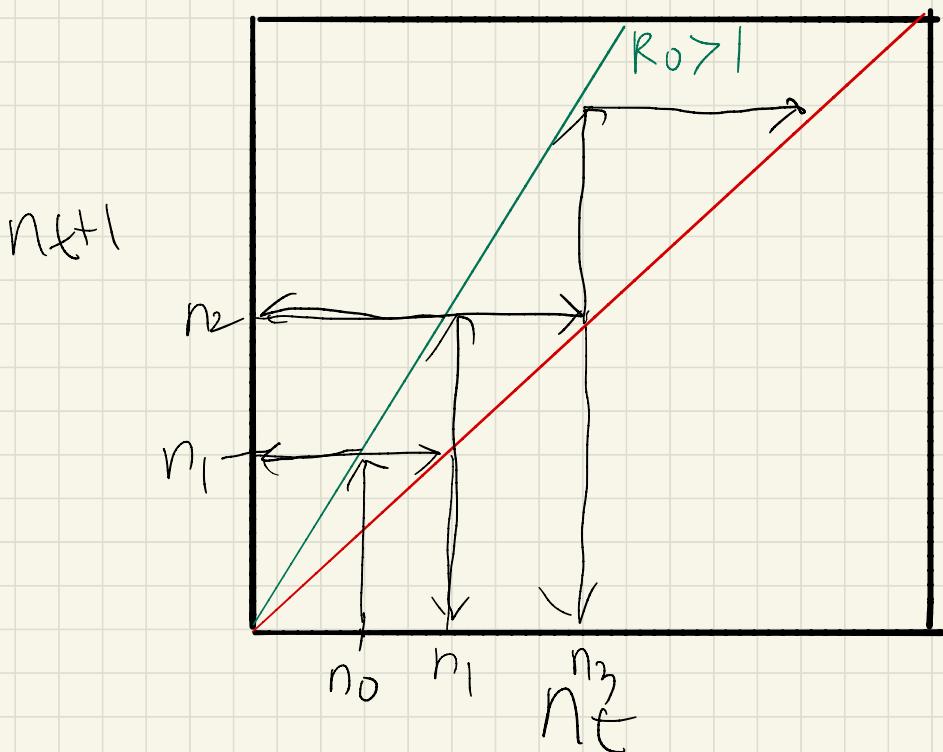
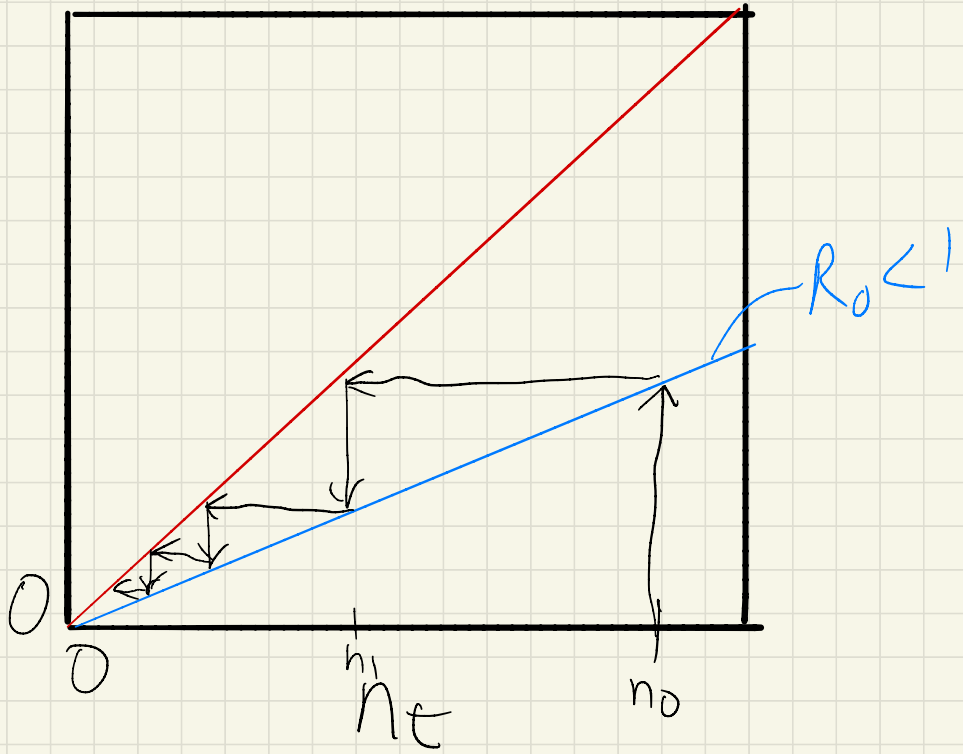


