

CSE12 - Lecture 21

Wednesday, November 22, 2023 8:00 AM

PA7 and PA5 Late/Resubmit - slip day - due Thursday @ 8am

No class on Friday - holiday

PA8 released today

Discussion - tonight is on Zoom only - see Piazza post for link

Lecture 21

Heap Applications

Median

```

class Tracker {
    PriorityQueue<Integer> pq1 = new PriorityQueue<>(Collections.reverseOrder(Integer::compare));
    PriorityQueue<Integer> pq2 = new PriorityQueue<>(Integer::compare);
    void add(int n) {
        if(pq2.size() == 0 && pq1.size() == 0) { }
        pq2.add(n);
        return;
    }
    int current = get();
    if(n >= current) {
        pq2.add(n);
    }
    else {
        pq1.add(n);
    }
    int sizeDifference = pq2.size() - pq1.size();
    if(sizeDifference > 1) { pq1.add(pq2.poll()); }
    else if(sizeDifference < -1) { pq2.add(pq1.poll()); }

    int get() {
        if(pq2.size() == pq1.size()) { return (pq2.peek() + pq1.peek()) / 2; }
        if(pq2.size() > pq1.size()) { return pq2.peek(); }
        else { return pq1.peek(); }
    }

    public String toString() {
        return "" + pq1 + " " + this.get() + " " + pq2;
    }
}

```

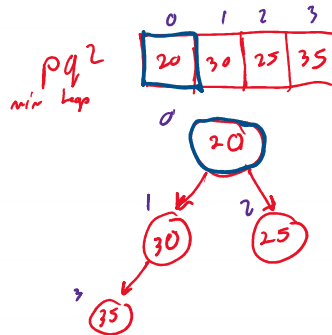
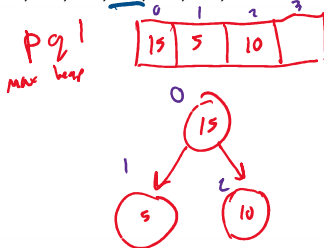
Annotations:

- heap* (pointing to pq1)
- high to low → max heap* (pointing to pq1)
- low to high → min heap* (pointing to pq2)
- add()* (pointing to add method)
- sorted input* (pointing to pq2)
- height → log₂(n)* (pointing to a tree diagram)
- BC* (pointing to pq2)
- 1 + log₂(n)* (pointing to pq2)
- 2 * log₂(n)* (pointing to pq2)
- log₂(n)* (pointing to a tree diagram)
- 3/1*, *0/2/1*, *0/0/1* (pointing to get method)

Draw the picture and the arrays for the following:

Add the following elements to the Tracker (in this order):

5, 10, 15, 20, 25, 30, 35



value of final get()? 20

Name: _____ PID: _____ Code: 8634

What is the result of the call to get() after adding all the elements?

20

What is the run-time for the tracker?

Worst Case: $\mathcal{O}(\log_2(n))$ $\mathcal{O}(1)$
Best Case: $\mathcal{O}(1)$
 \hookrightarrow add evenly to both sides

Write a method to use the tracker:

```
int findNumber (Integer[] arr) {  
    MedianTracker tracker = new _____  
    for (int i=0; i<arr.length; i++) {  
        tracker.add(arr[i]);  
    }  
    return tracker.get();  
}
```

$\log_2(n)$ $\left. \begin{array}{l} 1 \\ 1 \end{array} \right\} \underline{N * \log_2(n)}$

What is the total run-time using the tracker:

$N + \log_2(n)$

Using a PriorityQueue, write a Heap Sort method to perform an in-place sort of an array: