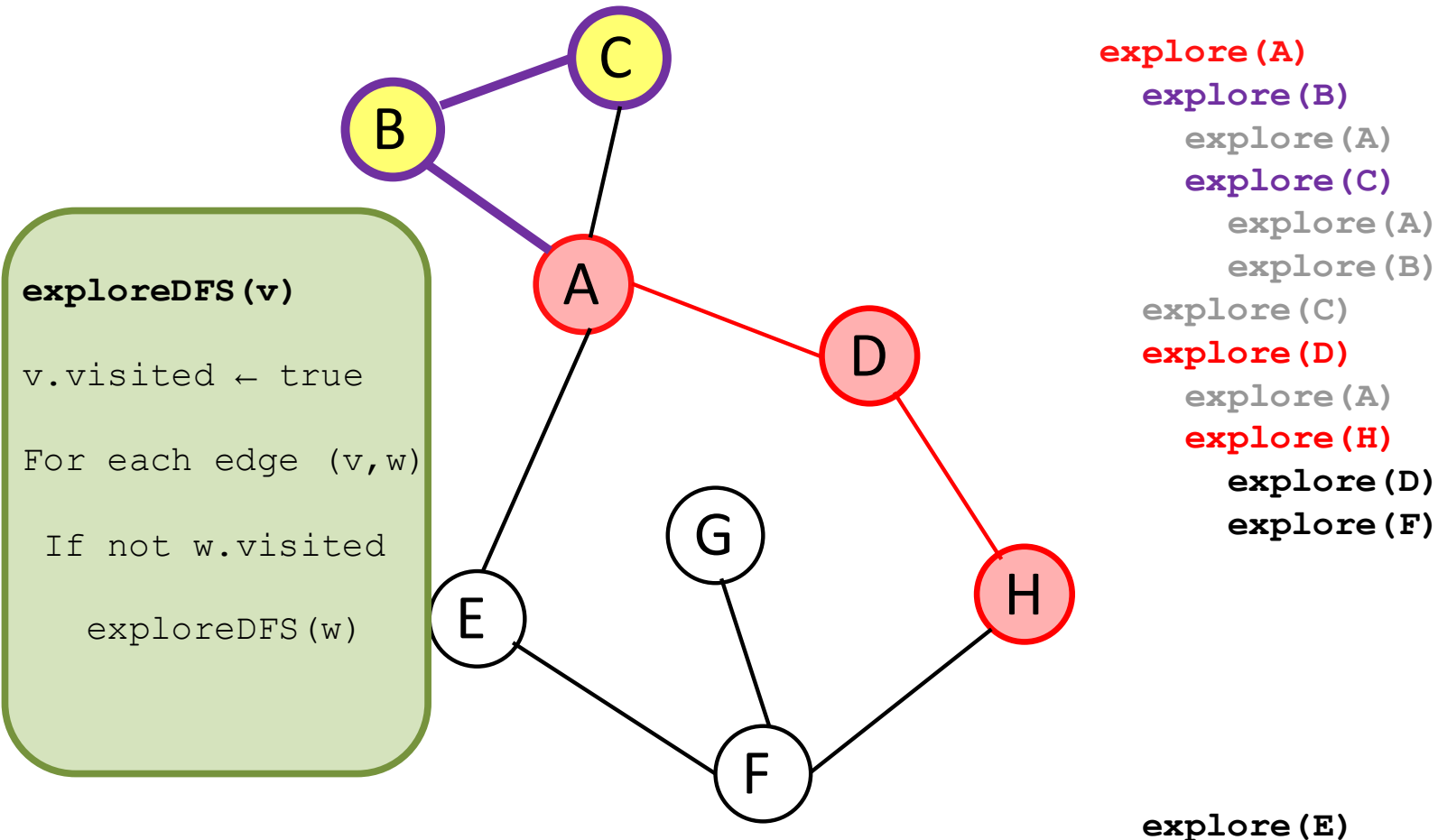
# Explore (Depth First): Example



# Explore (Depth First): Example

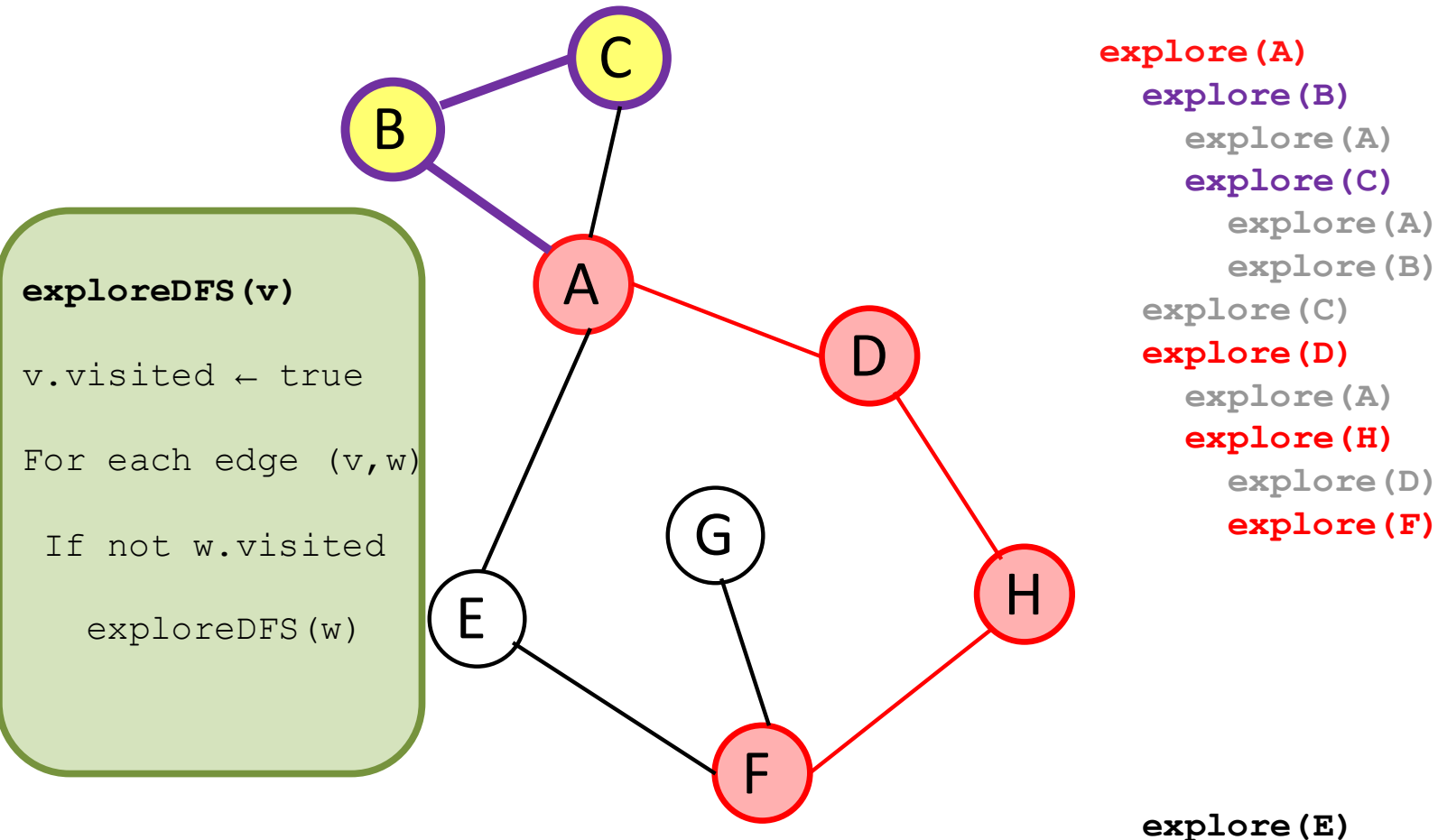


# Explore (Depth First): Example

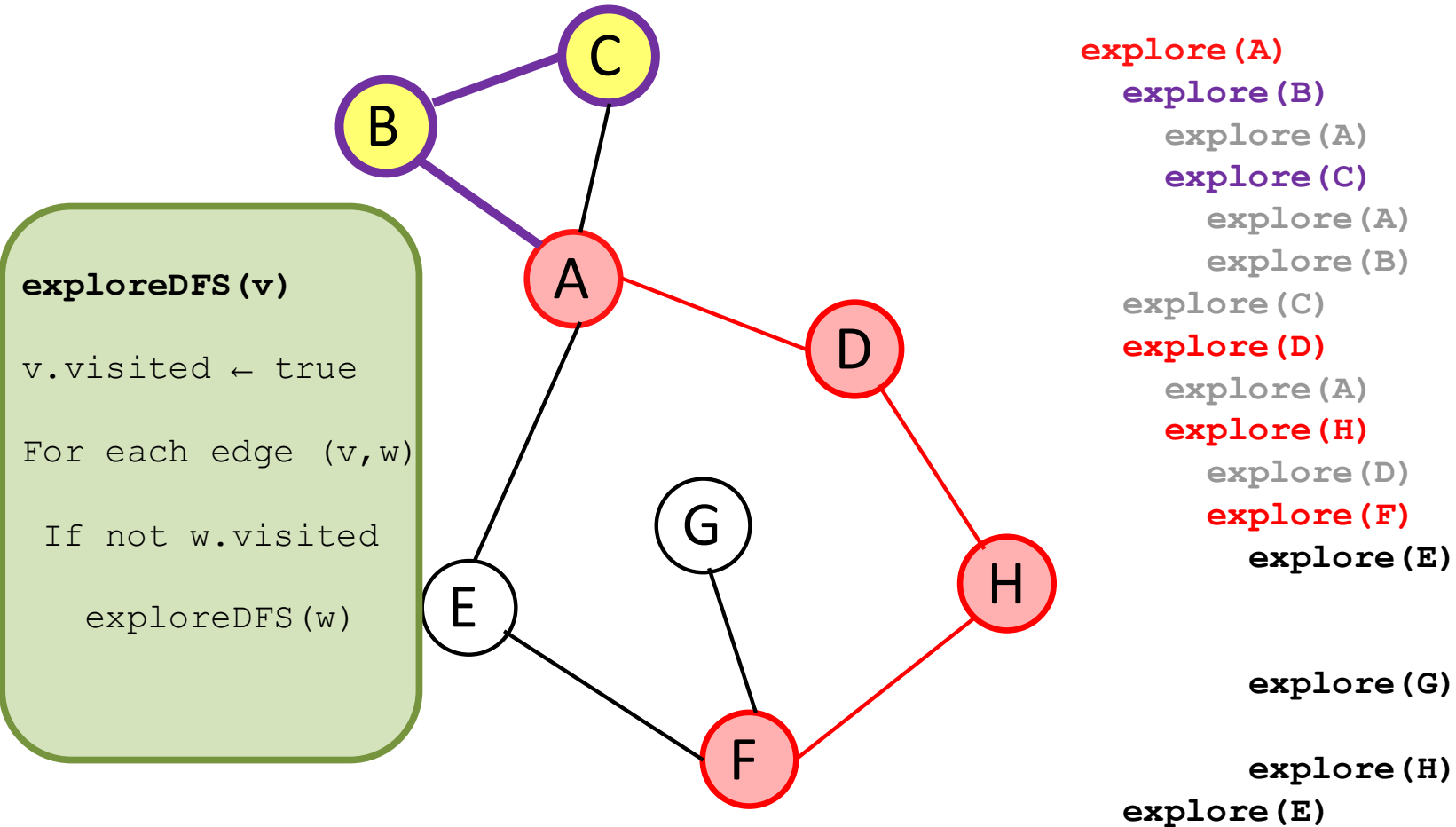




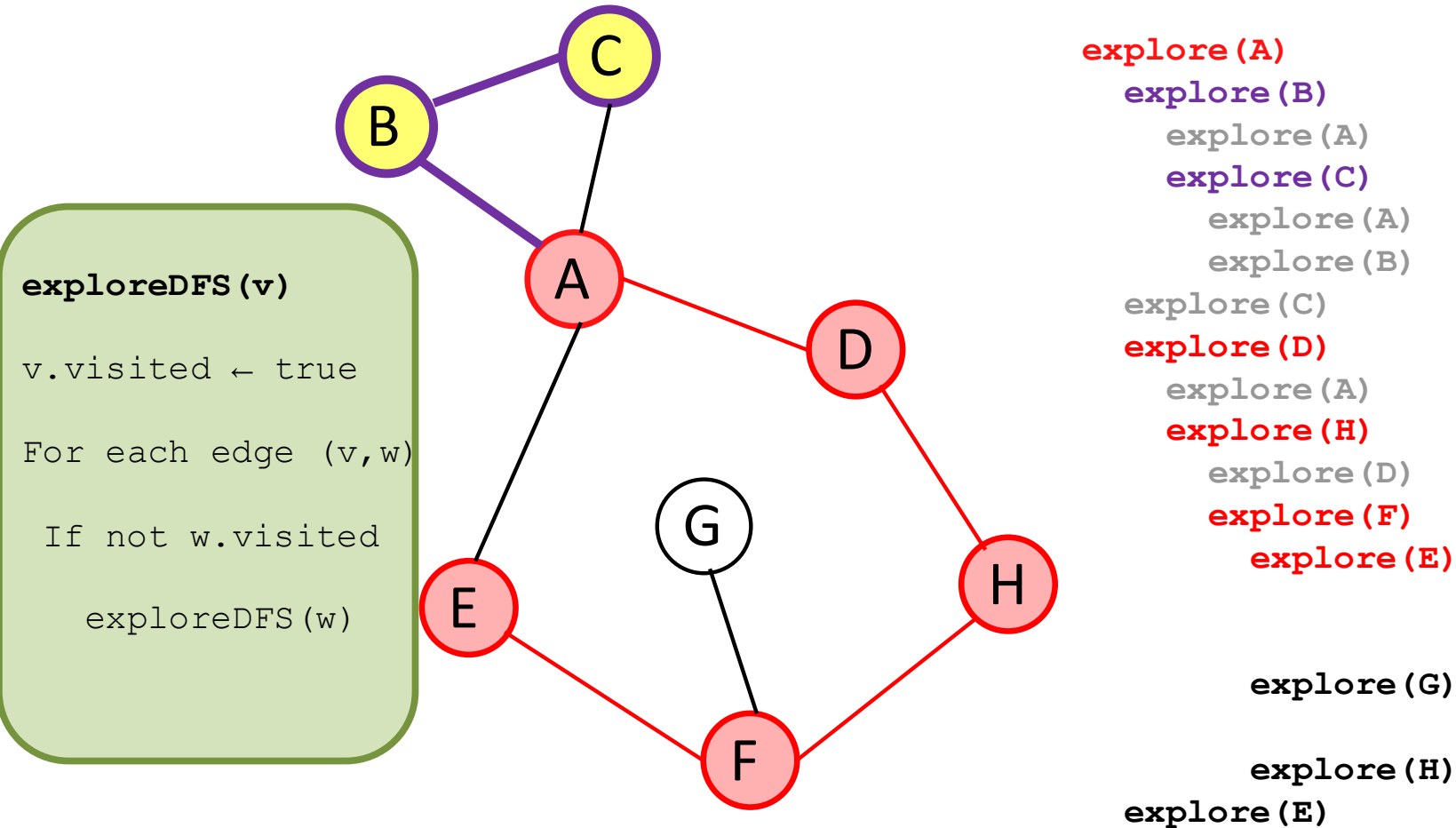
# Explore (Depth First): Example



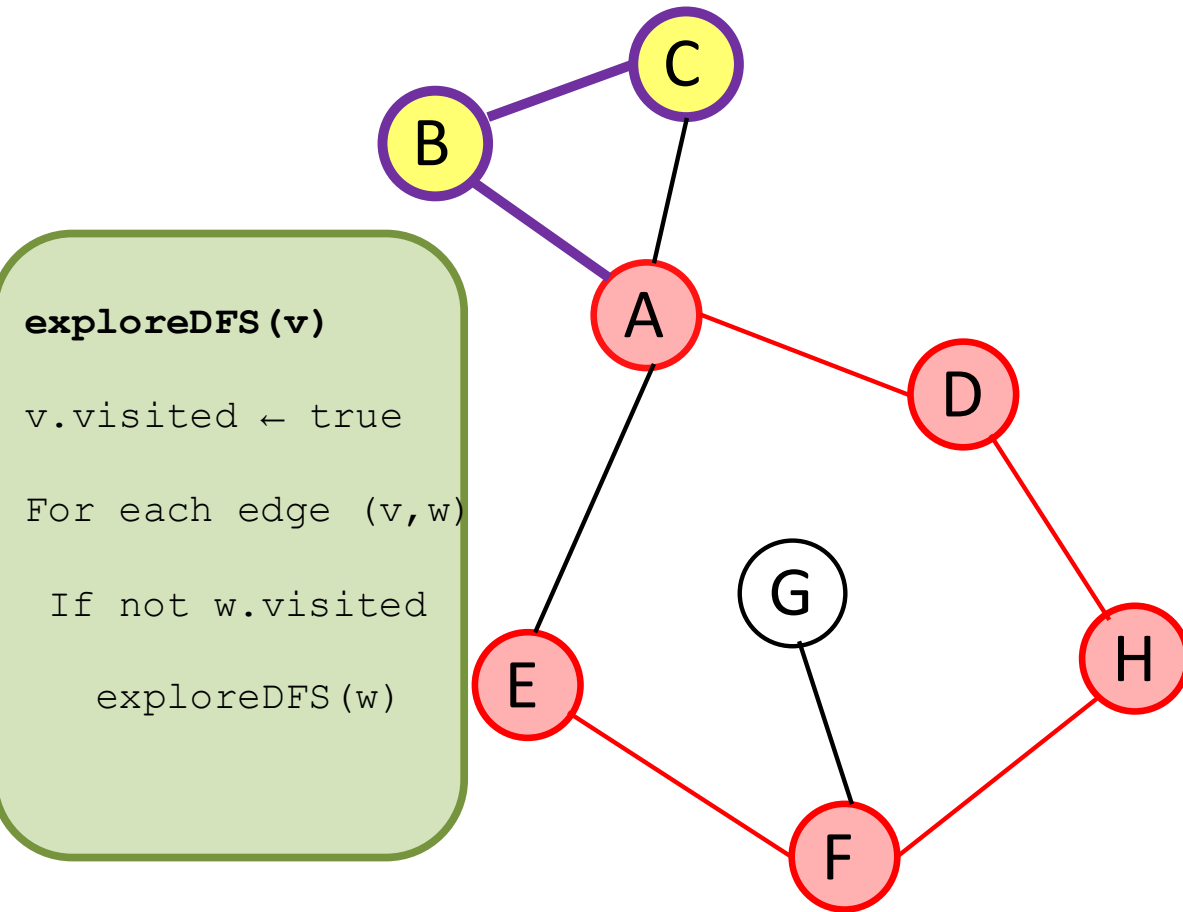
# Explore (Depth First): Example



# Explore (Depth First): Example

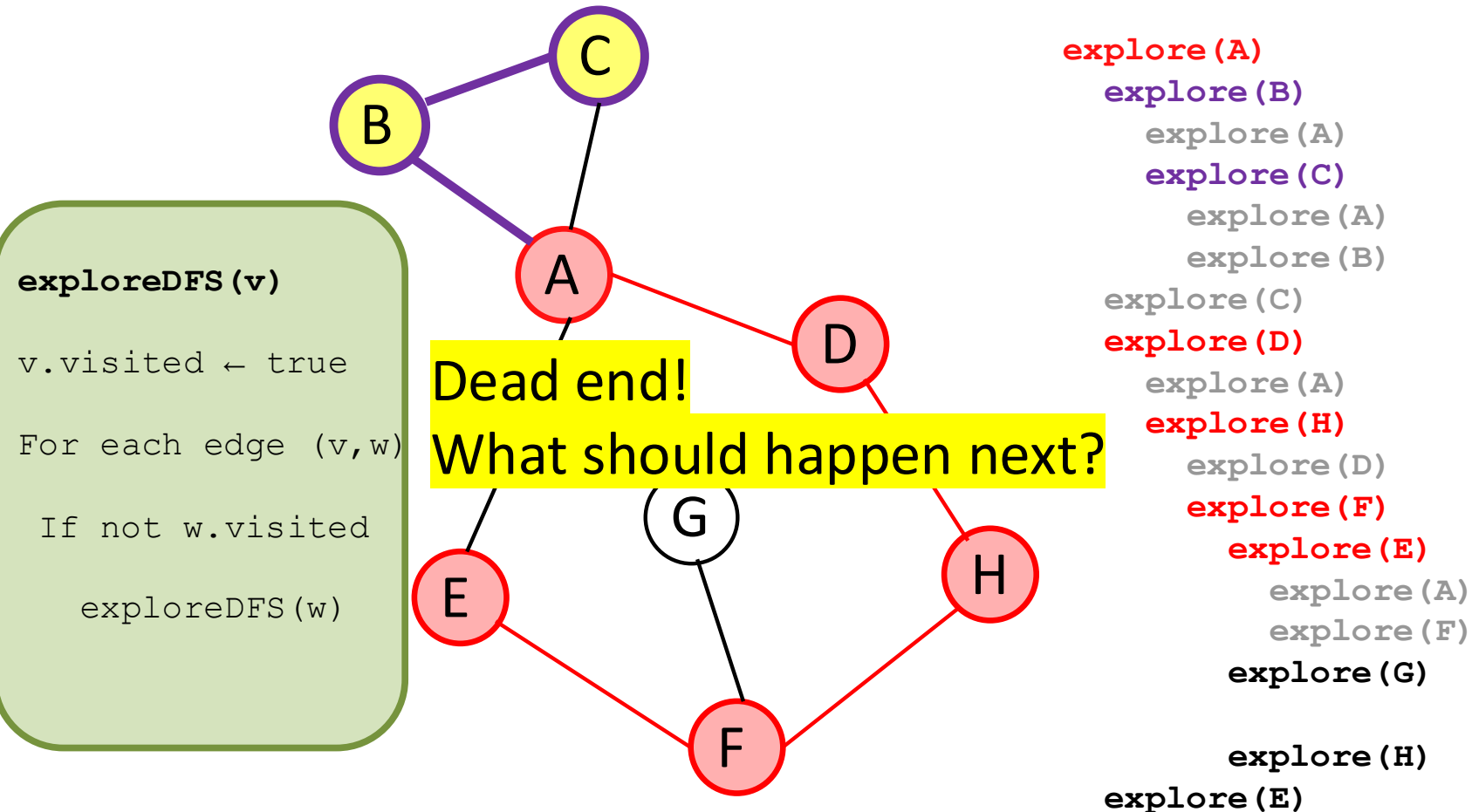


