

Welcome 😊

Reattempt 1 not

3 hrs.

reflected.

5<sup>th</sup> Aug 12:01 am → 9 days

Agenda: Hashing 2

① Pair sum = K

② distinct elements in every window of len = K

Q Given N array elements, check if there exists a pair (i, j) such that  $arr[i] + arr[j] = K$  &  $i \neq j$

arr[] :    0    1    2    3    4    5    6    7    8    9  
          8    9    1    -2    4    5    11    -6    7    5

K=11    i    j     $arr[4] + arr[8] \Rightarrow 4 + 7 \Rightarrow 11$

K=6    2    5     $arr[2] + arr[5] \Rightarrow 1 + 5 \Rightarrow 6$

K=22    no such pair. return false.

Ideas

Idea 1

Check every pair sum = K.

T.C →  $O(N^2)$  S.C →  $O(1)$

Pseudo code

TO DO

Idea 2

arr[] : <sup>0</sup>8 <sup>1</sup>9 <sup>2</sup>1 <sup>3</sup>-2 <sup>4</sup>4 <sup>5</sup>5 <sup>6</sup>11 <sup>7</sup>-6 <sup>8</sup>7 <sup>9</sup>5

Optimisation using hashset  
Insert all elements in hashset.

$$K = 11$$
$$a + b = 11$$

a	b = (K - a)	Yes/No
8	3	X
9	2	X
1	10	X
-2	13	X
4	7	✓✓ return True.

a	b	Yes/No
8	-3	X
9	-4	X
1	4	✓✓ return True.

arr[] : <sup>0</sup>8 <sup>1</sup>9 <sup>2</sup>1 <sup>3</sup>-2 <sup>4</sup>4 <sup>5</sup>5 <sup>6</sup>11 <sup>7</sup>-6 <sup>8</sup>7 <sup>9</sup>5

$$a + b = 22$$

Edge case.

a	b	Yes/No
8	14	X
9	13	X
1	21	X
-2	24	X
4	18	X
5	17	X
11	11	✓

return True but  $i = j$ .  
Therefore this case not valid.

### Idea 3

Optimisation using hashmap  $\langle \text{int}, \text{int} \rangle$   
 $\downarrow \quad \downarrow$   
 $\text{arr}[i] \quad \text{freq.}$

$\text{arr}[] :$     <sup>0</sup>8    <sup>1</sup>9    <sup>2</sup>4    <sup>3</sup>-2    <sup>4</sup>4    <sup>5</sup>5    <sup>6</sup>11    <sup>7</sup>-6    <sup>8</sup>7    <sup>9</sup>5

$$K = 10$$

① insert all the elements in the map.

$\langle 8, 1 \rangle$   $\langle 9, 1 \rangle$   $\langle 4, 2 \rangle$   $\langle -2, 1 \rangle$  ,

$\langle 5, 2 \rangle$   $\langle 11, 1 \rangle$   $\langle -6, 1 \rangle$   $\langle 7, 1 \rangle$   ~~$\langle 5, 1 \rangle$~~

$$a + b = 10$$

a	b (K-a)	yes/no
8	2	X
9	1	X
4	6	X
-2	12	X
4	6	X
5	5	Yes <sup><math>a=b</math></sup> , $\text{freq}[b] > 1$

$$\underline{\underline{K = 22}}$$

a	b	yes/no.
8	14	X
9	13	X
4	18	X
-2	24	X
4	18	X
5	17	X
11	11	<u>NO</u> b/c freq of 11 is <u>1</u>

## Pseudo code

```
bool pairSum ( int a[], int K )  
{  
    hashmap < int, int > hm;  
    ① Insert all the elements in hashmap  
    for ( int i = 0; i < n; i++ )  
    {  
        a = arr[i]          b = K - a  
        if ( a != b && hm.search(b) == true )  
            return true;  
        else if ( a == b && hm[a] > 1 )  
            return true;  
    }  
    return false;  
}
```

## Idea 4 Optimization using hashset

arr[] :    0    1    2    3    4    5    6    7    8    9  
          8    9    1    -2   4    5   11   7    5   -6

idea  $\Rightarrow$  if we are at index  $i$ , insert only  $[0, i-1]$  elements in hashset.

$K = 11$

a	b	<u>H-S</u>	Yes/No.
8	3	{ 3 } $\nearrow$ insert 8	X
9	2	{ 8 }	X
		$\nearrow$ insert 9	
1	10	{ 8, 9 }	X

-2	13	$\{ 8, 9, 1 \}$ $\swarrow$ insert 1	X
4	7	$\{ 8, 9, 1, -2 \}$ $\swarrow$ insert -2	X
5	6	$\{ 8, 9, 1, -2, 4 \}$ $\swarrow$ insert 4	X
11	0	$\{ 8, 9, 1, -2, 4, 5 \}$ $\swarrow$ insert 5	X
7	4	$\{ 8, 9, 1, -2, 4, 5, 11 \}$ $\swarrow$ insert 11	$\checkmark$ <u>return true</u>

### Pseudo code

```

bool targetSumSet ( int arr[], int K )
{
    int n = arr.length;
    HashSet<int> hs;
    for ( int i = 0 ; i < n ; i++ )
    {
        a = arr[i]      b = K - a
        if ( hs.search(b) == true ) return true;
        hs.insert(a)
    }
    return false.
}
  
