

Name: (as it would appear on official course roster)		
UCSB email address:	@ucsb.edu	Perm ID Number:
Lab Section Time:		
Optional: name you wish to be called if different from above		
Optional: name of "homework buddy" (leaving this blank signifies "I worked alone")		

Lab 03: Introduction to Digital Logic

Assigned: *Wednesday, November 13th, 2019*

Due: *Wednesday, November 20th, 2019*

Points: 100

- You may collaborate on this homework with AT MOST one person, an optional "homework buddy".
- MAY ONLY BE TURNED ON **GRADESCOPE** as a **PDF file**.
- There is NO MAKEUP for missed assignments.
- We are strict about enforcing the LATE POLICY for all assignments (see syllabus).

1. In class, we went through the example of splitting a binary addition into single bit additions. This is simplest in terms of design time, but it does not lead to the fastest implementation. Instead, let's create a 2-bit adder as the smallest unit. In this case, there are four bits of input from the two numbers, in addition to the single input carry. There are two result bits and a single output carry. A0 is the least significant bit (the one on the right). inputs: A1, A0, B1, B0, Cin outputs: R0, R1, Cout. For example, if we are performing an addition, it looks like this:

```

      A1 A0
      B1 B0
        Cin
-----
Cout R1 R0

```

(Question on next page...)

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- a. Fill in this truth table for the function described above (16 pts)

[illegible]

- b. Write the unoptimized sum of products equations for **each** of the 3 outputs (12 pts)

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2. Given this truth table:

A	B	C	O
0	0	0	0
0	0	1	1
0	1	0	0
0	1	1	1
1	0	0	1
1	0	1	0
1	1	0	1
1	1	1	0

a. Write the unoptimized sum of products equation for the output **O** (4 pts)

3. Given this truth table:

A	B	C	D	O
0	0	0	0	1
0	0	0	1	1
0	0	1	0	1
0	0	1	1	1
0	1	0	0	1
0	1	0	1	0
0	1	1	0	0
0	1	1	1	0
1	0	0	0	1
1	0	0	1	0
1	0	1	0	0
1	0	1	1	0
1	1	0	0	1
1	1	0	1	0
1	1	1	0	0
1	1	1	1	0

a. Write the unoptimized sum of products equation for the output **O** (4 pts)

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4. Given this truth table:

A	B	C	D	O
0	0	0	0	0
0	0	0	1	0
0	0	1	0	0
0	0	1	1	0
0	1	0	0	1
0	1	0	1	1
0	1	1	0	0
0	1	1	1	0
1	0	0	0	0
1	0	0	1	0
1	0	1	0	0
1	0	1	1	0
1	1	0	0	1
1	1	0	1	1
1	1	1	0	0
1	1	1	1	1

- a. Write the unoptimized sum of products equation for the output **O** (4 pts)
5. For each problem use **Boolean algebra** to simplify the equation. SHOW YOUR WORK, one step per line. You should use only variable names, negation (use '!'), AND (by putting terms next to each other), OR (with '+'), and parentheses. In addition, each line should start with an equal sign (=). The first step has been done for you to show how.

$$\begin{aligned}
 \text{Example: } f(Z,Y,X) &= !ZY!X + ZY!X + !YX \\
 &= (!Z + Z)Y!X + !YX \\
 &= Y!X + !YX
 \end{aligned}$$

- a. $f(A,B,C) = !A!BC + A!B!C + !ABC + !AB!C + A!BC$ (6 pts)

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b. $f(A,B,C,D) = (A!D + !AC)(!B(C + BD))$ (6 pts)

c. $f(A,B,C,D) = (!A!C + AD)(B(D + !BC))$ (6 pts)

6. Given the following truth table:

A	B	C	D	O
0	0	0	0	0
0	0	0	1	1
0	0	1	0	0
0	0	1	1	0
0	1	0	0	1
0	1	0	1	0
0	1	1	0	1
0	1	1	1	0
1	0	0	0	0
1	0	0	1	1
1	0	1	0	0
1	0	1	1	0
1	1	0	0	0
1	1	0	1	0
1	1	1	0	0
1	1	1	1	0

a. Write the unoptimized sum of products equation for the output **O** (4 pts)

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b. Draw the K-map, mark it clearly (cleanly), and simplify the output function (4 pts)

c. Write the optimized sum of products equation for the output **O** (2 pts)

d. Draw the circuit for the optimized output function (3 pts)

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7. Given this truth table (and note the use of don't-cares, represented by **X**):

A	B	C	D	O
0	0	0	0	1
0	0	0	1	X
0	0	1	0	0
0	0	1	1	1
0	1	0	0	X
0	1	0	1	0
0	1	1	0	X
0	1	1	1	0
1	0	0	0	X
1	0	0	1	0
1	0	1	0	1
1	0	1	1	0
1	1	0	0	1
1	1	0	1	0
1	1	1	0	X
1	1	1	1	0

- Write the unoptimized sum of products equation for the output **O** (4 pts)
- Draw the K-map, mark it clearly (cleanly), and simplify the output function (4 pts)

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c. Write the **optimized** sum of products equation for the output **0** (2 pts)

d. Draw the circuit for the optimized output function (3 pts)

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8. The 8-input MUX can be constructed entirely with 2-input MUXes. I will start you out: put inputs A and B into one MUX and inputs C and D into another MUX. Continue on with E F and G H like this. This is the first stage of the solution. Now, decide how to reconcile the two results from those MUXes. Look hard at the logic for the 2-input MUX vs the 8-input MUX. Look at the discussion we've had in class (**Lecture 13**) on this.
- a. How many 2-input MUXes are needed to create an 8-input MUX? (2 pts)
 - b. How many select lines are needed? (2 pts)
 - c. Draw the circuit, using 2-input muxes as your building blocks. (4 pts)
9. Now think of a MUX that has 2^n inputs. All of your answers will have the variable n in them.
- a. How many select bits are there? (2 pts)
 - b. If it is implemented with 2-input MUXes, how many MUXes are there in the first stage? (2 pts)
 - c. How many 2-input MUXes are there in the second stage? (2 pts)
 - d. How many stages of 2-input MUXes are there? (2 pts)