

Tree branching

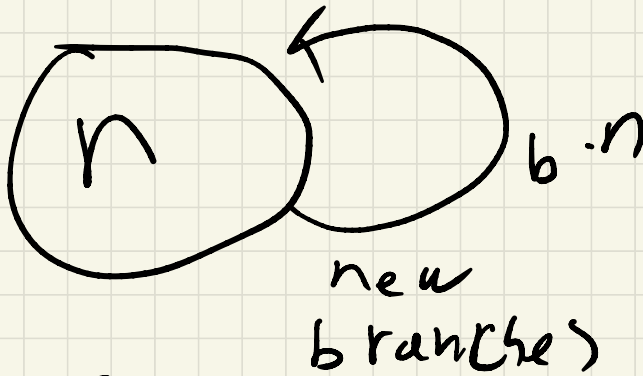


$n_t \equiv \# \text{ of branches}$

$t \equiv \text{time}$

$b \equiv \text{chance that branch splits}$

Flow Diagram

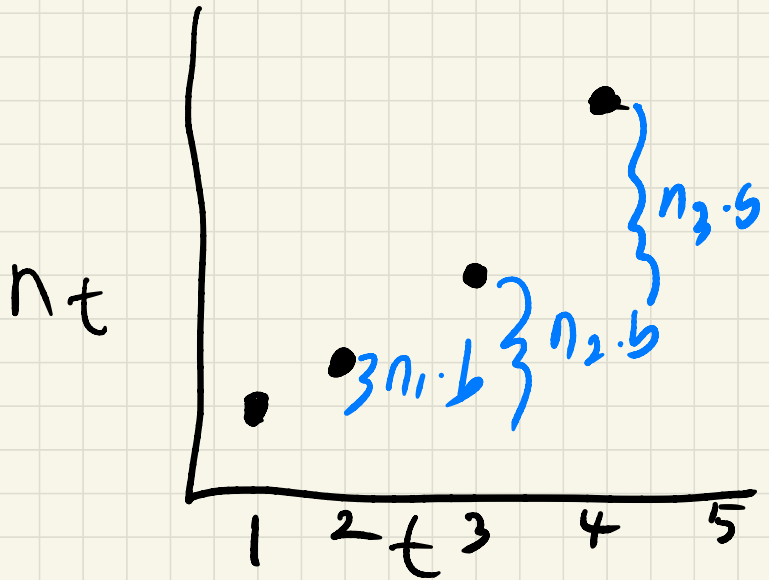


Assumptions?
All branches act the same

so

$$n_{t+1} = n_t + n_t \cdot b$$

How does n change?



$$n_{t+1} = n_t + b \cdot n_t = (1+b)n_t$$

if at $t=0$ $n = n_0$

$$n_1 = n_0(1+b)$$

$$n_2? \Rightarrow n_2 = n_1 \cdot (1+b)$$

$$n_2 = n_0(1+b)(1+b)$$

$$n_2 = n_0(1+b)^2$$

if at $t=0$ $n = n_0$

$$n_1 = n_0(1+b)$$

$$n_2? \Rightarrow n_2 = n_1 \cdot (1+b)$$

$$n_2 = n_0(1+b)(1+b)$$

$$n_2 = n_0(1+b)^2$$

$$n_3 = n_2(1+b) \Rightarrow n_3 = n_0(1+b)^3$$

So

$$n_t = n_0(1+b)^t$$

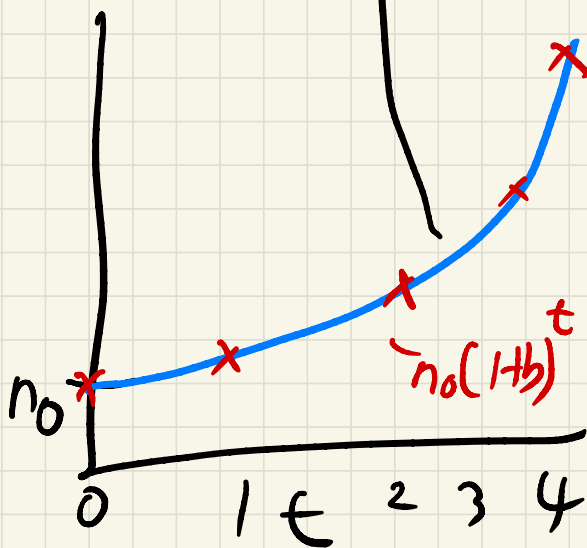
|||
Geometric Growth
Also

$$\Delta n = b \cdot n \cdot t$$

Continuous time and n
(for comparison)

