

State Transformers

Lets capture the above “pattern” as a type

1. A State Type

```
type State = ... -- lets "fix" it to Int for now...
```

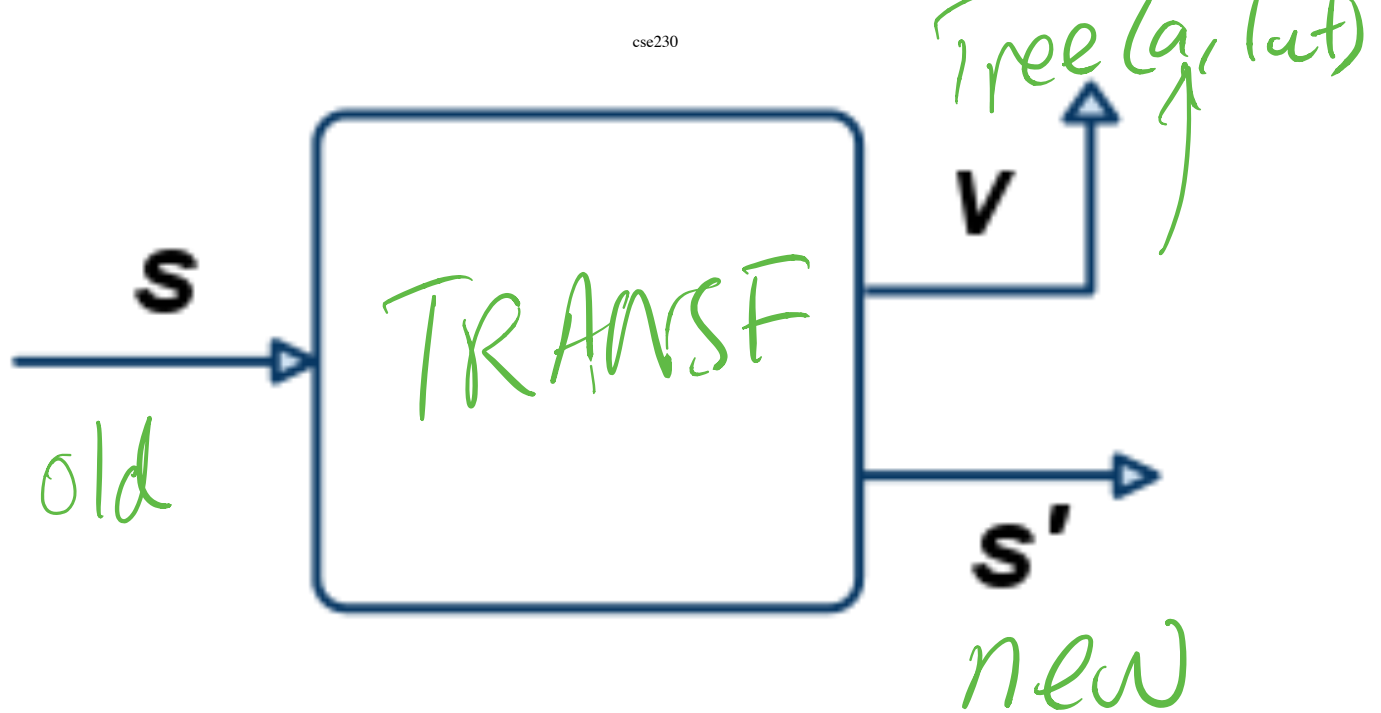
2. A State Transformer Type

```
data ST a = STC (State -> (State, a))
```



A *state transformer* is a function that

- takes as input an **old** $s :: \text{State}$
- returns as output a **new** $s' :: \text{State}$ and **value** $v :: a$



Executing Transformers

Lets write a function to *evaluate* an ST a

```
evalState :: State -> ST a -> a  
evalState = ???
```

QUIZ

What is the value of quiz ?

```
st :: St [Int]  
st = STC (\n -> (n+3, [n, n+1, n+2]))
```

```
quiz = evalState100 st
```

A. 103

- B. `[100, 101, 102]`
- C. `(103, [100, 101, 102])`
- D. `[0, 1, 2]`
- E. Type error

Lets Make State Transformer a Monad!

instance Monad ST where

return :: a -> ST a

return = returnST

(>>=) :: ST a -> (a -> ST b) -> ST b

(>>=) = bindST

EXERCISE: Implement `returnST`!