# Explore (Depth First): Example

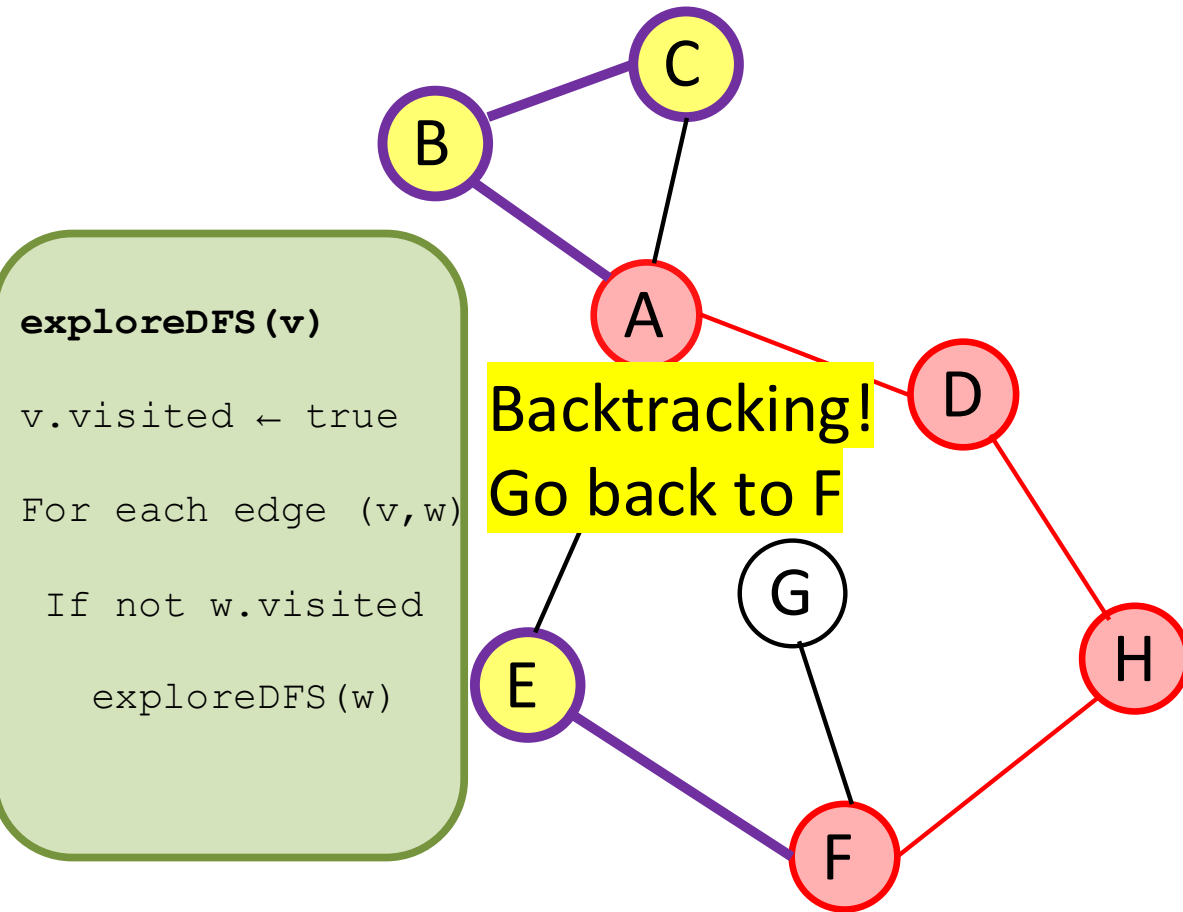


```
explore(A)
  explore(B)
    explore(A)
    explore(C)
      explore(A)
      explore(B)
    explore(C)
  explore(D)
    explore(A)
    explore(H)
      explore(D)
    explore(F)
      explore(E)
        explore(A)
        explore(F)
        explore(G)
      explore(H)
    explore(E)
```

