



Learning Apache Spark with Python

Wenqiang Feng

July 21, 2019

CONTENTS

1 Preface	3
1.1 About	3
1.2 Motivation for this tutorial	4
1.3 Copyright notice and license info	4
1.4 Acknowledgement	4
1.5 Feedback and suggestions	5
2 Why Spark with Python ?	7
2.1 Why Spark?	7
2.2 Why Spark with Python (PySpark)?	8
3 Configure Running Platform	11
3.1 Run on Databricks Community Cloud	11
3.2 Configure Spark on Mac and Ubuntu	16
3.3 Configure Spark on Windows	19
3.4 PySpark With Text Editor or IDE	19
3.5 PySparkling Water: Spark + H2O	26
3.6 Set up Spark on Cloud	27
3.7 Demo Code in this Section	27
4 An Introduction to Apache Spark	29
4.1 Core Concepts	29
4.2 Spark Components	29
4.3 Architecture	32
4.4 How Spark Works?	32
5 Programming with RDDs	33
5.1 Create RDD	33
5.2 Spark Operations	37
5.3 <code>rdd.DataFrame</code> vs <code>pd.DataFrame</code>	39
6 Statistics and Linear Algebra Preliminaries	55
6.1 Notations	55
6.2 Linear Algebra Preliminaries	55
6.3 Measurement Formula	57
6.4 Confusion Matrix	58

6.5	Statistical Tests	59
7	Data Exploration	61
7.1	Univariate Analysis	61
7.2	Multivariate Analysis	74
8	Regression	81
8.1	Linear Regression	81
8.2	Generalized linear regression	93
8.3	Decision tree Regression	100
8.4	Random Forest Regression	106
8.5	Gradient-boosted tree regression	113
9	Regularization	121
9.1	Ordinary least squares regression	121
9.2	Ridge regression	121
9.3	Least Absolute Shrinkage and Selection Operator (LASSO)	122
9.4	Elastic net	122
10	Classification	123
10.1	Binomial logistic regression	123
10.2	Multinomial logistic regression	134
10.3	Decision tree Classification	145
10.4	Random forest Classification	154
10.5	Gradient-boosted tree Classification	164
10.6	XGBoost: Gradient-boosted tree Classification	164
10.7	Naive Bayes Classification	166
11	Clustering	179
11.1	K-Means Model	179
12	RFM Analysis	191
12.1	RFM Analysis Methodology	192
12.2	Demo	194
12.3	Extension	200
13	Text Mining	207
13.1	Text Collection	207
13.2	Text Preprocessing	215
13.3	Text Classification	217
13.4	Sentiment analysis	224
13.5	N-grams and Correlations	231
13.6	Topic Model: Latent Dirichlet Allocation	231
14	Social Network Analysis	249
14.1	Introduction	249
14.2	Co-occurrence Network	249
14.3	Appendix: matrix multiplication in PySpark	253
14.4	Correlation Network	256

15 ALS: Stock Portfolio Recommendations	257
15.1 Recommender systems	258
15.2 Alternating Least Squares	259
15.3 Demo	259
16 Monte Carlo Simulation	267
16.1 Simulating Casino Win	267
16.2 Simulating a Random Walk	269
17 Markov Chain Monte Carlo	279
17.1 Metropolis algorithm	279
17.2 A Toy Example of Metropolis	280
17.3 Demos	281
18 Neural Network	289
18.1 Feedforward Neural Network	289
19 Wrap PySpark Package	293
19.1 Package Wrapper	293
19.2 Pacakge Publishing on PyPI	295
20 PySpark Data Audit Library	297
20.1 Install with pip	297
20.2 Install from Repo	297
20.3 Uninstall	297
20.4 Test	298
20.5 Auditing on Big Dataset	299
21 Zeppelin to jupyter notebook	309
21.1 How to Install	309
21.2 Converting Demos	310
22 My Cheat Sheet	315
23 PySpark API	319
23.1 Stat API	319
23.2 Regression API	325
23.3 Classification API	346
23.4 Clustering API	369
23.5 Recommendation API	385
23.6 Pipeline API	390
23.7 Tuning API	392
23.8 Evaluation API	397
24 Main Reference	403
Bibliography	405
Python Module Index	407



Welcome to my **Learning Apache Spark with Python** note! In this note, you will learn a wide array of concepts about **PySpark** in Data Mining, Text Mining, Machine Learning and Deep Learning. The PDF version can be downloaded from [HERE](#).

**CHAPTER
ONE**

PREFACE

1.1 About

1.1.1 About this note

This is a shared repository for [Learning Apache Spark Notes](#). The PDF version can be downloaded from [HERE](#). The first version was posted on Github in [ChenFeng \(\[Feng2017\]\)](#). This shared repository mainly contains the self-learning and self-teaching notes from Wenqiang during his [IMA Data Science Fellowship](#). The reader is referred to the repository <https://github.com/runawayhorse001/LearningApacheSpark> for more details about the dataset and the .ipynb files.

In this repository, I try to use the detailed demo code and examples to show how to use each main functions. If you find your work wasn't cited in this note, please feel free to let me know.

Although I am by no means an data mining programming and Big Data expert, I decided that it would be useful for me to share what I learned about PySpark programming in the form of easy tutorials with detailed example. I hope those tutorials will be a valuable tool for your studies.

The tutorials assume that the reader has a preliminary knowledge of programming and Linux. And this document is generated automatically by using [sphinx](#).

1.1.2 About the authors

- **Wenqiang Feng**
 - Sr. Data Scientist and PhD in Mathematics
 - University of Tennessee at Knoxville
 - Email: von198@gmail.com

- **Biography**

Wenqiang Feng is a Sr. Data Scientist at HR & Block. Before joining Block, Dr. Feng is a Data Scientist at Applied Analytics Group, DST (now SS&C). Dr. Feng's responsibilities include providing clients with access to cutting-edge skills and technologies, including Big Data analytic solutions, advanced analytic and data enhancement techniques and modeling.

Dr. Feng has deep analytic expertise in data mining, analytic systems, machine learning algorithms, business intelligence, and applying Big Data tools to strategically solve industry problems in a cross-functional business. Before joining DST, Dr. Feng was an IMA Data Science Fellow at The Institute for Mathematics and its Applications (IMA) at the University of Minnesota. While there, he helped startup companies make marketing decisions based on deep predictive analytics.

Dr. Feng graduated from University of Tennessee, Knoxville, with Ph.D. in Computational Mathematics and Master's degree in Statistics. He also holds Master's degree in Computational Mathematics from Missouri University of Science and Technology (MST) and Master's degree in Applied Mathematics from the University of Science and Technology of China (USTC).

- **Declaration**

The work of Wenqiang Feng was supported by the IMA, while working at IMA. However, any opinion, finding, and conclusions or recommendations expressed in this material are those of the author and do not necessarily reflect the views of the IMA, UTK, DST and HR & Block.

1.2 Motivation for this tutorial

I was motivated by the [IMA Data Science Fellowship](#) project to learn PySpark. After that I was impressed and attracted by the PySpark. And I foud that:

1. It is no exaggeration to say that Spark is the most powerful Bigdata tool.
2. However, I still found that learning Spark was a difficult process. I have to Google it and identify which one is true. And it was hard to find detailed examples which I can easily learned the full process in one file.
3. Good sources are expensive for a graduate student.

1.3 Copyright notice and license info

This [Learning Apache Spark with Python](#) PDF file is supposed to be a free and living document, which is why its source is available online at <https://runawayhorse001.github.io/LearningApacheSpark/pyspark.pdf>. But this document is licensed according to both [MIT License](#) and [Creative Commons Attribution-NonCommercial 2.0 Generic \(CC BY-NC 2.0\) License](#).

When you plan to use, copy, modify, merge, publish, distribute or sublicense, Please see the terms of those licenses for more details and give the corresponding credits to the author.

1.4 Acknowledgement

At here, I would like to thank Ming Chen, Jian Sun and Zhongbo Li at the University of Tennessee at Knoxville for the valuable disscussion and thank the generous anonymous authors for providing the detailed solutions and source code on the internet. Without those help, this repository would not have been possible to be made. Wenqiang also would like to thank the [Institute for Mathematics and Its Applications \(IMA\)](#) at [University of Minnesota, Twin Cities](#) for support during his IMA Data Scientist Fellow visit.

A special thank you goes to [Dr. Haiping Lu](#), Lecturer in Machine Learning at Department of Computer Science, University of Sheffield, for recommending and heavily using my tutorial in his teaching class and for the valuable suggestions.

1.5 Feedback and suggestions

Your comments and suggestions are highly appreciated. I am more than happy to receive corrections, suggestions or feedbacks through email (von198@gmail.com) for improvements.

WHY SPARK WITH PYTHON ?

Chinese proverb

Sharpening the knife longer can make it easier to hack the firewood – old Chinese proverb

I want to answer this question from the following two parts:

2.1 Why Spark?

I think the following four main reasons from Apache Spark™ official website are good enough to convince you to use Spark.

1. Speed

Run programs up to 100x faster than Hadoop MapReduce in memory, or 10x faster on disk.

Apache Spark has an advanced DAG execution engine that supports acyclic data flow and in-memory computing.



Fig. 1: Logistic regression in Hadoop and Spark

2. Ease of Use

Write applications quickly in Java, Scala, Python, R.

Spark offers over 80 high-level operators that make it easy to build parallel apps. And you can use it interactively from the Scala, Python and R shells.

3. Generality

Combine SQL, streaming, and complex analytics.

Spark powers a stack of libraries including SQL and DataFrames, MLlib for machine learning, GraphX, and Spark Streaming. You can combine these libraries seamlessly in the same application.

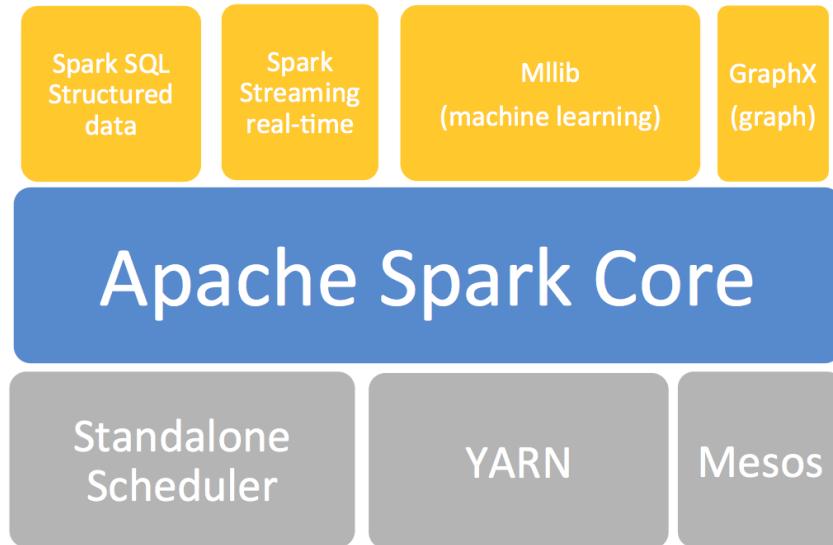


Fig. 2: The Spark stack

4. Runs Everywhere

Spark runs on Hadoop, Mesos, standalone, or in the cloud. It can access diverse data sources including HDFS, Cassandra, HBase, and S3.

2.2 Why Spark with Python (PySpark)?

No matter you like it or not, Python has been one of the most popular programming languages.



Fig. 3: The Spark platform



Fig. 4: KDnuggets Analytics/Data Science 2017 Software Poll from [kdnnuggets](#).

**CHAPTER
THREE**

CONFIGURE RUNNING PLATFORM

Chinese proverb

Good tools are prerequisite to the successful execution of a job. – old Chinese proverb

A good programming platform can save you lots of troubles and time. Herein I will only present how to install my favorite programming platform and only show the easiest way which I know to set it up on Linux system. If you want to install on the other operator system, you can Google it. In this section, you may learn how to set up Pyspark on the corresponding programming platform and package.

3.1 Run on Databricks Community Cloud

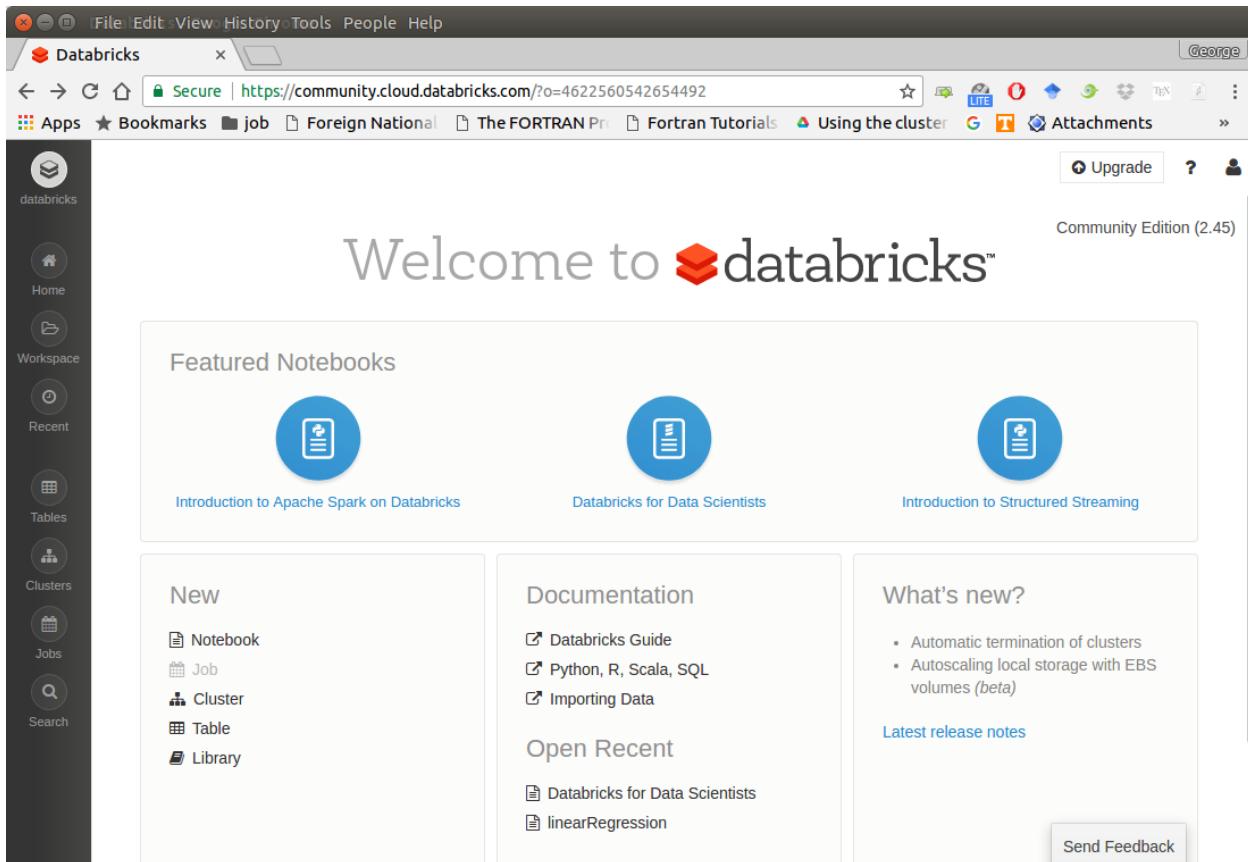
If you don't have any experience with Linux or Unix operator system, I would love to recommend you to use Spark on Databricks Community Cloud. Since you do not need to setup the Spark and it's totally **free** for Community Edition. Please follow the steps listed below.

1. Sign up a account at: <https://community.cloud.databricks.com/login.html>
2. Sign in with your account, then you can creat your cluster(machine), table(dataset) and notebook(code).
3. Create your cluster where your code will run
4. Import your dataset

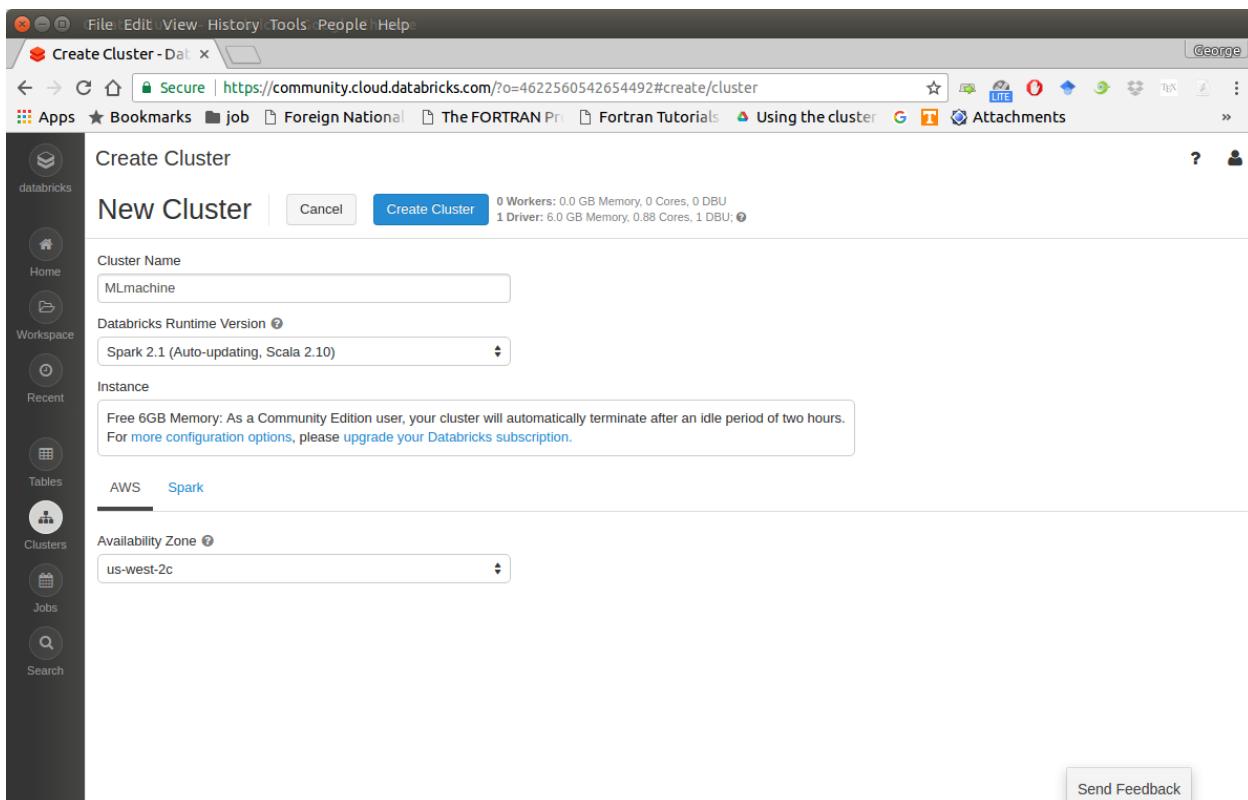
Note: You need to save the path which appears at Uploaded to DBFS: /File-Store/tables/05rmhuqv1489687378010/. Since we will use this path to load the dataset.

5. Creat your notebook





The screenshot shows the Databricks Community Edition (2.45) homepage. On the left is a dark sidebar with icons for Home, Workspace, Recent, Tables, Clusters, Jobs, and Search. The main area has a "Welcome to databricks™" header. Below it is a "Featured Notebooks" section with three circular icons labeled "Introduction to Apache Spark on Databricks", "Databricks for Data Scientists", and "Introduction to Structured Streaming". Underneath are three columns: "New" (Notebook, Job, Cluster, Table, Library), "Documentation" (Databricks Guide, Python, R, Scala, SQL, Importing Data), and "What's new?" (Automatic termination of clusters, Autoscaling local storage with EBS volumes (beta)). A "Send Feedback" button is at the bottom right.



The screenshot shows the "Create Cluster" dialog. The title bar says "Create Cluster - Dat x". The main form has a "New Cluster" tab selected. It includes fields for "Cluster Name" (set to "MLmachine"), "DataBricks Runtime Version" (set to "Spark 2.1 (Auto-updating, Scala 2.10)"), and "Instance" (a note about free memory and upgrade options). Below that are tabs for "AWS" and "Spark", and a "Availability Zone" dropdown set to "us-west-2c". A "Send Feedback" button is at the bottom right.

Learning Apache Spark with Python

The screenshot shows the 'Create Table' interface in Databricks. On the left is a sidebar with icons for Home, Workspace, Recent, Tables, Clusters, Jobs, and Search. The main area has a title 'Create Table' and a sub-section 'Data Import'. It shows a dropdown 'Data Source' set to 'File' and a large input field labeled 'File(s)' with the placeholder 'Drop file or click here to upload'. A 'Send Feedback' button is at the bottom right.

The screenshot shows the 'Create Table' interface after a file has been uploaded. The 'File(s)' section now displays 'Heart (1).csv' with a size of '19.9 KB' and a 'Remove file' link. Below this, it says 'Uploaded to DBFS' and shows the path '/FileStore/tables/nlqogm7b1495157186117/Heart__1_-466d4.csv'. A 'Preview Table' button is visible. The 'Table Details' section on the left shows 'Table name: heart', 'File type: CSV', and 'Column Delimiter: ,'. The 'First row is header' checkbox is checked. A preview table grid shows two rows of data:

	_c0	Age	Sex	ChestPain	RestBP
1	63	1	typical	145	
2	67	1	asymptomatic	160	

A 'Create Table' button is at the bottom of the 'Table Details' section. A 'Send Feedback' button is at the bottom right.



1. Linear Regression with PySpark on Databricks

Author: Wenqiang Feng

Set up SparkSession

```

Cmd 1
1 from pyspark.sql import SparkSession
2
3 spark = SparkSession \
4     .builder \
5     .appName("Python Spark Linear Regression Example") \
6     .config("spark.some.config.option", "some-value") \
7     .getOrCreate()

```

Command took 0.16 seconds -- by wfeng1@utk.edu at 4/2/2017, 11:12:21 PM on MLmachine

2. Load dataset

```

Cmd 5
1 df = spark.read.format('com.databricks.spark.csv') \
2     .options(header='true', \
3             inferSchema='true') \
4     .load("/FileStore/tables/05rmhuqv1489687378010/", header= True)

```

After finishing the above 5 steps, you are ready to run your Spark code on Databricks Community Cloud. I will run all the following demos on Databricks Community Cloud. Hopefully, when you run the demo code, you will get the following results:

```
+---+---+---+---+  
| _c0 | TV | Radio | Newspaper | Sales |  
+---+---+---+---+  
| 1 | 230.1 | 37.8 | 69.2 | 22.1 |  
| 2 | 44.5 | 39.3 | 45.1 | 10.4 |  
| 3 | 17.2 | 45.9 | 69.3 | 9.3 |  
| 4 | 151.5 | 41.3 | 58.5 | 18.5 |  
| 5 | 180.8 | 10.8 | 58.4 | 12.9 |  
+---+---+---+---+  
only showing top 5 rows  
  
root  
|-- _c0: integer (nullable = true)  
|-- TV: double (nullable = true)  
|-- Radio: double (nullable = true)  
|-- Newspaper: double (nullable = true)  
|-- Sales: double (nullable = true)
```

3.2 Configure Spark on Mac and Ubuntu

3.2.1 Installing Prerequisites

I will strongly recommend you to install Anaconda, since it contains most of the prerequisites and support multiple Operator Systems.

1. Install Python

Go to Ubuntu Software Center and follow the following steps:

- Open Ubuntu Software Center
- Search for python
- And click Install

Or Open your terminal and using the following command:

```
sudo apt-get install build-essential checkinstall  
sudo apt-get install libreadline-gplv2-dev libncursesw5-dev libssl-dev  
      libsqlite3-dev tk-dev libgdbm-dev libc6-dev libbz2-dev  
sudo apt-get install python  
sudo easy_install pip  
sudo pip install ipython
```

3.2.2 Install Java

Java is used by many other softwares. So it is quite possible that you have already installed it. You can by using the following command in Command Prompt:

```
java -version
```

Otherwise, you can follow the steps in [How do I install Java for my Mac?](#) to install java on Mac and use the following command in Command Prompt to install on Ubuntu:

```
sudo apt-add-repository ppa:webupd8team/java
sudo apt-get update
sudo apt-get install oracle-java8-installer
```

3.2.3 Install Java SE Runtime Environment

I installed ORACLE Java JDK.

Warning: Installing Java and Java SE Runtime Environment steps are very important, since Spark is a domain-specific language written in Java.

You can check if your Java is available and find it's version by using the following command in Command Prompt:

```
java -version
```

If your Java is installed successfully, you will get the similar results as follows:

```
java version "1.8.0_131"
Java(TM) SE Runtime Environment (build 1.8.0_131-b11)
Java HotSpot(TM) 64-Bit Server VM (build 25.131-b11, mixed mode)
```

3.2.4 Install Apache Spark

Actually, the Pre-build version doesn't need installation. You can use it when you unpack it.

- Download: You can get the Pre-built Apache Spark™ from [Download Apache Spark™](#).
- Unpack: Unpack the Apache Spark™ to the path where you want to install the Spark.
- Test: Test the Prerequisites: change the direction spark-#.#. #-bin-hadoop#.#/bin and run

```
./pyspark
```

3.2.5 Configure the Spark

- a. **Mac Operator System:** open your bash_profile in Terminal

```
vim ~/.bash_profile
```

And add the following lines to your bash_profile (remember to change the path)

```
# add for spark
export SPARK_HOME=your_spark_installation_path
export PATH=$PATH:$SPARK_HOME/bin:$SPARK_HOME/sbin
export PATH=$PATH:$SPARK_HOME/bin
export PYSPARK_DRIVER_PYTHON="jupyter"
export PYSPARK_DRIVER_PYTHON_OPTS="notebook"
```

At last, remember to source your bash_profile

```
source ~/.bash_profile
```

- b. **Ubuntu Operator Sysytem:** open your bashrc in Terminal

```
vim ~/.bashrc
```

And add the following lines to your bashrc (remember to change the path)

```
# add for spark
export SPARK_HOME=your_spark_installation_path
export PATH=$PATH:$SPARK_HOME/bin:$SPARK_HOME/sbin
export PATH=$PATH:$SPARK_HOME/bin
export PYSPARK_DRIVE_PYTHON="jupyter"
export PYSPARK_DRIVE_PYTHON_OPTS="notebook"
```

At last, remember to source your bashrc

```
source ~/.bashrc
```

3.3 Configure Spark on Windows

Installing open source software on Windows is always a nightmare for me. Thanks for Deelesh Mandloi. You can follow the detailed procedures in the blog [Getting Started with PySpark on Windows](#) to install the Apache Spark™ on your Windows Operator System.

3.4 PySpark With Text Editor or IDE

3.4.1 PySpark With Jupyter Notebook

After you finishing the above setup steps in [Configure Spark on Mac and Ubuntu](#), then you should be good to write and run your PySpark Code in Jupyter notebook.

3.4.2 PySpark With PyCharm

After you finishing the above setup steps in [Configure Spark on Mac and Ubuntu](#), then you should be good to add the PySpark to your PyCharm project.

1. Create a new PyCharm project

2. Go to Project Structure

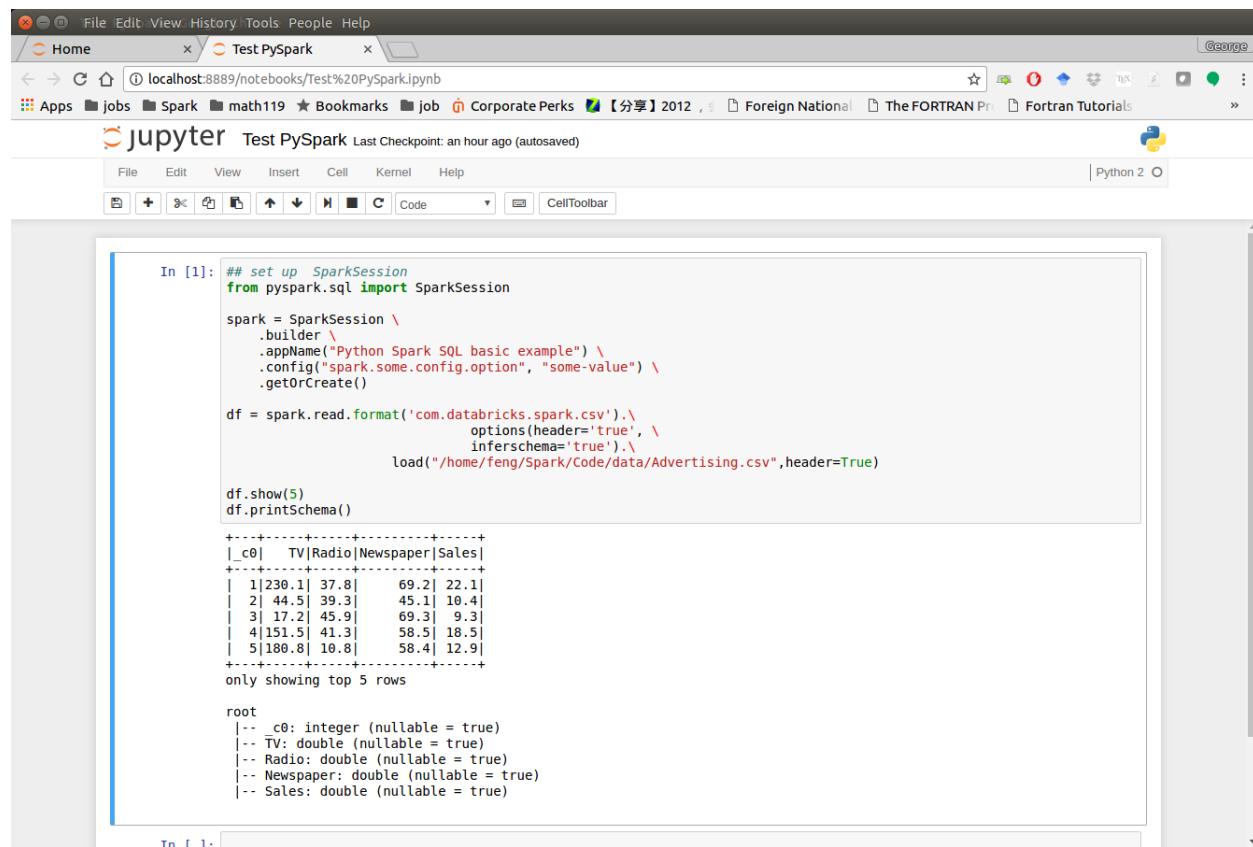
Option 1: File -> Settings -> Project: -> Project Structure

Option 2: PyCharm -> Preferences -> Project: -> Project Structure

3. Add Content Root: all ZIP files from \$SPARK_HOME/python/lib

4. Run your script

Learning Apache Spark with Python



The screenshot shows a Jupyter Notebook interface running on a web browser. The title bar says "Test PySpark". The notebook has one cell, In [1], containing Python code to set up a SparkSession and read a CSV file. The output shows the first five rows of the DataFrame and its schema.

```
In [1]: ## set up SparkSession
from pyspark.sql import SparkSession

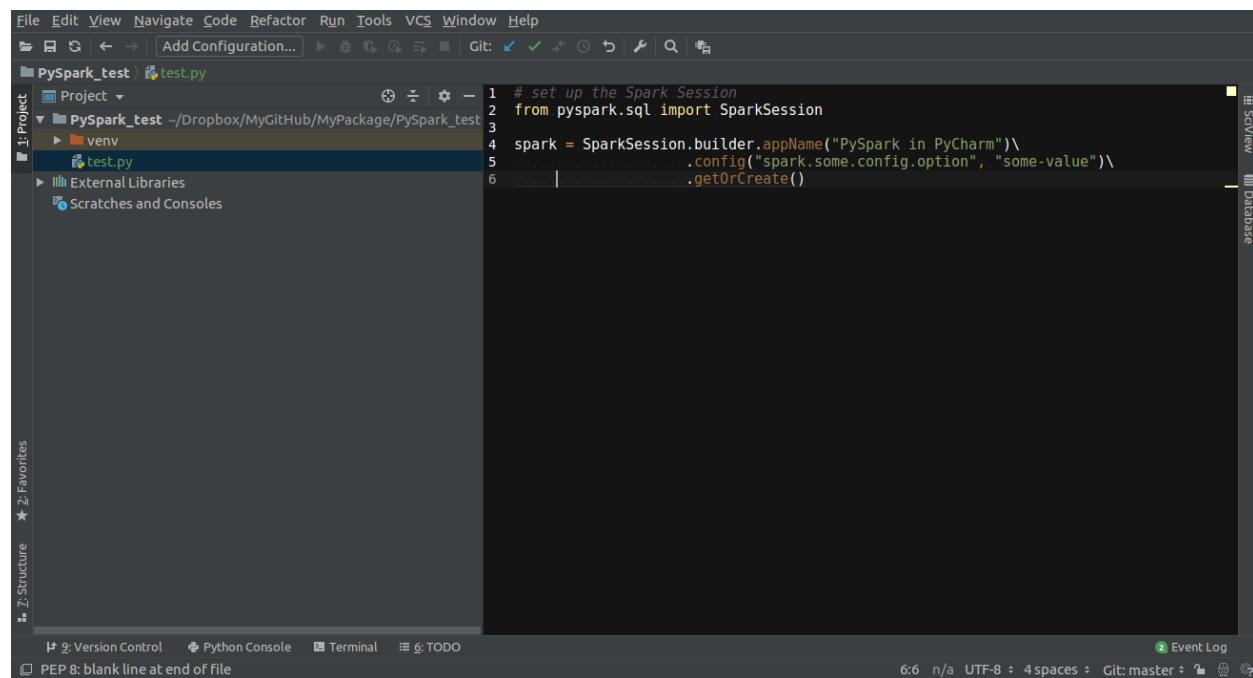
spark = SparkSession \
    .builder \
    .appName("Python Spark SQL basic example") \
    .config("spark.some.config.option", "some-value") \
    .getOrCreate()

df = spark.read.format('com.databricks.spark.csv') \
    .options(header='true', \
            inferSchema='true') \
    .load("/home/feng/Spark/Code/data/Advertising.csv",header=True)

df.show(5)
df.printSchema()

+---+---+---+---+
|_c0| TV|Radio|Newspaper|Sales|
+---+---+---+---+
| 1|230.1| 37.8|   69.2| 22.1|
| 2| 44.5| 39.3|   45.1| 10.4|
| 3| 17.2| 45.9|   69.3|  9.3|
| 4|151.5| 41.3|   58.5| 18.5|
| 5|180.8| 10.8|   58.4| 12.9|
+---+---+---+---+
only showing top 5 rows

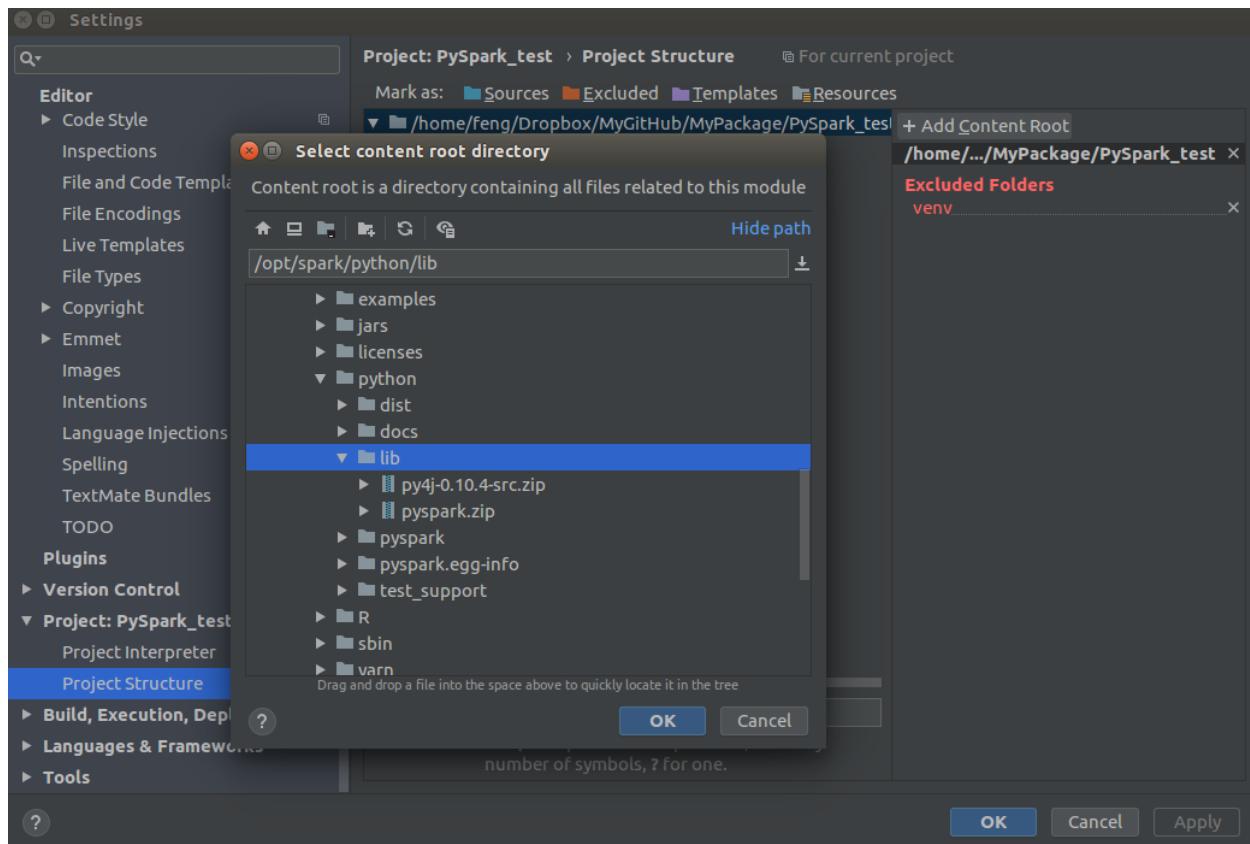
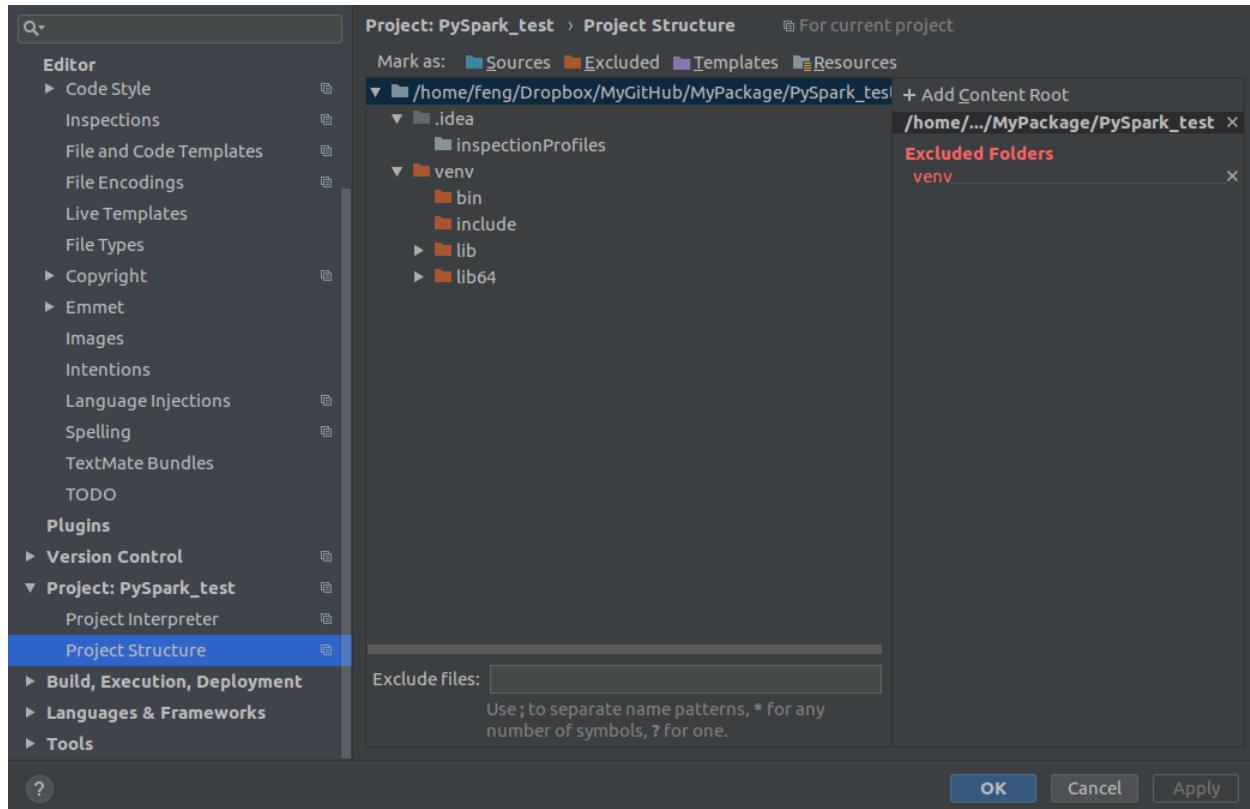
root
 |-- _c0: integer (nullable = true)
 |-- TV: double (nullable = true)
 |-- Radio: double (nullable = true)
 |-- Newspaper: double (nullable = true)
 |-- Sales: double (nullable = true)
```



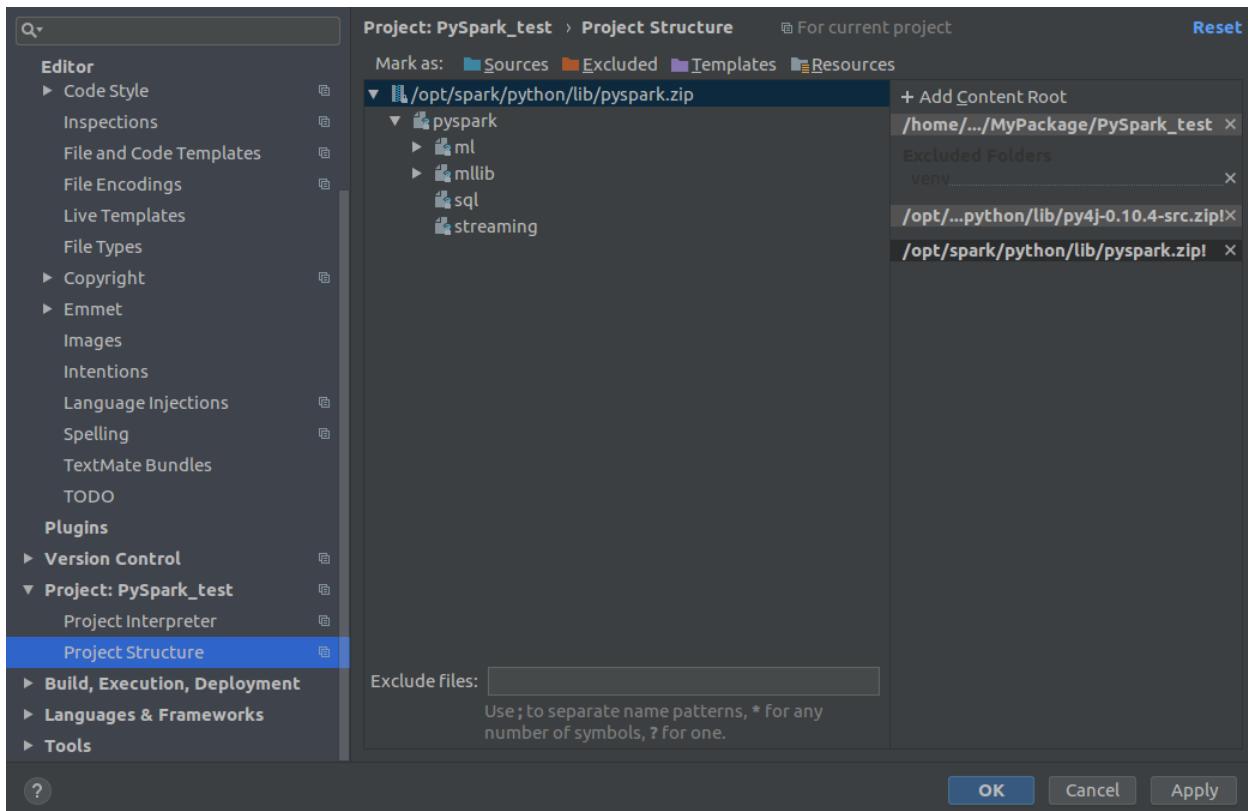
The screenshot shows a PyCharm IDE interface with a project named "PySpark_test". The "test.py" file is open in the editor, displaying the same code as the Jupyter notebook. The code sets up a SparkSession and reads a CSV file.

```
# set up the Spark Session
from pyspark.sql import SparkSession

spark = SparkSession.builder.appName("PySpark in PyCharm") \
    .config("spark.some.config.option", "some-value") \
    .getOrCreate()
```



Learning Apache Spark with Python



The screenshot shows the PyCharm IDE interface. The top menu bar includes File, Edit, View, Navigate, Code, Refactor, Run, Tools, VCS, Window, and Help. The toolbar has icons for file operations like Open, Save, and Run. The left sidebar shows the 'Project' view with 'PySpark_test' selected, displaying files like 'Heart.csv' and external libraries. The main code editor window shows a Python script 'test.py' with the following code:

```
1 # set up the Spark Session
2 from pyspark.sql import SparkSession
3
4 spark = SparkSession.builder.appName("PySpark in PyCharm")\
5     .config("spark.some.config.option", "some-value")\
6     .getOrCreate()
7
8 #.load data
9 data = spark.read.format('com.databricks.spark.csv')\
10    .options(header='true', inferSchema='true')\
11    .load("Heart.csv", header=True)
12
13 #.show data
14 data.show(5)
```

The 'Run' tool window at the bottom shows the output of the script. It displays the first five rows of a dataset from 'Heart.csv':

Age	Sex	ChestPain	RestBP	Chol	Fbs	RestECG	MaxHR	ExAng	Oldpeak	Slope	Ca	Thal	AHD
63	1	typical	145	233	1	2	150	0	2.3	3	0	fixed	No
67	1	asymptomatic	160	286	0	2	108	1	1.5	2	3	normal	Yes
67	1	asymptomatic	120	229	0	2	129	1	2.6	2	2	reversible	Yes
37	1	nontypical	130	256	0	0	187	0	3.5	3	0	normal	No
41	0	nontypical	130	204	0	2	172	0	1.4	1	0	normal	No

The message 'only showing top 5 rows' is displayed below the table. The status bar at the bottom indicates 'Process finished with exit code 0'.

3.4.3 PySpark With Apache Zeppelin

After you finishing the above setup steps in [Configure Spark on Mac and Ubuntu](#), then you should be good to write and run your PySpark Code in Apache Zeppelin.

The screenshot shows a Apache Zeppelin notebook interface running on localhost:8080. The notebook contains several cells:

- test**: A cell containing PySpark code to read a CSV file and show the first 4 rows. The output shows the first four rows of a dataset with columns like age, job, marital, education, etc.
- spark.pyspark**: A cell showing the output of df.show(4) command. It lists 4 rows of data from the 'bank' dataset.
- spark.pyspark**: A cell showing the output of df.registerTempTable("bank") command.
- maxAge**: A cell containing SQL query to find the maximum age. It includes a pie chart visualization where each slice represents an age group (e.g., 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29).
- marital**: A cell containing SQL query to group by marital status. It includes a pie chart visualization.
- marital**: A cell containing SQL query to group by marital status. It includes a histogram visualization showing the count of individuals per age group.

3.4.4 PySpark With Sublime Text

After you finishing the above setup steps in [Configure Spark on Mac and Ubuntu](#), then you should be good to use Sublime Text to write your PySpark Code and run your code as a normal python code in Terminal.

```
python test_pyspark.py
```

Then you should get the output results in your terminal.

A screenshot of a terminal window titled "Feng@feng-ThinkPad: ~/Spark/Code". The window shows the execution of a PySpark script named "test_pyspark.py". The code reads a CSV file "Advertising.csv" and prints the first 5 rows and the schema. The terminal output includes logs about failed service binds and the resulting DataFrame schema.

```
## set up SparkSession
from pyspark.sql import SparkSession
spark = SparkSession \
    .builder \
    .appName("Python Spark SQL basic example") \
    .config("spark.some.config.option", "some-value") \
    .getOrCreate()
df = spark.read.format('com.databricks.spark.csv') \
    .options(header='true', \
            inferSchema='true') \
    .load("/home/feng/Spark/Code/data/Advertising.csv", header=True)
df.show(5)
df.printSchema()
```

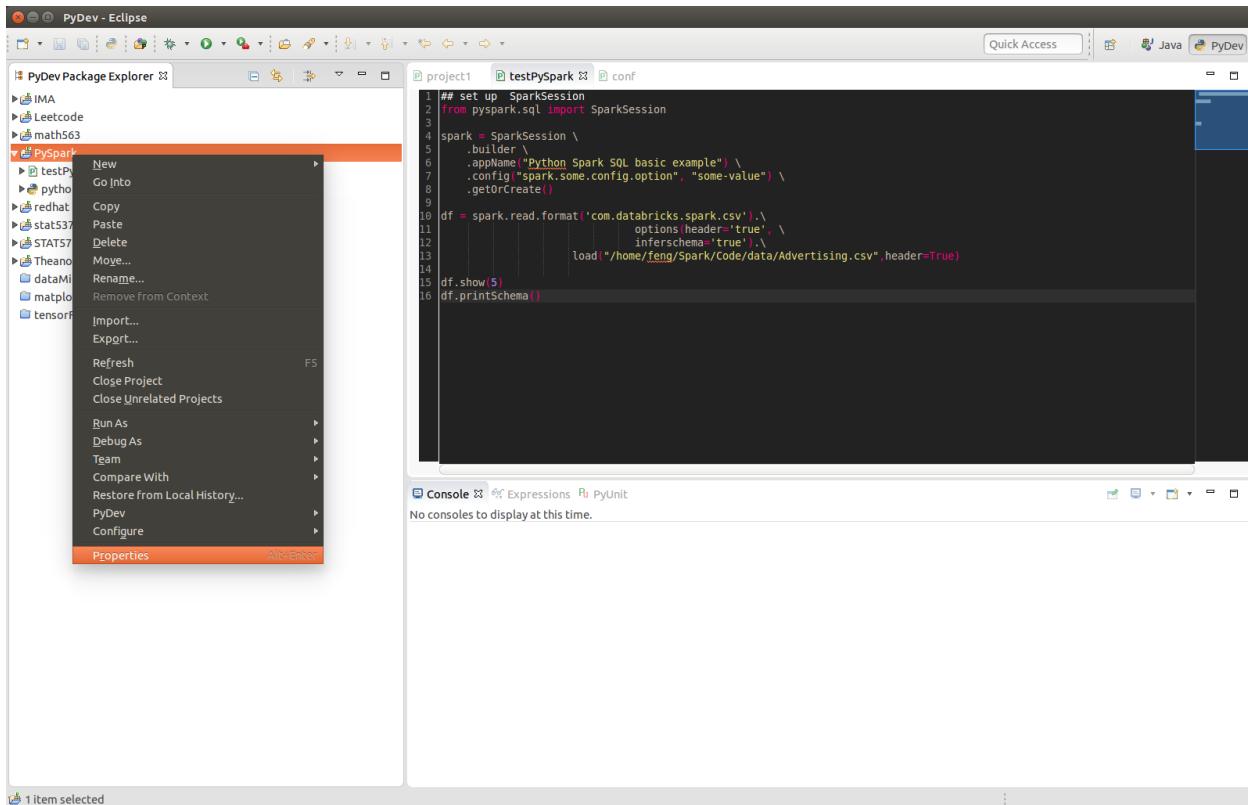
```
+---+---+---+---+
|_c0| TV|Radio|Newspaper|Sales|
+---+---+---+---+
| 1|230.1| 37.8|   69.2| 22.1|
| 2| 44.5| 39.3|   45.1| 10.4|
| 3| 17.2| 45.9|   69.3|  9.3|
| 4|151.5| 41.3|   58.5| 18.5|
| 5|180.8| 10.8|   58.4| 12.9|
+---+---+---+---+
only showing top 5 rows

root
|-- _c0: integer (nullable = true)
|-- TV: double (nullable = true)
|-- Radio: double (nullable = true)
|-- Newspaper: double (nullable = true)
|-- Sales: double (nullable = true)
```

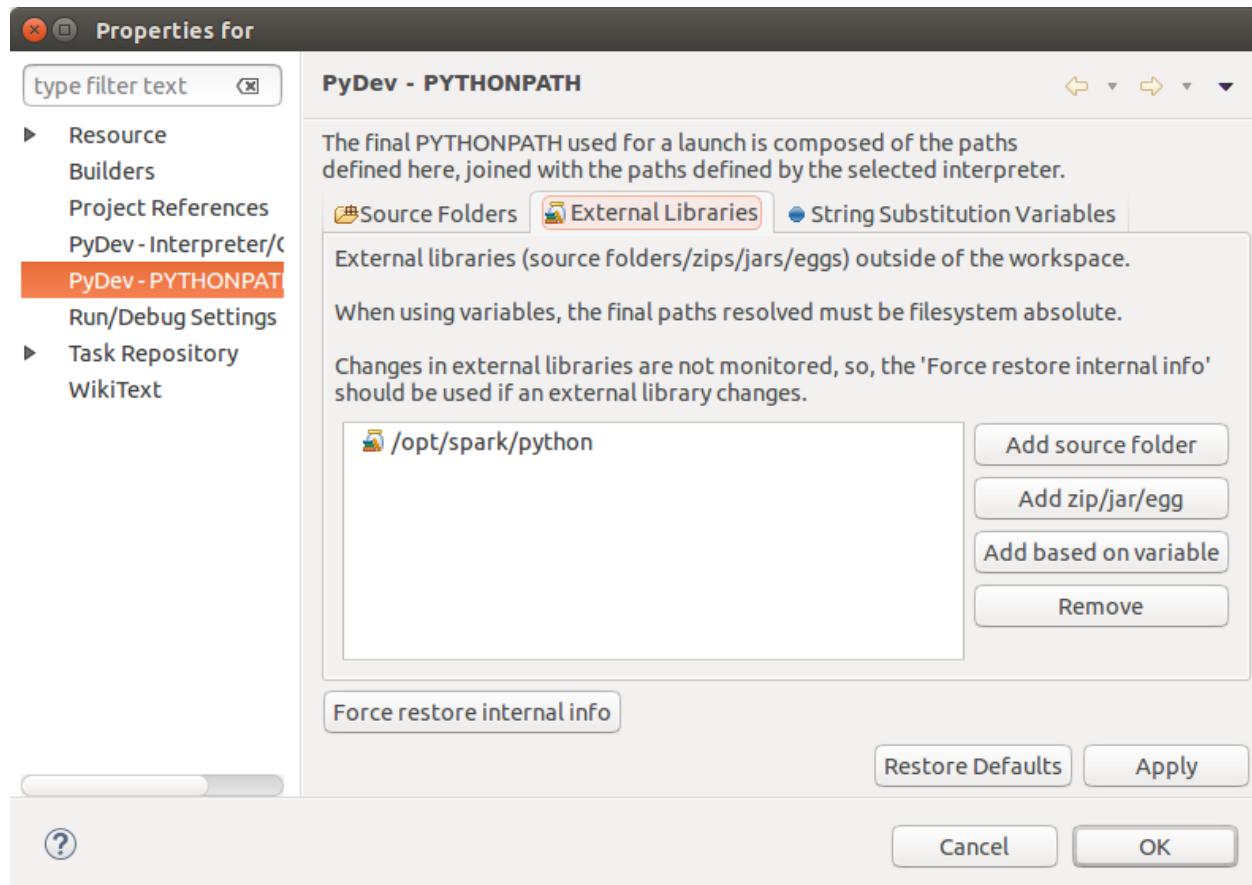
3.4.5 PySpark With Eclipse

If you want to run PySpark code on Eclipse, you need to add the paths for the **External Libraries** for your **Current Project** as follows:

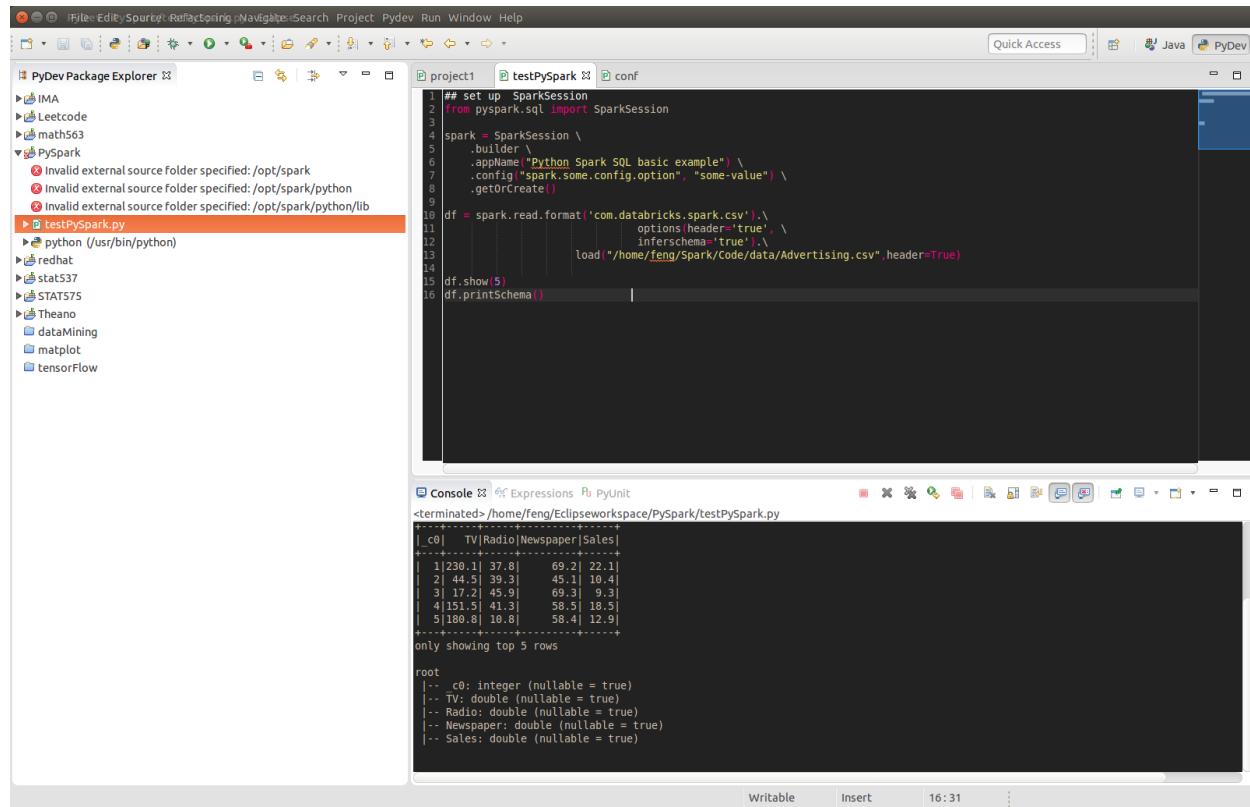
1. Open the properties of your project



2. Add the paths for the **External Libraries**



And then you should be good to run your code on Eclipse with PyDev.



3.5 PySparkling Water: Spark + H2O

1. Download Sparkling Water from: <https://s3.amazonaws.com/h2o-release/sparkling-water/rel-2.4/5/index.html>
2. Test PySparkling

```
unzip sparkling-water-2.4.5.zip
cd ~/sparkling-water-2.4.5/bin
./pysparkling
```

If you have a correct setup for PySpark, then you will get the following results:

```
Using Spark defined in the SPARK_HOME=/Users/dt216661/spark environmental
property

Python 3.7.1 (default, Dec 14 2018, 13:28:58)
[GCC 4.2.1 Compatible Apple LLVM 6.0 (clang-600.0.57)] on darwin
Type "help", "copyright", "credits" or "license" for more information.
2019-02-15 14:08:30 WARN NativeCodeLoader:62 - Unable to load native-hadoop
library for your platform... using builtin-java classes where applicable
```

(continues on next page)

(continued from previous page)

```
Setting default log level to "WARN".
Using Spark's default log4j profile: org/apache/spark/log4j-defaults.
→properties
Setting default log level to "WARN".
To adjust logging level use sc.setLogLevel(newLevel). For SparkR, use
→setLogLevel(newLevel).
2019-02-15 14:08:31 WARN  Utils:66 - Service 'SparkUI' could not bind on port
→4040. Attempting port 4041.
2019-02-15 14:08:31 WARN  Utils:66 - Service 'SparkUI' could not bind on port
→4041. Attempting port 4042.
17/08/30 13:30:12 WARN NativeCodeLoader: Unable to load native-hadoop
library for your platform... using builtin-java classes where applicable
17/08/30 13:30:17 WARN ObjectStore: Failed to get database global_temp,
returning NoSuchObjectException
Welcome to

    / _/_/ _ _ _ _ /_/_/
   \ \_ \_ \_ \_ `/_/_/ ' _/
    /_ / . _/_\_,/_/_/ /_/\_ \
    /_/

    version 2.4.0

Using Python version 3.7.1 (default, Dec 14 2018 13:28:58)
SparkSession available as 'spark'.
```

3. Setup pysparkling with Jupyter notebook

Add the following alias to your `bashrc` (Linux systems) or `bash_profile` (Mac system)

```
alias sparkling="PYSPARK_DRIVER_PYTHON='ipython' PYSPARK_DRIVER_PYTHON_OPTS='--notebook' ~/~/sparkling-water-2.4.5/bin/pysparkling"
```

4. Open pysparkling in terminal

sparkling

3.6 Set up Spark on Cloud

Following the setup steps in [Configure Spark on Mac and Ubuntu](#), you can set up your own cluster on the cloud, for example AWS, Google Cloud. Actually, for those clouds, they have their own Big Data tool. You can run them directly without any setting just like Databricks Community Cloud. If you want more details, please feel free to contact with me.

3.7 Demo Code in this Section

The code for this section is available for download [test_pyspark](#), and the Jupyter notebook can be download from [test_pyspark_ipynb](#).

- Python Source code

```
## set up SparkSession
from pyspark.sql import SparkSession

spark = SparkSession \
    .builder \
    .appName("Python Spark SQL basic example") \
    .config("spark.some.config.option", "some-value") \
    .getOrCreate()

df = spark.read.format('com.databricks.spark.csv') \
    .options(header='true', \
            inferSchema='true') \
    .load("/home/feng/Spark/Code/data/Advertising.csv"
         ,header=True)

df.show(5)
df.printSchema()
```

**CHAPTER
FOUR**

AN INTRODUCTION TO APACHE SPARK

Chinese proverb

Know yourself and know your enemy, and you will never be defeated – idiom, from Sunzi's Art of War

4.1 Core Concepts

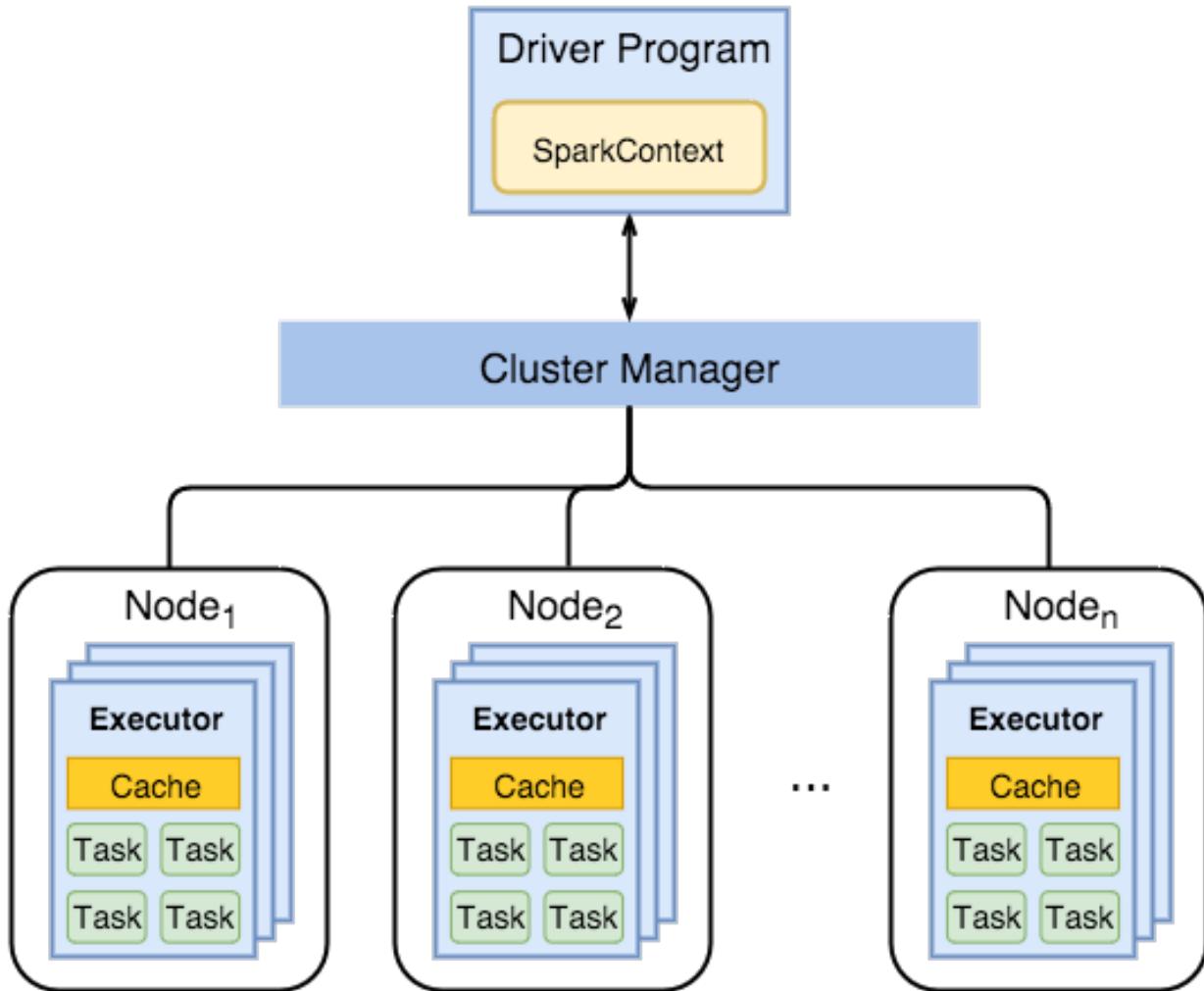
Most of the following content comes from [Kirillov2016]. So the copyright belongs to **Anton Kirillov**. I will refer you to get more details from [Apache Spark core concepts, architecture and internals](#).

Before diving deep into how Apache Spark works, lets understand the jargon of Apache Spark

- Job: A piece of code which reads some input from HDFS or local, performs some computation on the data and writes some output data.
- Stages: Jobs are divided into stages. Stages are classified as a Map or reduce stages (Its easier to understand if you have worked on Hadoop and want to correlate). Stages are divided based on computational boundaries, all computations (operators) cannot be Updated in a single Stage. It happens over many stages.
- Tasks: Each stage has some tasks, one task per partition. One task is executed on one partition of data on one executor (machine).
- DAG: DAG stands for Directed Acyclic Graph, in the present context its a DAG of operators.
- Executor: The process responsible for executing a task.
- Master: The machine on which the Driver program runs
- Slave: The machine on which the Executor program runs

4.2 Spark Components

1. Spark Driver



- separate process to execute user applications
- creates SparkContext to schedule jobs execution and negotiate with cluster manager

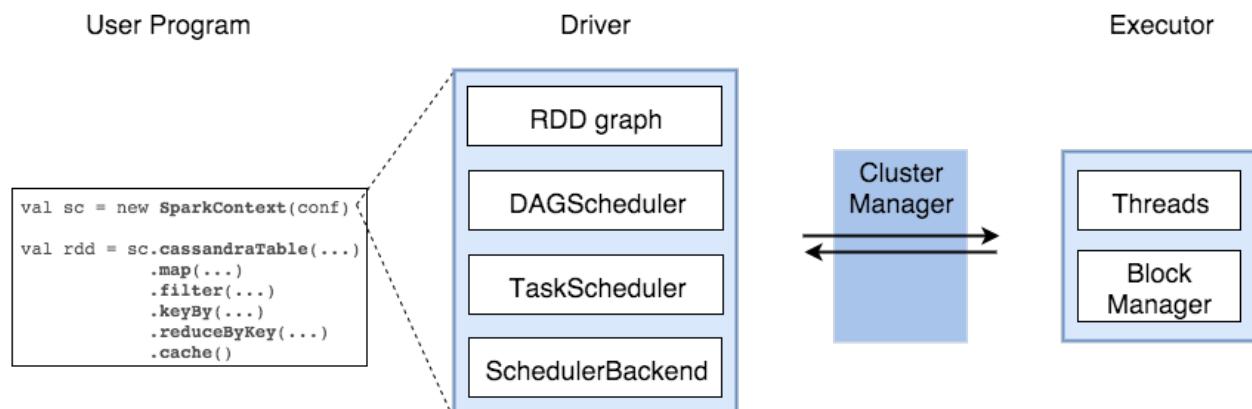
2. Executors

- run tasks scheduled by driver
- store computation results in memory, on disk or off-heap
- interact with storage systems

3. Cluster Manager

- Mesos
- YARN
- Spark Standalone

Spark Driver contains more components responsible for translation of user code into actual jobs executed on cluster:



- **SparkContext**
 - represents the connection to a Spark cluster, and can be used to create RDDs, accumulators and broadcast variables on that cluster
- **DAGScheduler**
 - computes a DAG of stages for each job and submits them to TaskScheduler determines preferred locations for tasks (based on cache status or shuffle files locations) and finds minimum schedule to run the jobs
- **TaskScheduler**
 - responsible for sending tasks to the cluster, running them, retrying if there are failures, and mitigating stragglers
- **SchedulerBackend**

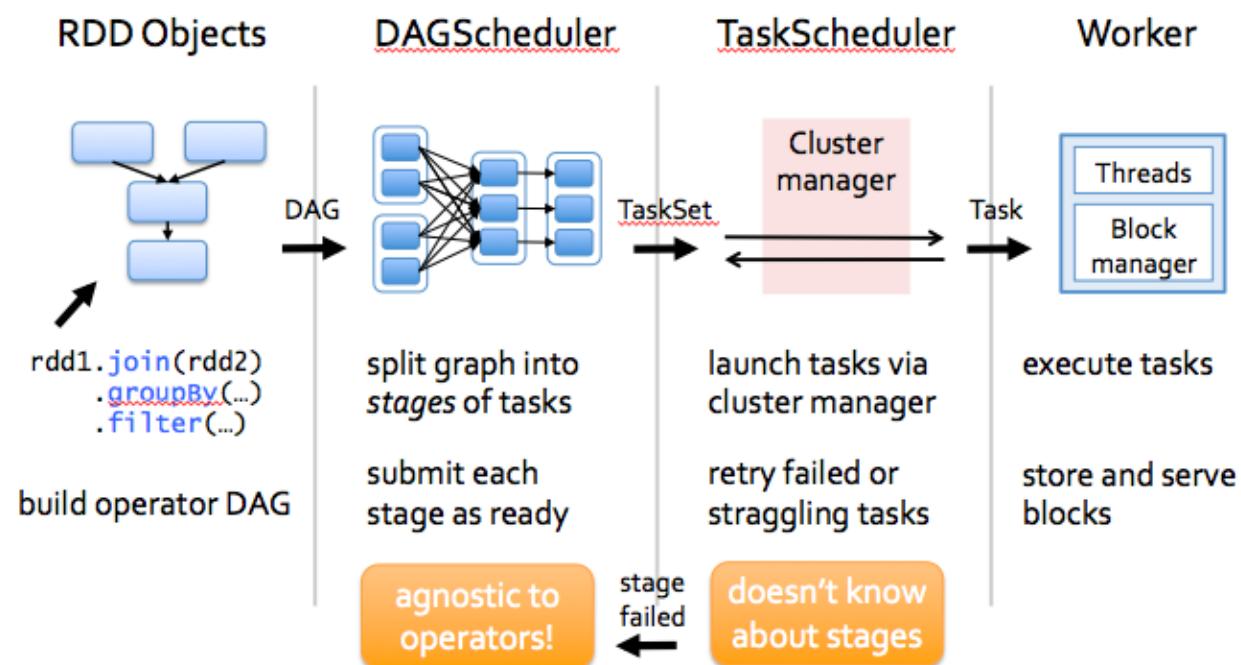
- backend interface for scheduling systems that allows plugging in different implementations(Mesos, YARN, Standalone, local)
- BlockManager
 - provides interfaces for putting and retrieving blocks both locally and remotely into various stores (memory, disk, and off-heap)

4.3 Architecture

4.4 How Spark Works?

Spark has a small code base and the system is divided in various layers. Each layer has some responsibilities. The layers are independent of each other.

The first layer is the interpreter, Spark uses a Scala interpreter, with some modifications. As you enter your code in spark console (creating RDD's and applying operators), Spark creates a operator graph. When the user runs an action (like collect), the Graph is submitted to a DAG Scheduler. The DAG scheduler divides operator graph into (map and reduce) stages. A stage is comprised of tasks based on partitions of the input data. The DAG scheduler pipelines operators together to optimize the graph. For e.g. Many map operators can be scheduled in a single stage. This optimization is key to Spaks performance. The final result of a DAG scheduler is a set of stages. The stages are passed on to the Task Scheduler. The task scheduler launches tasks via cluster manager. (Spark Standalone/Yarn/Mesos). The task scheduler doesn't know about dependencies among stages.



PROGRAMMING WITH RDDS

Chinese proverb

If you only know yourself, but not your opponent, you may win or may lose. If you know neither yourself nor your enemy, you will always endanger yourself – idiom, from Sunzi's Art of War

RDD represents **Resilient Distributed Dataset**. An RDD in Spark is simply an immutable distributed collection of objects sets. Each RDD is split into multiple partitions (similar pattern with smaller sets), which may be computed on different nodes of the cluster.

5.1 Create RDD

Usually, there are two popular ways to create the RDDs: loading an external dataset, or distributing a set of collection of objects. The following examples show some simplest ways to create RDDs by using `parallelize()` function which takes an already existing collection in your program and pass the same to the Spark Context.

1. By using `parallelize()` function

```
from pyspark.sql import SparkSession

spark = SparkSession \
    .builder \
    .appName("Python Spark create RDD example") \
    .config("spark.some.config.option", "some-value") \
    .getOrCreate()

df = spark.sparkContext.parallelize([(1, 2, 3, 'a b c'),
                                     (4, 5, 6, 'd e f'),
                                     (7, 8, 9, 'g h i')]).toDF(['col1', 'col2', 'col3', 'col4'])
```

Then you will get the RDD data:

```
df.show()
+---+---+---+---+
```

(continues on next page)

(continued from previous page)

```
| col1|col2|col3| col4|
+---+---+---+---+
|   1|   2|   3|a b c|
|   4|   5|   6|d e f|
|   7|   8|   9|g h i|
+---+---+---+---+
```

```
from pyspark.sql import SparkSession

spark = SparkSession \
    .builder \
    .appName("Python Spark create RDD example") \
    .config("spark.some.config.option", "some-value") \
    .getOrCreate()

myData = spark.sparkContext.parallelize([(1, 2), (3, 4), (5, 6), (7, 8), (9, 10)])
```

Then you will get the RDD data:

```
myData.collect()
[(1, 2), (3, 4), (5, 6), (7, 8), (9, 10)]
```

2. By using createDataFrame() function

```
from pyspark.sql import SparkSession

spark = SparkSession \
    .builder \
    .appName("Python Spark create RDD example") \
    .config("spark.some.config.option", "some-value") \
    .getOrCreate()

Employee = spark.createDataFrame([
    ('1', 'Joe', '70000', '1'),
    ('2', 'Henry', '80000', '2'),
    ('3', 'Sam', '60000', '2'),
    ('4', 'Max', '90000', '1')],
    ['Id', 'Name', 'Salary', 'DepartmentId']
)
```

Then you will get the RDD data:

```
+---+---+---+---+
| Id| Name|Salary|DepartmentId|
+---+---+---+---+
|  1| Joe| 70000|      1|
|  2| Henry| 80000|      2|
|  3| Sam| 60000|      2|
|  4| Max| 90000|      1|
+---+---+---+---+
```

3. By using read and load functions

a. Read dataset from .csv file

```
## set up SparkSession
from pyspark.sql import SparkSession

spark = SparkSession \
    .builder \
    .appName("Python Spark create RDD example") \
    .config("spark.some.config.option", "some-value") \
    .getOrCreate()

df = spark.read.format('com.databricks.spark.csv').\
    options(header='true', \
            inferschema='true') \
    .load("/home/feng/Spark/Code/data/Advertising.csv",
        header=True)

df.show(5)
df.printSchema()
```

Then you will get the RDD data:

```
+---+---+---+---+
|_c0| TV |Radio|Newspaper|Sales|
+---+---+---+---+
| 1 | 230.1| 37.8| 69.2| 22.1|
| 2 | 44.5 | 39.3| 45.1| 10.4|
| 3 | 17.2 | 45.9| 69.3| 9.3 |
| 4 | 151.5| 41.3| 58.5| 18.5|
| 5 | 180.8| 10.8| 58.4| 12.9|
+---+---+---+---+
only showing top 5 rows

root
|-- _c0: integer (nullable = true)
|-- TV: double (nullable = true)
|-- Radio: double (nullable = true)
|-- Newspaper: double (nullable = true)
|-- Sales: double (nullable = true)
```

Once created, RDDs offer two types of operations: transformations and actions.

b. Read dataset from DataBase

```
## set up SparkSession
from pyspark.sql import SparkSession

spark = SparkSession \
    .builder \
    .appName("Python Spark create RDD example") \
    .config("spark.some.config.option", "some-value") \
```

(continues on next page)

(continued from previous page)

```
.getOrCreate()

## User information
user = 'your_username'
pw   = 'your_password'

## Database information
table_name = 'table_name'
url = 'jdbc:postgresql://###.###.###.##:5432/dataset?user=' + user + '&
      password=' + pw
properties = {'driver': 'org.postgresql.Driver', 'password': pw, 'user':
      ': user'}

df = spark.read.jdbc(url=url, table=table_name,_
                     properties=properties)

df.show(5)
df.printSchema()
```

Then you will get the RDD data:

```
+---+---+---+---+
| _c0 | TV | Radio | Newspaper | Sales |
+---+---+---+---+
| 1 | 230.1 | 37.8 | 69.2 | 22.1 |
| 2 | 44.5 | 39.3 | 45.1 | 10.4 |
| 3 | 17.2 | 45.9 | 69.3 | 9.3 |
| 4 | 151.5 | 41.3 | 58.5 | 18.5 |
| 5 | 180.8 | 10.8 | 58.4 | 12.9 |
+---+---+---+---+
only showing top 5 rows

root
| -- _c0: integer (nullable = true)
| -- TV: double (nullable = true)
| -- Radio: double (nullable = true)
| -- Newspaper: double (nullable = true)
| -- Sales: double (nullable = true)
```

Note: Reading tables from Database needs the proper drive for the corresponding Database. For example, the above demo needs `org.postgresql.Driver` and you need to download it and put it in `jars` folder of your spark installation path. I download `postgresql-42.1.1.jar` from the official website and put it in `jars` folder.

C. Read dataset from HDFS

```
from pyspark.conf import SparkConf
from pyspark.context import SparkContext
from pyspark.sql import HiveContext
```

(continues on next page)

(continued from previous page)

```

sc= SparkContext('local','example')
hc = HiveContext(sc)
tf1 = sc.textFile("hdfs://cdhstltest/user/data/demo.CSV")
print(tf1.first())

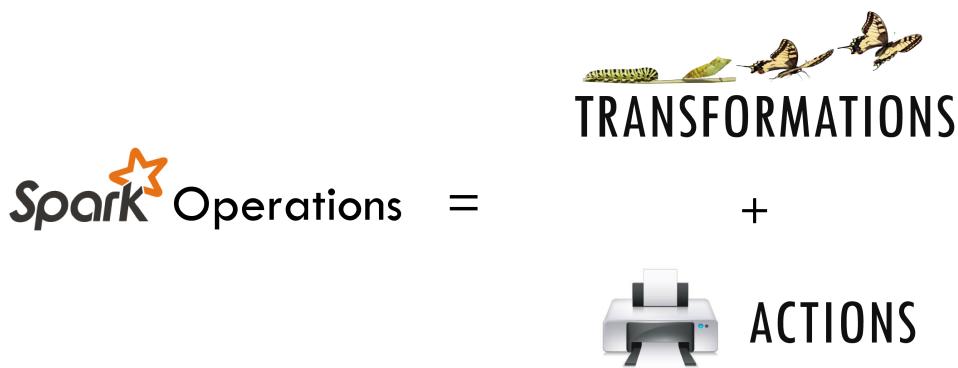
hc.sql("use intg_cme_w")
spf = hc.sql("SELECT * FROM spf LIMIT 100")
print(spf.show(5))

```

5.2 Spark Operations

Warning: All the figures below are from Jeffrey Thompson. The interested reader is referred to [pyspark pictures](#)

There are two main types of Spark operations: Transformations and Actions [Karau2015].

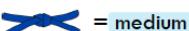


Note: Some people defined three types of operations: Transformations, Actions and Shuffles.

5.2.1 Spark Transformations

Transformations construct a new RDD from a previous one. For example, one common transformation is filtering data that matches a predicate.



 = easy  = medium

Essential Core & Intermediate Spark Operations

General	Math / Statistical	Set Theory / Relational	Data Structure / I/O
<ul style="list-style-type: none"> map filter flatMap mapPartitions mapPartitionsWithIndex groupByKey sortBy 	<ul style="list-style-type: none"> sample randomSplit 	<ul style="list-style-type: none"> union intersection subtract distinct cartesian zip 	<ul style="list-style-type: none"> keyBy zipWithIndex zipWithUniqueId zipPartitions coalesce repartition repartitionAndSortWithinPartitions pipe



 = easy  = medium

Essential Core & Intermediate PairRDD Operations

General	Math / Statistical	Set Theory / Relational	Data Structure
<ul style="list-style-type: none"> flatMapValues groupByKey reduceByKey reduceByKeyLocally foldByKey aggregateByKey sortByKey combineByKey 	<ul style="list-style-type: none"> sampleByKey 	<ul style="list-style-type: none"> cogroup (=groupWith) join subtractByKey fullOuterJoin leftOuterJoin rightOuterJoin 	<ul style="list-style-type: none"> partitionBy

5.2.2 Spark Actions

Actions, on the other hand, compute a result based on an RDD, and either return it to the driver program or save it to an external storage system (e.g., HDFS).



<ul style="list-style-type: none"> reduce collect aggregate fold first take foreach top treeAggregate treeReduce foreachPartition collectAsMap 	<ul style="list-style-type: none"> count takeSample max min sum histogram mean variance stdev sampleVariance countApprox countApproxDistinct 	<ul style="list-style-type: none"> takeOrdered 	<ul style="list-style-type: none"> saveAsTextFile saveAsSequenceFile saveAsObjectFile saveAsHadoopDataset saveAsHadoopFile saveAsNewAPIHadoopDataset saveAsNewAPIHadoopFile
--	--	---	--



- keys
- values
- countByKey
- countByValue
- countByValueApprox
- countApproxDistinctByKey
- countApproxDistinctByKey
- countByKeyApprox
- sampleByKeyExact

5.3 rdd.DataFrame vs pd.DataFrame

5.3.1 Create DataFrame

1. From List

```
my_list = [['a', 1, 2], ['b', 2, 3], ['c', 3, 4]]
col_name = ['A', 'B', 'C']
```

:: Python Code:

```
# caution for the columns=
pd.DataFrame(my_list,columns= col_name)
#
spark.createDataFrame(my_list, col_name).show()
```

:: Comparison:

	A	B	C	A	B	C
A	a	1	2	a	1	2
B	b	2	3	b	2	3
C	c	3	4	c	3	4

Attention: Pay attention to the parameter `columns=` in `pd.DataFrame`. Since the default value will make the list as rows.

:: Python Code:

```
# caution for the columns=
pd.DataFrame(my_list, columns= col_name)
#
pd.DataFrame(my_list, col_name)
```

:: Comparison:

	A	B	C	0	1	2
0	a	1	2	a	1	2
1	b	2	3	b	2	3
2	c	3	4	c	3	4

2. From Dict

```
d = {'A': [0, 1, 0],  
     'B': [1, 0, 1],  
     'C': [1, 0, 0]}
```

:: Python Code:

```
pd.DataFrame(d) for  
# Tedious for PySpark  
spark.createDataFrame(np.array(list(d.values())) .T.tolist(), list(d.keys())).  
show()
```

:: Comparison:

	A	B	C		A	B	C
0	0	1	1		0	1	1
1	1	0	0		1	0	0
2	0	1	0		0	1	0

5.3.2 Load DataFrame

1. From DataBase

Most of time, you need to share your code with your colleagues or release your code for Code Review or Quality assurance(QA). You will definitely do not want to have your User Information in the code. So you can save them in login.txt:

```
runawayhorse001  
PythonTips
```

and use the following code to import your User Information:

```
#User Information  
try:  
    login = pd.read_csv(r'login.txt', header=None)  
    user = login[0][0]  
    pw = login[0][1]  
    print('User information is ready!')  
except:  
    print('Login information is not available!!!!')  
  
#Database information  
host = '##.##.##.##'  
db_name = 'db_name'  
table_name = 'table_name'
```

:: Comparison:

```
conn = psycopg2.connect(host=host, database=db_name, user=user, password=pw)
cur = conn.cursor()

sql = """
    select *
    from {table_name}
""".format(table_name=table_name)
dp = pd.read_sql(sql, conn)
```

```
# connect to database
url = 'jdbc:postgresql://'+host+':5432/' +db_name+'?user=' +user+ '&password=' +pw
properties ={'driver': 'org.postgresql.Driver', 'password': pw, 'user': user}
ds = spark.read.jdbc(url=url, table=table_name, properties=properties)
```

Attention: Reading tables from Database with PySpark needs the proper drive for the corresponding Database. For example, the above demo needs org.postgresql.Driver and you need to download it and put it in jars folder of your spark installation path. I download postgresql-42.1.1.jar from the official website and put it in jars folder.

2. From .csv

:: Comparison:

```
# pd.DataFrame dp: DataFrame pandas
dp = pd.read_csv('Advertising.csv')
#rdd.DataFrame. dp: DataFrame spark
ds = spark.read.csv(path='Advertising.csv',
#                     sep=',',
#                     encoding='UTF-8',
#                     comment=None,
                     header=True,
                     inferSchema=True)
```

3. From .json

Data from: <http://api.luftdaten.info/static/v1/data.json>

```
dp = pd.read_json("data/data.json")
ds = spark.read.json('data/data.json')
```

:: Python Code:

```
dp[['id', 'timestamp']].head(4)
#
ds[['id', 'timestamp']].show(4)
```

:: Comparison:

```
+-----+-----+
|           id|       |
+-----+-----+
|2994551481|2019-02-28|
|2994551482|2019-02-28|
|2994551483|2019-02-28|
|2994551484|2019-02-28|
+-----+-----+
only showing top 4 rows
```

5.3.3 First n Rows

:: Python Code:

```
dp.head(4)  
#  
ds.show(4)
```

:: Comparison:

```

      TV   Radio  Newspaper   Sales
0  230.1    37.8       69.2    22.1
1   44.5    39.3       45.1    10.4
2   17.2    45.9       69.3     9.3
3  151.5    41.3       58.5    18.5

```

only showing top 4 rows

5.3.4 Column Names

:: Python Code:

```
dp.columns  
#  
ds.columns
```

:: Comparison:

```
Index(['TV', 'Radio', 'Newspaper', 'Sales'], dtype='object')
['TV', 'Radio', 'Newspaper', 'Sales']
```

5.3.5 Data types

:: Python Code:

```
dp.dtypes
#
ds.dtypes
```

:: Comparison:

TV	float64	[('TV', 'double'),
Radio	float64	('Radio', 'double'),
Newspaper	float64	('Newspaper', 'double'),
Sales	float64	('Sales', 'double')]
dtype: object		

5.3.6 Fill Null

```
my_list = [['a', 1, None], ['b', 2, 3], ['c', 3, 4]]
dp = pd.DataFrame(my_list, columns=['A', 'B', 'C'])
ds = spark.createDataFrame(my_list, ['A', 'B', 'C'])
#
dp.head()
ds.show()
```

:: Comparison:

	A	B	C		A	B	C
0	male	1	Nan		male	1	null
1	female	2	3.0		female	2	3
2	male	3	4.0		male	3	4

:: Python Code:

```
dp.fillna(-99)
#
ds.fillna(-99).show()
```

:: Comparison:

	A	B	C
--	---	---	---

(continues on next page)

(continued from previous page)

	A	B	C		A	B	C	
0	male	1	-99		male 1 -99			
1	female	2	3.0		female 2 3			
2	male	3	4.0		male 3 4			

5.3.7 Replace Values

:: Python Code:

```
# caution: you need to chose specific col
dp.A.replace(['male', 'female'], [1, 0], inplace=True)
dp
#caution: Mixed type replacements are not supported
ds.na.replace(['male','female'],['1','0']).show()
```

:: Comparison:

	A	B	C		A	B	C	
0	1	1	NaN		1 1 null			
1	0	2	3.0		0 2 3			
2	1	3	4.0		1 3 4			

5.3.8 Rename Columns

1. Rename all columns

:: Python Code:

```
dp.columns = ['a', 'b', 'c', 'd']
dp.head(4)
#
ds.toDF('a','b','c','d').show(4)
```

:: Comparison:

	a	b	c	d		a	b	c	d	
0	230.1	37.8	69.2	22.1		230.1 37.8 69.2 22.1				
1	44.5	39.3	45.1	10.4		44.5 39.3 45.1 10.4				
2	17.2	45.9	69.3	9.3		17.2 45.9 69.3 9.3				
3	151.5	41.3	58.5	18.5		151.5 41.3 58.5 18.5				

only showing top 4 rows

2. Rename one or more columns

```
mapping = {'Newspaper': 'C', 'Sales': 'D'}
```

:: Python Code:

```
dp.rename(columns=mapping).head(4)
#
new_names = [mapping.get(col, col) for col in ds.columns]
ds.toDF(*new_names).show(4)
```

:: Comparison:

	TV	Radio	C	D		TV	Radio	C	D
0	230.1	37.8	69.2	22.1		230.1	37.8	69.2	22.1
1	44.5	39.3	45.1	10.4		44.5	39.3	45.1	10.4
2	17.2	45.9	69.3	9.3		17.2	45.9	69.3	9.3
3	151.5	41.3	58.5	18.5		151.5	41.3	58.5	18.5

only showing top 4 rows

Note: You can also use `withColumnRenamed` to rename one column in PySpark.

