CSE 11 Accelerated Intro to Programming Lecture 7

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Announcements

- PA3 due tonight @ 11:59pm
- PA4 due Sunday @ 11:59pm
- → PA0.5 and PA1 resubmissions due tomorrow @ 11:59pm
- Quiz 3 due tomorrow @ 11:59pm
 - Make-up Lecture tomorrow same time, same zoom link

Both classes have a method with the **same header**

We can write an **interface** with the shared method

```
Method
interface Region {
boolean contains(Point p);
}
```

```
class CircleRegion
                                    class SquareRegion
  implements Region {
                                      implements Region {
  public boolean contains(Point p)
                                      public boolean contains(Point p)
```

Both classes have a method with the **same header**

We can write an **interface** with the shared method

```
interface Region {
                       boolean contains(Point p);
class CircleRegion.
                                    class.SquareRegion
  implements Region {
                                      implements Region {
  public boolean contains(Point p)
                                      public boolean contains(Point p)
```

Both classes have a method with the same header

```
interface Region {
public boolean contains(Point p);
}
```

```
class CircleRegion
  implements Region {
    impl
```

```
class ExamplesRegion {
  Region circ = new CircleRegion(new Point(10, 5), 4));
  Region square = new SquareRegion(new Point(5, 6), 8));
}
```

We can use the same

interface type

for references of classes that implement it

```
implements Region {
                                                  implements Region {
                Point center;
                                                  Point center;
                int radius
                                                  int sideLength;
                public boolean contains(Point p)
                                                  public boolean contains(Point p)
                { ... }
                                                  { ... }
                     class ExamplesRegion {
                        Region circ = new CircleRegion(new Point(10, 5), 4));
                       Region square = new SquareRegion(new Point(5, 6), 8));
                        int num = circ.radius;
                                                     A: 10 50:5
                       What is stored in
                                                     O B. 8 (2D) it's an error
                        the num field?
Using an interface, we can 7 E: something else only use methods on the interface 49?
```

boolean contains(Point p);

class SquareRegion

interface Region {

class CircleRegion

```
interface Region {
                      boolean contains(Point p);
class CircleRegion
                                   class SquareRegion
  implements Region {
                                     implements Region {
  Point center;
                                     Point center;
  int radius
                                     int sideLength;
  public boolean contains(Point p)
                                     public boolean contains(Point p)
  { ... }
                                     { ... }
       class ExamplesRegion {
         Region circ = new CircleRegion(new Point(10, 5), 4);
         Region square = new SquareRegion(new Point(5, 6), 8);
         boolean contains1 = circ.contains(new Point(7, 6));
                                     13(A)true 22: error
         What is stored in
       the contains 1 field?
```

```
boolean contains(Point p);
class CircleRegion
                                    class SquareRegion
  implements Region {
                                      implements Region {
  public boolean contains(Point p)
                                      public boolean contains(Point p)
  { ... }
class UnionRegion {
  Region r1, r2;
  UnionRegion(Region r1, Region r2) { ... }
  public boolean contains(Point p) {
    return this.r1.contains(p) ||
           this.r2.contains(p);
```

interface Region {

```
boolean contains(Point p);
class CircleRegion
                                   class SquareRegion
 implements Region {
                                     implements Region {
 public boolean contains(Point p)
                                     public boolean contains(Point p)
 { ... }
                                              What is the value of
class UnionRegion {
                                                   the bl field?
 Region r1, r2;
 UnionRegion(Region r1, Region r2) { ... }
 public boolean contains(Point_p) {
                                               (A:)true 🗸 Z: error
    return this.r1.contains(p)(||`
           this.r2.contains(p);
                                               B: false
class ExamplesRegion {
 Region circ = new CircleRegion(new Point(10, 5), 4);
 Region square = new SquareRegion(new Point(5, 6), 8);
 UnionRegion ur = new UnionRegion(this.square, this.circ);
 boolean b1 = this.ur.contains(new Point(13, 5));
```