# Explore (Depth First): Example



# Explore (Depth First): Example

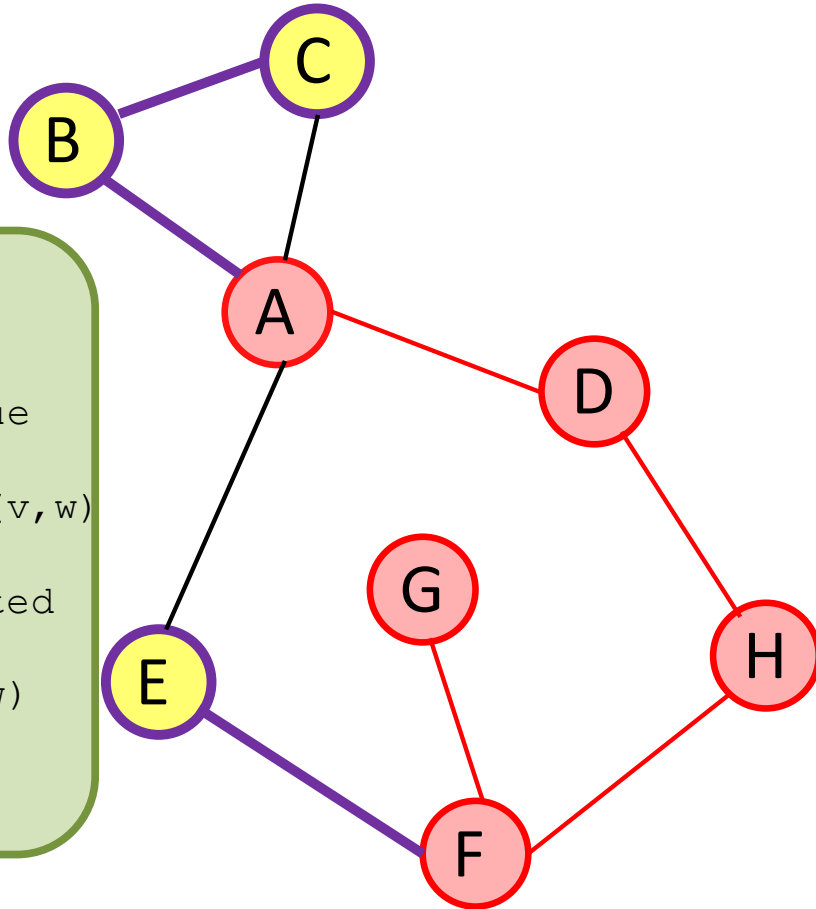


```
explore(A)
  explore(B)
    explore(A)
    explore(C)
      explore(A)
      explore(B)
    explore(C)
  explore(D)
    explore(A)
  explore(H)
    explore(D)
  explore(F)
    explore(E)
      explore(A)
      explore(F)
    explore(G)

    explore(H)
  explore(E)
```

# Explore (Depth First): Example

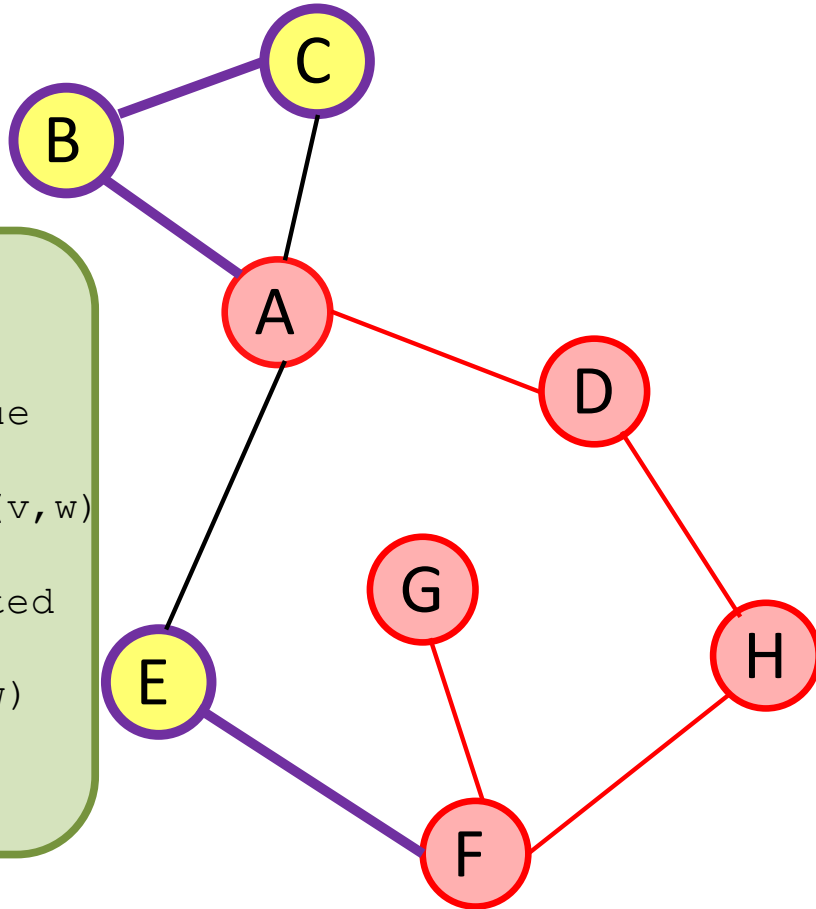
```
exploreDFS(v)  
v.visited ← true  
For each edge (v,w)  
  If not w.visited  
    exploreDFS(w)
```



```
explore(A)  
  explore(B)  
    explore(A)  
  explore(C)  
    explore(A)  
    explore(B)  
  explore(C)  
explore(D)  
  explore(A)  
explore(H)  
  explore(D)  
explore(F)  
  explore(E)  
    explore(A)  
    explore(F)  
explore(G)  
  
  explore(H)  
explore(E)
```

