Let's add first class functions

```
e ::= ...
| (defn (f x1... xn) e) ; definition
| (f e1 ... en) ; function call
```

```
(defn (incr x)
  (+ x 1))

(defn (f it)
  (it 5))

(f incr)
```

```
pub struct Defn {
   pub name: Option<String>,
   pub params: Vec<String>,
   pub body: Box<Expr>,
}

pub enum Expr {
   ...
   Fun(Defn),
   Call(String, Vec<Expr>),
}
```

Code Labels as Values

```
(defn (incr x) (+ x 1))
(defn (f it) (it 5))
(f incr)
```

```
;; definition of incr
fun_start_incr:
push rbp
mov rbp, rsp
 sub rsp, 8*100
fun body incr:
mov rax, [rbp - 8*-2]; load x
                        ; add <1>
add rax, 2
fun exit incr:
mov rsp, rbp
pop rbp
ret
;; definition of f
fun start f:
push rbp
mov rbp, rsp
 sub rsp, 8*100
fun body f:
mov rax, 10
push rax
call FIXME1
add rsp, 8*1
fun exit f:
mov rsp, rbp
pop rbp
ret
;; definition of main
our code starts here:
; setup stack frame
push rbp
mov rbp, rsp
sub rsp, 8*100
 ; body of `main`
mov [rbp - 8], rdi ; save `input`
mov r11, rsi ; save start of
heap
push FIXME2
call fun start f
add rsp, 8*1
 ; teardown stack frame
mov rsp, rbp
pop rbp
ret
```

```
(let (f (fn (it) (it 5)))
  (let (inc (fn (z) (+ z 1)))
      (f foo)))
```

```
;; block for `(let f (fn ...))`
jmp fun_finish_f
fun_start_f:
 push rbp
 mov rbp, rsp
 sub rsp, 8*101
fun_body_f:
 mov rax, 10
                 ;; push arg 5
 push rax
 mov rax, [rbp - 8*-2] ;; load `it`
 call rax
                     ;; call `it`
                      ;; pop arg
 add rsp, 8*1
fun_exit_f:
mov rsp, rbp
 pop rbp
 ret
fun finish f:
mov rax, fun_start_f ;; save `f` as local#1
(f) in "main"
mov [rbp - 8*2], rax
;; block for `(let inc (fn ...))`
 jmp fun finish anon 1
fun_start_anon_1:
 push rbp
mov rbp, rsp
 sub rsp, 8*100
fun_body_anon_1:
mov rax, [rbp - 8*-2];; load z
                    ;; add 1
 add rax, 2
fun exit anon 1:
mov rsp, rbp
 pop rbp
ret
fun_finish_anon_1:
mov rax, fun_start_anon_1
mov [rbp - 8*3], rax ;; save `fn..` as
local#2 (inc) in "main"
;; block for `(f incr)`
mov rax, [rbp - 8*3] ;; load `foo` into
rax
push rax
                       ;; push as arg
mov rax, [rbp - 8*2]
                      ;; load caller `f`
into rax
call rax
add rsp, 8*1
```