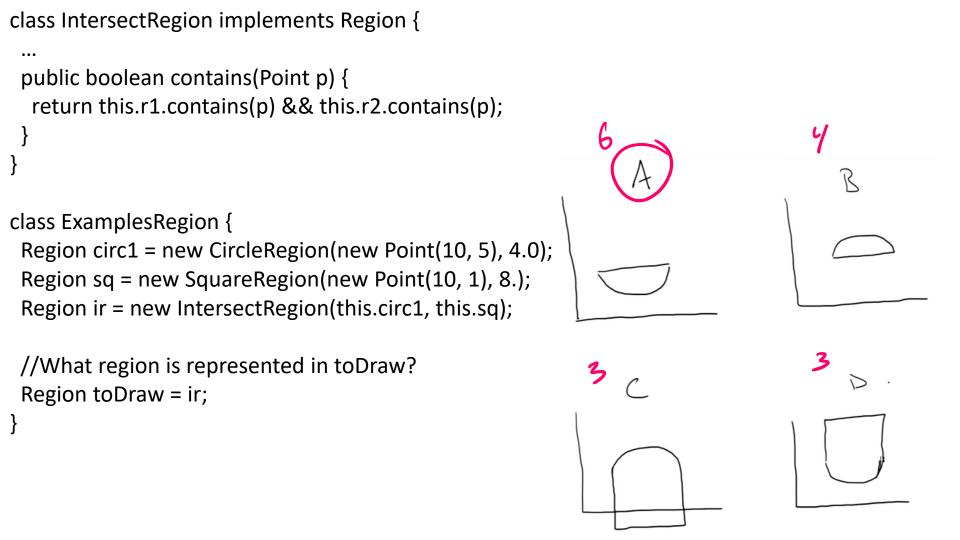
interface Region {

Using Interfaces

- Add Region interface
- Update RectRegion & CircRegion

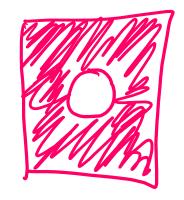
Intersect Region

```
interface Region {
 boolean contains(Point p);
                                   class IntersectRegion implements Region {
                                    Region r1;
                                    Region r2;
                                    IntersectRegion(Region r1, Region r2) {
                                      this.r1 = r1;
                                      this.r2 = r2;
                                    public boolean contains(Point p) {
                                      return this.r1.contains(p) && this.r2.contains(p);
```



SubtractRegion

- Write a new class called SubtractRegion
 - That also implements Region
- Represents all the points in region1 that aren't in region2
 - Start with a shape and subtract another shape from it XOr
 - Subtract a circle from another circle to create a ring
- Write the class
 - Fields and constructor
 - What does the contains method look like?







Something more complicated

- What if we wanted a region that was 3 circles next to each other:
- How could we construct an example of this?

Inheritance

- New terms
 - abstract class
 - extends

Abstract Class Summary

- Why did we introduce abstract classes?
 - Multiple classes had the exact same method
 - Same method header (same types)
 - Same implementation
 - add() method put into all the region classes
 - Same implementation in all of them
 - Made an abstract class
 - Had one implementation of that method
 - Used extends so that all of the implementations could share that one method

```
private double x, y;
  Point(double x, double y) { this.x = x; this.y = y; }
  double distance(Point other) {
     return Math.sqrt(
       Math.pow(this.x - other.x, 2) + Math.pow(this.y - other.y, 2));
  double xDistance(Point other) { return Math.abs(other.x - this.x); }
double yDistance(Point other) { return Math.abs(other.y - this.y); }
interface Region {
 boolean contains(Point p);
Region ald(Region other);
Region overlap(Region other);
public Region add(Region other) {
  return new UnionRegion(this, other);
  public Region overlap(Region other) {
     return new IntersectRegion(this, other);
class UnionRegion extends ARegion {
  Region region1, region2;
UnionRegion(Region region1, Region region2) {
this.region1 = region1;
this.region2 = region2;
  public boolean contains(Point toCheck) {
     return this.region1.contains(toCheck) ||
             this.region2.contains(toCheck);
class IntersectRegion extends ARegion {
  Region region1, region2;
  IntersectRegion(Region region1, Region region2) {
     this.region1 = region1;
this.region2 = region2;
  public boolean contains(Point toCheck) {
  return this.region1.contains(toCheck) &6
    this.region2.contains(toCheck);
class SubtractRegion implements Region {
  Region region1;
  Region region2;
  SubtractRegion(Region region1, Region region2) {
     this.region1 = region1;
this.region2 = region2;
  public boolean contains(Point toCheck) {
    return this.region1.contains(toCheck) && !this.region2.contains(toCheck);
class SquareRegion extends ARegion {
  Point center;
double sideLength;
  SquareRegion(Point center, double sideLength) {
     this.center = center;
     this.sideLength = sideLength;
  public boolean contains(Point toCheck) {
     return this.center.xDistance(toCheck) <= (this.sideLength / 2) 66
              this.center.vDistance(toCheck) <= (this.sideLength / 2);
class CircleRegion extends ARegion {
  Point center;
  double radius;
  CircleRegion(Point center, double radius) {
     this.center = center;
     this.radius = radius;
  public boolean contains(Point toCheck) {
     return this.center.distance(toCheck) <= this.radius;
class ExamplesARegion {
  Region circ1 = new CircleRegion(new Point(10, 5), 4.0);
  Region sq = new SquareRegion(new Point(10, 1), 8.0);
Region ir = this.circl.add(this.sq);
```

