

Welcome 😊

Agenda: 10 questions

Q Given an integer array A, find the index of nearest smaller element on left of $A[i]$.

Formally, find j st $A[j] < A[i]$ & $j < i$ & j has to be max.

eg:

0	1	2	3	4	5	6	7
8	2	4	9	7	5	3	10
-1	-1	1	2	2	2	1	6

Sol 1 \Rightarrow Brute force \Rightarrow \forall index travel towards left & find nearest smaller element.

T.C $\rightarrow O(N^2)$
S.C $\rightarrow O(1)$

Sol 2

0	1	2	3	4	5	6	7
8	—	—	—	—	5	<u>u</u>	—

$u \leq 5$
 $5 < u \leq 8$
 $u > 8$

Ans $\neq 0$
Ans = 5
Ans = 5
Ans $\neq 0$

0	1	2	3	4	5	6	7
8	2	4	9	7	5	3	10
-1	-1	1	2	2	2	1	6

\rightarrow check for the rightmost (latest) smaller element on left. \rightarrow stack

code

```

for ( i → 0 to N-1 )
{
    while ( ! st.isEmpty() && A[st.peek()] >= A[i] )
    {
        st.pop()
    }
    if ( st.isEmpty() )
        ans[i] = -1
    else
        ans[i] = st.peek()
    st.push(i)
}

```

T.C → $O(N)$
S.C → $O(N)$

✓ 0	✓ 1	✓ 2	✓ 3	✓ 4	5	6	7
8	2	4	9	7	5	3	10
-1	-1	1	2	2			

4
3
2
1
0

Q2 At: find nearest smaller or equal on left

Q3 At: find nearest greater on left

Q4 At: find nearest greater or equal on left

Q5 At: find nearest smaller on right

code

```

for ( i → N-1 to 0 )
{
    while ( ! st.isEmpty() && A[st.peek()] >= A[i] )
    {
        st.pop()
    }
    if ( st.isEmpty() )

```

```

        ans[i] = -1
    else
        ans[i] = st.peek()
    st.push(i)
}
T.C  $\rightarrow O(N)$ 
S.C  $\rightarrow O(N)$ 

```

✓ 0	✓ 1	✓ 2	✓ 3	✓ 4	5	6	7
8	2	4	9	7	5	3	10
-1	-1	1	2	2			

4
3
2
1
0

Q6 $\forall i$ find nearest smaller or equal on right

Q7 $\forall i$ find nearest greater on right

Q8 $\forall i$ find nearest greater or equal on right

Q9 Given an integer array with distinct integers, \forall subarrays, find (max-min) & return its sum as ans.

eg: [2 5 3] \Rightarrow 2 $\Rightarrow (2-2)$ 5 $\Rightarrow (5-5)$
 2 5 $\Rightarrow (5-2)$ 5 3 $\Rightarrow (5-3)$
 2 5 3 $\Rightarrow (5-2)$ 3 $\Rightarrow (3-3)$
8

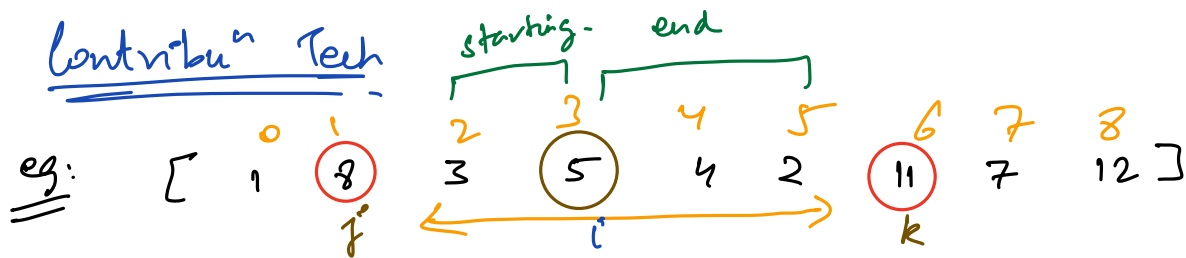
Sol1 Brute force

\forall subarray
 $\Sigma (\text{max} - \text{min})$

T.C $\Rightarrow O(N^3) \rightarrow O(N^2)$
 S.C $\Rightarrow O(1)$

Sol²

Contribution Tech



$\sum_{i=0}^{N-1}$ Contribution of $A[i]$

$$\text{Contribution} = A[i] * \left(\begin{array}{l} \# \text{ subarrays where } A[i] \text{ is max} \\ - \# \text{ subarrays where } A[i] \text{ is min} \end{array} \right)$$