:: Python Code:

```
ds.withColumnRenamed('Newspaper', 'Paper').show(4)
```

:: Comparison:

	TV	Radio	Paper	Sales
0	230.1	37.8	69.2	22.1
1	44.5	39.3	45.1	10.4
2	17.2	45.9	69.3	9.3
3	151.5	41.3	58.5	18.5

only showing top 4 rows

5.3.9 Drop Columns

```
drop_name = ['Newspaper', 'Sales']
```

:: Python Code:

```
dp.drop(drop_name, axis=1).head(4)
#
ds.drop(*drop_name).show(4)
```

:: Comparison:

	TV	Radio		TV	Radio
0	230.1	37.8		230.1	37.8
1	44.5	39.3		44.5	39.3
2	17.2	45.9		17.2	45.9
3	151.5	41.3		151.5	41.3

only showing top 4 rows

5.3.10 Filter

```
dp = pd.read_csv('Advertising.csv')
#
ds = spark.read.csv(path='Advertising.csv',
                     header=True,
                     inferSchema=True)
```

:: Python Code:

```
dp[dp.Newspaper<20].head(4)
#
ds[ds.Newspaper<20].show(4)
```

:: Comparison:

	TV	Radio	Newspaper	Sales	TV	Radio	Newspaper	Sales
7	120.2	19.6	11.6	13.2	120.2	19.6	11.6	13.2
8	8.6	2.1	1.0	4.8	8.6	2.1	1.0	4.8
11	214.7	24.0	4.0	17.4	214.7	24.0	4.0	17.4
13	97.5	7.6	7.2	9.7	97.5	7.6	7.2	9.7

only showing top 4 rows

:: Python Code:

```
dp[(dp.Newspaper<20) & (dp.TV>100)].head(4)
#
ds[(ds.Newspaper<20) & (ds.TV>100)].show(4)
```

:: Comparison:

	TV	Radio	Newspaper	Sales				
7	120.2	19.6	11.6	13.2				
11	214.7	24.0	4.0	17.4				
19	147.3	23.9	19.1	14.6				
25	262.9	3.5	19.5	12.0				

only showing top 4 rows

5.3.11 With New Column

:: Python Code:

```
dp['tv_norm'] = dp.TV/sum(dp.TV)
dp.head(4)
#
ds.withColumn('tv_norm', ds.TV/ds.groupBy().agg(F.sum("TV")).collect()[0][0]).show(4)
```

:: Comparison:

	TV	Radio	Newspaper	Sales	tv_norm			
0	230.1	37.8	69.2	22.1	0.007824			
1	44.5	39.3	45.1	10.4	0.001513			
2	17.2	45.9	69.3	9.3	0.000585			
3	151.5	41.3	58.5	18.5	0.005152			

only showing top 4 rows

:: Python Code:

```
dp['cond'] = dp.apply(lambda c: 1 if ((c.TV>100)&(c.Radio<40)) else 2 if c.Sales> 10 else 3, axis=1)
#
ds.withColumn('cond', F.when((ds.TV>100)&(ds.Radio<40), 1)\n        .when(ds.Sales>10, 2)\n        .otherwise(3)).show(4)
```

:: Comparison:

	TV	Radio	Newspaper	Sales	cond			
0	230.1	37.8	69.2	22.1	1	230.1	37.8	69.2 22.1
1	44.5	39.3	45.1	10.4	2	44.5	39.3	45.1 10.4
2	17.2	45.9	69.3	9.3	3	17.2	45.9	69.3 9.3
3	151.5	41.3	58.5	18.5	2	151.5	41.3	58.5 18.5
						+-----+-----+	+-----+-----+	+-----+-----+

only showing top 4 rows

:: Python Code:

```
dp['log_tv'] = np.log(dp.TV)
dp.head(4)
#
ds.withColumn('log_tv', F.log(ds.TV)).show(4)
```

:: Comparison:

	TV	Radio	Newspaper	Sales	log_tv			
0	230.1	37.8	69.2	22.1	5.438514	230.1	37.8	69.2 22.1
1	44.5	39.3	45.1	10.4	3.795489	44.5	39.3	45.1 10.
2	17.2	45.9	69.3	9.3	2.844909	17.2	45.9	69.3 9.
3	151.5	41.3	58.5	18.5	5.020586	151.5	41.3	58.5 18.5
						+-----+-----+	+-----+-----+	+-----+-----+

only showing top 4 rows

:: Python Code:

```
dp['tv+10'] = dp.TV.apply(lambda x: x+10)
dp.head(4)
#
ds.withColumn('tv+10', ds.TV+10).show(4)
```

:: Comparison:

	TV	Radio	Newspaper	Sales	tv+10				
0	230.1	37.8	69.2	22.1	240.1	230.1	37.8	69.2	22.
1	44.5	39.3	45.1	10.4	54.5	44.5	39.3	45.1	10.4
2	17.2	45.9	69.3	9.3	27.2	17.2	45.9	69.3	9.3
3	151.5	41.3	58.5	18.5	161.5	151.5	41.3	58.5	18.

only showing top 4 rows

5.3.12 Join

```
leftp = pd.DataFrame({'A': ['A0', 'A1', 'A2', 'A3'],
                      'B': ['B0', 'B1', 'B2', 'B3'],
                      'C': ['C0', 'C1', 'C2', 'C3'],
                      'D': ['D0', 'D1', 'D2', 'D3']},
                     index=[0, 1, 2, 3])

rightp = pd.DataFrame({'A': ['A0', 'A1', 'A6', 'A7'],
                       'F': ['B4', 'B5', 'B6', 'B7'],
                       'G': ['C4', 'C5', 'C6', 'C7'],
                       'H': ['D4', 'D5', 'D6', 'D7']},
                      index=[4, 5, 6, 7])

lefts = spark.createDataFrame(leftp)
rights = spark.createDataFrame(rightp)
```

	A	B	C	D		A	F	G	H	
0	A0	B0	C0	D0		4	A0	B4	C4	D4
1	A1	B1	C1	D1		5	A1	B5	C5	D5
2	A2	B2	C2	D2		6	A6	B6	C6	D6
3	A3	B3	C3	D3		7	A7	B7	C7	D7

1. Left Join

:: Python Code:

```
leftp.merge(rightp, on='A', how='left')
#
lefts.join(rights, on='A', how='left')
    .orderBy('A', ascending=True).show()
```

:: Comparison:

	A	B	C	D	F	G	H	A	B	C	D	F	H
0	A0	B0	C0	D0	B4	C4	D4	A0	B0	C0	D0	B4	
1	A1	B1	C1	D1	B5	C5	D5	A1	B1	C1	D1	B5	
2	A2	B2	C2	D2	NaN	NaN	NaN	A2	B2	C2			
3	A3	B3	C3	D3	NaN	NaN	NaN	A3	B3	C3			

2. Right Join

:: Python Code:

```
leftp.merge(rightp, on='A', how='right')
#
lefts.join(rights, on='A', how='right')
    .orderBy('A', ascending=True).show()
```

:: Comparison:

	A	B	C	D	F	G	H	A	B	C	D	F	H
0	A0	B0	C0	D0	B4	C4	D4	A0	B0	C0	D0	B4	
1	A1	B1	C1	D1	B5	C5	D5	A1	B1	C1	D1	B5	
2	A6	NaN	NaN	NaN	B6	C6	D6	A6	NaN	NaN	NaN	B6	
3	A7	NaN	NaN	NaN	B7	C7	D7	A7	NaN	NaN	NaN	B7	

3. Inner Join

:: Python Code:

```
leftp.merge(rightp, on='A', how='inner')
#
lefts.join(rights, on='A', how='inner')
    .orderBy('A', ascending=True).show()
```

:: Comparison:

	A	B	C	D	F	G	H	
0	A0	B0	C0	D0	B4	C4	D4	A0 B0 C0 D0 B4 C4 D4
1	A1	B1	C1	D1	B5	C5	D5	A1 B1 C1 D1 B5 C5 D5

4. Full Join

:: Python Code:

```
leftp.merge(rightp, on='A', how='full')
# lefts.join(rights, on='A', how='full')
    .orderBy('A', ascending=True).show()
```

:: Comparison:

	A	B	C	D	F	G	H	
0	A0	B0	C0	D0	B4	C4	D4	A0 B0 C0 D0 ↴
1	A1	B1	C1	D1	B5	C5	D5	A1 B1 C1 D1 ↴
2	A2	B2	C2	D2	NaN	NaN	NaN	A2 B2 C2 ↴
3	A3	B3	C3	D3	NaN	NaN	NaN	A3 B3 C3 ↴
4	A6	NaN	NaN	NaN	B6	C6	D6	A6 null null null ↴
5	A7	NaN	NaN	NaN	B7	C7	D7	A7 null null null ↴
6								+-----+-----+-----+-----+

5.3.13 Concat Columns

```
my_list = [('a', 2, 3),
           ('b', 5, 6),
           ('c', 8, 9),
           ('a', 2, 3),
           ('b', 5, 6),
           ('c', 8, 9)]
col_name = ['col1', 'col2', 'col3']
#
```

(continues on next page)

(continued from previous page)

```
dp = pd.DataFrame(my_list,columns=col_name)
ds = spark.createDataFrame(my_list,schema=col_name)
```

	col1	col2	col3
0	a	2	3
1	b	5	6
2	c	8	9
3	a	2	3
4	b	5	6
5	c	8	9

:: Python Code:

```
dp['concat'] = dp.apply(lambda x:'%s%s'%(x['col1'],x['col2']),axis=1)
dp
#
ds.withColumn('concat',F.concat('col1','col2')).show()
```

:: Comparison:

	col1	col2	col3	concat
0	a	2	3	a2
1	b	5	6	b5
2	c	8	9	c8
3	a	2	3	a2
4	b	5	6	b5
5	c	8	9	c8

5.3.14 GroupBy

:: Python Code:

```
dp.groupby(['col1']).agg({'col2':'min','col3':'mean'})
#
ds.groupBy(['col1']).agg({'col2': 'min', 'col3': 'avg'}).show()
```

:: Comparison:

	col2	col3	col1 min(col2) avg(col3)
col1			
a	2	3	c 8 9.0
b	5	6	b 5 6.0
c	8	9	a 2 3.0

5.3.15 Pivot

:: Python Code:

```
pd.pivot_table(dp, values='col3', index='col1', columns='col2', aggfunc=np.sum)
#
ds.groupBy(['col1']).pivot('col2').sum('col3').show()
```

:: Comparison:

	2	5	8	
col2	2	5	8	col1 2 5 8
col1				+-----+-----+-----+
a	6.0	NaN	NaN	c null null 18
b	NaN	12.0	NaN	b null 12 null
c	NaN	NaN	18.0	a 6 null null
				+-----+-----+-----+

5.3.16 Window

```
d = {'A': ['a', 'b', 'c', 'd'], 'B': ['m', 'm', 'n', 'n'], 'C': [1, 2, 3, 6]}
dp = pd.DataFrame(d)
ds = spark.createDataFrame(dp)
```

:: Python Code:

```
dp['rank'] = dp.groupby('B')[['C']].rank('dense', ascending=False)
#
from pyspark.sql.window import Window
w = Window.partitionBy('B').orderBy(ds.C.desc())
ds = ds.withColumn('rank', F.rank().over(w))
```

:: Comparison:

	A	B	C	rank	
0	a	m	1	2.0	b m 2 1
1	b	m	2	1.0	a m 1 2
2	c	n	3	2.0	d n 6 1
3	d	n	6	1.0	c n 3 2
					+-----+-----+-----+

5.3.17 rank vs dense_rank

```
d = {'Id':[1,2,3,4,5,6],
      'Score': [4.00, 4.00, 3.85, 3.65, 3.65, 3.50]}
```

(continues on next page)

(continued from previous page)

```
#  
data = pd.DataFrame(d)  
dp = data.copy()  
ds = spark.createDataFrame(data)
```

	Id	Score
0	1	4.00
1	2	4.00
2	3	3.85
3	4	3.65
4	5	3.65
5	6	3.50

:: Python Code:

```
dp['Rank_dense'] = dp['Score'].rank(method='dense', ascending =False)  
dp['Rank'] = dp['Score'].rank(method='min', ascending =False)  
dp  
#  
import pyspark.sql.functions as F  
from pyspark.sql.window import Window  
w = Window.orderBy(ds.Score.desc())  
ds = ds.withColumn('Rank_spark_dense',F.dense_rank().over(w))  
ds = ds.withColumn('Rank_spark',F.rank().over(w))  
ds.show()
```

:: Comparison:

	Id	Score	Rank_dense	Rank	Id	Score	Rank_spark_dense	Rank_spark
0	1	4.00	1.0	1.0	1	4.0	1	1
1	2	4.00	1.0	1.0	2	4.0	1	1
2	3	3.85	2.0	3.0	3	3.85	2	3
3	4	3.65	3.0	4.0	4	3.65	3	4
4	5	3.65	3.0	4.0	5	3.65	3	4
5	6	3.50	4.0	6.0	6	3.5	4	6

CHAPTER
SIX

STATISTICS AND LINEAR ALGEBRA PRELIMINARIES

Chinese proverb

If you only know yourself, but not your opponent, you may win or may lose. If you know neither yourself nor your enemy, you will always endanger yourself – idiom, from Sunzi's Art of War

6.1 Notations

- m : the number of the samples
- n : the number of the features
- y_i : i-th label
- \hat{y}_i : i-th predicted label
- $\bar{\mathbf{y}} = \frac{1}{m} \sum_{i=1}^m y_i$: the mean of \mathbf{y} .
- \mathbf{y} : the label vector.
- $\hat{\mathbf{y}}$: the predicted label vector.

6.2 Linear Algebra Preliminaries

Since I have documented the Linear Algebra Preliminaries in my Prelim Exam note for Numerical Analysis, the interested reader is referred to [Feng2014] for more details (Figure. *Linear Algebra Preliminaries*).

1 Preliminaries

1.1 Linear Algebra Preliminaries

1.1.1 Common Properties

Properties 1.1. (Structure of Matrices) Let $A = [A_{ij}]$ be a square or rectangular matrix, A is called

- **diagonal** : if $a_{ij} = 0, \forall i \neq j,$
- **upper triangular** : if $a_{ij} = 0, \forall i > j,$
- **upper Hessenberg** : if $a_{ij} = 0, \forall i > j + 1,$
- **block diagonal** : $A = \text{diag}(A_{11}, A_{22}, \dots, A_{nn}),$
- **tridiagonal** : if $a_{ij} = 0, \forall |i - j| > 1,$
- **lower triangular** : if $a_{ij} = 0, \forall i < j,$
- **lower Hessenberg** : if $a_{ij} = 0, \forall j > i + 1,$
- **block diagonal** : $A = \text{diag}(A_{i,i-1}, A_{ii}, \dots, A_{i,i+1}).$

Properties 1.2. (Type of Matrices) Let $A = [A_{ij}]$ be a square or rectangular matrix, A is called

- **Hermitian** : if $A^* = A,$
- **symmetric** : if $A^T = A,$
- **normal** : if $A^T A = AA^T, \text{when } A \in \mathbb{R}^{n \times n},$
if $A^* A = AA^*, \text{when } A \in \mathbb{C}^{n \times n},$
- **skew hermitian** : if $A^* = -A,$
- **skew symmetric** : if $A^T = -A,$
- **orthogonal** : if $A^T A = I, \text{when } A \in \mathbb{R}^{n \times n},$
unitary : if $A^* A = I, \text{when } A \in \mathbb{C}^{n \times n}.$

Properties 1.3. (Properties of invertible matrices) Let A be $n \times n$ square matrix. If A is **invertible**, then

- $\det(A) \neq 0,$
- $\text{rank}(A) = n,$
- $Ax = b$ has a unique solution for every $b \in \mathbb{R}^n$
- the row vectors are **linearly independent**,
- the row vectors of A form a basis for $\mathbb{R}^n.$
- $\text{nullity}(A) = 0,$
- $\lambda_i \neq 0, (\lambda_i \text{ eigenvalues}),$
- $Ax = 0$ has only trivial solution,
- the column vectors are **linearly independent**,
- the column vectors of A form a basis for $\mathbb{R}^n,$
- the column vectors of A span $\mathbb{R}^n.$

Properties 1.4. (Properties of conjugate transpose) Let A,B be $n \times n$ square matrix and γ be a complex constant, then

- $(A^*)^* = A,$
- $(AB)^* = B^* A^*,$
- $(A + B)^* = A^* + B^*,$
- $\det(A^*) = \det(A)$
- $\text{tr}(A^*) = \text{tr}(A)$
- $(\gamma A)^* = \gamma^* A^*.$

Properties 1.5. (Properties of similar matrices) If $A \sim B$, then

- $\det(A) = \det(B),$
- $\text{eig}(A) = \text{eig}(B),$
- $A \sim A,$
- $\text{rank}(A) = \text{rank}(B),$
- if $B \sim C, \text{then } A \sim C$
- $B \sim A$

Fig. 1: Linear Algebra Preliminaries

6.3 Measurement Formula

6.3.1 Mean absolute error

In statistics, **MAE** (Mean absolute error) is a measure of difference between two continuous variables. The Mean Absolute Error is given by:

$$\text{MAE} = \frac{1}{m} \sum_{i=1}^m |\hat{y}_i - y_i|.$$

6.3.2 Mean squared error

In statistics, the **MSE** (Mean Squared Error) of an estimator (of a procedure for estimating an unobserved quantity) measures the average of the squares of the errors or deviations—that is, the difference between the estimator and what is estimated.

$$\text{MSE} = \frac{1}{m} \sum_{i=1}^m (\hat{y}_i - y_i)^2$$

6.3.3 Root Mean squared error

$$\text{RMSE} = \sqrt{\text{MSE}} = \sqrt{\frac{1}{m} \sum_{i=1}^m (\hat{y}_i - y_i)^2}$$

6.3.4 Total sum of squares

In statistical data analysis the **TSS** (Total Sum of Squares) is a quantity that appears as part of a standard way of presenting results of such analyses. It is defined as being the sum, over all observations, of the squared differences of each observation from the overall mean.

$$\text{TSS} = \sum_{i=1}^m (y_i - \bar{y})^2$$

6.3.5 Explained Sum of Squares

In statistics, the **ESS** (Explained sum of squares), alternatively known as the model sum of squares or sum of squares due to regression.

The ESS is the sum of the squares of the differences of the predicted values and the mean value of the response variable which is given by:

$$\text{ESS} = \sum_{i=1}^m (\hat{y}_i - \bar{y})^2$$

6.3.6 Residual Sum of Squares

In statistics, **RSS** (Residual sum of squares), also known as the sum of squared residuals (SSR) or the sum of squared errors of prediction (SSE), is the sum of the squares of residuals which is given by:

$$\text{RSS} = \sum_{i=1}^m (\hat{y}_i - y_i)^2$$

6.3.7 Coefficient of determination R^2

$$R^2 := \frac{\text{ESS}}{\text{TSS}} = 1 - \frac{\text{RSS}}{\text{TSS}}.$$

Note: In general ($\mathbf{y}^T \bar{\mathbf{y}} = \hat{\mathbf{y}}^T \bar{\mathbf{y}}$), total sum of squares = explained sum of squares + residual sum of squares, i.e.:

$$\text{TSS} = \text{ESS} + \text{RSS} \text{ if and only if } \mathbf{y}^T \bar{\mathbf{y}} = \hat{\mathbf{y}}^T \bar{\mathbf{y}}.$$

More details can be found at [Partitioning in the general ordinary least squares model](#).

6.4 Confusion Matrix

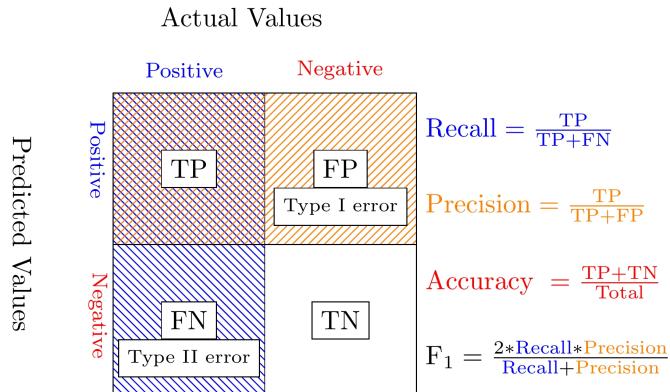


Fig. 2: Confusion Matrix

6.4.1 Recall

$$\text{Recall} = \frac{\text{TP}}{\text{TP}+\text{FN}}$$

6.4.2 Precision

$$\text{Precision} = \frac{\text{TP}}{\text{TP} + \text{FP}}$$

6.4.3 Accuracy

$$\text{Accuracy} = \frac{\text{TP} + \text{TN}}{\text{Total}}$$

6.4.4 F_1 -score

$$F_1 = \frac{2 * \text{Recall} * \text{Precision}}{\text{Recall} + \text{Precision}}$$

6.5 Statistical Tests

6.5.1 Correlational Test

- Pearson correlation: Tests for the strength of the association between two continuous variables.
- Spearman correlation: Tests for the strength of the association between two ordinal variables (does not rely on the assumption of normal distributed data).
- Chi-square: Tests for the strength of the association between two categorical variables.

6.5.2 Comparison of Means test

- Paired T-test: Tests for difference between two related variables.
- Independent T-test: Tests for difference between two independent variables.
- ANOVA: Tests the difference between group means after any other variance in the outcome variable is accounted for.

6.5.3 Non-parametric Test

- Wilcoxon rank-sum test: Tests for difference between two independent variables - takes into account magnitude and direction of difference.
- Wilcoxon sign-rank test: Tests for difference between two related variables - takes into account magnitude and direction of difference.
- Sign test: Tests if two related variables are different – ignores magnitude of change, only takes into account direction.

CHAPTER SEVEN

DATA EXPLORATION

Chinese proverb

A journey of a thousand miles begins with a single step – idiom, from Laozi.

I wouldn't say that understanding your dataset is the most difficult thing in data science, but it is really important and time-consuming. Data Exploration is about describing the data by means of statistical and visualization techniques. We explore data in order to understand the features and bring important features to our models.

7.1 Univariate Analysis

In mathematics, univariate refers to an expression, equation, function or polynomial of only one variable. “Uni” means “one”, so in other words your data has only one variable. So you do not need to deal with the causes or relationships in this step. Univariate analysis takes data, summarizes that variables (attributes) one by one and finds patterns in the data.

There are many ways that can describe patterns found in univariate data include central tendency (mean, mode and median) and dispersion: range, variance, maximum, minimum, quartiles (including the interquartile range), coefficient of variation and standard deviation. You also have several options for visualizing and describing data with univariate data. Such as frequency Distribution Tables, bar Charts, histograms, frequency Polygons, pie Charts.

The variable could be either categorical or numerical, I will demonstrate the different statistical and visualization techniques to investigate each type of the variable.

- The Jupyter notebook can be download from [Data Exploration](#).
- The data can be downloaf from [German Credit](#).

7.1.1 Numerical Variables

- Describe

The `descibe` function in pandas and spark will give us most of the statistical results, such as min, median, max, quartiles and standard deviation. With the help of the user defined function, you can get even more statistical results.

```
# selected variables for the demonstration
num_cols = ['Account Balance','No of dependents']
df.select(num_cols).describe().show()
```

```
+-----+-----+-----+
|summary| Account Balance| No of dependents|
+-----+-----+-----+
| count | 1000 | 1000 |
| mean | 2.577 | 1.155 |
| stddev | 1.2576377271108936 | 0.36208577175319395 |
| min | 1 | 1 |
| max | 4 | 2 |
+-----+-----+-----+
```

You may find out that the default function in PySpark does not include the quartiles. The following function will help you to get the same results in Pandas

```
def describe_pd(df_in, columns, deciles=False):
    """
    Function to union the basic stats results and deciles
    :param df_in: the input dataframe
    :param columns: the column name list of the numerical variable
    :param deciles: the deciles output

    :return : the numerical describe info. of the input dataframe

    :author: Ming Chen and Wenqiang Feng
    :email: von198@gmail.com
    """

    if deciles:
        percentiles = np.array(range(0, 110, 10))
    else:
        percentiles = [25, 50, 75]

    percs = np.transpose([np.percentile(df_in.select(x).collect(), percentiles) for x in columns])
    percs = pd.DataFrame(percs, columns=columns)
    percs['summary'] = [str(p) + '%' for p in percentiles]

    spark_describe = df_in.describe().toPandas()
    new_df = pd.concat([spark_describe, percs], ignore_index=True)
    new_df = new_df.round(2)
    return new_df[['summary']] + columns
```

```
describe_pd(df, num_cols)
```

summary	Account Balance	No of dependents
count	1000.0	1000.0
mean	2.577	1.155
stddev	1.2576377271108936	0.362085771753194
min	1.0	1.0
max	4.0	2.0
25%	1.0	1.0
50%	2.0	1.0
75%	4.0	1.0

Sometimes, because of the confidential data issues, you can not deliver the real data and your clients may ask more statistical results, such as deciles. You can apply the following function to achieve it.

```
describe_pd(df, num_cols, deciles=True)
```

summary	Account Balance	No of dependents
count	1000.0	1000.0
mean	2.577	1.155
stddev	1.2576377271108936	0.362085771753194
min	1.0	1.0
max	4.0	2.0
0%	1.0	1.0
10%	1.0	1.0
20%	1.0	1.0
30%	2.0	1.0
40%	2.0	1.0
50%	2.0	1.0
60%	3.0	1.0
70%	4.0	1.0
80%	4.0	1.0
90%	4.0	2.0
100%	4.0	2.0

- Skewness and Kurtosis

This subsection comes from Wikipedia [Skewness](#).

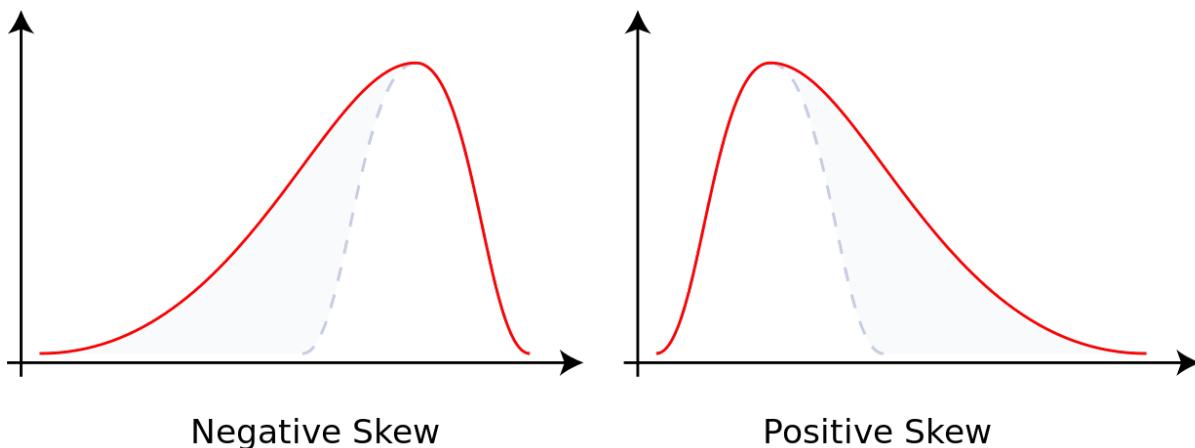
In probability theory and statistics, skewness is a measure of the asymmetry of the probability distribution of a real-valued random variable about its mean. The skewness value can be positive or negative, or undefined. For a unimodal distribution, negative skew commonly indicates that the tail is on the left side of the distribution, and positive skew indicates that the tail is on the right.

Consider the two distributions in the figure just below. Within each graph, the values on the right side of the distribution taper differently from the values on the left side. These tapering sides are called tails, and they provide a visual means to determine which of the two kinds of skewness a distribution has:

1. negative skew: The left tail is longer; the mass of the distribution is concentrated on the right of the figure. The distribution is said to be left-skewed, left-tailed, or skewed to the left, despite the fact that the curve itself appears to be skewed or leaning to the right; left instead refers to the left tail being drawn out and, often, the mean being skewed to the left of a typical center of the data. A left-skewed distribution usually appears as a right-leaning curve.
2. positive skew: The right tail is longer; the mass of the distribution is concentrated on the left of the figure. The distribution is said to be right-skewed, right-tailed, or skewed to the right, despite the fact that the curve itself appears to be skewed or leaning to the left; right instead refers to the right tail being drawn out and, often, the mean being skewed to the right of a typical center of the data. A right-skewed distribution usually appears as a left-leaning curve.

This subsection comes from Wikipedia [Kurtosis](#).

In probability theory and statistics, kurtosis (kyrtos or kurtos, meaning “curved, arching”) is a measure of the “tailedness” of the probability distribution of a real-valued random variable. In a similar way to the concept of skewness, kurtosis is a descriptor of the shape of a probability distribution and, just as for skewness, there are different ways of quantifying it for a theoretical distribution and corresponding ways of estimating it from a sample from a population.



```
from pyspark.sql.functions import col, skewness, kurtosis
df.select(skewness(var), kurtosis(var)).show()
```

```
+-----+-----+
|skewness(Age (years))|kurtosis(Age (years))|
+-----+-----+
| 1.0231743160548064 | 0.6114371688367672 |
+-----+-----+
```

Warning: Sometimes the statistics can be misleading!

F. J. Anscombe once said that make both calculations and graphs. Both sorts of output should be studied; each will contribute to understanding. These 13 datasets in Figure [Same Stats, Different Graphs](#) (the Datasaurus, plus 12 others) each have the same summary statistics (x/y mean, x/y standard deviation, and Pearson’s correlation) to two decimal places, while being drastically different in appearance. This work

describes the technique we developed to create this dataset, and others like it. More details and interesting results can be found in [Same Stats Different Graphs](#).

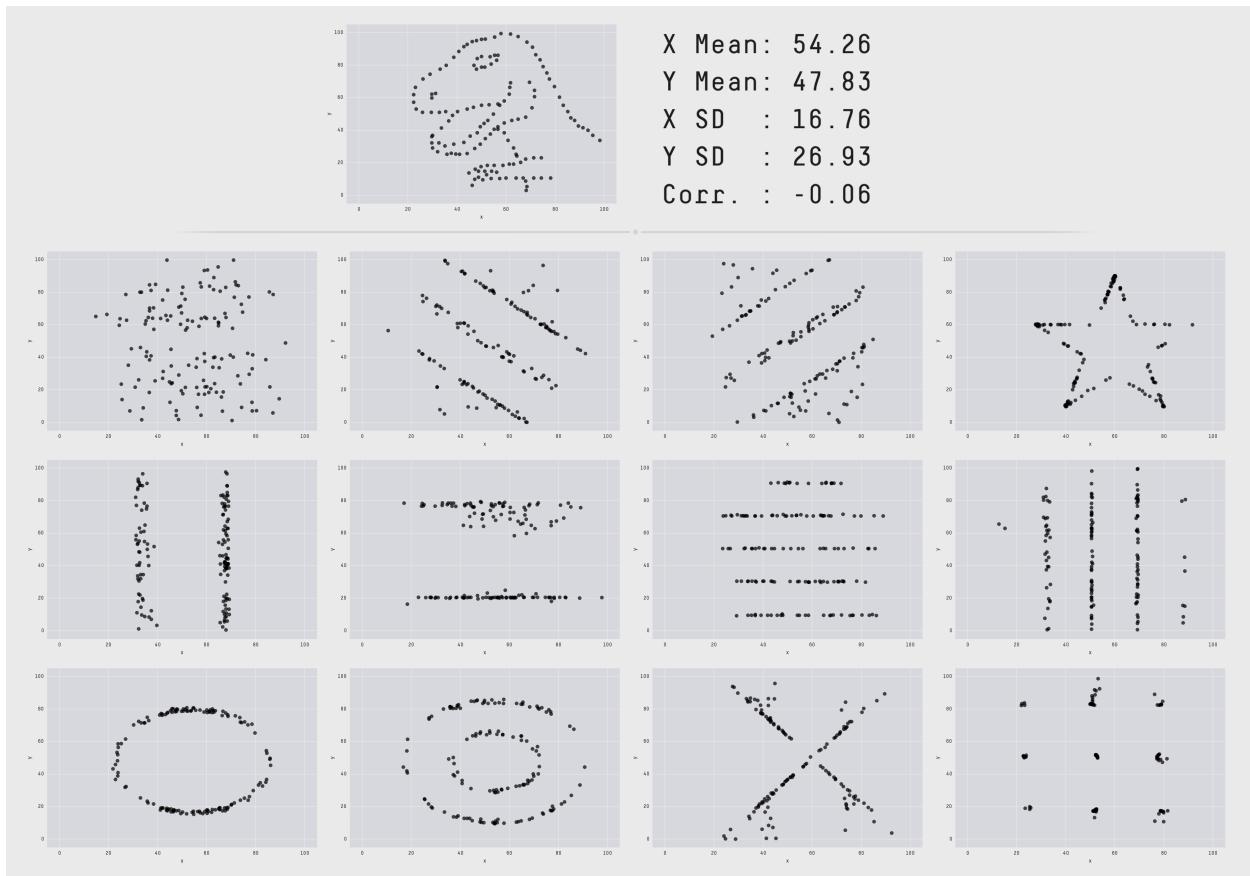


Fig. 1: Same Stats, Different Graphs

- Histogram

Warning: Histograms are often confused with Bar graphs!

The fundamental difference between histogram and bar graph will help you to identify the two easily is that there are gaps between bars in a bar graph but in the histogram, the bars are adjacent to each other. The interested reader is referred to [Difference Between Histogram and Bar Graph](#).

```
var = 'Age (years)'
x = data1[var]
bins = np.arange(0, 100, 5.0)

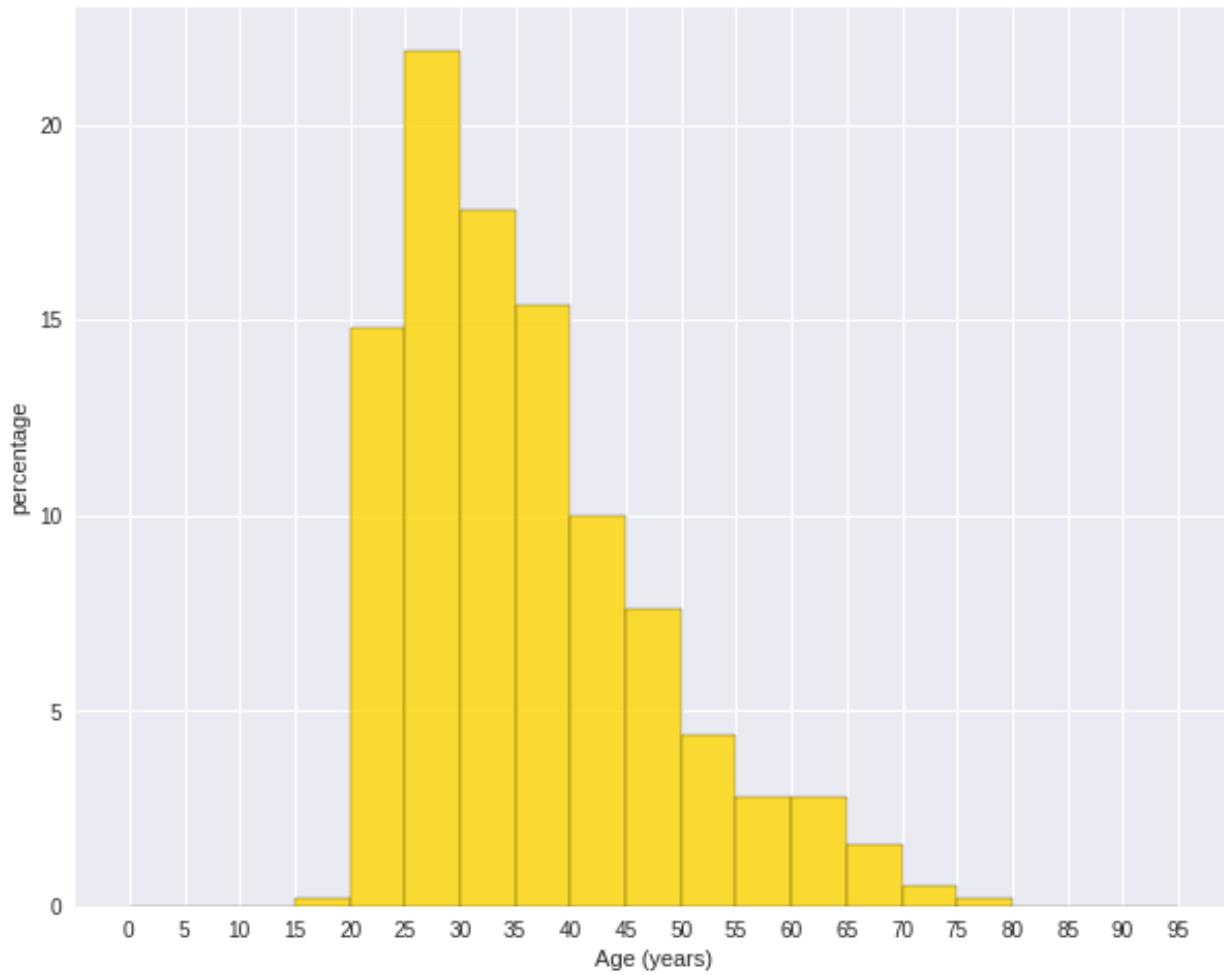
plt.figure(figsize=(10,8))
# the histogram of the data
plt.hist(x, bins, alpha=0.8, histtype='bar', color='gold',
         ec='black', weights=np.zeros_like(x) + 100. / x.size)
```

(continues on next page)

(continued from previous page)

```
plt.xlabel(var)
plt.ylabel('percentage')
plt.xticks(bins)
plt.show()

fig.savefig(var+".pdf", bbox_inches='tight')
```



```
var = 'Age (years)'
x = data1[var]
bins = np.arange(0, 100, 5.0)

#####
hist, bin_edges = np.histogram(x,bins,
                               weights=np.zeros_like(x) + 100. / x.size)
# make the histogram

fig = plt.figure(figsize=(20, 8))
ax = fig.add_subplot(1, 2, 1)
```

(continues on next page)

(continued from previous page)

```

# Plot the histogram heights against integers on the x axis
ax.bar(range(len(hist)),hist,width=1,alpha=0.8,ec ='black', color='gold')
# # Set the ticks to the middle of the bars
ax.set_xticks([0.5+i for i,j in enumerate(hist)])
# Set the xticklabels to a string that tells us what the bin edges were
labels =['{}'.format(int(bins[i+1])) for i,j in enumerate(hist)]
labels.insert(0,'0')
ax.set_xticklabels(labels)
plt.xlabel(var)
plt.ylabel('percentage')

#####
hist, bin_edges = np.histogram(x,bins) # make the histogram

ax = fig.add_subplot(1, 2, 2)
# Plot the histogram heights against integers on the x axis
ax.bar(range(len(hist)),hist,width=1,alpha=0.8,ec ='black', color='gold')

# # Set the ticks to the middle of the bars
ax.set_xticks([0.5+i for i,j in enumerate(hist)])

# Set the xticklabels to a string that tells us what the bin edges were
labels =['{}'.format(int(bins[i+1])) for i,j in enumerate(hist)]
labels.insert(0,'0')
ax.set_xticklabels(labels)
plt.xlabel(var)
plt.ylabel('count')
plt.suptitle('Histogram of {}: Left with percentage output; Right with count'_
             'output'
             .format(var), size=16)
plt.show()

fig.savefig(var+".pdf", bbox_inches='tight')

```

Sometimes, some people will ask you to plot the unequal width (invalid argument for histogram) of the bars. You can still achieve it by the following trick.

```

var = 'Credit Amount'
plot_data = df.select(var).toPandas()
x= plot_data[var]

bins =[0,200,400,600,700,800,900,1000,2000,3000,4000,5000,6000,10000,25000]

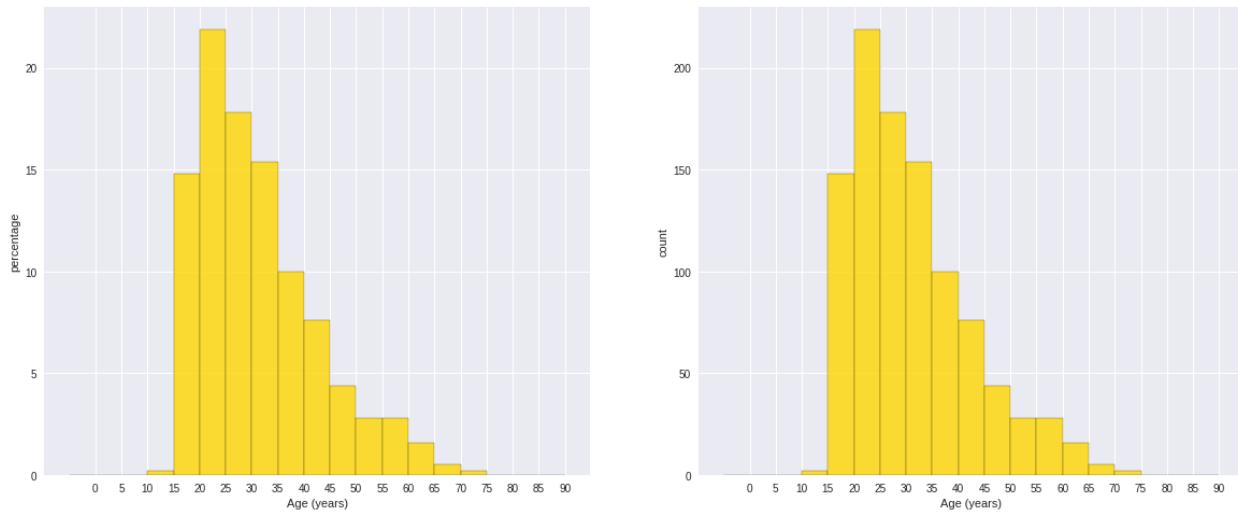
hist, bin_edges = np.histogram(x,bins,weights=np.zeros_like(x) + 100. / x_
                               .size) # make the histogram

fig = plt.figure(figsize=(10, 8))
ax = fig.add_subplot(1, 1, 1)
# Plot the histogram heights against integers on the x axis

```

(continues on next page)

Histogram of Age (years): Left with percentage output; Right with count output



(continued from previous page)

```
ax.bar(range(len(hist)),hist,width=1,alpha=0.8,ec ='black',color = 'gold')

# # Set the ticks to the middle of the bars
ax.set_xticks([0.5+i for i,j in enumerate(hist)])

# Set the xticklabels to a string that tells us what the bin edges were
#labels =['{}k'.format(int(bins[i+1]/1000)) for i,j in enumerate(hist)]
labels =['{}'.format(bins[i+1]) for i,j in enumerate(hist)]
labels.insert(0,'0')
ax.set_xticklabels(labels)
#plt.text(-0.6, -1.4,'0')
plt.xlabel(var)
plt.ylabel('percentage')
plt.show()
```

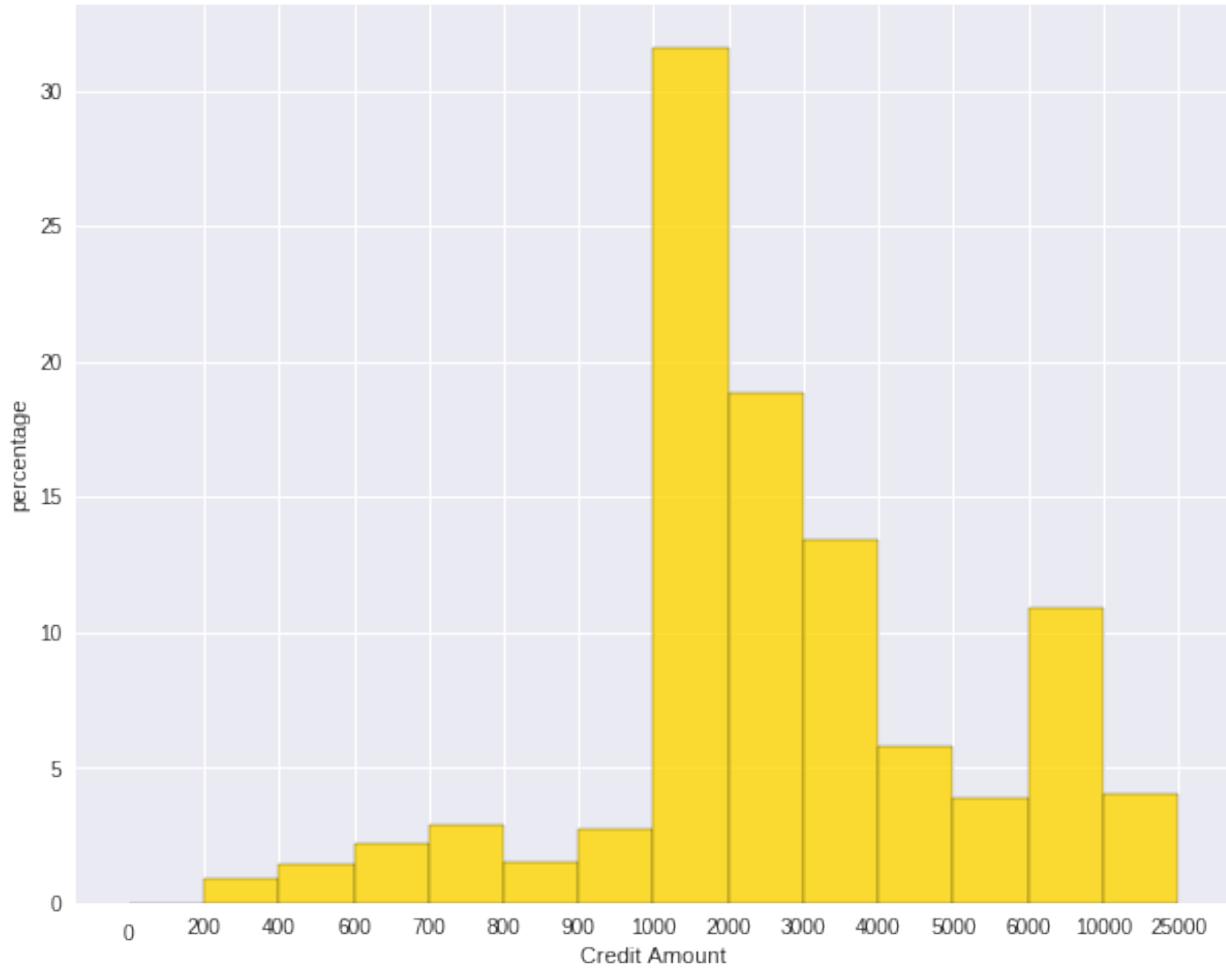
- Box plot and violin plot

Note that although violin plots are closely related to Tukey's (1977) box plots, the violin plot can show more information than box plot. When we perform an exploratory analysis, nothing about the samples could be known. So the distribution of the samples can not be assumed to a normal distribution and usually when you get a big data, the normal distribution will show some outliers in box plot.

However, the violin plots are potentially misleading for smaller sample sizes, where the density plots can appear to show interesting features (and group-differences therein) even when produced for standard normal data. Some poster suggested the sample size should larger than 250. The sample sizes (e.g. n>250 or ideally even larger), where the kernel density plots provide a reasonably accurate representation of the distributions, potentially showing nuances such as bimodality or other forms of non-normality that would be invisible or less clear in box plots. More details can be found in [A simple comparison of box plots and violin plots](#).

```
x = df.select(var).toPandas()
```

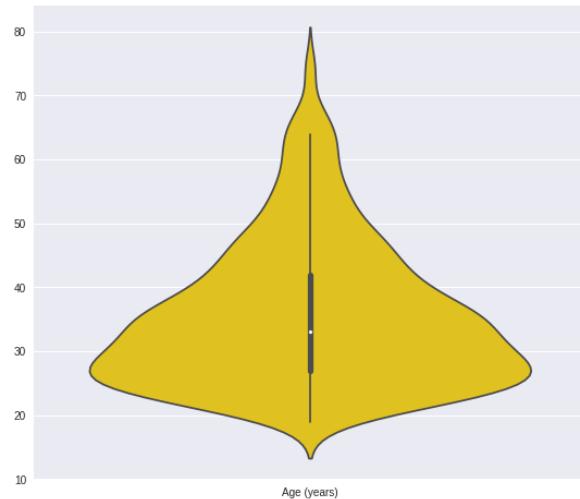
(continues on next page)



(continued from previous page)

```
fig = plt.figure(figsize=(20, 8))
ax = fig.add_subplot(1, 2, 1)
ax = sns.boxplot(data=x)

ax = fig.add_subplot(1, 2, 2)
ax = sns.violinplot(data=x)
```



7.1.2 Categorical Variables

Compared with the numerical variables, the categorical variables are much more easier to do the exploration.

- Frequency table

```
from pyspark.sql import functions as F
from pyspark.sql.functions import rank,sum,col
from pyspark.sql import Window

window = Window.rowsBetween(Window.unboundedPreceding,Window.
    unboundedFollowing)
# withColumn('Percent %',F.format_string("%5.0f%%\n",col('Credit_num')*100/
    <col('total'))).\
tab = df.select(['age_class','Credit Amount']).\
    groupBy('age_class').\
    agg(F.count('Credit Amount').alias('Credit_num'),
        F.mean('Credit Amount').alias('Credit_avg'),
        F.min('Credit Amount').alias('Credit_min'),
        F.max('Credit Amount').alias('Credit_max')).\
    withColumn('total',sum(col('Credit_num')).over(window)).\
    withColumn('Percent',col('Credit_num')*100/col('total')).\
    drop(col('total'))
```

age_class	Credit_num	Credit_avg	Credit_min	Credit_max	Percent

(continues on next page)

(continued from previous page)

	45-54	120	3183.066666666666	338	12612	12.0
	<25	150	2970.733333333333	276	15672	15.0
	55-64	56	3493.660714285714	385	15945	5.6
	35-44	254	3403.771653543307	250	15857	25.4
	25-34	397	3298.823677581864	343	18424	39.7
	65+	23	3210.1739130434785	571	14896	2.3

- Pie plot

```
# Data to plot
labels = plot_data.age_class
sizes = plot_data.Percent
colors = ['gold', 'yellowgreen', 'lightcoral', 'blue', 'lightskyblue', 'green',
         ↪'red']
explode = (0, 0.1, 0, 0, 0, 0) # explode 1st slice

# Plot
plt.figure(figsize=(10,8))
plt.pie(sizes, explode=explode, labels=labels, colors=colors,
         autopct='%.1f%%', shadow=True, startangle=140)

plt.axis('equal')
plt.show()
```

- Bar plot

```
labels = plot_data.age_class
missing = plot_data.Percent
ind = [x for x, _ in enumerate(labels)]

plt.figure(figsize=(10,8))
plt.bar(ind, missing, width=0.8, label='missing', color='gold')

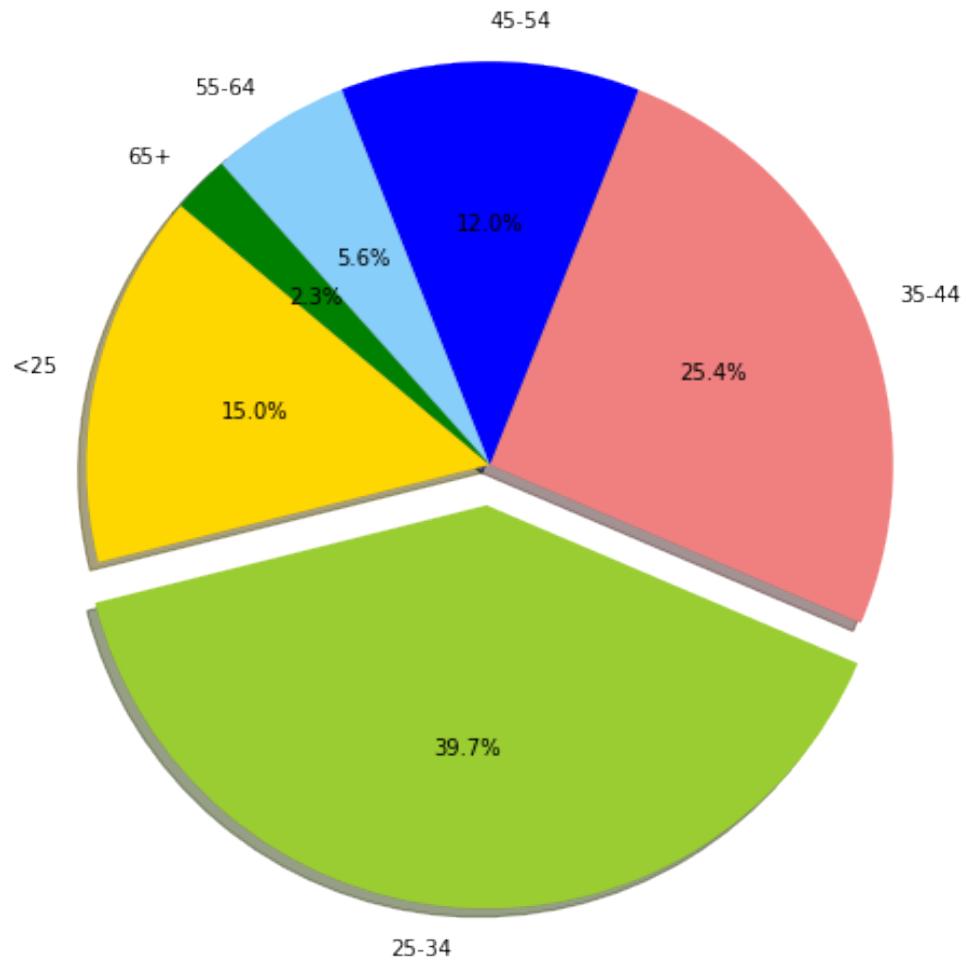
plt.xticks(ind, labels)
plt.ylabel("percentage")

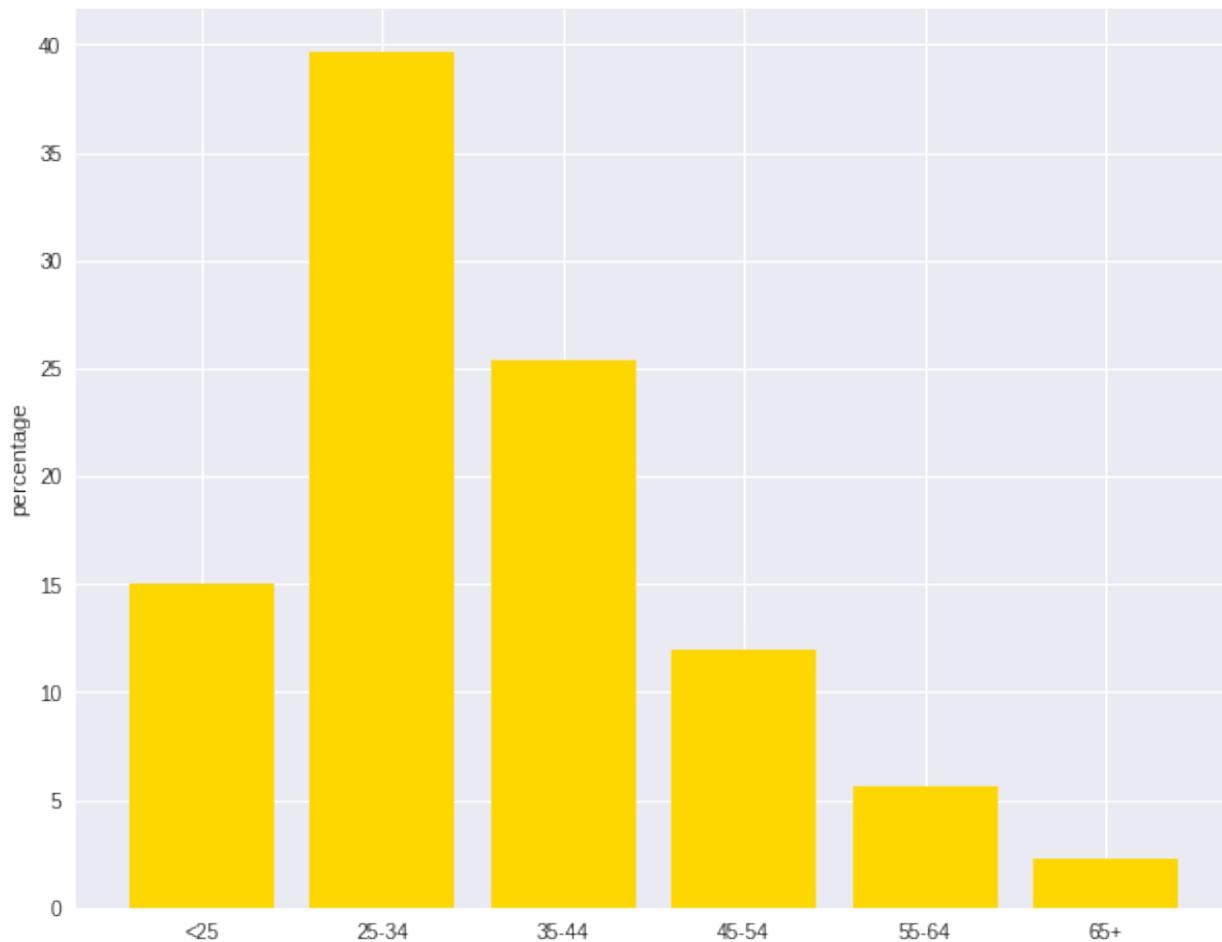
plt.show()
```

```
labels = ['missing', '<25', '25-34', '35-44', '45-54', '55-64', '65+']
missing = np.array([0.000095, 0.024830, 0.028665, 0.029477, 0.031918, 0.037073,
                   ↪0.026699])
man = np.array([0.000147, 0.036311, 0.038684, 0.044761, 0.051269, 0.059542, 0.
                   ↪0.054259])
women = np.array([0.004035, 0.032935, 0.035351, 0.041778, 0.048437, 0.056236,
                   ↪0.048091])
ind = [x for x, _ in enumerate(labels)]

plt.figure(figsize=(10,8))
plt.bar(ind, women, width=0.8, label='women', color='gold', ↪
         bottom=man+missing)
```

(continues on next page)



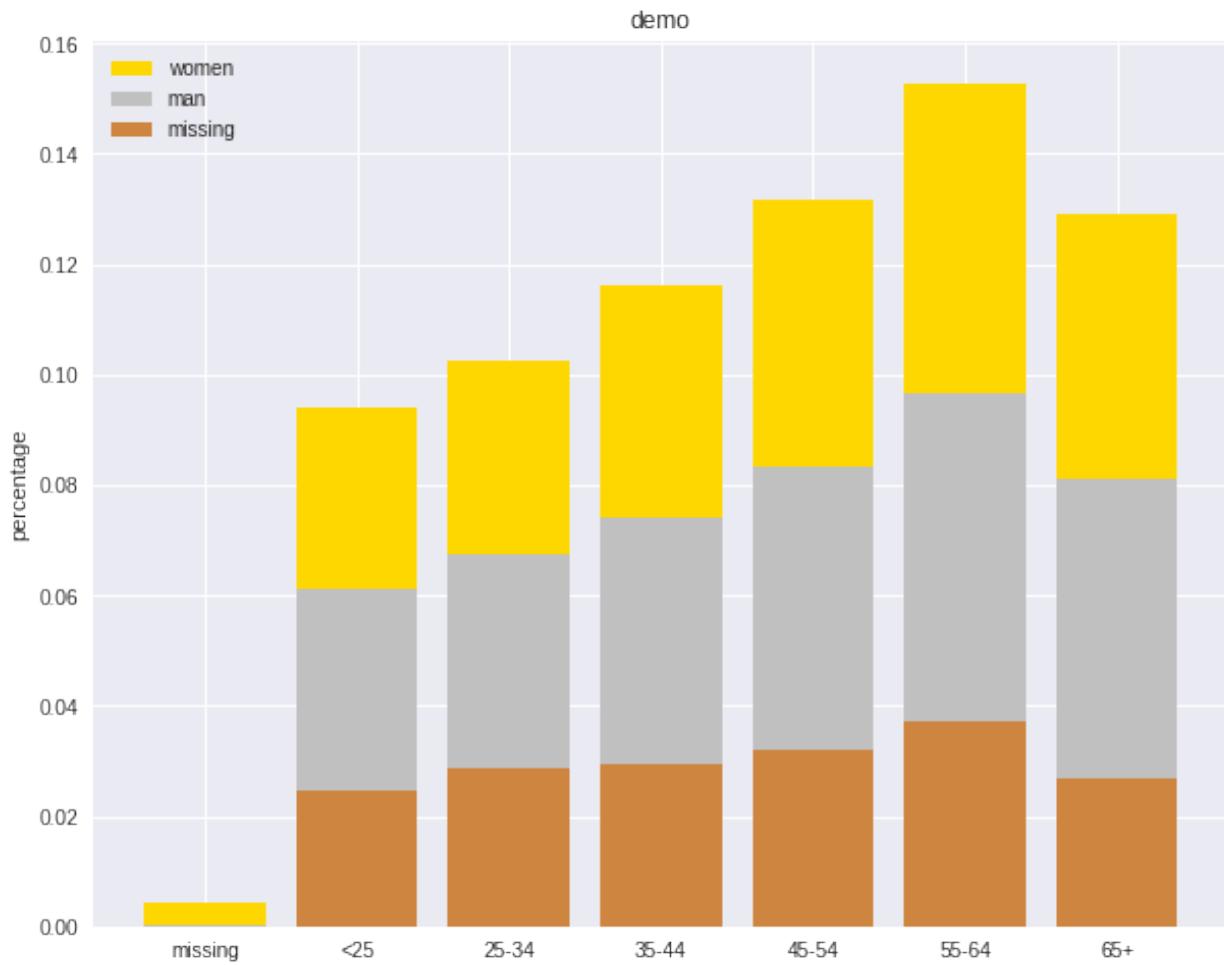


(continued from previous page)

```
plt.bar(ind, man, width=0.8, label='man', color='silver', bottom=missing)
plt.bar(ind, missing, width=0.8, label='missing', color='#CD853F')

plt.xticks(ind, labels)
plt.ylabel("percentage")
plt.legend(loc="upper left")
plt.title("demo")

plt.show()
```



7.2 Multivariate Analysis

In this section, I will only demonstrate the bivariate analysis. Since the multivariate analysis is the generation of the bivariate.

7.2.1 Numerical V.S. Numerical

- Correlation matrix

```
from pyspark.mllib.stat import Statistics
import pandas as pd

corr_data = df.select(num_cols)

col_names = corr_data.columns
features = corr_data.rdd.map(lambda row: row[0:]))
corr_mat=Statistics.corr(features, method="pearson")
corr_df = pd.DataFrame(corr_mat)
corr_df.index, corr_df.columns = col_names, col_names

print(corr_df.to_string())
```

Account Balance	No of dependents
1.0	-0.01414542650320914
-0.01414542650320914	1.0

- Scatter Plot

```
import seaborn as sns
sns.set(style="ticks")

df = sns.load_dataset("iris")
sns.pairplot(df, hue="species")
plt.show()
```

7.2.2 Categorical V.S. Categorical

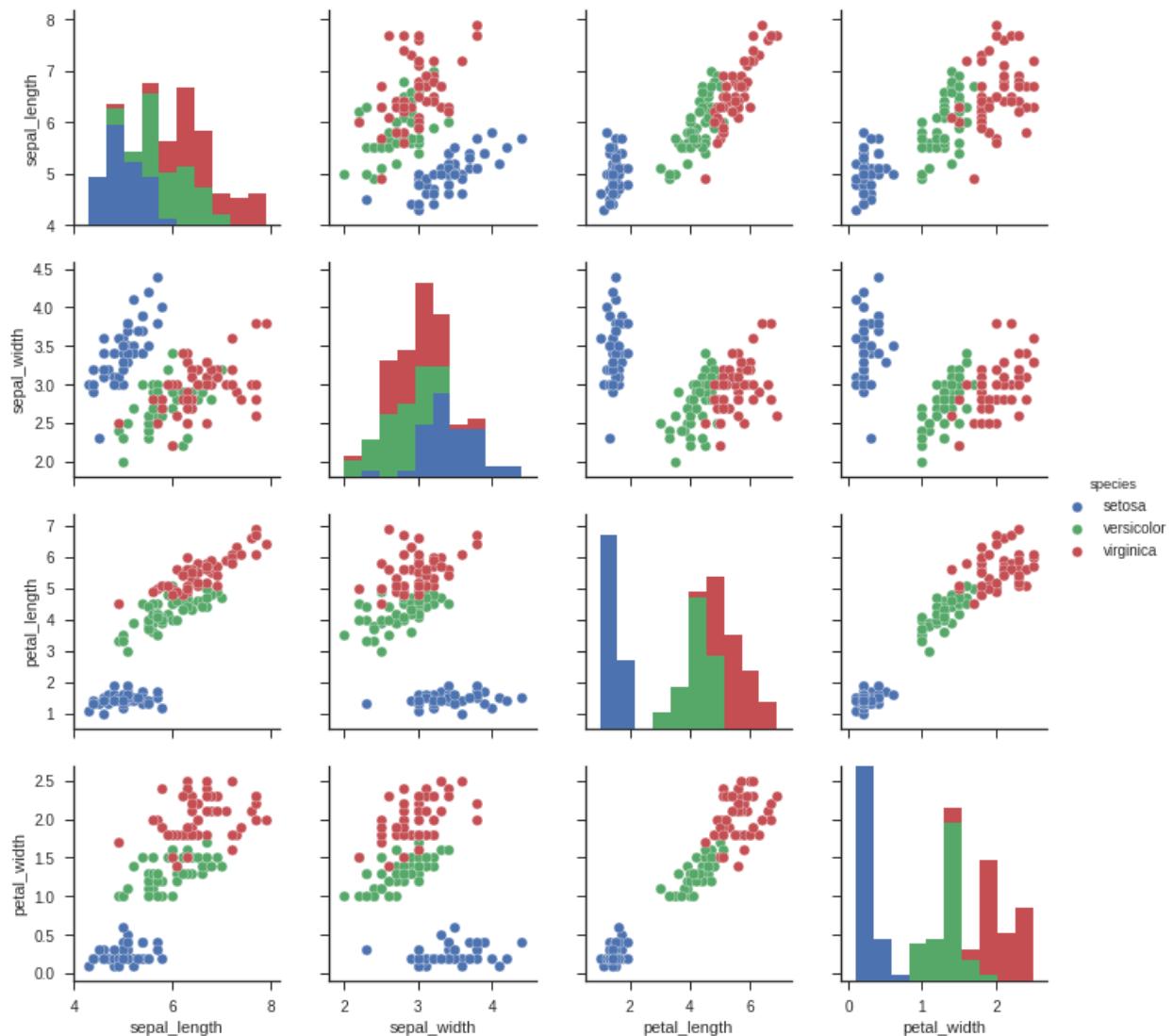
- Pearson's Chi-squared test

Warning: pyspark.ml.stat is only available in Spark 2.4.0.

```
from pyspark.ml.linalg import Vectors
from pyspark.ml.stat import ChiSquareTest

data = [(0.0, Vectors.dense(0.5, 10.0)),
        (0.0, Vectors.dense(1.5, 20.0)),
        (1.0, Vectors.dense(1.5, 30.0)),
        (0.0, Vectors.dense(3.5, 30.0)),
        (0.0, Vectors.dense(3.5, 40.0)),
        (1.0, Vectors.dense(3.5, 40.0))]
```

(continues on next page)



(continued from previous page)

```
df = spark.createDataFrame(data, ["label", "features"])

r = ChiSquareTest.test(df, "features", "label").head()
print("pValues: " + str(r.pValues))
print("degreesOfFreedom: " + str(r.degreesOfFreedom))
print("statistics: " + str(r.statistics))
```

```
pValues: [0.687289278791, 0.682270330336]
degreesOfFreedom: [2, 3]
statistics: [0.75, 1.5]
```

- Cross table

```
df.stat.crosstab("age_class", "Occupation").show()
```

age_class_Occupation	1	2	3	4
<25	4	34	108	4
55–64	1	15	31	9
25–34	7	61	269	60
35–44	4	58	143	49
65+	5	3	6	9
45–54	1	29	73	17

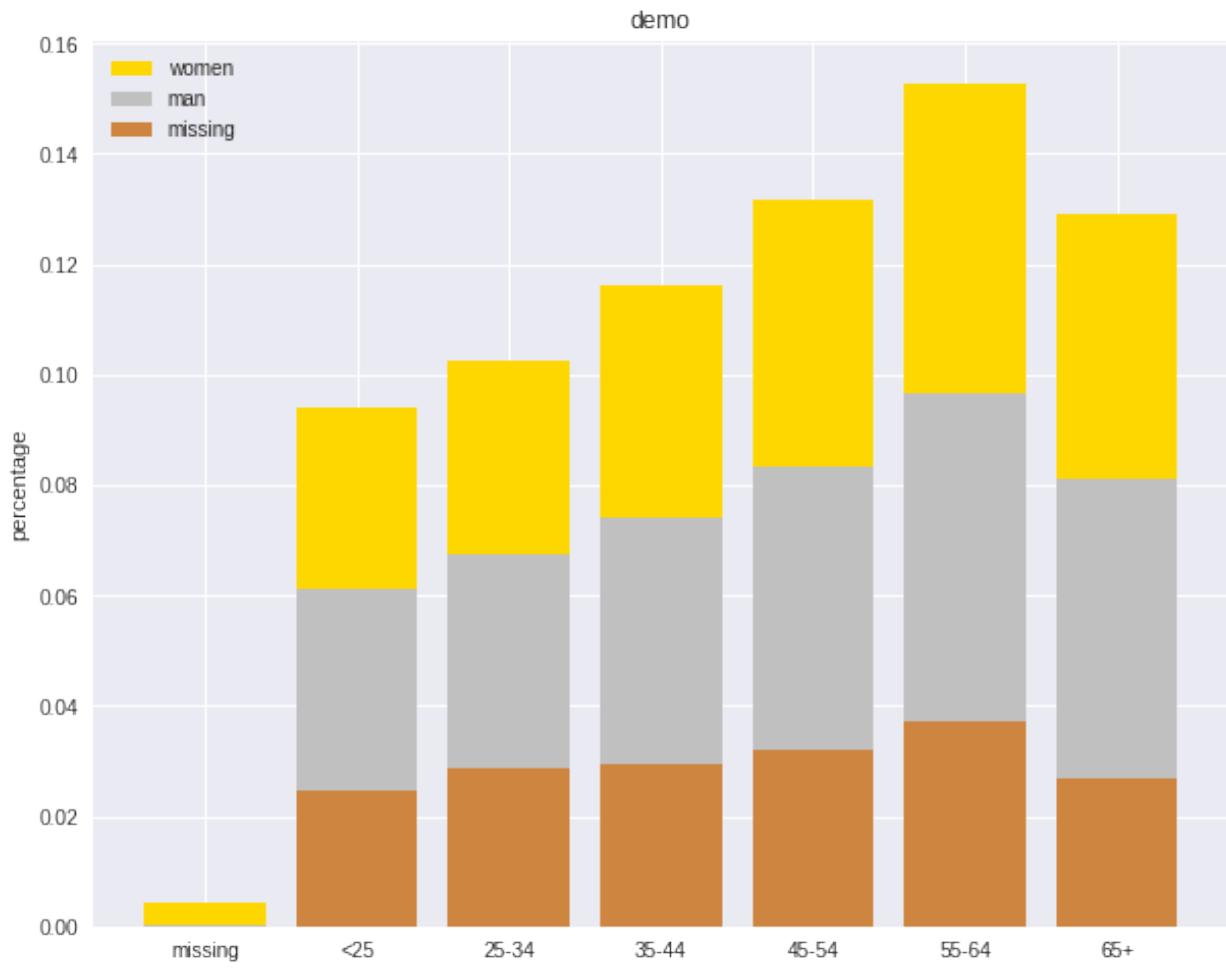
- Stacked plot

```
labels = ['missing', '<25', '25-34', '35-44', '45-54', '55-64', '65+']
missing = np.array([0.000095, 0.024830, 0.028665, 0.029477, 0.031918, 0.037073,
    ↪0.026699])
man = np.array([0.000147, 0.036311, 0.038684, 0.044761, 0.051269, 0.059542, 0.
    ↪0.054259])
women = np.array([0.004035, 0.032935, 0.035351, 0.041778, 0.048437, 0.056236,
    ↪0.048091])
ind = [x for x, _ in enumerate(labels)]

plt.figure(figsize=(10,8))
plt.bar(ind, women, width=0.8, label='women', color='gold', ↪
    ↪bottom=man+missing)
plt.bar(ind, man, width=0.8, label='man', color='silver', bottom=missing)
plt.bar(ind, missing, width=0.8, label='missing', color='#CD853F')

plt.xticks(ind, labels)
plt.ylabel("percentage")
plt.legend(loc="upper left")
plt.title("demo")

plt.show()
```



7.2.3 Numerical V.S. Categorical

**CHAPTER
EIGHT**

REGRESSION

Chinese proverb

A journey of a thousand miles begins with a single step. – old Chinese proverb

In statistical modeling, regression analysis focuses on investigating the relationship between a dependent variable and one or more independent variables. [Wikipedia Regression analysis](#)

In data mining, Regression is a model to represent the relationship between the value of lable (or target, it is numerical variable) and on one or more features (or predictors they can be numerical and categorical variables).

8.1 Linear Regression

8.1.1 Introduction

Given that a data set $\{x_{i1}, \dots, x_{in}, y_i\}_{i=1}^m$ which contains n features (variables) and m samples (data points), in simple linear regression model for modeling m data points with j independent variables: x_{ij} , the formula is given by:

$$y_i = \beta_0 + \beta_j x_{ij}, \text{ where, } i = 1, \dots, m, j = 1, \dots, n.$$

In matrix notation, the data set is written as $\mathbf{X} = [x_1, \dots, x_n]$ with $x_j = \{x_{ij}\}_{i=1}^m$, $\mathbf{y} = \{y_i\}_{i=1}^m$ (see Fig. [Feature matrix and label](#)) and $\boldsymbol{\beta}^\top = \{\beta_j\}_{j=1}^n$. Then the matrix format equation is written as

$$\mathbf{y} = \mathbf{X}\boldsymbol{\beta}. \quad (8.1)$$

8.1.2 How to solve it?

1. Direct Methods (For more information please refer to my [Prelim Notes for Numerical Analysis](#))

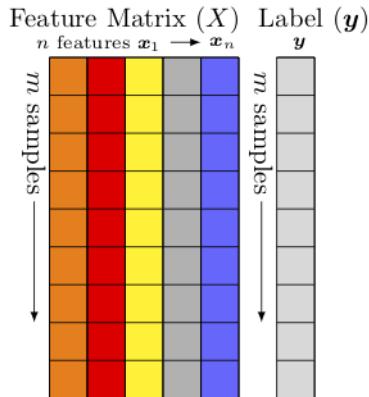


Fig. 1: Feature matrix and label

- For squared or rectangular matrices
 - Singular Value Decomposition
 - Gram-Schmidt orthogonalization
 - QR Decomposition
- For squared matrices
 - LU Decomposition
 - Cholesky Decomposition
 - Regular Splittings

2. Iterative Methods

- Stationary cases iterative method
 - Jacobi Method
 - Gauss-Seidel Method
 - Richardson Method
 - Successive Over Relaxation (SOR) Method
- Dynamic cases iterative method
 - Chebyshev iterative Method
 - Minimal residuals Method
 - Minimal correction iterative method
 - Steepest Descent Method
 - Conjugate Gradients Method

8.1.3 Ordinary Least Squares

In mathematics, (8.1) is a overdetermined system. The method of ordinary least squares can be used to find an approximate solution to overdetermined systems. For the system overdetermined system (8.1), the least squares formula is obtained from the problem

$$\min_{\beta} \|\mathbf{X}\beta - \mathbf{y}\|, \quad (8.2)$$

the solution of which can be written with the normal equations:

$$\beta = (\mathbf{X}^T \mathbf{X})^{-1} \mathbf{X}^T \mathbf{y} \quad (8.3)$$

where T indicates a matrix transpose, provided $(\mathbf{X}^T \mathbf{X})^{-1}$ exists (that is, provided \mathbf{X} has full column rank).

Note: Actually, (8.3) can be derived by the following way: multiply \mathbf{X}^T on side of (8.1) and then multiply $(\mathbf{X}^T \mathbf{X})^{-1}$ on both side of the former result. You may also apply the Extreme Value Theorem to (8.2) and find the solution (8.3).

8.1.4 Gradient Descent

Let's use the following hypothesis:

$$h_{\beta} = \beta_0 + \beta_j x_j, \text{ where, } j = 1, \dots, n.$$

Then, solving (8.2) is equivalent to minimize the following cost function:

8.1.5 Cost Function

$$J(\beta) = \frac{1}{2m} \sum_{i=1}^m (h_{\beta}(x^{(i)}) - y^{(i)})^2 \quad (8.4)$$

Note: The reason why we prefer to solve (8.4) rather than (8.2) is because (8.4) is convex and it has some nice properties, such as it's uniquely solvable and energy stable for small enough learning rate. the interested reader who has great interest in non-convex cost function (energy) case. is referred to [Feng2016PSD] for more details.

8.1.6 Batch Gradient Descent

Gradient descent is a first-order iterative optimization algorithm for finding the minimum of a function. It searches with the direction of the steepest descent which is defined by the negative of the gradient (see Fig. *Gradient Descent in 1D* and *Gradient Descent in 2D* for 1D and 2D, respectively) and with learning rate (search step) α .

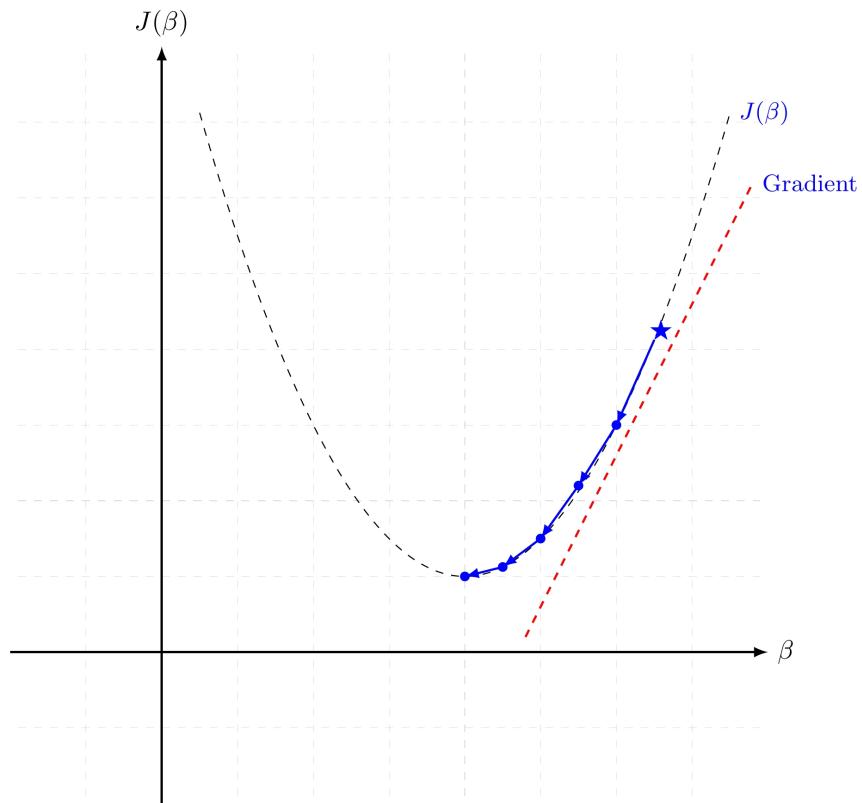


Fig. 2: Gradient Descent in 1D

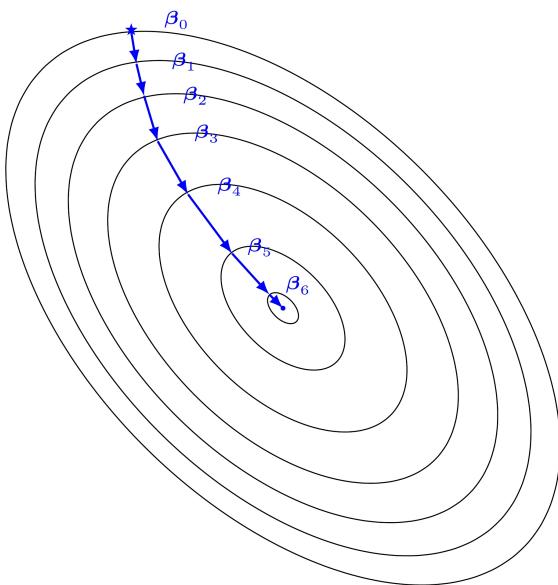


Fig. 3: Gradient Descent in 2D

8.1.7 Stochastic Gradient Descent

8.1.8 Mini-batch Gradient Descent

8.1.9 Demo

- The Jupyter notebook can be download from [Linear Regression](#) which was implemented without using Pipeline.
- The Jupyter notebook can be download from [Linear Regression with Pipeline](#) which was implemented with using Pipeline.
- I will only present the code with pipeline style in the following.
- For more details about the parameters, please visit [Linear Regression API](#).

1. Set up spark context and SparkSession

```
from pyspark.sql import SparkSession

spark = SparkSession \
    .builder \
    .appName("Python Spark regression example") \
    .config("spark.some.config.option", "some-value") \
    .getOrCreate()
```

2. Load dataset

```
df = spark.read.format('com.databricks.spark.csv') \
    .options(header='true', \
    inferschema='true') \
    .load("../data/Advertising.csv", header=True);
```

check the data set

```
df.show(5, True)
df.printSchema()
```

Then you will get

```
+----+----+----+----+
|    TV|Radio|Newspaper|Sales|
+----+----+----+----+
| 230.1| 37.8|   69.2| 22.1|
|  44.5| 39.3|   45.1| 10.4|
| 17.2| 45.9|   69.3|  9.3|
|151.5| 41.3|   58.5| 18.5|
|180.8| 10.8|   58.4| 12.9|
+----+----+----+----+
only showing top 5 rows

root
 |-- TV: double (nullable = true)
```

(continues on next page)

(continued from previous page)

```
| -- Radio: double (nullable = true)
| -- Newspaper: double (nullable = true)
| -- Sales: double (nullable = true)
```

You can also get the Statistical results from the data frame (Unfortunately, it only works for numerical).

```
df.describe().show()
```

Then you will get

```
+-----+-----+-----+-----+
|summary|      TV|      Radio|    Newspaper|
|Sales|  
+-----+-----+-----+-----+
| count |      200|      200|      200|
| mean | 147.0425| 23.26400000000024| 30.55399999999995| 14.  
02250000000003|
| stddev| 85.85423631490805| 14.846809176168728| 21.77862083852283| 5.  
217456565710477|
| min |      0.7|      0.0|      0.3|
| 1.6|  
| max |     296.4|      49.6|     114.0|
| 27.0|  
+-----+-----+-----+-----+
```

3. Convert the data to dense vector (**features** and **label**)

```
from pyspark.sql import Row
from pyspark.ml.linalg import Vectors

# I provide two ways to build the features and labels

# method 1 (good for small feature):
#def transData(row):
#    return Row(label=row["Sales"],
#               features=Vectors.dense([row["TV"],
#                                      row["Radio"],
#                                      row["Newspaper"]]))

# Method 2 (good for large features):
def transData(data):
    return data.rdd.map(lambda r: [Vectors.dense(r[:-1]), r[-1]]).toDF(['features',
                                                               'label'])
```

Note: You are strongly encouraged to try my `get_dummy` function for dealing with the categorical data in complex dataset.

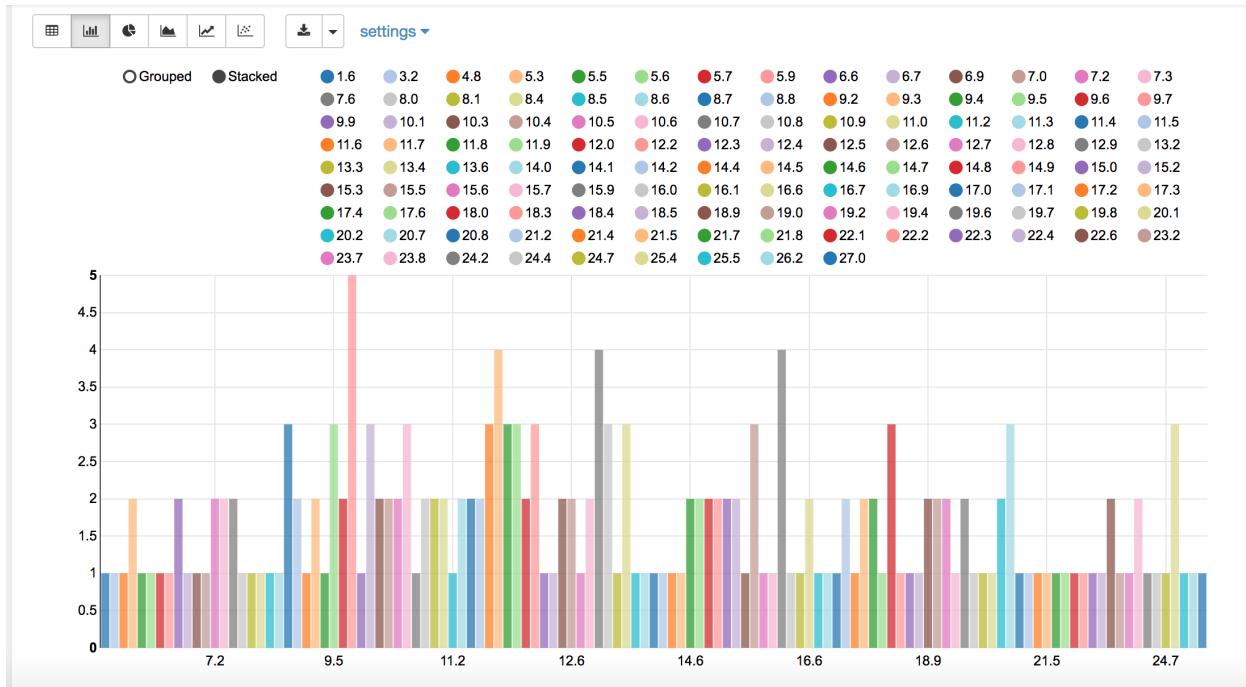


Fig. 4: Sales distribution

Supervised learning version:

```
def get_dummy(df, indexCol, categoricalCols, continuousCols, labelCol):

    from pyspark.ml import Pipeline
    from pyspark.ml.feature import StringIndexer, OneHotEncoder,
    ↪VectorAssembler
    from pyspark.sql.functions import col

    indexers = [ StringIndexer(inputCol=c, outputCol="{0}_indexed".
    ↪format(c))
        for c in categoricalCols ]

    # default setting: dropLast=True
    encoders = [ OneHotEncoder(inputCol=indexer.getOutputCol(),
        outputCol="{0}_encoded".format(indexer.
    ↪getOutputCol()))
        for indexer in indexers ]

    assembler = VectorAssembler(inputCols=[encoder.getOutputCol() ↪
    ↪for encoder in encoders]
        + continuousCols, outputCol="features"
    ↪" )

    pipeline = Pipeline(stages=indexers + encoders + [assembler])

    model=pipeline.fit(df)
    data = model.transform(df)
```

(continues on next page)

(continued from previous page)

```
data = data.withColumn('label', col(labelCol))

return data.select(indexCol, 'features', 'label')
```

Unsupervised learning version:

```
def get_dummy(df, indexCol, categoricalCols, continuousCols):
    """
    Get dummy variables and concat with continuous variables for
    unsupervised learning.
    :param df: the dataframe
    :param categoricalCols: the name list of the categorical data
    :param continuousCols: the name list of the numerical data
    :return k: feature matrix

    :author: Wenqiang Feng
    :email: von198@gmail.com
    """

    indexers = [ StringIndexer(inputCol=c, outputCol="{0}_indexed".
    format(c))
        for c in categoricalCols ]

    # default setting: dropLast=True
    encoders = [ OneHotEncoder(inputCol=indexer.getOutputCol(),
        outputCol="{0}_encoded".format(indexer.
    getOutputCol()))
        for indexer in indexers ]

    assembler = VectorAssembler(inputCols=[encoder.getOutputCol()].
    for encoder in encoders]
        + continuousCols, outputCol="features"
    )

    pipeline = Pipeline(stages=indexers + encoders + [assembler])

    model=pipeline.fit(df)
    data = model.transform(df)

    return data.select(indexCol, 'features')
```

4. Transform the dataset to DataFrame

```
transformed= transData(df)
transformed.show(5)
```

features	label

(continues on next page)

(continued from previous page)

```
| [230.1,37.8,69.2]| 22.1|
| [44.5,39.3,45.1]| 10.4|
| [17.2,45.9,69.3]| 9.3|
| [151.5,41.3,58.5]| 18.5|
| [180.8,10.8,58.4]| 12.9|
+-----+
only showing top 5 rows
```

Note: You will find out that all of the supervised machine learning algorithms in Spark are based on the **features** and **label** (unsupervised machine learning algorithms in Spark are based on the **features**). That is to say, you can play with all of the machine learning algorithms in Spark when you get ready the **features** and **label** in pipeline architecture.