ctass roint

```
private double x, y;
  Point(double x, double y) { this.x = x; this.y = y; }
  double distance(Point other) {
    return Math.sqrt(
      Math.pow(this.x - other.x, 2) + Math.pow(this.y - other.y, 2));
  double xDistance(Point other) { return Math.abs(other.x - this.x); }
double yDistance(Point other) { return Math.abs(other.y - this.y); }
interface Region {
 boolean contains(Point p);
Region add(Region other);
Region overlap(Region other);
public Region add(Region other) {
  return new UnionRegion(this, other);
  public Region overlap(Region other) {
    return new IntersectRegion(this, other);
class UnionRegion extends ARegion {
 Region region1, region2;
UnionRegion(Region region1, Region region2) {
this.region1 = region1;
    this.region2 = region2;
  public boolean contains(Point toCheck) {
    return this.region1.contains(toCheck) ||
            this.region2.contains(toCheck);
class IntersectRegion extends ARegion {
  class SubtractRegion implements Region {
   Region region1
   Region region2:
  public boolean contains(Point toCheck) {
    return this.region1.contains(toCheck) &&!this.region2.contains(toCheck);
class SquareRegion extends ARegion {
  Point center;
double sideLength;
  SquareRegion(Point center, double sideLength) {
    this.center = center;
     this.sideLength = sideLength;
  public boolean contains(Point toCheck) {
    return this.center.xDistance(toCheck) <= (this.sideLength / 2) 66
             this.center.vDistance(toCheck) <= (this.sideLength / 2);
class CircleRegion extends ARegion {
  Point center;
  double radius;
  CircleRegion(Point center, double radius) {
    this.center = center;
    this.radius = radius;
  public boolean contains(Point toCheck) {
     return this.center.distance(toCheck) <= this.radius;
class ExamplesARegion {
  Region circ1 = new CircleRegion(new Point(10, 5), 4.0);
  Region sq = new SquareRegion(new Point(10, 1), 8.0);
Region ir = this.circl.add(this.sq);
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ctass roint

