# R - Statistical Inference Course Project - Part 1

Uday T

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#### A Simulation Exercise

In this project you will investigate the exponential distribution in R and compare it with the Central Limit Theorem. The exponential distribution can be simulated in R with rexp(n, lambda) where lambda is the rate parameter. The mean of exponential distribution is 1/lambda and the standard deviation is also 1/lambda. Set lambda = 0.2 for all of the simulations. You will investigate the distribution of averages of 40 exponentials. Note that you will need to do a thousand simulations.

#### 1. Show the sample mean and compare it to the theoretical mean of the distribution.

We will create a simulation sample called simulated\_samp each of size 40 drawn from exponential distribution with rate parameterlambda = 0.2 Seed will be set at 333 to make the simulation reproducible.

```
library(ggplot2)
```

## Warning: package 'ggplot2' was built under R version 3.6.1

```
# set seed for reproducability
set.seed(333)
# set lambda to 0.2
lambda <- 0.2
# 40 samples
n <- 40
# 1000 simulations
n.sim <- 1000
# simulate
sim_sample <- matrix(rexp(n*n.sim, rate = lambda), nrow = n.sim, ncol = n)
# calculate mean of exponentials
sim_samp_mean <- apply(sim_sample, 1, mean)
mean(sim_samp_mean)</pre>
```

## [1] 5.045337

```
# Theoritical mean
theo_mean <- 1/lambda
theo_mean</pre>
```

## [1] 5

The sample mean is 5.0453, which is close to the theoretical mean!

2. Show how variable the sample is (via variance) and compare it to the theoretical variance of the distribution.

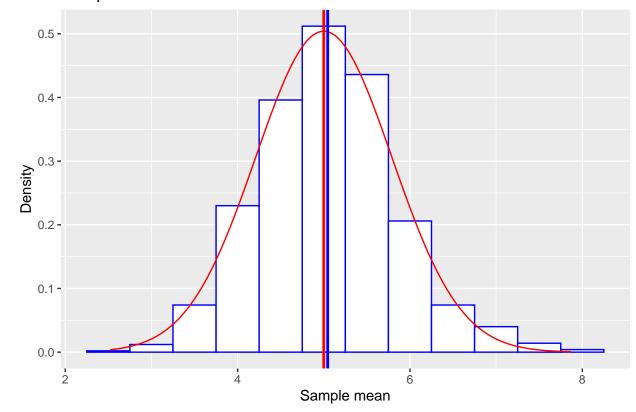
```
var(sim_samp_mean)
## [1] 0.6260539
theo_var <- (1 / lambda ^ 2) / n
theo_var</pre>
```

## [1] 0.625

The sample variance is 0.626, which is also close the theoretical variance 0.625

### 3. Show that the distribution is approximately normal

## Sample distribution and Theoretical distribution



The above figure shows the distribution of the sample mean. It is Approximately Normally Distributed (AND). The red density curve corresponds to N(5,0.626) density. This proves the Central Limit Theorem, As the sample size increases it will tend to move towards a perfectly normal distribution.