Anonymous Functions

```
;; block to define `f`
                                                                                 lam-arity.s
jmp fun_finish_anon_1
fun_start_anon_1:
  push rbp
  mov rbp, rsp
  sub rsp, 8*101
fun_body_anon_1:
  mov rax, 10
  push rax
                         ;; push arg <5>
  mov rax, [rbp - 8*-2] ;; load `it`
  call rax
                        ;; call `it`
  add rsp, 8*1
fun_exit_anon_1:
  mov rsp, rbp
  pop rbp
  ret
fun_finish_anon_1:
                    ;; save `fn` as local-#1 `f`
  mov rax, fun_start_anon_1
  mov [rbp - 8*2], rax
;; block to define `add`
jmp fun_finish_anon_2
fun_start_anon_2:
 push rbp
 mov rbp, rsp
 sub rsp, 8*105
fun_body_anon_2:
 mov rax, [rbp - 8*-2]
 mov rcx, [rbp - 8*-3]
 add rax, rcx
 mov rcx, [rbp - 8*-4]
 add rax, rcx
 mov rcx, [rbp - 8*-5]
 add rax, rcx
 mov rcx, [rbp - 8*-6]
 add rax, rcx
fun_exit_anon_2:
 mov rsp, rbp
 pop rbp
 ret
fun finish anon 2:
 mov rax, fun_start_anon_2
 mov [rbp - 8*3], rax
;; (f add)
mov rax, [rbp - 8*3] ;; push `add` as arg
push rax
mov rax, [rbp - 8*2]
                      ;; load `f` into rax
call rax
add rsp, 8*1
```

```
;; block to define `five` as local#1
mov rax, 10
mov [rbp - 8*2], rax
;; block to define `f`
jmp fun_finish_anon_1
fun_start_anon_1:
push rbp
mov rbp, rsp
sub rsp, 8*101
fun_body_anon_1:
                      ;; FIXME: what is `five`?
mov rax, ?FIVE
                      ;; push arg <5>
mov rax, [rbp - 8*-2] ;; load `it`
;; CHECK FUNCTION
;; CHECK ARITY
sub rax, 5
                     ;; remove TAG
                     ;; load actual label of `it` into rax
mov rax, [rax]
call rax
                      ;; call `it`
add rsp, 8*1
fun_exit_anon_1:
mov rsp, rbp
pop rbp
ret
fun_finish_anon_1:
;; allocate tuple for fun_start_anon_1
mov rax, fun_start_anon_1
mov [r11], rax
                  ;; save label
mov rax, 1
mov [r11 + 8], rax ;; save arity = 1
mov rax, r11
                      ;; save tuple address
                      ;; bump allocation pointer (16-byte aligned)
add r11, 16
add rax, 5
                      ;; tag rax as "function"
mov [rbp - 8*3], rax ;; save `fn` as local-#2 `f`
;; block to define `inc`
jmp fun_finish_anon_2
fun_start_anon_2:
push rbp
mov rbp, rsp
 sub rsp, 8*105
fun_body_anon_2:
 mov rax, [rbp - 8*-2]
 add rax, 2
fun_exit_anon_2:
 mov rsp, rbp
 pop rbp
ret
fun_finish_anon_2:
;; allocate tuple for fun_start_anon_2
mov rax, fun_start_anon_2
                     ;; save label
mov [r11], rax
 mov rax, 1
 mov [r11 + 8], rax ;; save arity = 1
                      ;; save tuple address
 mov rax, r11
                       ;; bump allocation pointer
 add r11, 16
 add rax, 5
                       ;; tag rax as "function"
 mov [rbp - 8*4], rax ;; save `fn` as local#3 `inc`
;; (f inc)
mov rax, [rbp - 8*4] ;; push `inc` as arg
push rax
mov rax, [rbp - 8*3]
                       ;; load `f` tuple into rax
;; CHECK function TAG
;; CHECK arity
sub rax, 5
mov rax, [rax]
                       ;; load actual label
call rax
add rsp, 8*1
```

Free (non-local) Variables?

```
fn free_vars(e: &Expr) -> HashSet<String> {
   match e {
       Expr::Num( ) | Expr::Input | Expr::True | Expr::False
       Expr::Var(x)
         =>
       Expr::Fun(defn)
         =>
       Expr::Add1(e)
         Expr::Sub1(e)
        Expr::Neg(e)
        Expr::Set( , e)
        Expr::Loop(e)
        Expr::Break(e)
        Expr::Print(e)
        Expr::Get(e, _)
         =>
       Expr::Let(x, e1, e2) \Rightarrow
       Expr::Eq(e1, e2)
       | Expr::Le(e1, e2)
       | Expr::Plus(e1, e2)
       | Expr::Mult(e1, e2)
       | Expr::Vec(e1, e2) =>
       Expr::If(e1, e2, e3) =>
       Expr::Block(es) =>
       Expr::Call(f, es) =>
   }
}
```