



COURSE NAME: CSE230

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Q1) Compare the time complexity of Merge Sort and Quick Sort. Discuss the scenarios where one algorithm might outperform the other, considering real-world scenarios such as sorting large datasets in database management systems or processing real-time data streams in financial trading platforms.

Ans 1)

On the basis of	Merge sort	Quick sort
Time Complexity	Time Complexity: $O(n \log n)$ in all cases	Average Time Complexity: $O(n \log n)$.
	Merge Sort divides the array into two halves recursively until each sub-array contains only one element. Then, it merges the sorted sub-arrays in a sorted manner. The time complexity of the merge operation is linear, and the total time complexity is $O(n \log n)$, where n is the number of elements in the array	Quick Sort selects a pivot element and partitions the array into two sub-arrays such that elements less than the pivot are on one side, and elements greater than the pivot are on the other side. It then recursively sorts the sub-arrays. In the average case, the time complexity is $O(n \log n)$, but in the worst case, it can degrade to $O(n^2)$

Scenarios where one algorithm might outperform the other:

1) Sorting large datasets in database management systems:

Merge Sort is often preferred in this scenario due to its stable time complexity of $O(n \log n)$. Since database systems typically deal with large datasets, Merge Sort's consistent performance is advantageous.

Quick Sort can also be efficient but may suffer from worst-case scenarios where the dataset is already partially sorted, leading to poor pivot selection and quadratic time complexity. However, Quick Sort's in-place partitioning can be beneficial in terms of memory usage compared to Merge Sort's additional space requirement for merging.

2) processing real-time data streams in financial trading platforms

Quick Sort might be preferred in this scenario due to its average-case time complexity of $O(n \log n)$, which is generally faster than Merge Sort.

The partitioning step of Quick Sort can be highly efficient for sorting real-time data streams, especially if the pivot selection strategy is optimized for the data distribution. This allows for quick updates to the sorted order as new data arrives.

However, the worst-case time complexity of Quick Sort is a concern especially in critical financial systems where consistency and reliability are paramount. In such cases, algorithms like Merge Sort, with their guaranteed performance might be preferred despite their slightly slower average-case time complexity

Q2) Provide a step-by-step explanation of the Quick Sort algorithm with a Java implementation. Discuss the partitioning process and its significance in the sorting process. Illustrate the importance of efficient partitioning in solving real-world problems, such as sorting employee records based on performance ratings or organizing customer feedback data for sentiment analysis.

Ans 2)

Quick Sort is a widely used sorting algorithm that follows the divide-and-conquer strategy. It recursively divides the array into smaller sub-arrays based on a chosen pivot element, and then sorts those sub-arrays. Here's a step-by-step explanation of the Quick Sort algorithm along with a Java implementation:

- 1) Choose a Pivot: Select a pivot element from the array. This pivot will be used to partition the array into two sub-arrays.
- 2) Partitioning: Rearrange the elements in the array so that all elements less than the pivot are placed before it, and all elements greater than the pivot are placed after it. After partitioning, the pivot is in its final sorted position. This step is crucial in Quick Sort and is often implemented using the "partition" function.
- 3) Recursively Sort Sub-arrays: Recursively apply the Quick Sort algorithm to the sub-arrays formed by partitioning until the entire array is sorted.
- 4) Base Case: The recursion stops when the sub-array size becomes 1 or 0, as a single element array is considered sorted.

Partitioning Process and Significance:

The partitioning process is significant because it determines the position of the pivot element in the sorted array. Efficient partitioning ensures that elements smaller than the pivot are on its left, and elements greater than the pivot are on its right.

If the partitioning is done efficiently, the average time complexity of Quick Sort remains $O(n \log n)$, making it a highly efficient sorting algorithm.

Sorting Employee Records Based on Performance Ratings:

You need to sort this dataset based on performance ratings to identify the top-performing employees or to analyse the distribution of performance across different departments.

Efficient Partitioning Significance: Efficient partitioning ensures that feedback entries with similar sentiment scores or sentiments are grouped together in the sorted array or sub-array.

This facilitates quick identification of trends, such as identifying common positive or negative sentiments expressed by customers. It enables targeted analysis of feedback for specific products, services, or marketing campaigns.