Graphing Recursions and Stability Analysis

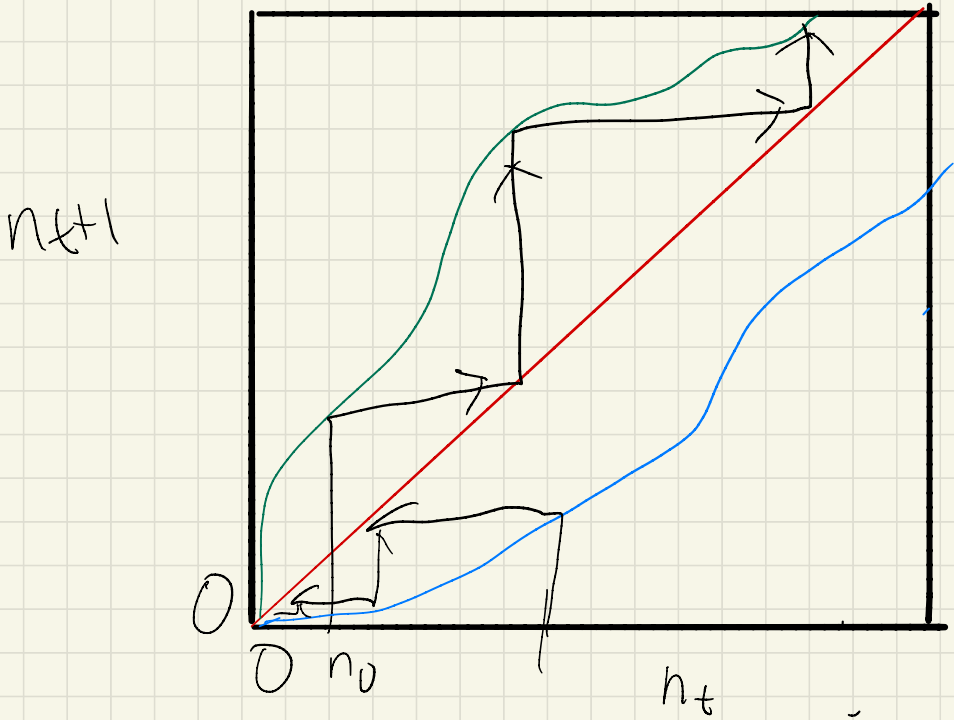
$$n_{t+1} = n_t R_0$$

$$n_{t+1} - n_t = n_t R_0 - n_t = n_t (R_0 - 1)$$



$$n+1$$


$$n_{t+1} = f(n_t)$$

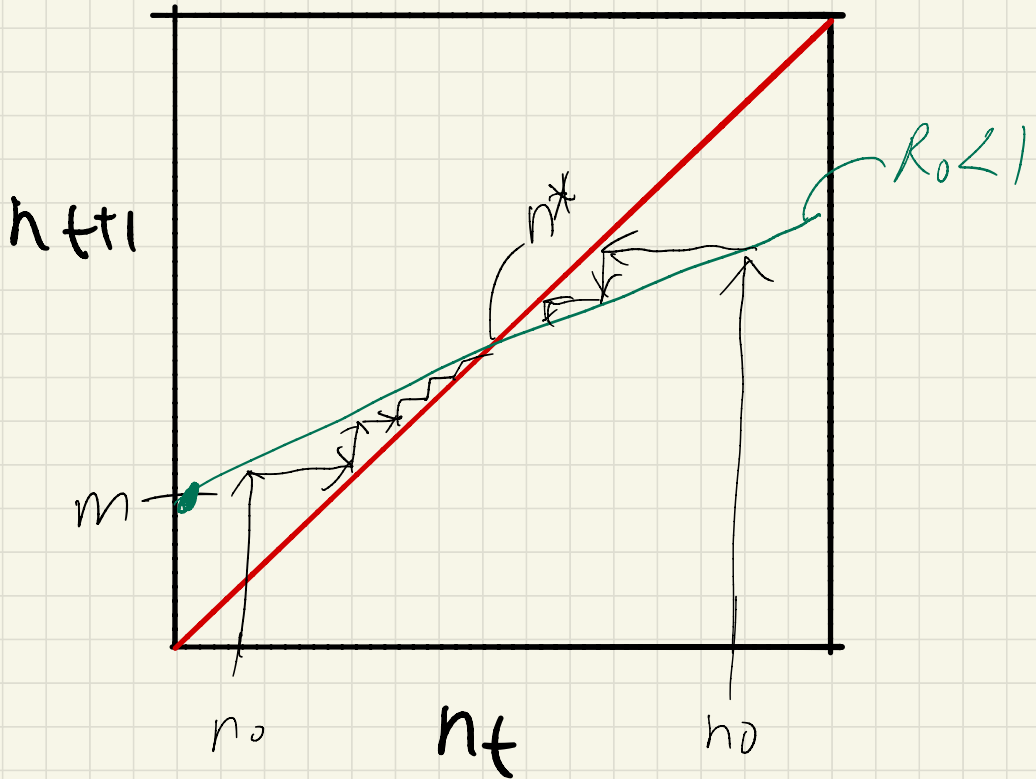


if $f'(0) > 1 \Rightarrow n$ goes up: unstable

if $0 < f'(0) < 1 \Rightarrow n$ goes down: stable

$m \equiv \# \text{ immigrants}$

$$n_{t+1} = n_t R_0 + m$$