```
private double x, y;
  Point(double x, double y) { this.x = x; this.y = y; }
  double distance(Point other) {
    return Math.sqrt(
     Math.pow(this.x - other.x, 2) +
     Math.pow(this.y - other.y, 2));
                                                                                                          class UnionRegion extends ARegion {
 double xDistance(Point other) { return Math.abs(other.x - this.x); }
double yDistance(Point other) { return Math.abs(other.y - this.y); }
                                                                                                              Region r1, r2;
interface Region {
                                                                                                              UnionRegion(Region r1, Region r2) {
 boolean contains(Point p);
  Region add(Region other);
                                                                                                                  this.r1 = r1:
 Region overlap(Region other);
abstract class ARegion implements Region {
  public Region add(Region other) {
                                                                                                                  this.r2 = r2:
    return new UnionRegion(this, other);
  public Region overlap(Region other) {
    return new IntersectRegion(this, other);
class UnionRegion extends ARegion {
 Region region1, region2;
UnionRegion(Region region1, Region region2) {
  this.region1 = region1;
  public boolean contains(Point toCheck) {
   return this.region1.contains(toCheck) ||
          this.region2.contains(toCheck);
class IntersectRegion extends ARegion {
  IntersectRegion(Region region1, Region region2)
  public boolean contains(Point toCheck) {
  return this.region1.contains(toCheck) &&
          this.region2.contains(toCheck);
class SubtractRegion implements Region {
  SubtractRegion(Region region1, Region region2) {
                                                                                                           Region r1, r2;
  public boolean contains(Point toCheck) {
   return this.region1.contains(toCheck) &&
           !this.region2.contains(toCheck);
                                                                                                                this.r1 = r1;
                                                                                                                 this.r2 = r2;
class SquareRegion extends ARegion {
  Point center;
  double sideLength;
  SquareRegion(Point center, double sideLength) {
   this.center = center;
    this.sideLength = sideLength;
 public boolean contains(Point toCheck) {
   return this.center.xDistance(toCheck) <= (this.sideLength / 2) &&
          this.center.yDistance(toCheck) <= (this.sideLength / 2):
                                                                                                                                  this.r2.contains(p);
class CircleRegion extends ARegion {
 Point center:
  double radius
  CircleRegion(Point center, double radius) {
   this.center = center;
    this.radius = radius:
  public boolean contains(Point toCheck) {
    return this.center.distance(toCheck) <= this.radius;
class ExamplesARegion {
 Region circ1 = new CircleRegion(new Point(10, 5), 4.0);
 Region sq = new SquareRegion(new Point(10, 1), 8.0);
  Region ir = this.circl.add(this.sg);
```

ctass roint

```
public boolean contains(Point p) {
      return this.r1.contains(p) &&
             this.r2.contains(p);
class IntersectRection extends ARegion {
  IntersectRegion(Region r1, Region r2) {
  public boolean contains(Point p) {
     return this.rl.contains(p) ||
```

```
private double x, y;
 Point(double x, double y) { this.x = x; this.y = y; }
  double distance(Point other) (
   return Math.sgrt[
     Math.powithis.x - other.x, 21 -
     Math.pow(this.y - other.y, 21);
                                                                                                 class UnionRegion extends ARegion {
 double xDistance(Point other) { return Math.abs(other.x - this.x); } double yDistance(Point other) { return Math.abs(other.y - this.y); }
                                                                                                     Region r1, r2;
interface Region {
                                                                                                     UnionRegion(Region r1, Region r2) {
 boolean contains(Point p);
  Region add(Region other);
                                                                                                         this.r1 = r1:
 Region overlap(Region other);
                                                                                                         this.r2 = r2:
abstract class ARegion implements Region (
public Region add(Region other) {
   return new UnionRegion(this, other);
  public Region overlap(Region other) {
                                                                                                      public boolean contains(Point p) {
   return new IntersectRegion(this, other);
                                                                                                            return this.rl.contains(p) &&
class UnionRegion extends ARegion
 Region region1, region2;
UnionRegion(Region region1, Region region2)
this.region1 = region1;
                                                                                                                          this.r2.contains(p);
  public boolean contains(Point toCheck) (
   return this.region1.contains(toCheck) ||
          this, region2.contains(toCheck);
class IntersectRegion extends ARegion {
 public boolean contains(Point toCheck) {
  return this.region1.contains(toCheck) 66
          this.region2.contains(toCheck);
class SubtractRegion implements Region (
                                                                                               Slass IntersectRection extends ARegion {
  SubtractRegion(Region region], Region region2) (
   this.region1 = region1;
this.region2 = region2;
                                                                                                   Region r1, r2;
  public boolean contains(Point toCheck) {
                                                                                                   IntersectRegion(Region r1, Region r2)
   return this.region1.contains(toCheck) 66
          !this.region2.contains(toCheck);
                                                                                                        this.r1 = r1:
class SquareRegion extends ARegion (
                                                                                                        this.r2 = r2:
 double sideLength;
  SquareRegion(Point center, double sideLength) (
   this center = center;
                                                                                                   public boolean contains(Point p) {
   this.sideLength = sideLength;
  public boolean contains(Point toCheck) (
                                                                                                         return this.rl.contains(p) ||
   return this,center.xDistance(toCheck) <= (this,sideLength / 2) 66
          this.center.yDistance(toCheck) <= (this.sideLength / 2);
                                                                                                                        this.r2.contains(p);
class CircleRegion extends ARegion (
 Point center:
  double radius:
  CircleRegion(Point center, double radius) (
   this.center = center;
   this.radius = radius;
  public boolean contains(Point toCheck) (
   return this.center.distance(toCheck) <= this.radius;
class ExamplesARegion {
 Region circl = new CircleRegion(new Point(10, 5), 4,0);
 Region sq n new SquareRegion(new Point(18, 1); 8.8);
  Region ir = this, circl, add(this, sq);
```