5. Deal With Categorical Variables

```
from pyspark.ml import Pipeline
from pyspark.ml.regression import LinearRegression
from pyspark.ml.feature import VectorIndexer
from pyspark.ml.evaluation import RegressionEvaluator

# Automatically identify categorical features, and index them.
# We specify maxCategories so features with > 4 distinct values are treated
# as continuous.

featureIndexer = VectorIndexer(inputCol="features", \
                                outputCol="indexedFeatures", \
                                maxCategories=4).fit(transformed)

data = featureIndexer.transform(transformed)
```

Now you check your dataset with

```
data.show(5, True)
```

you will get

```
+-----+-----+-----+
|       features|label| indexedFeatures|
+-----+-----+-----+
| [230.1,37.8,69.2]| 22.1|[230.1,37.8,69.2]|
| [44.5,39.3,45.1]| 10.4|[44.5,39.3,45.1]|
| [17.2,45.9,69.3]| 9.3|[17.2,45.9,69.3]|
| [151.5,41.3,58.5]| 18.5|[151.5,41.3,58.5]|
| [180.8,10.8,58.4]| 12.9|[180.8,10.8,58.4]|
+-----+-----+-----+
only showing top 5 rows
```

6. Split the data into training and test sets (40% held out for testing)

```
# Split the data into training and test sets (40% held out for testing)
(trainingData, testData) = transformed.randomSplit([0.6, 0.4])
```

You can check your train and test data as follows (In my opinion, it is always good to keep tracking your data during prototype phase):

```
trainingData.show(5)
testData.show(5)
```

Then you will get

```
+-----+-----+
|      features|label|indexedFeatures|
+-----+-----+
| [4.1,11.6,5.7]|  3.2| [4.1,11.6,5.7]|
| [5.4,29.9,9.4]|  5.3| [5.4,29.9,9.4]|
| [7.3,28.1,41.4]|  5.5|[7.3,28.1,41.4]|
| [7.8,38.9,50.6]|  6.6|[7.8,38.9,50.6]|
| [8.6,2.1,1.0] |  4.8| [8.6,2.1,1.0]|
+-----+-----+
only showing top 5 rows

+-----+-----+
|      features|label| indexedFeatures|
+-----+-----+
| [0.7,39.6,8.7]|  1.6| [0.7,39.6,8.7]|
| [8.4,27.2,2.1]|  5.7| [8.4,27.2,2.1]|
| [11.7,36.9,45.2]|  7.3|[11.7,36.9,45.2]|
| [13.2,15.9,49.6]|  5.6|[13.2,15.9,49.6]|
| [16.9,43.7,89.4]|  8.7|[16.9,43.7,89.4]|
+-----+-----+
only showing top 5 rows
```

7. Fit Ordinary Least Square Regression Model

For more details about the parameters, please visit [Linear Regression API](#).

```
# Import LinearRegression class
from pyspark.ml.regression import LinearRegression

# Define LinearRegression algorithm
lr = LinearRegression()
```

8. Pipeline Architecture

```
# Chain indexer and tree in a Pipeline
pipeline = Pipeline(stages=[featureIndexer, lr])

model = pipeline.fit(trainingData)
```

9. Summary of the Model

Spark has a poor summary function for data and model. I wrote a summary function which has similar format as **R** output for the linear regression in PySpark.

```
def modelsummary(model):
    import numpy as np
    print ("Note: the last rows are the information for Intercept")
    print ("##", "-----")
    print ("##", " Estimate | Std.Error | t Values | P-value")
    coef = np.append(list(model.coefficients),model.intercept)
    Summary=model.summary

    for i in range(len(Summary.pValues)):
        print ("##", '{:10.6f}'.format(coef[i]), \
              '{:10.6f}'.format(Summary.coefficientStandardErrors[i]), \
              '{:8.3f}'.format(Summary.tValues[i]), \
              '{:10.6f}'.format(Summary.pValues[i]))

    print ("##", '---')
    print ("##", "Mean squared error: % .6f" \
          % Summary.meanSquaredError, ", RMSE: % .6f" \
          % Summary.rootMeanSquaredError )
    print ("##", "Multiple R-squared: %f" % Summary.r2, ", \
          Total iterations: %i" % Summary.totalIterations)
```

```
modelsummary(model.stages[-1])
```

You will get the following summary results:

```
Note: the last rows are the information for Intercept
('##', '-----')
('##', ' Estimate | Std.Error | t Values | P-value')
('##', ' 0.044186', ' 0.001663', ' 26.573', ' 0.000000')
('##', ' 0.206311', ' 0.010846', ' 19.022', ' 0.000000')
('##', ' 0.001963', ' 0.007467', ' 0.263', ' 0.793113')
('##', ' 2.596154', ' 0.379550', ' 6.840', ' 0.000000')
('##', '---')
('##', 'Mean squared error: 2.588230', ', RMSE: 1.608798')
('##', 'Multiple R-squared: 0.911869', ', Total iterations: 1')
```

10. Make predictions

```
# Make predictions.
predictions = model.transform(testData)
```

```
# Select example rows to display.
predictions.select("features", "label", "predictedLabel").show(5)
```

features	label	prediction
[0.7, 39.6, 8.7]	1.6	10.81405928637388
[8.4, 27.2, 2.1]	5.7	8.583086404079918

(continues on next page)

(continued from previous page)

```
| [11.7,36.9,45.2] | 7.3|10.814712818232422 |
| [13.2,15.9,49.6] | 5.6| 6.557106943899219 |
| [16.9,43.7,89.4] | 8.7|12.534151375058645 |
+-----+-----+
only showing top 5 rows
```

9. Evaluation

```
from pyspark.ml.evaluation import RegressionEvaluator
# Select (prediction, true label) and compute test error
evaluator = RegressionEvaluator(labelCol="label",
                                 predictionCol="prediction",
                                 metricName="rmse")

rmse = evaluator.evaluate(predictions)
print("Root Mean Squared Error (RMSE) on test data = %g" % rmse)
```

The final Root Mean Squared Error (RMSE) is as follows:

```
Root Mean Squared Error (RMSE) on test data = 1.63114
```

You can also check the R^2 value for the test data:

```
y_true = predictions.select("label").toPandas()
y_pred = predictions.select("prediction").toPandas()

import sklearn.metrics
r2_score = sklearn.metrics.r2_score(y_true, y_pred)
print('r2_score: {0}'.format(r2_score))
```

Then you will get

```
r2_score: 0.854486655585
```

Warning: You should know most softwares are using different formula to calculate the R^2 value when no intercept is included in the model. You can get more information from the [disscussion at StackExchange](#).

8.2 Generalized linear regression

8.2.1 Introduction

8.2.2 How to solve it?

8.2.3 Demo

- The Jupyter notebook can be download from [Generalized Linear Regression](#).
 - For more details about the parameters, please visit [Generalized Linear Regression API](#) .
1. Set up spark context and SparkSession

```
from pyspark.sql import SparkSession

spark = SparkSession \
    .builder \
    .appName("Python Spark regression example") \
    .config("spark.some.config.option", "some-value") \
    .getOrCreate()
```

2. Load dataset

```
df = spark.read.format('com.databricks.spark.csv') \
    .options(header='true', \
    inferschema='true') \
    .load("../data/Advertising.csv", header=True);
```

check the data set

```
df.show(5, True)
df.printSchema()
```

Then you will get

```
+---+---+---+---+
| TV|Radio|Newspaper|Sales|
+---+---+---+---+
| 230.1| 37.8| 69.2| 22.1|
| 44.5| 39.3| 45.1| 10.4|
| 17.2| 45.9| 69.3| 9.3|
| 151.5| 41.3| 58.5| 18.5|
| 180.8| 10.8| 58.4| 12.9|
+---+---+---+---+
only showing top 5 rows

root
 |-- TV: double (nullable = true)
 |-- Radio: double (nullable = true)
 |-- Newspaper: double (nullable = true)
 |-- Sales: double (nullable = true)
```

Learning Apache Spark with Python

You can also get the Statistical results from the data frame (Unfortunately, it only works for numerical).

```
df.describe().show()
```

Then you will get

summary	TV	Radio	Newspaper
Sales			
count	200	200	200
mean	147.0425	23.26400000000024	30.55399999999995
stddev	85.85423631490805	14.846809176168728	21.77862083852283
min	0.7	0.0	0.3
max	296.4	49.6	114.0

3. Convert the data to dense vector (**features** and **label**)

Note: You are strongly encouraged to try my `get_dummy` function for dealing with the categorical data in complex dataset.

Supervised learning version:

```
def get_dummy(df, indexCol, categoricalCols, continuousCols, labelCol):  
  
    from pyspark.ml import Pipeline  
    from pyspark.ml.feature import StringIndexer, OneHotEncoder,  
    VectorAssembler  
    from pyspark.sql.functions import col  
  
    indexers = [ StringIndexer(inputCol=c, outputCol="{0}_indexed".  
    format(c))  
                for c in categoricalCols ]  
  
    # default setting: dropLast=True  
    encoders = [ OneHotEncoder(inputCol=indexer.getOutputCol(),  
                                outputCol="{0}_encoded".format(indexer.  
                                getOutputCol()))  
                for indexer in indexers ]  
  
    assembler = VectorAssembler(inputCols=[encoder.getOutputCol()  
    for encoder in encoders]  
                                + continuousCols, outputCol="features")
```

(continues on next page)

(continued from previous page)

```

pipeline = Pipeline(stages=indexers + encoders + [assembler])

model=pipeline.fit(df)
data = model.transform(df)

data = data.withColumn('label',col(labelCol))

return data.select(indexCol,'features','label')

```

Unsupervised learning version:

```

def get_dummy(df,indexCol,categoricalCols,continuousCols):
    """
    Get dummy variables and concat with continuous variables for
    unsupervised learning.
    :param df: the dataframe
    :param categoricalCols: the name list of the categorical data
    :param continuousCols: the name list of the numerical data
    :return k: feature matrix

    :author: Wenqiang Feng
    :email: von198@gmail.com
    """

    indexers = [ StringIndexer(inputCol=c, outputCol="{0}_indexed".
    format(c))
        for c in categoricalCols ]

    # default setting: dropLast=True
    encoders = [ OneHotEncoder(inputCol=indexer.getOutputCol(),
                                outputCol="{0}_encoded".format(indexer.
    getOutputCol()))
        for indexer in indexers ]

    assembler = VectorAssembler(inputCols=[encoder.getOutputCol()].
    for encoder in encoders]
                                + continuousCols, outputCol="features
    ")

    pipeline = Pipeline(stages=indexers + encoders + [assembler])

    model=pipeline.fit(df)
    data = model.transform(df)

    return data.select(indexCol,'features')

```

```

from pyspark.sql import Row
from pyspark.ml.linalg import Vectors

```

(continues on next page)

(continued from previous page)

```
# I provide two ways to build the features and labels

# method 1 (good for small feature):
def transData(row):
    return Row(label=row["Sales"],
               features=Vectors.dense([row["TV"],
                                       row["Radio"],
                                       row["Newspaper"]]))

# Method 2 (good for large features):
def transData(data):
    return data.rdd.map(lambda r: [Vectors.dense(r[:-1]), r[-1]]).toDF(['features',
                                                               'label'])
```

```
transformed= transData(df)
transformed.show(5)
```

```
+-----+----+
|      features|label |
+-----+----+
| [230.1,37.8,69.2]| 22.1|
| [44.5,39.3,45.1]| 10.4|
| [17.2,45.9,69.3]|  9.3|
| [151.5,41.3,58.5]| 18.5|
| [180.8,10.8,58.4]| 12.9|
+-----+----+
only showing top 5 rows
```

Note: You will find out that all of the machine learning algorithms in Spark are based on the **features** and **label**. That is to say, you can play with all of the machine learning algorithms in Spark when you get ready the **features** and **label**.

4. Convert the data to dense vector

```
# convert the data to dense vector
def transData(data):
    return data.rdd.map(lambda r: [r[-1], Vectors.dense(r[:-1])]).\
        toDF(['label','features'])

from pyspark.sql import Row
from pyspark.ml.linalg import Vectors

data= transData(df)
data.show()
```

5. Deal with the Categorical variables

```

from pyspark.ml import Pipeline
from pyspark.ml.regression import LinearRegression
from pyspark.ml.feature import VectorIndexer
from pyspark.ml.evaluation import RegressionEvaluator

# Automatically identify categorical features, and index them.
# We specify maxCategories so features with > 4
# distinct values are treated as continuous.

featureIndexer = VectorIndexer(inputCol="features", \
                                outputCol="indexedFeatures", \
                                maxCategories=4).fit(transformed)

data = featureIndexer.transform(transformed)

```

When you check your data at this point, you will get

features	label	indexedFeatures
[230.1, 37.8, 69.2]	22.1	[230.1, 37.8, 69.2]
[44.5, 39.3, 45.1]	10.4	[44.5, 39.3, 45.1]
[17.2, 45.9, 69.3]	9.3	[17.2, 45.9, 69.3]
[151.5, 41.3, 58.5]	18.5	[151.5, 41.3, 58.5]
[180.8, 10.8, 58.4]	12.9	[180.8, 10.8, 58.4]

only showing top 5 rows

6. Split the data into training and test sets (40% held out for testing)

```

# Split the data into training and test sets (40% held out for testing)
(trainingData, testData) = transformed.randomSplit([0.6, 0.4])

```

You can check your train and test data as follows (In my opinion, it is always good to keep tracking your data during prototype phase):

```

trainingData.show(5)
testData.show(5)

```

Then you will get

features	label	indexedFeatures
[5.4, 29.9, 9.4]	5.3	[5.4, 29.9, 9.4]
[7.8, 38.9, 50.6]	6.6	[7.8, 38.9, 50.6]
[8.4, 27.2, 2.1]	5.7	[8.4, 27.2, 2.1]
[8.7, 48.9, 75.0]	7.2	[8.7, 48.9, 75.0]
[11.7, 36.9, 45.2]	7.3	[11.7, 36.9, 45.2]

only showing top 5 rows

(continues on next page)

(continued from previous page)

```
+-----+-----+
|      features|label|indexedFeatures|
+-----+-----+
| [0.7,39.6,8.7]|  1.6| [0.7,39.6,8.7] |
| [4.1,11.6,5.7]|  3.2| [4.1,11.6,5.7] |
| [7.3,28.1,41.4]|  5.5|[7.3,28.1,41.4] |
| [8.6,2.1,1.0]|  4.8| [8.6,2.1,1.0] |
| [17.2,4.1,31.6]|  5.9|[17.2,4.1,31.6] |
+-----+-----+
only showing top 5 rows
```

7. Fit Generalized Linear Regression Model

```
# Import LinearRegression class
from pyspark.ml.regression import GeneralizedLinearRegression

# Define LinearRegression algorithm
glr = GeneralizedLinearRegression(family="gaussian", link="identity", \
                                    maxIter=10, regParam=0.3)
```

8. Pipeline Architecture

```
# Chain indexer and tree in a Pipeline
pipeline = Pipeline(stages=[featureIndexer, glr])

model = pipeline.fit(trainingData)
```

9. Summary of the Model

Spark has a poor summary function for data and model. I wrote a summary function which has similar format as R output for the linear regression in PySpark.

```
def modelsummary(model):
    import numpy as np
    print ("Note: the last rows are the information for Intercept")
    print ("##", "-----")
    print ("##", " Estimate | Std.Error | t Values | P-value")
    coef = np.append(list(model.coefficients),model.intercept)
    Summary=model.summary

    for i in range(len(Summary.pValues)):
        print ("##", '{:10.6f}'.format(coef[i]), \
              '{:10.6f}'.format(Summary.coefficientStandardErrors[i]), \
              '{:8.3f}'.format(Summary.tValues[i]), \
              '{:10.6f}'.format(Summary.pValues[i]))

    print ("##", '---')
    #    print ("##", "Mean squared error: % .6f" \
    #          "% Summary.meanSquaredError, ", RMSE: % .6f" \
    #          "% Summary.rootMeanSquaredError )
    #    print ("##", "Multiple R-squared: %f" % Summary.r2, ", \
    #          Total iterations: %i" % Summary.totalIterations)
```

```
modelsummary(model.stages[-1])
```

You will get the following summary results:

```
Note: the last rows are the information for Intercept
('##', '-----')
('##', ' Estimate | Std.Error | t Values | P-value')
('##', ' 0.042857', ' 0.001668', ' 25.692', ' 0.000000')
('##', ' 0.199922', ' 0.009881', ' 20.232', ' 0.000000')
('##', ' -0.001957', ' 0.006917', ' -0.283', ' 0.777757')
('##', ' 3.007515', ' 0.406389', ' 7.401', ' 0.000000')
('##', '---')
```

10. Make predictions

```
# Make predictions.
predictions = model.transform(testData)
```

```
# Select example rows to display.
predictions.select("features", "label", "predictedLabel").show(5)
```

features	label	prediction
[0.7, 39.6, 8.7]	1.6	10.937383732327625
[4.1, 11.6, 5.7]	3.2	5.491166258750164
[7.3, 28.1, 41.4]	5.5	8.8571603947873
[8.6, 2.1, 1.0]	4.8	3.793966281660073
[17.2, 4.1, 31.6]	5.9	4.502507124763654

only showing top 5 rows

11. Evaluation

```
from pyspark.ml.evaluation import RegressionEvaluator
from pyspark.ml.evaluation import RegressionEvaluator
# Select (prediction, true label) and compute test error
evaluator = RegressionEvaluator(labelCol="label",
                                 predictionCol="prediction",
                                 metricName="rmse")

rmse = evaluator.evaluate(predictions)
print("Root Mean Squared Error (RMSE) on test data = %g" % rmse)
```

The final Root Mean Squared Error (RMSE) is as follows:

```
Root Mean Squared Error (RMSE) on test data = 1.89857
```

```
y_true = predictions.select("label").toPandas()
y_pred = predictions.select("prediction").toPandas()
```

(continues on next page)

(continued from previous page)

```
import sklearn.metrics
r2_score = sklearn.metrics.r2_score(y_true, y_pred)
print('r2_score: {}'.format(r2_score))
```

Then you will get the R^2 value:

```
r2_score: 0.87707391843
```

8.3 Decision tree Regression

8.3.1 Introduction

8.3.2 How to solve it?

8.3.3 Demo

- The Jupyter notebook can be download from [Decision Tree Regression](#).
 - For more details about the parameters, please visit [Decision Tree Regressor API](#) .
1. Set up spark context and SparkSession

```
from pyspark.sql import SparkSession

spark = SparkSession \
    .builder \
    .appName("Python Spark regression example") \
    .config("spark.some.config.option", "some-value") \
    .getOrCreate()
```

2. Load dataset

```
df = spark.read.format('com.databricks.spark.csv') \
    .options(header='true', \
    inferschema='true') \
    .load("../data/Advertising.csv", header=True);
```

check the data set

```
df.show(5, True)
df.printSchema()
```

Then you will get

TV	Radio	Newspaper	Sales
230.1	37.8	69.2	22.1

(continues on next page)

(continued from previous page)

```
| 44.5| 39.3|      45.1| 10.4|
| 17.2| 45.9|      69.3|   9.3|
|151.5| 41.3|      58.5| 18.5|
|180.8| 10.8|      58.4| 12.9|
+---+---+---+---+
only showing top 5 rows
```

```
root
 |-- TV: double (nullable = true)
 |-- Radio: double (nullable = true)
 |-- Newspaper: double (nullable = true)
 |-- Sales: double (nullable = true)
```

You can also get the Statistical results from the data frame (Unfortunately, it only works for numerical).

```
df.describe().show()
```

Then you will get

```
+-----+-----+-----+-----+
|summary|          TV|        Radio|    Newspaper|
|Sales|-----+-----+-----+
+-----+-----+-----+-----+
|  count |      200|      200|      200|
|  mean | 147.0425|23.26400000000024|30.55399999999995|14.
|stddev|85.85423631490805|14.846809176168728| 21.77862083852283| 5.
|  min |      0.7|      0.0|      0.3|
|  max |    296.4|     49.6|    114.0|
+-----+-----+-----+-----+
|-----+
```

3. Convert the data to dense vector (**features** and **label**)

Note: You are strongly encouraged to try my `get_dummy` function for dealing with the categorical data in complex dataset.

Supervised learning version:

```
def get_dummy(df, indexCol, categoricalCols, continuousCols, labelCol):
    from pyspark.ml import Pipeline
    from pyspark.ml.feature import StringIndexer, OneHotEncoder,
    VectorAssembler
    from pyspark.sql.functions import col
```

(continues on next page)

(continued from previous page)

```

indexers = [ StringIndexer(inputCol=c, outputCol="{0}_indexed".
˓→format(c))
             for c in categoricalCols ]

# default setting: dropLast=True
encoders = [ OneHotEncoder(inputCol=indexer.getOutputCol(),
                            outputCol="{0}_encoded".format(indexer.
˓→getOutputCol()))
             for indexer in indexers ]

assembler = VectorAssembler(inputCols=[encoder.getOutputCol()].
˓→for encoder in encoders]
                           + continuousCols, outputCol="features
˓→")

pipeline = Pipeline(stages=indexers + encoders + [assembler])

model=pipeline.fit(df)
data = model.transform(df)

data = data.withColumn('label', col(labelCol))

return data.select(indexCol, 'features', 'label')

```

Unsupervised learning version:

```

def get_dummy(df, indexCol, categoricalCols, continuousCols):
    """
    Get dummy variables and concat with continuous variables for
    →unsupervised learning.
    :param df: the dataframe
    :param categoricalCols: the name list of the categorical data
    :param continuousCols: the name list of the numerical data
    :return k: feature matrix

    :author: Wenqiang Feng
    :email: von198@gmail.com
    """

    indexers = [ StringIndexer(inputCol=c, outputCol="{0}_indexed".
˓→format(c))
                 for c in categoricalCols ]

    # default setting: dropLast=True
    encoders = [ OneHotEncoder(inputCol=indexer.getOutputCol(),
                                outputCol="{0}_encoded".format(indexer.
˓→getOutputCol()))
                 for indexer in indexers ]

    assembler = VectorAssembler(inputCols=[encoder.getOutputCol()].
˓→for encoder in encoders]

```

(continues on next page)

(continued from previous page)

```
+ continuousCols, outputCol="features"
    ↵")
pipeline = Pipeline(stages=indexers + encoders + [assembler])

model=pipeline.fit(df)
data = model.transform(df)

return data.select(indexCol, 'features')
```

```
from pyspark.sql import Row
from pyspark.ml.linalg import Vectors

# I provide two ways to build the features and labels

# method 1 (good for small feature):
#def transData(row):
#    return Row(label=row["Sales"],
#               features=Vectors.dense([row["TV"],
#                                      row["Radio"],
#                                      row["Newspaper"]]))

# Method 2 (good for large features):
def transData(data):
    return data.rdd.map(lambda r: [Vectors.dense(r[:-1]), r[-1]]).toDF(['features',
    ↵'label'])
```

```
transformed= transData(df)
transformed.show(5)
```

```
+-----+----+
|      features|label|
+-----+----+
| [230.1,37.8,69.2]| 22.1|
| [44.5,39.3,45.1]| 10.4|
| [17.2,45.9,69.3]|  9.3|
| [151.5,41.3,58.5]| 18.5|
| [180.8,10.8,58.4]| 12.9|
+-----+----+
only showing top 5 rows
```

Note: You will find out that all of the machine learning algorithms in Spark are based on the **features** and **label**. That is to say, you can play with all of the machine learning algorithms in Spark when you get ready the **features** and **label**.

4. Convert the data to dense vector

```
# convert the data to dense vector
def transData(data):
    return data.rdd.map(lambda r: [r[-1], Vectors.dense(r[:-1])]).\
        toDF(['label','features'])

transformed = transData(df)
transformed.show(5)
```

5. Deal with the Categorical variables

```
from pyspark.ml import Pipeline
from pyspark.ml.regression import LinearRegression
from pyspark.ml.feature import VectorIndexer
from pyspark.ml.evaluation import RegressionEvaluator

# Automatically identify categorical features, and index them.
# We specify maxCategories so features with > 4
# distinct values are treated as continuous.

featureIndexer = VectorIndexer(inputCol="features", \
                                outputCol="indexedFeatures", \
                                maxCategories=4).fit(transformed)

data = featureIndexer.transform(transformed)
```

When you check your data at this point, you will get

```
+-----+-----+
|      features|label| indexedFeatures|
+-----+-----+
| [230.1,37.8,69.2]| 22.1|[230.1,37.8,69.2]|
| [44.5,39.3,45.1]| 10.4|[44.5,39.3,45.1]|
| [17.2,45.9,69.3]|  9.3|[17.2,45.9,69.3]|
| [151.5,41.3,58.5]| 18.5|[151.5,41.3,58.5]|
| [180.8,10.8,58.4]| 12.9|[180.8,10.8,58.4]|
+-----+-----+
only showing top 5 rows
```

6. Split the data into training and test sets (40% held out for testing)

```
# Split the data into training and test sets (40% held out for testing)
(trainingData, testData) = transformed.randomSplit([0.6, 0.4])
```

You can check your train and test data as follows (In my opinion, it is always good to keep tracking your data during prototype phase):

```
trainingData.show(5)
testData.show(5)
```

Then you will get

```
+-----+-----+
|      features|label|indexedFeatures|
+-----+-----+
| [4.1,11.6,5.7]|  3.2| [4.1,11.6,5.7]|
| [7.3,28.1,41.4]|  5.5|[7.3,28.1,41.4]|
| [8.4,27.2,2.1]|  5.7| [8.4,27.2,2.1]|
| [8.6,2.1,1.0]|  4.8| [8.6,2.1,1.0]|
| [8.7,48.9,75.0]| 7.2|[8.7,48.9,75.0]|
+-----+-----+
only showing top 5 rows

+-----+-----+
|      features|label| indexedFeatures|
+-----+-----+
| [0.7,39.6,8.7]|  1.6| [0.7,39.6,8.7]|
| [5.4,29.9,9.4]|  5.3| [5.4,29.9,9.4]|
| [7.8,38.9,50.6]|  6.6| [7.8,38.9,50.6]|
| [17.2,45.9,69.3]| 9.3|[17.2,45.9,69.3]|
| [18.7,12.1,23.4]| 6.7|[18.7,12.1,23.4]|
+-----+-----+
only showing top 5 rows
```

7. Fit Decision Tree Regression Model

```
from pyspark.ml.regression import DecisionTreeRegressor

# Train a DecisionTree model.
dt = DecisionTreeRegressor(featuresCol="indexedFeatures")
```

8. Pipeline Architecture

```
# Chain indexer and tree in a Pipeline
pipeline = Pipeline(stages=[featureIndexer, dt])

model = pipeline.fit(trainingData)
```

9. Make predictions

```
# Make predictions.
predictions = model.transform(testData)
```

```
# Select example rows to display.
predictions.select("features", "label", "predictedLabel").show(5)
```

```
+-----+-----+
|prediction|label|      features|
+-----+-----+
|       7.2|  1.6| [0.7,39.6,8.7]|
|       7.3|  5.3| [5.4,29.9,9.4]|
|       7.2|  6.6| [7.8,38.9,50.6]|
|      8.64| 9.3|[17.2,45.9,69.3]|
+-----+-----+
```

(continues on next page)

(continued from previous page)

```
|      6.45|   6.7|[18.7,12.1,23.4]|
+-----+-----+
only showing top 5 rows
```

10. Evaluation

```
from pyspark.ml.evaluation import RegressionEvaluator
from pyspark.ml.evaluation import RegressionEvaluator
# Select (prediction, true label) and compute test error
evaluator = RegressionEvaluator(labelCol="label",
                                 predictionCol="prediction",
                                 metricName="rmse")

rmse = evaluator.evaluate(predictions)
print("Root Mean Squared Error (RMSE) on test data = %g" % rmse)
```

The final Root Mean Squared Error (RMSE) is as follows:

```
Root Mean Squared Error (RMSE) on test data = 1.50999
```

```
y_true = predictions.select("label").toPandas()
y_pred = predictions.select("prediction").toPandas()

import sklearn.metrics
r2_score = sklearn.metrics.r2_score(y_true, y_pred)
print('r2_score: {}'.format(r2_score))
```

Then you will get the R^2 value:

```
r2_score: 0.911024318967
```

You may also check the importance of the features:

```
model.stages[1].featureImportances
```

The you will get the weight for each features

```
SparseVector(3, {0: 0.6811, 1: 0.3187, 2: 0.0002})
```

8.4 Random Forest Regression

8.4.1 Introduction

8.4.2 How to solve it?

8.4.3 Demo

- The Jupyter notebook can be download from Random Forest Regression.

- For more details about the parameters, please visit [Random Forest Regressor API](#).

1. Set up spark context and SparkSession

```
from pyspark.sql import SparkSession

spark = SparkSession \
    .builder \
    .appName("Python Spark RandomForest Regression example") \
    .config("spark.some.config.option", "some-value") \
    .getOrCreate()
```

2. Load dataset

```
df = spark.read.format('com.databricks.spark.csv') \
    .options(header='true', \
    inferSchema='true') \
    .load("../data/Advertising.csv", header=True);

df.show(5, True)
df.printSchema()
```

```
+---+---+---+---+
| TV|Radio|Newspaper|Sales|
+---+---+---+---+
| 230.1| 37.8| 69.2| 22.1|
| 44.5| 39.3| 45.1| 10.4|
| 17.2| 45.9| 69.3| 9.3|
| 151.5| 41.3| 58.5| 18.5|
| 180.8| 10.8| 58.4| 12.9|
+---+---+---+---+
only showing top 5 rows

root
|-- TV: double (nullable = true)
|-- Radio: double (nullable = true)
|-- Newspaper: double (nullable = true)
|-- Sales: double (nullable = true)
```

```
df.describe().show()

+-----+-----+-----+-----+
|summary|          TV|        Radio|      Newspaper|
|Sales|          200|          200|          200|
+-----+-----+-----+-----+
|  count|          200|          200|          200|
|  mean| 147.0425| 23.26400000000024| 30.55399999999995|
| stddev| 85.85423631490805| 14.846809176168728| 21.77862083852283|
|  stdDev| 217456565710477|
```

(continues on next page)

(continued from previous page)

min	0.7	0.0	0.3	
↪ 1.6				↪
max	296.4	49.6	114.0	↪
↪ 27.0				↪
+-----+	+-----+	+-----+	+-----+	
↪-----+				

3. Convert the data to dense vector (**features** and **label**)

Note: You are strongly encouraged to try my `get_dummy` function for dealing with the categorical data in comple dataset.

Supervised learning version:

```
def get_dummy(df, indexCol, categoricalCols, continuousCols, labelCol):

    from pyspark.ml import Pipeline
    from pyspark.ml.feature import StringIndexer, OneHotEncoder,
    ↪VectorAssembler
    from pyspark.sql.functions import col

    indexers = [ StringIndexer(inputCol=c, outputCol="{0}_indexed".
    ↪format(c))
        for c in categoricalCols ]

    # default setting: dropLast=True
    encoders = [ OneHotEncoder(inputCol=indexer.getOutputCol(),
        outputCol="{0}_encoded".format(indexer.
    ↪getOutputCol()))
        for indexer in indexers ]

    assembler = VectorAssembler(inputCols=[encoder.getOutputCol() ↪
    ↪for encoder in encoders]
        + continuousCols, outputCol="features"
    ↪"})

    pipeline = Pipeline(stages=indexers + encoders + [assembler])

    model=pipeline.fit(df)
    data = model.transform(df)

    data = data.withColumn('label', col(labelCol))

    return data.select(indexCol, 'features', 'label')
```

Unsupervised learning version:

```
def get_dummy(df, indexCol, categoricalCols, continuousCols):
    '''

    Get dummy variables and concat with continuous variables for
    ↪unsupervised learning.
```

(continues on next page)

(continued from previous page)

```

:param df: the dataframe
:param categoricalCols: the name list of the categorical data
:param continuousCols: the name list of the numerical data
:return k: feature matrix

:author: Wenqiang Feng
:email: von198@gmail.com
'''

indexers = [ StringIndexer(inputCol=c, outputCol="{0}_indexed".
format(c))
             for c in categoricalCols ]

# default setting: dropLast=True
encoders = [ OneHotEncoder(inputCol=indexer.getOutputCol(),
                            outputCol="{0}_encoded".format(indexer.
getOutputCol()))
             for indexer in indexers ]

assembler = VectorAssembler(inputCols=[encoder.getOutputCol()].
for encoder in encoders]
                           + continuousCols, outputCol="features"
)

pipeline = Pipeline(stages=indexers + encoders + [assembler])

model=pipeline.fit(df)
data = model.transform(df)

return data.select(indexCol,'features')

```

```

from pyspark.sql import Row
from pyspark.ml.linalg import Vectors

# convert the data to dense vector
#def transData(row):
#    return Row(label=row["Sales"],
#               features=Vectors.dense([row["TV"],
#                                      row["Radio"],
#                                      row["Newspaper"]]))
def transData(data):
    return data.rdd.map(lambda r: [Vectors.dense(r[:-1]), r[-1]]).toDF([
        'features', 'label'])

```

4. Convert the data to dense vector

```

transformed= transData(df)
transformed.show(5)

```

```
+-----+-----+
|       features|label|
+-----+-----+
| [230.1,37.8,69.2]| 22.1 |
| [44.5,39.3,45.1]| 10.4 |
| [17.2,45.9,69.3]|  9.3 |
| [151.5,41.3,58.5]| 18.5 |
| [180.8,10.8,58.4]| 12.9 |
+-----+-----+
only showing top 5 rows
```

5. Deal with the Categorical variables

```
from pyspark.ml import Pipeline
from pyspark.ml.regression import LinearRegression
from pyspark.ml.feature import VectorIndexer
from pyspark.ml.evaluation import RegressionEvaluator

featureIndexer = VectorIndexer(inputCol="features", \
                                outputCol="indexedFeatures", \
                                maxCategories=4).fit(transformed)

data = featureIndexer.transform(transformed)
data.show(5, True)
```

```
+-----+-----+-----+
|       features|label| indexedFeatures|
+-----+-----+-----+
| [230.1,37.8,69.2]| 22.1|[230.1,37.8,69.2]|
| [44.5,39.3,45.1]| 10.4|[44.5,39.3,45.1]|
| [17.2,45.9,69.3]|  9.3|[17.2,45.9,69.3]|
| [151.5,41.3,58.5]| 18.5|[151.5,41.3,58.5]|
| [180.8,10.8,58.4]| 12.9|[180.8,10.8,58.4]|
+-----+-----+-----+
only showing top 5 rows
```

6. Split the data into training and test sets (40% held out for testing)

```
# Split the data into training and test sets (40% held out for testing)
(trainingData, testData) = data.randomSplit([0.6, 0.4])

trainingData.show(5)
testData.show(5)
```

```
+-----+-----+-----+
|       features|label| indexedFeatures|
+-----+-----+-----+
| [0.7,39.6,8.7]| 1.6|[0.7,39.6,8.7]|
| [8.6,2.1,1.0]| 4.8|[8.6,2.1,1.0]|
| [8.7,48.9,75.0]| 7.2|[8.7,48.9,75.0]|
| [11.7,36.9,45.2]| 7.3|[11.7,36.9,45.2]|
+-----+-----+-----+
```

(continues on next page)

(continued from previous page)

```
| [13.2,15.9,49.6] | 5.6| [13.2,15.9,49.6] |
+-----+-----+
only showing top 5 rows

+-----+-----+
|      features|label|indexedFeatures|
+-----+-----+
| [4.1,11.6,5.7]| 3.2| [4.1,11.6,5.7] |
| [5.4,29.9,9.4]| 5.3| [5.4,29.9,9.4] |
| [7.3,28.1,41.4]| 5.5|[7.3,28.1,41.4] |
| [7.8,38.9,50.6]| 6.6|[7.8,38.9,50.6] |
| [8.4,27.2,2.1]| 5.7|[8.4,27.2,2.1] |
+-----+-----+
only showing top 5 rows
```

7. Fit RandomForest Regression Model

```
# Import LinearRegression class
from pyspark.ml.regression import RandomForestRegressor

# Define LinearRegression algorithm
rf = RandomForestRegressor() # featuresCol="indexedFeatures", numTrees=2,
                           ↴maxDepth=2, seed=42
```

Note: If you decide to use the indexedFeatures features, you need to add the parameter featuresCol="indexedFeatures".

8. Pipeline Architecture

```
# Chain indexer and tree in a Pipeline
pipeline = Pipeline(stages=[featureIndexer, rf])
model = pipeline.fit(trainingData)
```

9. Make predictions

```
predictions = model.transform(testData)

# Select example rows to display.
predictions.select("features", "label", "prediction").show(5)
```

```
+-----+-----+
|      features|label|      prediction|
+-----+-----+
| [4.1,11.6,5.7]| 3.2| 8.155439814814816|
| [5.4,29.9,9.4]| 5.3|10.412769901394899|
| [7.3,28.1,41.4]| 5.5| 12.13735648148148|
| [7.8,38.9,50.6]| 6.6|11.321796703296704|
| [8.4,27.2,2.1]| 5.7|12.071421957671957|
```

(continues on next page)

(continued from previous page)

```
+-----+-----+
only showing top 5 rows
```

10. Evaluation

```
# Select (prediction, true label) and compute test error
evaluator = RegressionEvaluator(
    labelCol="label", predictionCol="prediction", metricName="rmse")
rmse = evaluator.evaluate(predictions)
print("Root Mean Squared Error (RMSE) on test data = %g" % rmse)
```

```
Root Mean Squared Error (RMSE) on test data = 2.35912
```

```
import sklearn.metrics
r2_score = sklearn.metrics.r2_score(y_true, y_pred)
print('r2_score: {:.4f}'.format(r2_score))
```

```
r2_score: 0.831
```

11. Feature importances

```
model.stages[-1].featureImportances
```

```
SparseVector(3, {0: 0.4994, 1: 0.3196, 2: 0.181})
```

```
model.stages[-1].trees
```

```
[DecisionTreeRegressionModel (uid=dtr_c75f1c75442c) of depth 5 with 43 nodes,
 DecisionTreeRegressionModel (uid=dtr_70fc2d441581) of depth 5 with 45 nodes,
 DecisionTreeRegressionModel (uid=dtr_bc8464f545a7) of depth 5 with 31 nodes,
 DecisionTreeRegressionModel (uid=dtr_a8a7e5367154) of depth 5 with 59 nodes,
 DecisionTreeRegressionModel (uid=dtr_3ea01314fcbc) of depth 5 with 47 nodes,
 DecisionTreeRegressionModel (uid=dtr_be9a04ac22a6) of depth 5 with 45 nodes,
 DecisionTreeRegressionModel (uid=dtr_38610d47328a) of depth 5 with 51 nodes,
 DecisionTreeRegressionModel (uid=dtr_bf14aea0ad3b) of depth 5 with 49 nodes,
 DecisionTreeRegressionModel (uid=dtr_cde24ebd6bb6) of depth 5 with 39 nodes,
 DecisionTreeRegressionModel (uid=dtr_a1fc9bd4fbe) of depth 5 with 57 nodes,
 DecisionTreeRegressionModel (uid=dtr_37798d6db1ba) of depth 5 with 41 nodes,
 DecisionTreeRegressionModel (uid=dtr_c078b73ada63) of depth 5 with 41 nodes,
 DecisionTreeRegressionModel (uid=dtr_fd00e3a070ad) of depth 5 with 55 nodes,
 DecisionTreeRegressionModel (uid=dtr_9d01d5fb8604) of depth 5 with 45 nodes,
 DecisionTreeRegressionModel (uid=dtr_8bd8bdddf642) of depth 5 with 41 nodes,
 DecisionTreeRegressionModel (uid=dtr_e53b7bae30f8) of depth 5 with 49 nodes,
 DecisionTreeRegressionModel (uid=dtr_808a869db21c) of depth 5 with 47 nodes,
 DecisionTreeRegressionModel (uid=dtr_64d0916bceb0) of depth 5 with 33 nodes,
 DecisionTreeRegressionModel (uid=dtr_0891055fff94) of depth 5 with 55 nodes,
 DecisionTreeRegressionModel (uid=dtr_19c8bbad26c2) of depth 5 with 51 nodes]
```

8.5 Gradient-boosted tree regression

8.5.1 Introduction

8.5.2 How to solve it?

8.5.3 Demo

- The Jupyter notebook can be download from [Gradient-boosted tree regression](#).
 - For more details about the parameters, please visit [Gradient boosted tree API](#) .
1. Set up spark context and SparkSession

```
from pyspark.sql import SparkSession

spark = SparkSession \
    .builder \
    .appName("Python Spark GBTRegressor example") \
    .config("spark.some.config.option", "some-value") \
    .getOrCreate()
```

2. Load dataset

```
df = spark.read.format('com.databricks.spark.csv') \
    .options(header='true', \
    inferSchema='true') \
    .load("../data/Advertising.csv", header=True);

df.show(5, True)
df.printSchema()
```

```
+----+-----+-----+-----+
|    TV|Radio|Newspaper|Sales|
+----+-----+-----+-----+
| 230.1| 37.8|     69.2|  22.1|
|   44.5| 39.3|     45.1| 10.4|
|   17.2| 45.9|     69.3|   9.3|
| 151.5| 41.3|     58.5| 18.5|
| 180.8| 10.8|     58.4| 12.9|
+----+-----+-----+-----+
only showing top 5 rows

root
 |-- TV: double (nullable = true)
 |-- Radio: double (nullable = true)
 |-- Newspaper: double (nullable = true)
 |-- Sales: double (nullable = true)
```

```
df.describe().show()
```

(continues on next page)

(continued from previous page)

summary	TV	Radio	Newspaper	
↳ Sales				↳
↳ count	200	200	200	↳
↳ 200				↳
↳ mean	147.0425	23.26400000000024	30.553999999999995	14.
↳ 02250000000003				
↳ stddev	85.85423631490805	14.846809176168728	21.77862083852283	5.
↳ 217456565710477				
↳ min	0.7	0.0	0.3	↳
↳ 1.6				↳
↳ max	296.4	49.6	114.0	↳
↳ 27.0				↳
↳				

3. Convert the data to dense vector (**features** and **label**)

Note: You are strongly encouraged to try my `get_dummy` function for dealing with the categorical data in comple dataset.

Supervised learning version:

```
def get_dummy(df, indexCol, categoricalCols, continuousCols, labelCol):
    from pyspark.ml import Pipeline
    from pyspark.ml.feature import StringIndexer, OneHotEncoder,
    ↳ VectorAssembler
    from pyspark.sql.functions import col

    indexers = [ StringIndexer(inputCol=c, outputCol="{0}_indexed".
    ↳ format(c))
        for c in categoricalCols ]

    # default setting: dropLast=True
    encoders = [ OneHotEncoder(inputCol=indexer.getOutputCol(),
        outputCol="{0}_encoded".format(indexer.
    ↳ getOutputCol()))
        for indexer in indexers ]

    assembler = VectorAssembler(inputCols=[encoder.getOutputCol() ↳
    ↳ for encoder in encoders]
        + continuousCols, outputCol="features"
    ↳ "")

    pipeline = Pipeline(stages=indexers + encoders + [assembler])

    model=pipeline.fit(df)
```

(continues on next page)

(continued from previous page)

```

data = model.transform(df)

data = data.withColumn('label', col(labelCol))

return data.select(indexCol, 'features', 'label')

```

Unsupervised learning version:

```

def get_dummy(df, indexCol, categoricalCols, continuousCols):
    """
    Get dummy variables and concat with continuous variables for
    ↪unsupervised learning.
    :param df: the dataframe
    :param categoricalCols: the name list of the categorical data
    :param continuousCols: the name list of the numerical data
    :return k: feature matrix

    :author: Wenqiang Feng
    :email: von198@gmail.com
    """

    indexers = [ StringIndexer(inputCol=c, outputCol="{0}_indexed".
    ↪format(c))
        for c in categoricalCols ]

    # default setting: dropLast=True
    encoders = [ OneHotEncoder(inputCol=indexer.getOutputCol(),
                                outputCol="{0}_encoded".format(indexer.
    ↪getOutputCol()))
        for indexer in indexers ]

    assembler = VectorAssembler(inputCols=[encoder.getOutputCol() ↪
    ↪for encoder in encoders]
                                + continuousCols, outputCol="features"
    ↪" )

    pipeline = Pipeline(stages=indexers + encoders + [assembler])

    model=pipeline.fit(df)
    data = model.transform(df)

    return data.select(indexCol, 'features')

```

```

from pyspark.sql import Row
from pyspark.ml.linalg import Vectors

# convert the data to dense vector
#def transData(row):
#    return Row(label=row["Sales"],
#               features=Vectors.dense([row["TV"]]),

```

(continues on next page)

(continued from previous page)

```
#           row["Radio"],
#           row["Newspaper"])))
def transData(data):
    return data.rdd.map(lambda r: [Vectors.dense(r[:-1]),r[-1]]).toDF([
    'features','label'])
```

4. Convert the data to dense vector

```
transformed= transData(df)
transformed.show(5)
```

```
+-----+-----+
|      features|label |
+-----+-----+
| [230.1,37.8,69.2]| 22.1 |
| [44.5,39.3,45.1]| 10.4 |
| [17.2,45.9,69.3]|  9.3 |
| [151.5,41.3,58.5]| 18.5 |
| [180.8,10.8,58.4]| 12.9 |
+-----+-----+
only showing top 5 rows
```

5. Deal with the Categorical variables

```
from pyspark.ml import Pipeline
from pyspark.ml.regression import GBTRRegressor
from pyspark.ml.feature import VectorIndexer
from pyspark.ml.evaluation import RegressionEvaluator

featureIndexer = VectorIndexer(inputCol="features", \
                                outputCol="indexedFeatures", \
                                maxCategories=4).fit(transformed)

data = featureIndexer.transform(transformed)
data.show(5, True)
```

```
+-----+-----+-----+
|      features|label| indexedFeatures |
+-----+-----+-----+
| [230.1,37.8,69.2]| 22.1|[230.1,37.8,69.2] |
| [44.5,39.3,45.1]| 10.4|[44.5,39.3,45.1] |
| [17.2,45.9,69.3]|  9.3|[17.2,45.9,69.3] |
| [151.5,41.3,58.5]| 18.5|[151.5,41.3,58.5] |
| [180.8,10.8,58.4]| 12.9|[180.8,10.8,58.4] |
+-----+-----+-----+
only showing top 5 rows
```

6. Split the data into training and test sets (40% held out for testing)

```
# Split the data into training and test sets (40% held out for testing)
(trainingData, testData) = data.randomSplit([0.6, 0.4])
```

(continues on next page)

(continued from previous page)

```
trainingData.show(5)
testData.show(5)
```

```
+-----+-----+
|      features|label| indexedFeatures|
+-----+-----+
| [0.7,39.6,8.7]| 1.6| [0.7,39.6,8.7]|
| [8.6,2.1,1.0]| 4.8| [8.6,2.1,1.0]|
| [8.7,48.9,75.0]| 7.2| [8.7,48.9,75.0]|
| [11.7,36.9,45.2]| 7.3|[11.7,36.9,45.2]|
| [13.2,15.9,49.6]| 5.6|[13.2,15.9,49.6]|
+-----+-----+
only showing top 5 rows
```

```
+-----+-----+
|      features|label|indexedFeatures|
+-----+-----+
| [4.1,11.6,5.7]| 3.2| [4.1,11.6,5.7]|
| [5.4,29.9,9.4]| 5.3| [5.4,29.9,9.4]|
| [7.3,28.1,41.4]| 5.5|[7.3,28.1,41.4]|
| [7.8,38.9,50.6]| 6.6|[7.8,38.9,50.6]|
| [8.4,27.2,2.1]| 5.7|[8.4,27.2,2.1]|
+-----+-----+
only showing top 5 rows
```

7. Fit RandomForest Regression Model

```
# Import LinearRegression class
from pyspark.ml.regression import GBTRegressor

# Define LinearRegression algorithm
rf = GBTRegressor() #numTrees=2, maxDepth=2, seed=42
```

Note: If you decide to use the indexedFeatures features, you need to add the parameter featuresCol="indexedFeatures".

8. Pipeline Architecture

```
# Chain indexer and tree in a Pipeline
pipeline = Pipeline(stages=[featureIndexer, rf])
model = pipeline.fit(trainingData)
```

9. Make predictions

```
predictions = model.transform(testData)

# Select example rows to display.
predictions.select("features", "label", "prediction").show(5)
```

```
+-----+-----+-----+
|      features|label|      prediction|
+-----+-----+-----+
| [7.8,38.9,50.6]| 6.6| 6.836040343319862|
| [8.6,2.1,1.0]| 4.8| 5.652202764688849|
| [8.7,48.9,75.0]| 7.2| 6.908750296855572|
| [13.1,0.4,25.6]| 5.3| 5.784020210692574|
| [19.6,20.1,17.0]| 7.6| 6.8678921062629295|
+-----+-----+-----+
only showing top 5 rows
```

10. Evaluation

```
# Select (prediction, true label) and compute test error
evaluator = RegressionEvaluator(
    labelCol="label", predictionCol="prediction", metricName="rmse")
rmse = evaluator.evaluate(predictions)
print("Root Mean Squared Error (RMSE) on test data = %g" % rmse)
```

```
Root Mean Squared Error (RMSE) on test data = 1.36939
```

```
import sklearn.metrics
r2_score = sklearn.metrics.r2_score(y_true, y_pred)
print('r2_score: {:.4f}'.format(r2_score))
```

```
r2_score: 0.932
```

11. Feature importances

```
model.stages[-1].featureImportances
```

```
SparseVector(3, {0: 0.3716, 1: 0.3525, 2: 0.2759})
```

```
model.stages[-1].trees
```

```
[DecisionTreeRegressionModel (uid=dtr_7f5cd2ef7cb6) of depth 5 with 61 nodes,
 DecisionTreeRegressionModel (uid=dtr_ef3ab6baeac9) of depth 5 with 39 nodes,
 DecisionTreeRegressionModel (uid=dtr_07c6e3cf3819) of depth 5 with 45 nodes,
 DecisionTreeRegressionModel (uid=dtr_ce724af79a2b) of depth 5 with 47 nodes,
 DecisionTreeRegressionModel (uid=dtr_d149ecc71658) of depth 5 with 55 nodes,
 DecisionTreeRegressionModel (uid=dtr_d3a79bdea516) of depth 5 with 43 nodes,
 DecisionTreeRegressionModel (uid=dtr_7abc1a337844) of depth 5 with 51 nodes,
 DecisionTreeRegressionModel (uid=dtr_480834b46d8f) of depth 5 with 33 nodes,
 DecisionTreeRegressionModel (uid=dtr_0cbd1eaaa3874) of depth 5 with 39 nodes,
 DecisionTreeRegressionModel (uid=dtr_8088ac71a204) of depth 5 with 57 nodes,
 DecisionTreeRegressionModel (uid=dtr_2ceb9e8deb45) of depth 5 with 47 nodes,
 DecisionTreeRegressionModel (uid=dtr_cc334e84e9a2) of depth 5 with 57 nodes,
 DecisionTreeRegressionModel (uid=dtr_a665c562929e) of depth 5 with 41 nodes,
 DecisionTreeRegressionModel (uid=dtr_2999b1ffd2dc) of depth 5 with 45 nodes,
 DecisionTreeRegressionModel (uid=dtr_29965cbe8cfcc) of depth 5 with 55 nodes,
```

(continues on next page)

(continued from previous page)

```
DecisionTreeRegressionModel (uid=dtr_731df51bf0ad) of depth 5 with 41 nodes,  
DecisionTreeRegressionModel (uid=dtr_354cf33424da) of depth 5 with 51 nodes,  
DecisionTreeRegressionModel (uid=dtr_4230f200b1c0) of depth 5 with 41 nodes,  
DecisionTreeRegressionModel (uid=dtr_3279cdc1ce1d) of depth 5 with 45 nodes,  
DecisionTreeRegressionModel (uid=dtr_f474a99ff06e) of depth 5 with 55 nodes]
```


REGULARIZATION

In mathematics, statistics, and computer science, particularly in the fields of machine learning and inverse problems, regularization is a process of introducing additional information in order to solve an ill-posed problem or to prevent overfitting ([Wikipedia Regularization](#)).

Due to the sparsity within our data, our training sets will often be ill-posed (singular). Applying regularization to the regression has many advantages, including:

1. Converting ill-posed problems to well-posed by adding additional information via the penalty parameter λ
2. Preventing overfitting
3. Variable selection and the removal of correlated variables ([Glmnet Vignette](#)). The Ridge method shrinks the coefficients of correlated variables while the LASSO method picks one variable and discards the others. The elastic net penalty is a mixture of these two; if variables are correlated in groups then $\alpha = 0.5$ tends to select the groups as in or out. If α is close to 1, the elastic net performs much like the LASSO method and removes any degeneracies and wild behavior caused by extreme correlations.

9.1 Ordinary least squares regression

$$\min_{\beta \in \mathbb{R}^n} \frac{1}{n} \|\mathbf{X}\beta - \mathbf{y}\|^2$$

When $\lambda = 0$ (i.e. `regParam = 0`), then there is no penalty.

```
LinearRegression(featuresCol="features", labelCol="label", predictionCol=
  "prediction", maxIter=100,
  regParam=0.0, elasticNetParam=0.0, tol=1e-6, fitIntercept=True,
  standardization=True, solver="auto",
  weightCol=None, aggregationDepth=2)
```

9.2 Ridge regression

$$\min_{\beta \in \mathbb{R}^n} \frac{1}{n} \|\mathbf{X}\beta - \mathbf{y}\|^2 + \lambda \|\beta\|_2^2$$

When $\lambda > 0$ (i.e. `regParam > 0`) and $\alpha = 0$ (i.e. `elasticNetParam = 0`) , then the penalty is an L2 penalty.

```
LinearRegression(featuresCol="features", labelCol="label", predictionCol=
    "prediction", maxIter=100,
    regParam=0.1, elasticNetParam=0.0, tol=1e-6, fitIntercept=True,_
    standardization=True, solver="auto",
    weightCol=None, aggregationDepth=2)
```

9.3 Least Absolute Shrinkage and Selection Operator (LASSO)

$$\min_{\beta \in \mathbb{R}^n} \frac{1}{n} \|\mathbf{X}\beta - \mathbf{y}\|^2 + \lambda \|\beta\|_1$$

When $\lambda > 0$ (i.e. `regParam > 0`) and $\alpha = 1$ (i.e. `elasticNetParam = 1`), then the penalty is an L1 penalty.

```
LinearRegression(featuresCol="features", labelCol="label", predictionCol=
    "prediction", maxIter=100,
    regParam=0.0, elasticNetParam=0.0, tol=1e-6, fitIntercept=True,_
    standardization=True, solver="auto",
    weightCol=None, aggregationDepth=2)
```

9.4 Elastic net

$$\min_{\beta \in \mathbb{R}^n} \frac{1}{n} \|\mathbf{X}\beta - \mathbf{y}\|^2 + \lambda(\alpha \|\beta\|_1 + (1 - \alpha) \|\beta\|_2^2), \alpha \in (0, 1)$$

When $\lambda > 0$ (i.e. `regParam > 0`) and `elasticNetParam ∈ (0, 1)` (i.e. $\alpha \in (0, 1)$) , then the penalty is an L1 + L2 penalty.

```
LinearRegression(featuresCol="features", labelCol="label", predictionCol=
    "prediction", maxIter=100,
    regParam=0.0, elasticNetParam=0.0, tol=1e-6, fitIntercept=True,_
    standardization=True, solver="auto",
    weightCol=None, aggregationDepth=2)
```

CLASSIFICATION

Chinese proverb

Birds of a feather flock together. – old Chinese proverb

10.1 Binomial logistic regression

10.1.1 Introduction

10.1.2 Demo

- The Jupyter notebook can be download from [Logistic Regression](#).
- For more details, please visit [Logistic Regression API](#) .

Note: In this demo, I introduced a new function `get_dummy` to deal with the categorical data. I highly recommend you to use my `get_dummy` function in the other cases. This function will save a lot of time for you.

1. Set up spark context and SparkSession

```
from pyspark.sql import SparkSession

spark = SparkSession \
    .builder \
    .appName("Python Spark Logistic Regression example") \
    .config("spark.some.config.option", "some-value") \
    .getOrCreate()
```

2. Load dataset

```
df = spark.read.format('com.databricks.spark.csv') \
    .options(header='true', inferschema='true') \
```

(continues on next page)

(continued from previous page)

```
.load("./data/bank.csv", header=True);
df.drop('day', 'month', 'poutcome').show(5)
```

```
+---+-----+-----+-----+-----+-----+-----+-----+
|age|  
|job|marital|education|default|balance|housing|loan|contact|duration|campaign|pdays|previous|  
|y|  
+---+-----+-----+-----+-----+-----+-----+-----+  
| 58| management|married| tertiary| no| 2143| yes| no|unknown|  
| 261| 1| -1| 0| no|  
| 44| technician| single|secondary| no| 29| yes| no|unknown|  
| 151| 1| -1| 0| no|  
| 33|entrepreneur|married|secondary| no| 2| yes| yes|unknown|  
| 76| 1| -1| 0| no|  
| 47| blue-collar|married| unknown| no| 1506| yes| no|unknown|  
| 92| 1| -1| 0| no|  
| 33| unknown| single| unknown| no| 1| no| no|unknown|  
| 198| 1| -1| 0| no|  
+---+-----+-----+-----+-----+-----+-----+  
only showing top 5 rows
```

```
df.printSchema()
```

```
root
|-- age: integer (nullable = true)
|-- job: string (nullable = true)
|-- marital: string (nullable = true)
|-- education: string (nullable = true)
|-- default: string (nullable = true)
|-- balance: integer (nullable = true)
|-- housing: string (nullable = true)
|-- loan: string (nullable = true)
|-- contact: string (nullable = true)
|-- day: integer (nullable = true)
|-- month: string (nullable = true)
|-- duration: integer (nullable = true)
|-- campaign: integer (nullable = true)
|-- pdays: integer (nullable = true)
|-- previous: integer (nullable = true)
|-- poutcome: string (nullable = true)
|-- y: string (nullable = true)
```

Note: You are strongly encouraged to try my `get_dummy` function for dealing with the categorical data in complex dataset.

Supervised learning version:

```

def get_dummy(df,indexCol,categoricalCols,continuousCols,labelCol):

    from pyspark.ml import Pipeline
    from pyspark.ml.feature import StringIndexer, OneHotEncoder,
    ↪VectorAssembler
    from pyspark.sql.functions import col

    indexers = [ StringIndexer(inputCol=c, outputCol="{0}_indexed".
    ↪format(c))
        for c in categoricalCols ]

    # default setting: dropLast=True
    encoders = [ OneHotEncoder(inputCol=indexer.getOutputCol(),
        outputCol="{0}_encoded".format(indexer.
    ↪getOutputCol()))
        for indexer in indexers ]

    assembler = VectorAssembler(inputCols=[encoder.getOutputCol()].
    ↪for encoder in encoders]
        + continuousCols, outputCol="features"
    ↪)

    pipeline = Pipeline(stages=indexers + encoders + [assembler])

    model=pipeline.fit(df)
    data = model.transform(df)

    data = data.withColumn('label',col(labelCol))

    return data.select(indexCol,'features','label')

```

Unsupervised learning version:

```

def get_dummy(df,indexCol,categoricalCols,continuousCols):
    '''
        Get dummy variables and concat with continuous variables for
    ↪unsupervised learning.
        :param df: the dataframe
        :param categoricalCols: the name list of the categorical data
        :param continuousCols: the name list of the numerical data
        :return k: feature matrix

        :author: Wenqiang Feng
        :email: von198@gmail.com
    '''

    indexers = [ StringIndexer(inputCol=c, outputCol="{0}_indexed".
    ↪format(c))
        for c in categoricalCols ]

    # default setting: dropLast=True
    encoders = [ OneHotEncoder(inputCol=indexer.getOutputCol(),
        outputCol="{0}_encoded".format(indexer.
    ↪getOutputCol()))
        for indexer in indexers ]

```

(continues on next page)

(continued from previous page)

```

        outputCol="{0}_encoded".format(indexer.
→getOutputCol()))
    for indexer in indexers ]

    assembler = VectorAssembler(inputCols=[encoder.getOutputCol()_
→for encoder in encoders]
                                + continuousCols, outputCol="features"
→" )

    pipeline = Pipeline(stages=indexers + encoders + [assembler])

    model=pipeline.fit(df)
    data = model.transform(df)

    return data.select(indexCol,'features')

```

```

def get_dummy(df,categoricalCols,continuousCols,labelCol):

    from pyspark.ml import Pipeline
    from pyspark.ml.feature import StringIndexer, OneHotEncoder,
→VectorAssembler
    from pyspark.sql.functions import col

    indexers = [ StringIndexer(inputCol=c, outputCol="{0}_indexed".format(c))
                for c in categoricalCols ]

    # default setting: dropLast=True
    encoders = [ OneHotEncoder(inputCol=indexer.getOutputCol(),
                               outputCol="{0}_encoded".format(indexer.getOutputCol()))
                for indexer in indexers ]

    assembler = VectorAssembler(inputCols=[encoder.getOutputCol() for encoder_
→in encoders]
                                + continuousCols, outputCol="features")

    pipeline = Pipeline(stages=indexers + encoders + [assembler])

    model=pipeline.fit(df)
    data = model.transform(df)

    data = data.withColumn('label',col(labelCol))

    return data.select('features','label')

```

3. Deal with categorical data and Convert the data to dense vector

```

catcols = ['job','marital','education','default',
           'housing','loan','contact','poutcome']

num_cols = ['balance', 'duration', 'campaign','pdays','previous',]

```

(continues on next page)

(continued from previous page)

```
labelCol = 'y'

data = get_dummy(df, catcols, num_cols, labelCol)
data.show(5)
```

```
+-----+-----+
|       features|label|
+-----+-----+
| (29, [1,11,14,16,1...| no |
| (29, [2,12,13,16,1...| no |
| (29, [7,11,13,16,1...| no |
| (29, [0,11,16,17,1...| no |
| (29, [12,16,18,20,...| no |
+-----+-----+
only showing top 5 rows
```

4. Deal with Categorical Label and Variables

```
from pyspark.ml.feature import StringIndexer
# Index labels, adding metadata to the label column
labelIndexer = StringIndexer(inputCol='label',
                             outputCol='indexedLabel').fit(data)
labelIndexer.transform(data).show(5, True)
```

```
+-----+-----+-----+
|       features|label|indexedLabel|
+-----+-----+-----+
| (29, [1,11,14,16,1...| no | 0.0 |
| (29, [2,12,13,16,1...| no | 0.0 |
| (29, [7,11,13,16,1...| no | 0.0 |
| (29, [0,11,16,17,1...| no | 0.0 |
| (29, [12,16,18,20,...| no | 0.0 |
+-----+-----+-----+
only showing top 5 rows
```

```
from pyspark.ml.feature import VectorIndexer
# Automatically identify categorical features, and index them.
# Set maxCategories so features with > 4 distinct values are treated as
# continuous.
featureIndexer = VectorIndexer(inputCol="features", \
                                outputCol="indexedFeatures", \
                                maxCategories=4).fit(data)
featureIndexer.transform(data).show(5, True)
```

```
+-----+-----+-----+
|       features|label| indexedFeatures|
+-----+-----+-----+
| (29, [1,11,14,16,1...| no | (29, [1,11,14,16,1...|
| (29, [2,12,13,16,1...| no | (29, [2,12,13,16,1...|
| (29, [7,11,13,16,1...| no | (29, [7,11,13,16,1...|
```

(continues on next page)

(continued from previous page)

```
| (29, [0,11,16,17,1...|    no | (29, [0,11,16,17,1...|
| (29, [12,16,18,20,...|    no | (29, [12,16,18,20,...|
+-----+-----+-----+
only showing top 5 rows
```

5. Split the data to training and test data sets

```
# Split the data into training and test sets (40% held out for testing)
(trainingData, testData) = data.randomSplit([0.6, 0.4])

trainingData.show(5, False)
testData.show(5, False)
```

```
+-----+-----+
|features          |label|
```

```
+-----+-----+
| (29, [0,11,13,16,17,18,19,21,24,25,26,27], [1.0,1.0,1.0,1.0,1.0,1.0,1.0,1.0,-
| 731.0,401.0,4.0,-1.0]) |no   |
| (29, [0,11,13,16,17,18,19,21,24,25,26,27], [1.0,1.0,1.0,1.0,1.0,1.0,1.0,1.0,-
| 723.0,112.0,2.0,-1.0]) |no   |
| (29, [0,11,13,16,17,18,19,21,24,25,26,27], [1.0,1.0,1.0,1.0,1.0,1.0,1.0,1.0,-
| 626.0,205.0,1.0,-1.0]) |no   |
| (29, [0,11,13,16,17,18,19,21,24,25,26,27], [1.0,1.0,1.0,1.0,1.0,1.0,1.0,1.0,-
| 498.0,357.0,1.0,-1.0]) |no   |
| (29, [0,11,13,16,17,18,19,21,24,25,26,27], [1.0,1.0,1.0,1.0,1.0,1.0,1.0,1.0,-
| 477.0,473.0,2.0,-1.0]) |no   |
+-----+-----+
only showing top 5 rows
```



```
+-----+-----+
|features          |label|
```

```
+-----+-----+
| (29, [0,11,13,16,17,18,19,21,24,25,26,27], [1.0,1.0,1.0,1.0,1.0,1.0,1.0,1.0,-
| 648.0,280.0,2.0,-1.0]) |no   |
| (29, [0,11,13,16,17,18,19,21,24,25,26,27], [1.0,1.0,1.0,1.0,1.0,1.0,1.0,1.0,-
| 596.0,147.0,1.0,-1.0]) |no   |
| (29, [0,11,13,16,17,18,19,21,24,25,26,27], [1.0,1.0,1.0,1.0,1.0,1.0,1.0,1.0,-
| 529.0,416.0,4.0,-1.0]) |no   |
| (29, [0,11,13,16,17,18,19,21,24,25,26,27], [1.0,1.0,1.0,1.0,1.0,1.0,1.0,1.0,-
| 518.0,46.0,5.0,-1.0]) |no   |
| (29, [0,11,13,16,17,18,19,21,24,25,26,27], [1.0,1.0,1.0,1.0,1.0,1.0,1.0,1.0,-
| 470.0,275.0,2.0,-1.0]) |no   |
+-----+-----+
```

(continues on next page)

(continued from previous page)

```
only showing top 5 rows
```

6. Fit Logistic Regression Model

```
from pyspark.ml.classification import LogisticRegression
logr = LogisticRegression(featuresCol='indexedFeatures', labelCol=
    'indexedLabel')
```

7. Pipeline Architecture

```
# Convert indexed labels back to original labels.
labelConverter = IndexToString(inputCol="prediction", outputCol=
    "predictedLabel",
    labels=labelIndexer.labels)
```

```
# Chain indexers and tree in a Pipeline
pipeline = Pipeline(stages=[labelIndexer, featureIndexer, logr,
    labelConverter])
```

```
# Train model. This also runs the indexers.
model = pipeline.fit(trainingData)
```

8. Make predictions

```
# Make predictions.
predictions = model.transform(testData)
# Select example rows to display.
predictions.select("features", "label", "predictedLabel").show(5)
```

```
+-----+-----+-----+
|       features|label|predictedLabel|
+-----+-----+-----+
| (29, [0,11,13,16,1...| no|      no|
+-----+-----+-----+
only showing top 5 rows
```

9. Evaluation

```
from pyspark.ml.evaluation import MulticlassClassificationEvaluator

# Select (prediction, true label) and compute test error
evaluator = MulticlassClassificationEvaluator(
    labelCol="indexedLabel", predictionCol="prediction", metricName="accuracy")
accuracy = evaluator.evaluate(predictions)
print("Test Error = %g" % (1.0 - accuracy))
```

```
Test Error = 0.0987688
```

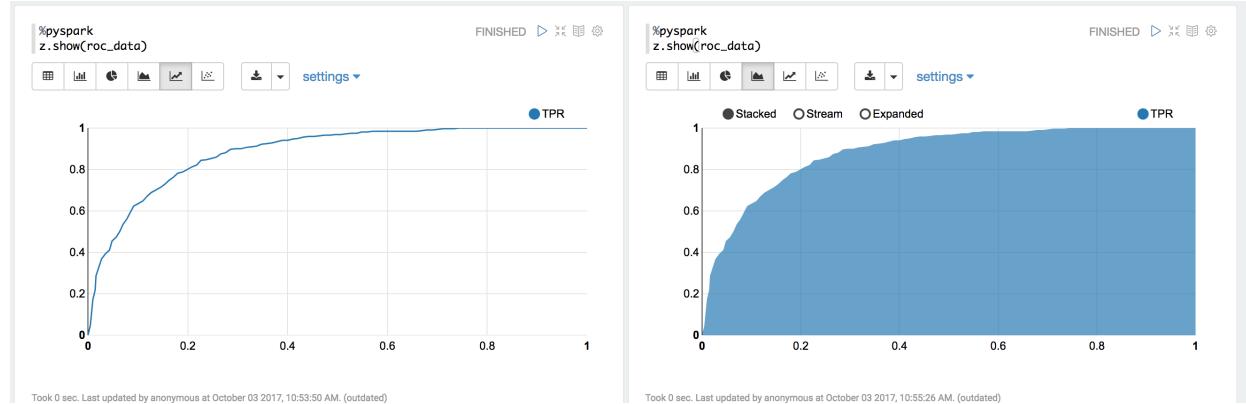
```
lrModel = model.stages[2]
trainingSummary = lrModel.summary

# Obtain the objective per iteration
# objectiveHistory = trainingSummary.objectiveHistory
# print("objectiveHistory:")
# for objective in objectiveHistory:
#     print(objective)

# Obtain the receiver-operating characteristic as a dataframe and
# areaUnderROC.
trainingSummary.roc.show(5)
print("areaUnderROC: " + str(trainingSummary.areaUnderROC))

# Set the model threshold to maximize F-Measure
fMeasure = trainingSummary.fMeasureByThreshold
maxFMeasure = fMeasure.groupBy().max('F-Measure').select('max(F-Measure)').head(5)
# bestThreshold = fMeasure.where(fMeasure['F-Measure'] == maxFMeasure['max(F-
# Measure)']) \
#     .select('threshold').head()['threshold']
# lr.setThreshold(bestThreshold)
```

You can use `z.show()` to get the data and plot the ROC curves:



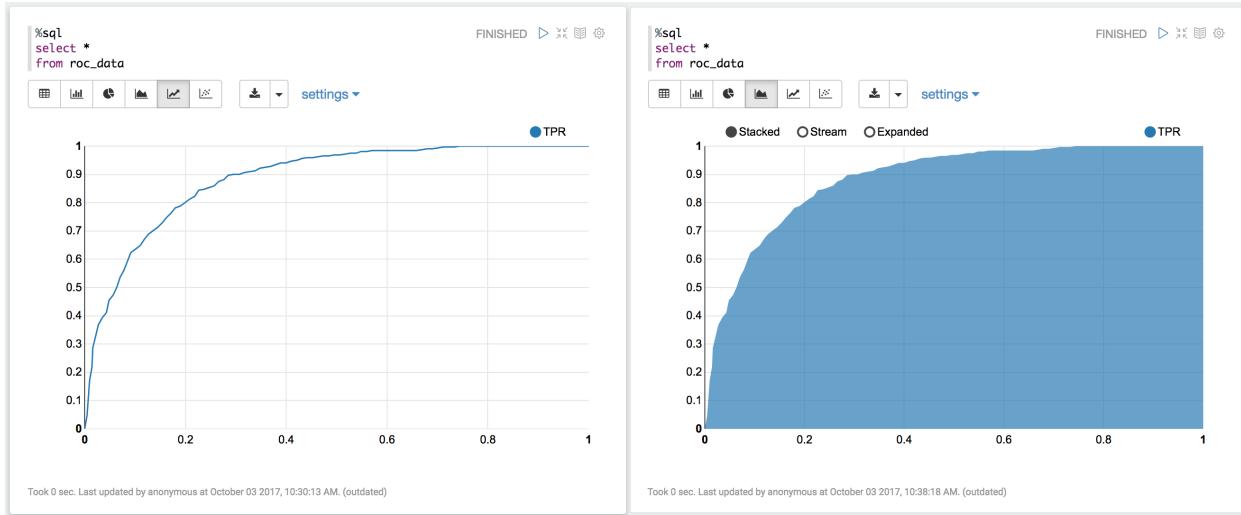
You can also register a TempTable `data.registerTempTable('roc_data')` and then use `sql` to plot the ROC curve:

10. visualization

```
import matplotlib.pyplot as plt
import numpy as np
import itertools

def plot_confusion_matrix(cm, classes,
                        normalize=False,
                        title='Confusion matrix',
```

(continues on next page)



(continued from previous page)

```
cmap=plt.cm.Blues):
"""
This function prints and plots the confusion matrix.
Normalization can be applied by setting `normalize=True`.
"""
if normalize:
    cm = cm.astype('float') / cm.sum(axis=1)[:, np.newaxis]
    print("Normalized confusion matrix")
else:
    print('Confusion matrix, without normalization')

print(cm)

plt.imshow(cm, interpolation='nearest', cmap=cmap)
plt.title(title)
plt.colorbar()
tick_marks = np.arange(len(classes))
plt.xticks(tick_marks, classes, rotation=45)
plt.yticks(tick_marks, classes)

fmt = '.2f' if normalize else 'd'
thresh = cm.max() / 2.
for i, j in itertools.product(range(cm.shape[0]), range(cm.shape[1])):
    plt.text(j, i, format(cm[i, j], fmt),
             horizontalalignment="center",
             color="white" if cm[i, j] > thresh else "black")

plt.tight_layout()
plt.ylabel('True label')
plt.xlabel('Predicted label')
```

```
class_temp = predictions.select("label").groupBy("label") \
    .count().sort('count', ascending=False).toPandas()
```

(continues on next page)

(continued from previous page)

```
class_temp = class_temp["label"].values.tolist()
class_names = map(str, class_temp)
# # # print(class_name)
class_names
```

```
['no', 'yes']
```

```
from sklearn.metrics import confusion_matrix
y_true = predictions.select("label")
y_true = y_true.toPandas()

y_pred = predictions.select("predictedLabel")
y_pred = y_pred.toPandas()

cnf_matrix = confusion_matrix(y_true, y_pred, labels=class_names)
cnf_matrix
```

```
array([[15657,    379],
       [ 1410,   667]])
```

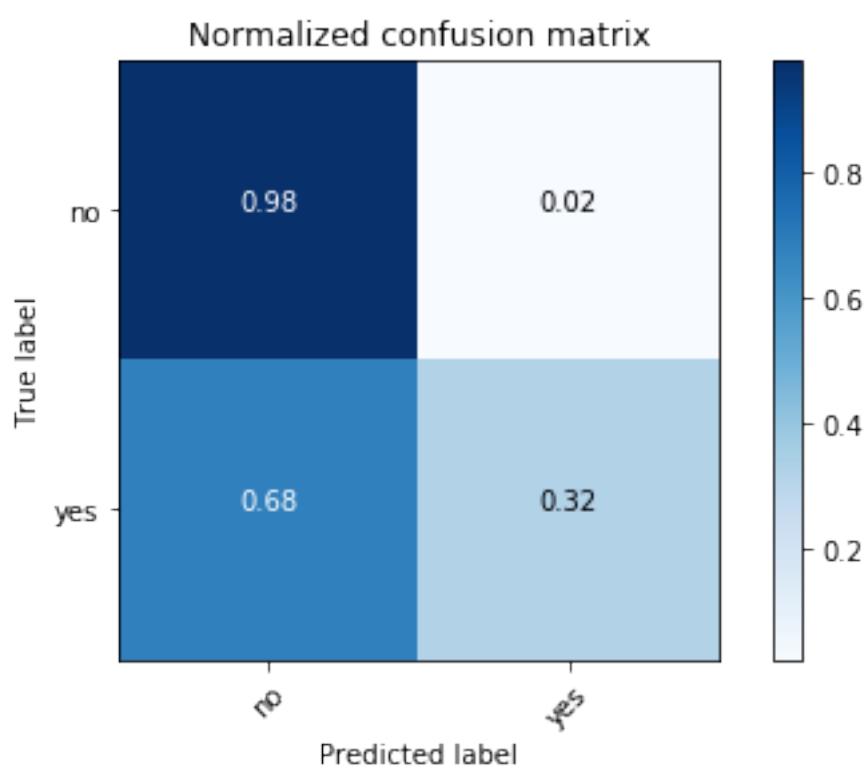
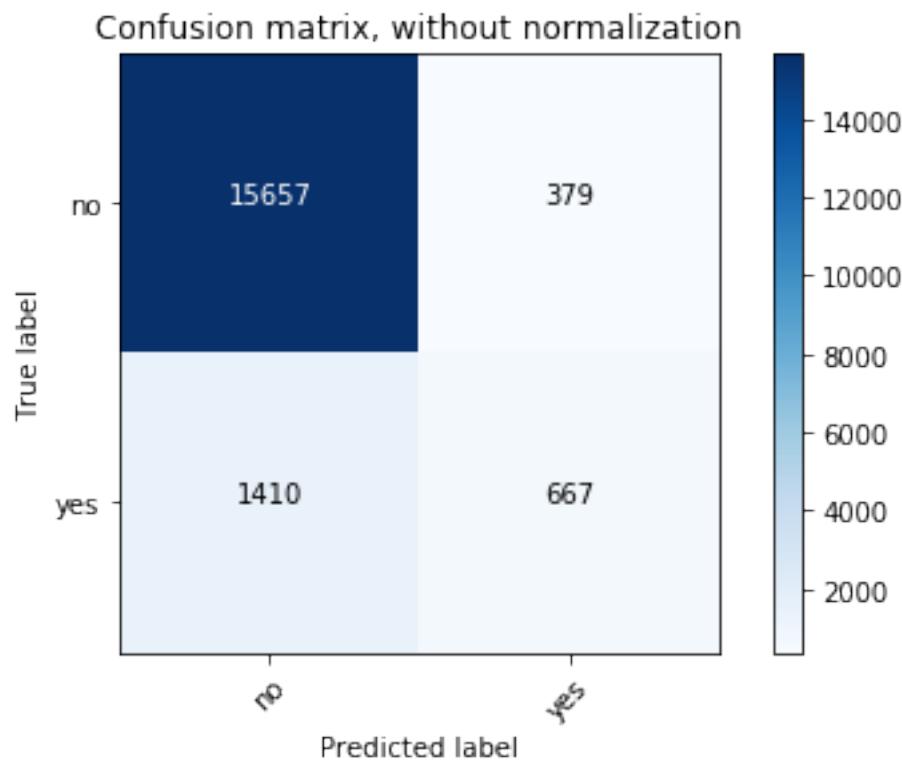
```
# Plot non-normalized confusion matrix
plt.figure()
plot_confusion_matrix(cnf_matrix, classes=class_names,
                      title='Confusion matrix, without normalization')
plt.show()
```

```
Confusion matrix, without normalization
[[15657  379]
 [ 1410  667]]
```

```
# Plot normalized confusion matrix
plt.figure()
plot_confusion_matrix(cnf_matrix, classes=class_names, normalize=True,
                      title='Normalized confusion matrix')

plt.show()
```

```
Normalized confusion matrix
[[ 0.97636568  0.02363432]
 [ 0.67886375  0.32113625]]
```



10.2 Multinomial logistic regression

10.2.1 Introduction

10.2.2 Demo

- The Jupyter notebook can be download from [Logistic Regression](#).
- For more details, please visit [Logistic Regression API](#).

Note: In this demo, I introduced a new function `get_dummy` to deal with the categorical data. I highly recommend you to use my `get_dummy` function in the other cases. This function will save a lot of time for you.

1. Set up spark context and SparkSession

```
from pyspark.sql import SparkSession

spark = SparkSession \
    .builder \
    .appName("Python Spark MultinomialLogisticRegression classification") \
    .config("spark.some.config.option", "some-value") \
    .getOrCreate()
```

2. Load dataset

```
df = spark.read.format('com.databricks.spark.csv') \
    .options(header='true', inferSchema='true') \
    .load("./data/WineData2.csv", header=True);
df.show(5)
```

fixed	volatile	citric	sugar	chlorides	free	total	density	pH	sulphates	alcohol	quality
7.4	0.7	0.0	1.9	0.076	11.0	34.0	0.9978	3.51	0.56		
9.4		5									
7.8	0.88	0.0	2.6	0.098	25.0	67.0	0.9968	3.2	0.68		
9.8		5									
7.8	0.76	0.04	2.3	0.092	15.0	54.0	0.997	3.26	0.65		
9.8		5									
11.2	0.28	0.56	1.9	0.075	17.0	60.0	0.998	3.16	0.58		
9.8		6									
7.4	0.7	0.0	1.9	0.076	11.0	34.0	0.9978	3.51	0.56		
9.4		5									

only showing top 5 rows

```
df.printSchema()
```

```
root
|-- fixed: double (nullable = true)
|-- volatile: double (nullable = true)
|-- citric: double (nullable = true)
|-- sugar: double (nullable = true)
|-- chlorides: double (nullable = true)
|-- free: double (nullable = true)
|-- total: double (nullable = true)
|-- density: double (nullable = true)
|-- pH: double (nullable = true)
|-- sulphates: double (nullable = true)
|-- alcohol: double (nullable = true)
|-- quality: string (nullable = true)
```

```
# Convert to float format
def string_to_float(x):
    return float(x)

#
def condition(r):
    if (0 <= r <= 4):
        label = "low"
    elif(4 < r <= 6):
        label = "medium"
    else:
        label = "high"
    return label

from pyspark.sql.functions import udf
from pyspark.sql.types import StringType, DoubleType
string_to_float_udf = udf(string_to_float, DoubleType())
quality_udf = udf(lambda x: condition(x), StringType())

df = df.withColumn("quality", quality_udf("quality"))

df.show(5, True)
```

fixed	volatile	citric	sugar	chlorides	free	total	density	pH	sulphates	alcohol	quality
7.4	0.7	0.0	1.9	0.076	11.0	34.0	0.9978	3.51	0.56		medium
9.4											medium
7.8	0.88	0.0	2.6	0.098	25.0	67.0	0.9968	3.2	0.68		medium
9.8											medium
7.8	0.76	0.04	2.3	0.092	15.0	54.0	0.997	3.26	0.65		medium
9.8											medium

(continues on next page)

(continued from previous page)

```
| 11.2|    0.28|   0.56|   1.9|    0.075|17.0|  60.0|   0.998|3.16|     0.58|   ↵
| 9.8| medium|
| 7.4|    0.7|   0.0|   1.9|    0.076|11.0|  34.0|   0.9978|3.51|     0.56|   ↵
| 9.4| medium|
+---+-----+---+-----+---+-----+---+-----+---+-----+---+
|---+-----+
only showing top 5 rows
```

```
df.printSchema()
```

```
root
|-- fixed: double (nullable = true)
|-- volatile: double (nullable = true)
|-- citric: double (nullable = true)
|-- sugar: double (nullable = true)
|-- chlorides: double (nullable = true)
|-- free: double (nullable = true)
|-- total: double (nullable = true)
|-- density: double (nullable = true)
|-- pH: double (nullable = true)
|-- sulphates: double (nullable = true)
|-- alcohol: double (nullable = true)
|-- quality: string (nullable = true)
```

3. Deal with categorical data and Convert the data to dense vector

Note: You are strongly encouraged to try my get_dummy function for dealing with the categorical data in complex dataset.