# Explore (Depth First): Example

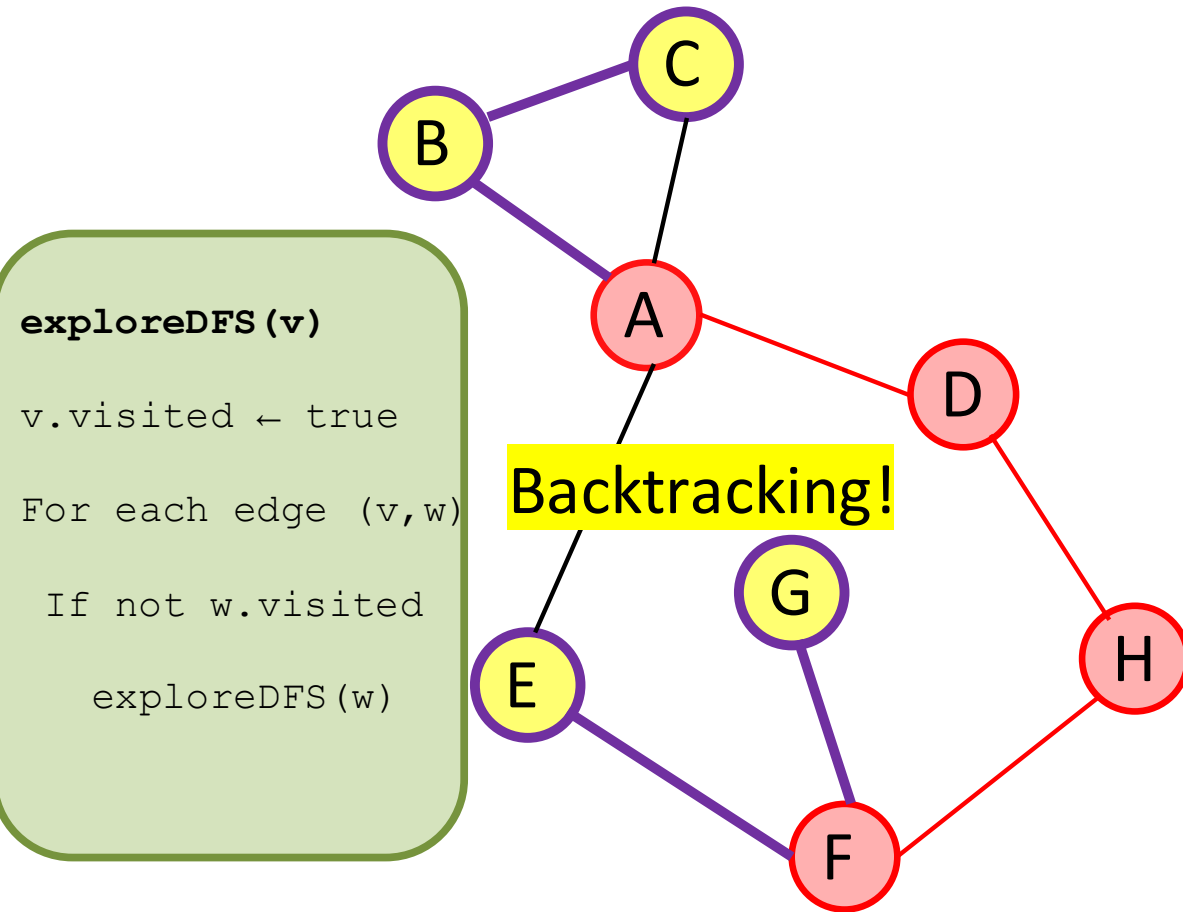
```
exploreDFS(v)  
v.visited ← true  
For each edge (v,w)  
  If not w.visited  
    exploreDFS(w)
```



```
explore(A)  
  explore(B)  
    explore(A)  
  explore(C)  
    explore(A)  
    explore(B)  
  explore(C)  
explore(D)  
  explore(A)  
explore(H)  
  explore(D)  
explore(F)  
  explore(E)  
    explore(A)  
    explore(F)  
  explore(G)  
    explore(F)  
  explore(H)  
explore(E)
```



# Explore (Depth First): Example

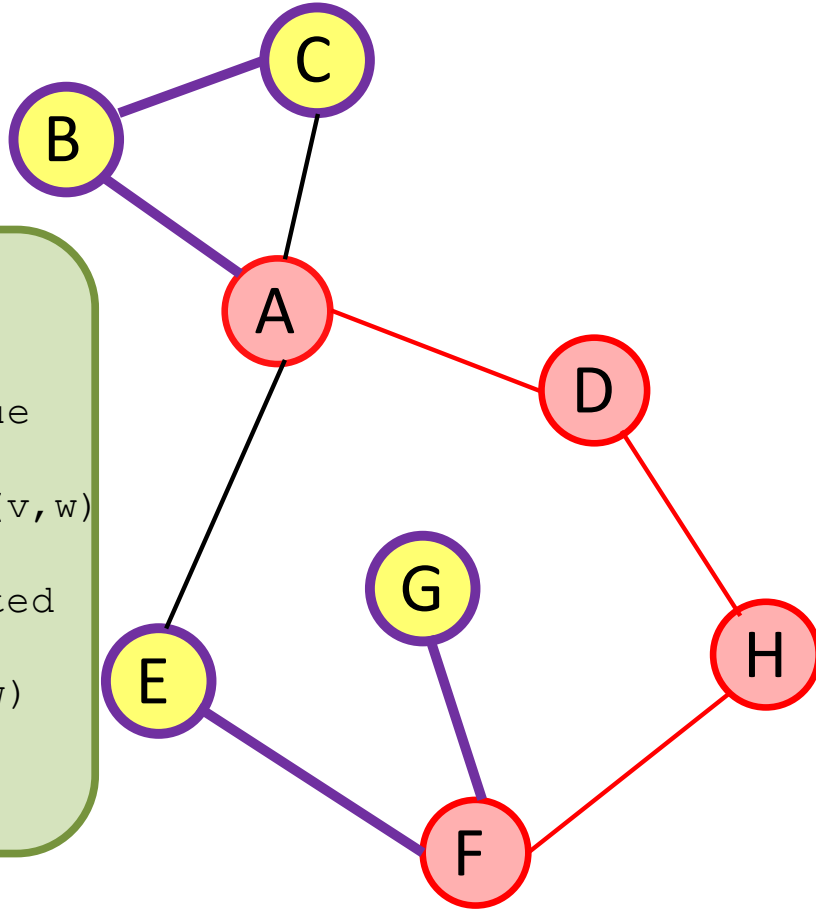


```
exploreDFS(v)  
v.visited ← true  
For each edge (v,w)  
  If not w.visited  
    exploreDFS(w)
```

```
explore(A)  
  explore(B)  
    explore(A)  
    explore(C)  
      explore(A)  
      explore(B)  
    explore(C)  
  explore(D)  
    explore(A)  
    explore(H)  
      explore(D)  
    explore(F)  
      explore(E)  
        explore(A)  
        explore(F)  
      explore(G)  
        explore(F)  
      explore(H)  
    explore(E)
```

