

**UNIVERSITY COLLEGE TATI (UC TATI)**

| FINAL EXAMINATION QUESTION BOOKLET |                   |
|------------------------------------|-------------------|
| COURSE CODE                        | : DTC 1053        |
| COURSE                             | : FLUID MECHANICS |
| SEMESTER/SESSION                   | : 1 / 2024-25     |
| DURATION                           | : 3 HOURS         |

**Instructions:**

1. This booklet contains 4 questions. Answer **ALL** questions.
2. All answers should be written in answer booklet.
3. Write legibly and draw sketches wherever required.
4. If in doubt, raise your hands and ask the invigilator.

DO NOT OPEN THIS BOOKLET UNTIL YOU ARE TOLD TO DO SO

**THIS BOOKLET CONTAINS 8 PRINTED PAGES INCLUDING COVER PAGE**

## QUESTION 1

- a) For fluid that occupies a volume of 24 L weighs 225 N at a location where the gravitational acceleration is  $9.80 \text{ m/s}^2$ . Identify the mass of this fluid and its density. (8 marks)
- b) Figure 1 shows water in a 3 m high from the ground with 8 m diameter swimming pool is to be emptied by a 3 cm diameter, 25 m long pipe attached horizontally to the bottom of the pool. Compute the maximum discharge rate of water through the pipe. (10 marks)

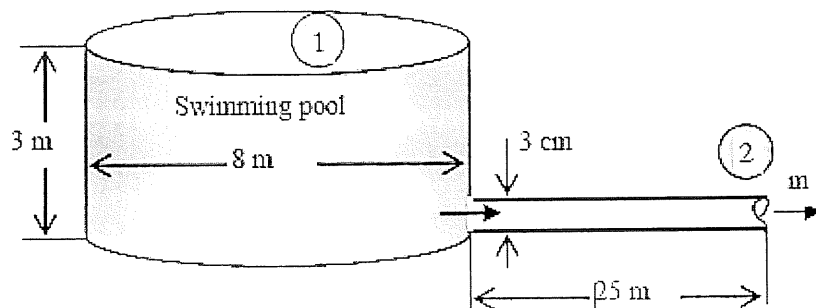


Figure 1

- c) Low velocity water enters the turbine nozzles at 800 kPa absolute (Figure 2). Compute the maximum velocity to which water can be hastened by the nozzles before striking the turbine blades, if the outlet nozzle is exposed to atmospheric pressure of 100 kPa. (10 marks)

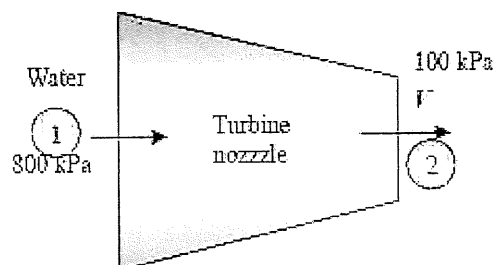


Figure 2

## QUESTION 2

- a) Consider a U-tube (Fig.3) whose arms are open to the atmosphere. Now water is poured into the U-tube from one arm, and light oil ( $\rho = 790 \text{ kg/m}^3$ ) from the other. One arm contains 70-cm-high water, while the other arm contains both fluids with an oil-to-water height ratio of 6. Solve the height of each fluid in that arm. (10 marks)

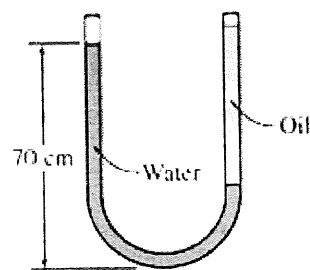


Figure 3

- b) A  $0.75 \text{ m}^3$  rigid tank initially contains air whose density is  $1.18 \text{ kg/m}^3$  as shown in Figure 4. The tank is connected to a high-pressure supply line through a valve. The valve is opened, and air is allowed to enter the tank until the density in the tank rises to  $4.95 \text{ kg/m}^3$ . Calculate the mass of air that has entered the tank. (10 marks)

