

Example:  
Start buckets array with size 4  
Use string length as the hash function

```
add("red", 70)
add("blue", 90)
add("pink", 100)
add("orange", 40)
add("purplish", 30)
```

- How many elements in bucket 0?  
A: 0 B: 1 C: 2 **D: 3** E: more than 3
- How many elements in bucket 1?  
**A: 0** B: 1 C: 2 D: 3 E: more than 3
- How many elements in bucket 2?  
A: 0 **B: 1** C: 2 D: 3 E: more than 3
- How many entries are checked for get("purplish")?  
A: 1 B: 2 C: 2 **D: 3** E: more than 3

A HashTable<Key, Value> using Separate Chaining has:

- size: an int
- buckets: an array of lists of Entries
- hash: a hash function for the Key type

An Entry is a single {key: value} pair.

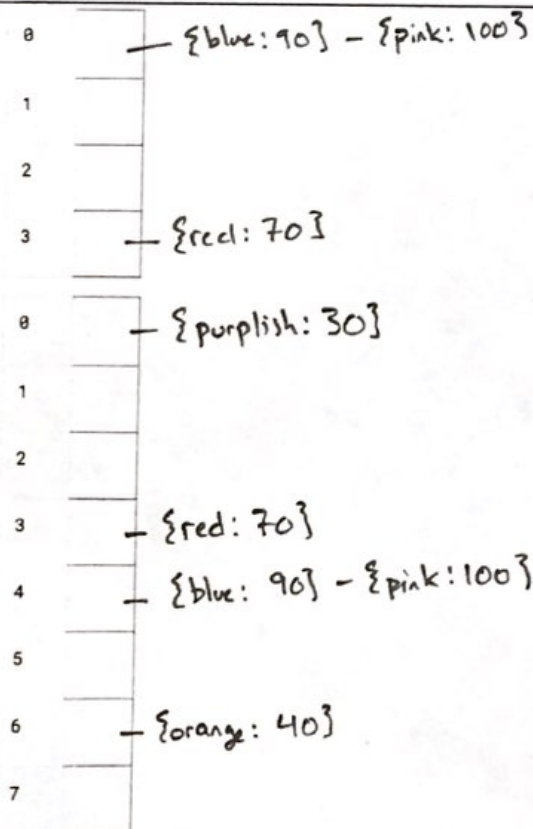
add  
void set(key, value):

```
hashed = hash(key)
index = hashed % this.buckets.length
if this.buckets[index] contains an Entry with key:
    update that Entry to contain value
else:
    increment size
    bucket = buckets[index]
    add {key: value} to end of bucket
```

Value get(key):

```
hashed = hash(key)
index = hashed % this.buckets.length
if this.buckets[index] contains an Entry with key:
    return the value of that entry
else:
    return null/report an error
```

LoadFactor =  $\frac{\text{\# entries}}{\text{\# buckets}}$  Java: 0.75 Python: 2/3



void set(key, value):

```
if LoadFactor ≥ 0.75: expandCapacity()
... as before ...
```

← first line

```
void expandCapacity():
newBuckets = new List[this.buckets.length * 2];
oldBuckets = this.buckets
this.buckets = newBuckets
this.size = 0
for each list of entries in oldBuckets:
    for each {k: v} in the list:
        this.set(k, v)
```

Example:  
Start buckets array with size 4  
Use string length as the hash function

A add("red", 70)  $\frac{1}{4}$   
B add("blue", 90)  $\frac{1}{2}$   
C add("pink", 100)  $\frac{3}{4}$   
D add("orange", 40)  $\frac{1}{2}$   
E add("purplish", 30)

When does expandCapacity happen?

```

int hash1(String s) {
    return s.length();
}

int hash2(String s) {
    int hash = 0;
    for (int i = 0; i < s.length(); i += 1) {
        hash += Character.codePointAt(s, i);
    }
    return hash;
}

public int hash3(String s) {
    int h = 0;
    for (int i = 0; i < s.length(); i++) {
        h = 31 * h + Character.codePointAt(s, i);
    }
    return h;
}

```

$$\begin{array}{cc}
 \begin{array}{c} 4 \ 15 \ 7 = 26 \\ \swarrow \downarrow \searrow \\ \text{"dog"} \end{array} & \begin{array}{c} 4 \ 9 \ 13 = 26 \\ \swarrow \downarrow \searrow \\ \text{"dim"} \end{array} \\
 ((4 * 31) + 15) * 31 + 7 & ((4 * 31) + 9) * 31 + 13
 \end{array}$$

"dog"

"log"

"ok"  $\leftarrow$  hash2  $\rightarrow$  "ALM"

"unheavenly"

"hypoplankton"

All strings (arbitrarily many!): "" ... "a" "b" ... "aa" "ab" ... "zz" ... "aaa" "aab" ... "zzzzzzzz..." ...

Hashed to  $2^{32}$  ints: -2147483648 -2147483647 ... -1001 -1000 ... -2 -1 0 1 2 ... 1000 1001 ... 2147483647

Made into array indices by %: 0 1 2 3 4 5 6 7 8 9 10 ...

distribute  
evenly

- Unique Even distribution
- Fast
- Deterministic