$$n_t = \underbrace{(n_t R_0)} + m \Rightarrow n_t(1 - R_0) = m$$

$$n_t = \frac{m}{1 - R_0} \Rightarrow n^* = \frac{m}{1 - R_0}$$

$$n_{t+1} = f(n_t)$$

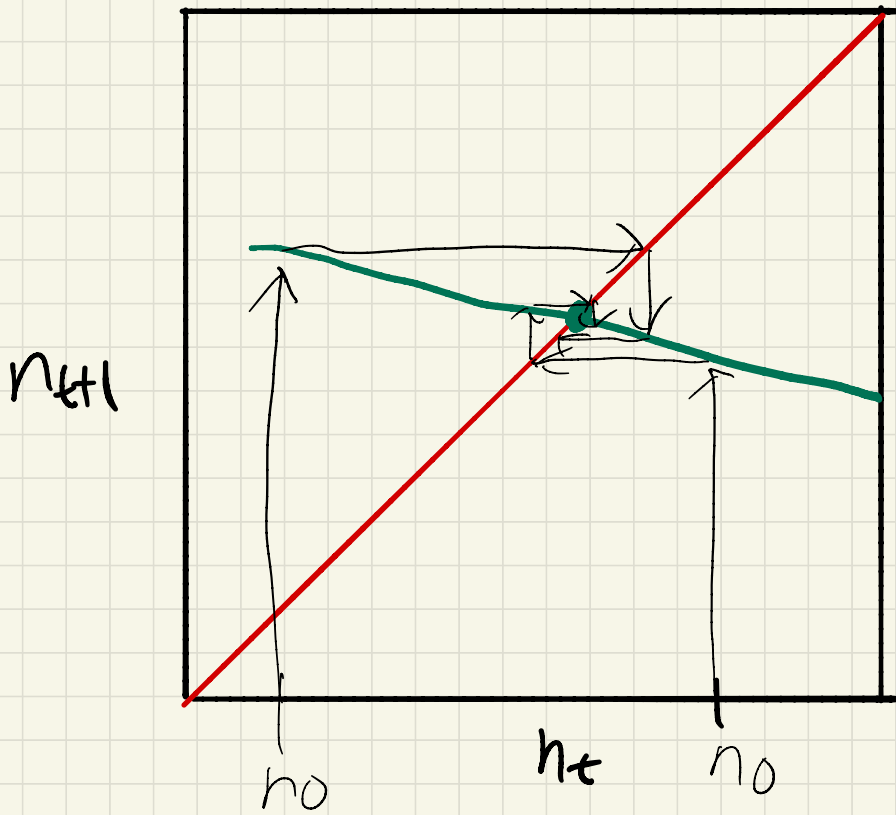
$$f(n^*) = n^*$$

$$\lambda = f'(n^*)$$

if $1 < \lambda < \infty$ then unstable

$0 < \lambda < 1$ then stable

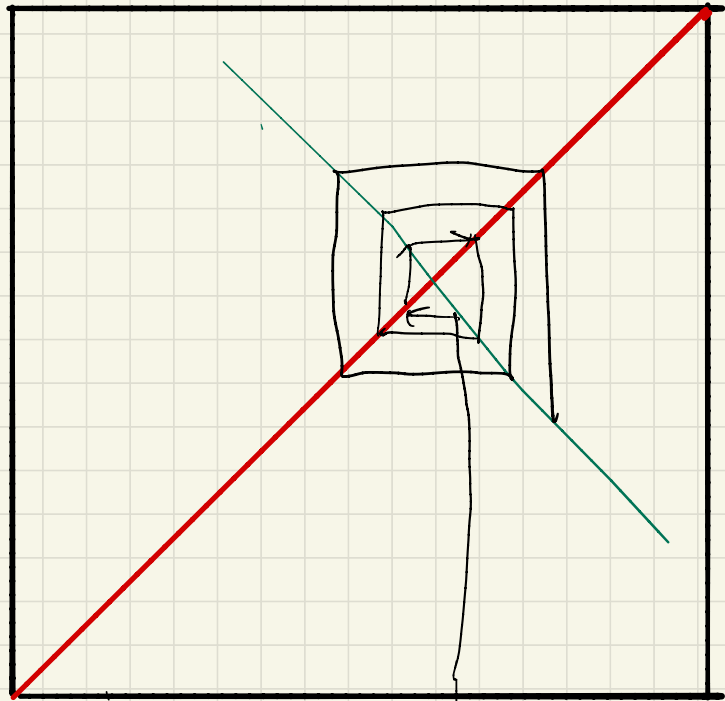
$$n_{t+1} = f(n_t)$$