Supervised learning version:

```
def get_dummy(df, indexCol, categoricalCols, continuousCols, labelCol):
    from pyspark.ml import Pipeline
    from pyspark.ml.feature import StringIndexer, OneHotEncoder, ↵
    VectorAssembler
    from pyspark.sql.functions import col

    indexers = [ StringIndexer(inputCol=c, outputCol="{0}_indexed".format(c))
        for c in categoricalCols ]

    # default setting: dropLast=True
    encoders = [ OneHotEncoder(inputCol=indexer.getOutputCol(),
        outputCol="{0}_encoded".format(indexer.
        getOutputCol()))
        for indexer in indexers ]

    assembler = VectorAssembler(inputCols=[encoder.getOutputCol() ↵
    for encoder in encoders]
```

(continues on next page)

(continued from previous page)

```

    + continuousCols, outputCol="features"
    ↵" )

pipeline = Pipeline(stages=indexers + encoders + [assembler])

model=pipeline.fit(df)
data = model.transform(df)

data = data.withColumn('label', col(labelCol))

return data.select(indexCol, 'features', 'label')

```

Unsupervised learning version:

```

def get_dummy(df, indexCol, categoricalCols, continuousCols):
    """
    Get dummy variables and concat with continuous variables for
    ↵unsupervised learning.
    :param df: the dataframe
    :param categoricalCols: the name list of the categorical data
    :param continuousCols: the name list of the numerical data
    :return k: feature matrix

    :author: Wenqiang Feng
    :email: von198@gmail.com
    """

    indexers = [ StringIndexer(inputCol=c, outputCol="{0}_indexed".
    ↵format(c))
        for c in categoricalCols ]

    # default setting: dropLast=True
    encoders = [ OneHotEncoder(inputCol=indexer.getOutputCol(),
        outputCol="{0}_encoded".format(indexer.
    ↵getOutputCol()))
        for indexer in indexers ]

    assembler = VectorAssembler(inputCols=[encoder.getOutputCol()
    ↵for encoder in encoders]
        + continuousCols, outputCol="features
    ↵" )

    pipeline = Pipeline(stages=indexers + encoders + [assembler])

    model=pipeline.fit(df)
    data = model.transform(df)

    return data.select(indexCol, 'features')

```

```
def get_dummy(df, categoricalCols, continuousCols, labelCol):
```

(continues on next page)

(continued from previous page)

```

from pyspark.ml import Pipeline
from pyspark.ml.feature import StringIndexer, OneHotEncoder,
→VectorAssembler
from pyspark.sql.functions import col

indexers = [ StringIndexer(inputCol=c, outputCol="{0}_indexed".format(c))
             for c in categoricalCols ]

# default setting: dropLast=True
encoders = [ OneHotEncoder(inputCol=indexer.getOutputCol(),
                            outputCol="{0}_encoded".format(indexer.getOutputCol()))
              for indexer in indexers ]

assembler = VectorAssembler(inputCols=[encoder.getOutputCol() for encoder
→in encoders]
                             + continuousCols, outputCol="features")

pipeline = Pipeline(stages=indexers + encoders + [assembler])

model=pipeline.fit(df)
data = model.transform(df)

data = data.withColumn('label', col(labelCol))

return data.select('features','label')

```

4. Transform the dataset to DataFrame

```

from pyspark.ml.linalg import Vectors # !!!!caution: not from pyspark.mllib.
→linalg import Vectors
from pyspark.ml import Pipeline
from pyspark.ml.feature import IndexToString, StringIndexer, VectorIndexer
from pyspark.ml.tuning import CrossValidator, ParamGridBuilder
from pyspark.ml.evaluation import MulticlassClassificationEvaluator

def transData(data):
    return data.rdd.map(lambda r: [Vectors.dense(r[:-1]), r[-1]]).toDF(['features',
→'label'])

```

```

transformed = transData(df)
transformed.show(5)

```

features	label
[7.4, 0.7, 0.0, 1.9, ...]	medium
[7.8, 0.88, 0.0, 2.6, ...]	medium
[7.8, 0.76, 0.04, 2, ...]	medium
[11.2, 0.28, 0.56, 1, ...]	medium
[7.4, 0.7, 0.0, 1.9, ...]	medium

(continues on next page)

(continued from previous page)

```
+-----+-----+
only showing top 5 rows
```

4. Deal with Categorical Label and Variables

```
# Index labels, adding metadata to the label column
labelIndexer = StringIndexer(inputCol='label',
                             outputCol='indexedLabel').fit(transformed)
labelIndexer.transform(transformed).show(5, True)
```

```
+-----+-----+-----+
|       features| label|indexedLabel|
+-----+-----+-----+
|[7.4,0.7,0.0,1.9,...|medium|      0.0|
|[7.8,0.88,0.0,2.6...|medium|      0.0|
|[7.8,0.76,0.04,2....|medium|      0.0|
|[11.2,0.28,0.56,1...|medium|      0.0|
|[7.4,0.7,0.0,1.9,...|medium|      0.0|
+-----+-----+-----+
only showing top 5 rows
```

```
# Automatically identify categorical features, and index them.
# Set maxCategories so features with > 4 distinct values are treated as
# continuous.
featureIndexer = VectorIndexer(inputCol="features", \
                                outputCol="indexedFeatures", \
                                maxCategories=4).fit(transformed)
featureIndexer.transform(transformed).show(5, True)
```

```
+-----+-----+-----+
|       features| label|     indexedFeatures|
+-----+-----+-----+
|[7.4,0.7,0.0,1.9,...|medium|[7.4,0.7,0.0,1.9,...|
|[7.8,0.88,0.0,2.6...|medium|[7.8,0.88,0.0,2.6...|
|[7.8,0.76,0.04,2....|medium|[7.8,0.76,0.04,2....|
|[11.2,0.28,0.56,1...|medium|[11.2,0.28,0.56,1...|
|[7.4,0.7,0.0,1.9,...|medium|[7.4,0.7,0.0,1.9,...|
+-----+-----+-----+
only showing top 5 rows
```

5. Split the data to training and test data sets

```
# Split the data into training and test sets (40% held out for testing)
(trainingData, testData) = data.randomSplit([0.6, 0.4])

trainingData.show(5, False)
testData.show(5, False)
```

features	label
----------	-------

(continues on next page)

(continued from previous page)

```
+-----+-----+
| [4.7,0.6,0.17,2.3,0.058,17.0,106.0,0.9932,3.85,0.6,12.9] |medium|
| [5.0,0.38,0.01,1.6,0.048,26.0,60.0,0.99084,3.7,0.75,14.0] |medium|
| [5.0,0.4,0.5,4.3,0.046,29.0,80.0,0.9902,3.49,0.66,13.6] |medium|
| [5.0,0.74,0.0,1.2,0.041,16.0,46.0,0.99258,4.01,0.59,12.5] |medium|
| [5.1,0.42,0.0,1.8,0.044,18.0,88.0,0.99157,3.68,0.73,13.6] |high |
+-----+-----+
only showing top 5 rows

+-----+-----+
|features |label |
+-----+-----+
| [4.6,0.52,0.15,2.1,0.054,8.0,65.0,0.9934,3.9,0.56,13.1] |low   |
| [4.9,0.42,0.0,2.1,0.048,16.0,42.0,0.99154,3.71,0.74,14.0] |high  |
| [5.0,0.42,0.24,2.0,0.06,19.0,50.0,0.9917,3.72,0.74,14.0] |high  |
| [5.0,1.02,0.04,1.4,0.045,41.0,85.0,0.9938,3.75,0.48,10.5] |low   |
| [5.0,1.04,0.24,1.6,0.05,32.0,96.0,0.9934,3.74,0.62,11.5] |medium|
+-----+-----+
only showing top 5 rows
```

6. Fit Multinomial logisticRegression Classification Model

```
from pyspark.ml.classification import LogisticRegression
logr = LogisticRegression(featuresCol='indexedFeatures', labelCol=
                           'indexedLabel')
```

7. Pipeline Architecture

```
# Convert indexed labels back to original labels.
labelConverter = IndexToString(inputCol="prediction", outputCol=
                               "predictedLabel",
                               labels=labelIndexer.labels)
```

```
# Chain indexers and tree in a Pipeline
pipeline = Pipeline(stages=[labelIndexer, featureIndexer, logr,
                           labelConverter])
```

```
# Train model. This also runs the indexers.
model = pipeline.fit(trainingData)
```

8. Make predictions

```
# Make predictions.
predictions = model.transform(testData)
# Select example rows to display.
predictions.select("features", "label", "predictedLabel").show(5)
```

```
+-----+-----+-----+
|       features| label|predictedLabel|
+-----+-----+-----+
```

(continues on next page)

(continued from previous page)

```
| [4.6,0.52,0.15,2....|    low|      medium|
| [4.9,0.42,0.0,2.1...|   high|       high|
| [5.0,0.42,0.24,2....|   high|       high|
| [5.0,1.02,0.04,1....|    low|      medium|
| [5.0,1.04,0.24,1....|medium|      medium|
+-----+-----+-----+
only showing top 5 rows
```

9. Evaluation

```
from pyspark.ml.evaluation import MulticlassClassificationEvaluator

# Select (prediction, true label) and compute test error
evaluator = MulticlassClassificationEvaluator(
    labelCol="indexedLabel", predictionCol="prediction", metricName="accuracy"
)
accuracy = evaluator.evaluate(predictions)
print("Test Error = %g" % (1.0 - accuracy))
```

```
Test Error = 0.181287
```

```
lrModel = model.stages[2]
trainingSummary = lrModel.summary

# Obtain the objective per iteration
# objectiveHistory = trainingSummary.objectiveHistory
# print("objectiveHistory:")
# for objective in objectiveHistory:
#     print(objective)

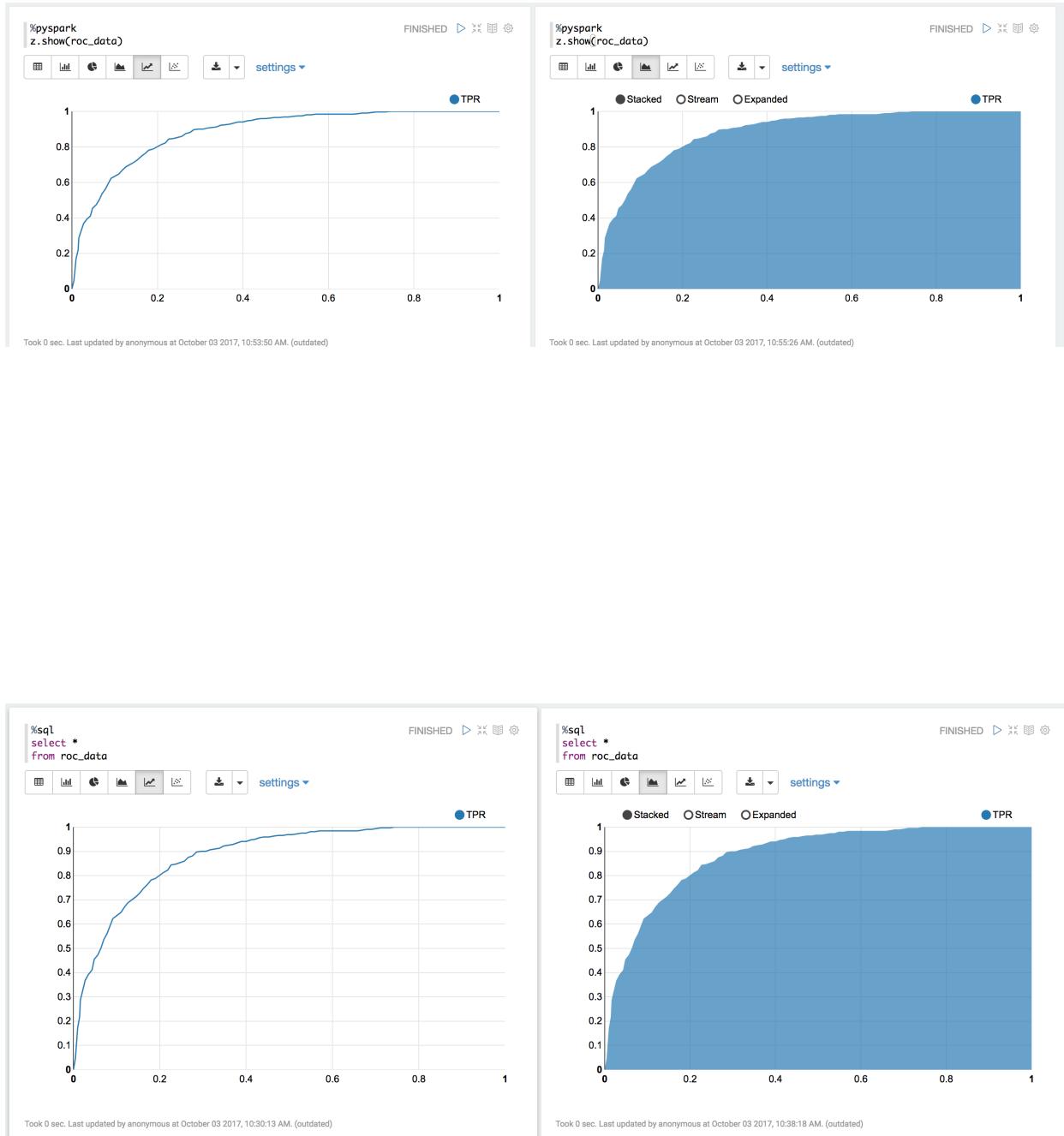
# Obtain the receiver-operating characteristic as a dataframe and
# areaUnderROC.
trainingSummary.roc.show(5)
print("areaUnderROC: " + str(trainingSummary.areaUnderROC))

# Set the model threshold to maximize F-Measure
fMeasure = trainingSummary.fMeasureByThreshold
maxFMeasure = fMeasure.groupBy().max('F-Measure').select('max(F-Measure)').head(5)
# bestThreshold = fMeasure.where(fMeasure['F-Measure'] == maxFMeasure['max(F-
# Measure)']) \
#     .select('threshold').head()['threshold']
# lr.setThreshold(bestThreshold)
```

You can use `z.show()` to get the data and plot the ROC curves:

You can also register a TempTable `data.registerTempTable('roc_data')` and then use `sql` to plot the ROC curve:

10. visualization



```

import matplotlib.pyplot as plt
import numpy as np
import itertools

def plot_confusion_matrix(cm, classes,
                         normalize=False,
                         title='Confusion matrix',
                         cmap=plt.cm.Blues):

    """
    This function prints and plots the confusion matrix.
    Normalization can be applied by setting `normalize=True`.
    """

    if normalize:
        cm = cm.astype('float') / cm.sum(axis=1)[:, np.newaxis]
        print("Normalized confusion matrix")
    else:
        print('Confusion matrix, without normalization')

    print(cm)

    plt.imshow(cm, interpolation='nearest', cmap=cmap)
    plt.title(title)
    plt.colorbar()
    tick_marks = np.arange(len(classes))
    plt.xticks(tick_marks, classes, rotation=45)
    plt.yticks(tick_marks, classes)

    fmt = '.2f' if normalize else 'd'
    thresh = cm.max() / 2.
    for i, j in itertools.product(range(cm.shape[0]), range(cm.shape[1])):
        plt.text(j, i, format(cm[i, j], fmt),
                 horizontalalignment="center",
                 color="white" if cm[i, j] > thresh else "black")

    plt.tight_layout()
    plt.ylabel('True label')
    plt.xlabel('Predicted label')

```

```

class_temp = predictions.select("label").groupBy("label") \
    .count().sort('count', ascending=False).toPandas()
class_temp = class_temp["label"].values.tolist()
class_names = map(str, class_temp)
# # # print(class_name)
class_names

```

```
['medium', 'high', 'low']
```

```

from sklearn.metrics import confusion_matrix
y_true = predictions.select("label")
y_true = y_true.toPandas()

```

(continues on next page)

(continued from previous page)

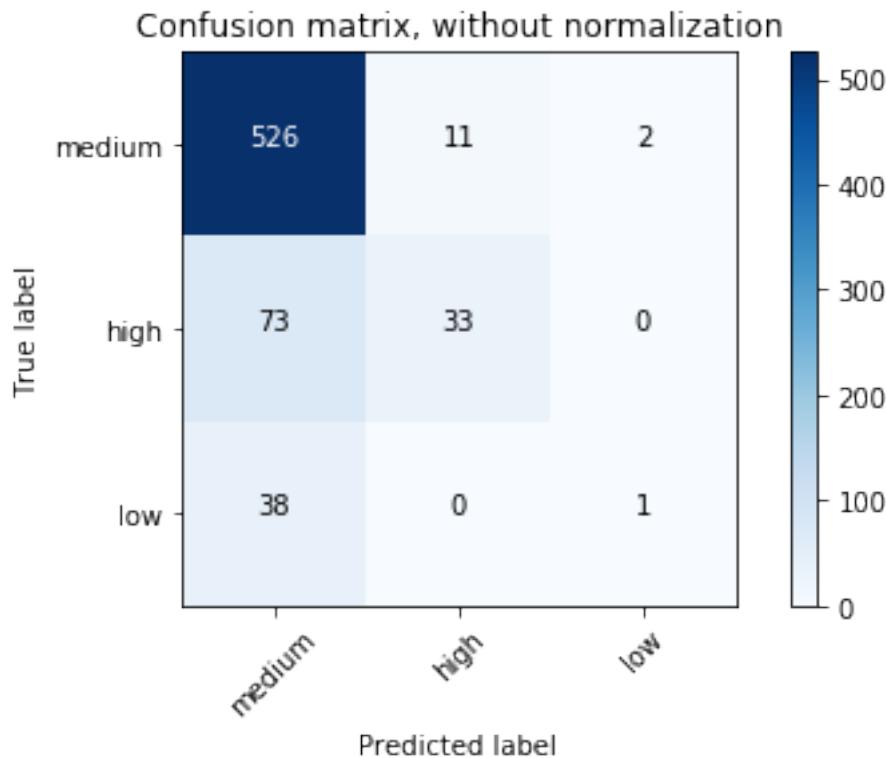
```
y_pred = predictions.select("predictedLabel")
y_pred = y_pred.toPandas()

cnf_matrix = confusion_matrix(y_true, y_pred, labels=class_names)
cnf_matrix
```

```
array([[526,   11,    2],
       [ 73,   33,    0],
       [ 38,    0,    1]])
```

```
# Plot non-normalized confusion matrix
plt.figure()
plot_confusion_matrix(cnf_matrix, classes=class_names,
                      title='Confusion matrix, without normalization')
plt.show()
```

```
Confusion matrix, without normalization
[[526  11  2]
 [ 73  33  0]
 [ 38   0  1]]
```



```
# Plot normalized confusion matrix
plt.figure()
plot_confusion_matrix(cnf_matrix, classes=class_names, normalize=True,
```

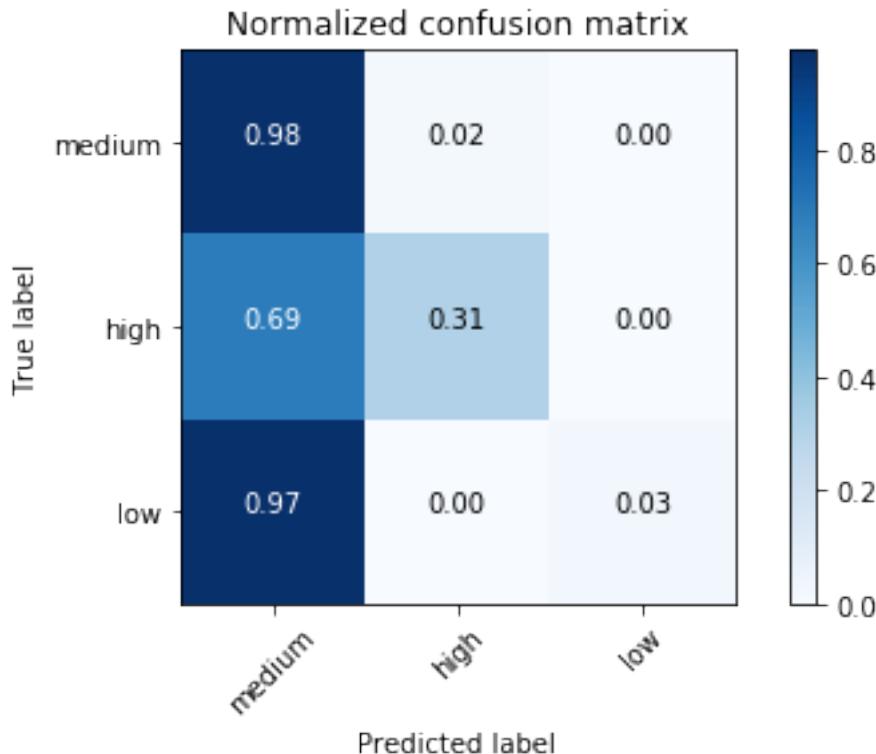
(continues on next page)

(continued from previous page)

```
title='Normalized confusion matrix')

plt.show()
```

```
Normalized confusion matrix
[[0.97588126 0.02040816 0.00371058]
 [0.68867925 0.31132075 0.        ]
 [0.97435897 0.        0.02564103]]
```



10.3 Decision tree Classification

10.3.1 Introduction

10.3.2 Demo

- The Jupyter notebook can be download from [Decision Tree Classification](#).
 - For more details, please visit [DecisionTreeClassifier API](#).
1. Set up spark context and SparkSession

```
from pyspark.sql import SparkSession
```

(continues on next page)

(continued from previous page)

```
spark = SparkSession \
    .builder \
    .appName("Python Spark Decision Tree classification") \
    .config("spark.some.config.option", "some-value") \
    .getOrCreate()
```

2. Load dataset

```
df = spark.read.format('com.databricks.spark.csv') \
    .options(header='true', \
             inferSchema='true') \
    .load("../data/WineData2.csv", header=True);
df.show(5, True)
```

	fixed	volatile	citric	sugar	chlorides	free	total	density	pH	sulphates	alcohol	quality
1	7.4	0.7	0.0	1.9	0.076	11.0	34.0	0.9978	3.51	0.56		
2	9.4	5										
3	7.8	0.88	0.0	2.6	0.098	25.0	67.0	0.9968	3.2	0.68		
4	9.8	5										
5	7.8	0.76	0.04	2.3	0.092	15.0	54.0	0.997	3.26	0.65		
6	9.8	5										
7	11.2	0.28	0.56	1.9	0.075	17.0	60.0	0.998	3.16	0.58		
8	9.8	6										
9	7.4	0.7	0.0	1.9	0.076	11.0	34.0	0.9978	3.51	0.56		
10	9.4	5										

only showing top 5 rows

```
# Convert to float format
def string_to_float(x):
    return float(x)

#
def condition(r):
    if (0 <= r <= 4):
        label = "low"
    elif(4 < r <= 6):
        label = "medium"
    else:
        label = "high"
    return label
```

```
from pyspark.sql.functions import udf
from pyspark.sql.types import StringType, DoubleType
```

(continues on next page)

(continued from previous page)

```
string_to_float_udf = udf(string_to_float, DoubleType())
quality_udf = udf(lambda x: condition(x), StringType())
```

```
df = df.withColumn("quality", quality_udf("quality"))
df.show(5, True)
df.printSchema()
```

fixed	volatile	citric	sugar	chlorides	free	total	density	pH	sulphates	alcohol	quality
7.4	0.7	0.0	1.9	0.076	11.0	34.0	0.9978	3.51	0.56		
9.4	medium										
7.8	0.88	0.0	2.6	0.098	25.0	67.0	0.9968	3.2	0.68		
9.8	medium										
7.8	0.76	0.04	2.3	0.092	15.0	54.0	0.997	3.26	0.65		
9.8	medium										
11.2	0.28	0.56	1.9	0.075	17.0	60.0	0.998	3.16	0.58		
9.8	medium										
7.4	0.7	0.0	1.9	0.076	11.0	34.0	0.9978	3.51	0.56		
9.4	medium										

only showing top 5 rows

```
root
|-- fixed: double (nullable = true)
|-- volatile: double (nullable = true)
|-- citric: double (nullable = true)
|-- sugar: double (nullable = true)
|-- chlorides: double (nullable = true)
|-- free: double (nullable = true)
|-- total: double (nullable = true)
|-- density: double (nullable = true)
|-- pH: double (nullable = true)
|-- sulphates: double (nullable = true)
|-- alcohol: double (nullable = true)
|-- quality: string (nullable = true)
```

3. Convert the data to dense vector

Note: You are strongly encouraged to try my `get_dummy` function for dealing with the categorical data in complex dataset.

Supervised learning version:

```
def get_dummy(df, indexCol, categoricalCols, continuousCols, labelCol):
```

(continues on next page)

(continued from previous page)

```

from pyspark.ml import Pipeline
from pyspark.ml.feature import StringIndexer, OneHotEncoder,
→VectorAssembler
from pyspark.sql.functions import col

indexers = [ StringIndexer(inputCol=c, outputCol="{0}_indexed".
→format(c))
            for c in categoricalCols ]

# default setting: dropLast=True
encoders = [ OneHotEncoder(inputCol=indexer.getOutputCol(),
                           outputCol="{0}_encoded".format(indexer.
→getOutputCol()))
            for indexer in indexers ]

assembler = VectorAssembler(inputCols=[encoder.getOutputCol()].
→for encoder in encoders]
                           + continuousCols, outputCol="features"
→")

pipeline = Pipeline(stages=indexers + encoders + [assembler])

model=pipeline.fit(df)
data = model.transform(df)

data = data.withColumn('label', col(labelCol))

return data.select(indexCol, 'features', 'label')

```

Unsupervised learning version:

```

def get_dummy(df,indexCol,categoricalCols,continuousCols):
    """
    Get dummy variables and concat with continuous variables for
    →unsupervised learning.
    :param df: the dataframe
    :param categoricalCols: the name list of the categorical data
    :param continuousCols: the name list of the numerical data
    :return k: feature matrix

    :author: Wenqiang Feng
    :email: von198@gmail.com
    """

    indexers = [ StringIndexer(inputCol=c, outputCol="{0}_indexed".
→format(c))
            for c in categoricalCols ]

    # default setting: dropLast=True
    encoders = [ OneHotEncoder(inputCol=indexer.getOutputCol(),
                               outputCol="{0}_encoded".format(indexer.
→getOutputCol()))
            for indexer in indexers ]

```

(continues on next page)

(continued from previous page)

```

        for indexer in indexers ]

    assembler = VectorAssembler(inputCols=[encoder.getOutputCol()_
    ↪for encoder in encoders]
                                + continuousCols, outputCol="features"
    ↪" )

    pipeline = Pipeline(stages=indexers + encoders + [assembler])

    model=pipeline.fit(df)
    data = model.transform(df)

    return data.select(indexCol,'features')

```

```

# !!!!caution: not from pyspark.mllib.linalg import Vectors
from pyspark.ml.linalg import Vectors
from pyspark.ml import Pipeline
from pyspark.ml.feature import IndexToString, StringIndexer, VectorIndexer
from pyspark.ml.tuning import CrossValidator, ParamGridBuilder
from pyspark.ml.evaluation import MulticlassClassificationEvaluator

```

```

def transData(data):
    return data.rdd.map(lambda r: [Vectors.dense(r[:-1]),r[-1]]).toDF([
    ↪'features','label'])

```

4. Transform the dataset to DataFrame

```

transformed = transData(df)
transformed.show(5)

```

```

+-----+-----+
|      features| label|
+-----+-----+
| [7.4,0.7,0.0,1.9,...|medium|
| [7.8,0.88,0.0,2.6...|medium|
| [7.8,0.76,0.04,2....|medium|
| [11.2,0.28,0.56,1...|medium|
| [7.4,0.7,0.0,1.9,...|medium|
+-----+-----+
only showing top 5 rows

```

5. Deal with Categorical Label and Variables

```

# Index labels, adding metadata to the label column
labelIndexer = StringIndexer(inputCol='label',
                             outputCol='indexedLabel').fit(transformed)
labelIndexer.transform(transformed).show(5, True)

```

```
+-----+-----+-----+
|       features| label|indexedLabel|
+-----+-----+-----+
|[7.4,0.7,0.0,1.9,...|medium|      0.0|
|[7.8,0.88,0.0,2.6...|medium|      0.0|
|[7.8,0.76,0.04,2....|medium|      0.0|
|[11.2,0.28,0.56,1...|medium|      0.0|
|[7.4,0.7,0.0,1.9,...|medium|      0.0|
+-----+-----+-----+
only showing top 5 rows
```

```
# Automatically identify categorical features, and index them.
# Set maxCategories so features with > 4 distinct values are treated as
˓→continuous.
featureIndexer = VectorIndexer(inputCol="features", \
                               outputCol="indexedFeatures", \
                               maxCategories=4).fit(transformed)
featureIndexer.transform(transformed).show(5, True)
```

```
+-----+-----+-----+
|       features| label|      indexedFeatures|
+-----+-----+-----+
|[7.4,0.7,0.0,1.9,...|medium|[7.4,0.7,0.0,1.9,...|
|[7.8,0.88,0.0,2.6...|medium|[7.8,0.88,0.0,2.6...|
|[7.8,0.76,0.04,2....|medium|[7.8,0.76,0.04,2....|
|[11.2,0.28,0.56,1...|medium|[11.2,0.28,0.56,1...|
|[7.4,0.7,0.0,1.9,...|medium|[7.4,0.7,0.0,1.9,...|
+-----+-----+-----+
only showing top 5 rows
```

6. Split the data to training and test data sets

```
# Split the data into training and test sets (40% held out for testing)
(trainingData, testData) = transformed.randomSplit([0.6, 0.4])

trainingData.show(5)
testData.show(5)
```

```
+-----+-----+
|       features| label|
+-----+-----+
|[4.6,0.52,0.15,2....|   low|
|[4.7,0.6,0.17,2.3...|medium|
|[5.0,1.02,0.04,1....|   low|
|[5.0,1.04,0.24,1....|medium|
|[5.1,0.585,0.0,1....|  high|
+-----+-----+
only showing top 5 rows
```



```
+-----+-----+
|       features| label|
+-----+-----+
```

(continues on next page)

(continued from previous page)

```
+-----+-----+
| [4.9,0.42,0.0,2.1...|  high|
| [5.0,0.38,0.01,1....|medium|
| [5.0,0.4,0.5,4.3,...|medium|
| [5.0,0.42,0.24,2....|  high|
| [5.0,0.74,0.0,1.2...|medium|
+-----+-----+
only showing top 5 rows
```

7. Fit Decision Tree Classification Model

```
from pyspark.ml.classification import DecisionTreeClassifier

# Train a DecisionTree model
dTree = DecisionTreeClassifier(labelCol='indexedLabel', featuresCol=
    'indexedFeatures')
```

8. Pipeline Architecture

```
# Convert indexed labels back to original labels.
labelConverter = IndexToString(inputCol="prediction", outputCol=
    "predictedLabel",
    labels=labelIndexer.labels)
```

```
# Chain indexers and tree in a Pipeline
pipeline = Pipeline(stages=[labelIndexer, featureIndexer, dTree,
    labelConverter])
```

```
# Train model. This also runs the indexers.
model = pipeline.fit(trainingData)
```

9. Make predictions

```
# Make predictions.
predictions = model.transform(testData)
# Select example rows to display.
predictions.select("features", "label", "predictedLabel").show(5)
```

```
+-----+-----+-----+
|       features| label|predictedLabel|
+-----+-----+-----+
| [4.9,0.42,0.0,2.1...|  high|      high|
| [5.0,0.38,0.01,1....|medium|   medium|
| [5.0,0.4,0.5,4.3,...|medium|   medium|
| [5.0,0.42,0.24,2....|  high|   medium|
| [5.0,0.74,0.0,1.2...|medium|   medium|
+-----+-----+-----+
only showing top 5 rows
```

10. Evaluation

```
from pyspark.ml.evaluation import MulticlassClassificationEvaluator

# Select (prediction, true label) and compute test error
evaluator = MulticlassClassificationEvaluator(
    labelCol="indexedLabel", predictionCol="prediction", metricName="accuracy"
)
accuracy = evaluator.evaluate(predictions)
print("Test Error = %g" % (1.0 - accuracy))

rfModel = model.stages[-2]
print(rfModel) # summary only
```

```
Test Error = 0.45509
DecisionTreeClassificationModel (uid=DecisionTreeClassifier_
˓→4545ac8dca9c8438ef2a)
of depth 5 with 59 nodes
```

11. visualization

```
import matplotlib.pyplot as plt
import numpy as np
import itertools

def plot_confusion_matrix(cm, classes,
                         normalize=False,
                         title='Confusion matrix',
                         cmap=plt.cm.Blues):
    """
    This function prints and plots the confusion matrix.
    Normalization can be applied by setting `normalize=True`.
    """
    if normalize:
        cm = cm.astype('float') / cm.sum(axis=1)[:, np.newaxis]
        print("Normalized confusion matrix")
    else:
        print('Confusion matrix, without normalization')

    print(cm)

    plt.imshow(cm, interpolation='nearest', cmap=cmap)
    plt.title(title)
    plt.colorbar()
    tick_marks = np.arange(len(classes))
    plt.xticks(tick_marks, classes, rotation=45)
    plt.yticks(tick_marks, classes)

    fmt = '.2f' if normalize else 'd'
    thresh = cm.max() / 2.
    for i, j in itertools.product(range(cm.shape[0]), range(cm.shape[1])):
        plt.text(j, i, format(cm[i, j], fmt),
                 horizontalalignment="center",
                 color="white" if cm[i, j] > thresh else "black")
```

(continues on next page)

(continued from previous page)

```
plt.tight_layout()
plt.ylabel('True label')
plt.xlabel('Predicted label')
```

```
class_temp = predictions.select("label").groupBy("label") \
    .count().sort('count', ascending=False).toPandas()
class_temp = class_temp["label"].values.tolist()
class_names = map(str, class_temp)
# # # print(class_name)
class_names
```

```
['medium', 'high', 'low']
```

```
from sklearn.metrics import confusion_matrix
y_true = predictions.select("label")
y_true = y_true.toPandas()

y_pred = predictions.select("predictedLabel")
y_pred = y_pred.toPandas()

cnf_matrix = confusion_matrix(y_true, y_pred, labels=class_names)
cnf_matrix
```

```
array([[497,  29,   7],
       [ 40,  42,   0],
       [ 22,   0,   2]])
```

```
# Plot non-normalized confusion matrix
plt.figure()
plot_confusion_matrix(cnf_matrix, classes=class_names,
                      title='Confusion matrix, without normalization')
plt.show()
```

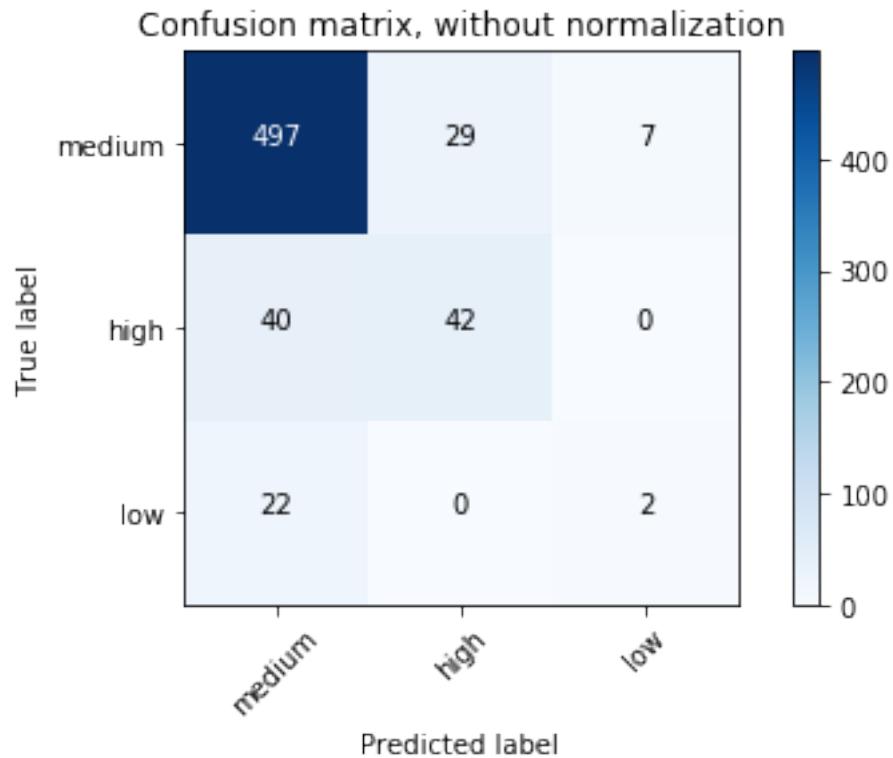
```
Confusion matrix, without normalization
[[497  29   7]
 [ 40  42   0]
 [ 22   0   2]]
```

```
# Plot normalized confusion matrix
plt.figure()
plot_confusion_matrix(cnf_matrix, classes=class_names, normalize=True,
                      title='Normalized confusion matrix')

plt.show()
```

```
Normalized confusion matrix
[[ 0.93245779  0.05440901  0.01313321]]
```

(continues on next page)



(continued from previous page)

```
[ 0.48780488  0.51219512  0.          ]
[ 0.91666667  0.          0.08333333] ]
```

10.4 Random forest Classification

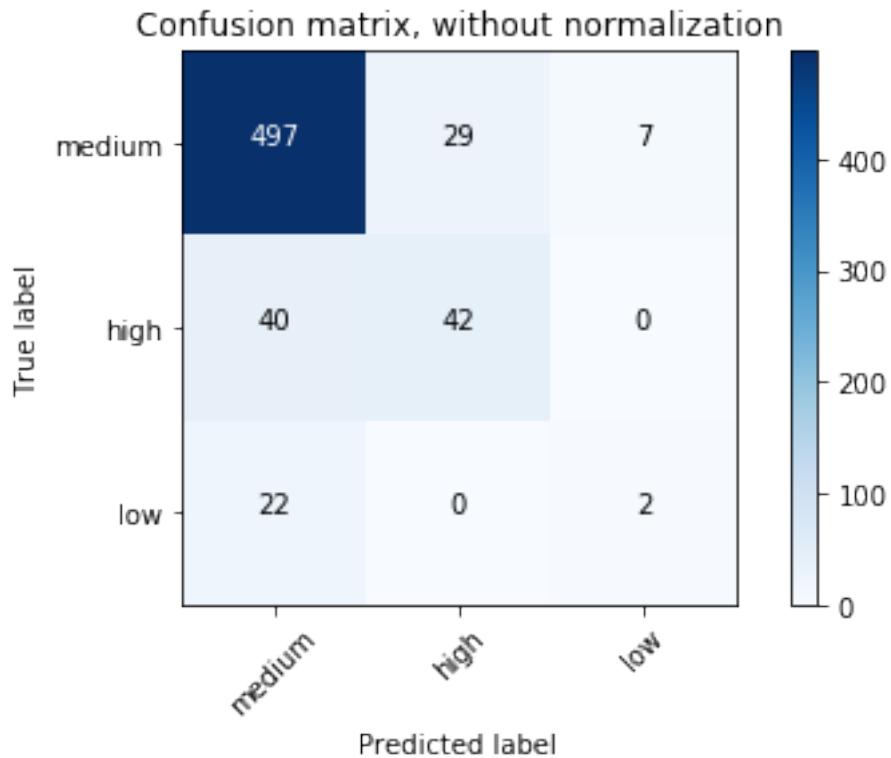
10.4.1 Introduction

10.4.2 Demo

- The Jupyter notebook can be download from Random forest Classification.
 - For more details, please visit [RandomForestClassifier API](#).
1. Set up spark context and SparkSession

```
from pyspark.sql import SparkSession

spark = SparkSession \
    .builder \
    .appName("Python Spark Decision Tree classification") \
    .config("spark.some.config.option", "some-value") \
    .getOrCreate()
```



2. Load dataset

```
df = spark.read.format('com.databricks.spark.csv') \
    .options(header='true', \
    inferSchema='true') \
    .load("../data/WineData2.csv", header=True);
df.show(5, True)
```

```
+---+---+---+---+---+---+---+---+---+---+---+---+---+---+
|fixed|volatile|citric|sugar|chlorides|free|total|density| pH|sulphates|alcohol|quality|
+---+---+---+---+---+---+---+---+---+---+---+---+---+---+
| 7.4| 0.7| 0.0| 1.9| 0.076|11.0| 34.0| 0.9978|3.51| 0.56| 
| 9.4| 5| 
| 7.8| 0.88| 0.0| 2.6| 0.098|25.0| 67.0| 0.9968| 3.2| 0.68| 
| 9.8| 5| 
| 7.8| 0.76| 0.04| 2.3| 0.092|15.0| 54.0| 0.997|3.26| 0.65| 
| 9.8| 5| 
| 11.2| 0.28| 0.56| 1.9| 0.075|17.0| 60.0| 0.998|3.16| 0.58| 
| 9.8| 6| 
| 7.4| 0.7| 0.0| 1.9| 0.076|11.0| 34.0| 0.9978|3.51| 0.56| 
| 9.4| 5| 
+---+---+---+---+---+---+---+---+---+---+---+---+---+---+
only showing top 5 rows
```

```
# Convert to float format
def string_to_float(x):
    return float(x)

#
def condition(r):
    if (0 <= r <= 4):
        label = "low"
    elif(4 < r <= 6):
        label = "medium"
    else:
        label = "high"
    return label
```

```
from pyspark.sql.functions import udf
from pyspark.sql.types import StringType, DoubleType
string_to_float_udf = udf(string_to_float, DoubleType())
quality_udf = udf(lambda x: condition(x), StringType())
```

```
df = df.withColumn("quality", quality_udf("quality"))
df.show(5, True)
df.printSchema()
```

```
+----+-----+-----+-----+-----+-----+-----+-----+
|fixed|volatile|citric|sugar|chlorides|free|total|density|
+----+-----+-----+-----+-----+-----+-----+-----+
|  7.4|     0.7|    0.0|   1.9|    0.076|11.0| 34.0| 0.9978|3.51|    0.56|
|  9.4| medium|
|  7.8|     0.88|   0.0|   2.6|    0.098|25.0| 67.0| 0.9968| 3.2|    0.68|
|  9.8| medium|
|  7.8|     0.76|   0.04|  2.3|    0.092|15.0| 54.0| 0.997|3.26|    0.65|
|  9.8| medium|
| 11.2|     0.28|   0.56|   1.9|    0.075|17.0| 60.0| 0.998|3.16|    0.58|
|  9.8| medium|
|  7.4|     0.7|    0.0|   1.9|    0.076|11.0| 34.0| 0.9978|3.51|    0.56|
|  9.4| medium|
+----+-----+-----+-----+-----+-----+-----+-----+
only showing top 5 rows
```

```
root
|-- fixed: double (nullable = true)
|-- volatile: double (nullable = true)
|-- citric: double (nullable = true)
|-- sugar: double (nullable = true)
|-- chlorides: double (nullable = true)
|-- free: double (nullable = true)
|-- total: double (nullable = true)
```

(continues on next page)

(continued from previous page)

```
|-- density: double (nullable = true)
|-- pH: double (nullable = true)
|-- sulphates: double (nullable = true)
|-- alcohol: double (nullable = true)
|-- quality: string (nullable = true)
```

3. Convert the data to dense vector

Note: You are strongly encouraged to try my get_dummy function for dealing with the categorical data in complex dataset.

Supervised learning version:

```
def get_dummy(df, indexCol, categoricalCols, continuousCols, labelCol):

    from pyspark.ml import Pipeline
    from pyspark.ml.feature import StringIndexer, OneHotEncoder, VectorAssembler
    from pyspark.sql.functions import col

    indexers = [ StringIndexer(inputCol=c, outputCol="{0}_indexed".
        format(c))
                for c in categoricalCols ]

    # default setting: dropLast=True
    encoders = [ OneHotEncoder(inputCol=indexer.getOutputCol(),
                                outputCol="{0}_encoded".format(indexer.
                                    getOutputCol()))
                for indexer in indexers ]

    assembler = VectorAssembler(inputCols=[encoder.getOutputCol()].
        for encoder in encoders]
                                + continuousCols, outputCol="features"
        )

    pipeline = Pipeline(stages=indexers + encoders + [assembler])

    model=pipeline.fit(df)
    data = model.transform(df)

    data = data.withColumn('label', col(labelCol))

    return data.select(indexCol, 'features', 'label')
```

Unsupervised learning version:

```
def get_dummy(df, indexCol, categoricalCols, continuousCols):
    """
    Get dummy variables and concat with continuous variables for
    unsupervised learning.
    :param df: the dataframe
```

(continues on next page)

(continued from previous page)

```

:param categoricalCols: the name list of the categorical data
:param continuousCols: the name list of the numerical data
:return k: feature matrix

:author: Wenqiang Feng
:email: von198@gmail.com
'''

indexers = [ StringIndexer(inputCol=c, outputCol="{0}_indexed".
format(c))
             for c in categoricalCols ]

# default setting: dropLast=True
encoders = [ OneHotEncoder(inputCol=indexer.getOutputCol(),
                            outputCol="{0}_encoded".format(indexer.
getOutputCol()))
             for indexer in indexers ]

assembler = VectorAssembler(inputCols=[encoder.getOutputCol()].
for encoder in encoders]
                           + continuousCols, outputCol="features"
)

pipeline = Pipeline(stages=indexers + encoders + [assembler])

model=pipeline.fit(df)
data = model.transform(df)

return data.select(indexCol,'features')

```

```

# !!!!caution: not from pyspark.mllib.linalg import Vectors
from pyspark.ml.linalg import Vectors
from pyspark.ml import Pipeline
from pyspark.ml.feature import IndexToString,StringIndexer, VectorIndexer
from pyspark.ml.tuning import CrossValidator, ParamGridBuilder
from pyspark.ml.evaluation import MulticlassClassificationEvaluator

```

```

def transData(data):
    return data.rdd.map(lambda r: [Vectors.dense(r[:-1]),r[-1]]).toDF([
    'features','label'])

```

4. Transform the dataset to DataFrame

```

transformed = transData(df)
transformed.show(5)

```

features	label
----------	-------

(continues on next page)

(continued from previous page)

```
| [7.4,0.7,0.0,1.9,...|medium|
| [7.8,0.88,0.0,2.6...|medium|
| [7.8,0.76,0.04,2....|medium|
| [11.2,0.28,0.56,1...|medium|
| [7.4,0.7,0.0,1.9,...|medium|
+-----+
only showing top 5 rows
```

5. Deal with Categorical Label and Variables

```
# Index labels, adding metadata to the label column
labelIndexer = StringIndexer(inputCol='label',
                             outputCol='indexedLabel').fit(transformed)
labelIndexer.transform(transformed).show(5, True)
```

```
+-----+-----+-----+
|       features| label|indexedLabel|
+-----+-----+-----+
| [7.4,0.7,0.0,1.9,...|medium|      0.0|
| [7.8,0.88,0.0,2.6...|medium|      0.0|
| [7.8,0.76,0.04,2....|medium|      0.0|
| [11.2,0.28,0.56,1...|medium|      0.0|
| [7.4,0.7,0.0,1.9,...|medium|      0.0|
+-----+-----+-----+
only showing top 5 rows
```

```
# Automatically identify categorical features, and index them.
# Set maxCategories so features with > 4 distinct values are treated as
˓→continuous.
featureIndexer = VectorIndexer(inputCol="features", \
                                outputCol="indexedFeatures", \
                                maxCategories=4).fit(transformed)
featureIndexer.transform(transformed).show(5, True)
```

```
+-----+-----+-----+
|       features| label|     indexedFeatures|
+-----+-----+-----+
| [7.4,0.7,0.0,1.9,...|medium|[7.4,0.7,0.0,1.9,...|
| [7.8,0.88,0.0,2.6...|medium|[7.8,0.88,0.0,2.6...|
| [7.8,0.76,0.04,2....|medium|[7.8,0.76,0.04,2....|
| [11.2,0.28,0.56,1...|medium|[11.2,0.28,0.56,1...|
| [7.4,0.7,0.0,1.9,...|medium|[7.4,0.7,0.0,1.9,...|
+-----+-----+-----+
only showing top 5 rows
```

6. Split the data to training and test data sets

```
# Split the data into training and test sets (40% held out for testing)
(trainingData, testData) = transformed.randomSplit([0.6, 0.4])
```

(continues on next page)

(continued from previous page)

```
trainingData.show(5)
testData.show(5)
```

```
+-----+-----+
|       features| label|
+-----+-----+
|[4.6,0.52,0.15,2....| low|
|[4.7,0.6,0.17,2.3...|medium|
|[5.0,1.02,0.04,1....| low|
|[5.0,1.04,0.24,1....|medium|
|[5.1,0.585,0.0,1....| high|
+-----+-----+
only showing top 5 rows

+-----+-----+
|       features| label|
+-----+-----+
|[4.9,0.42,0.0,2.1...| high|
|[5.0,0.38,0.01,1....|medium|
|[5.0,0.4,0.5,4.3,...|medium|
|[5.0,0.42,0.24,2....| high|
|[5.0,0.74,0.0,1.2...|medium|
+-----+-----+
only showing top 5 rows
```

7. Fit Random Forest Classification Model

```
from pyspark.ml.classification import RandomForestClassifier

# Train a RandomForest model.
rf = RandomForestClassifier(labelCol="indexedLabel", featuresCol=
    "indexedFeatures", numTrees=10)
```

8. Pipeline Architecture

```
# Convert indexed labels back to original labels.
labelConverter = IndexToString(inputCol="prediction", outputCol=
    "predictedLabel",
    labels=labelIndexer.labels)

# Chain indexers and tree in a Pipeline
pipeline = Pipeline(stages=[labelIndexer, featureIndexer, rf, labelConverter])

# Train model. This also runs the indexers.
model = pipeline.fit(trainingData)
```

9. Make predictions

```
# Make predictions.
predictions = model.transform(testData)
```

(continues on next page)

(continued from previous page)

```
# Select example rows to display.
predictions.select("features", "label", "predictedLabel").show(5)
```

features	label	predictedLabel
[4.9, 0.42, 0.0, 2.1...]	high	high
[5.0, 0.38, 0.01, 1....]	medium	medium
[5.0, 0.4, 0.5, 4.3, ...]	medium	medium
[5.0, 0.42, 0.24, 2....]	high	medium
[5.0, 0.74, 0.0, 1.2...]	medium	medium

only showing top 5 rows

10. Evaluation

```
from pyspark.ml.evaluation import MulticlassClassificationEvaluator

# Select (prediction, true label) and compute test error
evaluator = MulticlassClassificationEvaluator(
    labelCol="indexedLabel", predictionCol="prediction", metricName="accuracy")
accuracy = evaluator.evaluate(predictions)
print("Test Error = %g" % (1.0 - accuracy))

rfModel = model.stages[-2]
print(rfModel) # summary only
```

```
Test Error = 0.173502
RandomForestClassificationModel (uid=rfc_a3395531f1d2) with 10 trees
```

11. visualization

```
import matplotlib.pyplot as plt
import numpy as np
import itertools

def plot_confusion_matrix(cm, classes,
                        normalize=False,
                        title='Confusion matrix',
                        cmap=plt.cm.Blues):

    """
    This function prints and plots the confusion matrix.
    Normalization can be applied by setting `normalize=True`.
    """
    if normalize:
        cm = cm.astype('float') / cm.sum(axis=1)[:, np.newaxis]
        print("Normalized confusion matrix")
    else:
        print('Confusion matrix, without normalization')

    plt.imshow(cm, interpolation='nearest', cmap=cmap)
    plt.title(title)
    plt.colorbar()
    tick_marks = np.arange(len(classes))
    plt.xticks(tick_marks, classes, rotation=45)
    plt.yticks(tick_marks, classes)

    fmt = '.2f' if normalize else 'd'
    thresh = cm.max() / 2.
    for i, j in itertools.product(range(cm.shape[0]), range(cm.shape[1])):
        plt.text(j, i, format(cm[i, j], fmt),
                 horizontalalignment="center",
                 verticalalignment="center")

    plt.tight_layout()
    plt.ylabel('True label')
    plt.xlabel('Predicted label')
```

(continues on next page)

(continued from previous page)

```
print(cm)

plt.imshow(cm, interpolation='nearest', cmap=cmap)
plt.title(title)
plt.colorbar()
tick_marks = np.arange(len(classes))
plt.xticks(tick_marks, classes, rotation=45)
plt.yticks(tick_marks, classes)

fmt = '.2f' if normalize else 'd'
thresh = cm.max() / 2.
for i, j in itertools.product(range(cm.shape[0]), range(cm.shape[1])):
    plt.text(j, i, format(cm[i, j], fmt),
             horizontalalignment="center",
             color="white" if cm[i, j] > thresh else "black")

plt.tight_layout()
plt.ylabel('True label')
plt.xlabel('Predicted label')
```

```
class_temp = predictions.select("label").groupBy("label") \
    .count().sort('count', ascending=False).toPandas()
class_temp = class_temp["label"].values.tolist()
class_names = map(str, class_temp)
# # print(class_name)
class_names
```

```
['medium', 'high', 'low']
```

```
from sklearn.metrics import confusion_matrix
y_true = predictions.select("label")
y_true = y_true.toPandas()

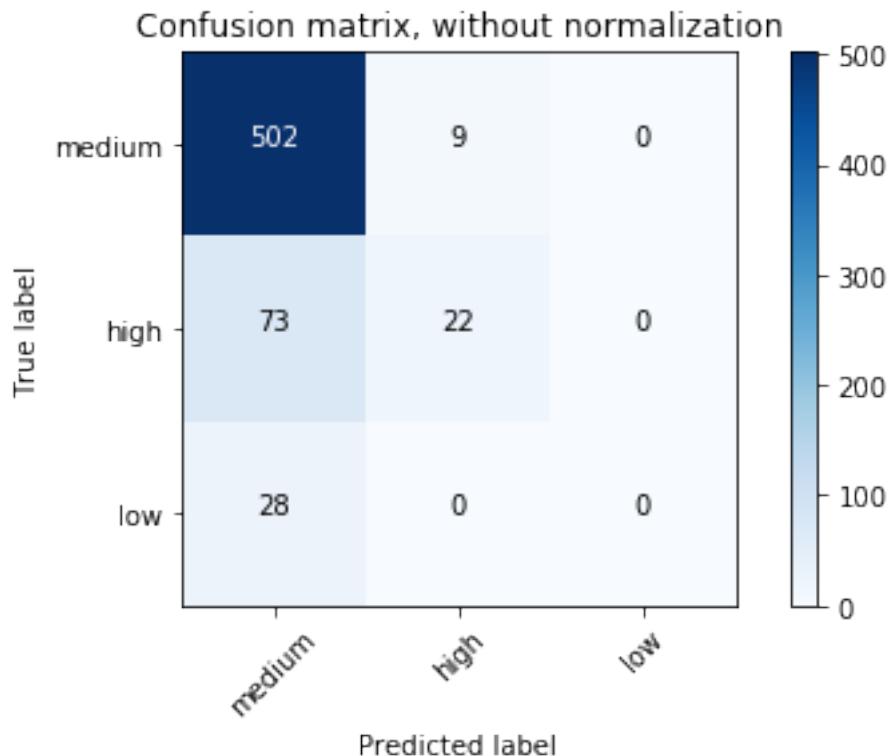
y_pred = predictions.select("predictedLabel")
y_pred = y_pred.toPandas()

cnf_matrix = confusion_matrix(y_true, y_pred, labels=class_names)
cnf_matrix
```

```
array([[502,    9,    0],
       [ 73,   22,    0],
       [ 28,    0,    0]])
```

```
# Plot non-normalized confusion matrix
plt.figure()
plot_confusion_matrix(cnf_matrix, classes=class_names,
                      title='Confusion matrix, without normalization')
plt.show()
```

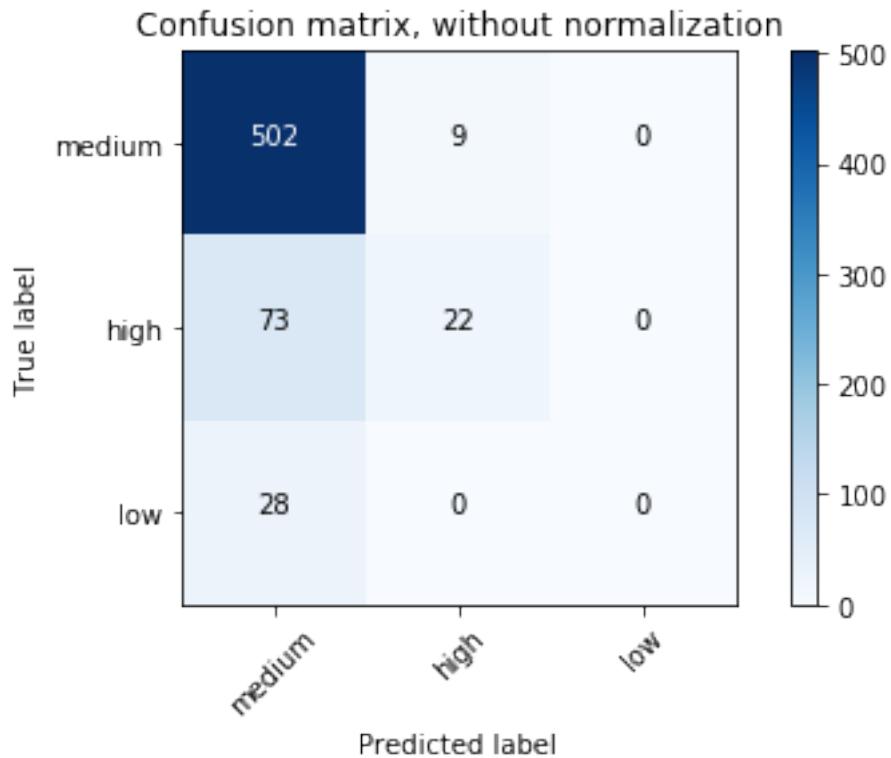
```
Confusion matrix, without normalization
[[502   9   0]
 [ 73  22   0]
 [ 28   0   0]]
```



```
# Plot normalized confusion matrix
plt.figure()
plot_confusion_matrix(cnf_matrix, classes=class_names, normalize=True,
                      title='Normalized confusion matrix')

plt.show()
```

```
Normalized confusion matrix
[[ 0.98238748  0.01761252  0.         ]
 [ 0.76842105  0.23157895  0.         ]
 [ 1.          0.          0.         ]]
```



10.5 Gradient-boosted tree Classification

10.5.1 Introduction

10.5.2 Demo

- The Jupyter notebook can be download from Gradient boosted tree Classification.
- For more details, please visit [GBTClassifier API](#).

Warning: Unfortunately, the GBTClassifier currently only supports binary labels.

10.6 XGBoost: Gradient-boosted tree Classification

10.6.1 Introduction

10.6.2 Demo

- The Jupyter notebook can be download from Gradient boosted tree Classification.
- For more details, please visit [GBTClassifier API](#).

Warning: Unfortunately, I didn't find a good way to setup the XGBoost directly in Spark. But I do get the XGBoost work with pysparkling on my machine.

1. Start H2O cluster inside the Spark environment

```
from pysparkling import *
hc = H2OContext.getOrCreate(spark)
```

```
Connecting to H2O server at http://192.168.0.102:54323... successful.
H2O cluster uptime:      07 secs
H2O cluster timezone:    America/Chicago
H2O data parsing timezone:    UTC
H2O cluster version:     3.22.1.3
H2O cluster version age:   20 days
H2O cluster name:        sparkling-water-dt216661_local-1550259209801
H2O cluster total nodes:  1
H2O cluster free memory: 848 Mb
H2O cluster total cores:  8
H2O cluster allowed cores: 8
H2O cluster status:      accepting new members, healthy
H2O connection url:     http://192.168.0.102:54323
H2O connection proxy:    None
H2O internal security:   False
H2O API Extensions:     XGBoost, Algos, AutoML, Core V3, Core V4
Python version:          3.7.1 final

Sparkling Water Context:
* H2O name: sparkling-water-dt216661_local-1550259209801
* cluster size: 1
* list of used nodes:
  (executorId, host, port)
  -----
  (driver, 192.168.0.102, 54323)
  -----
```

Open H2O Flow **in** browser: <http://192.168.0.102:54323> (CMD + click **in** Mac
→OSX)

2. Parse the data using H2O and convert them to Spark Frame

```
import h2o
frame = h2o.import_file("https://raw.githubusercontent.com/h2oai/sparkling-
water/master/examples/smalldata/prostate/prostate.csv")
spark_frame = hc.as_spark_frame(frame)
```

Parse progress: |██████████| 100%

```
spark_frame.show(4)
```

```
+---+-----+-----+-----+-----+-----+-----+
| ID | CAPSULE | AGE | RACE | DPROS | DCAPS | PSA | VOL | GLEASON |
+---+-----+-----+-----+-----+-----+-----+
| 1 | 0 | 65 | 1 | 2 | 1 | 1.4 | 0.0 | 6 |
| 2 | 0 | 72 | 1 | 3 | 2 | 6.7 | 0.0 | 7 |
| 3 | 0 | 70 | 1 | 1 | 2 | 4.9 | 0.0 | 6 |
| 4 | 0 | 76 | 2 | 2 | 1 | 51.2 | 20.0 | 7 |
+---+-----+-----+-----+-----+-----+
only showing top 4 rows
```

3. Train the model

```
from pysparkling.ml import H2OXGBoost
estimator = H2OXGBoost(predictionCol="AGE")
model = estimator.fit(spark_frame)
```

4. Run Predictions

```
predictions = model.transform(spark_frame)
predictions.show(4)
```

```
+---+-----+-----+-----+-----+-----+-----+-----+
| ID | CAPSULE | AGE | RACE | DPROS | DCAPS | PSA | VOL | GLEASON | prediction_output |
+---+-----+-----+-----+-----+-----+-----+-----+
| 1 | 0 | 65 | 1 | 2 | 1 | 1.4 | 0.0 | 6 | [64.85852813720703] |
| 2 | 0 | 72 | 1 | 3 | 2 | 6.7 | 0.0 | 7 | [72.0611801147461] |
| 3 | 0 | 70 | 1 | 1 | 2 | 4.9 | 0.0 | 6 | [70.26496887207031] |
| 4 | 0 | 76 | 2 | 2 | 1 | 51.2 | 20.0 | 7 | [75.26521301269531] |
+---+-----+-----+-----+-----+-----+-----+-----+
only showing top 4 rows
```

10.7 Naive Bayes Classification

10.7.1 Introduction

10.7.2 Demo

- The Jupyter notebook can be download from [Naive Bayes Classification](#).
- For more details, please visit [NaiveBayes API](#).

1. Set up spark context and SparkSession

```
from pyspark.sql import SparkSession

spark = SparkSession \
    .builder \
    .appName("Python Spark Naive Bayes classification") \
    .config("spark.some.config.option", "some-value") \
    .getOrCreate()
```

2. Load dataset

```
df = spark.read.format('com.databricks.spark.csv') \
    .options(header='true', inferSchema='true') \
    .load("./data/WineData2.csv", header=True);
df.show(5)
```

```
+----+-----+-----+-----+-----+-----+-----+-----+
|fixed|volatile|citric|sugar|chlorides|free|total|density| 
|pH|sulphates|alcohol|quality|
+----+-----+-----+-----+-----+-----+-----+-----+
| 7.4| 0.7| 0.0| 1.9| 0.076|11.0| 34.0| 0.9978|3.51| 0.56| 
| 9.4| 5| 
| 7.8| 0.88| 0.0| 2.6| 0.098|25.0| 67.0| 0.9968| 3.2| 0.68| 
| 9.8| 5| 
| 7.8| 0.76| 0.04| 2.3| 0.092|15.0| 54.0| 0.997|3.26| 0.65| 
| 9.8| 5| 
| 11.2| 0.28| 0.56| 1.9| 0.075|17.0| 60.0| 0.998|3.16| 0.58| 
| 9.8| 6| 
| 7.4| 0.7| 0.0| 1.9| 0.076|11.0| 34.0| 0.9978|3.51| 0.56| 
| 9.4| 5| 
+----+-----+-----+-----+-----+-----+-----+-----+
only showing top 5 rows
```

```
df.printSchema()
```

```
root
 |-- fixed: double (nullable = true)
 |-- volatile: double (nullable = true)
 |-- citric: double (nullable = true)
 |-- sugar: double (nullable = true)
 |-- chlorides: double (nullable = true)
 |-- free: double (nullable = true)
 |-- total: double (nullable = true)
 |-- density: double (nullable = true)
 |-- pH: double (nullable = true)
 |-- sulphates: double (nullable = true)
 |-- alcohol: double (nullable = true)
 |-- quality: string (nullable = true)
```

```
# Convert to float format
def string_to_float(x):
    return float(x)

#
def condition(r):
    if (0 <= r <= 6):
        label = "low"
```

(continues on next page)

(continued from previous page)

```

else:
    label = "high"
return label

from pyspark.sql.functions import udf
from pyspark.sql.types import StringType, DoubleType
string_to_float_udf = udf(string_to_float, DoubleType())
quality_udf = udf(lambda x: condition(x), StringType())

df = df.withColumn("quality", quality_udf("quality"))

df.show(5, True)

```

```

+-----+-----+-----+-----+-----+-----+-----+-----+
|fixed|volatile|citric|sugar|chlorides|free|total|density|
|pH|sulphates|alcohol|quality|
+-----+-----+-----+-----+-----+-----+-----+-----+
| 7.4| 0.7| 0.0| 1.9| 0.076|11.0| 34.0| 0.9978|3.51| 0.56|
| 9.4| medium|
| 7.8| 0.88| 0.0| 2.6| 0.098|25.0| 67.0| 0.9968| 3.2| 0.68|
| 9.8| medium|
| 7.8| 0.76| 0.04| 2.3| 0.092|15.0| 54.0| 0.997|3.26| 0.65|
| 9.8| medium|
| 11.2| 0.28| 0.56| 1.9| 0.075|17.0| 60.0| 0.998|3.16| 0.58|
| 9.8| medium|
| 7.4| 0.7| 0.0| 1.9| 0.076|11.0| 34.0| 0.9978|3.51| 0.56|
| 9.4| medium|
+-----+-----+-----+-----+-----+-----+-----+-----+
only showing top 5 rows

```

```
df.printSchema()
```

```

root
|-- fixed: double (nullable = true)
|-- volatile: double (nullable = true)
|-- citric: double (nullable = true)
|-- sugar: double (nullable = true)
|-- chlorides: double (nullable = true)
|-- free: double (nullable = true)
|-- total: double (nullable = true)
|-- density: double (nullable = true)
|-- pH: double (nullable = true)
|-- sulphates: double (nullable = true)
|-- alcohol: double (nullable = true)
|-- quality: string (nullable = true)

```

3. Deal with categorical data and Convert the data to dense vector

Note: You are strongly encouraged to try my get_dummy function for dealing with the categorical data in complex dataset.

Supervised learning version:

```
def get_dummy(df, indexCol, categoricalCols, continuousCols, labelCol):

    from pyspark.ml import Pipeline
    from pyspark.ml.feature import StringIndexer, OneHotEncoder,
    ↪VectorAssembler
    from pyspark.sql.functions import col

    indexers = [ StringIndexer(inputCol=c, outputCol="{0}_indexed".
    ↪format(c))
        for c in categoricalCols ]

    # default setting: dropLast=True
    encoders = [ OneHotEncoder(inputCol=indexer.getOutputCol(),
        outputCol="{0}_encoded".format(indexer.
    ↪getOutputCol())))
        for indexer in indexers ]

    assembler = VectorAssembler(inputCols=[encoder.getOutputCol()].
    ↪for encoder in encoders]
        + continuousCols, outputCol="features
    ↪")

    pipeline = Pipeline(stages=indexers + encoders + [assembler])

    model=pipeline.fit(df)
    data = model.transform(df)

    data = data.withColumn('label', col(labelCol))

    return data.select(indexCol, 'features', 'label')
```

Unsupervised learning version:

```
def get_dummy(df, indexCol, categoricalCols, continuousCols):
    '''

    Get dummy variables and concat with continuous variables for
    ↪unsupervised learning.
    :param df: the dataframe
    :param categoricalCols: the name list of the categorical data
    :param continuousCols: the name list of the numerical data
    :return k: feature matrix

    :author: Wenqiang Feng
    :email: von198@gmail.com
    '''

    indexers = [ StringIndexer(inputCol=c, outputCol="{0}_indexed".
    ↪format(c))
```

(continues on next page)

(continued from previous page)

```

        for c in categoricalCols ]

    # default setting: dropLast=True
    encoders = [ OneHotEncoder(inputCol=indexer.getOutputCol(),
                                outputCol="{0}_encoded".format(indexer.
→getOutputCol()))
                for indexer in indexers ]

    assembler = VectorAssembler(inputCols=[encoder.getOutputCol()_
→for encoder in encoders]
                                + continuousCols, outputCol="features"
→"})

    pipeline = Pipeline(stages=indexers + encoders + [assembler])

    model=pipeline.fit(df)
    data = model.transform(df)

    return data.select(indexCol, 'features')

```

```

def get_dummy(df,categoricalCols,continuousCols,labelCol):

    from pyspark.ml import Pipeline
    from pyspark.ml.feature import StringIndexer, OneHotEncoder,
→VectorAssembler
    from pyspark.sql.functions import col

    indexers = [ StringIndexer(inputCol=c, outputCol="{0}_indexed".format(c))
                 for c in categoricalCols ]

    # default setting: dropLast=True
    encoders = [ OneHotEncoder(inputCol=indexer.getOutputCol(),
                                outputCol="{0}_encoded".format(indexer.getOutputCol()))
                for indexer in indexers ]

    assembler = VectorAssembler(inputCols=[encoder.getOutputCol() for encoder_
→in encoders]
                                + continuousCols, outputCol="features")

    pipeline = Pipeline(stages=indexers + encoders + [assembler])

    model=pipeline.fit(df)
    data = model.transform(df)

    data = data.withColumn('label',col(labelCol))

    return data.select('features','label')

```

4. Transform the dataset to DataFrame

```

from pyspark.ml.linalg import Vectors # !!!!caution: not from pyspark.mllib.
from linalg import Vectors
from pyspark.ml import Pipeline
from pyspark.ml.feature import IndexToString, StringIndexer, VectorIndexer
from pyspark.ml.tuning import CrossValidator, ParamGridBuilder
from pyspark.ml.evaluation import MulticlassClassificationEvaluator

def transData(data):
    return data.rdd.map(lambda r: [Vectors.dense(r[:-1]), r[-1]]).toDF(['features',
    'label'])

```

```

transformed = transData(df)
transformed.show(5)

```

```

+-----+-----+
|      features|label|
+-----+-----+
|[7.4,0.7,0.0,1.9,...| low|
|[7.8,0.88,0.0,2.6...| low|
|[7.8,0.76,0.04,2....| low|
|[11.2,0.28,0.56,1...| low|
|[7.4,0.7,0.0,1.9,...| low|
+-----+-----+
only showing top 5 rows

```

4. Deal with Categorical Label and Variables

```

# Index labels, adding metadata to the label column
labelIndexer = StringIndexer(inputCol='label',
                             outputCol='indexedLabel').fit(transformed)
labelIndexer.transform(transformed).show(5, True)

```

```

+-----+-----+-----+
|      features|label|indexedLabel|
+-----+-----+-----+
|[7.4,0.7,0.0,1.9,...| low| 0.0|
|[7.8,0.88,0.0,2.6...| low| 0.0|
|[7.8,0.76,0.04,2....| low| 0.0|
|[11.2,0.28,0.56,1...| low| 0.0|
|[7.4,0.7,0.0,1.9,...| low| 0.0|
+-----+-----+-----+
only showing top 5 rows

```

```

# Automatically identify categorical features, and index them.
# Set maxCategories so features with > 4 distinct values are treated as
# continuous.
featureIndexer = VectorIndexer(inputCol="features", \
                                outputCol="indexedFeatures", \
                                maxCategories=4).fit(transformed)
featureIndexer.transform(transformed).show(5, True)

```

```
+-----+-----+-----+
|       features | label |      indexedFeatures |
+-----+-----+-----+
|[7.4,0.7,0.0,1.9,...] | low | [7.4,0.7,0.0,1.9,...]
|[7.8,0.88,0.0,2.6...] | low | [7.8,0.88,0.0,2.6...]
|[7.8,0.76,0.04,2....] | low | [7.8,0.76,0.04,2....]
|[11.2,0.28,0.56,1...] | low | [11.2,0.28,0.56,1...]
|[7.4,0.7,0.0,1.9,...] | low | [7.4,0.7,0.0,1.9,...]
+-----+-----+-----+
only showing top 5 rows
```

5. Split the data to training and test data sets

```
# Split the data into training and test sets (40% held out for testing)
(trainingData, testData) = data.randomSplit([0.6, 0.4])

trainingData.show(5, False)
testData.show(5, False)
```

```
+-----+-----+
| features                                | label |
+-----+-----+
|[5.0,0.38,0.01,1.6,0.048,26.0,60.0,0.99084,3.7,0.75,14.0] | low  |
|[5.0,0.42,0.24,2.0,0.06,19.0,50.0,0.9917,3.72,0.74,14.0] | high |
|[5.0,0.74,0.0,1.2,0.041,16.0,46.0,0.99258,4.01,0.59,12.5] | low  |
|[5.0,1.02,0.04,1.4,0.045,41.0,85.0,0.9938,3.75,0.48,10.5] | low  |
|[5.0,1.04,0.24,1.6,0.05,32.0,96.0,0.9934,3.74,0.62,11.5] | low  |
+-----+-----+
only showing top 5 rows
```

```
+-----+-----+
| features                                | label |
+-----+-----+
|[4.6,0.52,0.15,2.1,0.054,8.0,65.0,0.9934,3.9,0.56,13.1] | low  |
|[4.7,0.6,0.17,2.3,0.058,17.0,106.0,0.9932,3.85,0.6,12.9] | low  |
|[4.9,0.42,0.0,2.1,0.048,16.0,42.0,0.99154,3.71,0.74,14.0] | high |
|[5.0,0.4,0.5,4.3,0.046,29.0,80.0,0.9902,3.49,0.66,13.6] | low  |
|[5.2,0.49,0.26,2.3,0.09,23.0,74.0,0.9953,3.71,0.62,12.2] | low  |
+-----+-----+
only showing top 5 rows
```

6. Fit Naive Bayes Classification Model

```
from pyspark.ml.classification import NaiveBayes
nb = NaiveBayes(featuresCol='indexedFeatures', labelCol='indexedLabel')
```

7. Pipeline Architecture

```
# Convert indexed labels back to original labels.
labelConverter = IndexToString(inputCol="prediction", outputCol=
    "predictedLabel",
    labels=labelIndexer.labels)
```

```
# Chain indexers and tree in a Pipeline
pipeline = Pipeline(stages=[labelIndexer, featureIndexer, nb, labelConverter])
```

```
# Train model. This also runs the indexers.
model = pipeline.fit(trainingData)
```

8. Make predictions

```
# Make predictions.
predictions = model.transform(testData)
# Select example rows to display.
predictions.select("features", "label", "predictedLabel").show(5)
```

```
+-----+-----+-----+
|       features|label|predictedLabel|
+-----+-----+-----+
| [4.6,0.52,0.15,2....| low|      low|
| [4.7,0.6,0.17,2.3....| low|      low|
| [4.9,0.42,0.0,2.1....| high|      low|
| [5.0,0.4,0.5,4.3,...| low|      low|
| [5.2,0.49,0.26,2....| low|      low|
+-----+-----+-----+
only showing top 5 rows
```

9. Evaluation

```
from pyspark.ml.evaluation import MulticlassClassificationEvaluator

# Select (prediction, true label) and compute test error
evaluator = MulticlassClassificationEvaluator(
    labelCol="indexedLabel", predictionCol="prediction", metricName="accuracy"
)
accuracy = evaluator.evaluate(predictions)
print("Test Error = %g" % (1.0 - accuracy))
```

```
Test Error = 0.307339
```

```
lrModel = model.stages[2]
trainingSummary = lrModel.summary

# Obtain the objective per iteration
# objectiveHistory = trainingSummary.objectiveHistory
# print("objectiveHistory:")
# for objective in objectiveHistory:
#     print(objective)

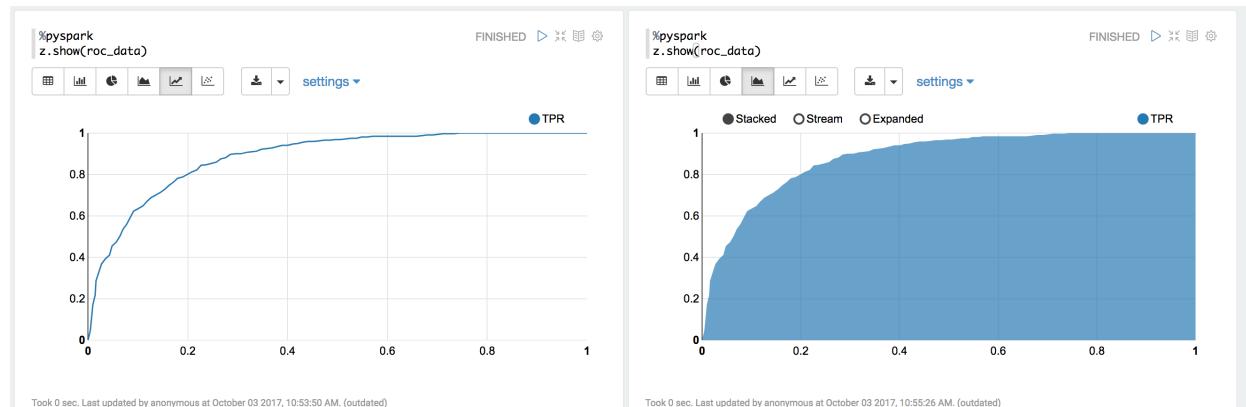
# Obtain the receiver-operating characteristic as a dataframe and
# areaUnderROC.
trainingSummary.roc.show(5)
print("areaUnderROC: " + str(trainingSummary.areaUnderROC))
```

(continues on next page)

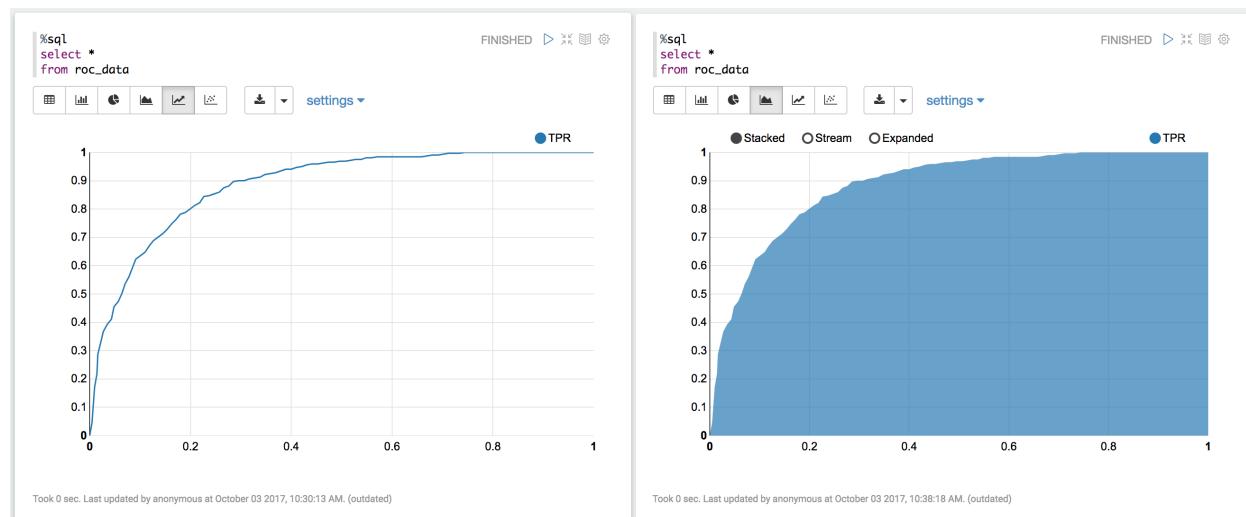
(continued from previous page)

```
# Set the model threshold to maximize F-Measure
fMeasure = trainingSummary.fMeasureByThreshold
maxFMeasure = fMeasure.groupBy().max('F-Measure').select('max(F-Measure)').head(5)
# bestThreshold = fMeasure.where(fMeasure['F-Measure'] == maxFMeasure['max(F-Measure)']) \
#     .select('threshold').head()['threshold']
# lr.setThreshold(bestThreshold)
```

You can use `z.show()` to get the data and plot the ROC curves:



You can also register a TempTable `data.registerTempTable('roc_data')` and then use `sql` to plot the ROC curve:



10. visualization

```
import matplotlib.pyplot as plt
import numpy as np
import itertools

def plot_confusion_matrix(cm, classes,
```

(continues on next page)

(continued from previous page)

```

        normalize=False,
        title='Confusion matrix',
        cmap=plt.cm.Blues):
"""

This function prints and plots the confusion matrix.
Normalization can be applied by setting `normalize=True`.
"""

if normalize:
    cm = cm.astype('float') / cm.sum(axis=1)[:, np.newaxis]
    print("Normalized confusion matrix")
else:
    print('Confusion matrix, without normalization')

print(cm)

plt.imshow(cm, interpolation='nearest', cmap=cmap)
plt.title(title)
plt.colorbar()
tick_marks = np.arange(len(classes))
plt.xticks(tick_marks, classes, rotation=45)
plt.yticks(tick_marks, classes)

fmt = '.2f' if normalize else 'd'
thresh = cm.max() / 2.
for i, j in itertools.product(range(cm.shape[0]), range(cm.shape[1])):
    plt.text(j, i, format(cm[i, j], fmt),
             horizontalalignment="center",
             color="white" if cm[i, j] > thresh else "black")

plt.tight_layout()
plt.ylabel('True label')
plt.xlabel('Predicted label')

```

```

class_temp = predictions.select("label").groupBy("label") \
    .count().sort('count', ascending=False).toPandas()
class_temp = class_temp["label"].values.tolist()
class_names = map(str, class_temp)
# # # print(class_name)
class_names

```

```
['low', 'high']
```

```

from sklearn.metrics import confusion_matrix
y_true = predictions.select("label")
y_true = y_true.toPandas()

y_pred = predictions.select("predictedLabel")
y_pred = y_pred.toPandas()

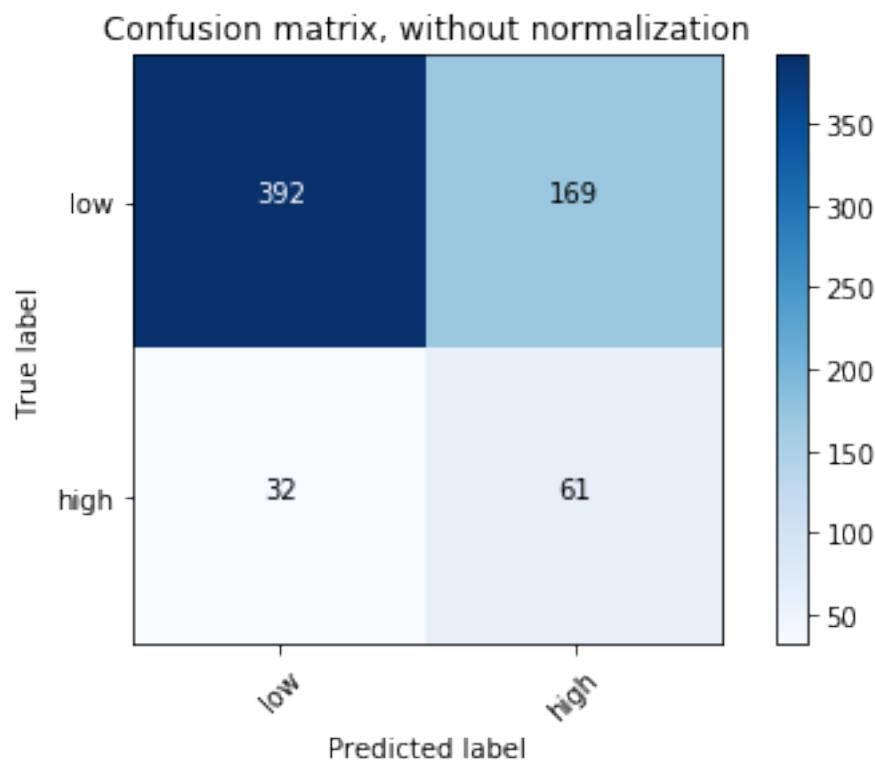
cnf_matrix = confusion_matrix(y_true, y_pred, labels=class_names)
cnf_matrix

```

```
array([[392, 169],  
       [ 32,   61]])
```

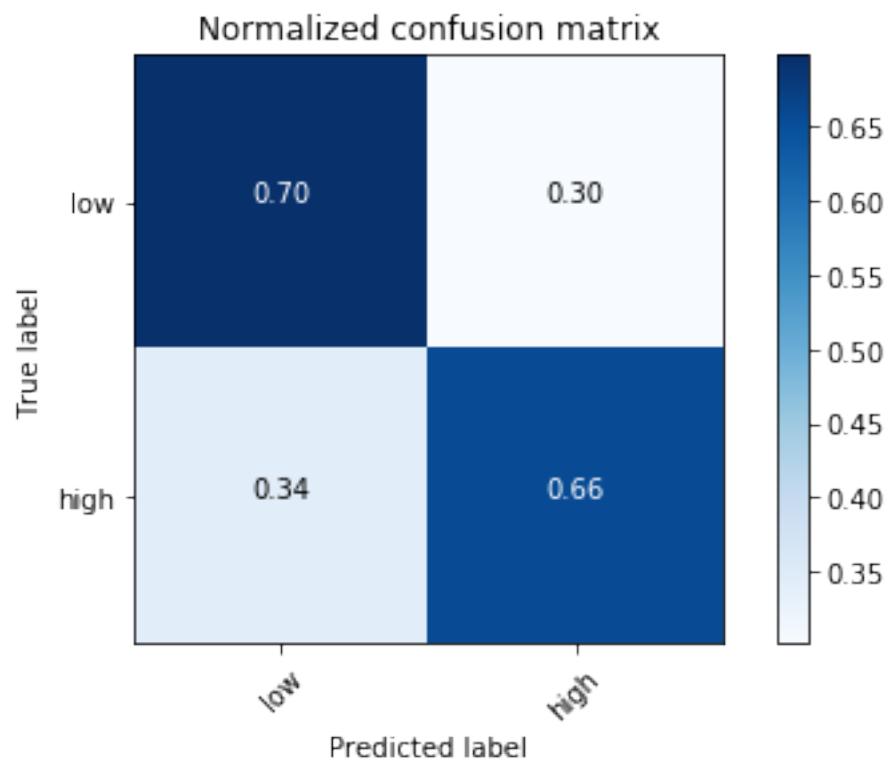
```
# Plot non-normalized confusion matrix  
plt.figure()  
plot_confusion_matrix(cnf_matrix, classes=class_names,  
                      title='Confusion matrix, without normalization')  
plt.show()
```

```
Confusion matrix, without normalization  
[[392 169]  
 [ 32  61]]
```



```
# Plot normalized confusion matrix  
plt.figure()  
plot_confusion_matrix(cnf_matrix, classes=class_names, normalize=True,  
                      title='Normalized confusion matrix')  
  
plt.show()
```

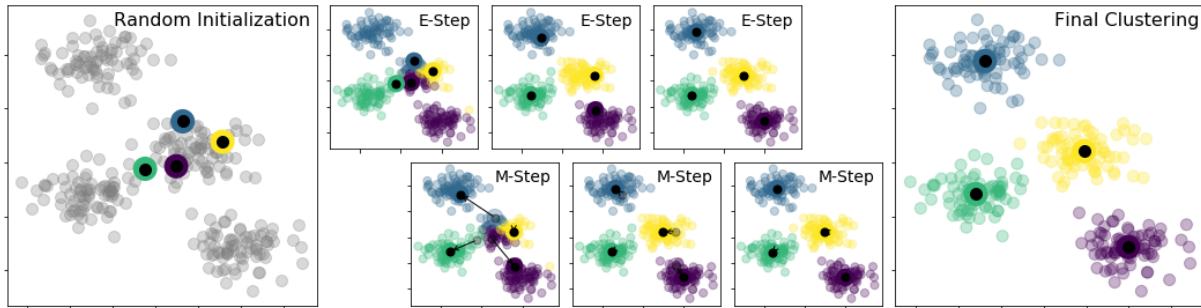
```
Normalized confusion matrix  
[[0.69875223 0.30124777]  
 [0.34408602 0.65591398]]
```



CLUSTERING

Chinese proverb

Sharpening the knife longer can make it easier to hack the firewood – old Chinese proverb



The above figure was generated by the code from: [Python Data Science Handbook](#).

11.1 K-Means Model

11.1.1 Introduction

k-means clustering is a method of vector quantization, originally from signal processing, that is popular for cluster analysis in data mining. The approach k-means follows to solve the problem is called **Expectation-Maximization**. It can be described as follows:

1. Assign some cluster centers
2. Repeated until converged
 - E-Step: assign points to the nearest center
 - M-step: set the cluster center to the mean

Given a set of observations (x_1, x_2, \dots, x_m) . The objective function is

$$J = \sum_{i=1}^m \sum_{k=1}^K w_{ik} \|x_i - c_k\|^2$$

where $w_{ik} = 1$ if x_i is in cluster k ; otherwise $w_{ik} = 0$ and c_k is the centroid of x_i 's cluster.

Mathematically, k-means is a minimization problem with two parts: First, we minimize J w.r.t w_{ik} with c_k fixed; Then minimize J w.r.t c_k with w_{ik} fixed. i.e.

E-step:

$$\frac{\partial J}{\partial w_{ik}} = \sum_{i=1}^m \sum_{k=1}^K \|x_i - c_k\|^2$$

$$\Rightarrow w_{ik} = \begin{cases} 1, & \text{if } k = \operatorname{argmin}_j \|x_i - c_j\|^2 \\ 0, & \text{otherwise} \end{cases}$$

M-step:

$$\frac{\partial J}{\partial c_k} = 2 \sum_{i=1}^m m w_{ik} (x_i - c_k) = 0 \Rightarrow c_k = \frac{\sum_{i=1}^m w_{ik} x_i}{\sum_{i=1}^m w_{ik}}$$

11.1.2 Demo

1. Set up spark context and SparkSession

```
from pyspark.sql import SparkSession

spark = SparkSession \
    .builder \
    .appName("Python Spark K-means example") \
    .config("spark.some.config.option", "some-value") \
    .getOrCreate()
```

2. Load dataset

```
df = spark.read.format('com.databricks.spark.csv') \
    .options(header='true', \
            inferSchema='true') \
    .load("../data/iris.csv", header=True);
```

check the data set

```
df.show(5, True)
df.printSchema()
```

Then you will get

sepal_length	sepal_width	petal_length	petal_width	species
5.1	3.5	1.4	0.2	setosa
4.9	3.0	1.4	0.2	setosa
4.7	3.2	1.3	0.2	setosa
4.6	3.1	1.5	0.2	setosa

(continues on next page)

(continued from previous page)

```
|      5.0|       3.6|       1.4|       0.2| setosa|
+-----+-----+-----+-----+
only showing top 5 rows

root
|-- sepal_length: double (nullable = true)
|-- sepal_width: double (nullable = true)
|-- petal_length: double (nullable = true)
|-- petal_width: double (nullable = true)
|-- species: string (nullable = true)
```

You can also get the Statistical results from the data frame (Unfortunately, it only works for numerical).

```
df.describe().show()
```

Then you will get

```
+-----+-----+-----+-----+
|summary|      sepal_length|      sepal_width|      petal_length|
|petal_width|  species|
+-----+-----+-----+-----+
| count |      150|      150|      150|
| mean |  5.84333333333335| 3.0540000000000007|3.7586666666666693|1.
| stddev| 0.8280661279778637|0.43359431136217375| 1.764420419952262|0.
| 7631607417008414|      null| | |
| min |      4.3|      2.0|      1.0|
| 0.1|  setosa|
| max |      7.9|      4.4|      6.9|
| 2.5|virginica|
+-----+-----+-----+-----+
```

3. Convert the data to dense vector (**features**)

```
# convert the data to dense vector
def transData(data):
    return data.rdd.map(lambda r: [Vectors.dense(r[:-1])]).toDF(['features'])
```

Note: You are strongly encouraged to try my `get_dummy` function for dealing with the categorical data in complex dataset.

Supervised learning version:

```
def get_dummy(df, indexCol, categoricalCols, continuousCols, labelCol):
    from pyspark.ml import Pipeline
```

(continues on next page)

(continued from previous page)

```

from pyspark.ml.feature import StringIndexer, OneHotEncoder,
→VectorAssembler
from pyspark.sql.functions import col

indexers = [ StringIndexer(inputCol=c, outputCol="{0}_indexed".
→format(c))
            for c in categoricalCols ]

# default setting: dropLast=True
encoders = [ OneHotEncoder(inputCol=indexer.getOutputCol(),
                           outputCol="{0}_encoded".format(indexer.
→getOutputCol()))
            for indexer in indexers ]

assembler = VectorAssembler(inputCols=[encoder.getOutputCol()].
→for encoder in encoders]
                           + continuousCols, outputCol="features
→")

pipeline = Pipeline(stages=indexers + encoders + [assembler])

model=pipeline.fit(df)
data = model.transform(df)

data = data.withColumn('label', col(labelCol))

return data.select(indexCol, 'features', 'label')

```

Unsupervised learning version:

```

def get_dummy(df, indexCol, categoricalCols, continuousCols):
    """
    Get dummy variables and concat with continuous variables for
    →unsupervised learning.
    :param df: the dataframe
    :param categoricalCols: the name list of the categorical data
    :param continuousCols: the name list of the numerical data
    :return k: feature matrix

    :author: Wenqiang Feng
    :email: von198@gmail.com
    """

    indexers = [ StringIndexer(inputCol=c, outputCol="{0}_indexed".
→format(c))
            for c in categoricalCols ]

    # default setting: dropLast=True
    encoders = [ OneHotEncoder(inputCol=indexer.getOutputCol(),
                               outputCol="{0}_encoded".format(indexer.
→getOutputCol()))
            for indexer in indexers ]

```

(continues on next page)

(continued from previous page)

```

assembler = VectorAssembler(inputCols=[encoder.getOutputCol()_  

    ↵for encoder in encoders]  

                                + continuousCols, outputCol="features  

    ↵")  
  

pipeline = Pipeline(stages=indexers + encoders + [assembler])  
  

model=pipeline.fit(df)  

data = model.transform(df)  
  

return data.select(indexCol, 'features')

```

4. Transform the dataset to DataFrame

```

transformed= transData(df)
transformed.show(5, False)

```

```

+-----+
| features      |
+-----+
|[5.1,3.5,1.4,0.2]|
|[4.9,3.0,1.4,0.2]|
|[4.7,3.2,1.3,0.2]|
|[4.6,3.1,1.5,0.2]|
|[5.0,3.6,1.4,0.2]|
+-----+
only showing top 5 rows

```

5. Deal With Categorical Variables

```

from pyspark.ml import Pipeline
from pyspark.ml.regression import LinearRegression
from pyspark.ml.feature import VectorIndexer
from pyspark.ml.evaluation import RegressionEvaluator

# Automatically identify categorical features, and index them.
# We specify maxCategories so features with > 4 distinct values are treated
    ↵as continuous.

featureIndexer = VectorIndexer(inputCol="features", \
                                outputCol="indexedFeatures", \
                                maxCategories=4).fit(transformed)

data = featureIndexer.transform(transformed)

```

Now you check your dataset with

```
data.show(5, True)
```

you will get

```
+-----+-----+
|       features| indexedFeatures|
+-----+-----+
|[5.1,3.5,1.4,0.2]| [5.1,3.5,1.4,0.2] |
|[4.9,3.0,1.4,0.2]| [4.9,3.0,1.4,0.2] |
|[4.7,3.2,1.3,0.2]| [4.7,3.2,1.3,0.2] |
|[4.6,3.1,1.5,0.2]| [4.6,3.1,1.5,0.2] |
|[5.0,3.6,1.4,0.2]| [5.0,3.6,1.4,0.2] |
+-----+-----+
only showing top 5 rows
```

Note: Since clustering algorithms including k-means use distance-based measurements to determine the similarity between data points, It's strongly recommended to standardize the data to have a mean of zero and a standard deviation of one.

6. Elbow method to determine the optimal number of clusters for k-means clustering

```
import numpy as np
cost = np.zeros(20)
for k in range(2,20):
    kmeans = KMeans() \
        .setK(k) \
        .setSeed(1) \
        .setFeaturesCol("indexedFeatures") \
        .setPredictionCol("cluster")

model = kmeans.fit(data)
cost[k] = model.computeCost(data) # requires Spark 2.0 or later
```

```
import numpy as np
import matplotlib.mlab as mlab
import matplotlib.pyplot as plt
import seaborn as sns
from matplotlib.ticker import MaxNLocator

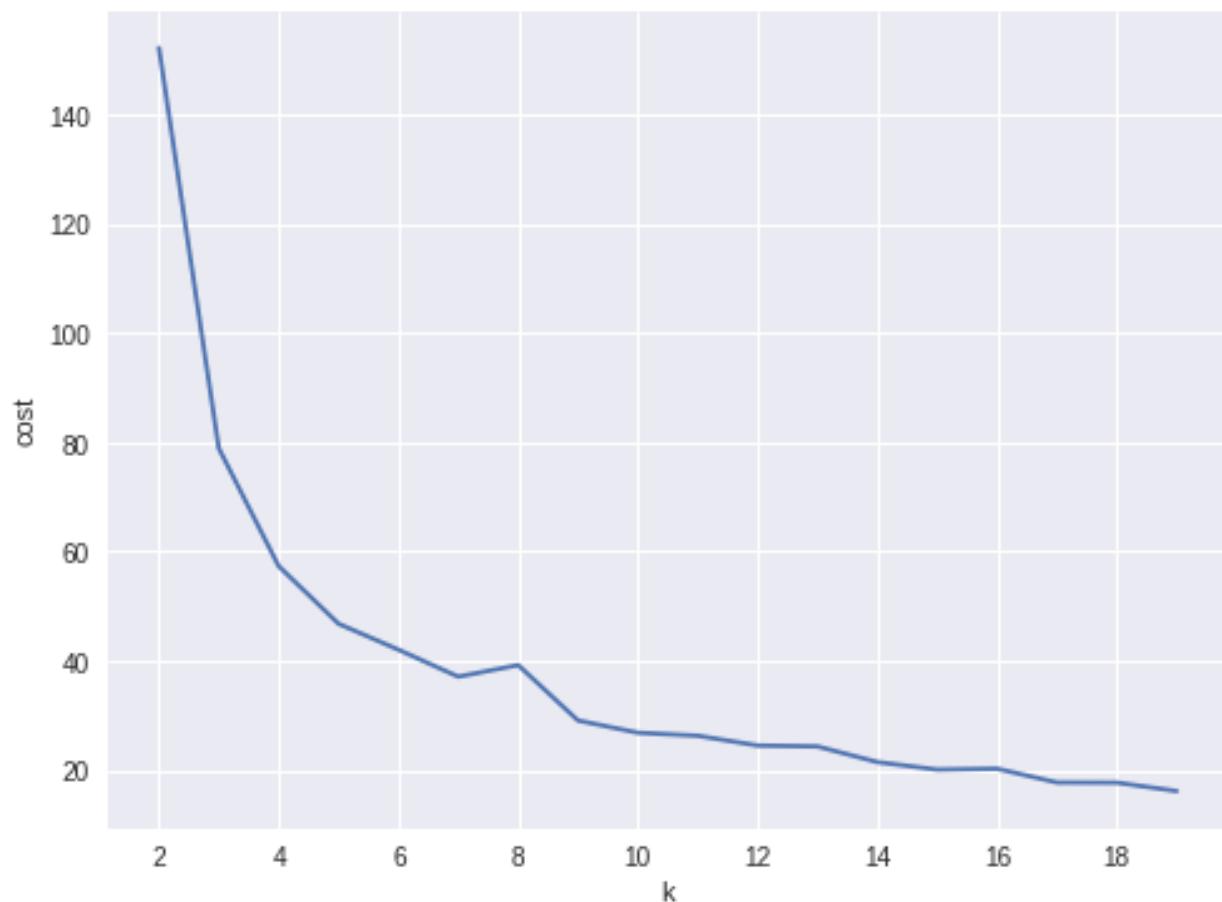
fig, ax = plt.subplots(1,1, figsize =(8,6))
ax.plot(range(2,20),cost[2:20])
ax.set_xlabel('k')
ax.set_ylabel('cost')
ax.xaxis.set_major_locator(MaxNLocator(integer=True))
plt.show()
```

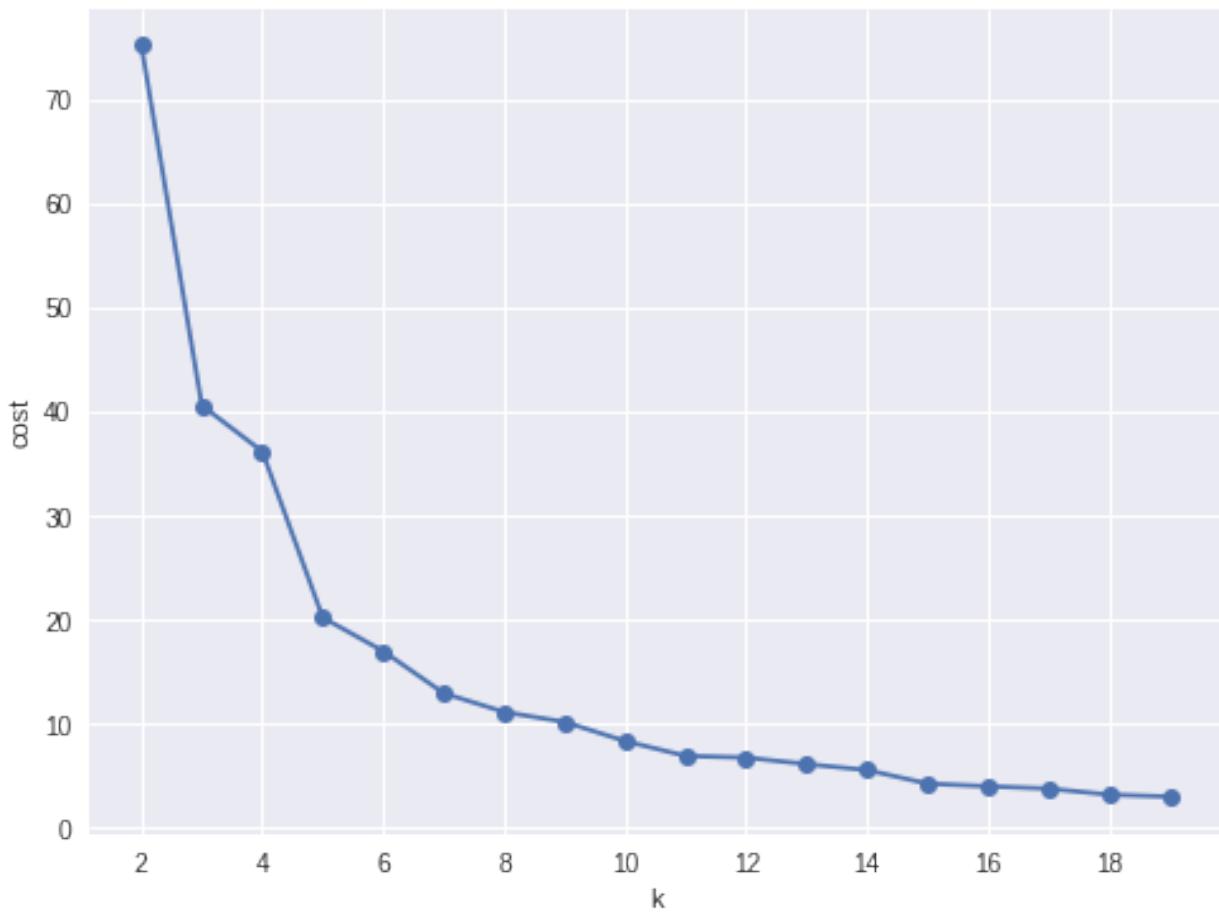
In my opinion, sometimes it's hard to choose the optimal number of the clusters by using the elbow method. As shown in the following Figure, you can choose 3, 5 or even 8. I will choose 3 in this demo.