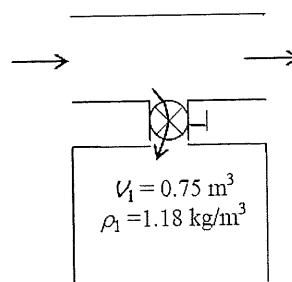


Figure 4

**QUESTION 3**

- a) In a tank contains fluid 1 ( $\rho = 500 \text{ kg/m}^3$ ), fluid 2 ( $\rho = 750 \text{ kg/m}^3$ ) and fluid 3 ( $\rho = 1000 \text{ kg/m}^3$ ). Calculate the pressure at position 1 in Figure 5. Given  $P_{\text{atm}} = 100 \text{ kPa}$ . (8 marks)

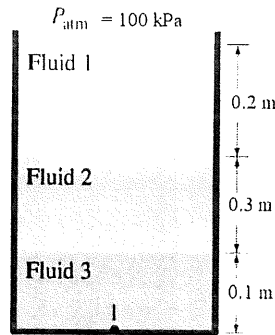


Figure 5

- b) Referring to Fig.6, given velocity at A is 1.5 m/s, estimate the value of:
- i) flow rate at point A (4 marks)
  - ii) velocity at point B (4 marks)
  - iii) flow rate at point B (2 marks)

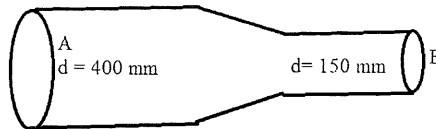


Figure 6

**QUESTION 4**

- a) Water at  $50^\circ\text{C}$  ( $\rho = 992.1 \text{ kg/m}^3$  and  $\mu = 0.653 \times 10^{-3} \text{ kg/m.s}$ ) is flowing steadily in a 7 cm-diameter horizontal pipe made of stainless steel at a rate of 250 L/min over a 60 m-long section of pipe. Calculate:

- i) The average velocity. (2 marks)
- ii) The flow regime based from Re number,  $N_{\text{Re}}$ . (2 marks)
- iii) The relative roughness of the pipe ( $\frac{\epsilon}{D}$ ). (2 marks)
- iv) The friction factor ( $f$ ). (3 marks)
- v) The pressure drop ( $\Delta P_L$ ). (3 marks)
- vi) The head loss ( $h_L$ ). (3 marks)
- vii) The requirement of pumping power to overcome this pressure drop ( $\dot{W}$ ). (4 marks)

- b) The flow rate of methanol at  $20^{\circ}\text{C}$  ( $\rho = 788.4 \text{ kg/m}^3$  and  $\mu = 5.857 \times 10^{-4} \text{ kg/m}\cdot\text{s}$ ) through a 4 cm diameter pipe is to be measured with a 3 cm diameter orifice meter equipped with a mercury manometer across the orifice plate, as shown in Figure 8. If the differential height of the manometer is 11 cm, calculate the flow rate of methanol through the pipe.

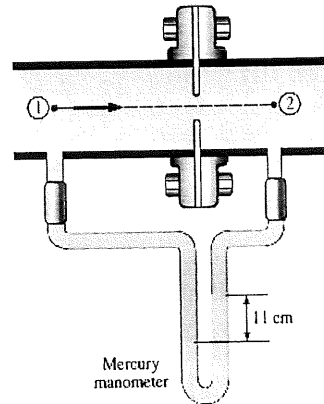


Figure 8

-----End of question-----

**FORMULA**

Specific weight = Weight/Volume

$$W = mg$$

$$\frac{P_1}{\rho g} + \frac{v_1^2}{2g} + z_1 = \frac{P_2}{\rho g} + \frac{v_2^2}{2g} + z_2 SG = \rho_{\text{substance}} / \rho_{\text{water}}$$