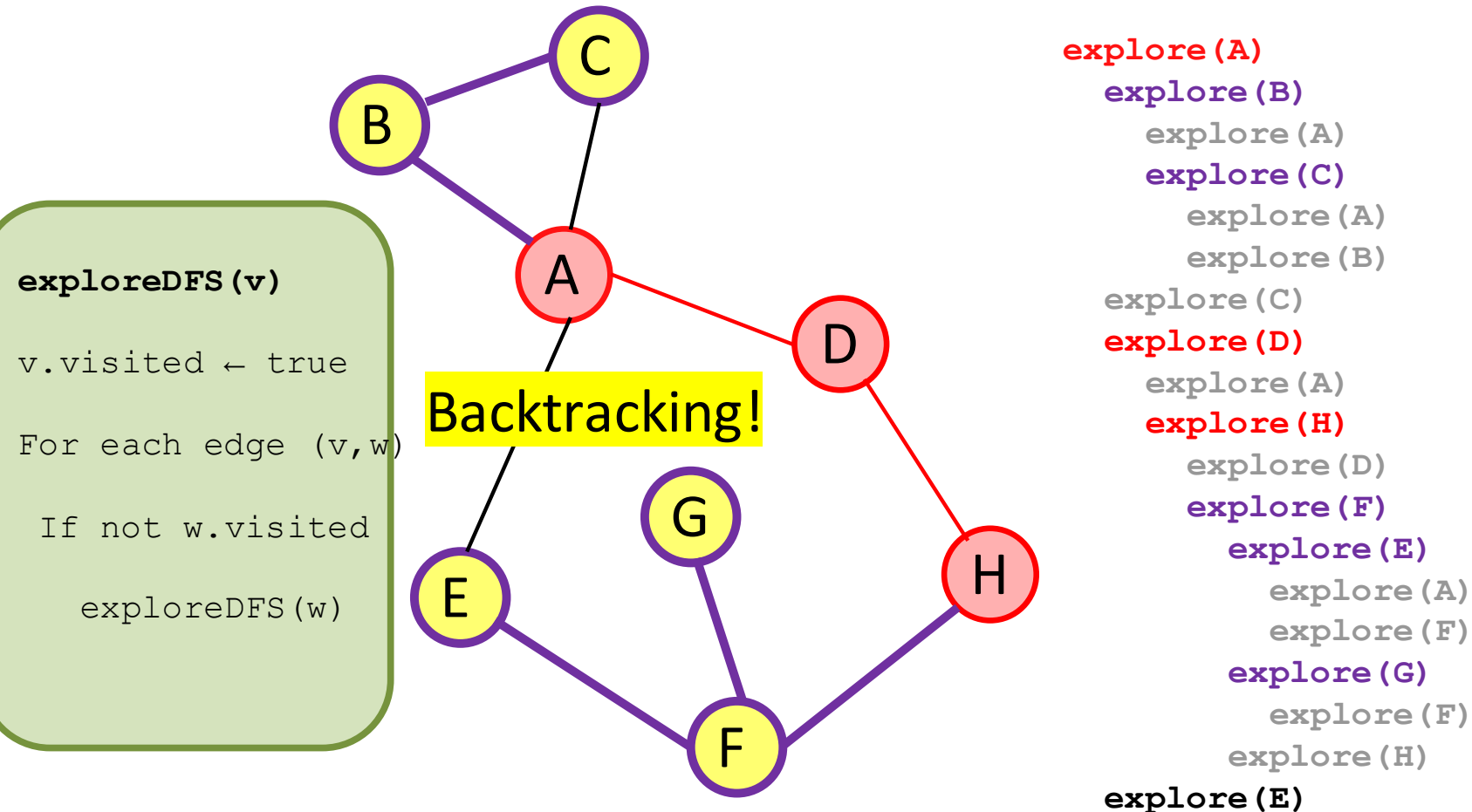
# Explore (Depth First): Example

```
exploreDFS(v)  
v.visited ← true  
For each edge (v,w)  
  If not w.visited  
    exploreDFS(w)
```

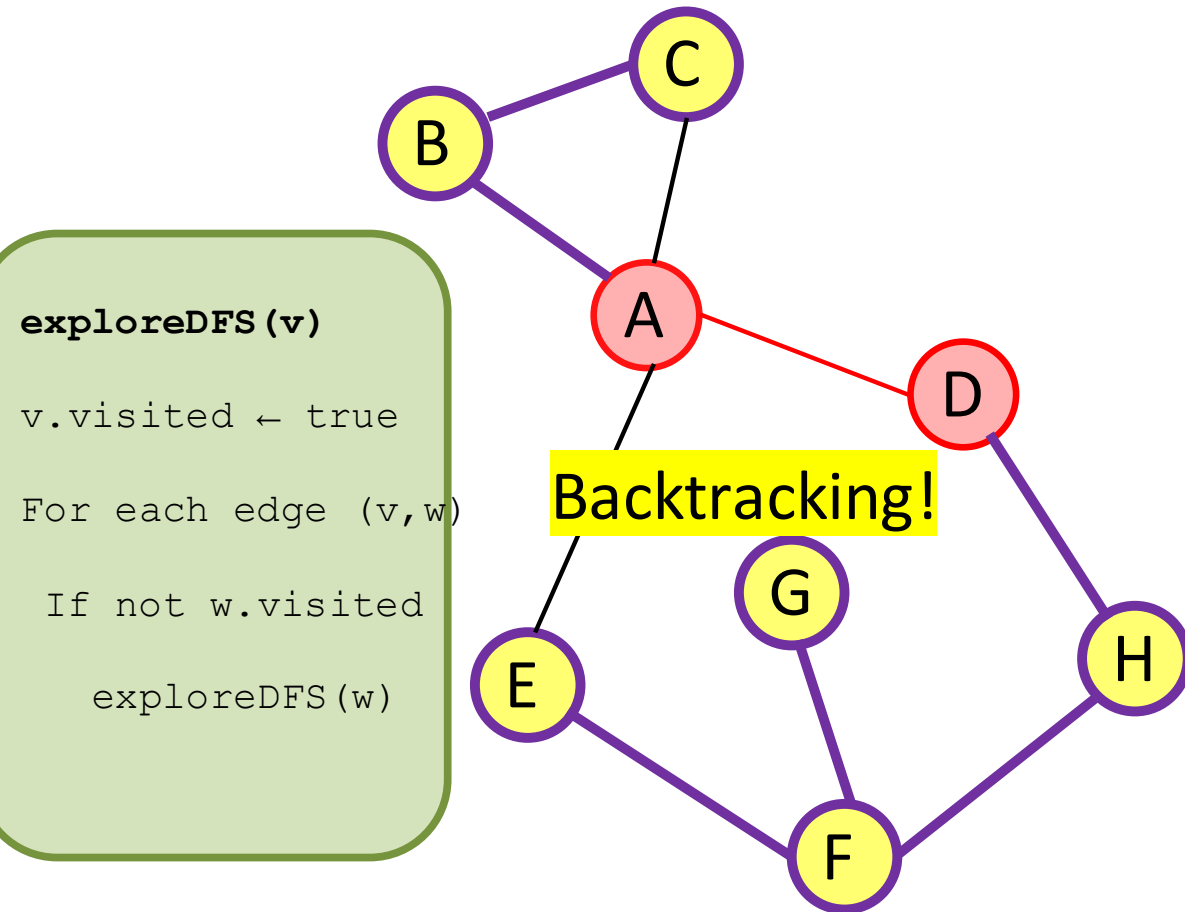


```
explore(A)  
  explore(B)  
    explore(A)  
    explore(C)  
      explore(A)  
      explore(B)  
    explore(C)  
  explore(D)  
    explore(A)  
    explore(H)  
      explore(D)  
    explore(F)  
      explore(E)  
        explore(A)  
        explore(F)  
      explore(G)  
        explore(F)  
        explore(H)  
    explore(E)
```

# Explore (Depth First): Example



# Explore (Depth First): Example



**explore (A)**

explore (B)

explore (A)

explore (C)

explore (A)

explore (B)

explore (C)

**explore (D)**

explore (A)

explore (H)

explore (D)

explore (F)

explore (E)

explore (A)

explore (F)