```
class UnionRegion extends ARegion
                                                     public boolean contains(Point p) {
                                                        return this.r1.contains(p) &&
                                                               this.r2.contains(p);
abstract class AComboRegion
  Region r1, r2;
  AComboRegion(Region r1, Region r2) {
    this.r1 = r1;
    this.r2 = r2;
                                                   class IntersectRection extends ARegion
                                                     public boolean contains(Point p) {
                                                        return this.r1.contains(p) ||
```

this.r2.contains(p);

```
class UnionRegion
                                                     public boolean contains(Point p) {
                                                        return this.r1.contains(p) &&
                                                               this.r2.contains(p);
abstract class AComboRegion extends ARegion {
  Region r1, r2;
  AComboRegion(Region r1, Region r2) {
    this.r1 = r1;
    this.r2 = r2;
                                                   class IntersectRection
                                                     public boolean contains(Point p) {
                                                        return this.r1.contains(p) ||
                                                               this.r2.contains(p);
```

class IntersectRection extends AComboRegion

this.r2 = r2;

```
class UnionRegion extends AComboRegion
                                                     UnionRegion(Region r1, Region r2) {
                                                       super(r1, r2);
                                                     public boolean contains(Point p) {
                                                        return this.rl.contains(p) &&
                                                               this.r2.contains(p);
abstract class AComboRegion extends ARegion {
 Region r1, r2;
 AComboRegion(Region r1, Region r2) {
    this.r1 = r1:
    this.r2 = r2;
                                                   class IntersectRection extends AComboRegion
                                                     IntersectRegion(Region r1, Region r2) {
                                                       super(r1, r2);
                                                     public boolean contains(Point p) {
                                                        return this.r1.contains(p) ||
                                                               this.r2.contains(p);
```

```
interface Region { ... }
abstract class ARegion implements Region { ... }
class SquareRegion extends ARegion { ... }
class CircleRegion extends ARegion { ... }
abstract class AComboRegion extends ARegion {
  Region r1, r2;
  AComboRegion(Region r1, Region r2) {
    this.r1 = r1;
    this.r2 = r2;
class UnionRegion extends AComboRegion {
  UnionRegion(Region r1, Region r2) {
    super(r1, r2);
  public boolean contains(Point p) {
      return this.r1.contains(p) &&
            this.r2.contains(p);
class ExamplesRegion {
  Region sq = new SquareRegion(new Point(4, 5), 8);
  Region ci = new CircleRegion(new Point(6, 7), 10);
  Region ur = new UnionRegion(this.sq, this.ci);
```

```
abstract class ARegion implements Region { ... }
class SquareRegion extends ARegion { ... }
class CircleRegion extends ARegion { ... }
abstract class AComboRegion extends ARegion {
  Region r1, r2;
  AComboRegion(Region r1, Region r2) {
    this.r1 = r1;
    this.r2 = r2;
class UnionRegion extends AComboRegion {
  UnionRegion(Region r1, Region r2) {
    super(r1, r2);
  public boolean contains(Point p) {
      return this.r1.contains(p) &&
            this.r2.contains(p);
                                                                                SquareRegion
class ExamplesRegion {
 Region sq = new SquareRegion(new Point(4, 5), 8);
  Region ci = new CircleRegion(new Point(6, 7), 10);
  Region ur = new UnionRegion(this.sq, this.ci);
                                                                                 CircleRegion
```

interface Region { ... }