$$\dot{V} = A \vartheta A_a \vartheta_a = A_b \vartheta_b$$

$$\dot{m}_1 = \dot{m}_2 \rightarrow \rho_1 \vartheta_1 A_1 = \rho_2 \vartheta_2 A_2$$

$$P = \rho RT$$

$$Re = \frac{\rho V D}{\mu}$$

$$Re = \frac{V D}{\nu}$$

$$\Delta P = \Delta P_L = f \frac{L}{D} \frac{\rho V^2}{2} \quad H_L = f \frac{L}{D} \frac{v_{avg}^2}{2g}$$

$$\frac{1}{\sqrt{f}} = -1.8 \log \left[ \frac{6.9}{Re} + \left( \frac{\epsilon/D}{3.7} \right) \right] C_d$$

$$= Q/Q_{th}$$

$$\dot{V} = A_0 C_d \sqrt{\frac{2(P_1 - P_2)}{\rho(1 - \beta^4)}}$$

$$\dot{W} = \dot{V} \Delta P_L$$

$$D = 4 \frac{A}{p} \text{ (A- cross-sectional area, p is its wetted perimeter)}$$

$$A_0 = A_2 = \pi d^2/4$$

$$\beta = d/D$$

Density of water is  $1000 \frac{kg}{m^3}$ , unless stated otherwise.

$$\text{Useful conversion factor} \frac{1000 kg \cdot m/s^2}{1 kPa \cdot m^2}, \frac{1000 N/m^2}{1 kPa}, \frac{1 kg \cdot m/s^2}{1 N}$$