```

T.C  $\rightarrow O(N)$   
S.C  $\rightarrow O(N)$

Q2 Given  $N$  elements, calculate no. of distinct elements in every subarray of size  $K$

eg:  $a[]$  :  $\overset{0}{2} \ \overset{1}{4} \ \overset{2}{3} \ \overset{3}{8} \ \overset{4}{3} \ \overset{5}{9} \ \overset{6}{4} \ \overset{7}{9} \ \overset{8}{4} \ \overset{9}{10}$

$K = 4$

Subarrays	print
$[0, 3]$	4
$[1, 4]$	3
$[2, 5]$	3
$[3, 6]$	4
$[4, 7]$	3
$[5, 8]$	<del>2</del>
$[6, 9]$	3

Idea 1

→ For every subarray of  $\text{len} = K$ , insert into hashtable and get no. of distinct elements.

$$\text{T.C} \Rightarrow (n - K + 1) * K$$

$\downarrow$                        $\downarrow$   
 # subarray      subarray len  
 of size  $K$ .

$$K = N/2 \Rightarrow \left(N - \frac{N}{2} + 1\right) * \left(\frac{N}{2}\right)$$

$$\Rightarrow O(N^2)$$

$$\text{S.C} \Rightarrow O(K)$$

Idea 2 Optimisation using hashtable.

eg:  $a[]$  :  $\overset{0}{2} \ \overset{1}{4} \ \overset{2}{3} \ \overset{3}{8} \ \overset{4}{3} \ \overset{5}{9} \ \overset{6}{4} \ \overset{7}{9} \ \overset{8}{4} \ \overset{9}{10}$

$K = 4$

$[0, 3] \longrightarrow \{2, 4, 3, 8\} \Rightarrow 4$

$[1, 4]$       ~~delete~~  $\text{arr}[0]$       ~~add~~  $\text{arr}[4]$       H.S  $\rightarrow \{4, 3, 8\} \Rightarrow 3$

$[2, 5]$        $\text{arr}[1]$        $\text{arr}[5]$       H.S  $\Rightarrow \{3, 8, 9\} \Rightarrow 3$

$[3, 6]$        $\text{arr}[2]$        $\text{arr}[6]$       H.S  $\Rightarrow \{\cancel{8}, \cancel{9}, 4\} \Rightarrow \cancel{3}$   
4 ✓

→ In hashtable, deleting element indirectly deletes all occurrences

### Idea 3 Optimisation using hashmap.

eg:  $a[]$  :  $\overset{0}{2} \quad \overset{1}{4} \quad \overset{2}{3} \quad \overset{3}{8} \quad \overset{4}{3} \quad \overset{5}{9} \quad \overset{6}{4} \quad \overset{7}{9} \quad \overset{8}{4} \quad \overset{9}{10}$   
 $K=4$

$arr[0,3] \longrightarrow \{ \langle 2,1 \rangle, \langle 4,1 \rangle, \langle 3,1 \rangle, \langle 8,1 \rangle \}$

$arr[1,4]$   $arr[0]$   $arr[4] \Rightarrow$   $\{ \langle 2,0 \rangle, \langle 4,1 \rangle, \langle 3,1 \rangle, \langle 8,1 \rangle \}$   
*delete* *add*  $\rightarrow$  since freq = 0, remove from hashing.  $\langle 3,1 \rangle$   $\downarrow$   $\langle 3,2 \rangle$   $\{ \}$   $\textcircled{4}$   $\textcircled{3}$

$arr[2,5]$   $arr[1]$   $arr[5] \Rightarrow \{ \langle 4,0 \rangle, \langle 8,1 \rangle, \langle 3,2 \rangle, \langle 9,1 \rangle \}$   $\textcircled{3}$

### Pseudo code

void distinctElements ( int arr[], int K )

{

int n = arr.len

hashmap < int, int > hm ;

// insert K elements in hm  $\rightarrow [0, K-1]$

for ( int i = 0 ; i < K ; i++ )  $\longrightarrow$  T.C =  $O(K)$

{ if ( hm.search ( arr[i] ) == true )

hm[arr[i]] += 1 ;

else

hm.insert ( arr[i], 1 ) ;

}

print ( hm.size() ) ;

s = 1

e = K

while ( e < N )

{

// sub [s, e] , remove s-1 , add e

hm[arr[s-1]] -= 1 ; // reduced freq by 1

$\longrightarrow$  T.C =  $O(N-K)$

```

    if ( hm[arr[s-1]] == 0 )
    {
        // remove element from hash map
        hm.remove ( arr[s-1] );
    }
    if ( hm.search ( arr[e] ) == true )
    {
        // increase freq by 1
        hm[arr[e]] += 1 ;
    }
    else {
        hm.insert ( arr[e], 1 );
    }
    s++;
    e++;
    print ( hm.size() );
}

```

Actual T.C  
 $K + (N-K)$

T.C  $\Rightarrow O(N)$

S.C  $\Rightarrow O(K)$   
 ~~$O(N)$~~

## Doubt session

Contest 1      Reattempt 2,3       $\Rightarrow$  next week.

Contest 2      Reattempt 2       $\Rightarrow$  live on  
 5<sup>th</sup> Aug 12:01 am  
 for 9 days.



[1, 2, 1]

Count sort

~~Count~~ Sorted array

a a a b b d f a a b c

---

a → 4  
b → 2  
d → 4

a a a a b b d d d d