```
interface Region { ... }
                                                                              ExamplesRegion
abstract class ARegion implements Region { ... }
class SquareRegion extends ARegion { ... }
class CircleRegion extends ARegion { ... }
                                                                                sq
abstract class AComboRegion extends ARegion {
                                                                                ci
  Region r1, r2;
  AComboRegion(Region r1, Region r2) {
                                                                                ur
    this.r1 = r1;
    this.r2 = r2;
class UnionRegion extends AComboRegion {
  UnionRegion(Region r1, Region r2) {
    super(r1, r2);
  public boolean contains(Point p) {
      return this.r1.contains(p) &&
             this.r2.contains(p);
                                                                                 SquareRegion
class ExamplesRegion {
  Region sq = new SquareRegion(new Point(4, 5), 8);
  Region ci = new CircleRegion(new Point(6, 7), 10);
  Region ur = new UnionRegion(this.sq, this.ci);
                                                                                  CircleRegion
```

```
interface Region { ... }
                                                                              ExamplesRegion
abstract class ARegion implements Region { ... }
class SquareRegion extends ARegion { ... }
class CircleRegion extends ARegion { ... }
                                                                                sq
abstract class AComboRegion extends ARegion {
                                                                                ci
  Region r1, r2;
  AComboRegion(Region r1, Region r2) {
                                                                                ur
    this.r1 = r1:
    this.r2 = r2;
                                                                                  UnionRegion
class UnionRegion extends AComboRegion {
  UnionRegion(Region r1, Region r2) {
    super(r1, r2);
                                                                               r2
  public boolean contains(Point p) {
      return this.rl.contains(p) &&
             this.r2.contains(p);
                                                                                 SquareRegion
class ExamplesRegion {
  Region sq = new SquareRegion(new Point(4, 5), 8);
  Region ci = new CircleRegion(new Point(6, 7), 10):
  Region ur = new UnionRegion(this.sq, this.ci);
                                                                                  CircleRegion
```

```
interface Region { ... }
                                                                               ExamplesRegion
abstract class ARegion implements Region { ... }
class SquareRegion extends ARegion { ... }
class CircleRegion extends ARegion { ... }
                                                                                sq
abstract class AComboRegion extends ARegion {
                                                                                 ci
  Region r1, r2;
  AComboRegion(Region r1, Region r2) {
                                                                                 ur
    this.r1 = r1:
    this.r2 = r2;
                                                   UnionRegion (con)
                                                   this
                                                                                  UnionRegion
class UnionRegion extends AComboRegion {
  UnionRegion(Region r1, Region r2) {
                                                   r1
    super(r1, r2);
                                                    r2
                                                                                r2
  public boolean contains(Point p) {
      return this.rl.contains(p) &&
             this.r2.contains(p);
                                                                                 SquareRegion
class ExamplesRegion {
  Region sq = new SquareRegion(new Point(4, 5), 8);
  Region ci = new CircleRegion(new Point(6, 7), 10):
  Region ur = new UnionRegion(this.sq, this.ci);
                                                                                  CircleRegion
```

```
interface Region { ... }
                                                                              ExamplesRegion
abstract class ARegion implements Region { ... }
class SquareRegion extends ARegion { ... }
class CircleRegion extends ARegion { ... }
                                                                                sq
abstract class AComboRegion extends ARegion {
                                                                                 ci
  Region r1, r2;
  AComboRegion(Region r1, Region r2) {
                                                                                 ur
    this.r1 = r1;
    this.r2 = r2;
                                                  UnionRegion (con)
                                                   this
                                                                                  UnionRegion
class UnionRegion extends AComboRegion {
  UnionRegion(Region r1, Region r2) {
                                                   r1
    super(r1, r2);
                                                    r2
                                                                                r2
  public boolean contains(Point p) {
     return this.rl.contains(p) &&
            this.r2.contains(p);
                                                                                 SquareRegion
class ExamplesRegion {
  Region sg = new SquareRegion(new Point(4, 5), 8);
  Region ci = new CircleRegion(new Point(6, 7), 10):
  Region ur = new UnionRegion(this.sq, this.ci);
                                                                                  CircleRegion
```

```
interface Region { ... }
                                                                               ExamplesRegion
abstract class ARegion implements Region { ... }
class SquareRegion extends ARegion { ... }
class CircleRegion extends ARegion { ... }
                                                                                sq
abstract class AComboRegion extends ARegion {
                                                                                 ci
  Region r1, r2;
  AComboRegion(Region r1, Region r2) {
                                                                                 ur
    this.r1 = r1:
    this.r2 = r2;
                                                   UnionRegion (con)
                                                   this
                                                                                  UnionRegion
class UnionRegion extends AComboRegion {
  UnionRegion(Region r1, Region r2) {
                                                   r1
    super(r1, r2);
                                                    r2
                                                                                r2
  public boolean contains(Point p) {
      return this.rl.contains(p) &&
             this.r2.contains(p);
                                                                                 SquareRegion
class ExamplesRegion {
  Region sq = new SquareRegion(new Point(4, 5), 8);
  Region ci = new CircleRegion(new Point(6, 7), 10):
  Region ur = new UnionRegion(this.sq, this.ci);
                                                                                  CircleRegion
```

