

Exam 1 - Wednesday

- <https://ucsd-cse12-sp24.github.io/lectures/exam1.html>

Categorizing Runtimes

Let $f(n) = 100$

Which of the following is NOT a correct bound?

- A. $f(n)$ is $O(2^n)$
- B. $f(n)$ is $O(n^2)$
- C. $f(n)$ is $O(n)$
- D. $f(n)$ is $O(n^{100})$
- E. None of these**

Let $f(n) = 3n^3 + 2n + 7$

Which of the following is a correct bound?

- ☒ A. $f(n)$ is $O(\log(n))$
☐ B. $f(n)$ is $O(n^2)$
☐ C. $f(n)$ is $O(n)$
☒ D. $f(n)$ is $O(n^3)$
☐ E. None of these

```
void printAllElementOfArray(int[] arr) {
    for (int i = 0; i < arr.length; i++) {
        printf("%d\n", arr[i]);
    }
}
```

Which of the following is a correct bound?

- ☒ B $f(n)$ is $O(n^2)$

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Which of the following is a correct bound?

- ~~A. $f(n)$ is $O(\log(n))$~~
~~B. $f(n)$ is $O(n^2)$~~
~~C. $f(n)$ is $O(n)$~~
~~D. $f(n)$ is $O(n^3)$~~
~~E. None of these~~

```
void printAllPossibleOrderPairs(int arr[]) {
    for (int i = 0; i < arr.length; i++) {
        for (int j = 0; j < arr.length; j++) {
            printf("%d = %d\n", arr[i], arr[j]);
        }
    }
}
```

$1 + (n-1) + n$
 $2n + 2 +$
 $n + n^2 + n + n^2 + n^2 \rightarrow 3n^2 + 2n$
 $f(n) \rightarrow 3n^2 + 4n + 2$

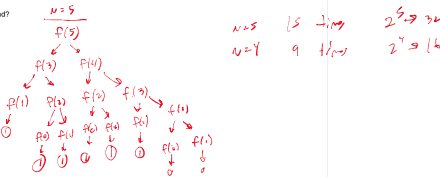
Which of the following is a correct bound?

- ☒ A $f(n)$ is $O(\log(n))$
☐ B $f(n)$ is $O(n^2)$
☐ C $f(n)$ is $O(n)$
☐ D $f(n)$ is $O(n^3)$
☐ E None of these

```
int fibonacci(int num) {
    if (num <= 1) return num;
    return fibonacci(num - 2) + fibonacci(num - 1);
}
```

Which of the following is a correct bound?

- A. $f(n)$ is $O(2^n)$
 B. $f(n)$ is $O(n^2)$
 C. $f(n)$ is $O(n)$
 D. $f(n)$ is $O(n^3)$
 E. None of these

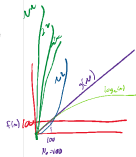


Rig-O upper bound

$$\underline{f(n) = O(g(n))} \text{, } f(n) \leq c * g(n) \text{ for all } n \geq n_0$$

For each function in the list below, it is related to the function below it by O , and the reverse is not true. That is, n is $O(n^2)$ but n^2 is not $O(n)$.

- $f(n) = 1/(n^2)$
- $f(n) = 1/n$
- $f(n) = 1$
- $f(n) = \log(n)$
- $f(n) = \sqrt{\log(n)}$
- $f(n) = n$
- $f(n) = n^2$
- $f(n) = n^3$
- $f(n) = n^4$
- ... and so on for constant polynomials ...
- $f(n) = 2^n$
- $f(n) = n!$
- $f(n) = n^n$



$P(n) \leq C \cdot 5(n)$
 $f(n) \leq 1 \cdot 5(n)$
 correct bound?
 C
 $5(n)$
 $U_n = 7$
 $3n^3 + 2n^3 + 7n^3 \rightarrow 12n^3$

 $3n^3 + 3n^3 + 7 \rightarrow 5n^3 + 7$
 $C = 5$
 $5(n) = n^3$
 $N_0 = 7$

$$\frac{1 + \frac{(n+1) + N}{N}}{3n + 2}$$

$C \geq 3$
 $f(n) = N$
 $M = 2$

$$\begin{aligned} & \frac{1}{2} \div \frac{1}{2} \rightarrow \underline{3u^2 + 2u} \\ f(u) & \rightarrow \underline{3u^2} + 4u + 2 \\ g(u) & \rightarrow \underline{u^2} \\ & 3u^2 + 4u + 2 \\ & \quad 7u^2 + 2 \\ & \quad \quad 6 \div 7 \\ & \quad \quad 14 \div 2 \end{aligned}$$

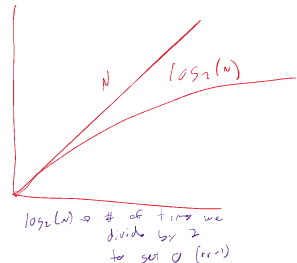
$n=5$ 15 $\rightarrow 10$ $2^5 \rightarrow 32$
 $n=4$ 9 $\rightarrow 6$ $2^4 \rightarrow 16$

```

boolean isPrimeAll(int num) {
    // Check for divisors of num
    for (int i = 2; i < num; i++) {
        if (num % i == 0) {
            // Any divisor other than 1 or num means num is not prime
            return false;
        }
    }
    // No other divisors found means num is prime
    return true;
}

boolean isPrimeHalf(int num) {
    // Check for divisors of num
    for (int i = 2; i <= num / 2; i++) {
        if (num % i == 0) {
            // Any divisor other than 1 or num means num is not prime
            return false;
        }
    }
    // No other divisors found means num is prime
    return true;
}

```

$$\begin{array}{r} 1 + (n+1) + n \\ n \\ 0 \\ 1 \end{array} \quad \left. \vphantom{\begin{array}{r} 1 + (n+1) + n \\ n \\ 0 \\ 1 \end{array}} \right\} 3n+3$$
$$1 + \frac{\left(\frac{N}{2} + 1\right) + \frac{N}{2}}{\frac{N}{2}}$$

$$\frac{3n}{2} + 3$$
$$g(n) = N \quad O(n)$$

$$C = 2$$

$$M = 3$$

What is the smallest correct bound?