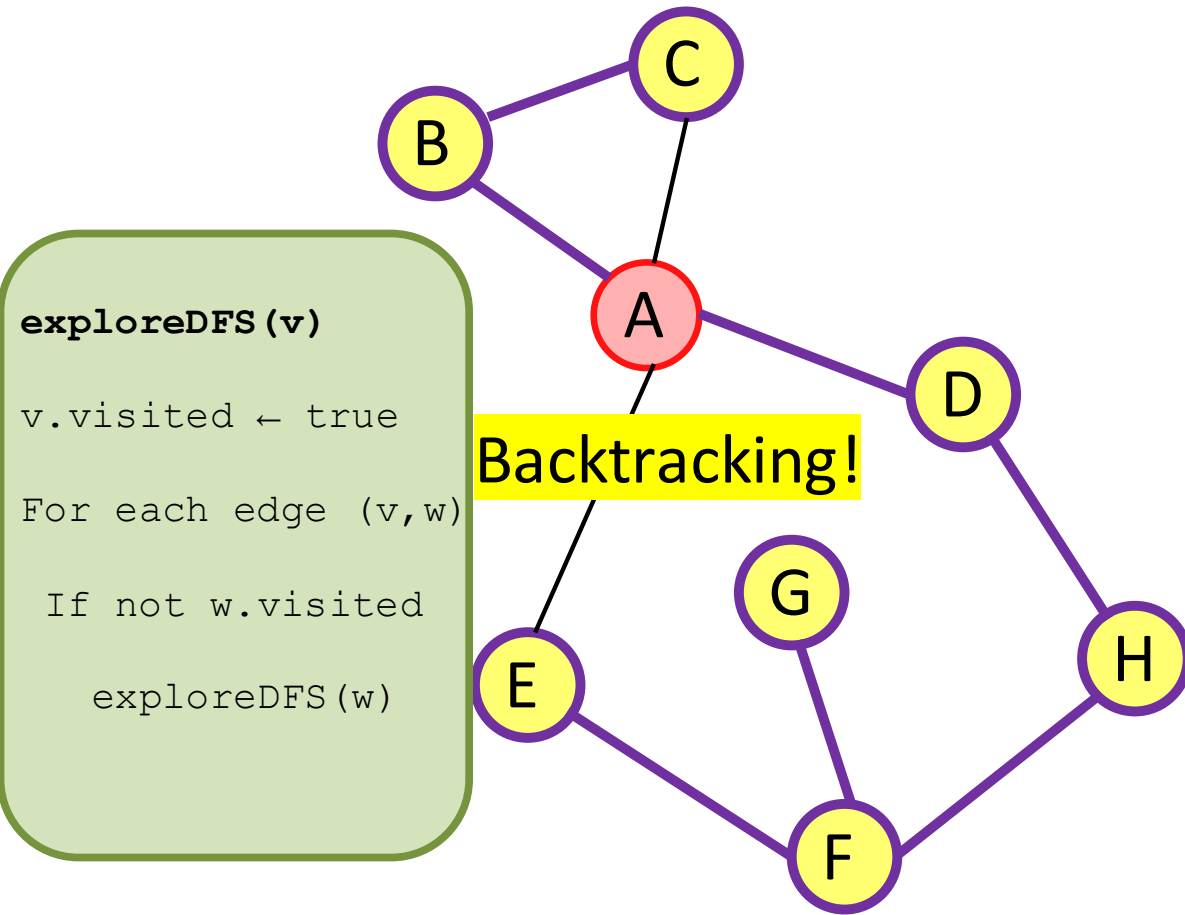
explore (G)

explore (F)

explore (H)

**explore (E)**

# Explore (Depth First): Example



**explore (A)**

explore (B)

explore (A)

explore (C)

explore (A)

explore (B)

explore (C)

**explore (D)**

explore (A)

**explore (H)**

explore (D)

**explore (F)**

**explore (E)**

explore (A)

explore (F)

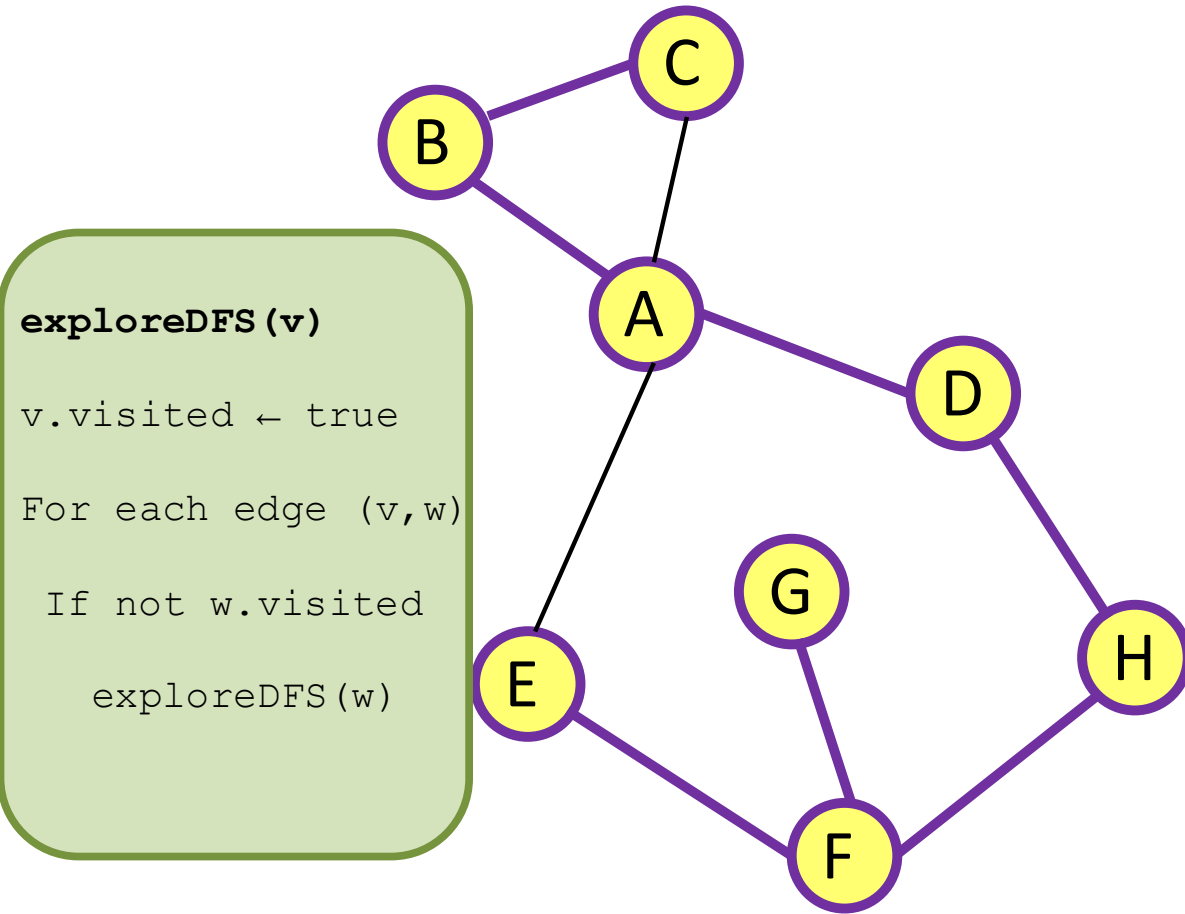
**explore (G)**

explore (F)

explore (H)

explore (E)

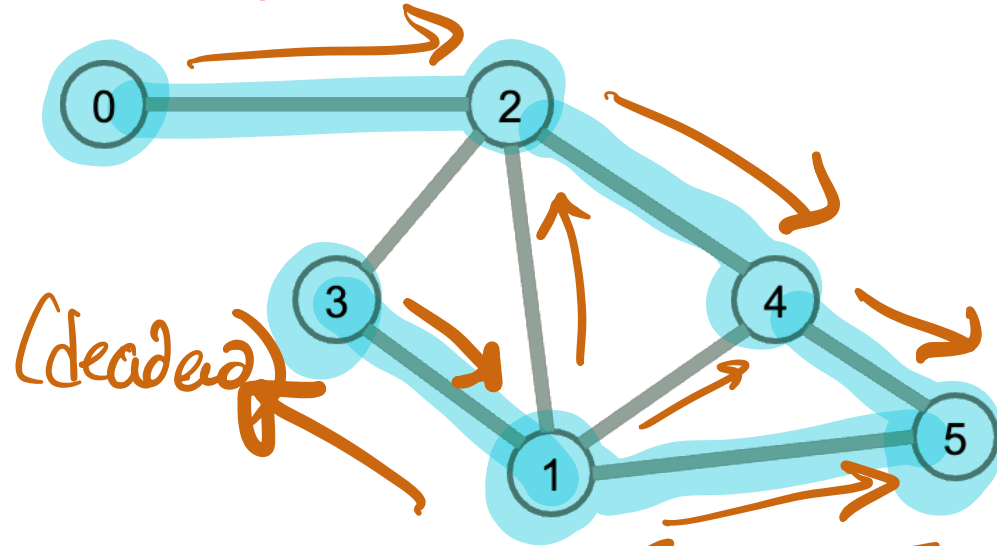
# Explore (Depth First): Example



```
explore (A)
  explore (B)
    explore (A)
    explore (C)
      explore (A)
      explore (B)
    explore (C)
  explore (D)
    explore (A)
    explore (H)
      explore (D)
    explore (F)
      explore (E)
        explore (A)
        explore (F)
      explore (G)
        explore (F)
      explore (H)
    explore (E)
```