$$\frac{dn}{dt} = n \cdot B \Rightarrow n(t) = n_0 e^{Bt}$$

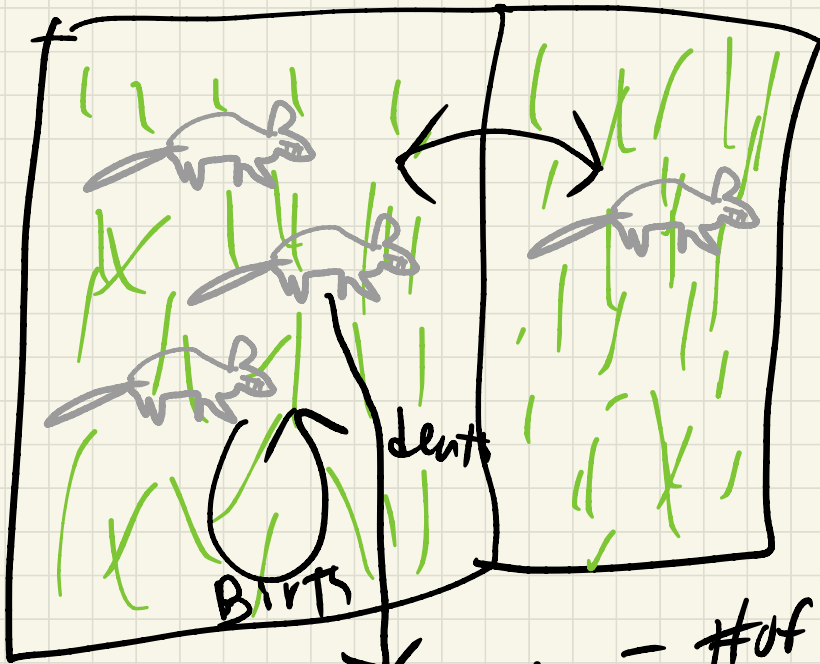
$$B = \log(1+b)n$$



So $B > 0$ or

$b > 0 \Rightarrow n$ grows over
time!

Backyard Mice

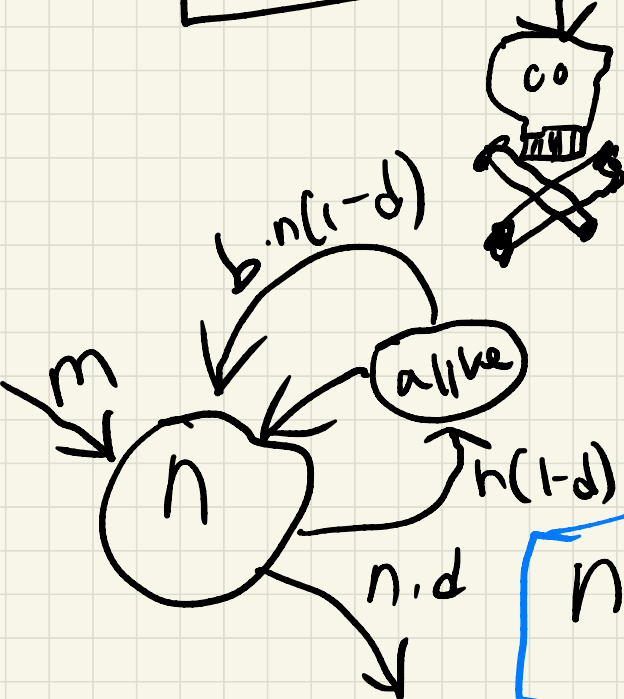


$n \equiv \# \text{ of } \text{mouse}$

$b \equiv \text{birth}$

$m \equiv \text{migration}$

$d \equiv \text{deaths}$



$$n_{t+1} = n_t(1-d)(1+b) + m$$

$$n_{t+1} = n_t(1-d)(1+b) + m$$

if $m=0$

$$n_t = n_0 [(1-d)(1+b)]^t$$