

Recursive Functions

CS 8: Introduction to Computer Science, Winter 2019
Lecture #15

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Administrative

- HW 7 due today!
- Left to-do:
 - HW 8 for Wednesday
 - Lab 7 for today (by midnite)
 - Project for Thursday

FINAL IS COMING!



- Material: **Everything!**
- Homework, Labs, Lectures, Textbook
- **Wednesday, 3/20 in this classroom**
- **Starts at 8:00 AM **SHARP****
- ***Bring your UCSB IDs and arrive 10-15 minutes early***
- Duration: **3 hours long** (but really designed for 1.5 – 2 hours)
- Closed book: no calculators, no phones, no computers
- Allowed: 1 sheet (**single**-sided) of written notes
 - Must be no bigger than 8.5" x 11"
 - **You have to turn it in with the exam**
- **You will write your answers on the exam sheet itself.**



**STUDY
GUIDE NOW
ONLINE!**

Lecture Outline

- Recursive Functions
- Exercises

How *Do* Functions Work?

- Consider these 3 functions and tell me: what is **demo(-4)** ?

```
def demo(x):  
    return x + f(x)
```

```
def f(x):  
    return 11*g(x) + g(x/2)
```

```
def g(x):  
    return -1 * x
```

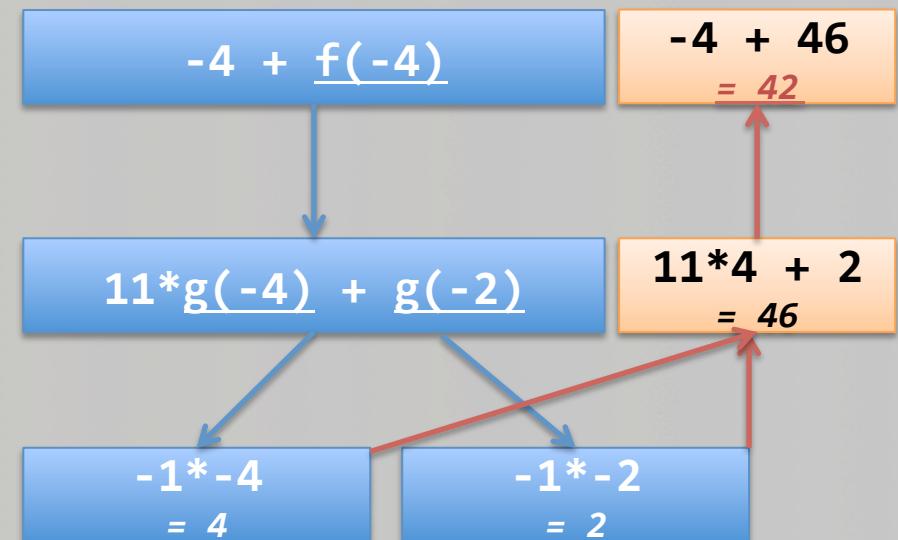
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What Keeps Track of All of This?!?

Ans: The Computer Memory Stack



- (1) keeps separate variables for each function call...
- (2) remembers where to send results back to...

*The stack is a special part of your computer's **memory**.*

*The **compiler** usually spells-out how the stack must be used with functions.*

**A child couldn't sleep,
so her mother told a story about a little frog,
who couldn't sleep,
so the frog's mother told a story about a little bear,
who couldn't sleep,
so bear's mother told a story about a little weasel
...who fell asleep.
...and the little bear fell asleep;
...and the little frog fell asleep;
...and the child fell asleep.**

Recursive Functions

- **Recursive: (adj.) Repeating unto itself**
- **A recursive function contains a call to itself**
- When breaking a task into subtasks, it may be
that the subtask is a smaller example of the same task
- Just like functions-calling-functions,
recursive functions make use of the stack

Simple Example: Factorial Function

Recall factorials:

$$2! = 1 * 2,$$

$$3! = 1 * 2 * 3,$$

$$4! = 1 * 2 * 3 * 4, \dots$$

$$N! = 1 * 2 * \dots * (N-1) * N$$

There's some repetition here... We could think of it as a loop
(how would you write that?)

```
def factorial(n):  
    f = 1  
    for m in range(1, n+1):  
        f = f * m  
    return f
```

Consider the Following...

```
def fac(N):  
    return N * fac(N-1)    # Yes, this is legal!  
print(fac(4))
```

What happens when `fac(4)` is called?

- A. It blows up! Does not compute! Does not compute!
- B. It returns the correct result (i.e. 24)
- C. The execution never stops (i.e. infinite loop)  ANS
- D. It produces a return value but that value is incorrect (i.e. not 24)

Just ‘Cause It’s Legal, Doesn’t Mean It’s Good Code!!!

```
def fac(N):  
    return N * fac(N-1)    # Yes, this is legal!
```

This goes on and on into an infinite loop!

Q: Why?

A: It’s missing a “base case”
(a.k.a a “stopping case”)

Q2: What’s a good “base case” here?



Base Case

```
def fac(N):  
    if N <= 1:  
        return 1  
    else:  
        return N * fac(N-1)
```

- Recursive functions should know **when to stop**
- There must be (at least) one **base case**, and the recursive step must converge on a base case, otherwise you get an “***infinite recursion***”

Under the Hood...

```
>>> fac(1)
```

I get:

1 # easy-peasy

```
>>> fac(5)
```

→ 5 * fac(4)
→ 5 * (4 * fac(3))
→ 5 * (4 * (3 * fac(2)))
→ 5 * (4 * (3 * (2 * fac(1))))
→ 5 * (4 * (3 * (2 * 1)))

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```
def fac(N):  
    if N <= 1:  
        return 1  
    else:  
        return N * fac(N-1)
```

*Every step, the new values are put into the **STACK** and kept track of by the computer*

= 120

Exercise

- What does **MyRecFun(3)** do?

```
def MyRecFun(n):  
    if n == 0:  
        return 2  
    else:  
        return 2*MyRecFun(n-1)
```

Another Example: Mathematical Series

- Popular example: Fibonacci Series

$$F(n) = 1, 1, 2, 3, 5, 8, 13, \dots, F(n-1) + F(n-2)$$

- There's some repetition here...

We could think of it as a loop also

- Or we could think of it as a recursive function!

Fibonacci Recursion

- What is/are the BASE CASE(S)?
- What is the recursive formula?

```
def fibo(n):
    if n == 0:
        return 0
    if n == 1:
        return 1
    else: # is this else necessary?
        return fibo(n-1) + fibo(n-2)
```

DEMO
TIME!

YOUR TO-DOS

- HW8 (due on Wednesday, 3/13)
- Lab7 (due on Monday, 3/11)
- Project Assignment (due on Thursday, 3/14)



</LECTURE>