Java implementation of the Quick Sort algorithm:

```

public class QuickSort {
    public static void quickSort(int[] arr, int low, int high) {
        if (low < high) {
            int pivotIndex = partition(arr, low, high);
            quickSort(arr, low, pivotIndex - 1);
            quickSort(arr, pivotIndex + 1, high);
        }
    }

    public static int partition(int[] arr, int low, int high) {
        int pivot = arr[high];
        int i = low - 1;
        for (int j = low; j < high; j++) {
            if (arr[j] < pivot) {
                i++;
                swap(arr, i, j);
            }
        }
        swap(arr, i + 1, high);
        return i + 1;
    }

    public static void swap(int[] arr, int i, int j) {
        int temp = arr[i];
        arr[i] = arr[j];
        arr[j] = temp;
    }

    public static void main(String[] args) {
        int[] arr = {10, 7, 8, 9, 1, 5};
        int n = arr.length;
        quickSort(arr, 0, n - 1);
        System.out.println("Sorted array:");
        for (int num : arr) {
            System.out.print(num + " ");
        }
    }
}

```

Q3) Implement Counting Sort in Java and demonstrate its application on an array of integers. Discuss the time complexity of Counting Sort and its suitability for different types of input data. Optimize the CountingSort implementation to handle large datasets efficiently, considering scenarios like sorting student exam scores or analyzing population demographics.

Ans3) Counting Sort is a non-comparison-based sorting algorithm that works well when the range of input data is relatively small

Time Complexity: Counting Sort has a time complexity of $O(n + k)$, where n is the number of elements in the input array and k is the range of the input data.

When the range of input data (k) is much smaller than the number of elements (n), Counting Sort becomes highly efficient, as it doesn't depend on comparisons between elements.

Suitability for Different Types of Input Data: Counting Sort is particularly suitable for scenarios where the range of input data is relatively small, such as sorting exam scores, analyzing population demographics based on age groups, or sorting student grades.

It may not be suitable for sorting datasets with a large range of values or datasets with negative values, as it requires extra preprocessing to handle such cases efficiently.

For sorting student exam scores or analyzing population demographics, Counting Sort can be particularly useful due to its efficiency when dealing with a small range of values. Let's discuss how Counting Sort can be optimized for these scenarios:

Sorting Student Exam Scores:

Data Characteristics: Student exam scores typically fall within a predefined range, such as 0 to 100 or 1 to 10 for grading systems. The range is usually small compared to the number of students.

Memory Optimization: Allocate count arrays based on the range of possible scores, rather than the entire range of integers.

Parallelization: Implement parallel Counting Sort to leverage multi-core processors and speed up sorting for large class sizes.

Streaming Data Handling: Develop algorithms that can handle streaming exam scores efficiently, updating count arrays dynamically as new scores are received.

External Sorting: For exceptionally large datasets, use external sorting techniques to divide the scores into manageable chunks, sort each chunk using Counting Sort, and then merge the sorted chunks.

Java implementation of the Counting Sort and its application on an array of integers:

```
public class CountingSort {
    public static void countingSort(int[] arr) {
        int max = getMax(arr);
        int[] count = new int[max + 1];
        int[] output = new int[arr.length];

        // Count occurrences of each element
        for (int num : arr) {
            count[num]++;
        }

        // Modify count array to store the position of each element
        for (int i = 1; i <= max; i++) {
            count[i] += count[i - 1];
        }

        // Build the output array
        for (int i = arr.length - 1; i >= 0; i--) {
            output[count[arr[i]] - 1] = arr[i];
            count[arr[i]]--;
        }

        // Copy sorted elements back to the original array
        System.arraycopy(output, 0, arr, 0, arr.length);
    }

    private static int getMax(int[] arr) {
        int max = arr[0];
        for (int num : arr) {
            if (num > max) {
                max = num;
            }
        }
        return max;
    }

    public static void main(String[] args) {
        int[] arr = {4, 2, 2, 8, 3, 3, 1};
        System.out.println("Original array:");
        printArray(arr);
        countingSort(arr);
        System.out.println("Sorted array:");
        printArray(arr);
    }

    private static void printArray(int[] arr) {
        for (int num : arr) {
            System.out.print(num + " ");
        }
        System.out.println();
    }
}
```

Q4) Compare the space complexity of Merge Sort, Quick Sort, and Heap Sort. Analyse how the space requirements of these algorithms impact their performance in resource-constrained environments, such as embedded systems or mobile applications processing large datasets.