- Silhouette analysis

```
#PySpark libraries
from pyspark.ml import Pipeline
from pyspark.ml.feature import StringIndexer, OneHotEncoder, VectorAssembler
```

(continues on next page)





(continued from previous page)

```

from pyspark.sql.functions import col, percent_rank, lit
from pyspark.sql.window import Window
from pyspark.sql import DataFrame, Row
from pyspark.sql.types import StructType
from functools import reduce # For Python 3.x

from pyspark.ml.clustering import KMeans
from pyspark.ml.evaluation import ClusteringEvaluator

def optimal_k(df_in, index_col, k_min, k_max, num_runs):
    """
    Determine optimal number of clusters by using Silhouette Score Analysis.
    :param df_in: the input dataframe
    :param index_col: the name of the index column
    :param k_min: the train dataset
    :param k_min: the minimum number of the clusters
    :param k_max: the maximum number of the clusters
    :param num_runs: the number of runs for each fixed clusters

    :return k: optimal number of the clusters
    :return silh_lst: Silhouette score
    :return r_table: the running results table

    :author: Wenqiang Feng
    :email: von198@gmail.com
    """

    start = time.time()
    silh_lst = []
    k_lst = np.arange(k_min, k_max+1)

    r_table = df_in.select(index_col).toPandas()
    r_table = r_table.set_index(index_col)
    centers = pd.DataFrame()

    for k in k_lst:
        silh_val = []
        for run in np.arange(1, num_runs+1):

            # Trains a k-means model.
            kmeans = KMeans() \
                .setK(k) \
                .setSeed(int(np.random.randint(100, size=1)))
            model = kmeans.fit(df_in)

            # Make predictions
            predictions = model.transform(df_in)
            r_table['cluster_{k}_{run}'.format(k=k, run=run)] = predictions
        select('prediction').toPandas()

            # Evaluate clustering by computing Silhouette score
        evaluator = ClusteringEvaluator()

```

(continues on next page)

(continued from previous page)

```
silhouette = evaluator.evaluate(predictions)
silh_val.append(silhouette)

silh_array=np.asarray(silh_val)
silh_lst.append(silh_array.mean())

elapsed = time.time() - start

silhouette = pd.DataFrame(list(zip(k_lst,silh_lst)),columns = ['k',
˓→'silhouette'])

print('+'-----+')
print("|      The finding optimal k phase took %8.0f s.      |"
˓→%elapsed)
print('+'-----+')

return k_lst[np.argmax(silh_lst, axis=0)], silhouette , r_table
```

```
k, silh_lst, r_table = optimal_k(scaledData,index_col,k_min, k_max,num_runs)

+-----+
|      The finding optimal k phase took      1783 s.      |
+-----+
```

```
spark.createDataFrame(silh_lst).show()

+---+-----+
|   k|      silhouette|
+---+-----+
|   3|0.8045154385557953|
|   4|0.6993528775512052|
|   5|0.6689286654221447|
|   6|0.6356184024841809|
|   7|0.7174102265711756|
|   8|0.6720861758298997|
|   9| 0.601771359881241|
|  10|0.6292447334578428|
+---+-----+
```

From the silhouette list, we can choose 3 as the optimal number of the clusters.

Warning: ClusteringEvaluator in pyspark.ml.evaluation requires Spark 2.4 or later!!

7. Pipeline Architecture

```
from pyspark.ml.clustering import KMeans, KMeansModel

kmeans = KMeans() \
```

(continues on next page)

(continued from previous page)

```

.setK(3) \
.setFeaturesCol("indexedFeatures") \
.setPredictionCol("cluster")

# Chain indexer and tree in a Pipeline
pipeline = Pipeline(stages=[featureIndexer, kmeans])

model = pipeline.fit(transformed)

cluster = model.transform(transformed)

```

8. k-means clusters

```
cluster = model.transform(transformed)
```

features	indexedFeatures	cluster
[5.1, 3.5, 1.4, 0.2]	[5.1, 3.5, 1.4, 0.2]	1
[4.9, 3.0, 1.4, 0.2]	[4.9, 3.0, 1.4, 0.2]	1
[4.7, 3.2, 1.3, 0.2]	[4.7, 3.2, 1.3, 0.2]	1
[4.6, 3.1, 1.5, 0.2]	[4.6, 3.1, 1.5, 0.2]	1
[5.0, 3.6, 1.4, 0.2]	[5.0, 3.6, 1.4, 0.2]	1
[5.4, 3.9, 1.7, 0.4]	[5.4, 3.9, 1.7, 0.4]	1
[4.6, 3.4, 1.4, 0.3]	[4.6, 3.4, 1.4, 0.3]	1
[5.0, 3.4, 1.5, 0.2]	[5.0, 3.4, 1.5, 0.2]	1
[4.4, 2.9, 1.4, 0.2]	[4.4, 2.9, 1.4, 0.2]	1
[4.9, 3.1, 1.5, 0.1]	[4.9, 3.1, 1.5, 0.1]	1
[5.4, 3.7, 1.5, 0.2]	[5.4, 3.7, 1.5, 0.2]	1
[4.8, 3.4, 1.6, 0.2]	[4.8, 3.4, 1.6, 0.2]	1
[4.8, 3.0, 1.4, 0.1]	[4.8, 3.0, 1.4, 0.1]	1
[4.3, 3.0, 1.1, 0.1]	[4.3, 3.0, 1.1, 0.1]	1
[5.8, 4.0, 1.2, 0.2]	[5.8, 4.0, 1.2, 0.2]	1
[5.7, 4.4, 1.5, 0.4]	[5.7, 4.4, 1.5, 0.4]	1
[5.4, 3.9, 1.3, 0.4]	[5.4, 3.9, 1.3, 0.4]	1
[5.1, 3.5, 1.4, 0.3]	[5.1, 3.5, 1.4, 0.3]	1
[5.7, 3.8, 1.7, 0.3]	[5.7, 3.8, 1.7, 0.3]	1
[5.1, 3.8, 1.5, 0.3]	[5.1, 3.8, 1.5, 0.3]	1

only showing top 20 rows

**CHAPTER
TWELVE**

RFM ANALYSIS

Segment	RFM	Description	Marketing
Best Customers	111	Bought most recently and most often, and spend the most	No price incentives, new products, and loyalty programs
Loyal Customers	X1X	Buy most frequently	Use R and M to further segment
Big Spenders	XX1	Spend the most	Market your most expensive products
Almost Lost	311	Haven't purchased for some time, but purchased frequently and spend the most	Aggressive price incentives
Lost Customers	411	Haven't purchased for some time, but purchased frequently and spend the most	Aggressive price incentives
Lost Cheap Customers	444	Last purchased long ago, purchased few, and spent little	Don't spend too much trying to re-acquire

The above figure source: Blast Analytics Marketing

RFM is a method used for analyzing customer value. It is commonly used in database marketing and direct marketing and has received particular attention in retail and professional services industries. More details

can be found at Wikipedia [RFM_wikipedia](#).

RFM stands for the three dimensions:

- Recency – How recently did the customer purchase? i.e. Duration since last purchase
- Frequency – How often do they purchase? i.e. Total number of purchases
- Monetary Value – How much do they spend? i.e. Total money this customer spent

12.1 RFM Analysis Methodology

RFM Analysis contains three main steps:

12.1.1 1. Build the RFM features matrix for each customer

CustomerID	Recency	Frequency	Monetary
14911	1	248	132572.62
12748	0	224	29072.1
17841	1	169	40340.78
14606	1	128	11713.85
15311	0	118	59419.34

only showing top 5 rows

12.1.2 2. Determine cutting points for each feature

CustomerID	Recency	Frequency	Monetary	r_seg	f_seg	m_seg
17420	50	3	598.83	2	3	2
16861	59	3	151.65	3	3	1
16503	106	5	1421.43	3	2	3
15727	16	7	5178.96	1	1	4
17389	0	43	31300.08	1	1	4

only showing top 5 rows

12.1.3 3. Determine the RFM scores and summarize the corresponding business value

CustomerID	Recency	Frequency	Monetary	r_seg	f_seg	m_seg	RFMScore

(continues on next page)

(continued from previous page)

	17988	11	8	191.17	1	1	1	111
	16892	1	7	496.84	1	1	2	112
	16668	15	6	306.72	1	1	2	112
	16554	3	7	641.55	1	1	2	112
	16500	4	6	400.86	1	1	2	112
+-----+-----+-----+-----+-----+-----+-----+								
only showing top 5 rows								

The corresponding business description and marketing value:

Segment	RFM	Description	Marketing
Best Customers	111	Bought most recently and most often, and spend the most	No price incentives, new products, and loyalty programs
Loyal Customers	X1X	Buy most frequently	Use R and M to further segment
Big Spenders	XX1	Spend the most	Market your most expensive products
Almost Lost	311	Haven't purchased for some time, but purchased frequently and spend the most	Aggressive price incentives
Lost Customers	411	Haven't purchased for some time, but purchased frequently and spend the most	Aggressive price incentives
Lost Cheap Customers	444	Last purchased long ago, purchased few, and spent little	Don't spend too much trying to re-acquire

Fig. 1: Source: Blast Analytics Marketing

12.2 Demo

- The Jupyter notebook can be download from Data Exploration.
- The data can be downloaf from [German Credit](#).

12.2.1 Load and clean data

1. Set up spark context and SparkSession

```
from pyspark.sql import SparkSession

spark = SparkSession \
    .builder \
    .appName("Python Spark RFM example") \
    .config("spark.some.config.option", "some-value") \
    .getOrCreate()
```

2. Load dataset

```
df_raw = spark.read.format('com.databricks.spark.csv') \
    .options(header='true', \
    inferschema='true') \
    .load("Online Retail.csv", header=True);
```

check the data set

```
df_raw.show(5)
df_raw.printSchema()
```

Then you will get

InvoiceNo	StockCode	Description	Quantity	InvoiceDate	UnitPrice	CustomerID	Country
536365	85123A	WHITE HANGING HEA...	6	12/1/10 8:26	2.55		
17850		United Kingdom					
536365	71053	WHITE METAL LANTERN	6	12/1/10 8:26	3.39		
17850		United Kingdom					
536365	84406B	CREAM CUPID HEART...	8	12/1/10 8:26	2.75		
17850		United Kingdom					
536365	84029G	KNITTED UNION FLA...	6	12/1/10 8:26	3.39		
17850		United Kingdom					
536365	84029E	RED WOOLLY HOTTIE...	6	12/1/10 8:26	3.39		
17850		United Kingdom					

only showing top 5 rows

(continues on next page)

(continued from previous page)

```

root
|-- InvoiceNo: string (nullable = true)
|-- StockCode: string (nullable = true)
|-- Description: string (nullable = true)
|-- Quantity: integer (nullable = true)
|-- InvoiceDate: string (nullable = true)
|-- UnitPrice: double (nullable = true)
|-- CustomerID: integer (nullable = true)
|-- Country: string (nullable = true)

```

3. Data clean and data manipulation

- check and remove the null values

```

from pyspark.sql.functions import count

def my_count(df_in):
    df_in.agg( *[ count(c).alias(c) for c in df_in.columns ] ).show()

```

```
my_count(df_raw)
```

```

+-----+-----+-----+-----+-----+-----+
|InvoiceNo|StockCode|Description|Quantity|InvoiceDate|UnitPrice|CustomerID|Country|
+-----+-----+-----+-----+-----+-----+
|      541909 |  541909 |      540455 |   541909 |      541909 |   541909 |  406829 |  _ 
|      541909 |
+-----+-----+-----+-----+-----+-----+
|      406829 |  406829 |      406829 |   406829 |      406829 |   406829 |  406829 |  _ 
|      406829 |
+-----+-----+-----+-----+-----+-----+

```

Since the count results are not the same, we have some null value in the CustomerID column. We can drop these records from the dataset.

```

df = df_raw.dropna(how='any')
my_count(df)

```

```

+-----+-----+-----+-----+-----+-----+
|InvoiceNo|StockCode|Description|Quantity|InvoiceDate|UnitPrice|CustomerID|Country|
+-----+-----+-----+-----+-----+-----+
|      406829 |  406829 |      406829 |   406829 |      406829 |   406829 |  406829 |  _ 
|      406829 |
+-----+-----+-----+-----+-----+-----+

```

- Dealwith the InvoiceDate

```
from pyspark.sql.functions import to_utc_timestamp, unix_timestamp, lit, u
datediff, col

timeFmt = "MM/dd/yy HH:mm"

df = df.withColumn('NewInvoiceDate'
    , to_utc_timestamp(unix_timestamp(col('InvoiceDate'),
    timeFmt).cast('timestamp')
    , 'UTC'))
```

```
df.show(5)
```

```
+-----+-----+-----+-----+-----+
| InvoiceNo | StockCode | Description | Quantity | 
| InvoiceDate | UnitPrice | CustomerID | Country | NewInvoiceDate |
+-----+-----+-----+-----+-----+
| 536365 | 85123A | WHITE HANGING HEA... | 6 | 12/1/10 8:26 | 2.55 |
| 17850 | United Kingdom | 2010-12-01 08:26:... |
| 536365 | 71053 | WHITE METAL LANTERN | 6 | 12/1/10 8:26 | 3.39 |
| 17850 | United Kingdom | 2010-12-01 08:26:... |
| 536365 | 84406B | CREAM CUPID HEART... | 8 | 12/1/10 8:26 | 2.75 |
| 17850 | United Kingdom | 2010-12-01 08:26:... |
| 536365 | 84029G | KNITTED UNION FLA... | 6 | 12/1/10 8:26 | 3.39 |
| 17850 | United Kingdom | 2010-12-01 08:26:... |
| 536365 | 84029E | RED WOOLLY HOTTIE... | 6 | 12/1/10 8:26 | 3.39 |
| 17850 | United Kingdom | 2010-12-01 08:26:... |
+-----+-----+-----+-----+-----+
only showing top 5 rows
```

Warning: The spark is pretty sensitive to the date format!

- calculate total price

```
from pyspark.sql.functions import round

df = df.withColumn('TotalPrice', round(df.Quantity * df.UnitPrice, 2))
```

- calculate the time difference

```
from pyspark.sql.functions import mean, min, max, sum, datediff, to_date

date_max = df.select(max('NewInvoiceDate')).toPandas()
current = to_utc_timestamp(unix_timestamp(lit(str(date_max.iloc[0][0])), \
'yy-MM-dd HH:mm').cast('timestamp'), 'UTC')

# Calculatre Duration
df = df.withColumn('Duration', datediff(lit(current), 'NewInvoiceDate'))
```

- build the Recency, Frequency and Monetary

```
recency = df.groupBy('CustomerID').agg(min('Duration').alias('Recency'))
frequency = df.groupBy('CustomerID', 'InvoiceNo').count() \
    .groupBy('CustomerID') \
    .agg(count('*').alias("Frequency"))
monetary = df.groupBy('CustomerID').agg(round(sum('TotalPrice'), 2).alias(
    'Monetary'))
rfm = recency.join(frequency, 'CustomerID', how = 'inner') \
    .join(monetary, 'CustomerID', how = 'inner')
```

```
rfm.show(5)
```

CustomerID	Recency	Frequency	Monetary
17420	50	3	598.83
16861	59	3	151.65
16503	106	5	1421.43
15727	16	7	5178.96
17389	0	43	31300.08

only showing top 5 rows

12.2.2 RFM Segmentation

4. Determine cutting points

In this section, you can use the techniques (statistical results and visualizations) in *Data Exploration* section to help you determine the cutting points for each attribute. In my opinion, the cutting points are mainly depend on the business sense. You's better talk to your makrting people and get feedback and suggestion from them. I will use the quantile as the cutting points in this demo.

```
cols = ['Recency', 'Frequency', 'Monetary']
describe_pd(rfm, cols, 1)
```

summary	Recency	Frequency	Monetary
count	4372.0	4372.0	4372.0
mean	91.58119853613907	5.07548032936871	1898.4597003659655
stddev	100.7721393138483	9.338754163574727	8219.345141139722
min	0.0	1.0	-4287.63
max	373.0	248.0	279489.02
25%	16.0	1.0	293.36249999999995
50%	50.0	3.0	648.075
75%	143.0	5.0	1611.725

The user defined function by using the cutting points:

```

def RScore(x):
    if x <= 16:
        return 1
    elif x<= 50:
        return 2
    elif x<= 143:
        return 3
    else:
        return 4

def FScore(x):
    if x <= 1:
        return 4
    elif x <= 3:
        return 3
    elif x <= 5:
        return 2
    else:
        return 1

def MScore(x):
    if x <= 293:
        return 4
    elif x <= 648:
        return 3
    elif x <= 1611:
        return 2
    else:
        return 1

from pyspark.sql.functions import udf
from pyspark.sql.types import StringType, DoubleType

R_udf = udf(lambda x: RScore(x), StringType())
F_udf = udf(lambda x: FScore(x), StringType())
M_udf = udf(lambda x: MScore(x), StringType())

```

5. RFM Segmentation

```

rfm_seg = rfm.withColumn("r_seg", R_udf("Recency"))
rfm_seg = rfm_seg.withColumn("f_seg", F_udf("Frequency"))
rfm_seg = rfm_seg.withColumn("m_seg", M_udf("Monetary"))
rfm_seg.show(5)

```

CustomerID	Recency	Frequency	Monetary	r_seg	f_seg	m_seg
17420	50	3	598.83	2	3	2
16861	59	3	151.65	3	3	1
16503	106	5	1421.43	3	2	3
15727	16	7	5178.96	1	1	4
17389	0	43	31300.08	1	1	4

(continues on next page)

(continued from previous page)

```
+-----+-----+-----+-----+-----+
only showing top 5 rows
```

```
rfm_seg = rfm_seg.withColumn('RFMScore',
                             F.concat(F.col('r_seg'), F.col('f_seg'), F.col('m_
                             seg'))))
rfm_seg.sort(F.col('RFMScore')).show(5)
```

```
+-----+-----+-----+-----+-----+-----+
|CustomerID|Recency|Frequency|Monetary|r_seg|f_seg|m_seg|RFMScore|
+-----+-----+-----+-----+-----+-----+
|    17988|     11|        8|   191.17|     1|     1|     1|     111|
|    16892|      1|        7|   496.84|     1|     1|     2|     112|
|    16668|     15|        6|   306.72|     1|     1|     2|     112|
|    16554|      3|        7|   641.55|     1|     1|     2|     112|
|    16500|      4|        6|   400.86|     1|     1|     2|     112|
+-----+-----+-----+-----+-----+-----+
only showing top 5 rows
```

12.2.3 Statistical Summary

6. Statistical Summary

- simple summary

```
rfm_seg.groupBy('RFMScore')\
    .agg({'Recency': 'mean',
          'Frequency': 'mean',
          'Monetary': 'mean'})\
    .sort(F.col('RFMScore')).show(5)
```

```
+-----+-----+-----+-----+
|RFMScore| avg(Recency) | avg(Monetary) | avg(Frequency) |
+-----+-----+-----+-----+
|    111|       11.0|      191.17|        8.0|
|    112|       8.0|      505.9775|        7.5|
| 113| 7.237113402061856| 1223.3604123711339| 7.752577319587629|
| 114| 6.035123966942149| 8828.888595041324| 18.882231404958677|
|    121|       9.6|      207.24|        4.4|
+-----+-----+-----+-----+
only showing top 5 rows
```

- complex summary

```
grp = 'RFMScore'
num_cols = ['Recency', 'Frequency', 'Monetary']
df_input = rfm_seg

quantile_grouped = quantile_agg(df_input, grp, num_cols)
```

(continues on next page)

(continued from previous page)

```
quantile_grouped.toPandas().to_csv(output_dir+'quantile_grouped.csv')  
  
deciles_grouped = deciles_agg(df_input,grp,num_cols)  
deciles_grouped.toPandas().to_csv(output_dir+'deciles_grouped.csv')
```

12.3 Extension

You can also apply the K-means clustering in *Clustering* section to do the segmentation.

12.3.1 Build feature matrix

1. build dense feature matrix

```
from pyspark.sql import Row  
from pyspark.ml.linalg import Vectors  
  
# method 1 (good for small feature):  
def transData(row):  
    #     return Row(label=row["Sales"],  
    #                 features=Vectors.dense([row["TV"],  
    #                                         row["Radio"],  
    #                                         row["Newspaper"]]))  
  
# Method 2 (good for large features):  
def transData(data):  
    return data.rdd.map(lambda r: [r[0], Vectors.dense(r[1:])]).toDF([  
    'CustomerID', 'rfm'])
```

```
transformed= transData(rfm)  
transformed.show(5)
```

```
+-----+-----+  
|CustomerID|      rfm|  
+-----+-----+  
| 17420| [50.0,3.0,598.83]|  
| 16861| [59.0,3.0,151.65]|  
| 16503| [106.0,5.0,1421.43]|  
| 15727| [16.0,7.0,5178.96]|  
| 17389| [0.0,43.0,31300.08]|  
+-----+-----+  
only showing top 5 rows
```

2. Scaler the feature matrix

```
from pyspark.ml.feature import MinMaxScaler  
  
scaler = MinMaxScaler(inputCol="rfm", \
```

(continues on next page)

(continued from previous page)

```
        outputCol="features")
scalerModel = scaler.fit(transformed)
scaledData = scalerModel.transform(transformed)
scaledData.show(5, False)
```

```
+-----+-----+
|CustomerID | rfm           | features
+-----+-----+
|17420      | [50.0, 3.0, 598.83] | [0.13404825737265416, 0.008097165991902834, 0.
|01721938714830836] |
|16861      | [59.0, 3.0, 151.65]  | [0.1581769436997319, 0.008097165991902834, 0.
|01564357039241953] |
|16503      | [106.0, 5.0, 1421.43] | [0.28418230563002683, 0.016194331983805668, 0.
|02011814573186342] |
|15727      | [16.0, 7.0, 5178.96]  | [0.04289544235924933, 0.024291497975708502, 0.
|03335929858922501] |
|17389      | [0.0, 43.0, 31300.08] | [0.0, 0.1700404858299595, 0.12540746393334334] |
+-----+-----+
only showing top 5 rows
```

12.3.2 K-means clustering

3. Find optimal number of cluster

I will present two popular ways to determine the optimal number of the cluster.

- elbow analysis

```
#PySpark libraries
from pyspark.ml import Pipeline
from pyspark.ml.feature import StringIndexer, OneHotEncoder, VectorAssembler
from pyspark.sql.functions import col, percent_rank, lit
from pyspark.sql.window import Window
from pyspark.sql import DataFrame, Row
from pyspark.sql.types import StructType
from functools import reduce # For Python 3.x

from pyspark.ml.clustering import KMeans
#from pyspark.ml.evaluation import ClusteringEvaluator # requires Spark 2.4
#or later

import numpy as np
cost = np.zeros(20)
for k in range(2,20):
    kmeans = KMeans() \
```

(continues on next page)

(continued from previous page)

```
.setK(k) \
.setSeed(1) \
.setFeaturesCol("features") \
.setPredictionCol("cluster")

model = kmeans.fit(scaledData)
cost[k] = model.computeCost(scaledData) # requires Spark 2.0 or later
```

```
import numpy as np
import matplotlib.mlab as mlab
import matplotlib.pyplot as plt
import seaborn as sns
from matplotlib.ticker import MaxNLocator

fig, ax = plt.subplots(1,1, figsize =(8,6))
ax.plot(range(2,20),cost[2:20], marker = "o")
ax.set_xlabel('k')
ax.set_ylabel('cost')
ax.xaxis.set_major_locator(MaxNLocator(integer=True))
plt.show()
```

In my opinion, sometimes it's hard to choose the number of the clusters. As shown in Figure *Cost v.s. the number of the clusters*, you can choose 3, 5 or even 8. I will choose 3 in this demo.

- Silhouette analysis

```
#PySpark libraries
from pyspark.ml import Pipeline
from pyspark.ml.feature import StringIndexer, OneHotEncoder, VectorAssembler
from pyspark.sql.functions import col, percent_rank, lit
from pyspark.sql.window import Window
from pyspark.sql import DataFrame, Row
from pyspark.sql.types import StructType
from functools import reduce # For Python 3.x

from pyspark.ml.clustering import KMeans
from pyspark.ml.evaluation import ClusteringEvaluator

def optimal_k(df_in,index_col,k_min, k_max,num_runs):
    """
    Determine optimal number of clusters by using Silhouette Score Analysis.
    :param df_in: the input dataframe
    :param index_col: the name of the index column
    :param k_min: the train dataset
    :param k_min: the minimum number of the clusters
    :param k_max: the maximum number of the clusters
    :param num_runs: the number of runs for each fixed clusters

    :return k: optimal number of the clusters
    :return silh_lst: Silhouette score
    :return r_table: the running results table
    """

    return k, silh_lst, r_table
```

(continues on next page)

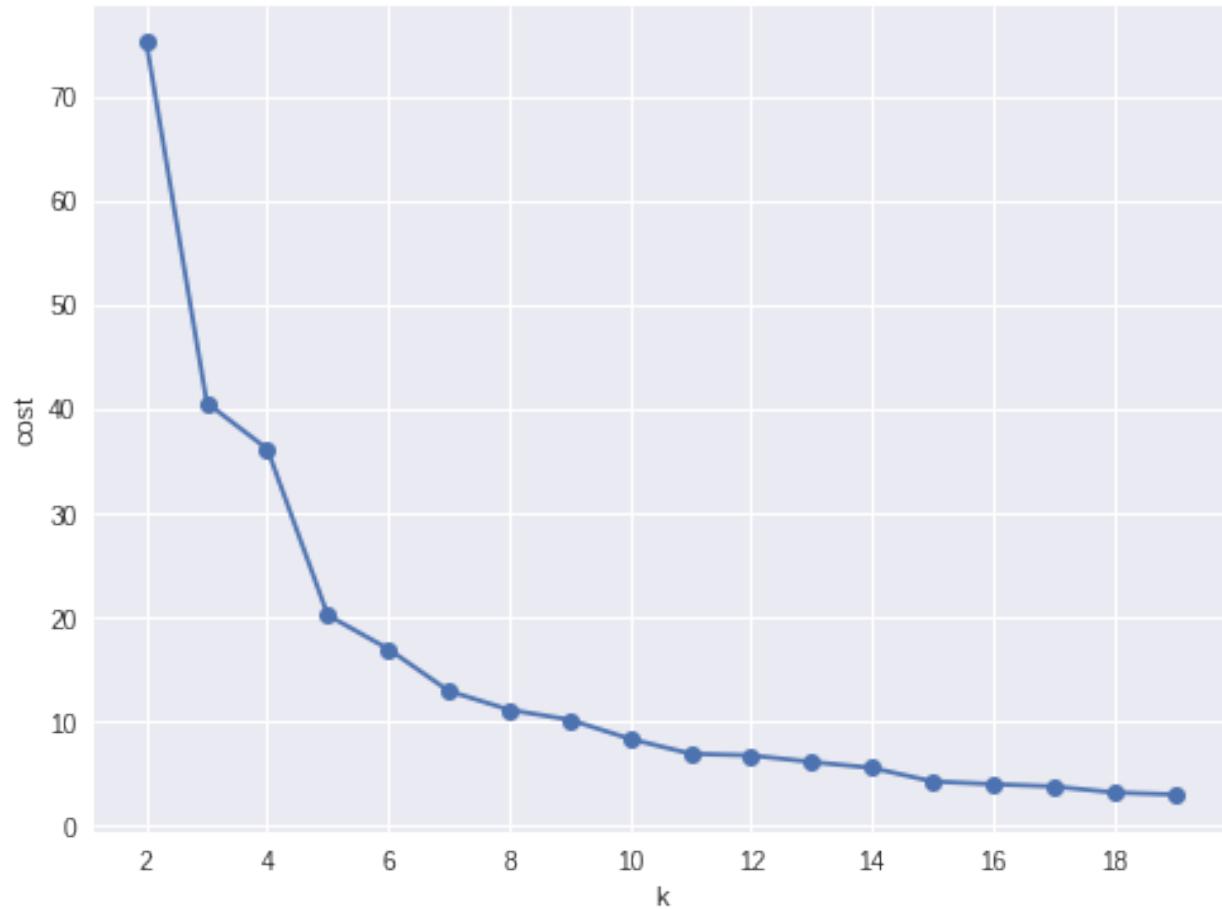


Fig. 2: Cost v.s. the number of the clusters

(continued from previous page)

```

:author: Wenqiang Feng
:email: von198@gmail.com.com
''

start = time.time()
silh_lst = []
k_lst = np.arange(k_min, k_max+1)

r_table = df_in.select(index_col).toPandas()
r_table = r_table.set_index(index_col)
centers = pd.DataFrame()

for k in k_lst:
    silh_val = []
    for run in np.arange(1, num_runs+1):

        # Trains a k-means model.
        kmeans = KMeans() \
            .setK(k) \
            .setSeed(int(np.random.randint(100, size=1)))
        model = kmeans.fit(df_in)

        # Make predictions
        predictions = model.transform(df_in)
        r_table['cluster_{k}_{run}'.format(k=k, run=run)] = predictions.
→select('prediction').toPandas()

        # Evaluate clustering by computing Silhouette score
        evaluator = ClusteringEvaluator()
        silhouette = evaluator.evaluate(predictions)
        silh_val.append(silhouette)

    silh_array=np.asanyarray(silh_val)
    silh_lst.append(silh_array.mean())

elapsed = time.time() - start

silhouette = pd.DataFrame(list(zip(k_lst,silh_lst)),columns = ['k',
→'silhouette'])

print('+'-----+')
print("|       The finding optimal k phase took %8.0f s.      |"
→%(elapsed))
print('+'-----+')

return k_lst[np.argmax(silh_lst, axis=0)], silhouette , r_table

```

```
k, silh_lst, r_table = optimal_k(scaledData,index_col,k_min, k_max,num_runs)
```

(continues on next page)

(continued from previous page)

```
+-----+
|       The finding optimal k phase took      1783 s.      |
+-----+
```

```
spark.createDataFrame(silh_lst).show()
```

```
+----+-----+
|   k |     silhouette|
+----+-----+
|  3 | 0.8045154385557953|
|  4 | 0.6993528775512052|
|  5 | 0.6689286654221447|
|  6 | 0.6356184024841809|
|  7 | 0.7174102265711756|
|  8 | 0.6720861758298997|
|  9 | 0.601771359881241|
| 10 | 0.6292447334578428|
+----+-----+
```

From the silhouette list, we can choose 3 as the optimal number of the clusters.

Warning: ClusteringEvaluator in pyspark.ml.evaluation requires Spark 2.4 or later!!

4. K-means clustering

```
k = 3
kmeans = KMeans().setK(k).setSeed(1)
model = kmeans.fit(scaledData)
# Make predictions
predictions = model.transform(scaledData)
predictions.show(5, False)
```

```
+-----+-----+-----+-----+
|CustomerID|          rfm|        features|prediction|
+-----+-----+-----+-----+
|    17420| [50.0,3.0,598.83]| [0.13404825737265...|      0|
|    16861| [59.0,3.0,151.65]| [0.15817694369973...|      0|
|    16503|[106.0,5.0,1421.43]| [0.28418230563002...|      2|
|    15727|[16.0,7.0,5178.96]| [0.04289544235924...|      0|
|    17389|[0.0,43.0,31300.08]| [0.0,0.1700404858...|      0|
+-----+-----+-----+-----+
only showing top 5 rows
```

12.3.3 Statistical summary

5. statistical summary

```
results = rfm.join(predictions.select('CustomerID','prediction'), 'CustomerID',
                     how='left')
results.show(5)
```

```
+-----+-----+-----+-----+
|CustomerID|Recency|Frequency|Monetary|prediction|
+-----+-----+-----+-----+
|      13098|     1|      41| 28658.88|      0|
|      13248|    124|      2|   465.68|      2|
|      13452|    259|      2|   590.0|      1|
|      13460|     29|      2|   183.44|      0|
|      13518|     85|      1|   659.44|      0|
+-----+-----+-----+-----+
only showing top 5 rows
```

- simple summary

```
results.groupBy('prediction')\
    .agg({'Recency': 'mean',
          'Frequency': 'mean',
          'Monetary': 'mean'})\
    .sort(F.col('prediction')).show(5)
```

```
+-----+-----+-----+
|prediction| avg(Recency) | avg(Monetary) | avg(Frequency) |
+-----+-----+-----+
|      0|30.966337980278816|2543.0355321319284| 6.514450867052023|
|      1|296.02403846153845|407.16831730769206|1.5592948717948718|
|      2|154.40148698884758| 702.5096406443623| 2.550185873605948|
+-----+-----+-----+
```

- complex summary

```
grp = 'RFMScore'
num_cols = ['Recency', 'Frequency', 'Monetary']
df_input = results

quantile_grouped = quantile_agg(df_input, grp, num_cols)
quantile_grouped.toPandas().to_csv(output_dir+'quantile_grouped.csv')

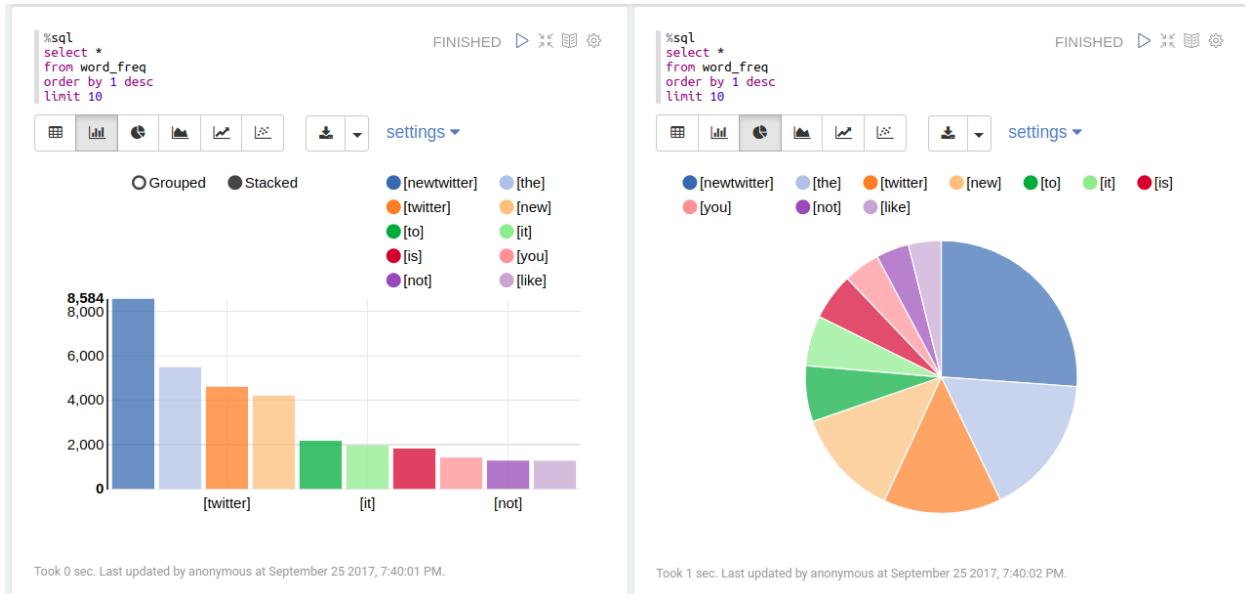
deciles_grouped = deciles_agg(df_input, grp, num_cols)
deciles_grouped.toPandas().to_csv(output_dir+'deciles_grouped.csv')
```

CHAPTER THIRTEEN

TEXT MINING

Chinese proverb

Articles showed more than intended. – Xianglong Shen



13.1 Text Collection

13.1.1 Image to text

- My img2txt function

```
def img2txt(img_dir):  
    """  
    convert images to text  
    """  
    import os, PythonMagick
```

(continues on next page)

(continued from previous page)

```
from datetime import datetime
import PyPDF2

from PIL import Image
import pytesseract

f = open('doc4img.txt', 'wa')
for img in [img_file for img_file in os.listdir(img_dir)
            if (img_file.endswith('.png') or
                img_file.endswith('.jpg') or
                img_file.endswith('.jpeg'))]:
    start_time = datetime.now()

    input_img = img_dir + "/" + img

    print('-----')
    print(img)
    print('Converting ' + img + '.....')
    print('-----')

# extract the text information from images
text = pytesseract.image_to_string(Image.open(input_img))
print(text)

# output text file
f.write(img + "\n")
f.write(text.encode('utf-8'))

print "CPU Time for converting" + img + ":" + str(datetime.now() - start_time) + "\n"
f.write("\n-----\n")

f.close()
```

- Demo

I applied my img2txt function to the image in Image folder.

```
image_dir = r"Image"

img2txt(image_dir)
```

Then I got the following results:

```
-----
feng.pdf_0.png
Converting feng.pdf_0.png.....
```

(continues on next page)

(continued from previous page)

```
-----
l I l w
```

Wenqiang Feng
Data Scientist
DST APPLIED ANALYTICS GROUP

Wenqiang Feng is Data Scientist **for** DST's Applied Analytics Group. Dr. Feng's responsibilities include providing DST clients with access to cutting--edge skills and technologies, including Big Data analytic solutions, advanced analytic and data enhancement techniques and modeling.

Dr. Feng has deep analytic expertise in data mining, analytic systems, machine learning algorithms, business intelligence, and applying Big Data tools to strategically solve industry problems in a cross--functional business. Before joining the DST Applied Analytics Group, Dr. Feng holds a MA Data Science Fellow at The Institute **for** Mathematics and Its Applications (IMA) at the University of Minnesota. While there, he helped startup companies make marketing decisions based on deep predictive analytics.

Dr. Feng graduated from University of Tennessee, Knoxville with PhD in Computational mathematics and Master's degree in Statistics. He also holds Master's degree in Computational Mathematics at Missouri University of Science and Technology (MST) and Master's degree in Applied Mathematics at University of science and technology of China (USTC). CPU Time **for** convertingfeng.pdf_0.png:0:00:02.061208

13.1.2 Image Enhanced to text

- My img2txt_enhance function

```
def img2txt_enhance(img_dir,scaler):
    """
    convert images files to text
    """

    import numpy as np
    import os, PythonMagick
    from datetime import datetime
    import PyPDF2
```

(continues on next page)

(continued from previous page)

```

from PIL import Image, ImageEnhance, ImageFilter
import pytesseract

f = open('doc4img.txt', 'wa')
for img in [img_file for img_file in os.listdir(img_dir)
            if (img_file.endswith(".png") or
                img_file.endswith(".jpg") or
                img_file.endswith(".jpeg"))]:
    start_time = datetime.now()

    input_img = img_dir + "/" + img
    enhanced_img = img_dir + "/" + "Enhanced" + "/" + img

    im = Image.open(input_img) # the second one
    im = im.filter(ImageFilter.MedianFilter())
    enhancer = ImageEnhance.Contrast(im)
    im = enhancer.enhance(1)
    im = im.convert('1')
    im.save(enhanced_img)

    for scale in np.ones(scaler):
        im = Image.open(enhanced_img) # the second one
        im = im.filter(ImageFilter.MedianFilter())
        enhancer = ImageEnhance.Contrast(im)
        im = enhancer.enhance(scale)
        im = im.convert('1')
        im.save(enhanced_img)

    print('-----')
    print(img)
    print('Converting ' + img + '.....')
    print('-----')
    print()

# extract the text information from images
text = pytesseract.image_to_string(Image.open(enhanced_img))
print(text)

# output text file
f.write(img + "\n")
f.write(text.encode('utf-8'))

print("CPU Time for converting" + img + ":" + str(datetime.now() - start_time) + "\n"
      f.write("\n-----\n"))

```

(continues on next page)

(continued from previous page)

```
f.close()
```

- Demo

I applied my `img2txt_enhance` function to the following noised image in `Enhance` folder.



```
image_dir = r"Enhance"  
pdf2txt_enhance(image_dir)
```

Then I got the following results:

```
-----  
noised.jpg  
Converting noised.jpg.....  
-----  
zHHH  
CPU Time for convertingnoised.jpg:0:00:00.135465
```

while the result from `img2txt` function is

```
-----  
noised.jpg  
Converting noised.jpg.....  
-----  
,2 WW  
CPU Time for convertingnoised.jpg:0:00:00.133508
```

which is not correct.

13.1.3 PDF to text

- My `pdf2txt` function

```
def pdf2txt(pdf_dir,image_dir):  
    """  
    convert PDF to text  
    """  
  
    import os, PythonMagick  
    from datetime import datetime  
    import PyPDF2
```

(continues on next page)

(continued from previous page)

```

from PIL import Image
import pytesseract

f = open('doc.txt', 'wa')
for pdf in [pdf_file for pdf_file in os.listdir(pdf_dir) if pdf_file.endswith('.pdf')]:
    start_time = datetime.now()

    input_pdf = pdf_dir + "/" + pdf

    pdf_im = PyPDF2.PdfFileReader(file(input_pdf, "rb"))
    npage = pdf_im.getNumPages()

    print('-----')
    print(pdf)
    print('Converting %d pages.' % npage)
    print('-----')

    f.write( "\n-----\n")

    for p in range(npage):
        pdf_file = input_pdf + '[' + str(p) + ']'
        image_file = image_dir + "/" + pdf + '_' + str(p) + '.png'

        # convert PDF files to Images
        im = PythonMagick.Image()
        im.density('300')
        im.read(pdf_file)
        im.write(image_file)

        # extract the text information from images
        text = pytesseract.image_to_string(Image.open(image_file))

        #print(text)

        # ouput text file
        f.write( pdf + "\n")
        f.write(text.encode('utf-8'))

    print("CPU Time for converting" + pdf + ":" + str(datetime.now() - start_time) + "\n"

f.close()

```

- Demo

I applied my pdf2txt function to my scanned bio pdf file in pdf folder.

```
pdf_dir = r"pdf"
image_dir = r"Image"

pdf2txt(pdf_dir, image_dir)
```

Then I got the following results:

```
-----
feng.pdf
Converting 1 pages.
-----
l l w

Wenqiang Feng
Data Scientist
DST APPLIED ANALYTICS GROUP

Wenqiang Feng is Data Scientist for DST's Applied Analytics Group. Dr. Feng's responsibilities include providing DST clients with access to cutting--edge skills and technologies, including Big Data analytic solutions, advanced analytic and data enhancement techniques and modeling. Dr. Feng has deep analytic expertise in data mining, analytic systems, machine learning algorithms, business intelligence, and applying Big Data tools to strategically solve industry problems in a cross--functional business. Before joining the DST Applied Analytics Group, Dr. Feng holds a MA Data Science Fellow at The Institute for Mathematics and Its Applications (IMA) at the University of Minnesota. While there, he helped startup companies make marketing decisions based on deep predictive analytics. Dr. Feng graduated from University of Tennessee, Knoxville with PhD in Computational mathematics and Master's degree in Statistics. He also holds Master's degree in Computational Mathematics at Missouri University of Science and Technology (MST) and Master's degree in Applied Mathematics at University of science and technology of China (USTC). CPU Time for convertingfeng.pdf:0:00:03.143800
```

13.1.4 Audio to text

- My audio2txt function

```
def audio2txt(audio_dir):
    ''' convert audio to text'''

    import speech_recognition as sr
    r = sr.Recognizer()

    f = open('doc.txt', 'w')
    for audio_n in [audio_file for audio_file in os.listdir(audio_dir) \
                    if audio_file.endswith(".wav")]:
        filename = audio_dir + "/" + audio_n

        # Read audio data
        with sr.AudioFile(filename) as source:
            audio = r.record(source) # read the entire audio file

        # Google Speech Recognition
        text = r.recognize_google(audio)

        # output text file
        f.write( audio_n + ": ")
        f.write(text.encode('utf-8'))
        f.write("\n")

    print('You said: ' + text)

f.close()
```

- Demo

I applied my audio2txt function to my audio records in audio folder.

```
audio_dir = r"audio"

audio2txt(audio_dir)
```

Then I got the following results:

```
You said: hello this is George welcome to my tutorial
You said: mathematics is important in daily life
You said: call me tomorrow
You said: do you want something to eat
You said: I want to speak with him
You said: nice to see you
You said: can you speak slowly
You said: have a good day
```

By the way, you can use my following python code to record your own audio and play with audio2txt function in Command-line python record.py "demo2.wav":

```
import sys, getopt
```

(continues on next page)

(continued from previous page)

```
import speech_recognition as sr

audio_filename = sys.argv[1]

r = sr.Recognizer()
with sr.Microphone() as source:
    r.adjust_for_ambient_noise(source)
    print("Hey there, say something, I am recording!")
    audio = r.listen(source)
    print("Done listening!")

with open(audio_filename, "wb") as f:
    f.write(audio.get_wav_data())
```

13.2 Text Preprocessing

- check to see if a row only contains whitespace

```
def check_blanks(data_str):
    is_blank = str(data_str.isspace())
    return is_blank
```

- Determine whether the language of the text content is english or not: Use langid module to classify the language to make sure we are applying the correct cleanup actions for English langid

```
def check_lang(data_str):
    predict_lang = langid.classify(data_str)
    if predict_lang[1] >= .9:
        language = predict_lang[0]
    else:
        language = 'NA'
    return language
```

- Remove features

```
def remove_features(data_str):
    # compile regex
    url_re = re.compile('https?://(www.)?\w+\.\w+(/(\w+)*)/?')
    punc_re = re.compile('[%s]' % re.escape(string.punctuation))
    num_re = re.compile('(\d+)')
    mention_re = re.compile('@(\w+)')
    alpha_num_re = re.compile("^[a-z0-9_.]+$")
    # convert to lowercase
    data_str = data_str.lower()
    # remove hyperlinks
    data_str = url_re.sub(' ', data_str)
    # remove @mentions
    data_str = mention_re.sub(' ', data_str)
    # remove punctuation
```

(continues on next page)

(continued from previous page)

```

data_str = punc_re.sub(' ', data_str)
# remove numeric 'words'
data_str = num_re.sub(' ', data_str)
# remove non a-z 0-9 characters and words shorter than 3 characters
list_pos = 0
cleaned_str = ''
for word in data_str.split():
    if list_pos == 0:
        if alpha_num_re.match(word) and len(word) > 2:
            cleaned_str = word
        else:
            cleaned_str = ' '
    else:
        if alpha_num_re.match(word) and len(word) > 2:
            cleaned_str = cleaned_str + ' ' + word
        else:
            cleaned_str += ' '
    list_pos += 1
return cleaned_str

```

- removes stop words

```

def remove_stops(data_str):
    # expects a string
    stops = set(stopwords.words("english"))
    list_pos = 0
    cleaned_str = ''
    text = data_str.split()
    for word in text:
        if word not in stops:
            # rebuild cleaned_str
            if list_pos == 0:
                cleaned_str = word
            else:
                cleaned_str = cleaned_str + ' ' + word
            list_pos += 1
    return cleaned_str

```

- tagging text

```

def tag_and_remove(data_str):
    cleaned_str = ''
    # noun tags
    nn_tags = ['NN', 'NNP', 'NNP', 'NNPS', 'NNS']
    # adjectives
    jj_tags = ['JJ', 'JJR', 'JJS']
    # verbs
    vb_tags = ['VB', 'VBD', 'VBG', 'VBN', 'VBP', 'VBZ']
    nltk_tags = nn_tags + jj_tags + vb_tags

    # break string into 'words'

```

(continues on next page)

(continued from previous page)

```

text = data_str.split()

# tag the text and keep only those with the right tags
tagged_text = pos_tag(text)
for tagged_word in tagged_text:
    if tagged_word[1] in nltk_tags:
        cleaned_str += tagged_word[0] + ' '

return cleaned_str

```

- lemmatization

```

def lemmatize(data_str):
    # expects a string
    list_pos = 0
    cleaned_str = ''
    lmtzr = WordNetLemmatizer()
    text = data_str.split()
    tagged_words = pos_tag(text)
    for word in tagged_words:
        if 'v' in word[1].lower():
            lemma = lmtzr.lemmatize(word[0], pos='v')
        else:
            lemma = lmtzr.lemmatize(word[0], pos='n')
        if list_pos == 0:
            cleaned_str = lemma
        else:
            cleaned_str = cleaned_str + ' ' + lemma
        list_pos += 1
    return cleaned_str

```

define the preprocessing function in PySpark

```

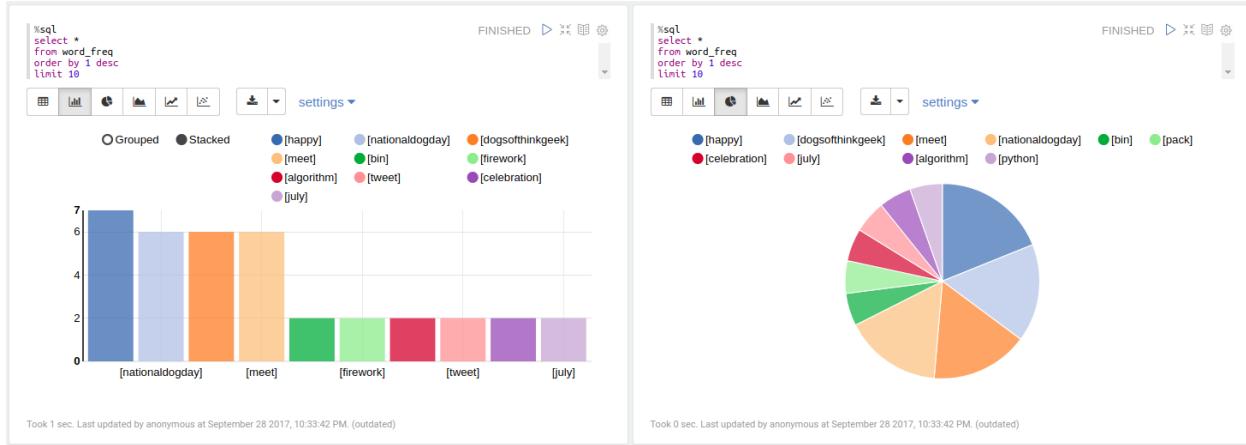
from pyspark.sql.functions import udf
from pyspark.sql.types import StringType
import preproc as pp

check_lang_udf = udf(pp.check_lang, StringType())
remove_stops_udf = udf(pp.remove_stops, StringType())
remove_features_udf = udf(pp.remove_features, StringType())
tag_and_remove_udf = udf(pp.tag_and_remove, StringType())
lemmatize_udf = udf(pp.lemmatize, StringType())
check_blanks_udf = udf(pp.check_blanks, StringType())

```

13.3 Text Classification

Theoretically speaking, you may apply any classification algorithms to do classification. I will only present Naive Bayes method is the following.



13.3.1 Introduction

13.3.2 Demo

1. create spark contexts

```
import pyspark
from pyspark.sql import SQLContext

# create spark contexts
sc = pyspark.SparkContext()
sqlContext = SQLContext(sc)
```

2. load dataset

```
# Load a text file and convert each line to a Row.
data_rdd = sc.textFile("../data/raw_data.txt")
parts_rdd = data_rdd.map(lambda l: l.split("\t"))

# Filter bad rows out
garantee_col_rdd = parts_rdd.filter(lambda l: len(l) == 3)
typed_rdd = guarantee_col_rdd.map(lambda p: (p[0], p[1], float(p[2])))

#Create DataFrame
data_df = sqlContext.createDataFrame(typed_rdd, ["text", "id", "label"])

# get the raw columns
raw_cols = data_df.columns

#data_df.show()
data_df.printSchema()
```

```
root
 |-- text: string (nullable = true)
 |-- id: string (nullable = true)
 |-- label: double (nullable = true)
```

```
+-----+-----+-----+
|       text|           id|label|
+-----+-----+-----+
|Fresh install of ...| 1018769417| 1.0|
|Well. Now I know ...| 10284216536| 1.0|
|"Literally six we...| 10298589026| 1.0|
|Mitsubishi i MiEV...|109017669432377344| 1.0|
+-----+-----+-----+
only showing top 4 rows
```

3. setup pyspark udf function

```
from pyspark.sql.functions import udf
from pyspark.sql.types import StringType
import preproc as pp

# Register all the functions in Preproc with Spark Context
check_lang_udf = udf(pp.check_lang, StringType())
remove_stops_udf = udf(pp.remove_stops, StringType())
remove_features_udf = udf(pp.remove_features, StringType())
tag_and_remove_udf = udf(pp.tag_and_remove, StringType())
lemmatize_udf = udf(pp.lemmatize, StringType())
check_blanks_udf = udf(pp.check_blanks, StringType())
```

4. language identification

```
lang_df = data_df.withColumn("lang", check_lang_udf(data_df["text"]))
en_df = lang_df.filter(lang_df["lang"] == "en")
en_df.show(4)
```

```
+-----+-----+-----+
|       text|           id|label|lang|
+-----+-----+-----+
|RT @goeentertain:...|665305154954989568| 1.0| en|
|Teforia Uses Mach...|660668007975268352| 1.0| en|
| Apple TV or Roku?| 25842461136| 1.0| en|
|Finished http://t...| 9412369614| 1.0| en|
+-----+-----+-----+
only showing top 4 rows
```

5. remove stop words

```
rm_stops_df = en_df.select(raw_cols) \
    .withColumn("stop_text", remove_stops_udf(en_df["text"]))
rm_stops_df.show(4)
```

```
+-----+-----+-----+-----+
|       text|           id|label|           stop_text|
+-----+-----+-----+-----+
|RT @goeentertain:...|665305154954989568| 1.0|RT @goeentertain:...|
|Teforia Uses Mach...|660668007975268352| 1.0|Teforia Uses Mach...|
```

(continues on next page)

(continued from previous page)

```
| Apple TV or Roku?|      25842461136| 1.0|      Apple TV Roku?|
|Finished http://t...|      9412369614| 1.0|Finished http://t...|
+-----+-----+-----+
only showing top 4 rows
```

6. remove irrelevant features

```
rm_features_df = rm_stops_df.select(raw_cols+["stop_text"])\n    .withColumn("feat_text", \\\n        remove_features_udf(rm_stops_df["stop_text"]))\nrm_features_df.show(4)
```

```
+-----+-----+-----+\n+-----+\n|          text|          id|label|          stop_text|\n+-----+\n|feat_text|\n+-----+\n+-----+\n|RT @goeentertain:...|665305154954989568| 1.0|RT @goeentertain:...| future_\n|blase ...|\n|Teforia Uses Mach...|660668007975268352| 1.0|Teforia Uses Mach...|teforia_\n|uses mach...|\n| Apple TV or Roku?|      25842461136| 1.0|      Apple TV Roku?|\n|apple roku|\n|Finished http://t...|      9412369614| 1.0|Finished http://t...|\n| finished|\n+-----+\n+-----+\nonly showing top 4 rows
```

7. tag the words

```
tagged_df = rm_features_df.select(raw_cols+["feat_text"])\n    .withColumn("tagged_text", \\\n        tag_and_remove_udf(rm_features_df.feat_text))\n\ntagged_df.show(4)
```

```
+-----+-----+-----+\n+-----+\n|          text|          id|label|          feat_text|\n+-----+\n|tagged_text|\n+-----+\n+-----+\n|RT @goeentertain:...|665305154954989568| 1.0|  future blase ...| future_\n|blase vic...|\n|Teforia Uses Mach...|660668007975268352| 1.0|teforia uses mach...| teforia_\n|uses mac...|\n| Apple TV or Roku?|      25842461136| 1.0|      apple roku|\n|apple roku |\n|Finished http://t...|      9412369614| 1.0|      finished|\n| finished |
```

(continues on next page)

(continued from previous page)

```
+-----+-----+-----+-----+
|-----+
only showing top 4 rows
```

8. lemmatization of words

```
lemm_df = tagged_df.select(raw_cols+["tagged_text"]) \
    .withColumn("lemm_text", lemmatize_udf(tagged_df["tagged_"
    ↪text"]))
lemm_df.show(4)
```

```
+-----+-----+-----+-----+
|-----+
|   text |           id|label|      tagged_text |
|-----+-----+-----+-----+
|-----+
|RT @goeentertain:...|665305154954989568| 1.0| future blase vic...|future_
|blase vice...|
|Teforia Uses Mach...|660668007975268352| 1.0| teforia uses mac...|teforia_
|use machi...|
| Apple TV or Roku?| 25842461136| 1.0|       apple roku |
|apple roku|
|Finished http://t...| 9412369614| 1.0|        finished |
|finish|
|-----+-----+-----+-----+
|-----+
only showing top 4 rows
```

9. remove blank rows and drop duplicates

```
check_blanks_df = lemm_df.select(raw_cols+["lemm_text"]) \
    .withColumn("is_blank", check_blanks_udf(lemm_df[
    ↪"lemm_text"]))
    # remove blanks
no_blanks_df = check_blanks_df.filter(check_blanks_df["is_blank"] ==
    ↪"False")

# drop duplicates
dedup_df = no_blanks_df.dropDuplicates(['text', 'label'])

dedup_df.show(4)
```

```
+-----+-----+-----+-----+
|   text |           id|label|      lemm_text|is_blank |
|-----+-----+-----+-----+
|RT @goeentertain:...|665305154954989568| 1.0|future blase vice...| False|
|Teforia Uses Mach...|660668007975268352| 1.0|teforia use machi...| False|
| Apple TV or Roku?| 25842461136| 1.0|       apple roku| False|
|Finished http://t...| 9412369614| 1.0|        finish| False|
|-----+-----+-----+-----+
```

(continues on next page)

(continued from previous page)

```
only showing top 4 rows
```

10. add unieq ID

```
from pyspark.sql.functions import monotonically_increasing_id
# Create Unique ID
dedup_df = dedup_df.withColumn("uid", monotonically_increasing_id())
dedup_df.show(4)
```

```
+-----+-----+-----+-----+
|       text|      id|label|      lemm_text|is_blank|
|       uid|
```

text	id	label	lemm_text	is_blank
uid				
dragon	1546813742	1.0	dragon	False
85899345920				
hurt much	1558492525	1.0	hurt much	
False 111669149696				
seth blog word se...	383221484023709697	1.0	seth blog word se...	
False 128849018880				
teforia use machi...	660668007975268352	1.0	teforia use machi...	
False 137438953472				
only showing top 4 rows				

11. create final dataset

```
data = dedup_df.select('uid', 'id', 'text', 'label')
data.show(4)
```

```
+-----+-----+-----+
|       uid|      id|      text|label|
+-----+-----+-----+
| 85899345920| 1546813742| dragon| 1.0|
|111669149696| 1558492525| hurt much| 1.0|
|128849018880|383221484023709697|seth blog word se...| 1.0|
|137438953472|660668007975268352|teforia use machi...| 1.0|
+-----+-----+-----+
only showing top 4 rows
```

12. Create taining and test sets

```
# Split the data into training and test sets (40% held out for testing)
(trainingData, testData) = data.randomSplit([0.6, 0.4])
```

13. NaiveBayes Pipeline

```

from pyspark.ml.feature import HashingTF, IDF, Tokenizer
from pyspark.ml import Pipeline
from pyspark.ml.classification import NaiveBayes, RandomForestClassifier
from pyspark.ml.classification import DecisionTreeClassifier
from pyspark.ml.evaluation import MulticlassClassificationEvaluator
from pyspark.ml.tuning import ParamGridBuilder
from pyspark.ml.tuning import CrossValidator
from pyspark.ml.feature import IndexToString, StringIndexer, VectorIndexer
from pyspark.ml.feature import CountVectorizer

# Configure an ML pipeline, which consists of tree stages: tokenizer, ↵
# hashingTF, and nb.
tokenizer = Tokenizer(inputCol="text", outputCol="words")
hashingTF = HashingTF(inputCol=tokenizer.getOutputCol(), outputCol=
    "rawFeatures")
# vectorizer = CountVectorizer(inputCol= "words", outputCol="rawFeatures")
idf = IDF(minDocFreq=3, inputCol="rawFeatures", outputCol="features")

# Naive Bayes model
nb = NaiveBayes()

# Pipeline Architecture
pipeline = Pipeline(stages=[tokenizer, hashingTF, idf, nb])

# Train model. This also runs the indexers.
model = pipeline.fit(trainingData)

```

14. Make predictions

```

predictions = model.transform(testData)

# Select example rows to display.
predictions.select("text", "label", "prediction").show(5, False)

```

text	label	prediction
finish	1.0	1.0
meet rolo dogsofthinkgeek happy nationaldogday	1.0	1.0
pumpkin family	1.0	1.0
meet jet dogsofthinkgeek happy nationaldogday	1.0	1.0
meet vixie dogsofthinkgeek happy nationaldogday	1.0	1.0

only showing top 5 rows

15. evaluation

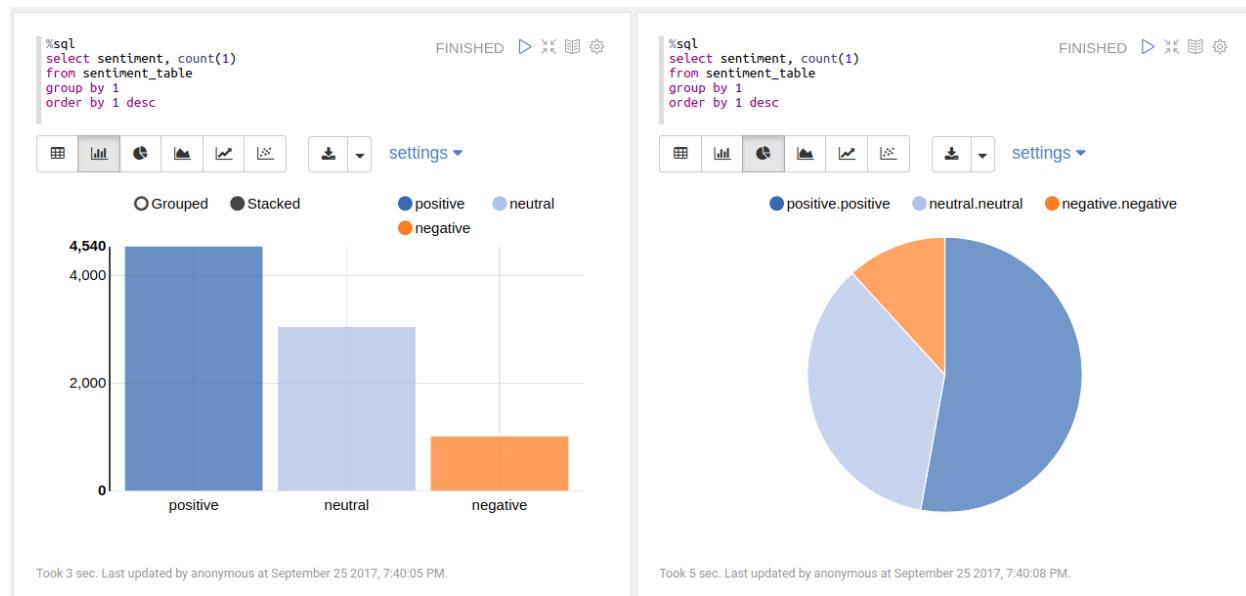
```

from pyspark.ml.evaluation import MulticlassClassificationEvaluator
evaluator = MulticlassClassificationEvaluator(predictionCol="prediction")
evaluator.evaluate(predictions)

```

0.912655971479501

13.4 Sentiment analysis



13.4.1 Introduction

Sentiment analysis (sometimes known as opinion mining or emotion AI) refers to the use of natural language processing, text analysis, computational linguistics, and biometrics to systematically identify, extract, quantify, and study affective states and subjective information. Sentiment analysis is widely applied to voice of the customer materials such as reviews and survey responses, online and social media, and healthcare materials for applications that range from marketing to customer service to clinical medicine.

Generally speaking, sentiment analysis aims to **determine the attitude** of a speaker, writer, or other subject with respect to some topic or the overall contextual polarity or emotional reaction to a document, interaction, or event. The attitude may be a judgment or evaluation (see appraisal theory), affective state (that is to say, the emotional state of the author or speaker), or the intended emotional communication (that is to say, the emotional effect intended by the author or interlocutor).

Sentiment analysis in business, also known as opinion mining is a process of identifying and cataloging a piece of text according to the tone conveyed by it. It has broad application:

- Sentiment Analysis in Business Intelligence Build up
- Sentiment Analysis in Business for Competitive Advantage
- Enhancing the Customer Experience through Sentiment Analysis in Business



Fig. 1: Sentiment Analysis Pipeline

13.4.2 Pipeline

13.4.3 Demo

1. Set up spark context and SparkSession

```

from pyspark.sql import SparkSession

spark = SparkSession \
    .builder \
    .appName("Python Spark Sentiment Analysis example") \
    .config("spark.some.config.option", "some-value") \
    .getOrCreate()
  
```

2. Load dataset

```

df = spark.read.format('com.databricks.spark.csv') \
    .options(header='true', \
    inferSchema='true') \
    .load("../data/newtwitter.csv", header=True);
  
```

text	id	pubdate
10 Things Missing...	2602860537	18536
RT @_NATURALBWINN...	2602850443	18536
RT @HBO24 yo the ...	2602761852	18535
Aaaaaaaaaand I have...	2602738438	18535
I can I please have...	2602684185	18535

only showing top 5 rows

3. Text Preprocessing

- remove non ASCII characters

```

from pyspark.sql.functions import udf
from pyspark.sql.types import StringType

from nltk.stem.wordnet import WordNetLemmatizer
from nltk.corpus import stopwords
from nltk import pos_tag
  
```

(continues on next page)

(continued from previous page)

```
import string
import re

# remove non ASCII characters
def strip_non_ascii(data_str):
    ''' Returns the string without non ASCII characters'''
    stripped = (c for c in data_str if 0 < ord(c) < 127)
    return ''.join(stripped)
# setup pyspark udf function
strip_non_ascii_udf = udf(strip_non_ascii, StringType())
```

check:

```
df = df.withColumn('text_non_ascii', strip_non_ascii_udf(df['text']))
df.show(5, True)
```

output:

text	id	pubdate	text_non_ascii
10 Things Missing...	2602860537	18536	10 Things Missing...
RT @_NATURALBWINN...	2602850443	18536	RT @_NATURALBWINN...
RT @HBO24 yo the ...	2602761852	18535	RT @HBO24 yo the ...
Aaaaaaaaand I have...	2602738438	18535	Aaaaaaaaand I have...
can I please have...	2602684185	18535	can I please have...

only showing top 5 rows

- fixed abbreviation

```
# fixed abbreviation
def fix_abbreviation(data_str):
    data_str = data_str.lower()
    data_str = re.sub(r'\bthat\b', 'that is', data_str)
    data_str = re.sub(r'\bive\b', 'i have', data_str)
    data_str = re.sub(r'\bim\b', 'i am', data_str)
    data_str = re.sub(r'\bya\b', 'yeah', data_str)
    data_str = re.sub(r'\bcant\b', 'can not', data_str)
    data_str = re.sub(r'\bdont\b', 'do not', data_str)
    data_str = re.sub(r'\bwont\b', 'will not', data_str)
    data_str = re.sub(r'\bid\b', 'i would', data_str)
    data_str = re.sub(r'\wtf', 'what the fuck', data_str)
    data_str = re.sub(r'\bwth\b', 'what the hell', data_str)
    data_str = re.sub(r'\br\b', 'are', data_str)
    data_str = re.sub(r'\bu\b', 'you', data_str)
    data_str = re.sub(r'\bk\b', 'OK', data_str)
    data_str = re.sub(r'\bsux\b', 'sucks', data_str)
    data_str = re.sub(r'\bno+\b', 'no', data_str)
    data_str = re.sub(r'\bcoo+\b', 'cool', data_str)
    data_str = re.sub(r'\rt\b', '', data_str)
```

(continues on next page)

(continued from previous page)

```

data_str = data_str.strip()
return data_str

fix_abbreviation_udf = udf(fix_abbreviation, StringType())

```

check:

```

df = df.withColumn('fixed_abbrev', fix_abbreviation_udf(df['text_non_ascii'
    ↪'])))
df.show(5, True)

```

output:

text	id	pubdate	text_non_ascii	fixed_abbrev
10 Things Missing... 2602860537 18536 10 Things Missing... 10 things <u>_missing... </u>				
RT @_NATURALBWINN... 2602850443 18536 RT @_NATURALBWINN... @_naturalbwinner ...				
RT @HBO24 yo the ... 2602761852 18535 RT @HBO24 yo the ... @hbo24 yo the #ne.../				
Aaaaaaaaand I have... 2602738438 18535 Aaaaaaaaand I have... aaaaaaaand i <u>_have... </u>				
can I please have... 2602684185 18535 can I please have... can i please <u>_have... </u>				

only showing top 5 rows

- remove irrelevant features

```

def remove_features(data_str):
    # compile regex
    url_re = re.compile('https?://(www.)?\w+\.\w+(/(\w+)*/?')
    punc_re = re.compile('[%s]' % re.escape(string.punctuation))
    num_re = re.compile('(\d+)')
    mention_re = re.compile('@(\w+)')
    alpha_num_re = re.compile("^[a-z0-9_.]+$")
    # convert to lowercase
    data_str = data_str.lower()
    # remove hyperlinks
    data_str = url_re.sub(' ', data_str)
    # remove @mentions
    data_str = mention_re.sub(' ', data_str)
    # remove punctuation
    data_str = punc_re.sub(' ', data_str)
    # remove numeric 'words'

```

(continues on next page)

(continued from previous page)

```

data_str = num_re.sub(' ', data_str)
# remove non a-z 0-9 characters and words shorter than 1 characters
list_pos = 0
cleaned_str = ''
for word in data_str.split():
    if list_pos == 0:
        if alpha_num_re.match(word) and len(word) > 1:
            cleaned_str = word
    else:
        cleaned_str = ' '
    else:
        if alpha_num_re.match(word) and len(word) > 1:
            cleaned_str = cleaned_str + ' ' + word
        else:
            cleaned_str += ' '
    list_pos += 1
# remove unwanted space, *.split() will automatically split on
# whitespace and discard duplicates, the " ".join() joins the
# resulting list into one string.
return " ".join(cleaned_str.split())
# setup pyspark udf function
remove_features_udf = udf(remove_features, StringType())

```

check:

```

df = df.withColumn('removed', remove_features_udf(df['fixed_abbrev']))
df.show(5, True)

```

output:

text	id	pubdate	text_non_ascii	fixed_abbrev
removed				
10 Things Missing... 2602860537 18536 10 Things Missing... 10 things				
missing... things missing in...				
RT @_NATURALBWINN... 2602850443 18536 RT @_NATURALBWINN... @_naturalbwinner ... oh and do not lik...				
RT @HBO24 yo the ... 2602761852 18535 RT @HBO24 yo the ... @hbo24 yo the				
#ne... yo the newtwitter.../				
Aaaaaaaaand I have... 2602738438 18535 Aaaaaaaaand I have... aaaaaaaand i				
have... aaaaaaaaand have t...				
can I please have... 2602684185 18535 can I please have... can i please				
have... can please have t...				
only showing top 5 rows				

4. Sentiment Analysis main function

```
from pyspark.sql.types import FloatType

from textblob import TextBlob

def sentiment_analysis(text):
    return TextBlob(text).sentiment.polarity

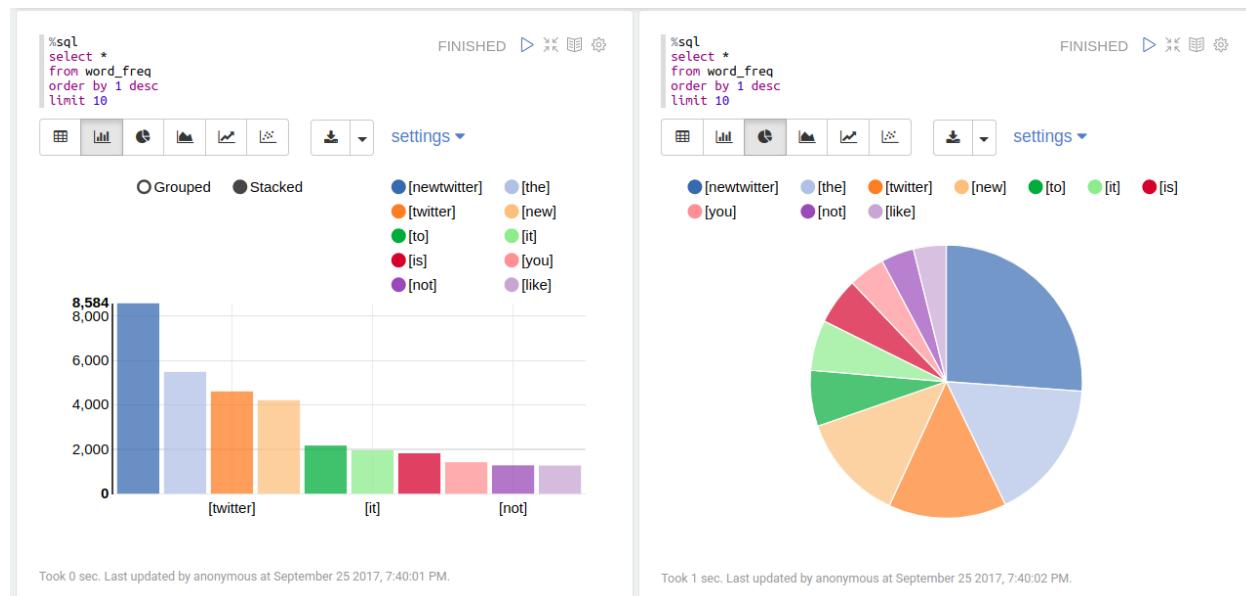
sentiment_analysis_udf = udf(sentiment_analysis, FloatType())
```

```
df = df.withColumn("sentiment_score", sentiment_analysis_udf(df['removed']))
df.show(5, True)
```

- Sentiment score

```
+-----+-----+
|       removed | sentiment_score |
+-----+-----+
| things missing in... | -0.03181818 |
| oh and do not lik... | -0.03181818 |
| yo the newtwitter... | 0.3181818 |
| aaaaaaaaaand have t... | 0.11818182 |
| can please have t... | 0.13636364 |
+-----+-----+
only showing top 5 rows
```

- Words frequency



- Sentiment Classification

```
def condition(r):
    if (r >= 0.1):
```

(continues on next page)

(continued from previous page)

```

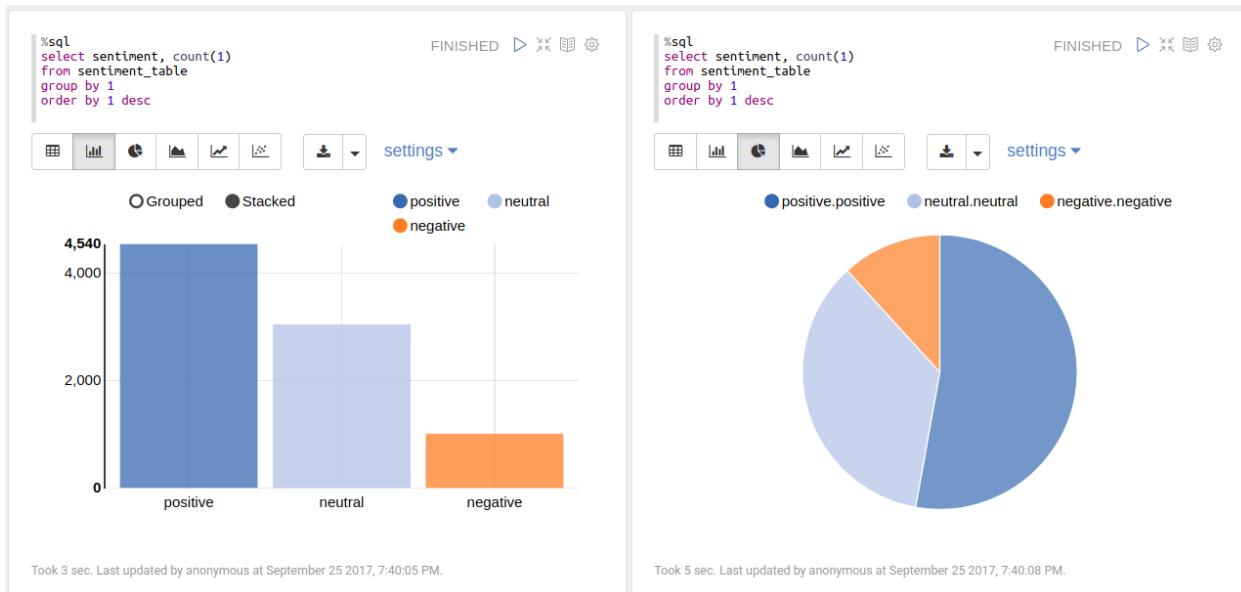
label = "positive"
elif(r <= -0.1):
    label = "negative"
else:
    label = "neutral"
return label

sentiment_udf = udf(lambda x: condition(x), StringType())

```

5. Output

- Sentiment Class



- Top tweets from each sentiment class

```
+-----+-----+-----+
|           text | sentiment_score | sentiment |
+-----+-----+-----+
| and this #newtwit... /      1.0 | positive | |
| "RT @SarahsJokes:... |      1.0 | positive |
| #newtwitter using... /      1.0 | positive |
| The #NewTwitter h... /      1.0 | positive |
| You can now undo ... |      1.0 | positive |
+-----+-----+-----+
only showing top 5 rows
```

```
+-----+-----+-----+
|           text | sentiment_score | sentiment |
+-----+-----+-----+
| Lists on #NewTwit... /     -0.1 | neutral | |
| Too bad most of m... |     -0.1 | neutral |
| the #newtwitter i... |     -0.1 | neutral |
```

(continues on next page)

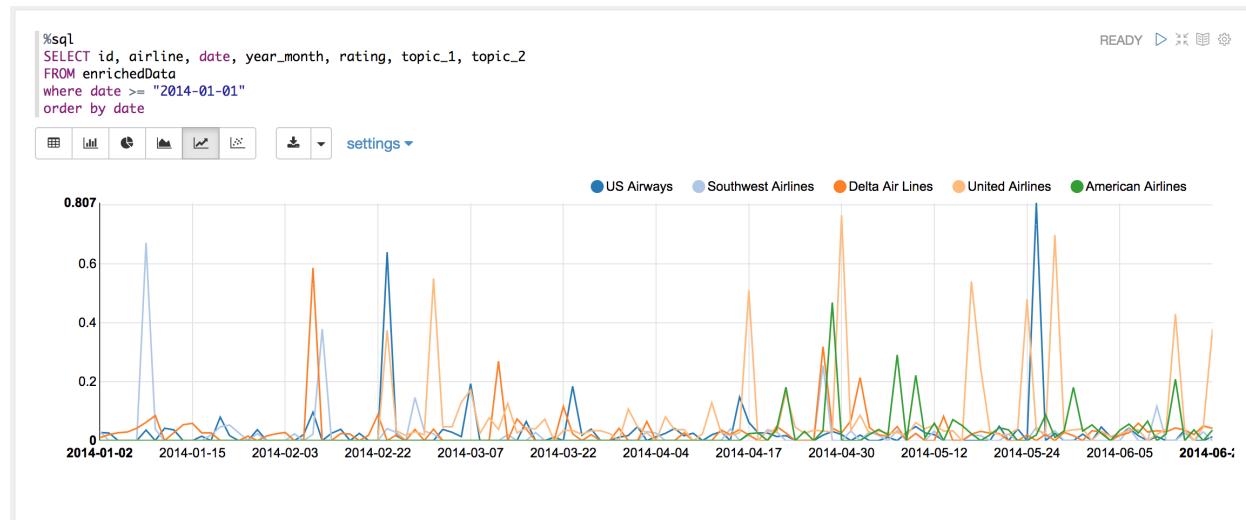
(continued from previous page)

```
| Looks like our re... |      -0.1 |  neutral |
| i switched to the... |      -0.1 |  neutral |
+-----+-----+-----+
only showing top 5 rows
```

```
+-----+-----+-----+
|           text | sentiment_score | sentiment |
+-----+-----+-----+
| oh. #newtwitter i... /      -1.0 | negative | |
| RT @chqwn: #NewTw... /      -1.0 | negative |
| Copy that - its W... |      -1.0 | negative |
| RT @chqwn: #NewTw... /      -1.0 | negative |
| #NewTwitter has t... /      -1.0 | negative |
+-----+-----+-----+
only showing top 5 rows
```

13.5 N-grams and Correlations

13.6 Topic Model: Latent Dirichlet Allocation



13.6.1 Introduction

In text mining, a topic model is a unsupervised model for discovering the abstract “topics” that occur in a collection of documents.

Latent Dirichlet Allocation (LDA) is a mathematical method for estimating both of these at the same time: finding the mixture of words that is associated with each topic, while also determining the mixture of topics that describes each document.