```
interface Region { ... }
                                                                              ExamplesRegion
abstract class ARegion implements Region { ... }
class SquareRegion extends ARegion { ... }
class CircleRegion extends ARegion { ... }
                                                                                sq
abstract class AComboRegion extends ARegion {
                                                                                ci
  Region r1, r2;
  AComboRegion(Region r1, Region r2) {
                                                                                ur
    this.r1 = 1:
    this.r2 = r2
                                                  UnionRegion (con)
                                                   this
                                                                                  UnionRegion
class UnionRegion extends AComboRegion {
  UnionRegion(Region r1, Region r2) {
                                                   r1
    super(r1, r2);
                                                    r2
                                                                                r2
  public boolean contains(Point p) {
      return this.rl.contains(p) &&
             this.r2.contains(p);
                                                                                 SquareRegion
class ExamplesRegion {
  Region sq = new SquareRegion(new Point(4, 5), 8);
  Region ci = new CircleRegion(new Point(6, 7), 10):
  Region ur = new UnionRegion(this.sq, this.ci);
                                                                                  CircleRegion
```

```
interface Region { ... }
                                                                              ExamplesRegion
abstract class ARegion implements Region { ... }
                                                 AComboRegion (con)
class SquareRegion extends ARegion { ... }
class CircleRegion extends ARegion { ... }
                                                   this
                                                                                sq
abstract class AComboRegion extends ARegion {
                                                   r1
                                                                                ci
  Region r1, r2;
                                                    r2
  AComboRegion(Region r1, Region r2) {
                                                                                ur
    this.r1 = 1;
    this.r2 = r_2
                                                  UnionRegion (con)
                                                   this
                                                                                  UnionRegion
class UnionRegion extends AComboRegion {
  UnionRegion(Region r1, Region r2) {
                                                   r1
    super(r1, r2);
                                                    r2
                                                                                r2
  public boolean contains(Point p) {
     return this.rl.contains(p) &&
            this.r2.contains(p);
                                                                                 SquareRegion
class ExamplesRegion {
  Region sg = new SquareRegion(new Point(4, 5), 8);
  Region ci = new CircleRegion(new Point(6, 7), 10):
  Region ur = new UnionRegion(this.sq, this.ci);
                                                                                  CircleRegion
```

```
interface Region { ... }
                                                                              ExamplesRegion
abstract class ARegion implements Region { ... }
                                                 AComboRegion (con)
class SquareRegion extends ARegion { ... }
class CircleRegion extends ARegion { ... }
                                                   this
                                                                                sq
abstract class AComboRegion extends ARegion {
                                                   r1
                                                                                ci
  Region r1, r2;
                                                    r2
  AComboRegion(Region r1, Region r2) {
                                                                                ur
    this.r1 = 1:
    this.r2 = r2
                                                  UnionRegion (con)
                                                   this
                                                                                  UnionRegion
class UnionRegion extends AComboRegion {
  UnionRegion(Region r1, Region r2) {
                                                   r1
    super(r1, r2);
                                                    r2
                                                                                r2
  public boolean contains(Point p) {
     return this.rl.contains(p) &&
            this.r2.contains(p);
                                                                                 SquareRegion
class ExamplesRegion {
  Region sq = new SquareRegion(new Point(4, 5), 8);
  Region ci = new CircleRegion(new Point(6, 7), 10):
  Region ur = new UnionRegion(this.sq, this.ci);
                                                                                  CircleRegion
```

```
interface Region { ... }
                                                                              ExamplesRegion
abstract class ARegion implements Region { ... }
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                                                  UnionRegion (con)
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class UnionRegion extends AComboRegion {
  UnionRegion(Region r1, Region r2) {
                                                   r1
    super(r1, r2);
                                                    r2
                                                                                r2
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