## Explore (Depth First)

Search as far down a single path as possible, backtrack as needed



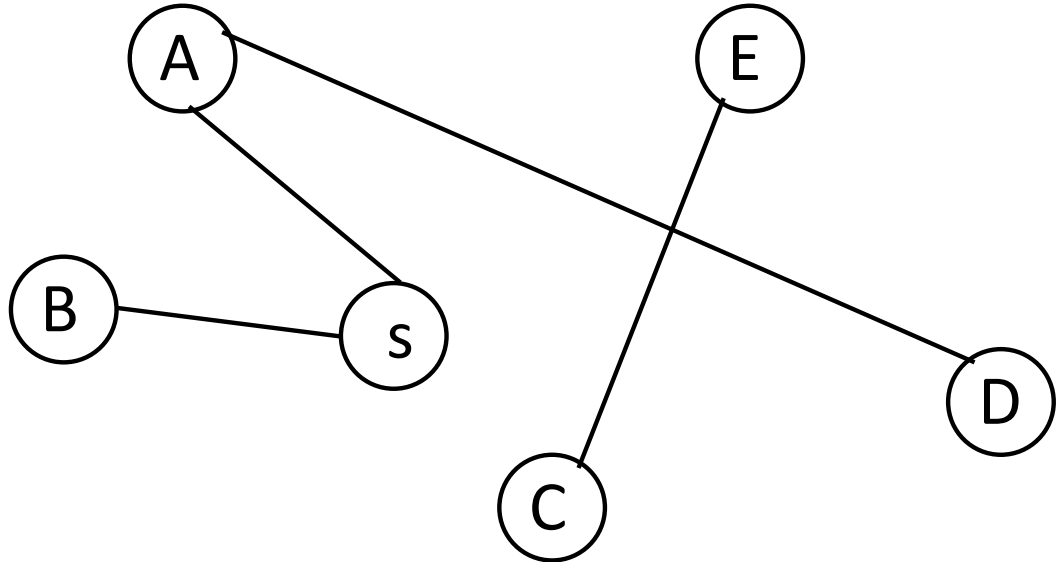
Assuming `exploreDFS` chooses the lower number node to explore first, in what order does `exploreDFS` visit the nodes in this graph starting at source 0?

- A. 0, 2, 0, 1, 3, 4, 5
- B. 0, 2, 3, 4, 1, 5
- C. 0, 2, 1, 3, 4, 5
- D. Something else

## Question: exploreDFS

Which vertices does exploreDFS(s) mark as visited?

- A. All the vertices
- B. All vertices except C & E
- C. None of the above

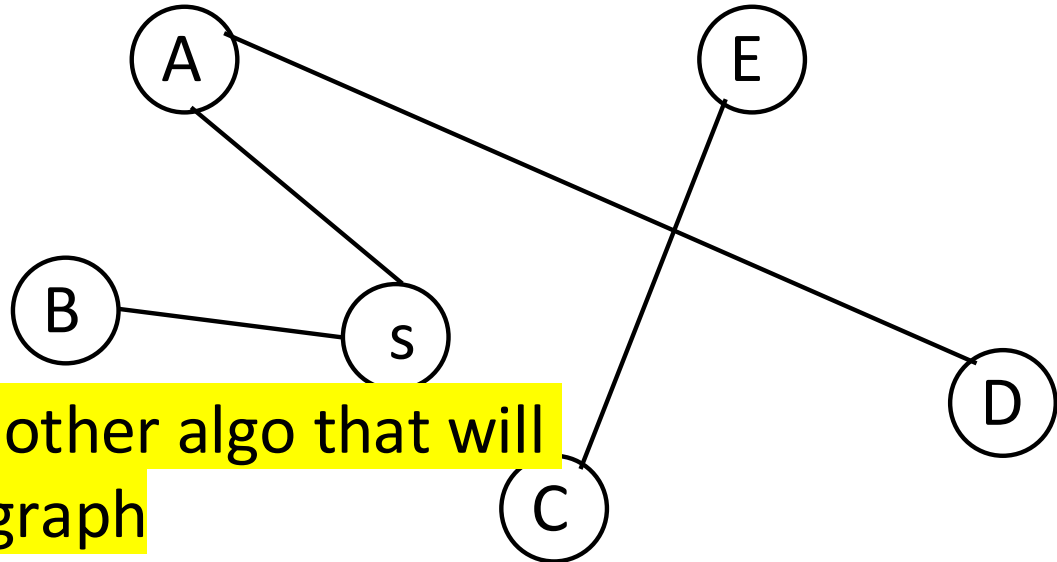




## Question: exploreDFS

Which vertices does exploreDFS(s) mark as visited?

- A. All the vertices
- B. All vertices except C & E
- C. None of the above



Use exploreDFS to write another algo that will visit all the vertices in this graph

# Depth First Search

`exploreDFS` only finds the part of the graph reachable from a single vertex. If you want to discover the entire graph, you may need to run it multiple times.

```
DepthFirstSearch(G)
```

```
    Mark all  $v \in G$  as unvisited
```

```
    For  $v \in G$ 
```

```
        If not  $v.visited$ , exploreDFS(v)
```

There are  $n$  rooms labeled from 0 to  $n - 1$  and all the rooms are locked except for room 0. Your goal is to visit all the rooms. However, you cannot enter a locked room without having its key.

When you visit a room, you may find a set of distinct keys in it. Each key has a number on it, denoting which room it unlocks, and you can take all of them with you to unlock the other rooms.

Given an array `rooms` where `rooms[i]` is the set of keys that you can obtain if you visited room  $i$ , return `true` if you can visit all the rooms, or `false` otherwise.

**Input:** `rooms = [[1],[2, 3],[1],[]]`

**Output:** ? *true*

*enter* → 0

0 1 2 3

↑

*[[], [1, 2, 3], [0]]*

0

<https://leetcode.com/problems/keys-and-rooms/description/>

**Input:** rooms = [[1],[2, 3],[1],[]]

**Output:** true      0      1      2      3

**Explanation:**

We visit room 0 and pick up key 1.

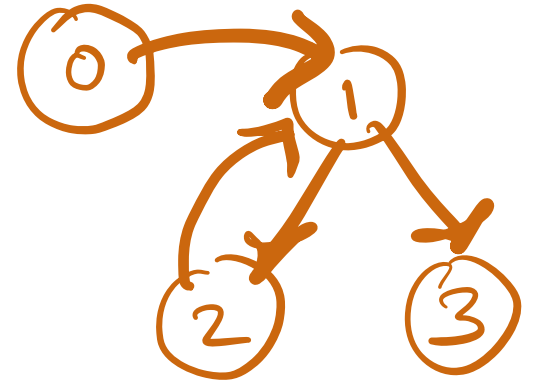
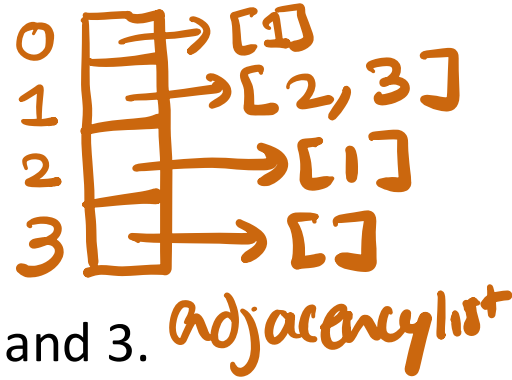
We then visit room 1 and pick up keys 2 and 3. *adjacency list*

We then visit room 2 and pick up key 1.

We then visit room 3.

Since we were able to visit every room, we return true.

Cast as a graph exploration problem



# Before next lecture...

Complete the preclass activities from last lecture if you haven't done so already.

- Review pa03 tutorial: <https://ucsb-cs24.github.io/s25/pa/pa03-tutorial/>
- Watch intro video on NN (3Blue1Brown) : <https://youtu.be/aircAruvnKk?feature=share>

Next lecture preclass activities:

- Watch videos from statQuest:
  - Neural Network Basics (great for understanding the prediction algorithm):  
<https://youtu.be/CqOfi41LfDw?si=8waS2U01uMWcpH2i>
  - Back Propagation (great for understanding the contribute algorithm):  
<https://youtu.be/IN2XmBhILt4?si=bnDft-3T4DQ2iO9X>
- Finish the PA03 “check your understanding assignment” on Gradscope.

# Acknowledgements

Slides on Depth First Search and animation from Prof. Daniel Kane at UC San Diego