What is a valid implementation of `returnST`?

```
type State = Int  
data ST a = STC (State -> (State, a))
```

```
returnST :: a -> ST a  
returnST = ???
```

What is `returnST` doing?

`returnST v` is a *state transformer* that ... ???

(Can someone suggest an explanation in English?)

HELP

Now, lets implement `bindST` !

```
type State = Int
```

```
data ST a  = STC (State -> (State, a))
```

```
bindST :: ST a -> (a -> ST b) -> ST b
```

```
bindST = ???
```

What is *returnST* doing?

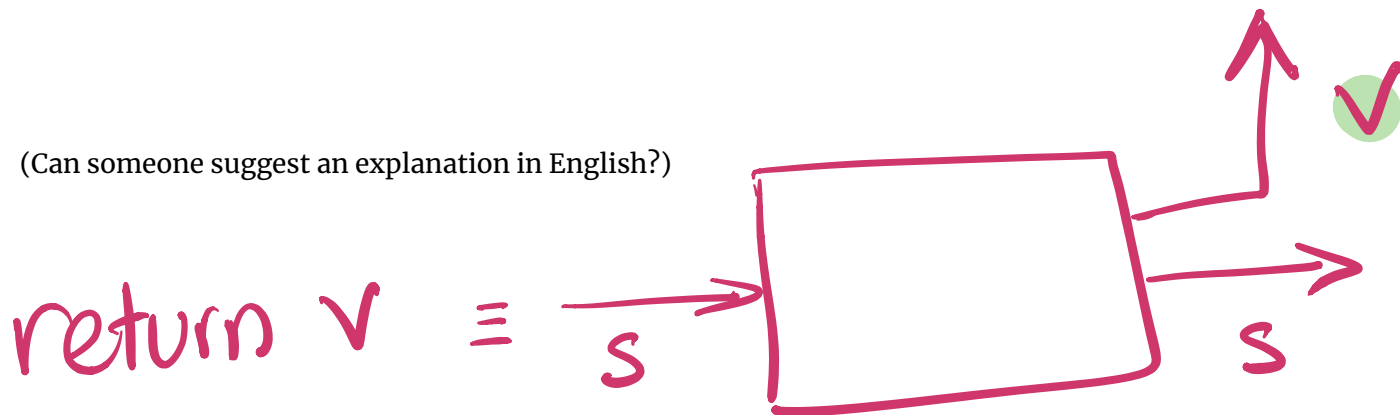
`returnST v` is a *state transformer* that ... ???

(Can someone suggest an explanation in English?)

What is *returnST* doing?

`returnST v` is a *state transformer* that ... ???

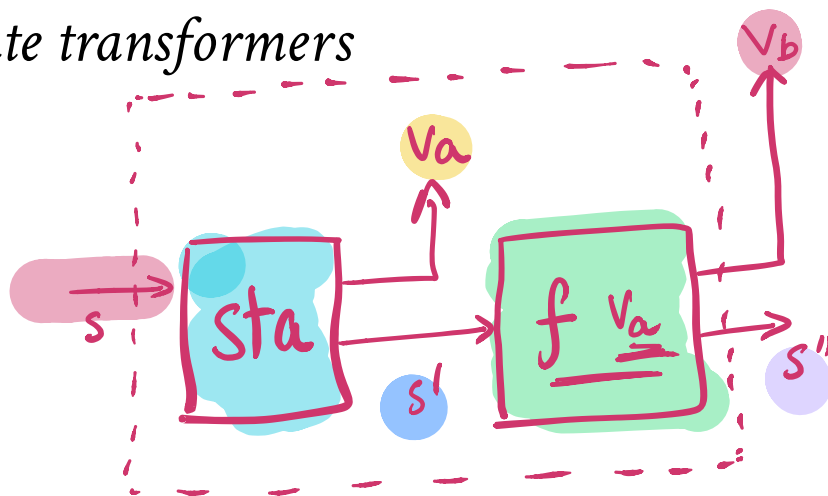
(Can someone suggest an explanation in English?)