$-1 < \lambda < 0$ oscillate ; stable

$$n_{t+1} = f(n_t)$$

n_{t+1}

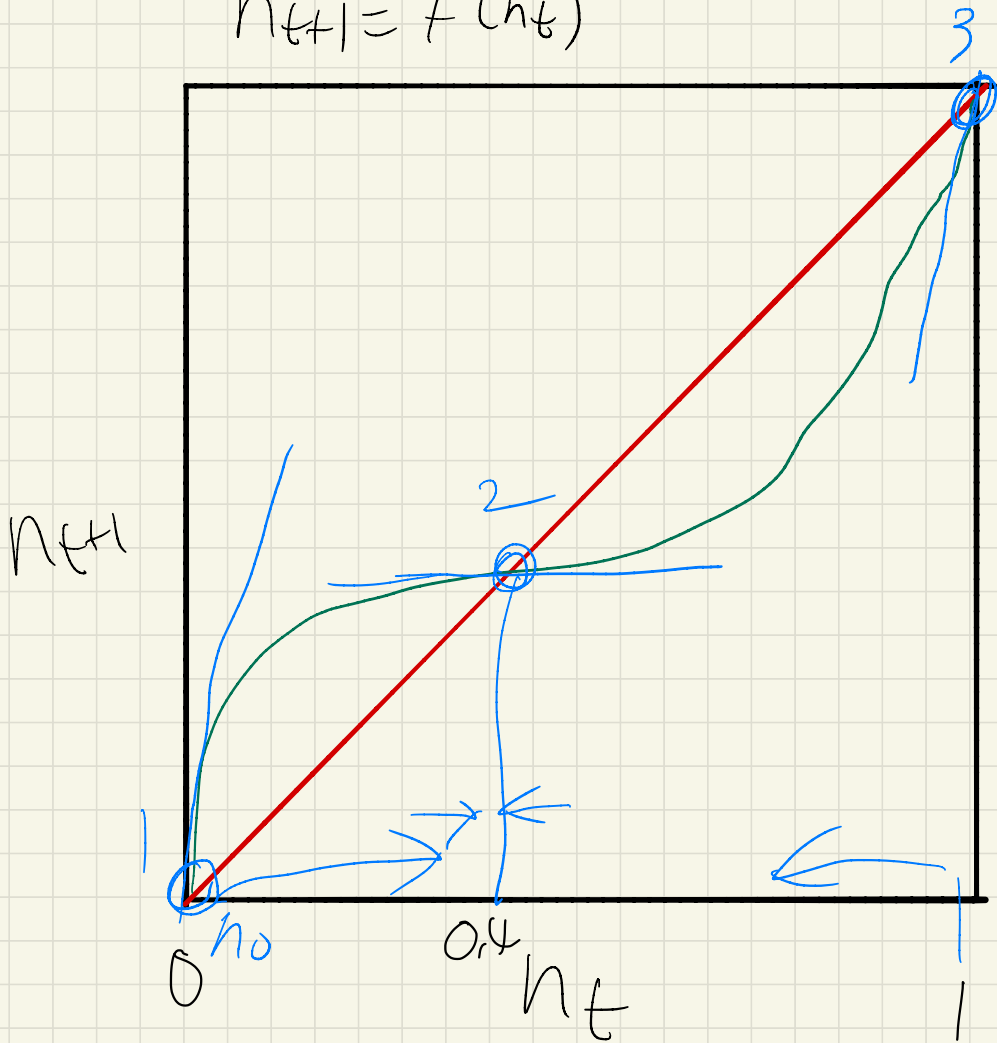


n_t no

$-2 < \lambda < -1$ oscillates ; unstable

λ		stable?	oscillates?
above	below		
1	∞	No	No
0	1	Yes	No
-1	0	Yes	Yes
$-\infty$	-1	No	Yes

$$n_{t+1} = f(n_t)$$



Read off the equilibria
Check the slope

eq #	n_i^*	λ	stable?
1	0	> 1	No
2	0.4	$0 < \lambda < 1$	yes
3	1	$\lambda > 1$	No