## FLUID MECHANICS (DTC 1053)

Unit Conversion Table

| Name, Symbol, Dimensions     |                       |            | Conversion Formula  |
|------------------------------|-----------------------|------------|---|
| Length                       | $L$                   | $L$        | $1 \text{ m} = 3.281 \text{ ft} = 1.094 \text{ yd} = 39.37 \text{ in} = \text{km}/1000 = 10^6 \mu\text{m}$<br>$1 \text{ ft} = 0.3048 \text{ m} = 12 \text{ in} = \text{mile}/5280 = \text{km}/3281$<br>$1 \text{ mm} = \text{m}/1000 = \text{in}/25.4 = 39.37 \text{ mil} = 1000 \mu\text{m} = 10^3 \text{ \AA}$  |
| Speed                        | $V$                   | $L/T$      | $1 \text{ m/s} = 3.600 \text{ km/hr} = 3.281 \text{ ft/s} = 2.237 \text{ mph} = 1.944 \text{ knots}$<br>$1 \text{ ft/s} = 0.3048 \text{ m/s} = 0.6818 \text{ mph} = 1.097 \text{ km/hr} = 0.5925 \text{ knots}$   |
| Mass                         | $m$                   | $M$        | $1 \text{ kg} = 2.205 \text{ lbm} = 1000 \text{ g} = \text{slug}/14.59 = (\text{metric ton or tonne or Mg})/1000$<br>$1 \text{ lbm} = \text{lb} \cdot \text{s}^2/(32.17 \text{ ft}) = \text{kg}/2.205 = \text{slug}/32.17 = 453.6 \text{ g}$<br>$= 16 \text{ oz} = 7000 \text{ grains} = \text{short ton}/2000 = \text{metric ton (tonne)}/2205$  |
| Density                      | $\rho$                | $M/L^3$    | $1000 \text{ kg/m}^3 = 62.43 \text{ lbm/ft}^3 = 1.940 \text{ slug/ft}^3 = 8.345 \text{ lbm/gal (US)}$   |
| Force                        | $F$                   | $ML/T^2$   | $1 \text{ lbf} = 4.448 \text{ N} = 32.17 \text{ lbm} \cdot \text{ft/s}^2$<br>$1 \text{ N} = \text{kg} \cdot \text{m/s}^2 = 0.2248 \text{ lbf} = 10^5 \text{ dyne}$  |
| Pressure                     | $P$                   | $M/LT^2$   | $1 \text{ Pa} = \text{N/m}^2 = \text{kg/m} \cdot \text{s}^2 = 10^{-5} \text{ bar} = 1.450 \times 10^{-4} \text{ lbf/in}^2 = \text{inch H}_2\text{O}/249.1$<br>$= 0.007501 \text{ torr} = 10.00 \text{ dyne/cm}^2$<br>$1 \text{ atm} = 101.3 \text{ kPa} = 2116 \text{ psf} = 1.013 \text{ bar} = 14.70 \text{ lbf/in}^2 = 33.90 \text{ ft of water}$<br>$= 29.92 \text{ in of mercury} = 10.33 \text{ m of water} = 760 \text{ mm of mercury} = 760 \text{ torr}$<br>$1 \text{ psi} = \text{atm}/14.70 = 6.895 \text{ kPa} = 27.68 \text{ in H}_2\text{O} = 51.71 \text{ torr}$ |
| Volume                       | $V$                   | $L^3$      | $1 \text{ m}^3 = 35.31 \text{ ft}^3 = 1000 \text{ L} = 264.2 \text{ U.S. gal}$<br>$1 \text{ ft}^3 = 0.02832 \text{ m}^3 = 28.32 \text{ L} = 7.481 \text{ U.S. gal} = \text{acre-ft}/43,560$<br>$1 \text{ U.S. gal} = 231 \text{ in}^3 = \text{barrel (petroleum)}/42 = 4 \text{ U.S. quarts} = 8 \text{ U.S. pints}$<br>$= 3.785 \text{ L} = 0.003785 \text{ m}^3$  |
| Volume Flow Rate (Discharge) | $Q$                   | $L^3/T$    | $1 \text{ m}^3/\text{s} = 35.31 \text{ ft}^3/\text{s} = 2119 \text{ cfm} = 264.2 \text{ gal (US)}/\text{s} = 15850 \text{ gal (US)}/\text{m}$<br>$1 \text{ cfs} = 1 \text{ ft}^3/\text{s} = 28.32 \text{ L}/\text{s} = 7.481 \text{ gal (US)}/\text{s} = 448.8 \text{ gal (US)}/\text{m}$   |
| Mass Flow Rate               | $\dot{m}$             | $M/T$      | $1 \text{ kg/s} = 2.205 \text{ lbm/s} = 0.06852 \text{ slug/s}$   |
| Energy and Work              | $E, W$                | $ML^2/T^2$ | $1 \text{ J} = \text{kg} \cdot \text{m}^2/\text{s}^2 = \text{N} \cdot \text{m} = \text{W} \cdot \text{s} = \text{volt} \cdot \text{coulomb} = 0.7376 \text{ ft} \cdot \text{lbf}$<br>$= 9.478 \times 10^{-4} \text{ Btu} = 0.2388 \text{ cal} = 10^7 \text{ erg} = \text{kWh}/3.600 \times 10^6$  |
| Power                        | $P, \dot{E}, \dot{W}$ | $ML^2/T^3$ | $1 \text{ W} = \text{J/s} = \text{N} \cdot \text{m/s} = \text{kg} \cdot \text{m}^2/\text{s}^3 = 1.341 \times 10^{-3} \text{ hp}$<br>$= 0.7376 \text{ ft} \cdot \text{lbf/s} = 1.0 \text{ volt-ampere} = 0.2388 \text{ cal/s} = 9.478 \times 10^{-4} \text{ Btu/s}$<br>$1 \text{ hp} = 0.7457 \text{ kW} = 550 \text{ ft} \cdot \text{lbf/s} = 33,000 \text{ ft} \cdot \text{lbf/min} = 2544 \text{ Btu/h}$  |

The Moody Chart