Ans3)

On the basis of	Merge sort	Quick sort	Heap sort
Space Complexity	Space Complexity: $O(n)$	Space Complexity: $O(\log n)$ to $O(n)$	Space Complexity: $O(1)$
More about	Merge Sort typically requires additional space proportional to the size of the input array for the temporary arrays used during the merging process.	Quick Sort is an in-place sorting algorithm, meaning it doesn't require additional space proportional to the input size in the average case.	Heap Sort is an in-place sorting algorithm, meaning it doesn't require additional space proportional to the input size.
Worst case/ comparison	The space complexity of Merge Sort remains consistent regardless of the input data or its distribution	However, in the worst case, Quick Sort may require $O(n)$ space for the call stack due to recursive function calls if the pivot selection is poor and the input array is already sorted or nearly sorted.	Heap Sort operates directly on the input array, rearranging the elements to form a max-heap or min-heap without using additional data structures.

Embedded systems

Merge sort	Quick sort	Heap sort
Space Complexity: $O(n)$	Space Complexity: $O(\log n)$ to $O(n)$	Space Complexity: $O(1)$
Merge Sort's space complexity makes it less suitable for embedded systems with tight memory constraints.	Quick Sort's average-case space complexity of $O(\log n)$ makes it more favorable in embedded systems with limited memory.	Heap Sort's constant space complexity makes it highly suitable for embedded systems with limited memory resources.
In scenarios where memory usage must be minimized, allocating additional memory for Merge	The in-place nature of Quick Sort, where it typically doesn't require additional memory	Since Heap Sort operates directly on the input array and doesn't require additional memory, it is

Sort's temporary arrays can strain the limited resources of embedded systems.	beyond the input array, is advantageous in resource-constrained environments.	efficient in terms of memory usage.
However, if memory constraints are not overly restrictive and stability or predictable performance is more critical, Merge Sort might still be a viable option due to its stable time complexity and ease of implementation.	However, the worst-case space complexity of $O(n)$ due to stack space required for recursive function calls can still be a concern in extremely memory-constrained embedded systems or with very large datasets.	Heap Sort's predictable space requirements make it particularly attractive for embedded systems where memory usage must be carefully managed.

Q5) Discuss the stability of Counting Sort and Radix Sort. Explain why stability is an important characteristic in certain sorting applications, such as maintaining order in financial transaction records or preserving the sequence of customer reviews in e-commerce platforms.

Ans5) Stability in sorting algorithms refers to the ability of the algorithm to maintain the relative order of elements with equal keys. In other words, if two elements have the same key value, a stable sorting algorithm ensures that their original order is preserved in the sorted output

Counting sort	Radix sort
Counting Sort is a stable sorting algorithm. Since Counting Sort uses counting frequencies to determine the position of each element in the sorted output, elements with the same key value are placed in the output array in the order they appear in the input array.	Radix Sort can be stable or unstable depending on the implementation. When Radix Sort uses a stable sorting algorithm as a subroutine (such as Counting Sort or a stable version of Quick Sort) to sort elements at each digit position, it retains the stability property.
For example, if we have two elements with the same key value, say A and B, and A appears before B in the input array, Counting Sort ensures that A will appear before B in the sorted output if they have the same key value.	However, if an unstable sorting algorithm is used as a subroutine in Radix Sort, the overall sorting may become unstable

Financial Transaction Records:

In financial systems, maintaining the order of transactions is crucial for ensuring accuracy and consistency in financial records. For example, when sorting transactions based on transaction timestamps or transaction IDs, stability ensures that transactions with the same timestamp or ID remain in their original order, preventing discrepancies in financial reporting.

E-commerce Platforms

In e-commerce platforms, preserving the sequence of customer reviews is essential for providing accurate product feedback and maintaining customer trust. If multiple customers provide reviews with the same rating or timestamp, a stable sorting algorithm ensures that their reviews appear in the

same order they were submitted. This preserves the chronological or user-specific sequence of reviews, helping users make informed purchasing decisions.