13.6.2 Demo

1. Load data

```
rawdata = spark.read.load("../data/airlines.csv", format="csv",
    header=True)
rawdata.show(5)
```

id airline date location rating review								
cabin value recommended								
+-----+-----+-----+-----+-----+-----+-----+-----+								
10001 Delta Air Lines 21-Jun-14 Thailand 7 Economy 4								
YES Flew Mar 30 NRT t...								
10002 Delta Air Lines 19-Jun-14 USA 0 Economy 2								
NO Flight 2463 leavi...								
10003 Delta Air Lines 18-Jun-14 USA 0 Economy 1								
NO Delta Website fro...								
10004 Delta Air Lines 17-Jun-14 USA 9 Business 4								
YES "I just returned ...								
10005 Delta Air Lines 17-Jun-14 Ecuador 7 Economy 3								
YES "Round-trip flight...								
+-----+-----+-----+-----+-----+-----+-----+-----+								
only showing top 5 rows								

1. Text preprocessing

I will use the following raw column names to keep my table concise:

```
raw_cols = rawdata.columns
raw_cols
```

```
['id', 'airline', 'date', 'location', 'rating', 'cabin', 'value',
 'recommended', 'review']
```

```
rawdata = rawdata.dropDuplicates(['review'])
```

```
from pyspark.sql.functions import udf, col
from pyspark.sql.types import StringType, DoubleType, DateType

from nltk.stem.wordnet import WordNetLemmatizer
from nltk.corpus import stopwords
from nltk import pos_tag
import langid
import string
import re
```

- remove non ASCII characters

```
# remove non ASCII characters
def strip_non_ascii(data_str):
    ''' Returns the string without non ASCII characters'''
    stripped = (c for c in data_str if 0 < ord(c) < 127)
    return ''.join(stripped)
```

- check it blank line or not

```
# check to see if a row only contains whitespace
def check_blanks(data_str):
    is_blank = str(data_str.isspace())
    return is_blank
```

- check the language (a little bit slow, I skited this step)

```
# check the language (only apply to english)
def check_lang(data_str):
    from langid.langid import LanguageIdentifier, model
    identifier = LanguageIdentifier.from_modelstring(model, norm_
→probs=True)
    predict_lang = identifier.classify(data_str)

    if predict_lang[1] >= .9:
        language = predict_lang[0]
    else:
        language = predict_lang[1]
    return language
```

- fixed abbreviation

```
# fixed abbreviation
def fix_abbreviation(data_str):
    data_str = data_str.lower()
    data_str = re.sub(r'\bthats\b', 'that is', data_str)
    data_str = re.sub(r'\bive\b', 'i have', data_str)
    data_str = re.sub(r'\bim\b', 'i am', data_str)
    data_str = re.sub(r'\bya\b', 'yeah', data_str)
    data_str = re.sub(r'\bcant\b', 'can not', data_str)
    data_str = re.sub(r'\bdont\b', 'do not', data_str)
    data_str = re.sub(r'\bwont\b', 'will not', data_str)
    data_str = re.sub(r'\bid\b', 'i would', data_str)
    data_str = re.sub(r'\wtf', 'what the fuck', data_str)
    data_str = re.sub(r'\bwth\b', 'what the hell', data_str)
    data_str = re.sub(r'\br\b', 'are', data_str)
    data_str = re.sub(r'\bu\b', 'you', data_str)
    data_str = re.sub(r'\bk\b', 'OK', data_str)
    data_str = re.sub(r'\bsux\b', 'sucks', data_str)
    data_str = re.sub(r'\bno+\b', 'no', data_str)
    data_str = re.sub(r'\bcoo+\b', 'cool', data_str)
    data_str = re.sub(r'\rt\b', '', data_str)
    data_str = data_str.strip()
    return data_str
```

- remove irrelevant features

```
# remove irrelevant features
def remove_features(data_str):
    # compile regex
    url_re = re.compile('https?://(www.)?\w+\.\w+(/w+)*/?')
    punc_re = re.compile('[%s]' % re.escape(string.punctuation))
    num_re = re.compile('(\d+)')
    mention_re = re.compile('@(\w+)')
    alpha_num_re = re.compile("^[a-z0-9_.]+$")
    # convert to lowercase
    data_str = data_str.lower()
    # remove hyperlinks
    data_str = url_re.sub(' ', data_str)
    # remove @mentions
    data_str = mention_re.sub(' ', data_str)
    # remove punctuation
    data_str = punc_re.sub(' ', data_str)
    # remove numeric 'words'
    data_str = num_re.sub(' ', data_str)
    # remove non a-z 0-9 characters and words shorter than 1
    ↪characters
    list_pos = 0
    cleaned_str = ''
    for word in data_str.split():
        if list_pos == 0:
            if alpha_num_re.match(word) and len(word) > 1:
                cleaned_str = word
            else:
                cleaned_str = ' '
        else:
            if alpha_num_re.match(word) and len(word) > 1:
                cleaned_str = cleaned_str + ' ' + word
            else:
                cleaned_str += ' '
        list_pos += 1
    # remove unwanted space, *.split() will automatically split on
    # whitespace and discard duplicates, the ".join()" joins the
    # resulting list into one string.
    return " ".join(cleaned_str.split())
```

- removes stop words

```
# removes stop words
def remove_stops(data_str):
    # expects a string
    stops = set(stopwords.words("english"))
    list_pos = 0
    cleaned_str = ''
    text = data_str.split()
    for word in text:
        if word not in stops:
            # rebuild cleaned_str
```

(continues on next page)

(continued from previous page)

```

if list_pos == 0:
    cleaned_str = word
else:
    cleaned_str = cleaned_str + ' ' + word
list_pos += 1
return cleaned_str

```

- Part-of-Speech Tagging

```

# Part-of-Speech Tagging
def tag_and_remove(data_str):
    cleaned_str = ''
    # noun tags
    nn_tags = ['NN', 'NNP', 'NNP', 'NNPS', 'NNS']
    # adjectives
    jj_tags = ['JJ', 'JJR', 'JJS']
    # verbs
    vb_tags = ['VB', 'VBD', 'VBG', 'VBN', 'VBP', 'VBZ']
    nltk_tags = nn_tags + jj_tags + vb_tags

    # break string into 'words'
    text = data_str.split()

    # tag the text and keep only those with the right tags
    tagged_text = pos_tag(text)
    for tagged_word in tagged_text:
        if tagged_word[1] in nltk_tags:
            cleaned_str += tagged_word[0] + ' '

    return cleaned_str

```

- lemmatization

```

# lemmatization
def lemmatize(data_str):
    # expects a string
    list_pos = 0
    cleaned_str = ''
    lmtzr = WordNetLemmatizer()
    text = data_str.split()
    tagged_words = pos_tag(text)
    for word in tagged_words:
        if 'v' in word[1].lower():
            lemma = lmtzr.lemmatize(word[0], pos='v')
        else:
            lemma = lmtzr.lemmatize(word[0], pos='n')
        if list_pos == 0:
            cleaned_str = lemma
        else:
            cleaned_str = cleaned_str + ' ' + lemma
        list_pos += 1
    return cleaned_str

```

- setup pyspark udf function

```
# setup pyspark udf function
strip_non_ascii_udf = udf(strip_non_ascii, StringType())
check_blanks_udf = udf(check_blanks, StringType())
check_lang_udf = udf(check_lang, StringType())
fix_abbreviation_udf = udf(fix_abbreviation, StringType())
remove_stops_udf = udf(remove_stops, StringType())
remove_features_udf = udf(remove_features, StringType())
tag_and_remove_udf = udf(tag_and_remove, StringType())
lemmatize_udf = udf(lemmatize, StringType())
```

1. Text processing

- correct the data schema

```
rawdata = rawdata.withColumn('rating', rawdata.rating.cast('float'))
```

```
rawdata.printSchema()
```

```
root
|--- id: string (nullable = true)
|--- airline: string (nullable = true)
|--- date: string (nullable = true)
|--- location: string (nullable = true)
|--- rating: float (nullable = true)
|--- cabin: string (nullable = true)
|--- value: string (nullable = true)
|--- recommended: string (nullable = true)
|--- review: string (nullable = true)
```

```
from datetime import datetime
from pyspark.sql.functions import col

# https://docs.python.org/2/library/datetime.html#strftime-and-
# strptime-behavior
# 21-Jun-14 <----> %d-%b-%y
to_date = udf(lambda x: datetime.strptime(x, '%d-%b-%y'), DateType())

rawdata = rawdata.withColumn('date', to_date(col('date')))
```

```
rawdata.printSchema()
```

```
root
|--- id: string (nullable = true)
|--- airline: string (nullable = true)
|--- date: date (nullable = true)
|--- location: string (nullable = true)
|--- rating: float (nullable = true)
|--- cabin: string (nullable = true)
```

(continues on next page)

(continued from previous page)

```
|-- value: string (nullable = true)
|-- recommended: string (nullable = true)
|-- review: string (nullable = true)
```

```
rawdata.show(5)
```

<code>id</code>	<code>airline</code>	<code>date</code>	<code>location</code>	<code>rating</code>	<code>review</code>
10551	Southwest Airlines	2013-11-06	USA	1.0	Business
	NO Flight 3246 from ...				2 ↴
10298	US Airways	2014-03-31	UK	1.0	Business
	NO Flight from Manch...				0 ↴
10564	Southwest Airlines	2013-09-06	USA	10.0	Economy
	YES I'm Executive Pla...				5 ↴
10134	Delta Air Lines	2013-12-10	USA	8.0	Economy
	YES MSP-JFK-MXP and r...				4 ↴
10912	United Airlines	2014-04-07	USA	3.0	Economy
	NO Worst airline I h...				1 ↴

only showing top 5 rows

```
rawdata = rawdata.withColumn('non_ascii', strip_non_ascii_udf(rawdata['review']))

+-----+-----+-----+-----+-----+
| id | airline | date | location | rating |      non_ascii |
+-----+-----+-----+-----+-----+
| 10551 | Southwest Airlines | 2013-11-06 | USA | 1.0 | Business | 2 | ↴
|       NO|Flight 3246 from ...|Flight 3246 from ... |
| 10298 | US Airways | 2014-03-31 | UK | 1.0 | Business | 0 | ↴
|       NO|Flight from Manch...|Flight from Manch... |
| 10564 | Southwest Airlines | 2013-09-06 | USA | 10.0 | Economy | 5 | ↴
|       YES|I'm Executive Pla...|I'm Executive Pla... |
| 10134 | Delta Air Lines | 2013-12-10 | USA | 8.0 | Economy | 4 | ↴
|       YES|MSP-JFK-MXP and r...|MSP-JFK-MXP and r... |
| 10912 | United Airlines | 2014-04-07 | USA | 3.0 | Economy | 1 | ↴
|       NO|Worst airline I h...|Worst airline I h... |
+-----+-----+-----+-----+-----+
only showing top 5 rows
```

```

rawdata = rawdata.select(raw_cols+['non_ascii']) \
    .withColumn('fixed_abbreviation',
    udf(rawdata['non_ascii']))

+-----+-----+-----+-----+-----+
| id | airline | date | location | rating | review | non_ascii |
+-----+-----+-----+-----+-----+
| 10551 | Southwest Airlines | 2013-11-06 | USA | 1.0 | Business | 2 | 
|       NO|Flight 3246 from ...|Flight 3246 from ...|flight 3246 |
|from ... |
| 10298 | US Airways | 2014-03-31 | UK | 1.0 | Business | 0 | 
|       NO|Flight from Manch...|Flight from Manch...|flight from |
|manch... |
| 10564 | Southwest Airlines | 2013-09-06 | USA | 10.0 | Economy | 5 | 
|       YES|I'm Executive Pla...|I'm Executive Pla...|i'm executive |
|pla... |
| 10134 | Delta Air Lines | 2013-12-10 | USA | 8.0 | Economy | 4 | 
|       YES|MSP-JFK-MXP and r...|MSP-JFK-MXP and r...|msp-jfk-mxp |
|and r... |
| 10912 | United Airlines | 2014-04-07 | USA | 3.0 | Economy | 1 | 
|       NO|Worst airline I h...|Worst airline I h...|worst airline |
|i h... |
+-----+-----+-----+-----+-----+
|       |
|       |
|       |
only showing top 5 rows

```

```

rawdata = rawdata.select(raw_cols+['fixed_abbrev']) \
    .withColumn('stop_text', remove_stops_udf(rawdata[
    'fixed_abbrev']))

+-----+-----+-----+-----+-----+
| id | airline | date | location | rating | review | fixed_abbrev |
+-----+-----+-----+-----+-----+
| 10551 | Southwest Airlines | 2013-11-06 | USA | 1.0 | Business | 2 | 
|       NO|Flight 3246 from ...|flight 3246 from ...|flight 3246 |
|chica... |
| 10298 | US Airways | 2014-03-31 | UK | 1.0 | Business | 0 | 
|       NO|Flight from Manch...|flight from manch...|flight |
|manchester... |

```

(continues on next page)

(continued from previous page)

```
|10564|Southwest Airlines|2013-09-06|      USA| 10.0| Economy| 5|  
↳      YES|I'm Executive Pla...|i'm executive pla...|i'm executive  
↳pla...|  
|10134|  Delta Air Lines|2013-12-10|      USA|  8.0| Economy| 4|  
↳      YES|MSP-JFK-MXP and r...|msp-jfk-mxp and r...|msp-jfk-mxp  
↳retur...|  
|10912|  United Airlines|2014-04-07|      USA|  3.0| Economy| 1|  
↳      NO|Worst airline I h...|worst airline i h...|worst airline  
↳eve...|  
+-----+-----+-----+-----+-----+-----+-----+  
↳-----+-----+-----+-----+-----+-----+  
↳-----+  
only showing top 5 rows
```

```
rawdata = rawdata.select(raw_cols+['stop_text'])\n    .withColumn('feat_text', remove_features_udf(rawdata[\n        'stop_text']))\n\n+-----+-----+-----+-----+-----+-----+-----+  
↳-----+-----+-----+-----+-----+-----+-----+  
↳-----+  
|  id|      airline|      date|location|rating|  
↳cabin|value|recommended|           review|          stop_text|  
↳      feat_text|  
+-----+-----+-----+-----+-----+-----+-----+  
↳-----+-----+-----+-----+-----+-----+-----+  
↳-----+  
|10551|Southwest Airlines|2013-11-06|      USA| 1.0|Business| 2|  
↳      NO|Flight 3246 from ...|flight 3246 chica...|flight  
↳chicago mi...|  
|10298|      US Airways|2014-03-31|      UK|  1.0|Business| 0|  
↳      NO|Flight from Manch...|flight manchester...|flight  
↳manchester...|  
|10564|Southwest Airlines|2013-09-06|      USA| 10.0| Economy| 5|  
↳      YES|I'm Executive Pla...|i'm executive pla...|executive  
↳platinu...|  
|10134|  Delta Air Lines|2013-12-10|      USA|  8.0| Economy| 4|  
↳      YES|MSP-JFK-MXP and r...|msp-jfk-mxp retur...|msp jfk mxp  
↳retur...|  
|10912|  United Airlines|2014-04-07|      USA|  3.0| Economy| 1|  
↳      NO|Worst airline I h...|worst airline eve...|worst airline  
↳eve...|  
+-----+-----+-----+-----+-----+-----+-----+  
↳-----+-----+-----+-----+-----+-----+  
↳-----+  
only showing top 5 rows
```

```
rawdata = rawdata.select(raw_cols+['feat_text'])\n    .withColumn('tagged_text', tag_and_remove_\n        udf(rawdata['feat_text']))
```

(continues on next page)

(continued from previous page)

<code> id </code>	<code>airline </code>	<code>date location rating </code>	<code>review </code>	<code>feat_text </code>
<code> cabin value recommended </code>				
	<code>tagged_text </code>			
<code> 10551 Southwest Airlines 2013-11-06 </code>		<code>USA 1.0 Business </code>		<code>2 </code>
<code> ↳ NO Flight 3246 from ... </code>	<code>flight chicago mi... </code>	<code>flight</code>		
<code> ↳ chicago mi... </code>				
<code> 10298 US Airways 2014-03-31 </code>		<code>UK 1.0 Business </code>	<code>0 </code>	
<code> ↳ NO Flight from Manch... </code>	<code>flight manchester... </code>	<code>flight</code>		
<code> ↳ mancheste... </code>				
<code> 10564 Southwest Airlines 2013-09-06 </code>		<code>USA 10.0 Economy </code>	<code>5 </code>	
<code> ↳ YES I'm Executive Pla... </code>	<code>executive platinu... </code>	<code>executive</code>		
<code> ↳ platin... </code>				
<code> 10134 Delta Air Lines 2013-12-10 </code>		<code>USA 8.0 Economy </code>	<code>4 </code>	
<code> ↳ YES MSP-JFK-MXP and r... </code>	<code>msp jfk mxp retur... </code>	<code>msp jfk mxp</code>		
<code> ↳ retu... </code>				
<code> 10912 United Airlines 2014-04-07 </code>		<code>USA 3.0 Economy </code>	<code>1 </code>	
<code> ↳ NO Worst airline I h... </code>	<code>worst airline eve... </code>	<code>worst</code>		
<code> ↳ airline ua... </code>				
<code>+-----+-----+-----+-----+-----+</code>				
<code> ↳-----+-----+-----+-----+-----+</code>				
<code> ↳-----+-----+-----+-----+-----+</code>				
<code>only showing top 5 rows</code>				

```
rawdata = rawdata.select(raw_cols+['tagged_text']) \
    .withColumn('lemm_text', lemmatize_udf(rawdata['tagged_text']))
```

<code> id </code>	<code>airline </code>	<code>date location rating </code>	<code>review </code>	<code>tagged_text </code>
<code> cabin value recommended </code>				
	<code>lemm_text </code>			
<code> 10551 Southwest Airlines 2013-11-06 </code>		<code>USA 1.0 Business </code>	<code>2 </code>	
<code> ↳ NO Flight 3246 from ... </code>	<code>flight chicago mi... </code>	<code>flight</code>		
<code> ↳ chicago mi... </code>				
<code> 10298 US Airways 2014-03-31 </code>		<code>UK 1.0 Business </code>	<code>0 </code>	
<code> ↳ NO Flight from Manch... </code>	<code>flight manchester... </code>	<code>flight</code>		
<code> ↳ mancheste... </code>				
<code> 10564 Southwest Airlines 2013-09-06 </code>		<code>USA 10.0 Economy </code>	<code>5 </code>	
<code> ↳ YES I'm Executive Pla... </code>	<code>executive platinu... </code>	<code>executive</code>		
<code> ↳ platinu... </code>				

(continues on next page)

(continued from previous page)

```
| 10134 | Delta Air Lines|2013-12-10|      USA|     8.0| Economy|    4|_
↳ YES|MSP-JFK-MXP and r...| msp jfk mxp retur...|msp jfk mxp|
↳ return...
| 10912 | United Airlines|2014-04-07|      USA|     3.0| Economy|    1|_
↳ NO|Worst airline I h...| worst airline ua...|worst airline|
↳ ual...
+----+-----+-----+-----+-----+-----+-----+
↳ -----+-----+-----+-----+-----+
↳ -----+
only showing top 5 rows
```

```
rawdata = rawdata.select(raw_cols+[ 'lemm_text' ]) \
    .withColumn("is_blank", check_blanks_udf(rawdata[
↳ "lemm_text"]))
```

```
+----+-----+-----+-----+-----+-----+
↳ -----+-----+-----+-----+-----+
|   id|      airline|      date|location|rating|   _|
↳ cabin|value|recommended|           review|      lemm_
↳ text|is_blank|
+----+-----+-----+-----+-----+-----+
↳ -----+-----+-----+-----+
| 10551|Southwest Airlines|2013-11-06|      USA|     1.0|Business|    2|_
↳ NO|Flight 3246 from ...|flight chicago mi...| False|
| 10298 | US Airways|2014-03-31|      UK|     1.0|Business|    0|_
↳ NO|Flight from Manch...|flight manchester...| False|
| 10564|Southwest Airlines|2013-09-06|      USA|    10.0| Economy|    5|_
↳ YES|I'm Executive Pla...|executive platinu...| False|
| 10134 | Delta Air Lines|2013-12-10|      USA|     8.0| Economy|    4|_
↳ YES|MSP-JFK-MXP and r...| msp jfk mxp retur...| False|
| 10912 | United Airlines|2014-04-07|      USA|     3.0| Economy|    1|_
↳ NO|Worst airline I h...| worst airline ual...| False|
+----+-----+-----+-----+-----+-----+
↳ -----+-----+-----+-----+
only showing top 5 rows
```

```
from pyspark.sql.functions import monotonically_increasing_id
# Create Unique ID
rawdata = rawdata.withColumn("uid", monotonically_increasing_id())
data = rawdata.filter(rawdata["is_blank"] == "False")
```

```
+----+-----+-----+-----+-----+-----+
↳ -----+-----+-----+-----+-----+
|   id|      airline|      date|location|rating|   _
↳ cabin|value|recommended|           review|      lemm_
↳ text|is_blank|uid|
+----+-----+-----+-----+-----+-----+
↳ -----+-----+-----+-----+
| 10551|Southwest Airlines|2013-11-06|      USA|     1.0|Business|    2|_
↳ NO|Flight 3246 from ...|flight chicago mi...| False|  0|
```

(continues on next page)

(continued from previous page)

10298 US Airways 2014-03-31 UK 1.0 Business 0 ↵
↳ NO Flight from Manch... flight manchester... False 1 ↵
10564 Southwest Airlines 2013-09-06 USA 10.0 Economy 5 ↵
↳ YES I'm Executive Pla... executive platinu... False 2 ↵
10134 Delta Air Lines 2013-12-10 USA 8.0 Economy 4 ↵
↳ YES MSP-JFK-MXP and r... msp jfk mxp return... False 3 ↵
10912 United Airlines 2014-04-07 USA 3.0 Economy 1 ↵
↳ NO Worst airline I h... worst airline ual... False 4 ↵
+-----+-----+-----+-----+-----+-----+-----+
↳-----+-----+-----+-----+-----+-----+-----+

only showing top 5 rows

Pipeline for LDA model

```
from pyspark.ml.feature import HashingTF, IDF, Tokenizer
from pyspark.ml import Pipeline
from pyspark.ml.classification import NaiveBayes, ↵
    RandomForestClassifier
from pyspark.ml.clustering import LDA
from pyspark.ml.classification import DecisionTreeClassifier
from pyspark.ml.evaluation import MulticlassClassificationEvaluator
from pyspark.ml.tuning import ParamGridBuilder
from pyspark.ml.tuning import CrossValidator
from pyspark.ml.feature import IndexToString, StringIndexer, ↵
    VectorIndexer
from pyspark.ml.feature import CountVectorizer

# Configure an ML pipeline, which consists of tree stages: tokenizer,
↳ hashingTF, and nb.
tokenizer = Tokenizer(inputCol="lemm_text", outputCol="words")
#data = tokenizer.transform(data)
vectorizer = CountVectorizer(inputCol= "words", outputCol=
    ↵"rawFeatures")
idf = IDF(inputCol="rawFeatures", outputCol="features")
#idfModel = idf.fit(data)

lda = LDA(k=20, seed=1, optimizer="em")

pipeline = Pipeline(stages=[tokenizer, vectorizer,idf, lda])

model = pipeline.fit(data)
```

1. Results presentation

- Topics

topic	termIndices	termWeights
0 [60, 7, 12, 483, ... [0.01349507958269...		
1 [363, 29, 187, 55... [0.01247250144447...		

(continues on next page)

(continued from previous page)

```

| 2|[46, 107, 672, 27...|[0.01188684264641...
| 3|[76, 43, 285, 152...|[0.01132638300115...
| 4|[201, 13, 372, 69...|[0.01337529863256...
| 5|[122, 103, 181, 4...|[0.00930415977117...
| 6|[14, 270, 18, 74,...|[0.01253817708163...
| 7|[111, 36, 341, 10...|[0.01269584954257...
| 8|[477, 266, 297, 1...|[0.01017486869509...
| 9|[10, 73, 46, 1, 2...|[0.01050875237546...
| 10|[57, 29, 411, 10,...|[0.01777350667863...
| 11|[293, 119, 385, 4...|[0.01280305149305...
| 12|[116, 218, 256, 1...|[0.01570714218509...
| 13|[433, 171, 176, 3...|[0.00819684813575...
| 14|[74, 84, 45, 108,...|[0.01700630002172...
| 15|[669, 215, 14, 58...|[0.00779310974971...
| 16|[198, 21, 98, 164...|[0.01030577084202...
| 17|[96, 29, 569, 444...|[0.01297142577633...
| 18|[18, 60, 140, 64,...|[0.01306356985169...
| 19|[33, 178, 95, 2, ...|[0.00907425683229...
+-----+

```

- Topic terms

```

from pyspark.sql.types import ArrayType, StringType

def termsIdx2Term(vocabulary):
    def termsIdx2Term(termIndices):
        return [vocabulary[int(index)] for index in termIndices]
    return udf(termsIdx2Term, ArrayType(StringType()))

vectorizerModel = model.stages[1]
vocabList = vectorizerModel.vocabulary
final = ldatopics.withColumn("Terms", termsIdx2Term(vocabList) (
    "termIndices"))

```

topic	termIndices	Terms
0	[60, 7, 12, 483, 292, 326, 88, 4, 808, 32]	[pm, plane, board, kid, online, lga, schedule, get, memphis, arrive]
1	[363, 29, 187, 55, 48, 647, 30, 9, 204, 457]	[dublin, class, th, sit, entertainment, express, say, delay, dl, son]
2	[46, 107, 672, 274, 92, 539, 23, 27, 279, 8]	[economy, sfo, milwaukee, decent, comfortable, iad, return, united, average, airline]

(continues on next page)

(continued from previous page)

```

|3   | [76, 43, 285, 152, 102, 34, 300, 113, 24, 31] | [didn, pay, ]
  ↵lose, different, extra, bag, mile, baggage, leave, day]
  ↵
  ↵
|4   | [201, 13, 372, 692, 248, 62, 211, 187, 105, 110] | [houston, ]
  ↵crew, heathrow, louisville, london, great, denver, th, land, jfk]
  ↵
  ↵
|5   | [122, 103, 181, 48, 434, 10, 121, 147, 934, 169] | [lhr, serve, ]
  ↵screen, entertainment, ny, delta, excellent, atl, sin, newark]
  ↵
  ↵
|6   | [14, 270, 18, 74, 70, 37, 16, 450, 3, 20] | [check, ]
  ↵employee, gate, line, change, wait, take, fll, time, tell]
  ↵
  ↵
|7   | [111, 36, 341, 10, 320, 528, 844, 19, 195, 524] | [atlanta, ]
  ↵first, toilet, delta, washington, card, global, staff, route,
  ↵amsterdam]
  ↵
|8   | [477, 266, 297, 185, 1, 33, 22, 783, 17, 908] | [fuel, group,
  ↵pas, boarding, seat, trip, minute, orleans, make, select]
  ↵
  ↵
|9   | [10, 73, 46, 1, 248, 302, 213, 659, 48, 228] | [delta, lax, ]
  ↵economy, seat, london, detroit, comfo, weren, entertainment, wife]
  ↵
  ↵
|10  | [57, 29, 411, 10, 221, 121, 661, 19, 805, 733] | [business, ]
  ↵class, fra, delta, lounge, excellent, syd, staff, nov, mexico]
  ↵
  ↵
|11  | [293, 119, 385, 481, 503, 69, 13, 87, 176, 545] | [march, ua, ]
  ↵manchester, phx, envoy, drink, crew, american, aa, canada]
  ↵
  ↵
|12  | [116, 218, 256, 156, 639, 20, 365, 18, 22, 136] | [san, clt, ]
  ↵francisco, second, text, tell, captain, gate, minute, available]
  ↵
  ↵
|13  | [433, 171, 176, 339, 429, 575, 10, 26, 474, 796] | [daughter, ]
  ↵small, aa, ba, segment, proceed, delta, passenger, size, similar]
  ↵
  ↵
|14  | [74, 84, 45, 108, 342, 111, 315, 87, 52, 4] | [line, agent,
  ↵next, hotel, standby, atlanta, dallas, american, book, get]
  ↵
  ↵
|15  | [669, 215, 14, 58, 561, 59, 125, 179, 93, 5] | [fit, carry, ]
  ↵check, people, bathroom, ask, thing, row, don, fly]
  ↵
  ↵
|16  | [198, 21, 98, 164, 57, 141, 345, 62, 121, 174] | [ife, good,
  ↵nice, much, business, lot, dfw, great, excellent, carrier]
  ↵
  ↵
|17  | [96, 29, 569, 444, 15, 568, 21, 103, 657, 505] | [phl, class, ]
  ↵diego, lady, food, wheelchair, good, serve, miami, mia]
  ↵
  ↵
|18  | [18, 60, 140, 64, 47, 40, 31, 35, 2, 123] | [gate, pm,
  ↵phoenix, connection, cancel, connect, day, airpo, hour, charlotte]
  ↵
  ↵
|19  | [33, 178, 95, 2, 9, 284, 42, 4, 89, 31] | [trip,
  ↵counter, philadelphia, hour, delay, stay, way, get, southwest,
  ↵day]
  +-----+
  ↵-----+
  ↵-----+

```

(continues on next page)

(continued from previous page)

- LDA results

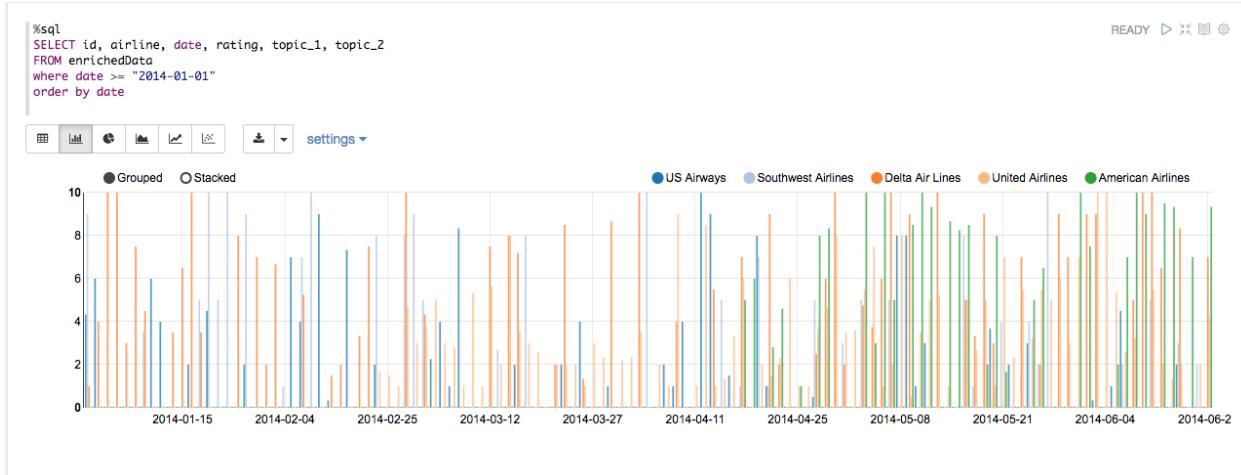
<code>id</code>	<code>airline</code>	<code>date</code>	<code>cabin</code>	<code>rating</code>	
<code>words</code>	<code>features</code>	<code>topicDistribution</code>			
<hr/>					
10551	Southwest Airlines	2013-11-06	Business	1.0	[flight, chicago, ... (4695, [0, 2, 3, 6, 11... [0.03640342580508...
10298	US Airways	2014-03-31	Business	1.0	[flight, manchest... (4695, [0, 1, 2, 6, 7, ... [0.01381306271470...
10564	Southwest Airlines	2013-09-06	Economy	10.0	[executive, plati... (4695, [0, 1, 6, 7, 11... [0.05063554352934...
10134	Delta Air Lines	2013-12-10	Economy	8.0	[msp, jfk, ... (4695, [0, 1, 3, 10, 1... [0.01494708959842...
10912	United Airlines	2014-04-07	Economy	3.0	[worst, airline, ... (4695, [0, 1, 7, 8, 13... [0.04421751181232...
10089	Delta Air Lines	2014-02-18	Economy	2.0	[dl, mia, ... (4695, [2, 4, 5, 7, 8, ... [0.02158861273876...
10385	US Airways	2013-10-21	Economy	10.0	[flew, gla, ... (4695, [0, 1, 3, 5, 14... [0.03343845991816...
10249	US Airways	2014-06-17	Economy	1.0	[friend, book, fl... (4695, [0, 2, 3, 4, 5, ... [0.02362432562165...
10289	US Airways	2014-04-12	Economy	10.0	[flew, air, ... (4695, [0, 1, 5, 8, 13... [0.01664012816210...
10654	Southwest Airlines	2012-07-10	Economy	8.0	[lhr, jfk, ... (4695, [0, 4, 5, 6, 8, ... [0.01526072330297...
10754	American Airlines	2014-05-04	Economy	10.0	[san, diego, ... (4695, [0, 2, 8, 15, 2... [0.03571177612496...
10646	Southwest Airlines	2012-08-17	Economy	7.0	[toledo, co, ... (4695, [0, 2, 3, 4, 7, ... [0.02394775146271...
10097	Delta Air Lines	2014-02-03	First Class	10.0	[honolulu, la, fi... (4695, [0, 4, 6, 7, 13... [0.02008375619661...
10132	Delta Air Lines	2013-12-16	Economy	7.0	[manchester, uk, ... (4695, [0, 1, 2, 3, 5, ... [0.01463126146601...
10560	Southwest Airlines	2013-09-20	Economy	9.0	[first, time, ... (4695, [0, 3, 7, 8, 9, ... [0.04934836409896...
10579	Southwest Airlines	2013-07-25	Economy	0.0	[plane, land, ... (4695, [2, 3, 4, 5, 7, ... [0.06106959241722...
10425	US Airways	2013-08-06	Economy	3.0	[airway, bad, pro... (4695, [2, 3, 4, 7, 8, ... [0.01770471771322...
10650	Southwest Airlines	2012-07-27	Economy	9.0	[flew, jfk, ... (4695, [0, 1, 6, 13, 1... [0.02676226245086...
10260	US Airways	2014-06-03	Economy	1.0	[february, air, u... (4695, [0, 2, 4, 17, 2... [0.02887390875079...
10202	Delta Air Lines	2013-09-14	Economy	10.0	[aug, lhr, jfk, b... (4695, [1, 2, 4, 7, 10... [0.02377704988307...

(continues on next page)

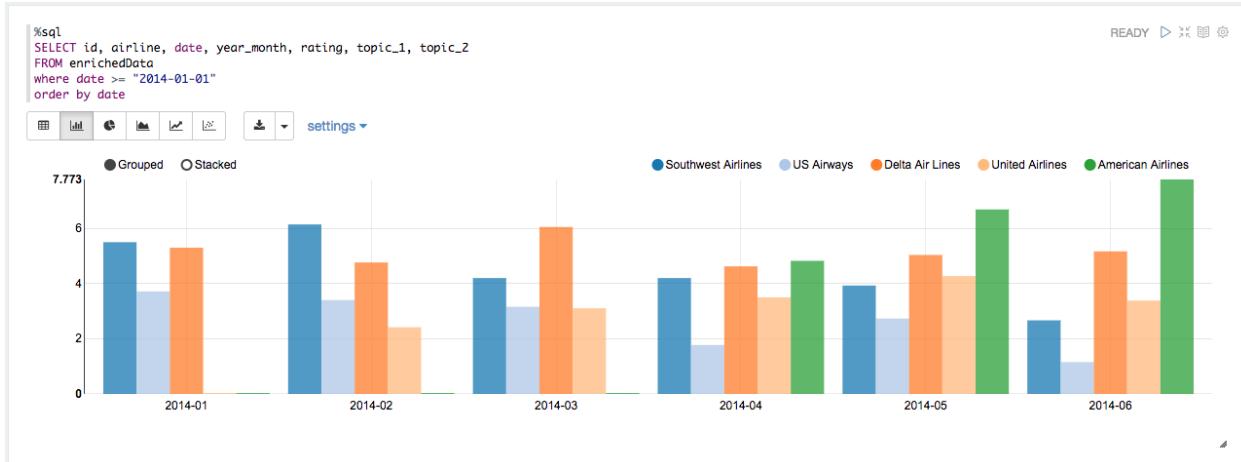
(continued from previous page)

only showing top 20 rows

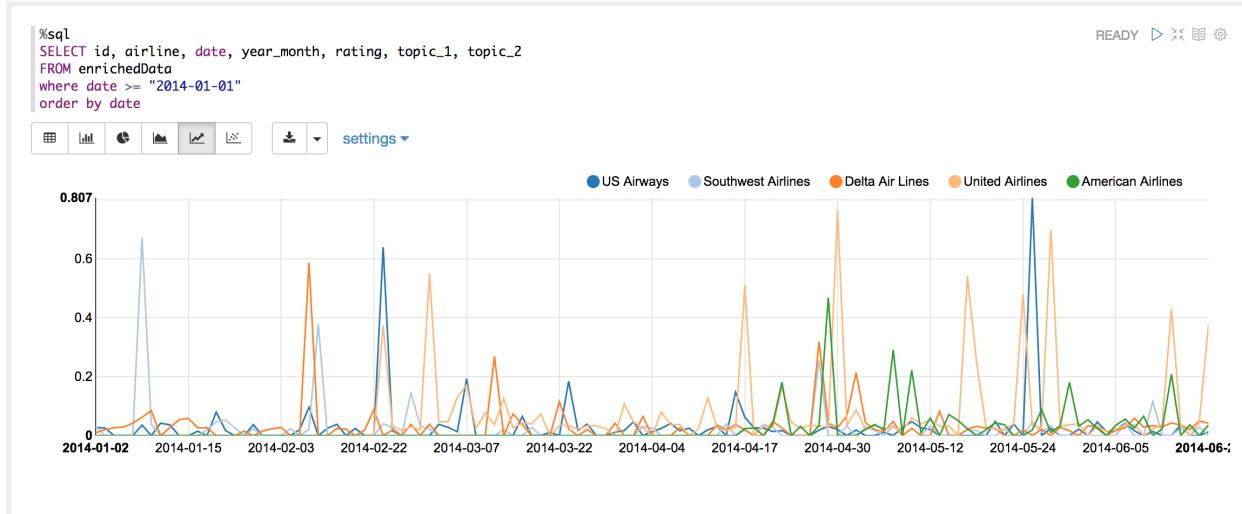
- Average rating and airlines for each day



- Average rating and airlines for each month



- Topic 1 corresponding to time line
- reviews (documents) relate to topic 1



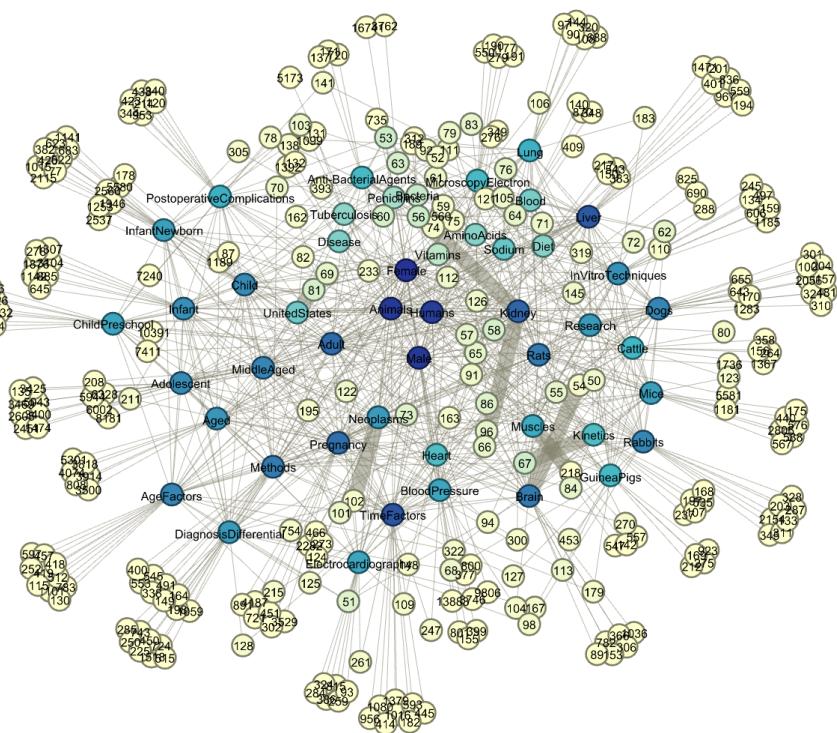
	id	airline	date	review
10263	US Airways	2014-05-25	"Delays on all booked flights. Outward bound - Dublin to Philadelphia Philadelphia to Vegas. Vegas to LA. Baggage did not arrive some hours later. Cabin staff were unfriendly and quite rude. From Dublin We were sitting at the back of the plane and and we were told ""thats what you get when you travel at the back"" . I opened my little tub of butter which had been heated in hot liquid and went all over my hand. I said to the stewardess who was passing by who could have brought me a napkin to sped by saying ""oh I know that happens"" . Only that I had a tray of food on my lap she would have had more to deal with! W baggage was to be stored in the overhead lockers or underneath the seat in front. This obviously does not apply to cabin staff back centre aisle seats of the plane it was not secured in any way. Their baggage was a danger to all the passengers in that what they preach and put staff baggage in the hold. Cabin crew were ungroomed in appearance. Homeward bound to Dublin delayed resulting in us overnighting in Orlando very grateful for the overnight accommodation provided at the Hyatt. Flew to Boarding for Dublin at Charlotte was very confused and inefficiently exercised by Gate staff - resulting in delay in take-off. En quality on those flights that had the facility. General impression overall. Very Disappointing."	

CHAPTER FOURTEEN

SOCIAL NETWORK ANALYSIS

Chinese proverb

A Touch of Cloth,linked in countless ways. – old Chinese proverb



14.1 Introduction

14.2 Co-occurrence Network

Co-occurrence networks are generally used to provide a graphic visualization of potential relationships

between people, organizations, concepts or other entities represented within written material. The generation and visualization of co-occurrence networks has become practical with the advent of electronically stored text amenable to text mining.

14.2.1 Methodology

- Build Corpus C
- Build Document-Term matrix D based on Corpus C
- Compute Term-Document matrix D^T
- Adjacency Matrix $A = D^T \cdot D$

There are four main components in this algorithm in the algorithm: Corpus C, Document-Term matrix D, Term-Document matrix D^T and Adjacency Matrix A. In this demo part, I will show how to build those four main components.

Given that we have three groups of friends, they are

```
+-----+  
| words |  
+-----+  
|[ [george] [jimmy] [john] [peter]] |  
|[ [vincent] [george] [stefan] [james]] |  
|[ [emma] [james] [olivia] [george]] |  
+-----+
```

1. Corpus C

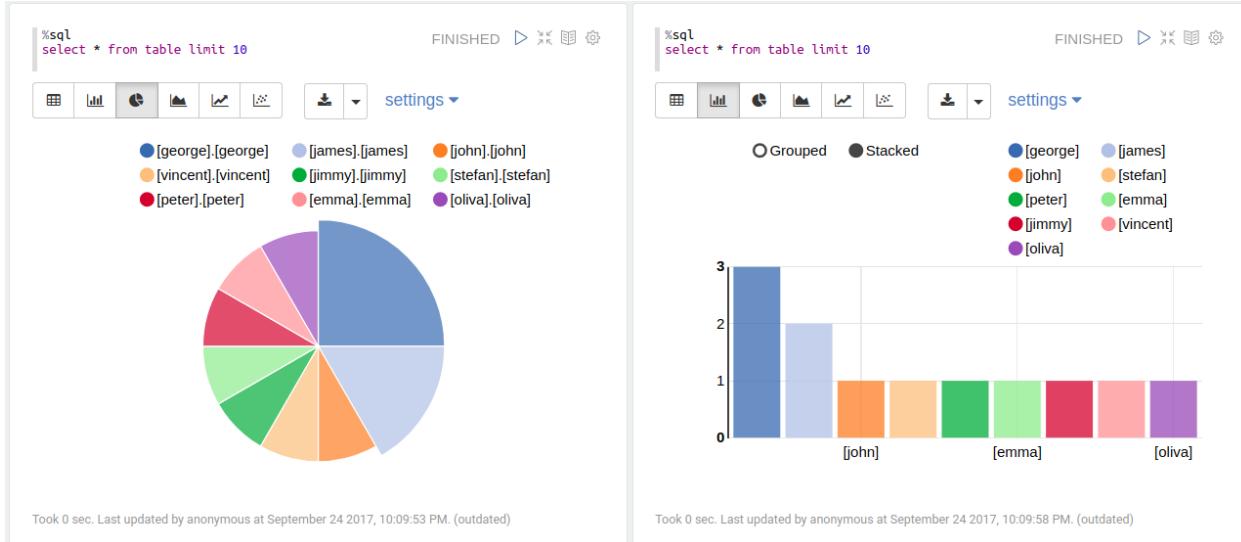
Then we can build the following corpus based on the unique elements in the given group data:

```
[u'george', u'james', u'jimmy', u'peter', u'stefan', u'veincent', u'  
→'olivia', u'john', u'emma']
```

The corresponding elements frequency:

2. Document-Term matrix D based on Corpus C (CountVectorizer)

```
from pyspark.ml.feature import CountVectorizer  
count_vectorizer_wo = CountVectorizer(inputCol='term', outputCol=  
→'features')  
# with total unique vocabulary  
countVectorizer_mod_wo = count_vectorizer_wo.fit(df)  
countVectorizer_twitter_wo = countVectorizer_mod_wo.transform(df)  
# with truncated unique vocabulary (99%)  
count_vectorizer = CountVectorizer(vocabSize=48, inputCol='term',  
→outputCol='features')  
countVectorizer_mod = count_vectorizer.fit(df)  
countVectorizer_twitter = countVectorizer_mod.transform(df)
```



```
+-----+
| features
+-----+
| (9, [0,2,3,7],[1.0,1.0,1.0,1.0]) |
| (9, [0,1,4,5],[1.0,1.0,1.0,1.0]) |
| (9, [0,1,6,8],[1.0,1.0,1.0,1.0]) |
+-----+
```

- Term-Document matrix D^T

RDD:

```
[array([ 1.,  1.,  1.]), array([ 0.,  1.,  1.]), array([ 1.,  0.,  0.
˓→]),
 array([ 1.,  0.,  0.]), array([ 0.,  1.,  0.]), array([ 0.,  1.,  0.
˓→]),
 array([ 0.,  0.,  1.]), array([ 1.,  0.,  0.]), array([ 0.,  0.,  1.
˓→])]
```

Matrix:

```
array([[ 1.,  1.,  1.],
       [ 0.,  1.,  1.],
       [ 1.,  0.,  0.],
       [ 1.,  0.,  0.],
       [ 0.,  1.,  0.],
       [ 0.,  1.,  0.],
       [ 0.,  0.,  1.],
       [ 1.,  0.,  0.],
       [ 0.,  0.,  1.]])
```

3. Adjacency Matrix $A = D^T \cdot D$

RDD:

```
[array([ 1.,  1.,  1.]), array([ 0.,  1.,  1.]), array([ 1.,  0.,  0.  
→]),  
 array([ 1.,  0.,  0.]), array([ 0.,  1.,  0.]), array([ 0.,  1.,  0.  
→]),  
 array([ 0.,  0.,  1.]), array([ 1.,  0.,  0.]), array([ 0.,  0.,  1.  
→])]
```

Matrix:

```
array([[ 3.,  2.,  1.,  1.,  1.,  1.,  1.,  1.,  1.,  1.],  
       [ 2.,  2.,  0.,  0.,  1.,  1.,  1.,  0.,  0.,  1.],  
       [ 1.,  0.,  1.,  1.,  0.,  0.,  0.,  1.,  0.,  0.],  
       [ 1.,  0.,  1.,  1.,  0.,  0.,  0.,  1.,  0.,  0.],  
       [ 1.,  1.,  0.,  0.,  1.,  1.,  0.,  0.,  0.,  0.],  
       [ 1.,  1.,  0.,  0.,  1.,  1.,  0.,  0.,  0.,  0.],  
       [ 1.,  1.,  0.,  0.,  0.,  0.,  1.,  0.,  0.,  1.],  
       [ 1.,  0.,  1.,  1.,  0.,  0.,  0.,  1.,  0.,  0.],  
       [ 1.,  1.,  0.,  0.,  0.,  0.,  1.,  0.,  0.,  1.]])
```

14.2.2 Coding Puzzle from my interview

- Problem

The attached utf-8 encoded text file contains the tags associated with an online biomedical scientific article formatted as follows (size: 100000). Each Scientific article is represented by a line in the file delimited by carriage return.

```
+-----+  
|          words |  
+-----+  
| [ACTH Syndrome, E... |  
| [Antibody Formati... |  
| [Adaptation, Phys... |  
| [Aerosol Propella... |  
+-----+  
only showing top 4 rows
```

Write a program that, using this file as input, produces a list of pairs of tags which appear TOGETHER in any order and position in at least fifty different Scientific articles. For example, in the above sample, [Female] and [Humans] appear together twice, but every other pair appears only once. Your program should output the pair list to stdout in the same form as the input (eg tag 1, tag 2n).

- My solution

The corresponding words frequency:

Output:

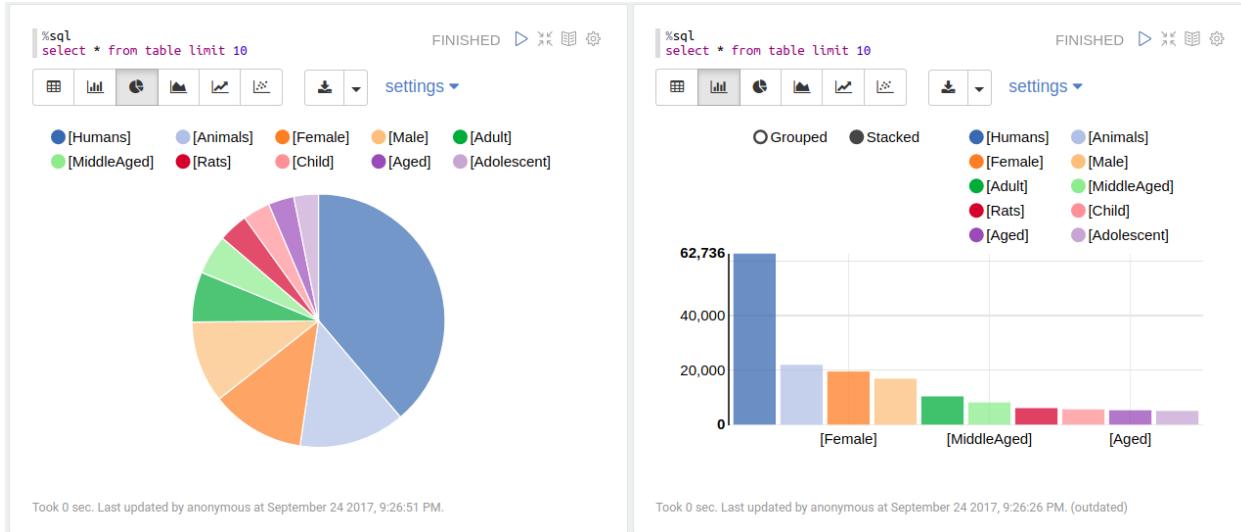


Fig. 1: Word frequency

```
+-----+-----+-----+
| term.x|term.y| freq |
+-----+-----+-----+
| Female| Humans| 16741.0 |
|     Male| Humans| 13883.0 |
|     Adult| Humans| 10391.0 |
|     Male| Female|  9806.0 |
| MiddleAged| Humans|  8181.0 |
|     Adult| Female|  7411.0 |
|     Adult|   Male|  7240.0 |
| MiddleAged|   Male|  6328.0 |
| MiddleAged| Female|  6002.0 |
| MiddleAged| Adult|  5944.0 |
+-----+-----+-----+
only showing top 10 rows
```

The corresponding Co-occurrence network:

Then you will get Figure *Co-occurrence network*

14.3 Appendix: matrix multiplication in PySpark

1. load test matrix

```
df = spark.read.csv("matrix1.txt", sep=",", inferSchema=True)
df.show()
```

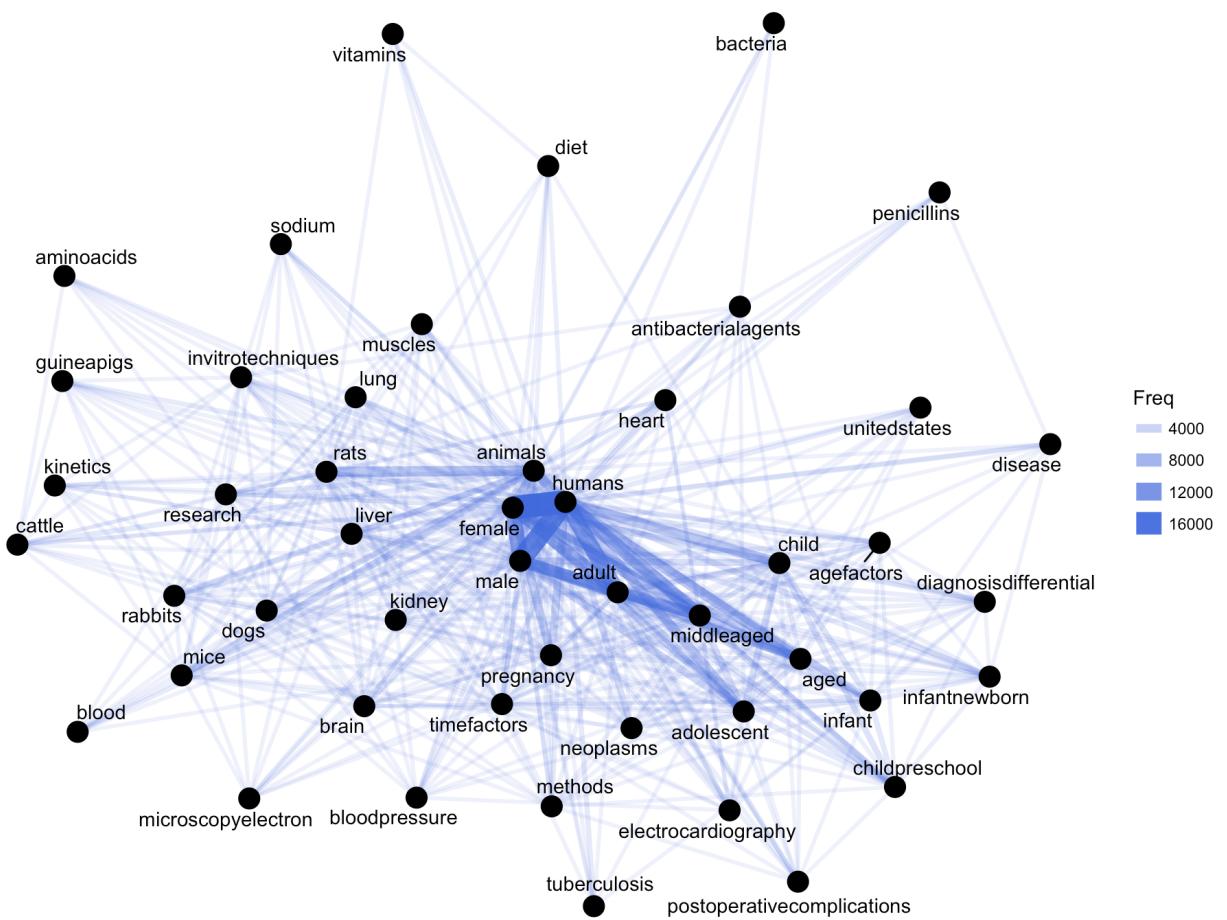


Fig. 2: Co-occurrence network

```
+---+---+---+---+
|_c0|_c1|_c2|_c3|
+---+---+---+---+
|1.2|3.4|2.3|1.1|
|2.3|1.1|1.5|2.2|
|3.3|1.8|4.5|3.3|
|5.3|2.2|4.5|4.4|
|9.3|8.1|0.3|5.5|
|4.5|4.3|2.1|6.6|
+---+---+---+---+
```

2. main function for matrix multiplication in PySpark

```
from pyspark.sql import functions as F
from functools import reduce
# reference: https://stackoverflow.com/questions/44348527/matrix-
→multiplication-at-a-in-pyspark
# do the sum of the multiplication that we want, and get
# one data frame for each column
colDFs = []
for c2 in df.columns:
    colDFs.append( df.select( [ F.sum(df[c1]*df[c2]).alias("op_{0}".
→format(i)) for i,c1 in enumerate(df.columns) ] ) )
# now union those separate data frames to build the "matrix"
mtxDF = reduce(lambda a,b: a.select(a.columns).union(b.select(a.columns)),_
→colDFs )
mtxDF.show()
```

```
+-----+-----+-----+-----+
|          op_0 |          op_1 |          op_2 |          op_3 |
+-----+-----+-----+-----+
|      152.45 | 118.8899999999999 |      57.15 | 121.44000000000001 |
| 118.889999999999 | 104.949999999999 |      38.93 |      94.71 |
|      57.15 |      38.93 | 52.54000000000006 |      55.99 |
| 121.44000000000001 |      94.71 |      55.99 | 110.1099999999999 |
+-----+-----+-----+-----+
```

3. Validation with python version

```
import numpy as np
a = np.genfromtxt("matrix1.txt", delimiter=",")
np.dot(a.T, a)
```

```
array([[152.45, 118.89,  57.15, 121.44],
       [118.89, 104.95,  38.93,  94.71],
       [ 57.15,  38.93,  52.54,  55.99],
       [121.44,  94.71,  55.99, 110.11]])
```

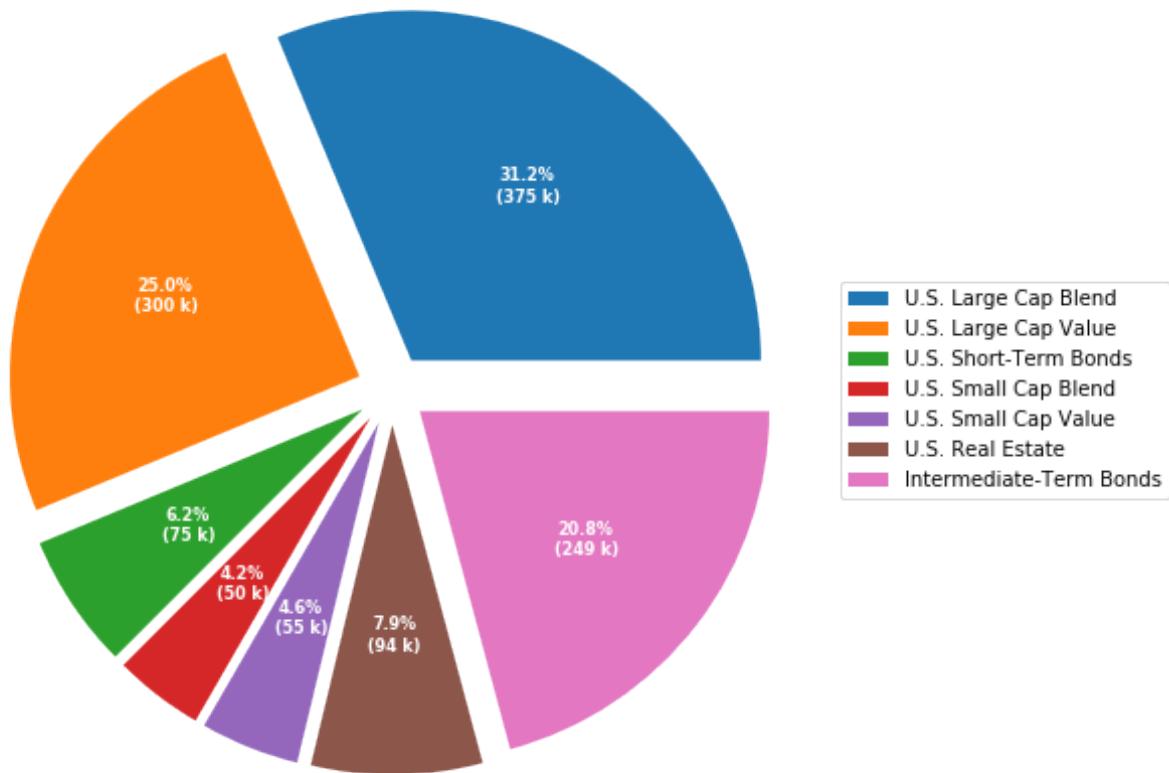
14.4 Correlation Network

TODO ..

ALS: STOCK PORTFOLIO RECOMMENDATIONS

Chinese proverb

Don't put all your eggs in one basket.



Code for the above figure:

```
import numpy as np
import matplotlib.pyplot as plt
```

(continues on next page)

(continued from previous page)

```

fig, ax = plt.subplots(figsize=(10, 8), subplot_kw=dict(aspect="equal"))

recipe = ["375 k U.S. Large Cap Blend",
          "300 k U.S. Large Cap Value",
          "75 k U.S. Short-Term Bonds",
          "50 k U.S. Small Cap Blend",
          "55 k U.S. Small Cap Value",
          "95 k U.S. Real Estate",
          "250 k Intermediate-Term Bonds"]

data = [float(x.split()[0]) for x in recipe]
ingredients = [' '.join(x.split()[2:]) for x in recipe]

print(data)
print(ingredients)
def func(pct, allvals):
    absolute = int(pct/100.*np.sum(allvals))
    return "{:.1f}%\n({:d} k)".format(pct, absolute)

explode = np.empty(len(data))#(0.1, 0.1, 0.1, 0.1, 0.1, 0.1) # explode 1st slice
explode.fill(0.1)

wedges, texts, autotexts = ax.pie(data, explode=explode, autopct=lambda pct:_
                                    func(pct, data),
                                    textprops=dict(color="w"))
ax.legend(wedges, ingredients,
          title="Stock portfolio",
          loc="center left",
          bbox_to_anchor=(1, 0, 0.5, 1))

plt.setp(autotexts, size=8, weight="bold")

#ax.set_title("Stock portfolio")

plt.show()

```

15.1 Recommender systems

Recommender systems or recommendation systems (sometimes replacing “system” with a synonym such as platform or engine) are a subclass of information filtering system that seek to predict the “rating” or “preference” that a user would give to an item.”

The main idea is to build a matrix users R items rating values and try to factorize it, to recommend main products rated by other users. A popular approach for this is matrix factorization is Alternating Least Squares (ALS)

15.2 Alternating Least Squares

Apache Spark ML implements ALS for collaborative filtering, a very popular algorithm for making recommendations.

ALS recommender is a matrix factorization algorithm that uses Alternating Least Squares with Weighted-Lambda-Regularization (ALS-WR). It factors the user to item matrix A into the user-to-feature matrix U and the item-to-feature matrix M : It runs the ALS algorithm in a parallel fashion. The ALS algorithm should uncover the latent factors that explain the observed user to item ratings and tries to find optimal factor weights to minimize the least squares between predicted and actual ratings.

<https://www.elenacuoco.com/2016/12/22/alternating-least-squares-als-spark-ml/>

15.3 Demo

- The Jupyter notebook can be download from [ALS Recommender systems](#).
- The data can be download from [German Credit](#).

15.3.1 Load and clean data

1. Set up spark context and SparkSession

```
from pyspark.sql import SparkSession

spark = SparkSession \
    .builder \
    .appName("Python Spark RFM example") \
    .config("spark.some.config.option", "some-value") \
    .getOrCreate()
```

2. Load dataset

```
df_raw = spark.read.format('com.databricks.spark.csv') \
    .options(header='true', \
    inferschema='true') \
    .load("Online Retail.csv", header=True);
```

check the data set

```
df_raw.show(5)
df_raw.printSchema()
```

Then you will get

InvoiceNo	StockCode	Description	Quantity	Country
22345	ST12A	Tea, Lipton, English Breakfast	100	GBR
34567	ST12A	Tea, Lipton, English Breakfast	100	GBR
54678	ST12A	Tea, Lipton, English Breakfast	100	GBR
54679	ST12A	Tea, Lipton, English Breakfast	100	GBR

(continues on next page)

(continued from previous page)

<hr/>						
536365 85123A WHITE HANGING HEA...	6 12/1/10 8:26	2.55				
17850 United Kingdom						
536365 71053 WHITE METAL LANTERN	6 12/1/10 8:26	3.39				
17850 United Kingdom						
536365 84406B CREAM CUPID HEART...	8 12/1/10 8:26	2.75				
17850 United Kingdom						
536365 84029G KNITTED UNION FLA...	6 12/1/10 8:26	3.39				
17850 United Kingdom						
536365 84029E RED WOOLLY HOTTIE...	6 12/1/10 8:26	3.39				
17850 United Kingdom						
<hr/>						
only showing top 5 rows						
<hr/>						
root						
-- InvoiceNo: string (nullable = true)						
-- StockCode: string (nullable = true)						
-- Description: string (nullable = true)						
-- Quantity: integer (nullable = true)						
-- InvoiceDate: string (nullable = true)						
-- UnitPrice: double (nullable = true)						
-- CustomerID: integer (nullable = true)						
-- Country: string (nullable = true)						

3. Data clean and data manipulation

- check and remove the null values

```
from pyspark.sql.functions import count

def my_count(df_in):
    df_in.agg( *[ count(c).alias(c) for c in df_in.columns ] ).show()
```

```
import pyspark.sql.functions as F
from pyspark.sql.functions import round
df_raw = df_raw.withColumn('Asset',round( F.col('Quantity') * F.col('UnitPrice')
    ), 2 ))
df = df_raw.withColumnRenamed('StockCode', 'Cusip')\
    .select('CustomerID','Cusip','Quantity','UnitPrice','Asset')
```

```
my_count(df)
```

CustomerID	Cusip	Quantity	UnitPrice	Asset
406829 541909 541909 541909 541909				

Since the count results are not the same, we have some null value in the CustomerID column. We can

drop these records from the dataset.

```
df = df.filter(F.col('Asset')>=0)
df = df.dropna(how='any')
my_count(df)
```

```
+-----+-----+-----+-----+
|CustomerID| Cusip|Quantity|UnitPrice| Asset|
+-----+-----+-----+-----+
| 397924 | 397924 | 397924 | 397924 |
+-----+-----+-----+-----+
```

```
df.show(3)

+-----+-----+-----+-----+
|CustomerID| Cusip|Quantity|UnitPrice|Asset|
+-----+-----+-----+-----+
| 17850 | 85123A | 6 | 2.55 | 15.3 |
| 17850 | 71053 | 6 | 3.39 | 20.34 |
| 17850 | 84406B | 8 | 2.75 | 22.0 |
+-----+-----+-----+-----+
only showing top 3 rows
```

- Convert the Cusip to consistent format

```
from pyspark.sql.functions import udf
from pyspark.sql.types import StringType, DoubleType

def toUpper(s):
    return s.upper()

upper_udf = udf(lambda x: toUpper(x), StringType())
```

- Find the most top n stockes

```
pop = df.groupBy('Cusip') \
    .agg(F.count('CustomerID').alias('Customers'), F.round(F.sum('Asset'), 2) \
    .alias('TotalAsset')) \
    .sort([F.col('Customers'), F.col('TotalAsset')], ascending=[0, 0])

pop.show(5)
```

```
+-----+-----+
| Cusip|Customers|TotalAsset|
+-----+-----+
| 85123A | 2035 | 100603.5 |
| 22423 | 1724 | 142592.95 |
| 85099B | 1618 | 85220.78 |
| 84879 | 1408 | 56580.34 |
| 47566 | 1397 | 68844.33 |
+-----+-----+
only showing top 5 rows
```

15.3.2 Build feature matrix

- Fetch the top n cusip list

```
top = 10
cusip_lst = pd.DataFrame(pop.select('Cusip').head(top)).astype('str').iloc[:, -1].tolist()
cusip_lst.insert(0, 'CustomerID')
```

- Create the portfolio table for each customer

```
pivot_tab = df.groupby('CustomerID').pivot('Cusip').sum('Asset')
pivot_tab = pivot_tab.fillna(0)
```

- Fetch the most n stock's portfolio table for each customer

```
selected_tab = pivot_tab.select(cusip_lst)
selected_tab.show(4)
```

```
+-----+-----+-----+-----+-----+-----+-----+-----+
|CustomerID|85123A|22423|85099B|84879|47566|20725|22720|20727|POST|23203|
+-----+-----+-----+-----+-----+-----+-----+-----+
|    16503|    0.0|    0.0|    0.0|    0.0|    0.0|    0.0|    0.0|   33.0|    0.0|    0.0|
|    15727|  123.9|  25.5|    0.0|    0.0|    0.0|  33.0|  99.0|    0.0|    0.0|    0.0|
|    14570|    0.0|    0.0|    0.0|    0.0|    0.0|    0.0|    0.0|    0.0|    0.0|    0.0|
|    14450|    0.0|    0.0|   8.32|    0.0|    0.0|    0.0|   49.5|    0.0|    0.0|    0.0|
+-----+-----+-----+-----+-----+-----+-----+-----+
only showing top 4 rows
```

- Build the rating matrix

```
def elemwiseDiv(df_in):
    num = len(df_in.columns)
    temp = df_in.rdd.map(lambda x: list(flatten([x[0], [x[i]/float(sum(x[1:])) if sum(x[1:])>0 else -x[i] for i in range(1, num)]])))
    return spark.createDataFrame(temp, df_in.columns)

ratings = elemwiseDiv(selected_tab)
```

```
ratings.show(4)
```

```
+-----+-----+-----+-----+-----+-----+-----+
|CustomerID|85123A|22423|85099B|84879|47566|20725|22720|20727|POST|23203|
+-----+-----+-----+-----+-----+-----+-----+
|    16503|    0.0|    0.0|    0.0|    0.0|    0.0|    0.0|    0.0|   1.0|    0.0|    0.0|
|    15727|    0.44|  0.09|    0.0|    0.0|    0.0|  0.12|  0.35|    0.0|    0.0|    0.0|
```

(continues on next page)

(continued from previous page)

14570 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0 0.0
14450 0.0 0.0 0.14 0.0 0.0 0.0 0.86 0.0 0.0 0.0 0.0 0.0

- Convert rating matrix to long table

```
from pyspark.sql.functions import array, col, explode, struct, lit

def to_long(df, by):
    """
    reference: https://stackoverflow.com/questions/37864222transpose-
    ↪column-to-row-with-spark
    """

    # Filter dtypes and split into column names and type description
    cols, dtypes = zip(*((c, t) for (c, t) in df.dtypes if c not in by))
    # Spark SQL supports only homogeneous columns
    assert len(set(dtypes)) == 1, "All columns have to be of the same type"

    # Create and explode an array of (column_name, column_value) structs
    kvs = explode(array([
        struct(lit(c).alias("Cusip"), col(c).alias("rating")) for c in cols
    ])).alias("kvs")
```

```
df_all = to_long(ratings, ['CustomerID'])
df_all.show(5)
```

CustomerID	Cusip	rating
16503	85123A	0.0
16503	22423	0.0
16503	85099B	0.0
16503	84879	0.0
16503	47566	0.0

only showing top 5 rows

- Convert the string Cusip to numerical index

```
from pyspark.ml.feature import StringIndexer
# Index labels, adding metadata to the label column
labelIndexer = StringIndexer(inputCol='Cusip',
                             outputCol='indexedCusip').fit(df_all)
df_all = labelIndexer.transform(df_all)

df_all.show(5, True)
df_all.printSchema()
```

CustomerID	indexedCusip
16503	0
16503	1
16503	2
16503	3
16503	4

(continues on next page)

(continued from previous page)

```
|CustomerID| Cusip|rating|indexedCusip|
+-----+-----+-----+
| 16503|85123A| 0.0| 6.0|
| 16503| 22423| 0.0| 9.0|
| 16503|85099B| 0.0| 5.0|
| 16503| 84879| 0.0| 1.0|
| 16503| 47566| 0.0| 0.0|
+-----+-----+-----+
only showing top 5 rows

root
|-- CustomerID: long (nullable = true)
|-- Cusip: string (nullable = false)
|-- rating: double (nullable = true)
|-- indexedCusip: double (nullable = true)
```

15.3.3 Train model

- build train and test dataset

```
train, test = df_all.randomSplit([0.8,0.2])

train.show(5)
test.show(5)
```

```
+-----+-----+-----+-----+
|CustomerID|Cusip|indexedCusip| rating|
+-----+-----+-----+-----+
| 12940|20725| 2.0| 0.0|
| 12940|20727| 4.0| 0.0|
| 12940|22423| 9.0| 0.49990198000392083|
| 12940|22720| 3.0| 0.0|
| 12940|23203| 7.0| 0.0|
+-----+-----+-----+-----+
only showing top 5 rows

+-----+-----+-----+-----+
|CustomerID|Cusip|indexedCusip| rating|
+-----+-----+-----+-----+
| 12940|84879| 1.0| 0.1325230346990786|
| 13285|20725| 2.0| 0.2054154995331466|
| 13285|20727| 4.0| 0.2054154995331466|
| 13285|47566| 0.0| 0.0|
| 13623|23203| 7.0| 0.0|
+-----+-----+-----+-----+
only showing top 5 rows
```

- train model

```

import itertools
from math import sqrt
from operator import add
import sys
from pyspark.ml.recommendation import ALS

from pyspark.ml.evaluation import RegressionEvaluator

evaluator = RegressionEvaluator(metricName="rmse", labelCol="rating",
                                 predictionCol="prediction")
def computeRmse(model, data):
    """
    Compute RMSE (Root mean Squared Error).
    """
    predictions = model.transform(data)
    rmse = evaluator.evaluate(predictions)
    print("Root-mean-square error = " + str(rmse))
    return rmse

#train models and evaluate them on the validation set

ranks = [4,5]
lambdas = [0.05]
numIters = [30]
bestModel = None
bestValidationRmse = float("inf")
bestRank = 0
bestLambda = -1.0
bestNumIter = -1

val = test.na.drop()
for rank, lmbda, numIter in itertools.product(ranks, lambdas, numIters):
    als = ALS(rank=rank, maxIter=numIter, regParam=lmbda, numUserBlocks=10,
              numItemBlocks=10, implicitPrefs=False,
              alpha=1.0,
              userCol="CustomerID", itemCol="indexedCusip", seed=1, ratingCol=
              "rating", nonnegative=True)
    model=als.fit(train)

    validationRmse = computeRmse(model, val)
    print("RMSE (validation) = %f for the model trained with " %
          validationRmse +
          "rank = %d, lambda = %.1f, and numIter = %d." % (rank, lmbda,
          numIter))
    if (validationRmse, bestValidationRmse):
        bestModel = model
        bestValidationRmse = validationRmse
        bestRank = rank
        bestLambda = lmbda
        bestNumIter = numIter

model = bestModel

```

15.3.4 Make prediction

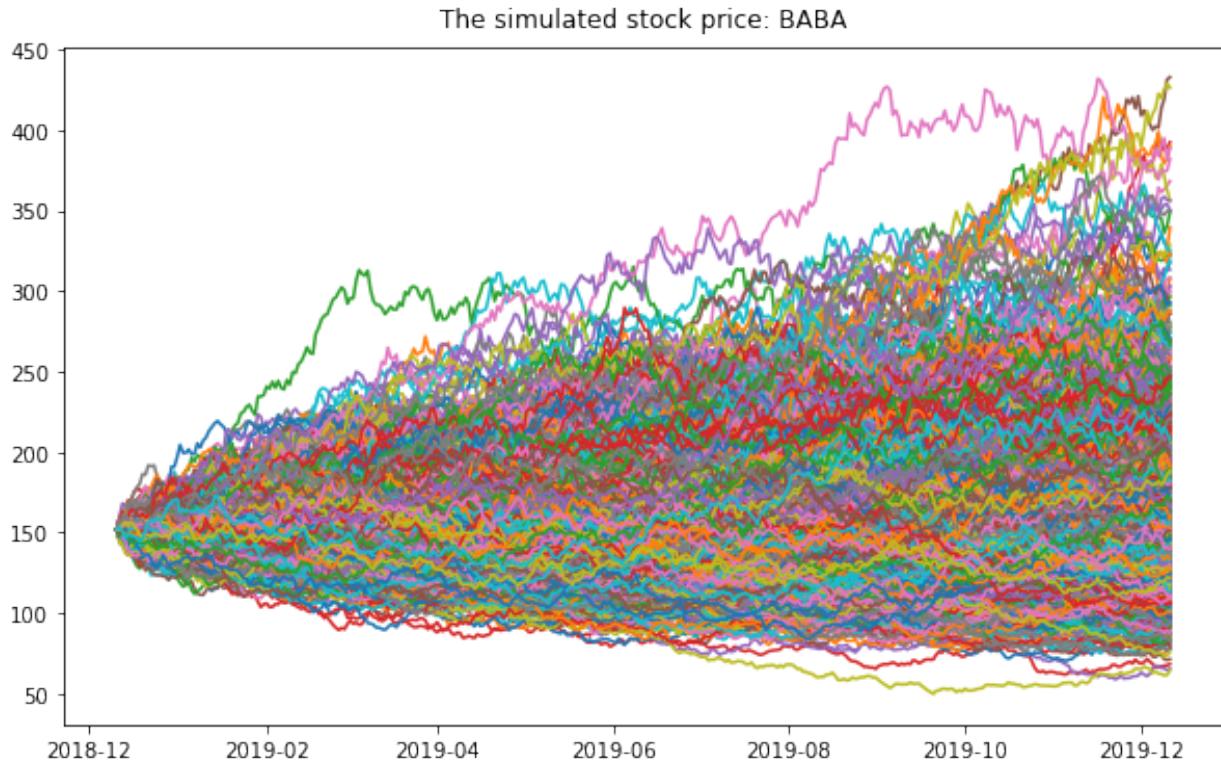
- make prediction

```
topredict=test[test['rating']==0]

predictions=model.transform(topredict)
predictions.filter(predictions.prediction>0) \
    .sort([F.col('CustomerID'),F.col('Cusip')],ascending=[0,0]).show(5)
```

```
+-----+-----+-----+-----+
|CustomerID| Cusip|indexedCusip|rating|  prediction|
+-----+-----+-----+-----+
|     18283| 47566|          0.0|   0.0|  0.01625076|
|     18282|85123A|          6.0|   0.0|  0.057172246|
|     18282| 84879|          1.0|   0.0|  0.059531752|
|     18282| 23203|          7.0|   0.0|  0.010502596|
|     18282| 22720|          3.0|   0.0|  0.053893942|
+-----+-----+-----+-----+
only showing top 5 rows
```

MONTE CARLO SIMULATION



Monte Carlo simulations are just a way of estimating a fixed parameter by repeatedly generating random numbers. More details can be found at [A Zero Math Introduction to Markov Chain Monte Carlo Methods](#).

Monte Carlo simulation is a technique used to understand the impact of risk and uncertainty in financial, project management, cost, and other forecasting models. A Monte Carlo simulator helps one visualize most or all of the potential outcomes to have a better idea regarding the risk of a decision. More details can be found at [The house always wins](#).

16.1 Simulating Casino Win

We assume that the player John has the 49% chance to win the game and the wager will be \$5 per game.

```

import numpy as np
import pandas as pd
import matplotlib.pyplot as plt

start_m = 100
wager = 5
bets = 100
trials = 1000

trans = np.vectorize(lambda t: -wager if t <=0.51 else wager)

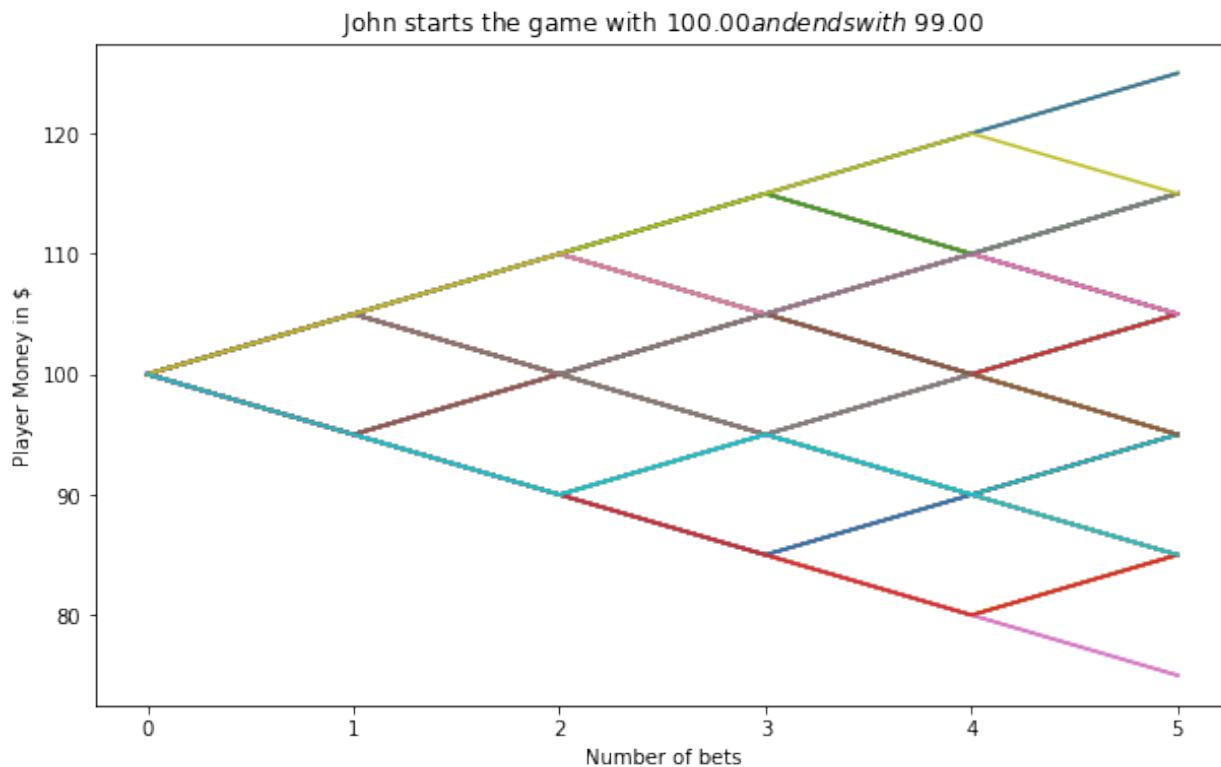
fig = plt.figure(figsize=(10, 6))
ax = fig.add_subplot(1,1,1)

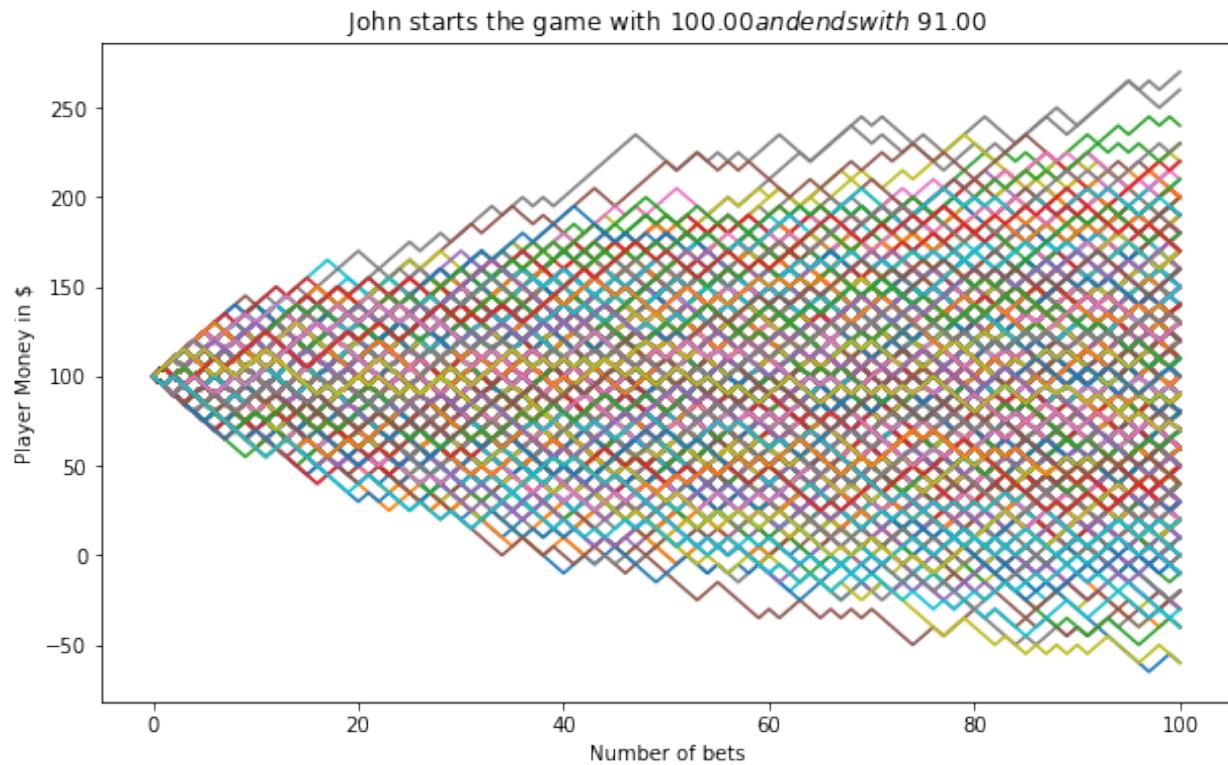
end_m = []

for i in range(trials):
    money = reduce(lambda c, x: c + [c[-1] + x], trans(np.random.
    ↪random(bets)), [start_m])
    end_m.append(money[-1])
    plt.plot(money)

plt.ylabel('Player Money in $')
plt.xlabel('Number of bets')
plt.title(("John starts the game with $ %.2f and ends with $ %.2f")%(start_m,
    ↪sum(end_m)/len(end_m)))
plt.show()

```





16.2 Simulating a Random Walk

16.2.1 Fetch the historical stock price

1. Fetch the data. If you need the code for this piece, you can contact with me.

```
stock.tail(4)

+-----+-----+-----+-----+-----+-----+
|      Date|      Open|      High|      Low|      Close| Adj Close|    Volume|
+-----+-----+-----+-----+-----+-----+
|2018-12-07|155.399994|158.050003|151.729996|153.059998|153.059998|17447900|
|2018-12-10|150.389999|152.809998|147.479996|151.429993|151.429993|15525500|
|2018-12-11|155.259995|156.240005|150.899994|151.830002|151.830002|13651900|
|2018-12-12|155.240005|156.169998|151.429993|      151.5|      151.5|16597900|
+-----+-----+-----+-----+-----+-----+
```

2. Convert the str type date to date type

```
stock['Date'] = pd.to_datetime(stock['Date'])
```

3. Data visualization

```
# Plot everything by leveraging the very powerful matplotlib package
width = 10
```

(continues on next page)

(continued from previous page)

```

height = 6
data = stock
fig = plt.figure(figsize=(width, height))
ax = fig.add_subplot(1,1,1)
ax.plot(data.Date, data.Close, label='Close')
ax.plot(data.Date, data.High, label='High')
# ax.plot(data.Date, data.Low, label='Low')
ax.set_xlabel('Date')
ax.set_ylabel('price ($)')
ax.legend()
ax.set_title('Stock price: ' + ticker, y=1.01)
#plt.xticks(rotation=70)
plt.show()

# Plot everything by leveraging the very powerful matplotlib package
fig = plt.figure(figsize=(width, height))
ax = fig.add_subplot(1,1,1)
ax.plot(data.Date, data.Volume, label='Volume')
#ax.plot(data.Date, data.High, label='High')
# ax.plot(data.Date, data.Low, label='Low')
ax.set_xlabel('Date')
ax.set_ylabel('Volume')
ax.legend()
ax.set_title('Stock volume: ' + ticker, y=1.01)
#plt.xticks(rotation=70)
plt.show()

```

16.2.2 Calculate the Compound Annual Growth Rate

The formula for Compound Annual Growth Rate (CAGR) is very useful for investment analysis. It may also be referred to as the annualized rate of return or annual percent yield or effective annual rate, depending on the algebraic form of the equation. Many investments such as stocks have returns that can vary wildly. The CAGR formula allows you to calculate a “smoothed” rate of return that you can use to compare to other investments. The formula is defined as (more details can be found at [CAGR Calculator and Formula](#))

$$\text{CAGR} = \left(\frac{\text{End Value}}{\text{Start Value}} \right)^{\frac{365}{\text{Days}}} - 1$$

```

days = (stock.Date.iloc[-1] - stock.Date.iloc[0]).days
cagr = (((stock['Adj Close'].iloc[-1]) / stock['Adj Close'].iloc[0])) ** (1/(365.0/days)) - 1
print ('CAGR =', str(round(cagr, 4)*100)+"%")
mu = cagr

```

16.2.3 Calculate the annual volatility

A stock’s volatility is the variation in its price over a period of time. For example, one stock may have a tendency to swing wildly higher and lower, while another stock may move in much steadier, less turbulent

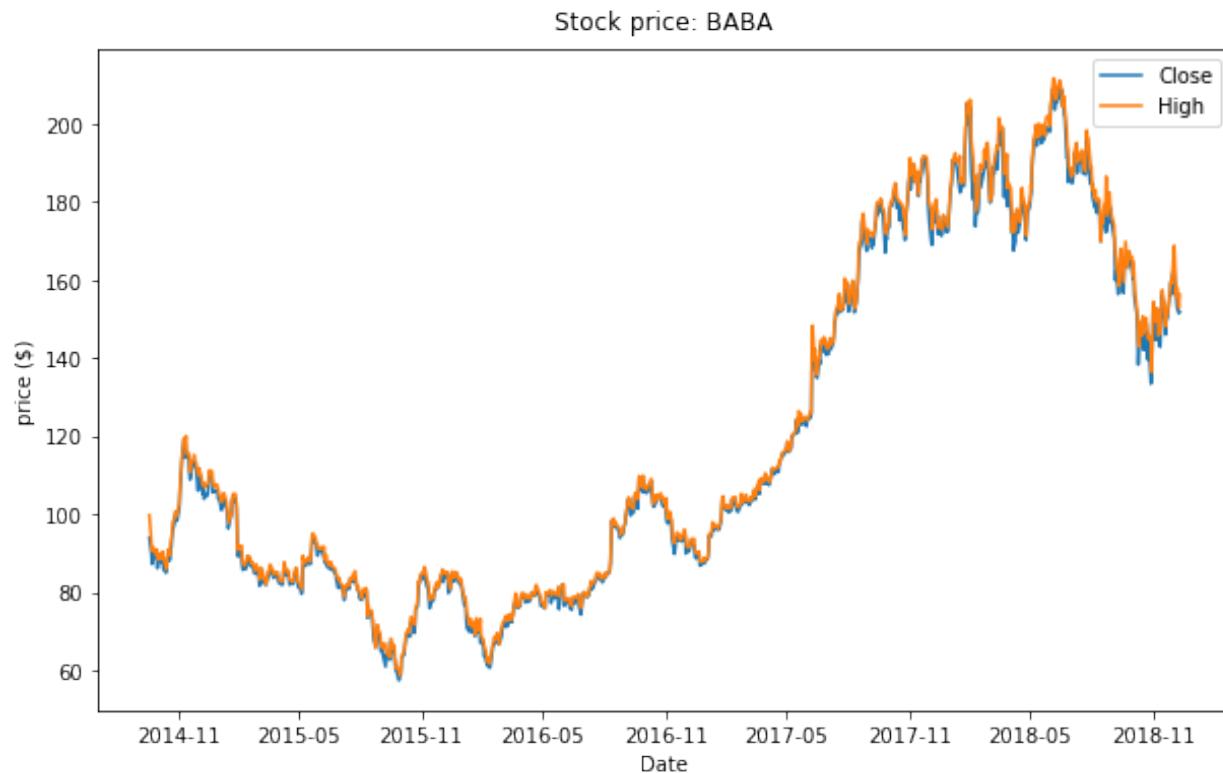


Fig. 1: Historical Stock Price

way. Both stocks may end up at the same price at the end of day, but their path to that point can vary wildly. First, we create a series of percentage returns and calculate the annual volatility of returns Annualizing volatility. To present this volatility in annualized terms, we simply need to multiply our daily standard deviation by the square root of 252. This assumes there are 252 trading days in a given year. More details can be found at [How to Calculate Annualized Volatility](#).

```
stock['Returns'] = stock['Adj Close'].pct_change()
vol = stock['Returns'].std()*np.sqrt(252)
```

16.2.4 Create matrix of daily returns

1. Create matrix of daily returns using random normal distribution Generates an RDD matrix comprised of i.i.d. samples from the uniform distribution $U(0.0, 1.0)$.

```
S = stock['Adj Close'].iloc[-1] #starting stock price (i.e. last available
                                ↵real stock price)
T = 5 #Number of trading days
mu = cagr #Return
vol = vol #Volatility
trials = 10000

mat = RandomRDDs.normalVectorRDD(sc, trials, T, seed=1)
```

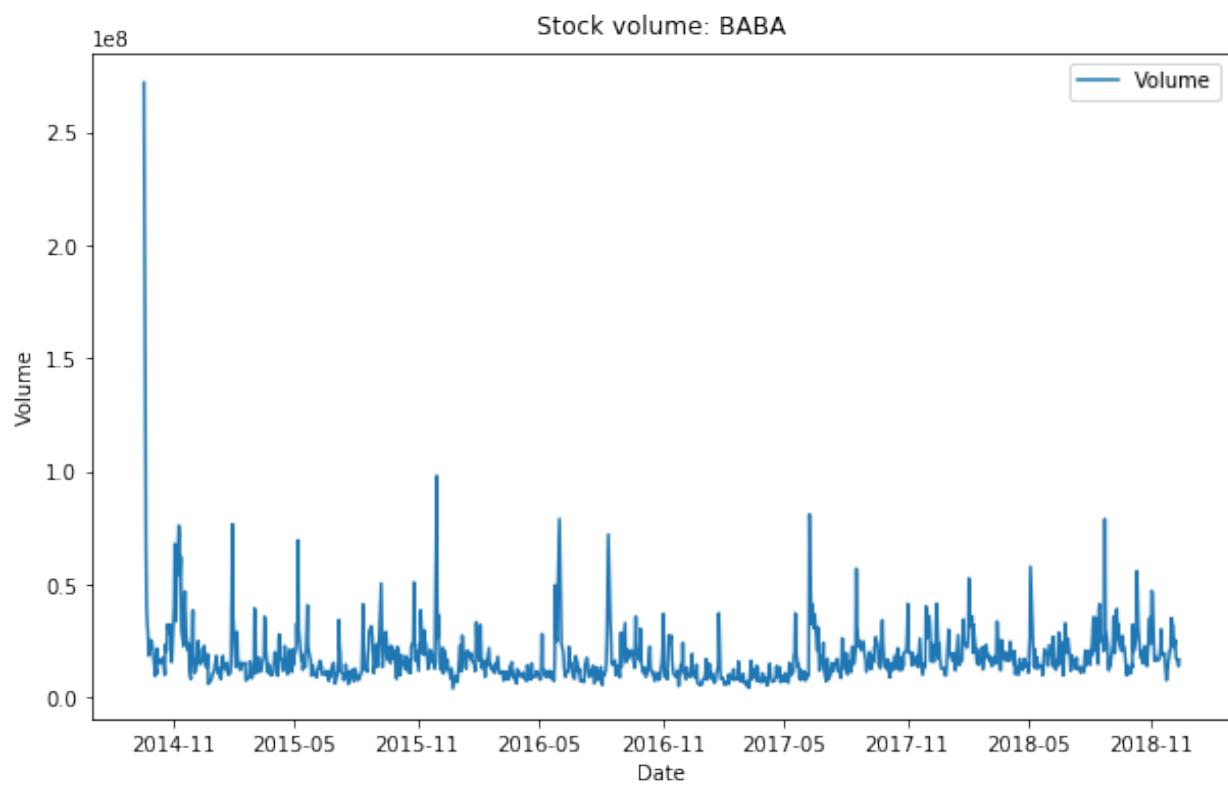


Fig. 2: Historical Stock Volume

2. Transform the distribution in the generated RDD from $U(0.0, 1.0)$ to $U(a, b)$, use RandomRDDs.uniformRDD(sc, n, p, seed) .map(lambda v: a + (b - a) * v)

```
a = mu/T
b = vol/math.sqrt(T)
v = mat.map(lambda x: a + (b - a) * x)
```

3. Convert Rdd mstrix to dataframe

```
df = v.map(lambda x: [round(i, 6)+1 for i in x]).toDF()
df.show(5)
```

```
+-----+-----+-----+-----+-----+
|      _1|      _2|      _3|      _4|      _5|
+-----+-----+-----+-----+-----+
| 0.935234| 1.162894| 1.07972| 1.238257| 1.066136|
| 0.878456| 1.045922| 0.990071| 1.045552| 0.854516|
| 1.186472| 0.944777| 0.742247| 0.940023| 1.220934|
| 0.872928| 1.030882| 1.248644| 1.114262| 1.063762|
| 1.09742| 1.188537| 1.137283| 1.162548| 1.024612|
+-----+-----+-----+-----+-----+
only showing top 5 rows
```

```
from pyspark.sql.functions import lit
S = stock['Adj Close'].iloc[-1]
price = df.withColumn('init_price', lit(S))
```

```
price.show(5)

+-----+-----+-----+-----+-----+-----+
|      _1|      _2|      _3|      _4|      _5| init_price |
+-----+-----+-----+-----+-----+-----+
| 0.935234| 1.162894| 1.07972| 1.238257| 1.066136|     151.5 |
| 0.878456| 1.045922| 0.990071| 1.045552| 0.854516|     151.5 |
| 1.186472| 0.944777| 0.742247| 0.940023| 1.220934|     151.5 |
| 0.872928| 1.030882| 1.248644| 1.114262| 1.063762|     151.5 |
| 1.09742| 1.188537| 1.137283| 1.162548| 1.024612|     151.5 |
+-----+-----+-----+-----+-----+
only showing top 5 rows
```

```
price = price.withColumn('day_0', col('init_price'))
price.show(5)
```

```
+-----+-----+-----+-----+-----+-----+
|      _1|      _2|      _3|      _4|      _5| init_price| day_0 |
+-----+-----+-----+-----+-----+-----+
| 0.935234| 1.162894| 1.07972| 1.238257| 1.066136|     151.5 | 151.5 |
| 0.878456| 1.045922| 0.990071| 1.045552| 0.854516|     151.5 | 151.5 |
| 1.186472| 0.944777| 0.742247| 0.940023| 1.220934|     151.5 | 151.5 |
| 0.872928| 1.030882| 1.248644| 1.114262| 1.063762|     151.5 | 151.5 |
| 1.09742| 1.188537| 1.137283| 1.162548| 1.024612|     151.5 | 151.5 |
+-----+-----+-----+-----+-----+
```

(continues on next page)

(continued from previous page)

```
+-----+-----+-----+-----+-----+-----+
only showing top 5 rows
```

16.2.5 Monte Carlo Simulation

```
from pyspark.sql.functions import round
for name in price.columns[:-2]:
    price = price.withColumn('day'+name, round(col(name)*col('init_price'),2))
    price = price.withColumn('init_price', col('day'+name))
```

```
price.show(5)

+-----+-----+-----+-----+-----+-----+
|      _1|      _2|      _3|      _4|      _5|init_price|day_0| day_1| day_2|_
|day_3| day_4| day_5|
+-----+-----+-----+-----+-----+-----+
|0.935234|1.162894| 1.07972|1.238257|1.066136|     234.87|151.5|141.69|164.
| 77|177.91| 220.3|234.87|
|0.878456|1.045922|0.990071|1.045552|0.854516|     123.14|151.5|133.09| 139.
| 2|137.82| 144.1|123.14|
|1.186472|0.944777|0.742247|0.940023|1.220934|     144.67|151.5|179.75|169.
| 82|126.05|118.49|144.67|
|0.872928|1.030882|1.248644|1.114262|1.063762|     201.77|151.5|132.25|136.
| 33|170.23|189.68|201.77|
| 1.09742|1.188537|1.137283|1.162548|1.024612|     267.7|151.5|166.26|197.
| 61|224.74|261.27| 267.7|
+-----+-----+-----+-----+-----+-----+
only showing top 5 rows
```

16.2.6 Summary

```
selected_col = [name for name in price.columns if 'day_' in name]

simulated = price.select(selected_col)
simulated.describe().show()
```

```
+-----+-----+-----+-----+-----+
|summary|2018-12-12| 2018-12-13| 2018-12-14| 2018-12-17|_
|        |2018-12-18| 2018-12-19|          |          |
+-----+-----+-----+-----+-----+
|  count| 10000.0| 10000.0| 10000.0| 10000.0|_
|        |10000.0| 10000.0|          |          |
+-----+-----+-----+-----+-----+
```

(continues on next page)

(continued from previous page)

mean 151.5 155.1164370000002	158.489058 162.2371320000003 ↵
↪ 166.049375 170.006525	
std 0.0 18.313783237787845 26.460919262517276 33.	
↪ 37780495150803 39.369101074463416 45.148120695490846	
min 151.5 88.2 74.54 65.87 ↵	
↪ 68.21 58.25	
25% 151.5 142.485 140.15 138.72 ↵	
↪ 138.365 137.33	
50% 151.5 154.97 157.175 159.82 ↵	
↪ 162.59 165.0450000000002	
75% 151.5 167.445 175.48499999999999 182.8625 ↵	
↪ 189.725 196.975	
max 151.5 227.48 275.94 319.17 ↵	
↪ 353.59 403.68	
+-----+-----+-----+-----+-----+	
↪ -----+-----+-----+-----+-----+	

```
data_plt = simulated.toPandas()
days = pd.date_range(stock['Date'].iloc[-1], periods= T+1, freq='B').date

width = 10
height = 6
fig = plt.figure(figsize=(width, height))
ax = fig.add_subplot(1,1,1)

days = pd.date_range(stock['Date'].iloc[-1], periods= T+1, freq='B').date

for i in range(trials):
    plt.plot(days, data_plt.iloc[i])
ax.set_xlabel('Date')
ax.set_ylabel('price ($)')
ax.set_title('Simulated Stock price: ' + ticker, y=1.01)
plt.show()
```

16.2.7 One-year Stock price simulation

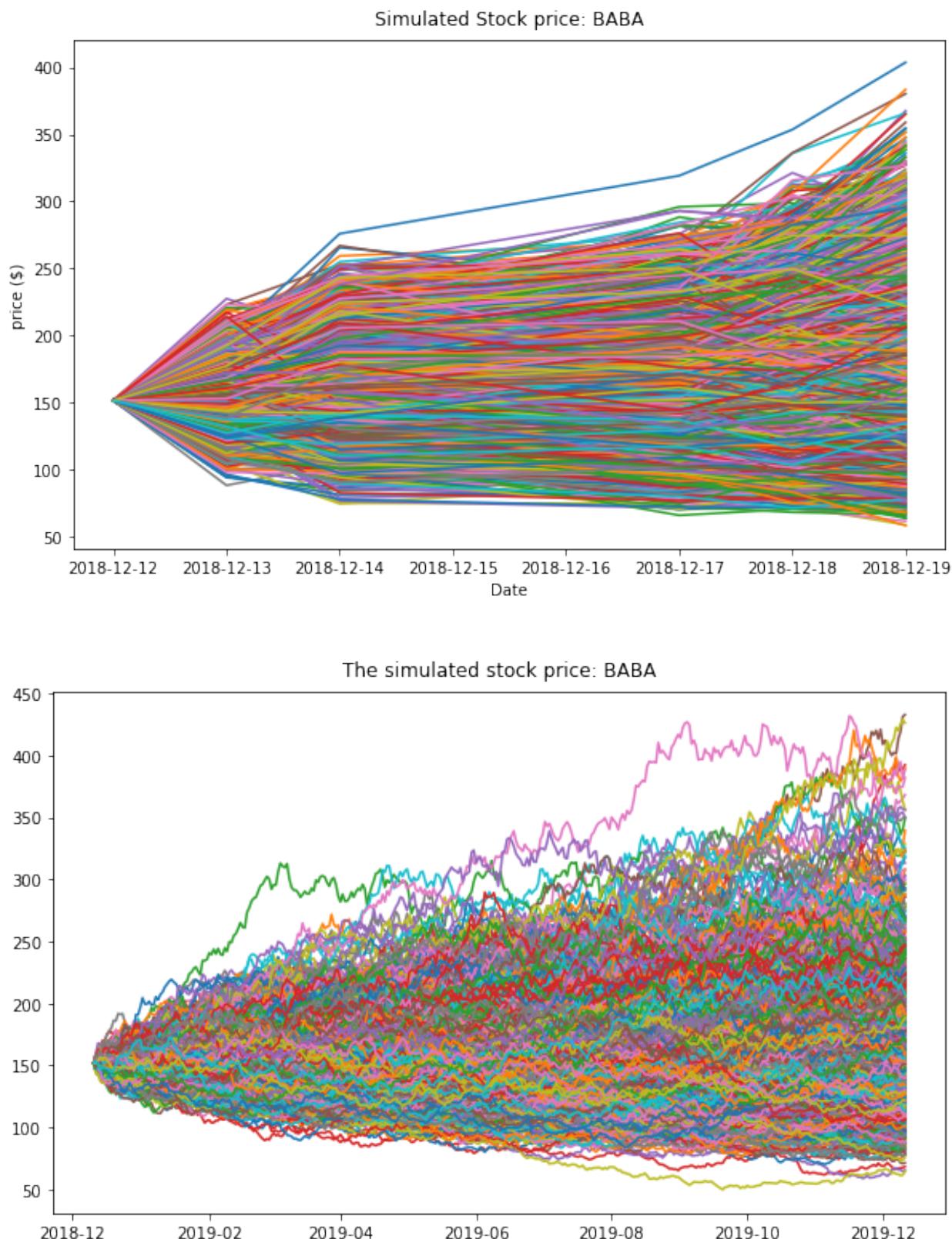


Fig. 3: Simulated Stock Price

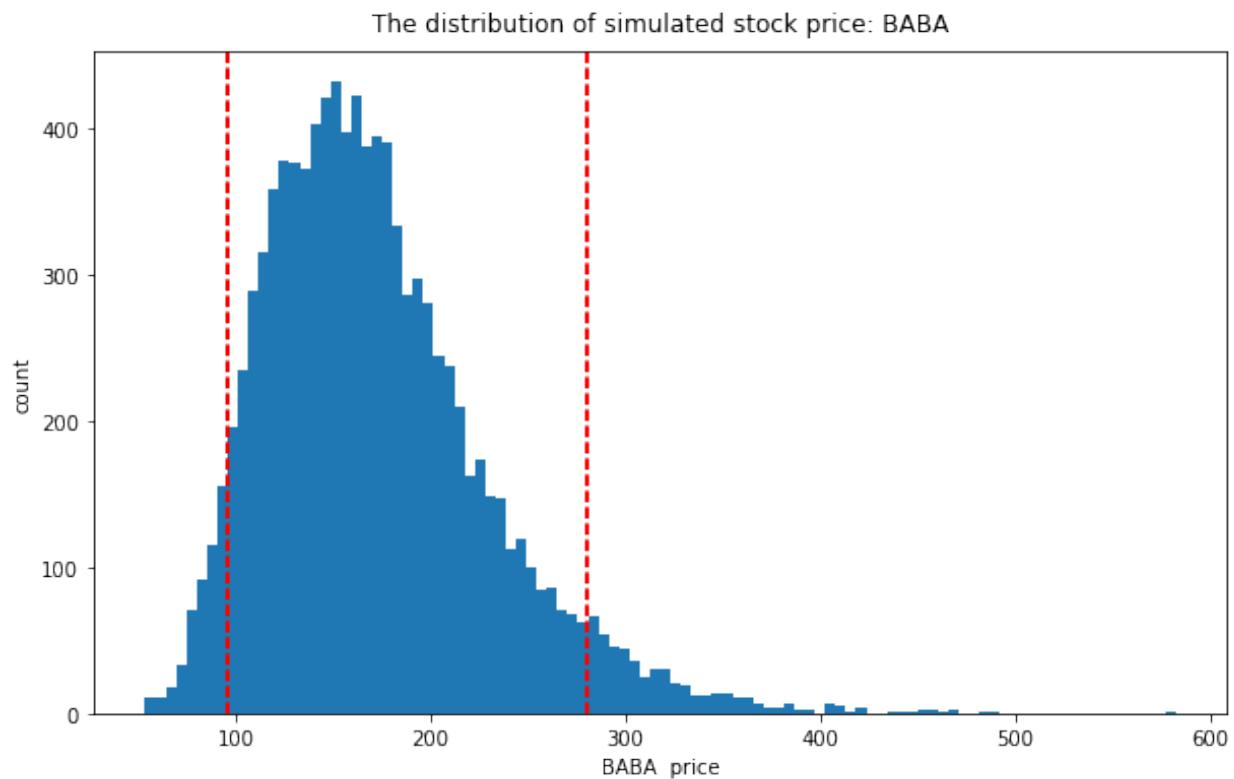


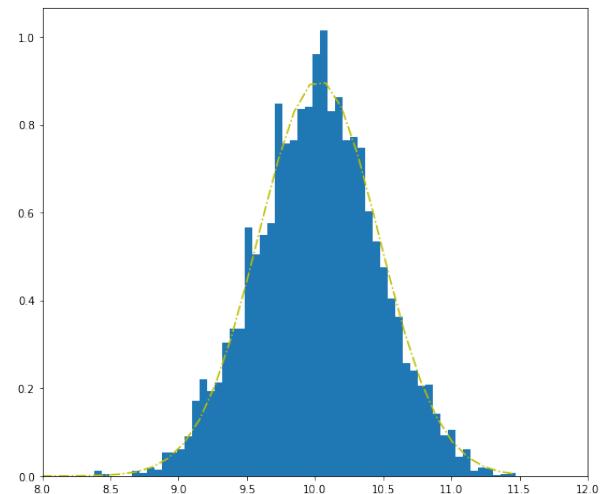
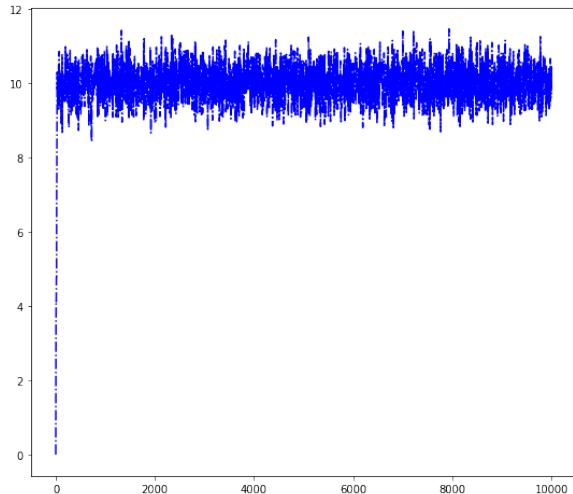
Fig. 4: Simulated Stock Price distribution

CHAPTER
SEVENTEEN

MARKOV CHAIN MONTE CARLO

Chinese proverb

A book is known in time of need.