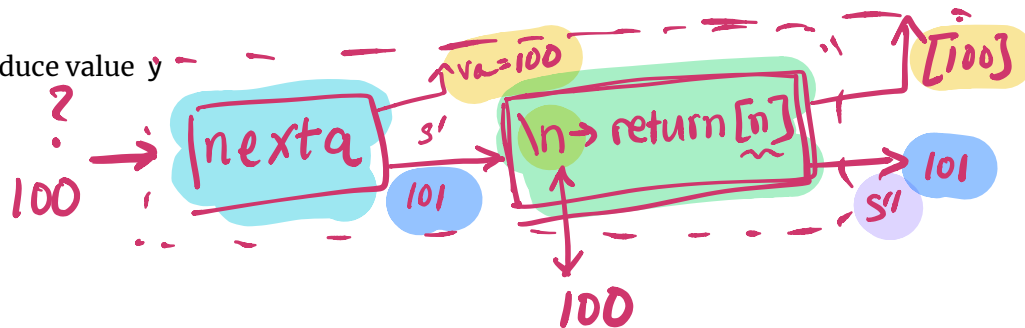
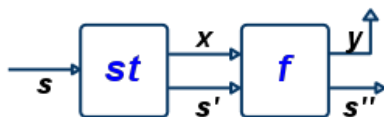
bindST lets us sequence state transformers

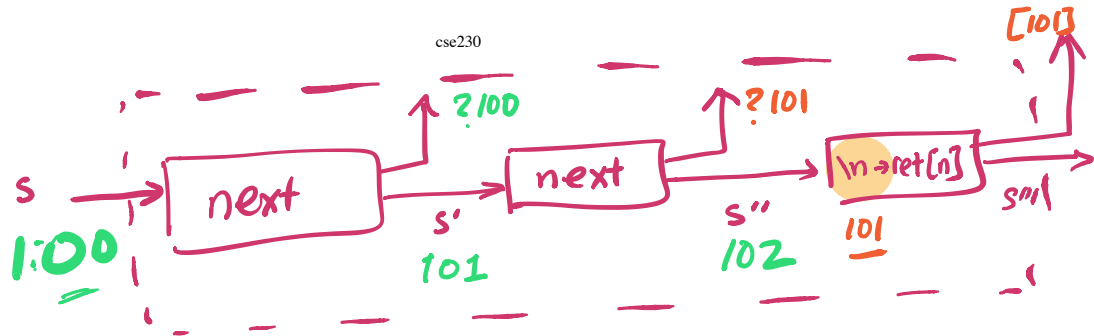
$st \gg= f$

1. Applies transformer st to an initial state s
 - to get output s' and value x
2. Then applies function f to the resulting value x
 - to get a *second* transformer
3. The *second* transformer is applied to s'
 - to get final s'' and value y



