

PA4 due Wednesday @ 8am

PA2 Late/Resubmit due Wednesday @ 8am

Lecture 12
Sorting Fast

Merge Sort → divide & conquer algorithm

```

public class SortFast {
    public static String s(int[] arr) { return Arrays.toString(arr); }

    public static int[] mergeSort(int[] part1, int[] part2) {
        int index1 = 0, index2 = 0;
        int[] combined = new int[part1.length + part2.length];
        while(index1 < part1.length && index2 < part2.length) {
            if(part1[index1] < part2[index2]) {
                combined[index1 + index2] = part1[index1];
                index1++;
            } else {
                combined[index1 + index2] = part2[index2];
                index2++;
            }
            while(index1 < part1.length) {
                combined[index1 + index2] = part1[index1];
                index1++;
            }
            while(index2 < part2.length) {
                combined[index1 + index2] = part2[index2];
                index2++;
            }
            System.out.println(s(part1) + " + " + s(part2) + " → " + s(combined));
            return combined;
        }

        public static int[] sort(int[] arr) {
            if(arr.length <= 1) { return arr; }
            else {
                int[] part1 = Arrays.copyOfRange(arr, 0, arr.length / 2);
                int[] part2 = Arrays.copyOfRange(arr, arr.length / 2, arr.length);
                System.out.println(s(arr) + " → " + s(part1) + " + " + s(part2));
                int[] sortedPart1 = sort(part1);
                int[] sortedPart2 = sort(part2);
                int[] sorted = combine(sortedPart1, sortedPart2);
                return sorted;
            }
        }

        public static void main(String[] args) {
            int[] result = SortFast.sort(new int[] { 34, 93, 12, 49, 69, 25, 39 });
            System.out.println(SortFast.s(result));
        }
    }

```

Draw the picture of sortC().

What is the tight bound of sortC.

Best case: _____ Worst case: _____

Name: _____ PID: _____ Code: 6229

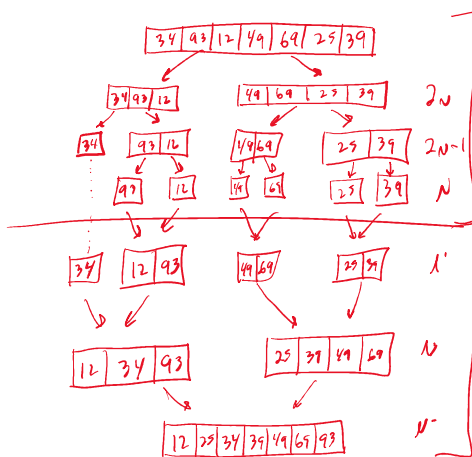
$$2 + 2(n+1) + (n+1) + 1$$

$$3n + 3n + 1$$

$$\Theta(n+1) \rightarrow \Theta(n)$$

combine/merge

$$\begin{array}{l} \text{copy of Range } \frac{N}{2} \\ \hookrightarrow \text{new array } \frac{N}{2} \\ \hookrightarrow \text{copy about } \frac{N}{2} \end{array} \left. \begin{array}{l} 2N \\ N \\ N \end{array} \right\}$$



splitting

$$N=7$$

$$\text{height} = 3$$

$$\hookrightarrow \log_2(N)$$

combining/merging

$$\text{height} = 3$$

$$\hookrightarrow \log_2(N)$$

$$N \cdot \log_2(N) \rightarrow \Theta(N \log_2(N))$$