Monte Carlo simulations are just a way of estimating a fixed parameter by repeatedly generating random numbers. More details can be found at [A Zero Math Introduction to Markov Chain Monte Carlo Methods](#).

Markov Chain Monte Carlo (MCMC) methods are used to approximate the posterior distribution of a parameter of interest by random sampling in a probabilistic space. More details can be found at [A Zero Math Introduction to Markov Chain Monte Carlo Methods](#).

The following theory and demo are from Dr. Rebecca C. Steorts's [Intro to Markov Chain Monte Carlo](#). More details can be found at Dr. Rebecca C. Steorts's STA 360/601: [Bayesian Methods and Modern Statistics](#) class at Duke.

17.1 Metropolis algorithm

The Metropolis algorithm takes three main steps:

1. Sample $\theta^* \sim J(\theta|\theta^{(s)})$

2. Compute the acceptance ratio (r)

$$r = \frac{p(\theta^*|y)}{p(\theta^{(s)}|y)} = \frac{p(y|\theta^*)p(\theta^*)}{p(y|\theta^{(s)})p(\theta^{(s)})}$$

3. Let

$$\theta^{(s+1)} = \begin{cases} \theta^* & \text{with prob } \min(r, 1) \\ \theta^{(s)} & \text{otherwise} \end{cases} \quad (17.1)$$

Note: Actually, the (17.1) in Step 3 can be replaced by sampling $u \sim \text{Uniform}(0, 1)$ and setting $\theta^{(s+1)} = \theta^*$ if $u < r$ and setting $\theta^{(s+1)} = \theta^{(s)}$ otherwise.

17.2 A Toy Example of Metropolis

The following example is going to test out the Metropolis algorithm for the conjugate Normal-Normal model with a known variance situation.

17.2.1 Conjugate Normal-Normal model

$$X_1, \dots, X_n \quad \theta \stackrel{iid}{\sim} \text{Normal}(\theta, \sigma^2) \\ \theta \sim \text{Normal}(\mu, \tau^2)$$

Recall that the posterior of θ is $\text{Normal}(\mu_n, \tau_n^2)$, where

$$\mu_n = \bar{x} \frac{n/\sigma^2}{n/\sigma^2 + 1/\tau^2} + \mu \frac{1/\tau^2}{n/\sigma^2 + 1/\tau^2}$$

and

$$\tau_n^2 = \frac{1}{n/\sigma^2 + 1/\tau^2}$$

17.2.2 Example setup

The rest of the parameters are $\sigma^2 = 1$, $\tau^2 = 10$, $\mu = 5$, $n = 5$ and

$$y = [9.37, 10.18, 9.16, 11.60, 10.33]$$

For this setup, we get that $\mu_n = 10.02745$ and $\tau_n^2 = 0.1960784$.

17.2.3 Essential mathematical derivation

In the *Metropolis algorithm*, we need to compute the acceptance ratio r , i.e.

$$\begin{aligned} r &= \frac{p(\theta^*|x)}{p(\theta^{(s)}|x)} \\ &= \frac{p(x|\theta^*)p(\theta^*)}{p(x|\theta^{(s)})p(\theta^{(s)})} \\ &= \left(\frac{\prod_i \text{dnorm}(x_i, \theta^*, \sigma)}{\prod_i \text{dnorm}(x_i, \theta^{(s)}, \sigma)} \right) \left(\frac{\text{dnorm}(\theta^*, \mu, \tau)}{\text{dnorm}(\theta^{(s)}, \mu, \tau)} \right) \end{aligned}$$

In many cases, computing the ratio r directly can be numerically unstable, however, this can be modified by taking $\log r$. i.e.

$$\begin{aligned} \log r &= \sum_i \left(\log[\text{dnorm}(x_i, \theta^*, \sigma)] - \log[\text{dnorm}(x_i, \theta^{(s)}, \sigma)] \right) \\ &\quad + \sum_i \left(\log[\text{dnorm}(\theta^*, \mu, \tau)] - \log[\text{dnorm}(\theta^{(s)}, \mu, \tau)] \right) \end{aligned}$$

Then the criteria of the acceptance becomes: if $\log u < \log r$, where u is sample from the Uniform(0, 1).

17.3 Demos

Now, We generate S iterations of the Metropolis algorithm starting at $\theta^{(0)} = 0$ and using a normal proposal distribution, where

$$\theta^{(s+1)} \sim \text{Normal}(\theta^{(s)}, 2).$$

17.3.1 R results

```

# setting values
set.seed(1)
s2<-1
t2<-10
mu<-5; n<-5

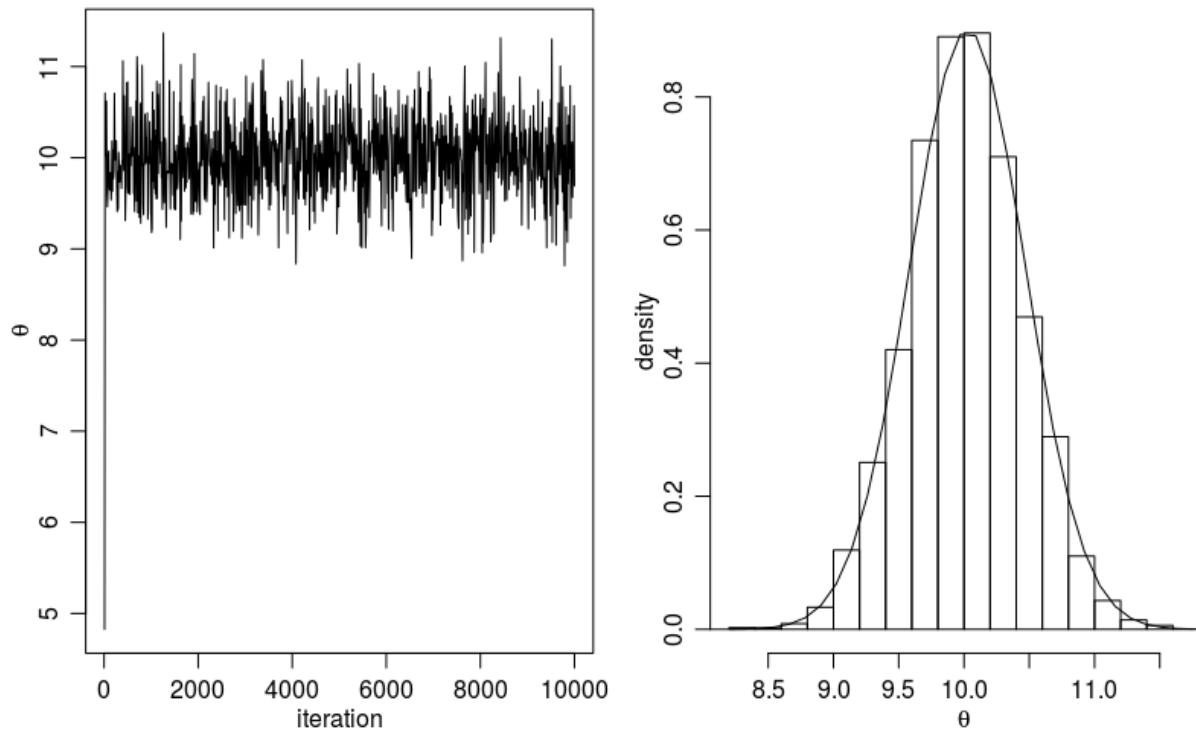
# rounding the rnorm to 2 decimal places
y<-round(rnorm(n,10,1),2)
# mean of the normal posterior
mu.n<-( mean(y)*n/s2 + mu/t2 )/( n/s2+1/t2 )
# variance of the normal posterior
t2.n<-1/(n/s2+1/t2)
# defining the data
y<-c(9.37, 10.18, 9.16, 11.60, 10.33)

#####metropolis part#####
##S = total num of simulations
theta<-0 ; delta<-2 ; S<-10000 ; THETA<-NULL ; set.seed(1)
for(s in 1:S){
  ## simulating our proposal
  #the new value of theta
  #print(theta)
  theta.star<-rnorm(1,theta,sqrt(delta))
  ##taking the log of the ratio r
  log.r<-( sum(dnorm(y,theta.star,sqrt(s2),log=TRUE))+
            dnorm(theta.star,mu,sqrt(t2),log=TRUE) )-
    ( sum(dnorm(y,theta,sqrt(s2),log=TRUE))+
      dnorm(theta,mu,sqrt(t2),log=TRUE) )
  #print(log.r)
  if(log(runif(1))<log.r) { theta<-theta.star }
  ##updating THETA
  #print(log(runif(1)))
  THETA<-c(THETA,theta)
}

##two plots: trace of theta and comparing the empirical distribution
##of simulated values to the true posterior
par(mar=c(3,3,1,1),mgp=c(1.75,.75,0))
par(mfrow=c(1,2))
# creating a sequence
skeep<-seq(10,S,by=10)
# making a trace place
plot(skeep,THETA[skeep],type="l",
      xlab="iteration",ylab=expression(theta))
# making a histogram
hist(THETA[-(1:50)],prob=TRUE,main="",
      xlab=expression(theta),ylab="density")
th<-seq(min(THETA),max(THETA),length=100)
lines(th,dnorm(th,mu.n,sqrt(t2.n)) )

```

Figure. *Histogram for the Metropolis algorithm with r* shows a trace plot for this run as well as a histogram for the Metropolis algorithm compared with a draw from the true normal density.

Fig. 1: Histogram for the Metropolis algorithm with r

17.3.2 Python results

```
# coding: utf-8

# In[1]:


import numpy as np


# In[2]:


from scipy.stats import norm


def rnorm(n,mean,sd):
    """
    same functions as rnorm in r
    r: rnorm(n, mean=0, sd=1)
    py: rvs(loc=0, scale=1, size=1, random_state=None)
    """
    return norm.rvs(loc=mean,scale=sd,size=n)

def dnorm(x,mean,sd, log=False):
    """
    same functions as dnorm in r
    """
```

(continues on next page)

(continued from previous page)

```
dnorm(x, mean=0, sd=1, log=FALSE)
pdf(x, loc=0, scale=1)
"""
if log:
    return np.log(norm.pdf(x=x, loc=mean, scale=sd) )
else:
    return norm.pdf(x=x, loc=mean, scale=sd)

def runif(n,min=0, max=1):
    """
    r: runif(n, min = 0, max = 1)
    py: random.uniform(low=0.0, high=1.0, size=None)
    """
    return np.random.uniform(min,max,size=n)

# In[3]: 

s2 = 1
t2 = 10
mu = 5
n = 5

# In[4]: 

y = rnorm(n,10,1)
y

# In[5]: 

# mean of the normal posterior
mu_n = (np.mean(y)*n/s2 + mu/float(t2))/(n/float(s2)+1/float(t2))
mu_n

# In[6]: 

# variance of the normal posterior
# t2.n<-1/(n/s2+1/t2)

t2_n = 1.0/(n/float(s2)+1.0/t2)
t2_n

# In[7]: 

# defining the data
# y<-c(9.37, 10.18, 9.16, 11.60, 10.33)
```

(continues on next page)

(continued from previous page)

```

y = [9.37, 10.18, 9.16, 11.60, 10.33]

# In[8]:
mu_n = (np.mean(y)*n/s2 + mu/float(t2))/(n/float(s2)+1/float(t2))
mu_n

# In[9]:
####metropolis part#####
##S = total num of simulations
# theta<-0 ; delta<-2 ; S<-10000 ; THETA<-NULL ; set.seed(1)

theta = 0
delta = 2

S = 10000

theta_v = []

# In[ ]:
for s in range(S):
    theta_star = norm.rvs(theta,np.sqrt(delta),1)
    logr = (sum(dnorm(y,theta_star,np.sqrt(s2),log=True)) +
            sum(dnorm(theta_star,mu,np.sqrt(t2),log=True))-
            (sum(dnorm(y,theta,np.sqrt(s2),log=True)) +
             sum(dnorm([theta],mu,np.sqrt(t2),log=True))))
    #print(logr)
    if np.log(runif(1))<logr:
        theta = theta_star
    #print(theta)
    theta_v.append(theta)

# In[ ]:
import matplotlib.mlab as mlab
import matplotlib.pyplot as plt

plt.figure(figsize=(20, 8))

plt.subplot(1, 2, 1)
plt.plot(theta_v,'b-.')

plt.subplot(1, 2, 2)
#bins = np.arange(0, S, 10)
plt.hist(theta_v, density=True,bins='auto')
x = np.linspace(min(theta_v),max(theta_v),100)

```

(continues on next page)

(continued from previous page)

```
y = norm.pdf(x,mu_n,np.sqrt(t2_n))
plt.plot(x,y,'y-.')
plt.xlim(right=12) # adjust the right leaving left unchanged
plt.xlim(left=8) # adjust the left leaving right unchanged
plt.show()

# In[ ]:
```

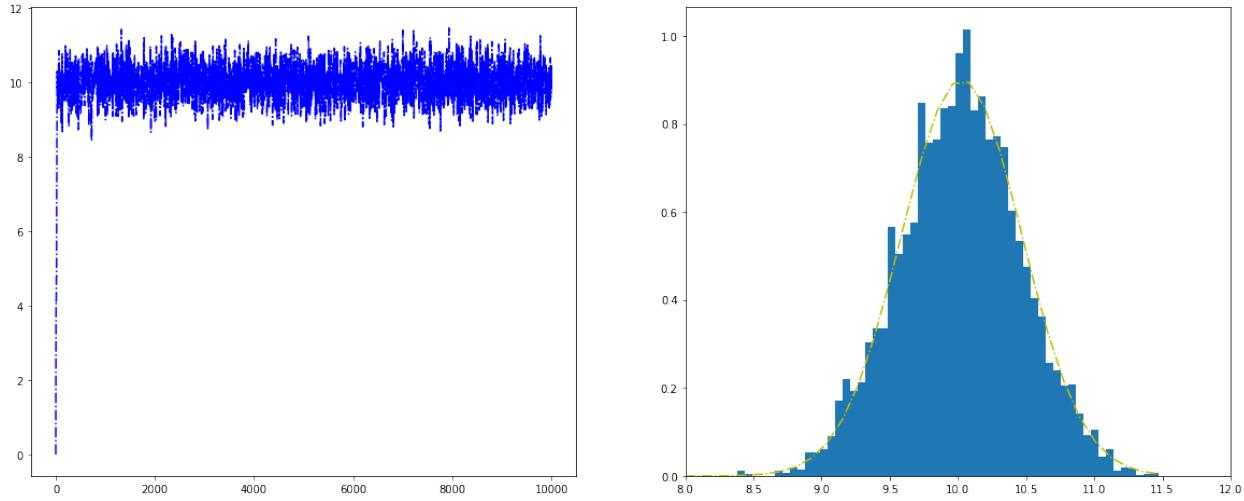


Fig. 2: Histogram for the Metropolis algorithm with python

Figure. *Histogram for the Metropolis algorithm with python* shows a trace plot for this run as well as a histogram for the Metropolis algorithm compared with a draw from the true normal density.

17.3.3 PySpark results

TODO...

Figure. *Histogram for the Metropolis algorithm with PySpark* shows a trace plot for this run as well as a histogram for the Metropolis algorithm compared with a draw from the true normal density.

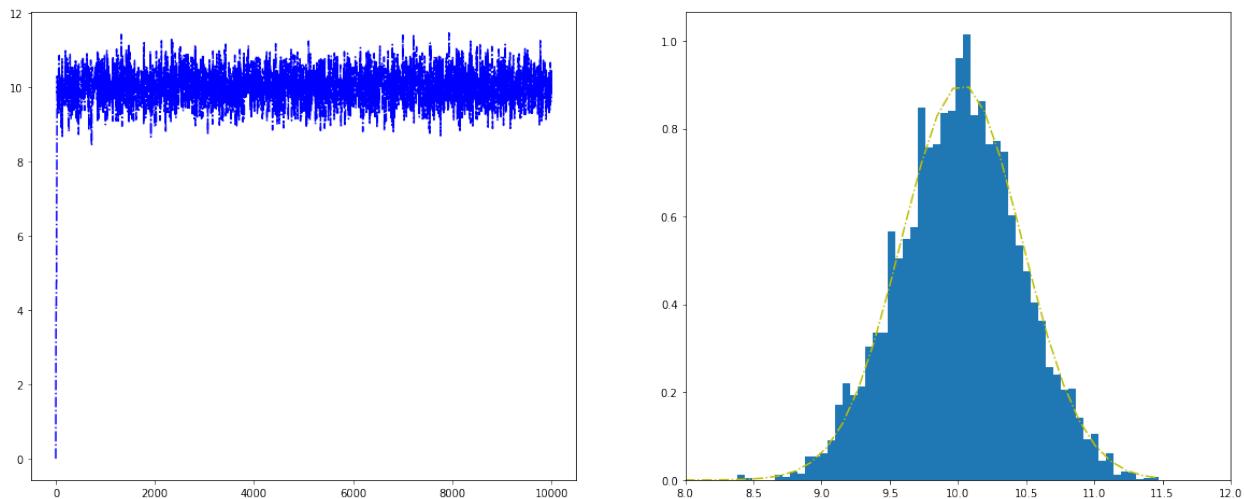


Fig. 3: Histogram for the Metropolis algorithm with PySpark

NEURAL NETWORK

Chinese proverb

Sharpening the knife longer can make it easier to hack the firewood – old Chinese proverb

18.1 Feedforward Neural Network

18.1.1 Introduction

A feedforward neural network is an artificial neural network wherein connections between the units do not form a cycle. As such, it is different from recurrent neural networks.

The feedforward neural network was the first and simplest type of artificial neural network devised. In this network, the information moves in only one direction, forward (see Fig. *MultiLayer Neural Network*), from the input nodes, through the hidden nodes (if any) and to the output nodes. There are no cycles or loops in the network.

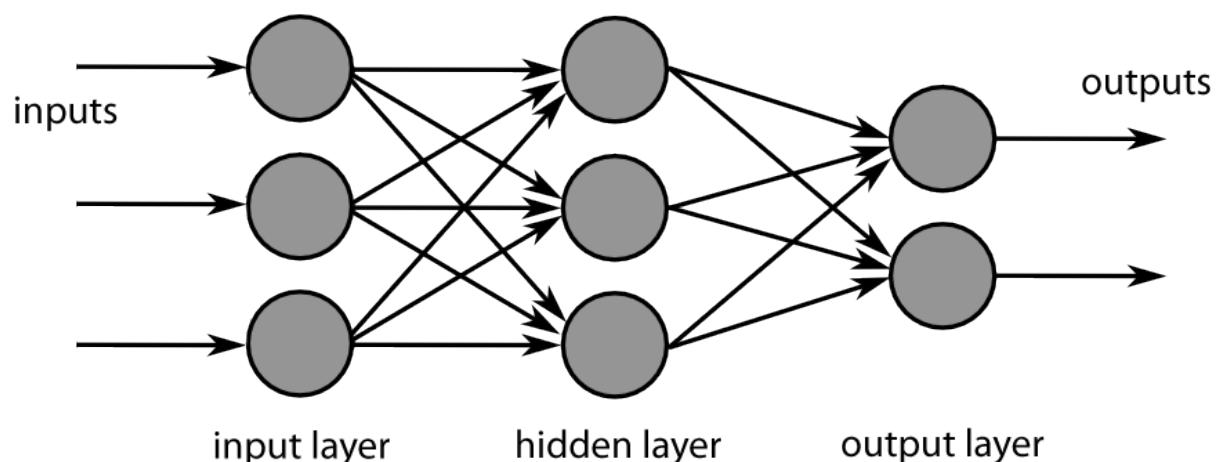


Fig. 1: MultiLayer Neural Network

18.1.2 Demo

1. Set up spark context and SparkSession

```
from pyspark.sql import SparkSession

spark = SparkSession \
    .builder \
    .appName("Python Spark Feedforward neural network example") \
    .config("spark.some.config.option", "some-value") \
    .getOrCreate()
```

2. Load dataset

```
+---+-----+-----+-----+-----+-----+-----+-----+-----+
|fixed|volatile|citric|sugar|chlorides|free|total|density| 
|pH|sulphates|alcohol|quality|
+---+-----+-----+-----+-----+-----+-----+-----+
| 7.4| 0.7| 0.0| 1.9| 0.076|11.0| 34.0| 0.9978|3.51| 0.56| 
| 9.4| 5| | | | | | | |
| 7.8| 0.88| 0.0| 2.6| 0.098|25.0| 67.0| 0.9968| 3.2| 0.68| 
| 9.8| 5| | | | | | | |
| 7.8| 0.76| 0.04| 2.3| 0.092|15.0| 54.0| 0.997|3.26| 0.65| 
| 9.8| 5| | | | | | | |
| 11.2| 0.28| 0.56| 1.9| 0.075|17.0| 60.0| 0.998|3.16| 0.58| 
| 9.8| 6| | | | | | | |
| 7.4| 0.7| 0.0| 1.9| 0.076|11.0| 34.0| 0.9978|3.51| 0.56| 
| 9.4| 5| | | | | | | |
+---+-----+-----+-----+-----+-----+-----+-----+
only showing top 5 rows
```

3. change categorical variable size

```
# Convert to float format
def string_to_float(x):
    return float(x)

#
def condition(r):
    if (0 <= r <= 4):
        label = "low"
    elif(4 < r <= 6):
        label = "medium"
    else:
        label = "high"
    return label
```

```
from pyspark.sql.functions import udf
from pyspark.sql.types import StringType, DoubleType
```

(continues on next page)

(continued from previous page)

```
string_to_float_udf = udf(string_to_float, DoubleType())
quality_udf = udf(lambda x: condition(x), StringType())
df= df.withColumn("quality", quality_udf("quality"))
```

4. Convert the data to dense vector

```
# convert the data to dense vector
def transData(data):
    return data.rdd.map(lambda r: [r[-1], Vectors.dense(r[:-1])]).\
        toDF(['label','features'])

from pyspark.sql import Row
from pyspark.ml.linalg import Vectors

data= transData(df)
data.show()
```

5. Split the data into training and test sets (40% held out for testing)

```
# Split the data into train and test
(trainingData, testData) = data.randomSplit([0.6, 0.4])
```

6. Train neural network

```
# specify layers for the neural network:
# input layer of size 11 (features), two intermediate of size 5 and 4
# and output of size 7 (classes)
layers = [11, 5, 4, 4, 3 , 7]

# create the trainer and set its parameters
FNN = MultilayerPerceptronClassifier(labelCol="indexedLabel", \
                                      featuresCol="indexedFeatures", \
                                      maxIter=100, layers=layers, \
                                      blockSize=128, seed=1234)
# Convert indexed labels back to original labels.
labelConverter = IndexToString(inputCol="prediction", outputCol=
                                "predictedLabel",
                                labels=labelIndexer.labels)
# Chain indexers and forest in a Pipeline
from pyspark.ml import Pipeline
pipeline = Pipeline(stages=[labelIndexer, featureIndexer, FNN, \
                           labelConverter])
# train the model
# Train model. This also runs the indexers.
model = pipeline.fit(trainingData)
```

7. Make predictions

```
# Make predictions.
predictions = model.transform(testData)
# Select example rows to display.
predictions.select("features","label","predictedLabel").show(5)
```

8. Evaluation

```
# Select (prediction, true label) and compute test error
evaluator = MulticlassClassificationEvaluator(
    labelCol="indexedLabel", predictionCol="prediction", metricName="accuracy"
)
accuracy = evaluator.evaluate(predictions)
print("Predictions accuracy = %g, Test Error = %g" % (accuracy, (1.0 -_
accuracy)))
```

WRAP PYSPARK PACKAGE

It's super easy to wrap your own package in Python. I packed some functions which I frequently used in my daily work. You can download and install it from [My PySpark Package](#). The hierarchical structure and the directory structure of this package are as follows.

19.1 Package Wrapper

19.1.1 Hierarchical Structure

```
|-- build
|   |-- bdist.linux-x86_64
|   |-- lib.linux-x86_64-2.7
|       |-- PySparkTools
|           |-- __init__.py
|           |-- Manipulation
|               |-- DataManipulation.py
|               |-- __init__.py
|           |-- Visualization
|               |-- __init__.py
|               |-- PyPlots.py
|-- dist
|   |-- PySparkTools-1.0-py2.7.egg
|-- __init__.py
|-- PySparkTools
|   |-- __init__.py
|   |-- Manipulation
|       |-- DataManipulation.py
|       |-- __init__.py
|   |-- Visualization
|       |-- __init__.py
|       |-- PyPlots.py
|       |-- PyPlots.pyc
|-- PySparkTools.egg-info
|   |-- dependency_links.txt
|   |-- PKG-INFO
|   |-- requires.txt
|   |-- SOURCES.txt
```

(continues on next page)

(continued from previous page)

```
|   |-- top_level.txt  
|-- README.md  
|-- requirements.txt  
|-- setup.py  
|-- test  
    |-- spark-warehouse  
    |-- test1.py  
    |-- test2.py
```

From the above hierarchical structure, you will find that you have to have `__init__.py` in each directory. I will explain the `__init__.py` file with the example below:

19.1.2 Set Up

```
from setuptools import setup, find_packages  
  
try:  
    with open("README.md") as f:  
        long_description = f.read()  
except IOError:  
    long_description = ""  
  
try:  
    with open("requirements.txt") as f:  
        requirements = [x.strip() for x in f.read().splitlines() if x.strip()]  
except IOError:  
    requirements = []  
  
setup(name='PySparkTools',  
      install_requires=requirements,  
      version='1.0',  
      description='Python Spark Tools',  
      author='Wenqiang Feng',  
      author_email='von198@gmail.com',  
      url='https://github.com/runawayhorse001/PySparkTools',  
      packages=find_packages(),  
      long_description=long_description  
)
```

19.1.3 ReadMe

```
# PySparkTools  
  
This is my PySpark Tools. If you want to clone and install it, you can use  
- clone  
``` {bash}
```

(continues on next page)

(continued from previous page)

```
git clone git@github.com:runawayhorse001/PySparkTools.git
```
- install

```{bash}
cd PySparkTools
pip install -r requirements.txt
python setup.py install
```

- test

```{bash}
cd PySparkTools/test
python test1.py
```

```

19.2 Pacakge Publishing on PyPI

19.2.1 Install twine

```
pip install twine
```

19.2.2 Build Your Package

```
python setup.py sdist bdist_wheel
```

Then you will get a new folder dist:

```
.
├── PySparkAudit-1.0.0-py2.7.egg
├── PySparkAudit-1.0.0-py2-none-any.whl
└── PySparkAudit-1.0.0.tar.gz
```

19.2.3 Upload Your Package

```
twine upload dist/*
```

During the uploading processing, you need to provide your PyPI account username and password:

```
Enter your username: runawayhorse001
Enter your password: *****
```

19.2.4 Package at PyPI

Here is my PySparkAudit package at [PyPI](<https://pypi.org/project/PySparkAudit>). You can install PySparkAudit using:

```
pip install PySparkAudit
```

CHAPTER
TWENTY

PYSPARK DATA AUDIT LIBRARY

PySparkAudit: PySpark Data Audit Library. The PDF version can be downloaded from [HERE](#). The python version **PyAudit:** Python Data Audit Library API can be found at [PyAudit](#).

20.1 Install with pip

You can install the PySparkAudit from [PyPI](<https://pypi.org/project/PySparkAudit>):

```
pip install PySparkAudit
```

20.2 Install from Repo

20.2.1 Clone the Repository

```
git clone https://github.com/runawayhorse001/PySparkAudit.git
```

20.2.2 Install

```
cd PySparkAudit
pip install -r requirements.txt
python setup.py install
```

20.3 Uninstall

```
pip uninstall statspy
```

20.4 Test

20.4.1 Run test code

```
cd PySparkAudit/test  
python test.py
```

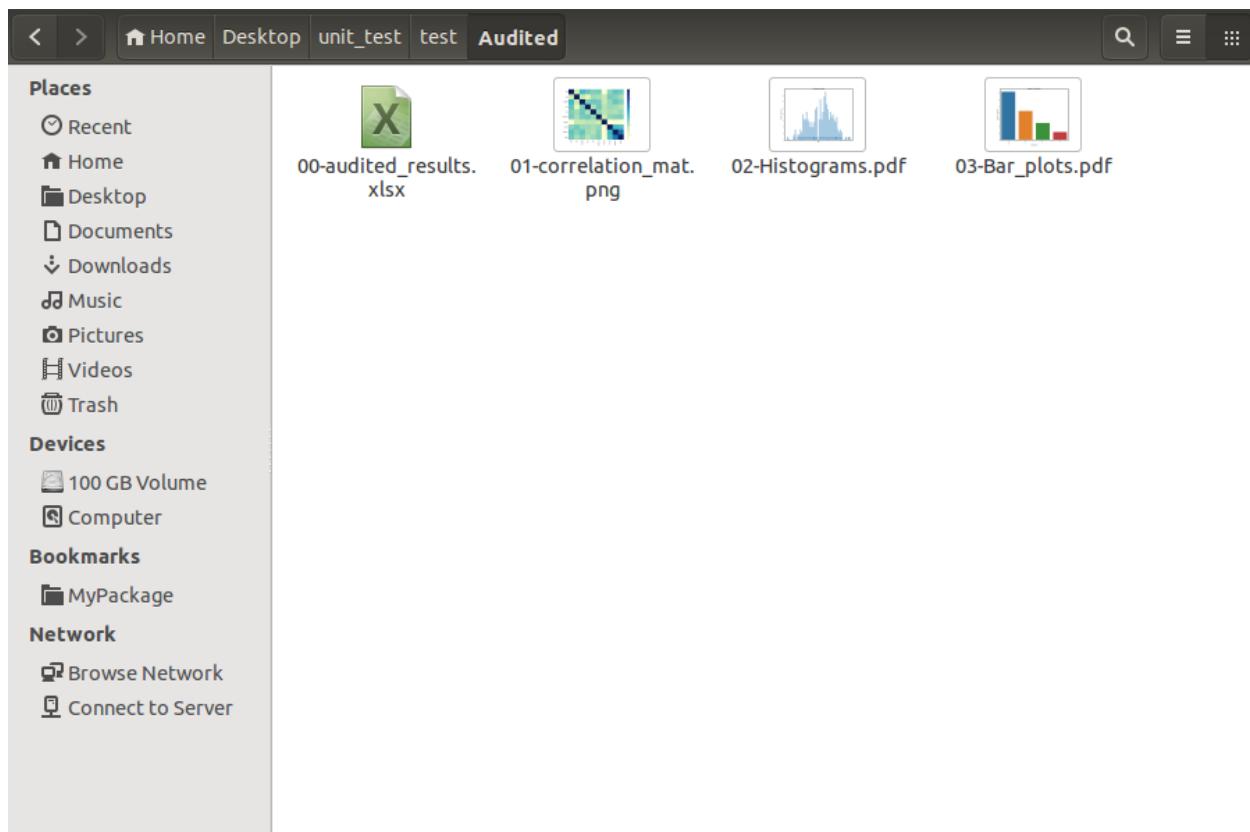
test.py

```
from pyspark.sql import SparkSession  
  
spark = SparkSession \  
    .builder \  
    .appName("Python Spark regression example") \  
    .config("spark.some.config.option", "some-value") \  
    .getOrCreate()  
  
# from PySparkAudit import dtypes_class, hist_plot, bar_plot, freq_items,  
# feature_len  
# from PySparkAudit import dataset_summary, rates, trend_plot  
  
# path = '/home/feng/Desktop'  
  
# import PySpark Audit function  
from PySparkAudit import auditing  
  
# load dataset  
data = spark.read.csv(path='Heart.csv',  
                      sep=',', encoding='UTF-8', comment=None, header=True, _  
                      inferSchema=True)  
  
# auditing in one function  
print(auditing(data, display=True))
```

20.4.2 Audited Results

The files in 00-audited_results.xlsx:

1. Dataset_summary
2. Numeric_summary
3. Category_summary



4. Correlation_matrix

5. Histograms in Histograms.pdf

6. Barplots in Bar_plots.pdf

20.5 Auditing on Big Dataset

In this section, we will demonstrate the auditing performance and audited results on the big data set. The data set is Spanish High Speed Rail tickets pricing. It is available at : <https://www.kaggle.com/thegurus/spanish-high-speed-rail-system-ticket-pricing>. This data set has 2579771 samples and 10 features.

From the following CPU time, you will see most of the time was spent on plotting the histograms. If your time and memory are limited, we will suggest you to use `sample_size` to generate the subset of the dataset to plot histograms.

For example:

The screenshot shows a spreadsheet application with a toolbar at the top containing various icons for file operations like saving, printing, and filtering. The title bar says "Calibri". The active cell is A30. The data starts from row 1 with a header "summary" and "value". Rows 2 through 17 provide specific statistics: sample_size (303), feature_size (14), single_unique_feature (0), row_w_null (0), row_w_empty (0), row_w_zero (299), row_avg_null_count (0), row_avg_empty_count (0), row_avg_zero_count (3.25083), numerical_fields (10), categorical_fields (4), date_fields (0), unsupported_fields (0), double (1), int (9), and string (4). Rows 18 through 26 are empty. The bottom navigation bar includes tabs for "Dataset_summary", "Numeric_summary", "Category_summary", and "Correlation_matrix". The status bar at the bottom shows "Sheet 1 / 4", "PageStyle_Dataset_summary", "Sum=0", and a zoom level of "100%".

| | A | B | C | D | E | F | G | H | I | J |
|----|-----------------------|--------------|---|---|---|---|---|---|---|---|
| 1 | summary | value | | | | | | | | |
| 2 | sample_size | 303 | | | | | | | | |
| 3 | feature_size | 14 | | | | | | | | |
| 4 | single_unique_feature | 0 | | | | | | | | |
| 5 | row_w_null | 0 | | | | | | | | |
| 6 | row_w_empty | 0 | | | | | | | | |
| 7 | row_w_zero | 299 | | | | | | | | |
| 8 | row_avg_null_count | 0 | | | | | | | | |
| 9 | row_avg_empty_count | 0 | | | | | | | | |
| 10 | row_avg_zero_count | 3.25083 | | | | | | | | |
| 11 | numerical_fields | 10 | | | | | | | | |
| 12 | categorical_fields | 4 | | | | | | | | |
| 13 | date_fields | 0 | | | | | | | | |
| 14 | unsupported_fields | 0 | | | | | | | | |
| 15 | double | 1 | | | | | | | | |
| 16 | int | 9 | | | | | | | | |
| 17 | string | 4 | | | | | | | | |
| 18 | | | | | | | | | | |
| 19 | | | | | | | | | | |
| 20 | | | | | | | | | | |
| 21 | | | | | | | | | | |
| 22 | | | | | | | | | | |
| 23 | | | | | | | | | | |
| 24 | | | | | | | | | | |
| 25 | | | | | | | | | | |
| 26 | | | | | | | | | | |

| | A | B | C | D | E | F | G | H | I | J | K |
|----|---------|--------|-----------|------------|----------------|-----------|-------------|-----|-----|-----|-----|
| 1 | feature | dtypes | row_count | null_count | distinct_count | mean | stddev | min | max | Q1 | Med |
| 2 | Age | int | 303 | 303 | 41 | 54.438949 | 0.03866229 | 77 | 48 | 56 | |
| 3 | Sex | int | 303 | 303 | 2 | 0.679867 | 0.4672980 | 1 | 0 | 1 | |
| 4 | RestBP | int | 303 | 303 | 50 | 131.6897 | 17.5997494 | 200 | 120 | 130 | |
| 5 | Chol | int | 303 | 303 | 152 | 246.6930 | 51.77691126 | 564 | 211 | 242 | |
| 6 | Fbs | int | 303 | 303 | 2 | 0.148514 | 0.3561970 | 1 | 0 | 0 | |
| 7 | RestECG | int | 303 | 303 | 3 | 0.990099 | 0.9949710 | 2 | 0 | 1 | |
| 8 | MaxHR | int | 303 | 303 | 91 | 149.6072 | 22.8750071 | 202 | 134 | 153 | |
| 9 | ExAng | int | 303 | 303 | 2 | 0.326732 | 0.4697940 | 1 | 0 | 0 | |
| 10 | Oldpeak | double | 303 | 303 | 40 | 1.039603 | 1.1610750.0 | 6.2 | 0 | 0.8 | |
| 11 | Slope | int | 303 | 303 | 3 | 1.600660 | 0.6162261 | 3 | 1 | 2 | |
| 12 | | | | | | | | | | | |
| 13 | | | | | | | | | | | |
| 14 | | | | | | | | | | | |
| 15 | | | | | | | | | | | |
| 16 | | | | | | | | | | | |
| 17 | | | | | | | | | | | |
| 18 | | | | | | | | | | | |
| 19 | | | | | | | | | | | |
| 20 | | | | | | | | | | | |
| 21 | | | | | | | | | | | |
| 22 | | | | | | | | | | | |
| 23 | | | | | | | | | | | |
| 24 | | | | | | | | | | | |
| 25 | | | | | | | | | | | |
| 26 | | | | | | | | | | | |

Dataset_summary Numeric_summary Category_summary Correlation_matrix

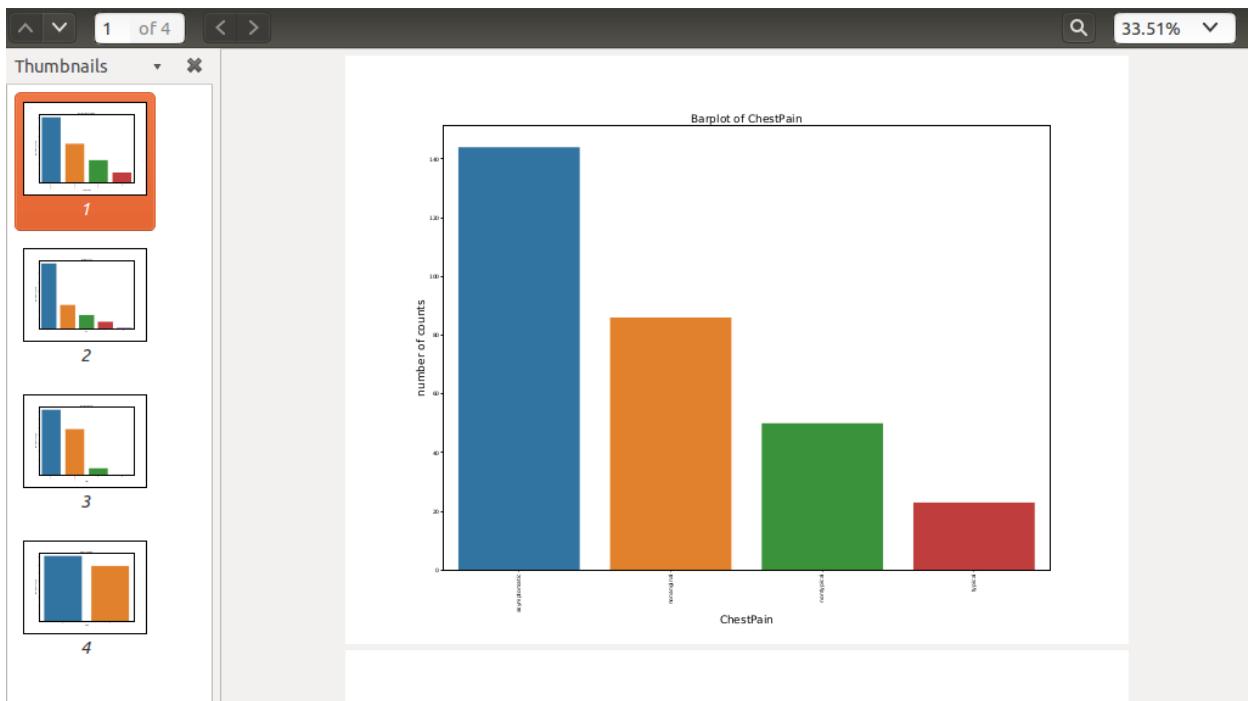
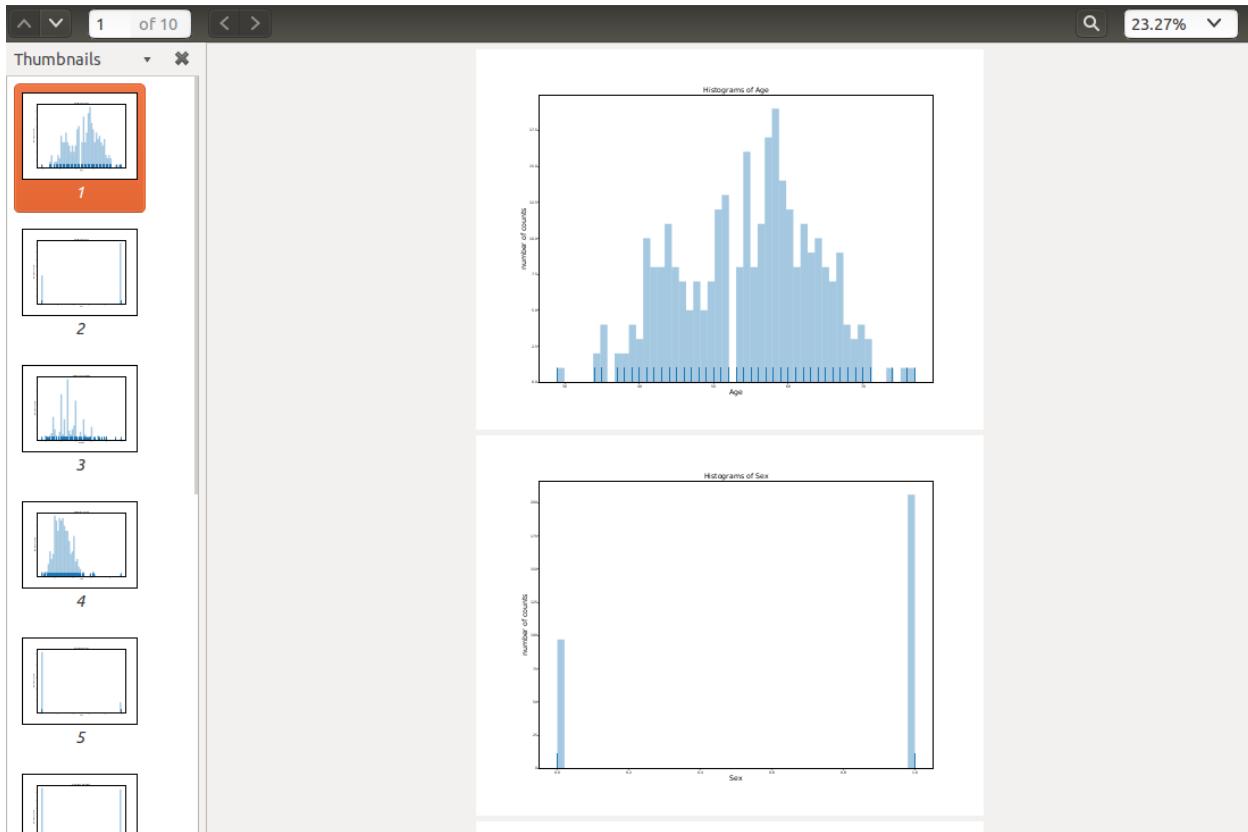
Find Find All Match Case

Sheet 2 / 4 PageStyle_Numeric_summary Sum=0 100%

The screenshot shows a spreadsheet application window with a toolbar at the top, a menu bar, and a status bar at the bottom. The main area displays a table with 26 rows and 13 columns. The columns are labeled A through K, and the rows are numbered 1 through 26. Row 1 contains the column headers: feature, dtypes, row_count, null_count, distinct_count, min_length, avg_length, max_length, ms[values], ure_vari, and rate_null. Rows 2 through 5 provide specific data points for features like ChestPain, Ca, Thal, and AHD. The status bar at the bottom shows tabs for 'Dataset_summary', 'Numeric_summary', 'Category_summary', and 'Correlation_matrix'. The bottom right corner of the status bar indicates a zoom level of 100%.

| A | B | C | D | E | F | G | H | I | J | K | |
|----|-----------|--------|-----------|------------|----------------|------------|------------|------------|---|----------|-----------|
| 1 | feature | dtypes | row_count | null_count | distinct_count | min_length | avg_length | max_length | ms[values] | ure_vari | rate_null |
| 2 | ChestPain | string | 303 | 303 | 4 | 7 | 10.7228 | 12 | [['asymptomatic' , 'no' , 'yes']] | 0.0132 | 0 |
| 3 | Ca | string | 303 | 303 | 5 | 1 | 1.0132 | 2 | [['0' , '176']] | 0.0165 | 0 |
| 4 | Thal | string | 303 | 303 | 4 | 2 | 7.45875 | 10 | [['normal' , 'fixed' , 'normal' , 'fixed']] | 0.0132 | 0 |
| 5 | AHD | string | 303 | 303 | 2 | 2 | 2.45875 | 3 | [['No' , 'Yes']] | 0.0066 | 0 |
| 6 | | | | | | | | | | | |
| 7 | | | | | | | | | | | |
| 8 | | | | | | | | | | | |
| 9 | | | | | | | | | | | |
| 10 | | | | | | | | | | | |
| 11 | | | | | | | | | | | |
| 12 | | | | | | | | | | | |
| 13 | | | | | | | | | | | |
| 14 | | | | | | | | | | | |
| 15 | | | | | | | | | | | |
| 16 | | | | | | | | | | | |
| 17 | | | | | | | | | | | |
| 18 | | | | | | | | | | | |
| 19 | | | | | | | | | | | |
| 20 | | | | | | | | | | | |
| 21 | | | | | | | | | | | |
| 22 | | | | | | | | | | | |
| 23 | | | | | | | | | | | |
| 24 | | | | | | | | | | | |
| 25 | | | | | | | | | | | |
| 26 | | | | | | | | | | | |

| | A | B | C | D | E | F | G | H | I | J | K |
|----|----------|----------|----------|----------|----------|----------|----------|----------|---------|----------|----------|
| 1 | Age | Sex | RestBP | Chol | Fbs | RestECG | MaxHR | ExAng | Oldpeak | Slope | |
| 2 | | -0.09754 | 0.28495 | 0.20895 | 0.11853 | 0.14887 | -0.39381 | 0.09166 | 0.20381 | 0.16177 | |
| 3 | -0.09754 | | 1 | -0.06446 | -0.19991 | 0.04786 | 0.02165 | -0.04866 | 0.1462 | 0.10217 | 0.03753 |
| 4 | 0.28495 | -0.06446 | | 1 | 0.13012 | 0.17534 | 0.14656 | -0.04535 | 0.06476 | 0.18917 | 0.11738 |
| 5 | 0.20895 | -0.19991 | 0.13012 | | 1 | 0.00984 | 0.17104 | -0.00343 | 0.06131 | 0.04656 | -0.00406 |
| 6 | 0.11853 | 0.04786 | 0.17534 | 0.00984 | | 1 | 0.06956 | -0.00785 | 0.02567 | 0.00575 | 0.05989 |
| 7 | 0.14887 | 0.02165 | 0.14656 | 0.17104 | 0.06956 | | 1 | -0.08339 | 0.08487 | 0.11413 | 0.13395 |
| 8 | -0.39381 | -0.04866 | -0.04535 | -0.00343 | -0.00785 | -0.08339 | | 1 | -0.3781 | -0.34309 | -0.3856 |
| 9 | 0.09166 | 0.1462 | 0.06476 | 0.06131 | 0.02567 | 0.08487 | -0.3781 | | 1 | 0.28822 | 0.25775 |
| 10 | 0.20381 | 0.10217 | 0.18917 | 0.04656 | 0.00575 | 0.11413 | -0.34309 | 0.28822 | | 1 | 0.57754 |
| 11 | 0.16177 | 0.03753 | 0.11738 | -0.00406 | 0.05989 | 0.13395 | -0.3856 | 0.25775 | 0.57754 | | 1 |
| 12 | | | | | | | | | | | |
| 13 | | | | | | | | | | | |
| 14 | | | | | | | | | | | |
| 15 | | | | | | | | | | | |
| 16 | | | | | | | | | | | |
| 17 | | | | | | | | | | | |
| 18 | | | | | | | | | | | |
| 19 | | | | | | | | | | | |
| 20 | | | | | | | | | | | |
| 21 | | | | | | | | | | | |
| 22 | | | | | | | | | | | |
| 23 | | | | | | | | | | | |
| 24 | | | | | | | | | | | |
| 25 | | | | | | | | | | | |
| 26 | | | | | | | | | | | |



```

from pyspark.sql import SparkSession

spark = SparkSession \
    .builder \
    .appName("Python Spark regression example") \
    .config("spark.some.config.option", "some-value") \
    .getOrCreate()

# from PySparkAudit import dtypes_class, hist_plot, bar_plot, freq_items,
# feature_len
# from PySparkAudit import dataset_summary, rates, trend_plot

# Audited results output path
out_path = '/home/feng/Desktop'

# import PySpark Audit function
from PySparkAudit import auditing

# load dataset
# Spanish High Speed Rail tickets pricing - Renfe (~2.58M)
# https://www.kaggle.com/theぐるす/spanish-high-speed-rail-system-ticket-
# pricing

data = spark.read.csv(path='/home/feng/Downloads/renfe.csv',
                      sep=',', encoding='UTF-8', comment=None, header=True,
                      inferSchema=True)

# auditing in one function
auditing(data, output_dir=out_path, tracking=True)

```

Result:

20.5.1 print in bash

```

=====
The audited results summary audited_results.xlsx was located at:
/home/feng/Desktop/Audited
Generate data set summary took = 60.535009145736694 s
=====
Collecting data types.... Please be patient!
Generate counts took = 0.0016515254974365234 s
=====
Collecting features' counts.... Please be patient!
Generate counts took = 6.502962350845337 s
=====
Collecting data frame description.... Please be patient!
Generate data frame description took = 1.5562639236450195 s
=====
Calculating percentiles.... Please be patient!
Generate percentiles took = 19.76785445213318 s

```

(continues on next page)

(continued from previous page)

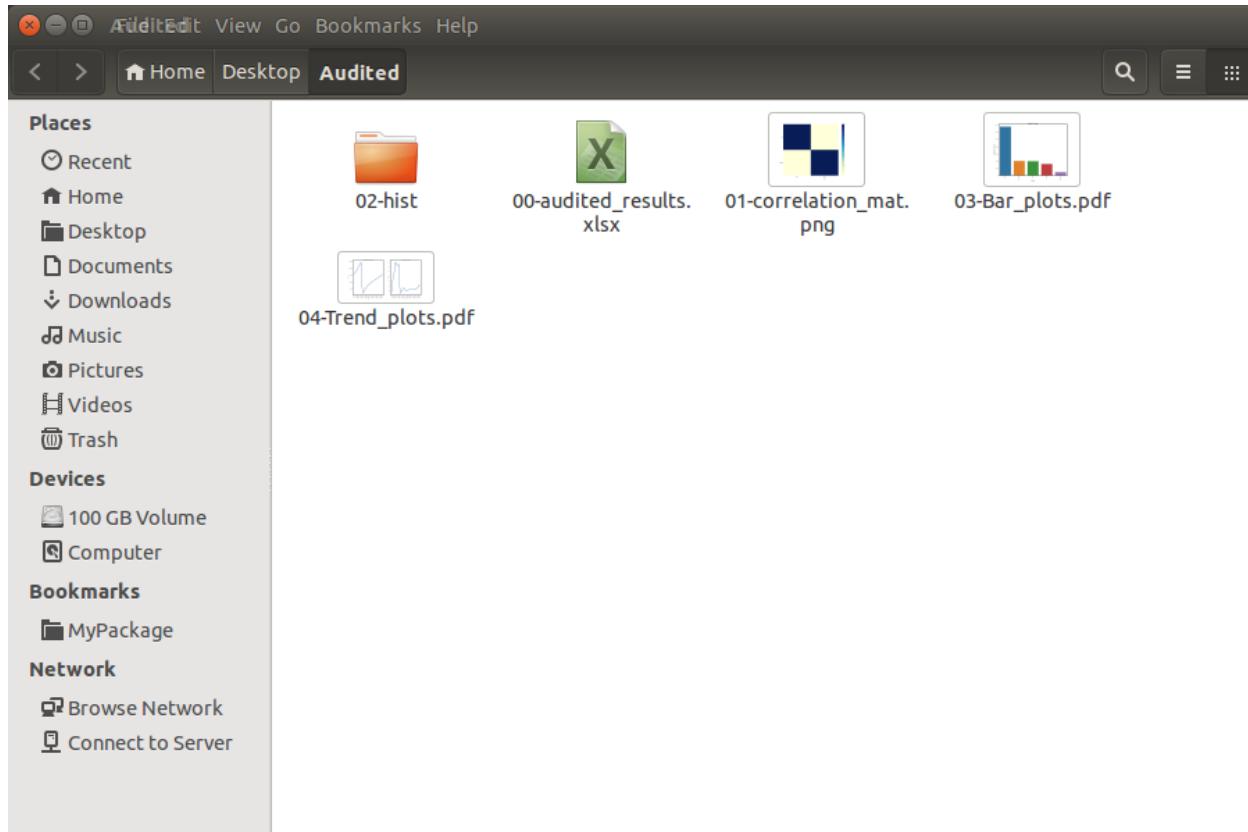
```
=====
Calculating features' length.... Please be patient!
Generate features' length took = 4.953453540802002 s
=====
Calculating top 5 frequent items.... Please be patient!
Generate rates took: 4.761325359344482 s
=====
Calculating rates.... Please be patient!
Generate rates took: 17.201056718826294 s
Auditing numerical data took = 54.77840781211853 s
=====
Collecting data types.... Please be patient!
Generate counts took = 0.001623392105102539 s
=====
Collecting features' counts.... Please be patient!
Generate counts took = 12.59226107597351 s
=====
Calculating features' length.... Please be patient!
Generate features' length took = 5.332952976226807 s
=====
Calculating top 5 frequent items.... Please be patient!
Generate rates took: 6.832213878631592 s
=====
Calculating rates.... Please be patient!
Generate rates took: 23.704302072525024 s
Auditing categorical data took = 48.484763622283936 s
=====
The correlation matrix plot Corr.png was located at:
/home/feng/Desktop/Audited
Calculating correlation matrix... Please be patient!
Generate correlation matrix took = 19.61273431777954 s
=====
The Histograms plots *.png were located at:
/home/feng/Desktop/Audited/02-hist
Plotting histograms of _c0.... Please be patient!
Plotting histograms of price.... Please be patient!
Histograms plots are DONE!!!
Generate histograms plots took = 160.3421311378479 s
=====
The Bar plot Bar_plots.pdf was located at:
/home/feng/Desktop/Audited
Plotting barplot of origin.... Please be patient!
Plotting barplot of destination.... Please be patient!
Plotting barplot of train_type.... Please be patient!
Plotting barplot of train_class.... Please be patient!
Plotting barplot of fare.... Please be patient!
Plotting barplot of insert_date.... Please be patient!
Plotting barplot of start_date.... Please be patient!
Plotting barplot of end_date.... Please be patient!
Bar plots are DONE!!!
Generate bar plots took = 24.17994236946106 s
=====
```

(continues on next page)

(continued from previous page)

```
The Trend plot Trend_plots.pdf was located at:  
/home/feng/Desktop/Audited  
Plotting trend plot of _c0.... Please be patient!  
Plotting trend plot of price.... Please be patient!  
Trend plots are DONE!!!  
Generate trend plots took = 11.697550296783447 s  
Generate all the figures took = 196.25823402404785 s  
Generate all audited results took = 379.73954820632935 s  
=====  
The auditing processes are DONE!!!
```

20.5.2 Audited results folder



ZEPPELIN TO JUPYTER NOTEBOOK

The Zeppelin users may have same problem with me that the Zeppelin .json notebook is hard to open and read. **ze2nb**: A piece of code to convert Zeppelin .json notebook to .ipynb Jupyter notebook, .py and .html file. This library is based on Ryan Blue's Jupyter/Zeppelin conversion: [[jupyter-zeppelin](#)]. The API book can be found at [ze2nb API](#) or [[zeppelin2nb](#)]. **You may download and distribute it. Please be aware, however, that the note contains typos as well as inaccurate or incorrect description.**

21.1 How to Install

21.1.1 Install with pip

You can install the `ze2nb` from [PyPI](<https://pypi.org/project/ze2nb>):

```
pip install ze2nb
```

21.1.2 Install from Repo

1. Clone the Repository

```
git clone https://github.com/runawayhorse001/ze2nb.git
```

2. Install

```
cd zeppelin2nb
pip install -r requirements.txt
python setup.py install
```

21.1.3 Uninstall

```
pip uninstall ze2nb
```

21.2 Converting Demos

The following demos are designed to show how to use zepplin2nb to convert the .json to .ipynb , .py and .html.

21.2.1 Converting in one function

For example:

```
# import python library
import os, sys

# import zeppelin2nb module
from ze2nb import ze2nb


# scenario 1
# file and output at the current directory
# output path, the default output path will be the current directory
ze2nb('H2o_Sparking.json')

# scenario 2
output = os.path.abspath(os.path.join(sys.path[0])) +'/output'
ze2nb('H2o_Sparking.json', out_path=output, to_html=True, to_py=True)

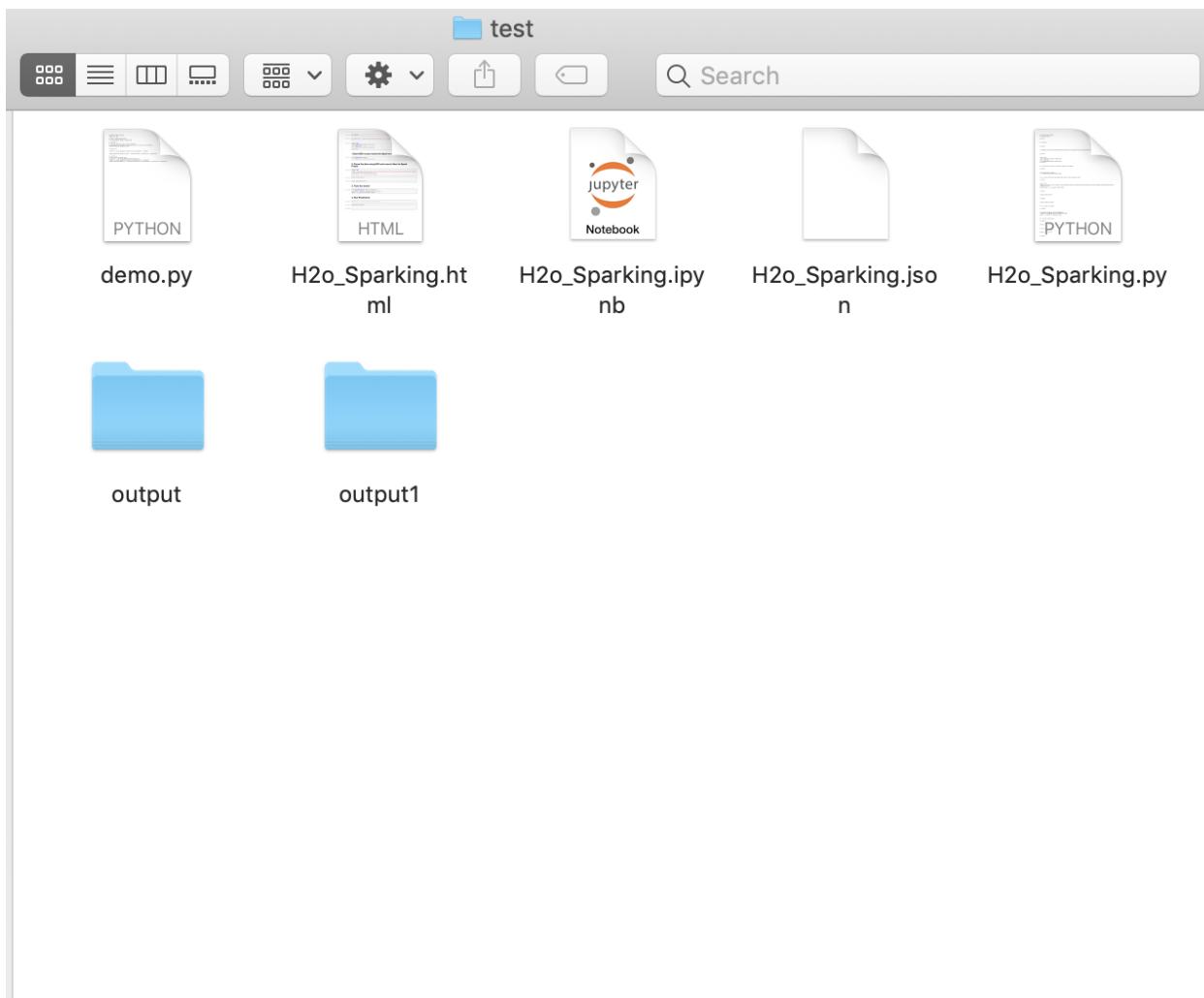
# scenario 3
# with load and output path
load_path = '/Users/dt216661/Documents/MyJson/'
output = os.path.abspath(os.path.join(sys.path[0])) +'/output1'
ze2nb('H2o_GBM.json', load_path=load_path, out_path=output, to_html=True, to_
→py=True)
```

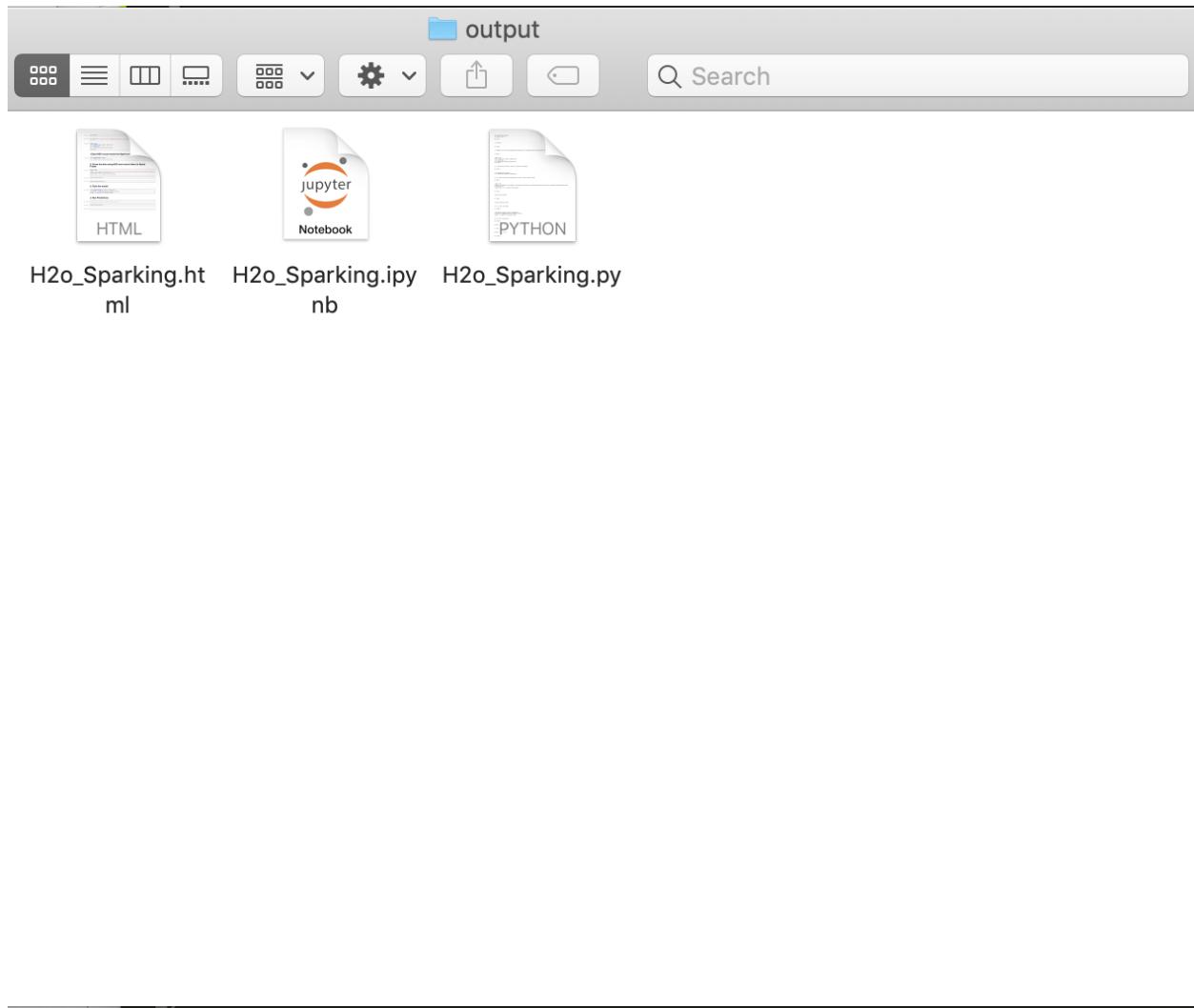
21.2.2 Converted results

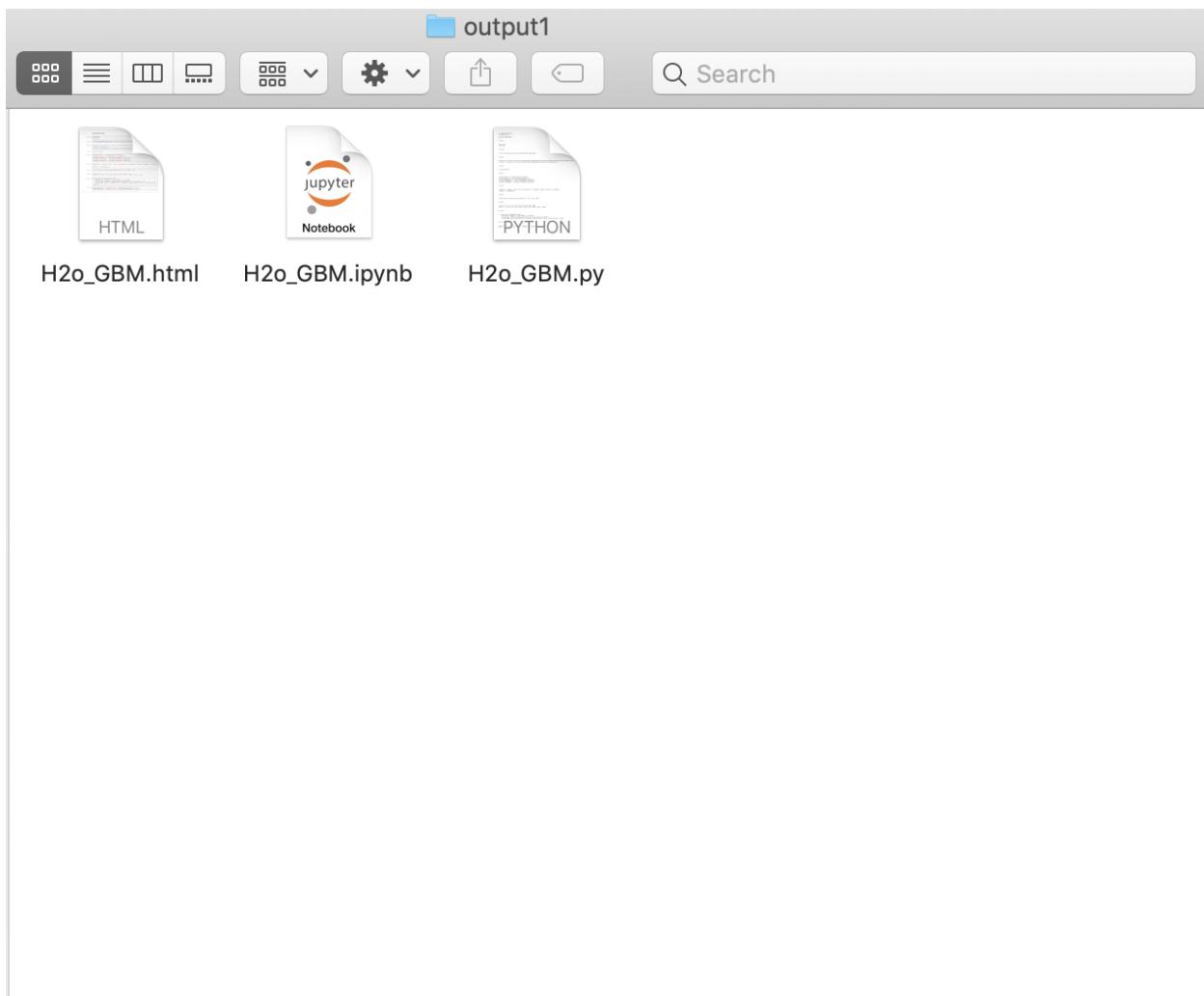
Result:

Results in output:

Results in output1:







CHAPTER

TWENTYTWO

MY CHEAT SHEET

You can download the PDF version: [PySpark Cheat Sheet](#) and [pdDataFrame vs rddDataFrame](#).

Cheat Sheet for PySpark

Wenqiang Feng

E-mail: von198@gmail.com, Web: <http://web.utk.edu/~wfeng1>; <https://runawayhorse001.github.io/LearningApacheSpark>

Spark Configuration

```
from pyspark.sql import SparkSession
spark = SparkSession.builder
    .appName("Python Spark regression example")
    .config("config.option", "value").getOrCreate()
```

Loading Data

- From RDDs
- # Using parallelize()
df = spark.sparkContext.parallelize([('1', 'Joe', '70000', '1'),
('2', 'Henry', '80000', None)])
 .toDF(['Id', 'Name', 'Salary', 'DepartmentId'])
- # Using createDataFrame()
df = spark.createDataFrame([('1', 'Joe', '70000', '1'),
('2', 'Henry', '80000', None),
('3', 'Tom', '100000', '1'),
('4', 'Herry', '80000', None)])
 .toDF(['Id', 'Name', 'Salary', 'DepartmentId'])

From Data Sources

- > From .csv
`ds = spark.read.csv(path='Advertising.csv',
sep=',', encoding='UTF-8', comment=None,
header=True,inferSchema=True)`

| | TV | Radio | Newspaper |
|--------|--------------------------------|--------------------|--------------------|
| count | 200 | 200 | 200 |
| mean | 147.0425123264000000000024 | 30.553999999999995 | 1.7786208322222222 |
| stddev | 8542363140.14.8680916161616161 | 21.778620832222222 | 0.31 |
| min | 0.71 | 0.01 | 0.01 |
| max | 296.41 | 49.61 | 114.01 |
- > From .json
`df = spark.read.json('/home/feng/Desktop/data.json')`

| | id | location | timestamp |
|---|-------------------------|------------------------|---------------------|
| 1 | TVRadio Newspaper Sales | (771,DE,8086,52,...) | 2019-02-23 22:36:52 |
| 2 | TVRadio Newspaper Sales | (598,5,BG,3985,42,...) | 2019-02-23 22:36:52 |
- > From Database
`user = 'username'; pw = 'password'
table = 'table_name';
url = 'jdbc:postgresql://##.##.##.##:5432/dataset?user=%s&password=%s'
#> user='password'+pw
#> driver='org.postgresql.Driver','password':pw,'user':user
df = spark.read.jdbc(url=url,table=table_name,properties={})`

| | TVRadio Newspaper Sales | location | timestamp |
|---|-------------------------|------------------------|---------------------|
| 1 | TVRadio Newspaper Sales | (771,DE,8086,52,...) | 2019-02-23 22:36:52 |
| 2 | TVRadio Newspaper Sales | (598,5,BG,3985,42,...) | 2019-02-23 22:36:52 |
- > From HDFS
`from pyspark.conf import SparkConf
from pyspark.context import SparkContext
from pyspark.sql import HiveContext
sc = SparkContext('local','example')
hc = HiveContext(sc)
rri = sc.textFile("hdfs://##/user/data/file_name")`

| | TVRadio Newspaper Sales | location | timestamp |
|---|-------------------------|------------------------|---------------------|
| 1 | TVRadio Newspaper Sales | (771,DE,8086,52,...) | 2019-02-23 22:36:52 |
| 2 | TVRadio Newspaper Sales | (598,5,BG,3985,42,...) | 2019-02-23 22:36:52 |

Auditing Data

Checking schema

```
df.printSchema()
root
 |-- c0: integer (nullable = true)
 |-- c1: double (nullable = true)
 |-- Radio: double (nullable = true)
 |-- Newspaper: double (nullable = true)
 |-- Sales: double (nullable = true)
```

Checking missing value

```
from pyspark.sql.functions import count
def my_count(df):
    df.agg(*[count(c).alias(c) for c in df.in_columns]).show()
my_count(df_raw)
```

| | InvoiceNo StockCode Quantity InvoiceDate UnitPrice CustomerID Country |
|---|---|
| 1 | 5419091 5419091 5419091 5419091 4068291 5419091 |

Checking statistical results

```
# Function from my pyspark
df_raw.describe().show()
```

| | TV | Radio | Newspaper |
|---------|--------------------------------|--------------------|--------------------|
| summary | | | |
| count | 200 | 200 | 200 |
| mean | 147.0425123264000000000024 | 30.553999999999995 | 1.7786208322222222 |
| stddev | 8542363140.14.8680916161616161 | 21.778620832222222 | 0.31 |
| min | 0.71 | 0.01 | 0.01 |
| max | 296.41 | 49.61 | 114.01 |

Manipulating Data (More details on next page)

Fixing missing value

| Function | Description |
|--------------|--------------------------------------|
| df.na.fill() | #Replace null values |
| df.na.drop() | #Dropping any rows with null values. |

Joining data

| Description | Function |
|-------------|--|
| #Data join | left.join(right,key, how='*') == left,right.inner,full |

Wrangling with UDF

```
from pyspark.sql import functions as F
from pyspark.sql.types import DoubleType
# user-defined function
def complexFun(x):
    return results
Fn = F.udf(lambda x: complexFun(x), DoubleType())
df.withColumn('2col', Fn(df.col))
```

Reducing features

```
df.select(featureNameList)
```

Modeling Pipeline

Deal with categorical feature and label data

```
# Deal with categorical feature data
from pyspark.ml.feature import VectorIndexer
featureIndexer = VectorIndexer(inputCol="features",
                                outputCol="indexedFeatures",
                                maxCategories=4).fit(data)
featureIndexer.transform(data).show(2, True)
```

| | features label | indexedFeatures |
|---|-----------------------|----------------------------|
| 1 | [29,[1,11,14,16,...]] | [sol(29,[1,11,14,16,...])] |

Deal with categorical label data

```
# Deal with categorical label data
labelIndexer=StringIndexer(inputCol="label",
                            outputCol="indexedLabel").fit(data)
labelIndexer.transform(data).show(2, True)
```

| | features label | indexedLabel |
|---|-----------------------|--------------|
| 1 | [29,[1,11,14,16,...]] | [sol(1,0.0)] |

Splitting the data to training and test data sets

```
(trainingData, testData) = data.randomSplit([0.6, 0.4])
```

Importing the model

```
from pyspark.ml.classification import LogisticRegression
lr = LogisticRegression(featuresCol="indexedFeatures",
                        labelCol="indexedLabel")
```

Converting indexed labels back to original labels

```
from pyspark.ml.feature import IndexToString
labelConverter = IndexToString(inputCol="prediction",
                                outputCol="predictedLabel",
                                labels=labelIndexer.labels)
```

Wrapping Pipeline

```
pipeline = Pipeline(stages=[labelIndexer, featureIndexer,
                           lr,labelConverter])
```

Training model and making predictions

```
model = pipeline.fit(trainingData)
predictions = model.transform(testData)
predictions.select("features","label","predictedLabel").show(2)
```

| | features label predictedLabel |
|---|-------------------------------------|
| 1 | [sol(29,[1,11,13,16,...]) no no] |

Evaluating

```
from pyspark.ml.evaluation import *
evaluator = MulticlassClassificationEvaluator(
    predictionCol="predictedLabel",
    labelCol="label",
    metricName="accuracy")
accu = evaluator.evaluate(predictions)
print("Test Error: %g, AUC: %g"%(1-accu,Summary.areaUnderROC))
Test Error: 0.098664269877
```

All Rights Reserved by Dr.Wenqiang Feng. Powered by LaTeX. Updated:02-26-2019 von198@gmail.com

315

| | | |
|--|--|--|
| <p>Data Wrangling: Combining DataFrame</p> <p>Mutating Joins</p> <pre> Result Function X1 X2 X3 x 1 2 4 b 2 3 5 c 2 3 5 </pre> <pre> #Join matching rows from B to A dfA.join(dfB, "X1", "left") .orderBy("X1", ascending=True).show() </pre>
<p>X1 X2 X3 #Join matching rows from A to B <code>dfA.join(dfB, "X1", "right")</code> <code>.orderBy("X1", ascending=True).show()</code></p>
<p>X1 X2 X3 #Retain only rows in both sets <code>dfA.join(dfB, "X1", "inner")</code> <code>.orderBy("X1", ascending=True).show()</code></p>
<p>X1 X2 X3 #Retain all values from A <code>dfA.join(dfB, "X1", "full")</code> <code>.orderBy("X1", ascending=True).show()</code></p> <p>Filtering Joins</p> <pre> Result Function X1 X2 a 1 2 b 2 3 </pre> <pre> #All rows in A that have a match in B dfA.join(dfB, "X1", "left_semi") .orderBy("X1", ascending=True).show() </pre>
<p>#All rows in A, don't have a match in B <code>dfA.join(dfB, "X1", "left_anti")</code> <code>.orderBy("X1", ascending=True).show()</code></p> <p>DataFrame Operations</p> <pre> Result Function Y Z X1 X2 X1 X2 a 1 2 b 2 3 b 2 3 c 3 4 c 3 4 d 4 5 </pre> <pre> #Show that appear in both Y and Z dfY.intersect(dfZ).show() </pre>
<p>#Show that appear in either or both Y and Z <code>dfY.union(dfZ).dropDuplicates()</code> <code>.orderBy("X1", ascending=True).show()</code></p>
<p>#Show that appear in Y but not Z <code>dfY.subtract(dfZ).show()</code></p> <p>Binding</p> <pre> Result Function X1 X2 X1 X2 a 1 2 b 2 3 b 2 3 c 3 4 c 3 4 d 4 5 </pre> <pre> #Append Z to Y as new rows dfY.zip(dfZ).show() </pre>
<p>#Append Z to Y as new columns <code>dfY.zipDataFrames(dfZ)</code> <code>.show()</code></p> | <p>Data Wrangling: Reshaping Data</p> <p>Change</p> <pre> Function df.select("key", df.value[0], df.value[1]).show() </pre>
<pre> Function df.select("key", F.explode(F.split("value", ",")).alias("value"), "val").select("key", expr("value[0]").alias("val")).show() </pre>
<pre> Function kva = explode(array(for c in cols col(c).alias("key"), col(c).alias("val")))).alias("key") return df.select(by + [kva.key, "vva.val"]) </pre> <p>Pivot</p> <pre> Function df.groupBy(["key"]).pivot("col1").sum("col1").show() </pre> <p>Subset Observations (Rows)</p> <pre> Function df.na.drop() </pre> <p>Subset Variables (Columns)</p> <pre> Function df.select() </pre> <p>Make New Variables</p> <pre> Function df.withColumn("new", 1 / df.col) .withColumn("new", F.log(df.col)) .withColumn("id", ps.monotonically_increasing_id()) .withColumn("new", Fn("col")) #Fn: Udf() .withColumn("new", F.when((df.c1>2)&(df.c2<2), 1) .otherwise(3)) </pre> | <p>Data Wrangling: Reshaping Data</p> <p>Summarise Data</p> <pre> Function df.describe() </pre> <p>Correlation</p> <pre> Function Correlation.corr(df) </pre> <p>Count</p> <pre> Function df.count() </pre> <p>Description Demo</p> <pre> Function #Sum df.agg(F.max(df.C).head(1)) #Similar for: F.min,max,avg,stddev </pre> <p>Group Data</p> <pre> Function df.groupby("A").agg(F.min("B").alias("min_b"), F.max("B").alias("max_b"), F.avg("C").alias("avg_c")).show() </pre>
<pre> Function def quant_pd(val_list): quant = np.round(np.percentile(val_list, [20, 50, 75]), 2) return list(map(float, quant)) </pre>
<pre> Function Fn = F.uff(quant_pd.ArrayType(FloatType())) df.groupby("A").agg(F.min("B").alias("min_b"), F.max("B").alias("max_b"), Fn(F.collect_list(col("C"))).alias("list_c")) </pre> <p>Windows</p> <pre> Function from pyspark.sql import Window #Define windows for difference w = Window.partitionBy(df.B) D = df.C.F.max(df.C).over(w) df.withColumn("D", D).show() df = df.withColumn("id", F.monotonically_increasing_id()) #Define windows for row_num w = Window.orderBy("id") d = df.withColumn("id", F.rank().over(w)) A B C D a 1 2 4 5 b 2 3 6 7 c 3 4 8 9 d 6 4 </pre>
<pre> Function #Define windows for rank w = Window.partitionBy("B") D = df.C.orderBy(df.C.desc()) df.withColumn("D", rank().over(w)).show() A B C D a 1 2 4 b 2 3 6 c 3 4 8 d 6 4 </pre> <p>Rename Variables</p> <pre> Function df.withColumnRenamed() #Renaming an existing column </pre> |
|--|--|--|

All Rights Reserved by Dr.Wenqiang Feng. Powered by iATP. Updated:02-26-2019 von1989@gmail.com

pd.DataFrame vs rdd.DataFrame

Wenqiang Feng

E-mail: von198@gmail.com, Web: <http://web.utk.edu/~wfeng1>; <https://runawayhorse001.github.io/LearningApacheSpark>

Creating DataFrame

From List

```
pd.DataFrame(my_list,columns= col_name)
spark.createDataFrame(my_list, col_name).show()
```

From Dictionary

```
pd.DataFrame(d)
spark.createDataFrame(np.array(list(d.values()))).T.tolist(),
list(d.keys())).show()
```

From Data Sources

From Database

```
conn = psycopg2.connect(host=host, database=db_name,
user=user, password=password)
cur = conn.cursor()
sql = """select * from table_name
        """.format(table_name=table_name)
dp = pd.read_sql(sql, conn)
url="jdbc:postgresql://"+host+":5432/"+db_name+"?user='"+user
+'&password='+password
ps.driver='org.postgresql.Driver';password':pu,'user':user
dsspark.read.jdbc(url,table_name, properties=p)
D. From csv
dp = pd.read_csv('Advertising.csv')
ds = spark.read.csv(path='Advertising.csv',
header=True,inferSchema=True)
D. From json
dp = pd.read_json('data/data.json')
ds = spark.read.json('data/data.json')
```

Basic Manipulation

| Data Types | Count |
|------------|----------------|
| dp.dtypes | dp.count() [1] |
| ds.dtypes | ds.count() |

| Column Names | Select Columns |
|--------------|---|
| dp.columns | dp['name_list'].head() ds['name_list'].show() |
| ds.columns | |

| Rename Columns | Drop Columns |
|---|--|
| dp.columns = name_list ds.DDF(name_list).show() | dp.drop(name_list, axis=1) ds.drop(name_list).show() |

| Distinct Rows | Cross Table |
|---|---|
| dp.drop_duplicates() ds.drop_duplicates() | pd.crosstab(dp.col1, dp.col2) ds.crosstab('col1', 'col2') |

Replace Values

```
dp.A.replace({'male': 'female'}, {1, 0}, inplace=True)
ds_na.replace({'male': 'female'}, {1, '0'}).show()
```

Basic Manipulation

Rename one or more columns

```
mapping = {'key1': 'val1', 'key2': 'val2'}
dp.rename(columns=mapping).head(4)
new_names = [mapping.get(col,col) for col in ds.columns]
ds.toDF(*new_names).show(4)
```

Replace one or more data types

```
a = '0.012' # str, float, str, str - string for pyspark
dp = pd.astype(a)
ds = ds.select(*[list(set(ds.columns)-set(d.keys())),
*(col[c[0]].astype(c[1]).alias(c[0]) for c in d.items())])
```

Random Split

```
from sklearn.model_selection import train_test_split
a, b = train_test_split(dp, test_size=0.8)
a, b = ds.randomSplit([0.2, 0.8])
```

Unixtime to Date

```
dp['date'] = dp.datetime(dp['ts'], unit='s').dt.tz_localize('UTC')
spark.conf.set("spark.sql.session.timeZone", "UTC")
ds.withColumn('date', F.from_unixtime('ts'))
```

Make New Variables

```
dp['tv_norm'] = dp.TV.sum(dp.TV)
ds.withColumn('tv_norm', ds.TV.ds.groupby()
.agg(F.sum("TV")).collect()[0][0]).show(4)
dp['cond'] = dp.apply(lambda c: 1 if ((c.TV > 100) & (c.Radio < 40))
else 2 if c.Sales > 10
else 3, axis=1)
ds.withColumn('cond', F.when((dp.TV > 100) & (dp.Radio < 40)), 1)
.when(dp.Sales > 10, 2)
.otherwise(3)).show(4)
dp['log_tv'] = np.log(dp.TV)
ds.withColumn('log_tv', F.log(ds.TV)).show(4)
dp['tv*10'] = dp.TV.apply(lambda x: x*10)
ds.withColumn('tv*10', ds.TV*10).show(4)
```

Summarise Data

```
dp.describe()
ds.describe().show()
dp.corr(method='pearson')
mat=statistics.corr(ds.rdd.map(lambda r: r[0]),method='pearson')
pd.DataFrame(mat,columns=ds.columns,index=ds.columns)

dp.C.max() #Similar for: min,max,mean,std
ds.agg(F.max(df.C)).head(0) #Similar for: min,max,avg,stdev
```

Mutating Joins

A

| | | |
|----|----|----|
| X1 | X2 | X3 |
| a | 1 | |
| b | 2 | |
| c | 3 | |

B

| | | |
|----|----|----|
| X1 | X2 | X3 |
| | | T |
| | F | |
| | T | |

Result

```
A.leftJoin(B, on=X1, how='left')
A.join(B, X1, how='left')
.A.orderBy(X1, ascending=True).show()
```

Join matching rows from B to A

```
A.merge(B, on=X1, how='right')
A.join(B, X1, how='right')
.A.orderBy(X1, ascending=True).show()
```

#Join matching rows from A to B

```
A.merge(B, on=X1, how='left')
A.join(B, X1, how='left')
.A.orderBy(X1, ascending=True).show()
```

#Retain only rows in both sets

```
A.merge(B, on=X1, how='inner')
A.join(B, X1, how='inner')
.A.orderBy(X1, ascending=True).show()
```

#Retain all values, all rows

```
A.merge(B, on=X1, how='full')
A.join(B, X1, how='full')
.A.orderBy(X1, ascending=True).show()
```

Group Data

Pivot

```
pd.pivot_table(dp, values='col1', index='key',
columns='col2', aggfunc=np.sum)
df.groupby(['key']).pivot('col1').sum('col2').show()
```

Windows

Rank

```
dp['rank'] = dp.groupby('B')[C].rank('dense', ascending=False)

w = Window.partitionBy('B').orderBy(ds.C.desc())
ds = ds.withColumn('rank', F.rank().over(w))
```

SQL

```
sql = """
    SELECT * FROM table_name
    """.format(table_name=table_name)
dp = pd.read_sql(sql, conn)
ds = spark.read.parquet('ds')
ds.registerTempTable('ds')
spark.sql("SELECT * FROM ds").show()
```

CHAPTER
TWENTYTHREE

PYSPARK API

Those APIs are automatically generated from PySpark package, so all the CopyRights belong to Spark.