OVERALL: Transform s to s'' and produce value y





Lets Implement a Global Counter

The (counter) State is an Int

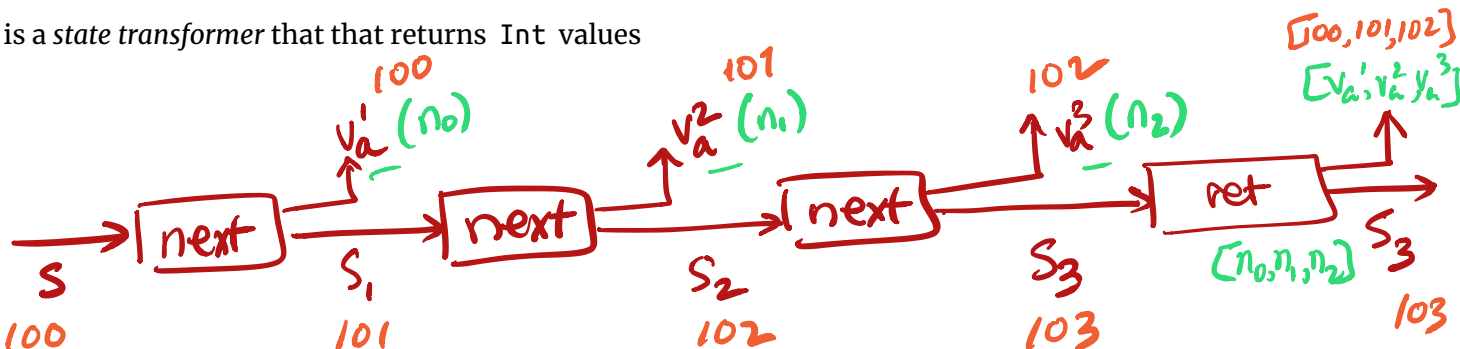
type State = Int

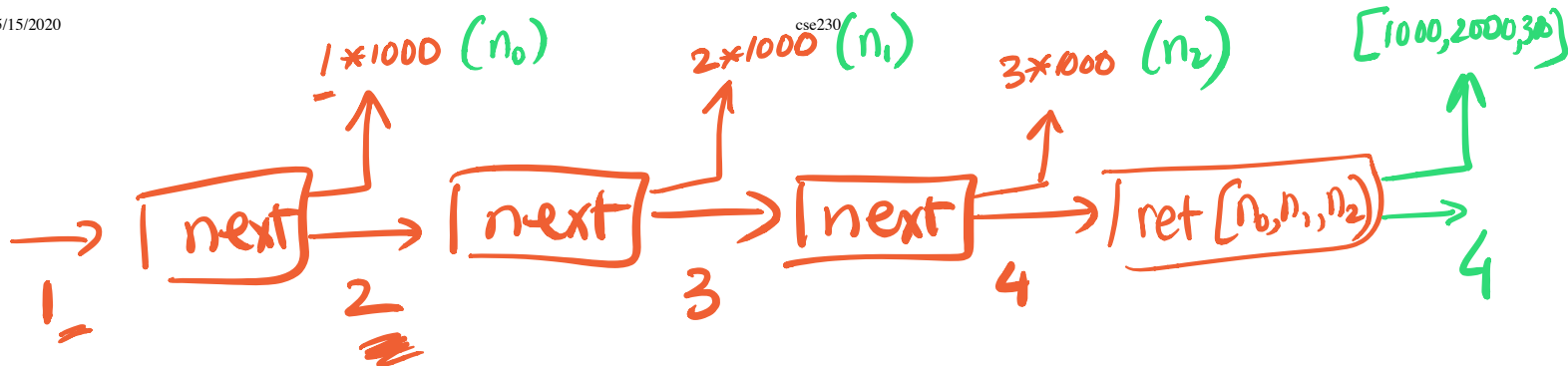
A function that *increments* the counter to *return* the next Int .

next :: ST Int

next = STC (\old -> let new = old + 1 in (new, old))

next is a *state transformer* that that returns Int values





QUIZ

Recall that

```
evalState :: State -> ST a -> a
evalState s (STC st) = snd (st s)
```

```
next :: ST Int
next = STC (\n -> (n+1, n))
```

What does quiz evaluate to?

```
quiz = evalState 100 next
```

- A. 100
- B. 101
- C. 0

D. 1

E. (101, 100)

QUIZ

Recall the definitions

```
evalState :: State -> ST a -> a  
evalState s (STC st) = snd (st s)
```

```
next :: ST Int  
next = STC (\n -> (n+1, n))
```

Now suppose we have

```
wtf1 = ST Int
wtf1 = next >=& \n ->
    return n
```

What does `quiz` evaluate to?

```
quiz = evalState 100 wtf1
```

A. 100

B. 101

C. 0

D. 1

E. (101, 100)

QUIZ

Consider a function `wtf2` defined as

```
wtf2 = next >=> \n1 ->  
    next >=> \n2 ->  
    next >=> \n3 ->  
    return [n1, n2, n3]
```

What does `quiz` evaluate to?

```
quiz = evalState 100 wtf
```

- A. Type Error!
- B. [100, 100, 100]
- C. [0, 0, 0]
- D. [100, 101, 102]
- E. [102, 102, 102]

Chaining Transformers

`>>=` lets us *chain* transformers into *one* big transformer!

So we can define a function to *increment the counter by 3*

```
-- Increment the counter by 3
next3 :: ST [Int, Int]
next3 = next >>= \n1 ->
    next >>= \n2 ->
    next >>= \n3 ->
    return [n1,n2,n3]
```

And then sequence it *twice* to get