$j \rightarrow$ nearest greater on left of i

$k \rightarrow$ nearest greater on right of i

$$\# \text{ subarrays} \Rightarrow (i - j) * (k - i)$$

Code

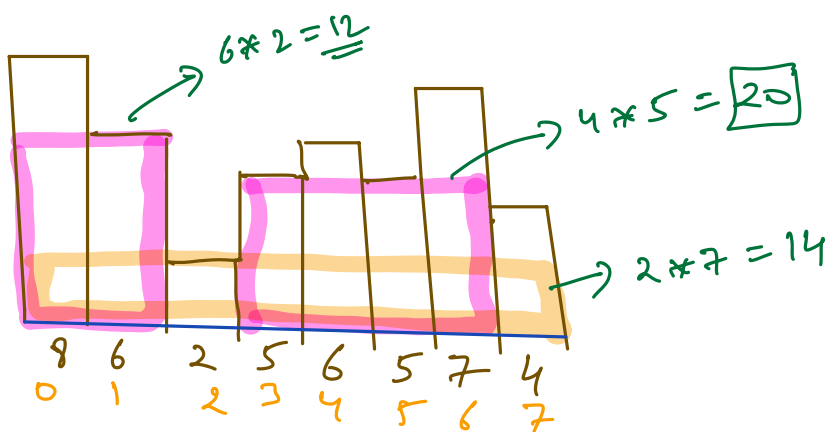
$$\text{Ans} = \sum_{i=0}^{N-1} A[i] * \left((i - \text{ng_left}(i)) * (\text{ng_right}(i) - i) - (i - \text{ns_left}(i)) * (\text{ns_right}(i) - i) \right)$$

$$\text{T.C} \rightarrow O(N)$$

$$\text{S.C} \rightarrow O(N)$$

Q10 Given an integer array A , where $A[i]$ is the height of i^{th} bar. width of each bar is 1. Find the area of largest rectangle formed by continuous bars.

eg:



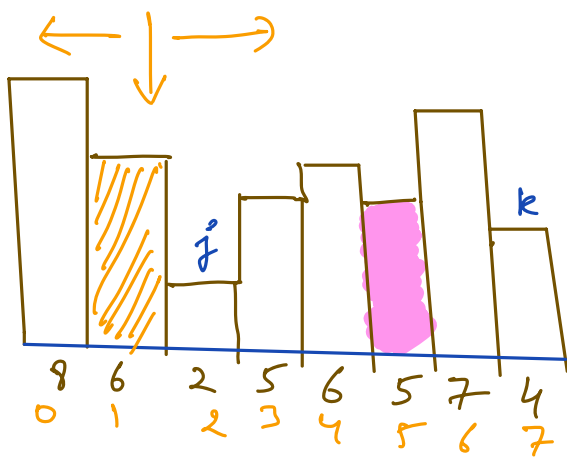
Brute force

For all subarrays as base
find min height & calc. area

min ele. in subarray B x H

T.C $\rightarrow O(N^3) \rightarrow O(N^2)$

S.C $\rightarrow O(1)$



$j \rightarrow$ Smaller ele. on left of i $k \rightarrow$ nearest smaller ele. on right of i

$$\text{Area} = (k - j - 1) * A[i]$$

code

$N-1$
for $i=0$

$$\max \left(A[i] * (ns_right(i) - ns_left(i) - 1) \right)$$

\rightarrow if not present return N

\downarrow
if not present
return -1

T.C $\rightarrow O(N)$

S.C $\rightarrow O(N)$