23.1 Stat API

```
class pyspark.ml.stat.ChiSquareTest
```

Note: Experimental

Conduct Pearson's independence test for every feature against the label. For each feature, the (feature, label) pairs are converted into a contingency matrix for which the Chi-squared statistic is computed. All label and feature values must be categorical.

The null hypothesis is that the occurrence of the outcomes is statistically independent.

New in version 2.2.0.

```
static test (dataset, featuresCol, labelCol)
```

Perform a Pearson's independence test using dataset.

Parameters

- **dataset** – DataFrame of categorical labels and categorical features. Real-valued features will be treated as categorical for each distinct value.
- **featuresCol** – Name of features column in dataset, of type *Vector* (*VectorUDT*).
- **labelCol** – Name of label column in dataset, of any numerical type.

Returns DataFrame containing the test result for every feature against the label. This DataFrame will contain a single Row with the following fields: - *pValues* : *Vector* - *degreesOfFreedom* : *Array[Int]* - *statistics* : *Vector* Each of these fields has one value per feature.

```
>>> from pyspark.ml.linalg import Vectors
>>> from pyspark.ml.stat import ChiSquareTest
>>> dataset = [[0, Vectors.dense([0, 0, 1])],
...             [0, Vectors.dense([1, 0, 1])],
...             [1, Vectors.dense([2, 1, 1])],
...             [1, Vectors.dense([3, 1, 1])]]
>>> dataset = spark.createDataFrame(dataset, ["label", "features"])
>>> chiSqResult = ChiSquareTest.test(dataset, 'features', 'label')
>>> chiSqResult.select("degreesOfFreedom").collect()[0]
Row(degreesOfFreedom=[3, 1, 0])
```

New in version 2.2.0.

```
class pyspark.ml.stat.Correlation
```

Note: Experimental

Compute the correlation matrix for the input dataset of Vectors using the specified method. Methods currently supported: *pearson* (default), *spearman*.

Note: For Spearman, a rank correlation, we need to create an RDD[Double] for each column and sort it in order to retrieve the ranks and then join the columns back into an RDD[Vector], which is fairly costly. Cache the input Dataset before calling corr with *method = 'spearman'* to avoid recomputing the common lineage.

New in version 2.2.0.

```
static corr(dataset, column, method='pearson')
```

Compute the correlation matrix with specified method using dataset.

Parameters

- **dataset** – A Dataset or a DataFrame.
- **column** – The name of the column of vectors for which the correlation coefficient needs to be computed. This must be a column of the dataset, and it must contain Vector objects.
- **method** – String specifying the method to use for computing correlation. Supported: *pearson* (default), *spearman*.

Returns A DataFrame that contains the correlation matrix of the column of vectors.

This DataFrame contains a single row and a single column of name ‘\$METHOD-NAME(\$COLUMN)’.

```
>>> from pyspark.ml.linalg import Vectors
>>> from pyspark.ml.stat import Correlation
>>> dataset = [[Vectors.dense([1, 0, 0, -2])],
...             [Vectors.dense([4, 5, 0, 3])],
```

(continues on next page)

(continued from previous page)

```

...           [Vectors.dense([6, 7, 0, 8])],
...
...           [Vectors.dense([9, 0, 0, 1])])
>>> dataset = spark.createDataFrame(dataset, ['features'])
>>> pearsonCorr = Correlation.corr(dataset, 'features', 'pearson').
->collect()[0][0]
>>> print(str(pearsonCorr).replace('nan', 'NaN'))
DenseMatrix([[ 1.          ,  0.0556...,      NaN,  0.4004...],
             [ 0.0556...,  1.          ,      NaN,  0.9135...],
             [      NaN,      NaN,  1.          ,      NaN],
             [ 0.4004...,  0.9135...,      NaN,  1.          ]])
>>> spearmanCorr = Correlation.corr(dataset, 'features', method=
->'spearman').collect()[0][0]
>>> print(str(spearmanCorr).replace('nan', 'NaN'))
DenseMatrix([[ 1.          ,  0.1054...,      NaN,  0.4        ],
             [ 0.1054...,  1.          ,      NaN,  0.9486...],
             [      NaN,      NaN,  1.          ,      NaN],
             [ 0.4        ,  0.9486...,      NaN,  1.          ]])

```

New in version 2.2.0.

`class pyspark.ml.stat.KolmogorovSmirnovTest`

Note: Experimental

Conduct the two-sided Kolmogorov Smirnov (KS) test for data sampled from a continuous distribution.

By comparing the largest difference between the empirical cumulative distribution of the sample data and the theoretical distribution we can provide a test for the null hypothesis that the sample data comes from that theoretical distribution.

New in version 2.4.0.

`static test(dataset, sampleCol, distName, *params)`

Conduct a one-sample, two-sided Kolmogorov-Smirnov test for probability distribution equality. Currently supports the normal distribution, taking as parameters the mean and standard deviation.

Parameters

- **dataset** – a Dataset or a DataFrame containing the sample of data to test.
- **sampleCol** – Name of sample column in dataset, of any numerical type.
- **distName** – a *string* name for a theoretical distribution, currently only support “norm”.
- **params** – a list of *Double* values specifying the parameters to be used for the theoretical distribution. For “norm” distribution, the parameters includes mean and variance.

Returns A DataFrame that contains the Kolmogorov-Smirnov test result for the input sampled data. This DataFrame will contain a single Row with the following fields:
- *pValue* : Double - *statistic* : Double

```
>>> from pyspark.ml.stat import KolmogorovSmirnovTest
>>> dataset = [[-1.0], [0.0], [1.0]]
>>> dataset = spark.createDataFrame(dataset, ['sample'])
>>> ksResult = KolmogorovSmirnovTest.test(dataset, 'sample', 'norm', ↵
    ↵0.0, 1.0).first()
>>> round(ksResult.pValue, 3)
1.0
>>> round(ksResult.statistic, 3)
0.175
>>> dataset = [[2.0], [3.0], [4.0]]
>>> dataset = spark.createDataFrame(dataset, ['sample'])
>>> ksResult = KolmogorovSmirnovTest.test(dataset, 'sample', 'norm', ↵
    ↵3.0, 1.0).first()
>>> round(ksResult.pValue, 3)
1.0
>>> round(ksResult.statistic, 3)
0.175
```

New in version 2.4.0.

```
class pyspark.ml.stat.Summarizer
```

Note: Experimental

Tools for vectorized statistics on MLlib Vectors. The methods in this package provide various statistics for Vectors contained inside DataFrames. This class lets users pick the statistics they would like to extract for a given column.

```
>>> from pyspark.ml.stat import Summarizer
>>> from pyspark.sql import Row
>>> from pyspark.ml.linalg import Vectors
>>> summarizer = Summarizer.metrics("mean", "count")
>>> df = sc.parallelize([Row(weight=1.0, features=Vectors.dense(1.0, 1.0,
    ↵ 1.0)),
...                     Row(weight=0.0, features=Vectors.dense(1.0, 2.0,
    ↵ 3.0))]).toDF()
>>> df.select(summarizer.summary(df.features, df.weight)).show(truncate=False)
+-----+
|aggregate_metrics(features, weight)|
+-----+
|[ [1.0,1.0,1.0], 1] |
+-----+
<BLANKLINE>
>>> df.select(summarizer.summary(df.features)).show(truncate=False)
+-----+
```

(continues on next page)

(continued from previous page)

```
|aggregate_metrics(features, 1.0) |
+-----+
|[ [1.0,1.5,2.0], 2]           |
+-----+
<BLANKLINE>
>>> df.select(Summarizer.mean(df.features, df.weight)) .
    ↵show(truncate=False)
+-----+
|mean(features) |
+-----+
|[1.0,1.0,1.0] |
+-----+
<BLANKLINE>
>>> df.select(Summarizer.mean(df.features)) . show(truncate=False)
+-----+
|mean(features) |
+-----+
|[1.0,1.5,2.0] |
+-----+
<BLANKLINE>
```

New in version 2.4.0.

static count(*col*, *weightCol=None*)
return a column of count summary

New in version 2.4.0.

static max(*col*, *weightCol=None*)
return a column of max summary

New in version 2.4.0.

static mean(*col*, *weightCol=None*)
return a column of mean summary

New in version 2.4.0.

static metrics(*metrics)
Given a list of metrics, provides a builder that it turns computes metrics from a column.

See the documentation of [[Summarizer]] for an example.

The following metrics are accepted (case sensitive):

- mean: a vector that contains the coefficient-wise mean.
- variance: a vector that contains the coefficient-wise variance.
- count: the count of all vectors seen.
- numNonzeros: a vector with the number of non-zeros for each coefficients
- max: the maximum for each coefficient.
- min: the minimum for each coefficient.

- normL2: the Euclidian norm for each coefficient.
- normL1: the L1 norm of each coefficient (sum of the absolute values).

Parameters `metrics` – metrics that can be provided.

Returns an object of `pyspark.ml.stat.SummaryBuilder`

Note: Currently, the performance of this interface is about 2x~3x slower then using the RDD interface.

New in version 2.4.0.

static min (`col, weightCol=None`)
return a column of min summary

New in version 2.4.0.

static normL1 (`col, weightCol=None`)
return a column of normL1 summary

New in version 2.4.0.

static normL2 (`col, weightCol=None`)
return a column of normL2 summary

New in version 2.4.0.

static numNonZeros (`col, weightCol=None`)
return a column of numNonZero summary

New in version 2.4.0.

static variance (`col, weightCol=None`)
return a column of variance summary

New in version 2.4.0.

class `pyspark.ml.stat.SummaryBuilder` (`jSummaryBuilder`)

Note: Experimental

A builder object that provides summary statistics about a given column.

Users should not directly create such builders, but instead use one of the methods in `pyspark.ml.stat.Summarizer`

New in version 2.4.0.

summary (`featuresCol, weightCol=None`)

Returns an aggregate object that contains the summary of the column with the requested metrics.

Parameters

- `featuresCol` – a column that contains features Vector object.

- **weightCol** – a column that contains weight value. Default weight is 1.0.

Returns an aggregate column that contains the statistics. The exact content of this structure is determined during the creation of the builder.

New in version 2.4.0.

23.2 Regression API

```
class pyspark.ml.regression.AFTSurvivalRegression(featuresCol='features',
                                                 labelCol='label', predictionCol='prediction',
                                                 fitIntercept=True, maxIter=100, tol=1e-06, censorCol='censor', quantileProbabilities=[0.01,
                                                 0.05, 0.1, 0.25, 0.5, 0.75, 0.9, 0.95, 0.99], quantilesCol=None,
                                                 aggregationDepth=2)
```

Note: Experimental

Accelerated Failure Time (AFT) Model Survival Regression

Fit a parametric AFT survival regression model based on the Weibull distribution of the survival time.

See also:

AFT Model

```
>>> from pyspark.ml.linalg import Vectors
>>> df = spark.createDataFrame([
...     (1.0, Vectors.dense(1.0), 1.0),
...     (1e-40, Vectors.sparse(1, [], []), 0.0)], ["label", "features",
...     "censor"])
>>> aftsr = AFTSurvivalRegression()
>>> model = aftsr.fit(df)
>>> model.predict(Vectors.dense(6.3))
1.0
>>> model.predictQuantiles(Vectors.dense(6.3))
DenseVector([0.0101, 0.0513, 0.1054, 0.2877, 0.6931, 1.3863, 2.3026, 2.
             9957, 4.6052])
>>> model.transform(df).show()
+-----+-----+-----+
| label | features|censor|prediction|
+-----+-----+-----+
| 1.0 | [1.0] | 1.0 | 1.0 |
| 1.0E-40 | (1, [], []) | 0.0 | 1.0 |
```

(continues on next page)

(continued from previous page)

```
+-----+-----+-----+-----+
...
>>> aftsr_path = temp_path + "/aftsr"
>>> aftsr.save(aftsr_path)
>>> aftsr2 = AFTSurvivalRegression.load(aftsr_path)
>>> aftsr2.getMaxIter()
100
>>> model_path = temp_path + "/aftsr_model"
>>> model.save(model_path)
>>> model2 = AFTSurvivalRegressionModel.load(model_path)
>>> model.coefficients == model2.coefficients
True
>>> model.intercept == model2.intercept
True
>>> model.scale == model2.scale
True
```

New in version 1.6.0.

getCensorCol()

Gets the value of censorCol or its default value.

New in version 1.6.0.

getQuantileProbabilities()

Gets the value of quantileProbabilities or its default value.

New in version 1.6.0.

getQuantilesCol()

Gets the value of quantilesCol or its default value.

New in version 1.6.0.

setCensorCol(value)

Sets the value of censorCol.

New in version 1.6.0.

setParams(featuresCol='features', labelCol='label', predictionCol='prediction', fitIntercept=True, maxIter=100, tol=1e-06, censorCol='censor', quantileProbabilities=[0.01, 0.05, 0.1, 0.25, 0.5, 0.75, 0.9, 0.95, 0.99], quantilesCol=None, aggregationDepth=2)
setParams(self, featuresCol="features", labelCol="label", predictionCol="prediction", fitIntercept=True, maxIter=100, tol=1E-6, censorCol="censor", quantileProbabilities=[0.01, 0.05, 0.1, 0.25, 0.5, 0.75, 0.9, 0.95, 0.99], quantilesCol=None, aggregationDepth=2):

New in version 1.6.0.

setQuantileProbabilities(value)

Sets the value of quantileProbabilities.

New in version 1.6.0.

setQuantilesCol (*value*)
Sets the value of quantilesCol.

New in version 1.6.0.

class pyspark.ml.regression.AFTSurvivalRegressionModel (*java_model=None*)

Note: Experimental

Model fitted by *AFTSurvivalRegression*.

New in version 1.6.0.

coefficients
Model coefficients.

New in version 2.0.0.

intercept
Model intercept.

New in version 1.6.0.

predict (*features*)
Predicted value

New in version 2.0.0.

predictQuantiles (*features*)
Predicted Quantiles

New in version 2.0.0.

scale
Model scale parameter.

New in version 1.6.0.

class pyspark.ml.regression.DecisionTreeRegressor (*featuresCol='features'*,
labelCol='label', *predictionCol='prediction'*,
maxDepth=5,
maxBins=32, *minInstancesPerNode=1*,
minInfoGain=0.0,
maxMemoryInMB=256,
cacheNodeIds=False,
checkpointInterval=10,
impurity='variance',
seed=None, *varianceCol=None*)

Decision tree learning algorithm for regression. It supports both continuous and categorical features.

```
>>> from pyspark.ml.linalg import Vectors
>>> df = spark.createDataFrame([
...     (1.0, Vectors.dense(1.0)),
...     (0.0, Vectors.sparse(1, [], [])), ["label", "features"])
>>> dt = DecisionTreeRegressor(maxDepth=2, varianceCol="variance")
>>> model = dt.fit(df)
>>> model.depth
1
>>> model.numNodes
3
>>> model.featureImportances
SparseVector(1, {0: 1.0})
>>> model.numFeatures
1
>>> test0 = spark.createDataFrame([(Vectors.dense(-1.0),)], ["features"])
>>> model.transform(test0).head().prediction
0.0
>>> test1 = spark.createDataFrame([(Vectors.sparse(1, [0], [1.0]),)], [
...     "features"])
>>> model.transform(test1).head().prediction
1.0
>>> dtr_path = temp_path + "/dtr"
>>> dt.save(dtr_path)
>>> dt2 = DecisionTreeRegressor.load(dtr_path)
>>> dt2.getMaxDepth()
2
>>> model_path = temp_path + "/dtr_model"
>>> model.save(model_path)
>>> model2 = DecisionTreeRegressionModel.load(model_path)
>>> model.numNodes == model2.numNodes
True
>>> model.depth == model2.depth
True
>>> model.transform(test1).head().variance
0.0
```

New in version 1.4.0.

setParams (*self*, *featuresCol*=“*features*”, *labelCol*=“*label*”, *predictionCol*=“*prediction*”, *maxDepth*=5, *maxBins*=32, *minInstancesPerNode*=1, *minInfoGain*=0.0, *maxMemoryInMB*=256, *cacheNodeIds*=False, *checkpointInterval*=10, *impurity*=“*variance*”, *seed*=None, *varianceCol*=None)

Sets params for the DecisionTreeRegressor.

New in version 1.4.0.

class pyspark.ml.regression.DecisionTreeRegressionModel (*java_model*=None)
Model fitted by *DecisionTreeRegressor*.

New in version 1.4.0.

featureImportances

Estimate of the importance of each feature.

This generalizes the idea of “Gini” importance to other losses, following the explanation of Gini importance from “Random Forests” documentation by Leo Breiman and Adele Cutler, and following the implementation from scikit-learn.

This feature importance is calculated as follows:

- $\text{importance}(\text{feature } j) = \sum (\text{over nodes which split on feature } j) \text{ of the gain}$, where gain is scaled by the number of instances passing through node
- Normalize importances for tree to sum to 1.

Note: Feature importance for single decision trees can have high variance due to correlated predictor variables. Consider using a `RandomForestRegressor` to determine feature importance instead.

New in version 2.0.0.

```
class pyspark.ml.regression.GBTRegressor(featuresCol='features',           la-
                                           labelCol='label',                 prediction-
                                           Col='prediction',               maxDepth=5,
                                           maxBins=32, minInstancesPerNode=1,
                                           minInfoGain=0.0,                maxMemory-
                                           InMB=256, cacheNodeIds=False,
                                           subsamplingRate=1.0, checkpointIn-
                                           terval=10, lossType='squared',
                                           maxIter=20, stepSize=0.1, seed=None,
                                           impurity='variance', featureSubset-
                                           Strategy='all')
```

Gradient-Boosted Trees (GBTs) learning algorithm for regression. It supports both continuous and categorical features.

```
>>> from numpy import allclose
>>> from pyspark.ml.linalg import Vectors
>>> df = spark.createDataFrame([
...     (1.0, Vectors.dense(1.0)),
...     (0.0, Vectors.sparse(1, [], []))], ["label", "features"])
>>> gbt = GBTRegressor(maxIter=5, maxDepth=2, seed=42)
>>> print(gbt.getImpurity())
variance
>>> print(gbt.getFeatureSubsetStrategy())
all
>>> model = gbt.fit(df)
>>> model.featureImportances
SparseVector(1, {0: 1.0})
>>> model.numFeatures
1
>>> allclose(model.treeWeights, [1.0, 0.1, 0.1, 0.1, 0.1])
True
>>> test0 = spark.createDataFrame([(Vectors.dense(-1.0),)], ["features"])
>>> model.transform(test0).head().prediction
0.0
```

(continues on next page)

(continued from previous page)

```
>>> test1 = spark.createDataFrame([(Vectors.sparse(1, [0], [1.0]),)], [←"features"])
>>> model.transform(test1).head().prediction
1.0
>>> gbtr_path = temp_path + "gbtr"
>>> gbt.save(gbtr_path)
>>> gbt2 = GBTRRegressor.load(gbtr_path)
>>> gbt2.getMaxDepth()
2
>>> model_path = temp_path + "gbtr_model"
>>> model.save(model_path)
>>> model2 = GBTRgressionModel.load(model_path)
>>> model.featureImportances == model2.featureImportances
True
>>> model.treeWeights == model2.treeWeights
True
>>> model.trees
[DecisionTreeRegressionModel (uid=...) of depth..., ↵DecisionTreeRegressionModel...]
>>> validation = spark.createDataFrame([(0.0, Vectors.dense(-1.0))],
...           ["label", "features"])
>>> model.evaluateEachIteration(validation, "squared")
[0.0, 0.0, 0.0, 0.0, 0.0]
```

New in version 1.4.0.

getLossType()

Gets the value of lossType or its default value.

New in version 1.4.0.

setFeatureSubsetStrategy(*value*)

Sets the value of featureSubsetStrategy.

New in version 2.4.0.

setLossType(*value*)

Sets the value of lossType.

New in version 1.4.0.

setParams(*self*, *featuresCol*=*"features"*, *labelCol*=*"label"*, *predictionCol*=*"prediction"*, maxDepth=5, maxBins=32, minInstancesPerNode=1, minInfoGain=0.0, maxMemoryInMB=256, cacheNodeIds=False, subsamplingRate=1.0, check- pointInterval=10, lossType="squared", maxIter=20, stepSize=0.1, seed=None, impurity="variance", featureSubsetStrategy="all")

Sets params for Gradient Boosted Tree Regression.

New in version 1.4.0.

```
class pyspark.ml.regression.GBTRgressionModel (java_model=None)
Model fitted by GBTRegressor.
```

New in version 1.4.0.

evaluateEachIteration(*dataset, loss*)

Method to compute error or loss for every iteration of gradient boosting.

Parameters

- **dataset** – Test dataset to evaluate model on, where dataset is an instance of `pyspark.sql.DataFrame`
- **loss** – The loss function used to compute error. Supported options: squared, absolute

New in version 2.4.0.

featureImportances

Estimate of the importance of each feature.

Each feature's importance is the average of its importance across all trees in the ensemble. The importance vector is normalized to sum to 1. This method is suggested by Hastie et al. (Hastie, Tibshirani, Friedman. “The Elements of Statistical Learning, 2nd Edition.” 2001.) and follows the implementation from scikit-learn.

See also:

`DecisionTreeRegressionModel.featureImportances`

New in version 2.0.0.

trees

These have null parent Estimators.

New in version 2.0.0.

Type Trees in this ensemble. Warning

```
class pyspark.ml.regression.GeneralizedLinearRegression(labelCol='label',
    fea-
    turesCol='features',
    prediction-
    Col='prediction',
    fam-
    ily='gaussian',
    link=None, fit-
    Intercept=True,
    maxIter=25,
    tol=1e-06, reg-
    Param=0.0,
    weight-
    Col=None,
    solver='irls',
    linkPrediction-
    Col=None, vari-
    ancePower=0.0,
    linkPower=None,
    offset-
    Col=None)
```

Note: Experimental

Generalized Linear Regression.

Fit a Generalized Linear Model specified by giving a symbolic description of the linear predictor (link function) and a description of the error distribution (family). It supports “gaussian”, “binomial”, “poisson”, “gamma” and “tweedie” as family. Valid link functions for each family is listed below. The first link function of each family is the default one.

- “gaussian” -> “identity”, “log”, “inverse”
- “binomial” -> “logit”, “probit”, “cloglog”
- “poisson” -> “log”, “identity”, “sqrt”
- “gamma” -> “inverse”, “identity”, “log”
- “tweedie” -> power link function specified through “linkPower”. The default link power in the tweedie family is 1 - variancePower.

See also:

[GLM](#)

```
>>> from pyspark.ml.linalg import Vectors
>>> df = spark.createDataFrame([
...     (1.0, Vectors.dense(0.0, 0.0)),
...     (1.0, Vectors.dense(1.0, 2.0)),
```

(continues on next page)

(continued from previous page)

```

...      (2.0, Vectors.dense(0.0, 0.0)),
...      (2.0, Vectors.dense(1.0, 1.0)),], ["label", "features"])
>>> glr = GeneralizedLinearRegression(family="gaussian", link="identity",
    ↪ linkPredictionCol="p")
>>> model = glr.fit(df)
>>> transformed = model.transform(df)
>>> abs(transformed.head().prediction - 1.5) < 0.001
True
>>> abs(transformed.head().p - 1.5) < 0.001
True
>>> model.coefficients
DenseVector([1.5..., -1.0...])
>>> model.numFeatures
2
>>> abs(model.intercept - 1.5) < 0.001
True
>>> glr_path = temp_path + "/glr"
>>> glr.save(glr_path)
>>> glr2 = GeneralizedLinearRegression.load(glr_path)
>>> glr.getFamily() == glr2.getFamily()
True
>>> model_path = temp_path + "/glr_model"
>>> model.save(model_path)
>>> model2 = GeneralizedLinearRegressionModel.load(model_path)
>>> model.intercept == model2.intercept
True
>>> model.coefficients[0] == model2.coefficients[0]
True

```

New in version 2.0.0.

getFamily()

Gets the value of family or its default value.

New in version 2.0.0.

getLink()

Gets the value of link or its default value.

New in version 2.0.0.

getLinkPower()

Gets the value of linkPower or its default value.

New in version 2.2.0.

getLinkPredictionCol()

Gets the value of linkPredictionCol or its default value.

New in version 2.0.0.

getOffsetCol()

Gets the value of offsetCol or its default value.

New in version 2.3.0.

getVariancePower()

Gets the value of variancePower or its default value.

New in version 2.2.0.

setFamily(value)

Sets the value of family.

New in version 2.0.0.

setLink(value)

Sets the value of link.

New in version 2.0.0.

setLinkPower(value)

Sets the value of linkPower.

New in version 2.2.0.

setLinkPredictionCol(value)

Sets the value of linkPredictionCol.

New in version 2.0.0.

setOffsetCol(value)

Sets the value of offsetCol.

New in version 2.3.0.

setParams(self, labelCol="label", featuresCol="features", predictionCol="prediction", family="gaussian", link=None, fitIntercept=True, maxIter=25, tol=1e-6, regParam=0.0, weightCol=None, solver="irls", linkPredictionCol=None, variancePower=0.0, linkPower=None, offsetCol=None)

Sets params for generalized linear regression.

New in version 2.0.0.

setVariancePower(value)

Sets the value of variancePower.

New in version 2.2.0.

class pyspark.ml.regression.GeneralizedLinearRegressionModel (java_model=None)

Note: Experimental

Model fitted by *GeneralizedLinearRegression*.

New in version 2.0.0.

coefficients

Model coefficients.

New in version 2.0.0.

evaluate(*dataset*)

Evaluates the model on a test dataset.

Parameters **dataset** – Test dataset to evaluate model on, where dataset is an instance of `pyspark.sql.DataFrame`

New in version 2.0.0.

hasSummary

Indicates whether a training summary exists for this model instance.

New in version 2.0.0.

intercept

Model intercept.

New in version 2.0.0.

summary

Gets summary (e.g. residuals, deviance, pValues) of model on training set. An exception is thrown if *trainingSummary* is *None*.

New in version 2.0.0.

class `pyspark.ml.regression.GeneralizedLinearRegressionSummary`(*java_obj=None*)

Note: Experimental

Generalized linear regression results evaluated on a dataset.

New in version 2.0.0.

aic

Akaike’s “An Information Criterion”(AIC) for the fitted model.

New in version 2.0.0.

degreesOfFreedom

Degrees of freedom.

New in version 2.0.0.

deviance

The deviance for the fitted model.

New in version 2.0.0.

dispersion

The dispersion of the fitted model. It is taken as 1.0 for the “binomial” and “poisson” families, and otherwise estimated by the residual Pearson’s Chi-Squared statistic (which is defined as sum of the squares of the Pearson residuals) divided by the residual degrees of freedom.

New in version 2.0.0.

nullDeviance

The deviance for the null model.

New in version 2.0.0.

numInstances

Number of instances in DataFrame predictions.

New in version 2.2.0.

predictionCol

Field in *predictions* which gives the predicted value of each instance. This is set to a new column name if the original model's *predictionCol* is not set.

New in version 2.0.0.

predictions

Predictions output by the model's *transform* method.

New in version 2.0.0.

rank

The numeric rank of the fitted linear model.

New in version 2.0.0.

residualDegreeOfFreedom

The residual degrees of freedom.

New in version 2.0.0.

residualDegreeOfFreedomNull

The residual degrees of freedom for the null model.

New in version 2.0.0.

residuals (*residualsType='deviance'*)

Get the residuals of the fitted model by type.

Parameters **residualsType** – The type of residuals which should be returned.

Supported options: deviance (default), pearson, working, and response.

New in version 2.0.0.

class pyspark.ml.regression.GeneralizedLinearRegressionTrainingSummary (*java_obj=None*)

Note: Experimental

Generalized linear regression training results.

New in version 2.0.0.

coefficientStandardErrors

Standard error of estimated coefficients and intercept.

If `GeneralizedLinearRegression.fitIntercept` is set to True, then the last element returned corresponds to the intercept.

New in version 2.0.0.

numIterations

Number of training iterations.

New in version 2.0.0.

pValues

Two-sided p-value of estimated coefficients and intercept.

If `GeneralizedLinearRegression.fitIntercept` is set to True, then the last element returned corresponds to the intercept.

New in version 2.0.0.

solver

The numeric solver used for training.

New in version 2.0.0.

tValues

T-statistic of estimated coefficients and intercept.

If `GeneralizedLinearRegression.fitIntercept` is set to True, then the last element returned corresponds to the intercept.

New in version 2.0.0.

```
class pyspark.ml.regression.IsotonicRegression(featuresCol='features',
                                                labelCol='label', predictionCol='prediction',
                                                weightCol=None, isotonic=True,
                                                featureIndex=0)
```

Currently implemented using parallelized pool adjacent violators algorithm. Only univariate (single feature) algorithm supported.

```
>>> from pyspark.ml.linalg import Vectors
>>> df = spark.createDataFrame([
...     (1.0, Vectors.dense(1.0)),
...     (0.0, Vectors.sparse(1, [], []))], ["label", "features"])
>>> ir = IsotonicRegression()
>>> model = ir.fit(df)
>>> test0 = spark.createDataFrame([(Vectors.dense(-1.0),)], ["features"])
>>> model.transform(test0).head().prediction
0.0
>>> model.boundaries
DenseVector([0.0, 1.0])
>>> ir_path = temp_path + "/ir"
>>> ir.save(ir_path)
>>> ir2 = IsotonicRegression.load(ir_path)
>>> ir2.getIsotonic()
True
```

(continues on next page)

(continued from previous page)

```
>>> model_path = temp_path + "/ir_model"
>>> model.save(model_path)
>>> model2 = IsotonicRegressionModel.load(model_path)
>>> model.boundaries == model2.boundaries
True
>>> model.predictions == model2.predictions
True
```

New in version 1.6.0.

getFeatureIndex()

Gets the value of featureIndex or its default value.

getIsotonic()

Gets the value of isotonic or its default value.

setFeatureIndex(value)

Sets the value of featureIndex.

setIsotonic(value)

Sets the value of isotonic.

```
setParams(featuresCol='features', labelCol='label', predictionCol='prediction', weight-
Col=None, isotonic=True, featureIndex=0)
setParams(self, featuresCol="features", labelCol="label", predictionCol="prediction", weight-
Col=None, isotonic=True, featureIndex=0): Set the params for IsotonicRegression.
```

```
class pyspark.ml.regression.IsotonicRegressionModel(java_model=None)
Model fitted by IsotonicRegression.
```

New in version 1.6.0.

boundaries

Boundaries in increasing order for which predictions are known.

New in version 1.6.0.

predictions

Predictions associated with the boundaries at the same index, monotone because of isotonic regression.

New in version 1.6.0.

```
class pyspark.ml.regression.LinearRegression(featuresCol='features',      la-
belCol='label',      prediction-
Col='prediction', maxIter=100,
regParam=0.0,      elasticNet-
Param=0.0,      tol=1e-06,      fit-
Intercept=True,      standard-
ization=True,      solver='auto',
weightCol=None,      aggregation-
Depth=2,      loss='squaredError',
epsilon=1.35)
```

Linear regression.

The learning objective is to minimize the specified loss function, with regularization. This supports two kinds of loss:

- squaredError (a.k.a squared loss)
- huber (a hybrid of squared error for relatively small errors and absolute error for relatively large ones, and we estimate the scale parameter from training data)

This supports multiple types of regularization:

- none (a.k.a. ordinary least squares)
- L2 (ridge regression)
- L1 (Lasso)
- L2 + L1 (elastic net)

Note: Fitting with huber loss only supports none and L2 regularization.

```
>>> from pyspark.ml.linalg import Vectors
>>> df = spark.createDataFrame([
...     (1.0, 2.0, Vectors.dense(1.0)),
...     (0.0, 2.0, Vectors.sparse(1, [1], [1]))], ["label", "weight",
... "features"])
>>> lr = LinearRegression(maxIter=5, regParam=0.0, solver="normal",
... weightCol="weight")
>>> model = lr.fit(df)
>>> test0 = spark.createDataFrame([(Vectors.dense(-1.0),)], ["features"])
>>> abs(model.transform(test0).head().prediction - (-1.0)) < 0.001
True
>>> abs(model.coefficients[0] - 1.0) < 0.001
True
>>> abs(model.intercept - 0.0) < 0.001
True
>>> test1 = spark.createDataFrame([(Vectors.sparse(1, [0], [1.0]),)], [
... "features"])
>>> abs(model.transform(test1).head().prediction - 1.0) < 0.001
True
>>> lr.setParams("vector")
Traceback (most recent call last):
...
TypeError: Method setParams forces keyword arguments.
>>> lr_path = temp_path + "/lr"
>>> lr.save(lr_path)
>>> lr2 = LinearRegression.load(lr_path)
>>> lr2.getMaxIter()
5
>>> model_path = temp_path + "/lr_model"
>>> model.save(model_path)
>>> model2 = LinearRegressionModel.load(model_path)
>>> model.coefficients[0] == model2.coefficients[0]
True
>>> model.intercept == model2.intercept
True
```

(continues on next page)

(continued from previous page)

```
>>> model.numFeatures  
1  
>>> model.write().format("pml").save(model_path + "_2")
```

New in version 1.4.0.

getEpsilon()

Gets the value of epsilon or its default value.

New in version 2.3.0.

setEpsilon(value)

Sets the value of epsilon.

New in version 2.3.0.

```
setParams(self, featuresCol="features", labelCol="label", predictionCol="prediction",
           maxIter=100, regParam=0.0, elasticNetParam=0.0, tol=1e-6, fitIntercept=True,
           standardization=True, solver="auto", weightCol=None, aggregationDepth=2,
           loss="squaredError", epsilon=1.35)
```

Sets params for linear regression.

New in version 1.4.0.

```
class pyspark.ml.regression.LinearRegressionModel(java_model=None)
```

Model fitted by *LinearRegression*.

New in version 1.4.0.

coefficients

Model coefficients.

New in version 2.0.0.

evaluate(dataset)

Evaluates the model on a test dataset.

Parameters **dataset** – Test dataset to evaluate model on, where dataset is an instance of `pyspark.sql.DataFrame`

New in version 2.0.0.

hasSummary

Indicates whether a training summary exists for this model instance.

New in version 2.0.0.

intercept

Model intercept.

New in version 1.4.0.

scale

The value by which $\|y - X'w\|$ is scaled down when loss is “huber”, otherwise 1.0.

New in version 2.3.0.

summary

Gets summary (e.g. residuals, mse, r-squared) of model on training set. An exception is thrown if *trainingSummary* is *None*.

New in version 2.0.0.

```
class pyspark.ml.regression.LinearRegressionSummary(java_obj=None)
```

Note: Experimental

Linear regression results evaluated on a dataset.

New in version 2.0.0.

coefficientStandardErrors

Standard error of estimated coefficients and intercept. This value is only available when using the “normal” solver.

If `LinearRegression.fitIntercept` is set to True, then the last element returned corresponds to the intercept.

See also:

`LinearRegression.solver`

New in version 2.0.0.

degreesOfFreedom

Degrees of freedom.

New in version 2.2.0.

devianceResiduals

The weighted residuals, the usual residuals rescaled by the square root of the instance weights.

New in version 2.0.0.

explainedVariance

Returns the explained variance regression score. $\text{explainedVariance} = 1 - \frac{\text{variance}(y - \hat{y})}{\text{variance}(y)}$

See also:

[Wikipedia explain variation](#)

Note: This ignores instance weights (setting all to 1.0) from `LinearRegression.weightCol`. This will change in later Spark versions.

New in version 2.0.0.

featuresCol

Field in “predictions” which gives the features of each instance as a vector.

New in version 2.0.0.

labelCol

Field in “predictions” which gives the true label of each instance.

New in version 2.0.0.

meanAbsoluteError

Returns the mean absolute error, which is a risk function corresponding to the expected value of the absolute error loss or l1-norm loss.

Note: This ignores instance weights (setting all to 1.0) from *LinearRegression.weightCol*. This will change in later Spark versions.

New in version 2.0.0.

meanSquaredError

Returns the mean squared error, which is a risk function corresponding to the expected value of the squared error loss or quadratic loss.

Note: This ignores instance weights (setting all to 1.0) from *LinearRegression.weightCol*. This will change in later Spark versions.

New in version 2.0.0.

numInstances

Number of instances in DataFrame predictions

New in version 2.0.0.

pValues

Two-sided p-value of estimated coefficients and intercept. This value is only available when using the “normal” solver.

If *LinearRegression.fitIntercept* is set to True, then the last element returned corresponds to the intercept.

See also:

LinearRegression.solver

New in version 2.0.0.

predictionCol

Field in “predictions” which gives the predicted value of the label at each instance.

New in version 2.0.0.

predictions

Dataframe outputted by the model’s *transform* method.

New in version 2.0.0.

r2

Returns R², the coefficient of determination.

See also:

[Wikipedia coefficient of determination](#)

Note: This ignores instance weights (setting all to 1.0) from `LinearRegression.weightCol`. This will change in later Spark versions.

New in version 2.0.0.

r2adj

Returns Adjusted R², the adjusted coefficient of determination.

See also:

[Wikipedia coefficient of determination](#), [Adjusted R²](#)

Note: This ignores instance weights (setting all to 1.0) from `LinearRegression.weightCol`. This will change in later Spark versions.

New in version 2.4.0.

residuals

Residuals (label - predicted value)

New in version 2.0.0.

rootMeanSquaredError

Returns the root mean squared error, which is defined as the square root of the mean squared error.

Note: This ignores instance weights (setting all to 1.0) from `LinearRegression.weightCol`. This will change in later Spark versions.

New in version 2.0.0.

tValues

T-statistic of estimated coefficients and intercept. This value is only available when using the “normal” solver.

If `LinearRegression.fitIntercept` is set to True, then the last element returned corresponds to the intercept.

See also:

`LinearRegression.solver`

New in version 2.0.0.

class `pyspark.ml.regression.LinearRegressionTrainingSummary (java_obj=None)`

Note: Experimental

Linear regression training results. Currently, the training summary ignores the training weights except for the objective trace.

New in version 2.0.0.

objectiveHistory

Objective function (scaled loss + regularization) at each iteration. This value is only available when using the “l-bfgs” solver.

See also:

`LinearRegression.solver`

New in version 2.0.0.

totalIterations

Number of training iterations until termination. This value is only available when using the “l-bfgs” solver.

See also:

`LinearRegression.solver`

New in version 2.0.0.

```
class pyspark.ml.regression.RandomForestRegressor(featuresCol='features',
                                                 labelCol='label', predictionCol='prediction',
                                                 maxDepth=5,
                                                 maxBins=32, minInstancesPerNode=1,
                                                 minInfoGain=0.0,
                                                 maxMemoryInMB=256,
                                                 cacheNodeIds=False,
                                                 checkpointInterval=10,
                                                 impurity='variance',
                                                 subsamplingRate=1.0, seed=None,
                                                 numTrees=20, featureSubsetStrategy='auto')
```

Random Forest learning algorithm for regression. It supports both continuous and categorical features.

```
>>> from numpy import allclose
>>> from pyspark.ml.linalg import Vectors
>>> df = spark.createDataFrame([
...     (1.0, Vectors.dense(1.0)),
...     (0.0, Vectors.sparse(1, [], []))], ["label", "features"])
>>> rf = RandomForestRegressor(numTrees=2, maxDepth=2, seed=42)
>>> model = rf.fit(df)
>>> model.featureImportances
```

(continues on next page)

(continued from previous page)

```

SparseVector(1, {0: 1.0})
>>> allclose(model.treeWeights, [1.0, 1.0])
True
>>> test0 = spark.createDataFrame([(Vectors.dense(-1.0),)], ["features"])
>>> model.transform(test0).head().prediction
0.0
>>> model.numFeatures
1
>>> model.trees
[DecisionTreeRegressionModel (uid=...) of depth..., ↴
DecisionTreeRegressionModel...]
>>> model.getNumTrees
2
>>> test1 = spark.createDataFrame([(Vectors.sparse(1, [0], [1.0]),)], [
    ↴"features"])
>>> model.transform(test1).head().prediction
0.5
>>> rfr_path = temp_path + "/rfr"
>>> rf.save(rfr_path)
>>> rf2 = RandomForestRegressor.load(rfr_path)
>>> rf2.getNumTrees()
2
>>> model_path = temp_path + "/rfr_model"
>>> model.save(model_path)
>>> model2 = RandomForestRegressionModel.load(model_path)
>>> model.featureImportances == model2.featureImportances
True

```

New in version 1.4.0.

setFeatureSubsetStrategy (*value*)

Sets the value of featureSubsetStrategy.

New in version 2.4.0.

setParams (*self*, *featuresCol*=“*features*”, *labelCol*=“*label*”, *predictionCol*=“*prediction*”,
maxDepth=5, *maxBins*=32, *minInstancesPerNode*=1, *minInfoGain*=0.0,
maxMemoryInMB=256, *cacheNodeIds*=False, *checkpointInterval*=10, *impu-*
rity=“*variance*”, *subsamplingRate*=1.0, *seed*=None, *numTrees*=20, *featureSub-*
setStrategy=“*auto*”)

Sets params for linear regression.

New in version 1.4.0.

class pyspark.ml.regression.**RandomForestRegressionModel** (*java_model*=None)

Model fitted by *RandomForestRegressor*.

New in version 1.4.0.

featureImportances

Estimate of the importance of each feature.

Each feature’s importance is the average of its importance across all trees in the ensemble. The importance vector is normalized to sum to 1. This method is suggested by Hastie et al. (Hastie,

Tibshirani, Friedman. “The Elements of Statistical Learning, 2nd Edition.” 2001.) and follows the implementation from scikit-learn.

See also:

`DecisionTreeRegressionModel.featureImportances`

New in version 2.0.0.

trees

These have null parent Estimators.

New in version 2.0.0.

Type Trees in this ensemble. Warning

23.3 Classification API

```
class pyspark.ml.classification.LinearSVC(featuresCol='features',           la-
                                              labelCol='label',           prediction-
                                              Col='prediction',         maxIter=100,
                                              regParam=0.0,          tol=1e-06, rawPre-
                                              dictionCol='rawPrediction',   fitIn-
                                              tercept=True, standardization=True,
                                              threshold=0.0,      weightCol=None,
                                              aggregationDepth=2)
```

Note: Experimental

Linear SVM Classifier

This binary classifier optimizes the Hinge Loss using the OWLQN optimizer. Only supports L2 regularization currently.

```
>>> from pyspark.sql import Row
>>> from pyspark.ml.linalg import Vectors
>>> df = sc.parallelize([
...     Row(label=1.0, features=Vectors.dense(1.0, 1.0, 1.0)),
...     Row(label=0.0, features=Vectors.dense(1.0, 2.0, 3.0))]).toDF()
>>> svm = LinearSVC(maxIter=5, regParam=0.01)
>>> model = svm.fit(df)
>>> model.coefficients
DenseVector([0.0, -0.2792, -0.1833])
>>> model.intercept
1.0206118982229047
>>> model.numClasses
2
>>> model.numFeatures
3
>>> test0 = sc.parallelize([Row(features=Vectors.dense(-1.0, -1.0, -1.
...     0))]).toDF()
```

(continues on next page)

(continued from previous page)

```
>>> result = model.transform(test0).head()
>>> result.prediction
1.0
>>> result.rawPrediction
DenseVector([-1.4831, 1.4831])
>>> svm_path = temp_path + "/svm"
>>> svm.save(svm_path)
>>> svm2 = LinearSVC.load(svm_path)
>>> svm2.getMaxIter()
5
>>> model_path = temp_path + "/svm_model"
>>> model.save(model_path)
>>> model2 = LinearSVCModel.load(model_path)
>>> model.coefficients[0] == model2.coefficients[0]
True
>>> model.intercept == model2.intercept
True
```

New in version 2.2.0.

setParams (*featuresCol*=’*features*’, *labelCol*=’*label*’, *predictionCol*=’*prediction*’, *maxIter*=100, *regParam*=0.0, *tol*=1e-06, *rawPredictionCol*=’*rawPrediction*’, *fitIntercept*=True, *standardization*=True, *threshold*=0.0, *weightCol*=None, *aggregationDepth*=2)
setParams(self, featuresCol=”features”, labelCol=”label”, predictionCol=”prediction”, maxIter=100, regParam=0.0, tol=1e-6, rawPredictionCol=”rawPrediction”, fitIntercept=True, standardization=True, threshold=0.0, weightCol=None, aggregationDepth=2): Sets params for Linear SVM Classifier.

New in version 2.2.0.

class pyspark.ml.classification.**LinearSVCModel** (*java_model*=None)

Note: Experimental

Model fitted by LinearSVC.

New in version 2.2.0.

coefficients

Model coefficients of Linear SVM Classifier.

New in version 2.2.0.

intercept

Model intercept of Linear SVM Classifier.

New in version 2.2.0.

```
class pyspark.ml.classification.LogisticRegression(featuresCol='features',
                                                    labelCol='label',
                                                    prediction-
                                                    Col='prediction',
                                                    maxIter=100,      reg-
Param=0.0, elasticNet-
Param=0.0, tol=1e-06,
fitIntercept=True,
threshold=0.5, thresh-
olds=None, probabili-
tyCol='probability',
rawPrediction-
Col='rawPrediction',
standardization=True,
weightCol=None, ag-
gregationDepth=2,fam-
ily='auto',lowerBound-
sOnCoefficients=None,
upperBoundsOn-
Coefficients=None,
lowerBoundsOn-
Intercepts=None,
upperBoundsOnInter-
cepts=None)
```

Logistic regression. This class supports multinomial logistic (softmax) and binomial logistic regression.

```
>>> from pyspark.sql import Row
>>> from pyspark.ml.linalg import Vectors
>>> bdf = sc.parallelize([
...     Row(label=1.0, weight=1.0, features=Vectors.dense(0.0, 5.0)),
...     Row(label=0.0, weight=2.0, features=Vectors.dense(1.0, 2.0)),
...     Row(label=1.0, weight=3.0, features=Vectors.dense(2.0, 1.0)),
...     Row(label=0.0, weight=4.0, features=Vectors.dense(3.0, 3.0))].
˓→toDF()
>>> blor = LogisticRegression(regParam=0.01, weightCol="weight")
>>> blorModel = blor.fit(bdf)
>>> blorModel.coefficients
DenseVector([-1.080..., -0.646...])
>>> blorModel.intercept
3.112...
>>> data_path = "data/mllib/sample_multiclass_classification_data.txt"
>>> mdf = spark.read.format("libsvm").load(data_path)
>>> mlor = LogisticRegression(regParam=0.1, elasticNetParam=1.0, family=
˓→"multinomial")
>>> mlorModel = mlor.fit(mdf)
>>> mlorModel.coefficientMatrix
SparseMatrix(3, 4, [0, 1, 2, 3], [3, 2, 1], [1.87..., -2.75..., -0.50...
˓→], 1)
>>> mlorModel.interceptVector
```

(continues on next page)

(continued from previous page)

```

DenseVector([0.04..., -0.42..., 0.37...])
>>> test0 = sc.parallelize([Row(features=Vectors.dense(-1.0, 1.0))]) .
    <--toDF()
>>> result = blorModel.transform(test0).head()
>>> result.prediction
1.0
>>> result.probability
DenseVector([0.02..., 0.97...])
>>> result.rawPrediction
DenseVector([-3.54..., 3.54...])
>>> test1 = sc.parallelize([Row(features=Vectors.sparse(2, [0], [1.
    <--0]))]).toDF()
>>> blorModel.transform(test1).head().prediction
1.0
>>> blor.setParams("vector")
Traceback (most recent call last):
...
TypeError: Method setParams forces keyword arguments.
>>> lr_path = temp_path + "/lr"
>>> blor.save(lr_path)
>>> lr2 = LogisticRegression.load(lr_path)
>>> lr2.getRegParam()
0.01
>>> model_path = temp_path + "/lr_model"
>>> blorModel.save(model_path)
>>> model2 = LogisticRegressionModel.load(model_path)
>>> blorModel.coefficients[0] == model2.coefficients[0]
True
>>> blorModel.intercept == model2.intercept
True
>>> model2
LogisticRegressionModel: uid = ..., numClasses = 2, numFeatures = 2

```

New in version 1.3.0.

getFamily()

Gets the value of `family` or its default value.

New in version 2.1.0.

getLowerBoundsOnCoefficients()

Gets the value of `lowerBoundsOnCoefficients`

New in version 2.3.0.

getLowerBoundsOnIntercepts()

Gets the value of `lowerBoundsOnIntercepts`

New in version 2.3.0.

getThreshold()

Get threshold for binary classification.

If `thresholds` is set with length 2 (i.e., binary classification), this returns the equivalent

threshold: $\frac{1}{1 + \frac{\text{thresholds}(0)}{\text{thresholds}(1)}}.$ Otherwise, returns threshold if set or its default value if unset.

New in version 1.4.0.

getThresholds()

If thresholds is set, return its value. Otherwise, if threshold is set, return the equivalent thresholds for binary classification: (1-threshold, threshold). If neither are set, throw an error.

New in version 1.5.0.

getUpperBoundsOnCoefficients()

Gets the value of upperBoundsOnCoefficients

New in version 2.3.0.

getUpperBoundsOnIntercepts()

Gets the value of upperBoundsOnIntercepts

New in version 2.3.0.

setFamily(*value*)

Sets the value of family.

New in version 2.1.0.

setLowerBoundsOnCoefficients(*value*)

Sets the value of lowerBoundsOnCoefficients

New in version 2.3.0.

setLowerBoundsOnIntercepts(*value*)

Sets the value of lowerBoundsOnIntercepts

New in version 2.3.0.

setParams(*featuresCol='features'*, *labelCol='label'*, *predictionCol='prediction'*, *maxIter=100*, *regParam=0.0*, *elasticNetParam=0.0*, *tol=1e-06*, *fitIntercept=True*, *threshold=0.5*, *thresholds=None*, *probabilityCol='probability'*, *rawPredictionCol='rawPrediction'*, *standardization=True*, *weightCol=None*, *aggregationDepth=2*, *family='auto'*, *lowerBoundsOnCoefficients=None*, *upperBoundsOnCoefficients=None*, *lowerBoundsOnIntercepts=None*, *upperBoundsOnIntercepts=None*)

setParams(self, featuresCol="features", labelCol="label", predictionCol="prediction", maxIter=100, regParam=0.0, elasticNetParam=0.0, tol=1e-6, fitIntercept=True, threshold=0.5, thresholds=None, probabilityCol="probability", rawPredictionCol="rawPrediction", standardization=True, weightCol=None, aggregationDepth=2, family="auto", lowerBoundsOnCoefficients=None, upperBoundsOnCoefficients=None, lowerBoundsOnIntercepts=None, upperBoundsOnIntercepts=None): Sets params for logistic regression. If the threshold and thresholds Params are both set, they must be equivalent.

New in version 1.3.0.

setThreshold(*value*)

Sets the value of threshold. Clears value of thresholds if it has been set.

New in version 1.4.0.

setThresholds (*value*)
Sets the value of thresholds. Clears value of threshold if it has been set.
New in version 1.5.0.

setUpUpperBoundsOnCoefficients (*value*)
Sets the value of upperBoundsOnCoefficients
New in version 2.3.0.

setUpUpperBoundsOnIntercepts (*value*)
Sets the value of upperBoundsOnIntercepts
New in version 2.3.0.

class pyspark.ml.classification.LogisticRegressionModel (*java_model=None*)
Model fitted by LogisticRegression.
New in version 1.3.0.

coefficientMatrix
Model coefficients.
New in version 2.1.0.

coefficients
Model coefficients of binomial logistic regression. An exception is thrown in the case of multinomial logistic regression.
New in version 2.0.0.

evaluate (*dataset*)
Evaluates the model on a test dataset.
Parameters **dataset** – Test dataset to evaluate model on, where dataset is an instance of pyspark.sql.DataFrame
New in version 2.0.0.

hasSummary
Indicates whether a training summary exists for this model instance.
New in version 2.0.0.

intercept
Model intercept of binomial logistic regression. An exception is thrown in the case of multinomial logistic regression.
New in version 1.4.0.

interceptVector
Model intercept.
New in version 2.1.0.

summary
Gets summary (e.g. accuracy/precision/recall, objective history, total iterations) of model trained on the training set. An exception is thrown if *trainingSummaryisNone*.

New in version 2.0.0.

```
class pyspark.ml.classification.LogisticRegressionSummary(java_obj=None)
```

Note: Experimental

Abstraction for Logistic Regression Results for a given model.

New in version 2.0.0.

accuracy

Returns accuracy. (equals to the total number of correctly classified instances out of the total number of instances.)

New in version 2.3.0.

fMeasureByLabel (*beta=1.0*)

Returns f-measure for each label (category).

New in version 2.3.0.

falsePositiveRateByLabel

Returns false positive rate for each label (category).

New in version 2.3.0.

featuresCol

Field in “predictions” which gives the features of each instance as a vector.

New in version 2.0.0.

labelCol

Field in “predictions” which gives the true label of each instance.

New in version 2.0.0.

labels

Returns the sequence of labels in ascending order. This order matches the order used in metrics which are specified as arrays over labels, e.g., truePositiveRateByLabel.

Note: In most cases, it will be values {0.0, 1.0, ..., numClasses-1}, However, if the training set is missing a label, then all of the arrays over labels (e.g., from truePositiveRateByLabel) will be of length numClasses-1 instead of the expected numClasses.

New in version 2.3.0.

precisionByLabel

Returns precision for each label (category).

New in version 2.3.0.

predictionCol

Field in “predictions” which gives the prediction of each class.

New in version 2.3.0.

predictions

Dataframe outputted by the model's *transform* method.

New in version 2.0.0.

probabilityCol

Field in "predictions" which gives the probability of each class as a vector.

New in version 2.0.0.

recallByLabel

Returns recall for each label (category).

New in version 2.3.0.

truePositiveRateByLabel

Returns true positive rate for each label (category).

New in version 2.3.0.

weightedFMeasure (*beta=1.0*)

Returns weighted averaged f-measure.

New in version 2.3.0.

weightedFalsePositiveRate

Returns weighted false positive rate.

New in version 2.3.0.

weightedPrecision

Returns weighted averaged precision.

New in version 2.3.0.

weightedRecall

Returns weighted averaged recall. (equals to precision, recall and f-measure)

New in version 2.3.0.

weightedTruePositiveRate

Returns weighted true positive rate. (equals to precision, recall and f-measure)

New in version 2.3.0.

class pyspark.ml.classification.LogisticRegressionTrainingSummary (*java_obj=None*)

Note: Experimental

Abstraction for multinomial Logistic Regression Training results. Currently, the training summary ignores the training weights except for the objective trace.

New in version 2.0.0.

objectiveHistory

Objective function (scaled loss + regularization) at each iteration.

New in version 2.0.0.

totalIterations

Number of training iterations until termination.

New in version 2.0.0.

```
class pyspark.ml.classification.BinaryLogisticRegressionSummary(java_obj=None)
```

Note: Experimental

Binary Logistic regression results for a given model.

New in version 2.0.0.

areaUnderROC

Computes the area under the receiver operating characteristic (ROC) curve.

Note: This ignores instance weights (setting all to 1.0) from *LogisticRegression.weightCol*. This will change in later Spark versions.

New in version 2.0.0.

fMeasureByThreshold

Returns a Dataframe with two fields (threshold, F-Measure) curve with beta = 1.0.

Note: This ignores instance weights (setting all to 1.0) from *LogisticRegression.weightCol*. This will change in later Spark versions.

New in version 2.0.0.

pr

Returns the precision-recall curve, which is a Dataframe containing two fields recall, precision with (0.0, 1.0) prepended to it.

Note: This ignores instance weights (setting all to 1.0) from *LogisticRegression.weightCol*. This will change in later Spark versions.

New in version 2.0.0.

precisionByThreshold

Returns a Dataframe with two fields (threshold, precision) curve. Every possible probability obtained in transforming the dataset are used as thresholds used in calculating the precision.

Note: This ignores instance weights (setting all to 1.0) from *LogisticRegression.weightCol*.

This will change in later Spark versions.

New in version 2.0.0.

recallByThreshold

Returns a dataframe with two fields (threshold, recall) curve. Every possible probability obtained in transforming the dataset are used as thresholds used in calculating the recall.

Note: This ignores instance weights (setting all to 1.0) from *LogisticRegression.weightCol*. This will change in later Spark versions.

New in version 2.0.0.

roc

Returns the receiver operating characteristic (ROC) curve, which is a Dataframe having two fields (FPR, TPR) with (0.0, 0.0) prepended and (1.0, 1.0) appended to it.

See also:

[Wikipedia reference](#)

Note: This ignores instance weights (setting all to 1.0) from *LogisticRegression.weightCol*. This will change in later Spark versions.

New in version 2.0.0.

class pyspark.ml.classification.**BinaryLogisticRegressionTrainingSummary** (*java_obj=None*)

Note: Experimental

Binary Logistic regression training results for a given model.

New in version 2.0.0.

```
class pyspark.ml.classification.DecisionTreeClassifier(featuresCol='features',
                                                       labelCol='label',
                                                       prediction-
                                                       Col='prediction',
                                                       probability-
                                                       Col='probability',
                                                       rawPrediction-
                                                       Col='rawPrediction',
                                                       maxDepth=5,
                                                       maxBins=32,
                                                       minInstances-
                                                       PerNode=1,
                                                       minInfoGain=0.0,
                                                       maxMemory-
                                                       InMB=256,
                                                       cacheN-
                                                       odelIds=False,
                                                       checkpointIn-
                                                       terval=10,    im-
                                                       purity='gini',
                                                       seed=None)
```

Decision tree learning algorithm for classification. It supports both binary and multiclass labels, as well as both continuous and categorical features.

```
>>> from pyspark.ml.linalg import Vectors
>>> from pyspark.ml.feature import StringIndexer
>>> df = spark.createDataFrame([
...     (1.0, Vectors.dense(1.0)),
...     (0.0, Vectors.sparse(1, [], []))], ["label", "features"])
>>> stringIndexer = StringIndexer(inputCol="label", outputCol="indexed")
>>> si_model = stringIndexer.fit(df)
>>> td = si_model.transform(df)
>>> dt = DecisionTreeClassifier(maxDepth=2, labelCol="indexed")
>>> model = dt.fit(td)
>>> model.numNodes
3
>>> model.depth
1
>>> model.featureImportances
SparseVector(1, {0: 1.0})
>>> model.numFeatures
1
>>> model.numClasses
2
>>> print(model.toDebugString)
DecisionTreeClassificationModel (uid=...) of depth 1 with 3 nodes...
>>> test0 = spark.createDataFrame([(Vectors.dense(-1.0),)], ["features"])
>>> result = model.transform(test0).head()
>>> result.prediction
0.0
```

(continues on next page)

(continued from previous page)

```
>>> result.probability
DenseVector([1.0, 0.0])
>>> result.rawPrediction
DenseVector([1.0, 0.0])
>>> test1 = spark.createDataFrame([(Vectors.sparse(1, [0], [1.0]),)], [←"features")]
>>> model.transform(test1).head().prediction
1.0
```

```
>>> dtc_path = temp_path + "/dtc"
>>> dt.save(dtc_path)
>>> dt2 = DecisionTreeClassifier.load(dtc_path)
>>> dt2.getMaxDepth()
2
>>> model_path = temp_path + "/dtc_model"
>>> model.save(model_path)
>>> model2 = DecisionTreeClassificationModel.load(model_path)
>>> model.featureImportances == model2.featureImportances
True
```

New in version 1.4.0.

setParams (*self*, *featuresCol*=“*features*”, *labelCol*=“*label*”, *predictionCol*=“*prediction*”, *probabilityCol*=“*probability*”, *rawPredictionCol*=“*rawPrediction*”, *maxDepth*=5, *maxBins*=32, *minInstancesPerNode*=1, *minInfoGain*=0.0, *maxMemoryInMB*=256, *cacheNodeIds*=False, *checkpointInterval*=10, *impu-*
rity=“*gini*”, *seed*=None)

Sets params for the DecisionTreeClassifier.

New in version 1.4.0.

class pyspark.ml.classification.DecisionTreeClassificationModel (*java_model*=None)
 Model fitted by DecisionTreeClassifier.

New in version 1.4.0.

featureImportances

Estimate of the importance of each feature.

This generalizes the idea of “Gini” importance to other losses, following the explanation of Gini importance from “Random Forests” documentation by Leo Breiman and Adele Cutler, and following the implementation from scikit-learn.

This feature importance is calculated as follows:

- $\text{importance}(\text{feature } j) = \sum (\text{over nodes which split on feature } j) \text{ of the gain, where gain is scaled by the number of instances passing through node}$
- Normalize importances for tree to sum to 1.

Note: Feature importance for single decision trees can have high variance due to correlated predictor variables. Consider using a *RandomForestClassifier* to determine feature im-

portance instead.

New in version 2.0.0.

```
class pyspark.ml.classification.GBTClassifier(featuresCol='features',
                                                labelCol='label',          predictionCol='prediction',
                                                maxDepth=5,    maxBins=32,
                                                minInstancesPerNode=1,
                                                minInfoGain=0.0,   maxMemoryInMB=256,
                                                cacheNodeIds=False,   checkpointInterval=10,
                                                lossType='logistic',
                                                maxIter=20,      stepSize=0.1,
                                                seed=None,       subsamplingRate=1.0,
                                                featureSubsetStrategy='all')
```

Gradient-Boosted Trees (GBTs) learning algorithm for classification. It supports binary labels, as well as both continuous and categorical features.

The implementation is based upon: J.H. Friedman. “Stochastic Gradient Boosting.” 1999.

Notes on Gradient Boosting vs. TreeBoost: - This implementation is for Stochastic Gradient Boosting, not for TreeBoost. - Both algorithms learn tree ensembles by minimizing loss functions. - TreeBoost (Friedman, 1999) additionally modifies the outputs at tree leaf nodes based on the loss function, whereas the original gradient boosting method does not. - We expect to implement TreeBoost in the future: [SPARK-4240](#)

Note: Multiclass labels are not currently supported.

```
>>> from numpy import allclose
>>> from pyspark.ml.linalg import Vectors
>>> from pyspark.ml.feature import StringIndexer
>>> df = spark.createDataFrame([
...     (1.0, Vectors.dense(1.0)),
...     (0.0, Vectors.sparse(1, [], []))], ["label", "features"])
>>> stringIndexer = StringIndexer(inputCol="label", outputCol="indexed")
>>> si_model = stringIndexer.fit(df)
>>> td = si_model.transform(df)
>>> gbt = GBTClassifier(maxIter=5, maxDepth=2, labelCol="indexed", 
  ↳seed=42)
>>> gbt.getFeatureSubsetStrategy()
'all'
>>> model = gbt.fit(td)
>>> model.featureImportances
SparseVector(1, {0: 1.0})
>>> allclose(model.treeWeights, [1.0, 0.1, 0.1, 0.1, 0.1])
True
>>> test0 = spark.createDataFrame([(Vectors.dense(-1.0),)], ["features"])
```

(continues on next page)

(continued from previous page)

```

>>> model.transform(test0).head().prediction
0.0
>>> test1 = spark.createDataFrame([(Vectors.sparse(1, [0], [1.0]),)], [
    "features"])
>>> model.transform(test1).head().prediction
1.0
>>> model.totalNumNodes
15
>>> print(model.toDebugString)
GBTClassificationModel (uid=...) ...with 5 trees...
>>> gbtc_path = temp_path + "gbtc"
>>> gbt.save(gbtc_path)
>>> gbt2 = GBTClassifier.load(gbtc_path)
>>> gbt2.getMaxDepth()
2
>>> model_path = temp_path + "gbtc_model"
>>> model.save(model_path)
>>> model2 = GBTClassificationModel.load(model_path)
>>> model.featureImportances == model2.featureImportances
True
>>> model.treeWeights == model2.treeWeights
True
>>> model.trees
[DecisionTreeRegressionModel (uid=...) of depth..., ]
>>> validation = spark.createDataFrame([(0.0, Vectors.dense(-1.0),)],
    ["indexed", "features"])
>>> model.evaluateEachIteration(validation)
[0.25..., 0.23..., 0.21..., 0.19..., 0.18...]
>>> model.numClasses
2

```

New in version 1.4.0.

getLossType()

Gets the value of lossType or its default value.

New in version 1.4.0.

setFeatureSubsetStrategy(value)

Sets the value of featureSubsetStrategy.

New in version 2.4.0.

setLossType(value)

Sets the value of lossType.

New in version 1.4.0.

setParams(self, featuresCol="features", labelCol="label", predictionCol="prediction", maxDepth=5, maxBins=32, minInstancesPerNode=1, minInfoGain=0.0, maxMemoryInMB=256, cacheNodeIds=False, checkpointInterval=10, lossType="logistic", maxIter=20, stepSize=0.1, seed=None, subsamplingRate=1.0, featureSubsetStrategy="all")

Sets params for Gradient Boosted Tree Classification.

New in version 1.4.0.

class pyspark.ml.classification.**GBTClassificationModel** (*java_model=None*)
Model fitted by GBTClassifier.

New in version 1.4.0.

evaluateEachIteration (*dataset*)

Method to compute error or loss for every iteration of gradient boosting.

Parameters **dataset** – Test dataset to evaluate model on, where dataset is an instance of pyspark.sql.DataFrame

New in version 2.4.0.

featureImportances

Estimate of the importance of each feature.

Each feature's importance is the average of its importance across all trees in the ensemble. The importance vector is normalized to sum to 1. This method is suggested by Hastie et al. (Hastie, Tibshirani, Friedman. “The Elements of Statistical Learning, 2nd Edition.” 2001.) and follows the implementation from scikit-learn.

See also:

DecisionTreeClassificationModel.featureImportances

New in version 2.0.0.

trees

These have null parent Estimators.

New in version 2.0.0.

Type Trees in this ensemble. Warning

```
class pyspark.ml.classification.RandomForestClassifier(featuresCol='features',
                                                       labelCol='label',
                                                       prediction-
                                                       Col='prediction',
                                                       probability-
                                                       Col='probability',
                                                       rawPrediction-
                                                       Col='rawPrediction',
                                                       maxDepth=5,
                                                       maxBins=32,
                                                       minInstances-
                                                       PerNode=1,
                                                       minInfoGain=0.0,
                                                       maxMemory-
                                                       InMB=256,
                                                       cacheN-
                                                       odeIds=False,
                                                       checkpointIn-
                                                       terval=10,    im-
                                                       purity='gini',
                                                       numTrees=20,
                                                       featureSubset-
                                                       Strategy='auto',
                                                       seed=None,
                                                       subsamplin-
                                                       gRate=1.0)
```

Random Forest learning algorithm for classification. It supports both binary and multiclass labels, as well as both continuous and categorical features.

```
>>> import numpy
>>> from numpy import allclose
>>> from pyspark.ml.linalg import Vectors
>>> from pyspark.ml.feature import StringIndexer
>>> df = spark.createDataFrame([
...     (1.0, Vectors.dense(1.0)),
...     (0.0, Vectors.sparse(1, [], []))], ["label", "features"])
>>> stringIndexer = StringIndexer(inputCol="label", outputCol="indexed")
>>> si_model = stringIndexer.fit(df)
>>> td = si_model.transform(df)
>>> rf = RandomForestClassifier(numTrees=3, maxDepth=2, labelCol="indexed"
->, seed=42)
>>> model = rf.fit(td)
>>> model.featureImportances
SparseVector(1, {0: 1.0})
>>> allclose(model.treeWeights, [1.0, 1.0, 1.0])
True
>>> test0 = spark.createDataFrame([(Vectors.dense(-1.0),)], ["features"])
>>> result = model.transform(test0).head()
>>> result.prediction
0.0
```

(continues on next page)

(continued from previous page)

```
>>> numpy.argmax(result.probability)
0
>>> numpy.argmax(result.rawPrediction)
0
>>> test1 = spark.createDataFrame([(Vectors.sparse(1, [0], [1.0])),], [←"features"])
>>> model.transform(test1).head().prediction
1.0
>>> model.trees
[DecisionTreeClassificationModel (uid=...) of depth..., ↵DecisionTreeClassificationModel...]
>>> rfc_path = temp_path + "/rfc"
>>> rf.save(rfc_path)
>>> rf2 = RandomForestClassifier.load(rfc_path)
>>> rf2.getNumTrees()
3
>>> model_path = temp_path + "/rfc_model"
>>> model.save(model_path)
>>> model2 = RandomForestClassificationModel.load(model_path)
>>> model.featureImportances == model2.featureImportances
True
```

New in version 1.4.0.

setFeatureSubsetStrategy (*value*)

Sets the value of `featureSubsetStrategy`.

New in version 2.4.0.

```
setParams (self, featuresCol="features", labelCol="label", predictionCol="prediction",
            probabilityCol="probability", rawPredictionCol="rawPrediction",
            maxDepth=5, maxBins=32, minInstancesPerNode=1, minInfoGain=0.0,
            maxMemoryInMB=256, cacheNodeIds=False, checkpointInterval=10,
            seed=None, impurity="gini", numTrees=20, featureSubsetStrategy="auto",
            subsamplingRate=1.0)
```

Sets params for linear classification.

New in version 1.4.0.

```
class pyspark.ml.classification.RandomForestClassificationModel (java_model=None)
```

Model fitted by `RandomForestClassifier`.

New in version 1.4.0.

featureImportances

Estimate of the importance of each feature.

Each feature's importance is the average of its importance across all trees in the ensemble. The importance vector is normalized to sum to 1. This method is suggested by Hastie et al. (Hastie, Tibshirani, Friedman. “The Elements of Statistical Learning, 2nd Edition.” 2001.) and follows the implementation from scikit-learn.

See also:

DecisionTreeClassificationModel.featureImportances

New in version 2.0.0.

trees

These have null parent Estimators.

New in version 2.0.0.

Type Trees in this ensemble. Warning

```
class pyspark.ml.classification.NaiveBayes(featuresCol='features',           labelCol='label',           predictionCol='prediction',           probabilityCol='probability',           rawPredictionCol='rawPrediction',           smoothing=1.0,           modelType='multinomial',           thresholds=None,           weightCol=None)
```

Naive Bayes Classifiers. It supports both Multinomial and Bernoulli NB. **Multinomial NB** can handle finitely supported discrete data. For example, by converting documents into TF-IDF vectors, it can be used for document classification. By making every vector a binary (0/1) data, it can also be used as Bernoulli NB. The input feature values must be nonnegative.

```
>>> from pyspark.sql import Row
>>> from pyspark.ml.linalg import Vectors
>>> df = spark.createDataFrame([
...     Row(label=0.0, weight=0.1, features=Vectors.dense([0.0, 0.0])),
...     Row(label=0.0, weight=0.5, features=Vectors.dense([0.0, 1.0])),
...     Row(label=1.0, weight=1.0, features=Vectors.dense([1.0, 0.0]))])
>>> nb = NaiveBayes(smoothing=1.0, modelType="multinomial", weightCol=
-> "weight")
>>> model = nb.fit(df)
>>> model.pi
DenseVector([-0.81..., -0.58...])
>>> model.theta
DenseMatrix(2, 2, [-0.91..., -0.51..., -0.40..., -1.09...], 1)
>>> test0 = sc.parallelize([Row(features=Vectors.dense([1.0, 0.0]))]).\
->toDF()
>>> result = model.transform(test0).head()
>>> result.prediction
1.0
>>> result.probability
DenseVector([0.32..., 0.67...])
>>> result.rawPrediction
DenseVector([-1.72..., -0.99...])
>>> test1 = sc.parallelize([Row(features=Vectors.sparse(2, [0], [1.
->0]))]).toDF()
>>> model.transform(test1).head().prediction
1.0
>>> nb_path = temp_path + "/nb"
>>> nb.save(nb_path)
>>> nb2 = NaiveBayes.load(nb_path)
```

(continues on next page)

(continued from previous page)

```
>>> nb2.getSmoothing()
1.0
>>> model_path = temp_path + "/nb_model"
>>> model.save(model_path)
>>> model2 = NaiveBayesModel.load(model_path)
>>> model.pi == model2.pi
True
>>> model.theta == model2.theta
True
>>> nb = nb.setThresholds([0.01, 10.00])
>>> model3 = nb.fit(df)
>>> result = model3.transform(test0).head()
>>> result.prediction
0.0
```

New in version 1.5.0.

getModelType()

Gets the value of modelType or its default value.

New in version 1.5.0.

getSmoothing()

Gets the value of smoothing or its default value.

New in version 1.5.0.

setModelType(*value*)

Sets the value of modelType.

New in version 1.5.0.

setParams(*self*, *featuresCol*="features", *labelCol*="label", *predictionCol*="prediction", *probabilityCol*="probability", *rawPredictionCol*="rawPrediction", *smoothing*=1.0, *modelType*="multinomial", *thresholds*=None, *weightCol*=None)

Sets params for Naive Bayes.

New in version 1.5.0.

setSmoothing(*value*)

Sets the value of smoothing.

New in version 1.5.0.

class pyspark.ml.classification.NaiveBayesModel (java_model=None)

Model fitted by NaiveBayes.

New in version 1.5.0.

pi

log of class priors.

New in version 2.0.0.

theta

log of class conditional probabilities.

New in version 2.0.0.

```
class pyspark.ml.classification.MultilayerPerceptronClassifier(featuresCol='features',
                                                               label-
                                                               Col='label',
                                                               pre-
                                                               dic-
                                                               tion-
                                                               Col='prediction',
                                                               max-
                                                               Iter=100,
                                                               tol=1e-
                                                               06,
                                                               seed=None,
                                                               lay-
                                                               ers=None,
                                                               block-
                                                               Size=128,
                                                               step-
                                                               Size=0.03,
                                                               solver='l-
                                                               bfgs',
                                                               ini-
                                                               tial-
                                                               Weights=None,
                                                               prob-
                                                               abil-
                                                               ity-
                                                               Col='probability',
                                                               raw-
                                                               Pre-
                                                               dic-
                                                               tion-
                                                               Col='rawPrediction')
```

Classifier trainer based on the Multilayer Perceptron. Each layer has sigmoid activation function, output layer has softmax. Number of inputs has to be equal to the size of feature vectors. Number of outputs has to be equal to the total number of labels.

```
>>> from pyspark.ml.linalg import Vectors
>>> df = spark.createDataFrame([
...     (0.0, Vectors.dense([0.0, 0.0])),
...     (1.0, Vectors.dense([0.0, 1.0])),
...     (1.0, Vectors.dense([1.0, 0.0])),
...     (0.0, Vectors.dense([1.0, 1.0])), ["label", "features"])
>>> mlp = MultilayerPerceptronClassifier(maxIter=100, layers=[2, 2, 2],_
    ↴blockSize=1, seed=123)
>>> model = mlp.fit(df)
>>> model.layers
[2, 2, 2]
```

(continues on next page)

(continued from previous page)

```
>>> model.weights.size
12
>>> testDF = spark.createDataFrame([
...     (Vectors.dense([1.0, 0.0]),),
...     (Vectors.dense([0.0, 0.0]),)], ["features"])
>>> model.transform(testDF).select("features", "prediction").show()
+-----+-----+
| features|prediction|
+-----+-----+
|[1.0,0.0]|      1.0|
|[0.0,0.0]|      0.0|
+-----+-----+
...
>>> mlp_path = temp_path + "/mlp"
>>> mlp.save(mlp_path)
>>> mlp2 = MultilayerPerceptronClassifier.load(mlp_path)
>>> mlp2.getBlockSize()
1
>>> model_path = temp_path + "/mlp_model"
>>> model.save(model_path)
>>> model2 = MultilayerPerceptronClassificationModel.load(model_path)
>>> model.layers == model2.layers
True
>>> model.weights == model2.weights
True
>>> mlp2 = mlp2.setInitialWeights(list(range(0, 12)))
>>> model3 = mlp2.fit(df)
>>> model3.weights != model2.weights
True
>>> model3.layers == model.layers
True
```

New in version 1.6.0.

getBlockSize()

Gets the value of blockSize or its default value.

New in version 1.6.0.

getInitialWeights()

Gets the value of initialWeights or its default value.

New in version 2.0.0.

getLayers()

Gets the value of layers or its default value.

New in version 1.6.0.

getStepSize()

Gets the value of stepSize or its default value.

New in version 2.0.0.

setBlockSize (value)
Sets the value of blockSize.
New in version 1.6.0.

setInitialWeights (value)
Sets the value of initialWeights.
New in version 2.0.0.

setLayers (value)
Sets the value of layers.
New in version 1.6.0.

setParams (featuresCol='features', labelCol='label', predictionCol='prediction', maxIter=100, tol=1e-06, seed=None, layers=None, blockSize=128, stepSize=0.03, solver='l-bfgs', initialWeights=None, probabilityCol='probability', rawPredictionCol='rawPrediction')
setParams(self, featuresCol="features", labelCol="label", predictionCol="prediction", maxIter=100, tol=1e-6, seed=None, layers=None, blockSize=128, stepSize=0.03, solver="l-bfgs", initialWeights=None, probabilityCol="probability", rawPredictionCol="rawPrediction"): Sets params for MultilayerPerceptronClassifier.
New in version 1.6.0.

setStepSize (value)
Sets the value of stepSize.
New in version 2.0.0.

class pyspark.ml.classification.MultilayerPerceptronClassificationModel (java_model=No
Model fitted by MultilayerPerceptronClassifier.
New in version 1.6.0.

layers
array of layer sizes including input and output layers.
New in version 1.6.0.

weights
the weights of layers.
New in version 2.0.0.

class pyspark.ml.classification.OneVsRest (featuresCol='features', labelCol='label', predictionCol='prediction', classifier=None, weightCol=None, parallelism=1)

Note: Experimental

Reduction of Multiclass Classification to Binary Classification. Performs reduction using one against all strategy. For a multiclass classification with k classes, train k models (one per class). Each example is scored against all k models and the model with highest score is picked to label the example.

```
>>> from pyspark.sql import Row
>>> from pyspark.ml.linalg import Vectors
>>> data_path = "data/mllib/sample_multiclass_classification_data.txt"
>>> df = spark.read.format("libsvm").load(data_path)
>>> lr = LogisticRegression(regParam=0.01)
>>> ovr = OneVsRest(classifier=lr)
>>> model = ovr.fit(df)
>>> model.models[0].coefficients
DenseVector([0.5..., -1.0..., 3.4..., 4.2...])
>>> model.models[1].coefficients
DenseVector([-2.1..., 3.1..., -2.6..., -2.3...])
>>> model.models[2].coefficients
DenseVector([0.3..., -3.4..., 1.0..., -1.1...])
>>> [x.intercept for x in model.models]
[-2.7..., -2.5..., -1.3...]
>>> test0 = sc.parallelize([Row(features=Vectors.dense(-1.0, 0.0, 1.0, 1.0))]).toDF()
>>> model.transform(test0).head().prediction
0.0
>>> test1 = sc.parallelize([Row(features=Vectors.sparse(4, [0], [1.0]))]).toDF()
>>> model.transform(test1).head().prediction
2.0
>>> test2 = sc.parallelize([Row(features=Vectors.dense(0.5, 0.4, 0.3, 0.2))]).toDF()
>>> model.transform(test2).head().prediction
0.0
>>> model_path = temp_path + "/ovr_model"
>>> model.save(model_path)
>>> model2 = OneVsRestModel.load(model_path)
>>> model2.transform(test0).head().prediction
0.0
```

New in version 2.0.0.

copy(*extra=None*)

Creates a copy of this instance with a randomly generated uid and some extra params. This creates a deep copy of the embedded paramMap, and copies the embedded and extra parameters over.

Parameters **extra** – Extra parameters to copy to the new instance

Returns Copy of this instance

New in version 2.0.0.

```
setParams(featuresCol='features', labelCol='label', predictionCol='prediction', classifier=None, weightCol=None, parallelism=1)
setParams(self, featuresCol="features", labelCol="label", predictionCol="prediction", classifier=None, weightCol=None, parallelism=1): Sets params for OneVsRest.
```

New in version 2.0.0.

```
class pyspark.ml.classification.OneVsRestModel (models)
```

Note: Experimental

Model fitted by OneVsRest. This stores the models resulting from training k binary classifiers: one for each class. Each example is scored against all k models, and the model with the highest score is picked to label the example.

New in version 2.0.0.

copy (*extra=None*)

Creates a copy of this instance with a randomly generated uid and some extra params. This creates a deep copy of the embedded paramMap, and copies the embedded and extra parameters over.

Parameters **extra** – Extra parameters to copy to the new instance

Returns Copy of this instance

New in version 2.0.0.

23.4 Clustering API

```
class pyspark.ml.clustering.BisectingKMeans (featuresCol='features', predictionCol='prediction', maxIter=20,  
seed=None, k=4, minDivisibleClusterSize=1.0, distanceMeasure='euclidean')
```

A bisecting k-means algorithm based on the paper “A comparison of document clustering techniques” by Steinbach, Karypis, and Kumar, with modification to fit Spark. The algorithm starts from a single cluster that contains all points. Iteratively it finds divisible clusters on the bottom level and bisects each of them using k-means, until there are k leaf clusters in total or no leaf clusters are divisible. The bisecting steps of clusters on the same level are grouped together to increase parallelism. If bisecting all divisible clusters on the bottom level would result more than k leaf clusters, larger clusters get higher priority.

```
>>> from pyspark.ml.linalg import Vectors
>>> data = [(Vectors.dense([0.0, 0.0])), (Vectors.dense([1.0, 1.0])), ...
...           (Vectors.dense([9.0, 8.0])), (Vectors.dense([8.0, 9.0]))]
>>> df = spark.createDataFrame(data, ["features"])
>>> bkm = BisectingKMeans(k=2, minDivisibleClusterSize=1.0)
>>> model = bkm.fit(df)
>>> centers = model.clusterCenters()
>>> len(centers)
2
>>> model.computeCost(df)
```

(continues on next page)

(continued from previous page)

```
2.000...
>>> model.hasSummary
True
>>> summary = model.summary
>>> summary.k
2
>>> summary.clusterSizes
[2, 2]
>>> transformed = model.transform(df).select("features", "prediction")
>>> rows = transformed.collect()
>>> rows[0].prediction == rows[1].prediction
True
>>> rows[2].prediction == rows[3].prediction
True
>>> bkm_path = temp_path + "/bkm"
>>> bkm.save(bkm_path)
>>> bkm2 = BisectingKMeans.load(bkm_path)
>>> bkm2.getK()
2
>>> bkm2.getDistanceMeasure()
'euclidean'
>>> model_path = temp_path + "/bkm_model"
>>> model.save(model_path)
>>> model2 = BisectingKMeansModel.load(model_path)
>>> model2.hasSummary
False
>>> model.clusterCenters()[0] == model2.clusterCenters()[0]
array([ True,  True], dtype=bool)
>>> model.clusterCenters()[1] == model2.clusterCenters()[1]
array([ True,  True], dtype=bool)
```

New in version 2.0.0.

getDistanceMeasure()

Gets the value of *distanceMeasure* or its default value.

New in version 2.4.0.

getK()

Gets the value of *k* or its default value.

New in version 2.0.0.

getMinDivisibleClusterSize()

Gets the value of *minDivisibleClusterSize* or its default value.

New in version 2.0.0.

setDistanceMeasure(*value*)

Sets the value of *distanceMeasure*.

New in version 2.4.0.

setK(*value*)

Sets the value of k.

New in version 2.0.0.

setMinDivisibleClusterSize (*value*)

Sets the value of minDivisibleClusterSize.

New in version 2.0.0.

setParams (*self*, *featuresCol*=*"features"*, *predictionCol*=*"prediction"*, *maxIter*=20, *seed*=*None*, *k*=4, *minDivisibleClusterSize*=1.0, *distanceMeasure*=*"euclidean"*)

Sets params for BisectingKMeans.

New in version 2.0.0.

class pyspark.ml.clustering.BisectingKMeansModel (*java_model*=*None*)

Model fitted by BisectingKMeans.

New in version 2.0.0.

clusterCenters ()

Get the cluster centers, represented as a list of NumPy arrays.

New in version 2.0.0.

computeCost (*dataset*)

Computes the sum of squared distances between the input points and their corresponding cluster centers.

New in version 2.0.0.

hasSummary

Indicates whether a training summary exists for this model instance.

New in version 2.1.0.

summary

Gets summary (e.g. cluster assignments, cluster sizes) of the model trained on the training set. An exception is thrown if no summary exists.

New in version 2.1.0.

class pyspark.ml.clustering.BisectingKMeansSummary (*java_obj*=*None*)

Note: Experimental

Bisecting KMeans clustering results for a given model.

New in version 2.1.0.

class pyspark.ml.clustering.KMeans (*featuresCol*=*'features'*, *predictionCol*=*'prediction'*, *k*=2, *initMode*=*'k-means||'*, *initSteps*=2, *tol*=0.0001, *maxIter*=20, *seed*=*None*, *distanceMeasure*=*'euclidean'*)

K-means clustering with a k-means++ like initialization mode (the k-means|| algorithm by Bahmani

et al).

```
>>> from pyspark.ml.linalg import Vectors
>>> data = [(Vectors.dense([0.0, 0.0]),), (Vectors.dense([1.0, 1.0]),),
...           (Vectors.dense([9.0, 8.0]),), (Vectors.dense([8.0, 9.0]),)]
>>> df = spark.createDataFrame(data, ["features"])
>>> kmeans = KMeans(k=2, seed=1)
>>> model = kmeans.fit(df)
>>> centers = model.clusterCenters()
>>> len(centers)
2
>>> model.computeCost(df)
2.000...
>>> transformed = model.transform(df).select("features", "prediction")
>>> rows = transformed.collect()
>>> rows[0].prediction == rows[1].prediction
True
>>> rows[2].prediction == rows[3].prediction
True
>>> model.hasSummary
True
>>> summary = model.summary
>>> summary.k
2
>>> summary.clusterSizes
[2, 2]
>>> summary.trainingCost
2.000...
>>> kmeans_path = temp_path + "/kmeans"
>>> kmeans.save(kmeans_path)
>>> kmeans2 = KMeans.load(kmeans_path)
>>> kmeans2.getK()
2
>>> model_path = temp_path + "/kmeans_model"
>>> model.save(model_path)
>>> model2 = KMeansModel.load(model_path)
>>> model2.hasSummary
False
>>> model.clusterCenters()[0] == model2.clusterCenters()[0]
array([ True,  True], dtype=bool)
>>> model.clusterCenters()[1] == model2.clusterCenters()[1]
array([ True,  True], dtype=bool)
```

New in version 1.5.0.

getDistanceMeasure()

Gets the value of *distanceMeasure*

New in version 2.4.0.

getInitMode()

Gets the value of *initMode*

New in version 1.5.0.

```
getInitSteps()
    Gets the value of initSteps

    New in version 1.5.0.

getK()
    Gets the value of k

    New in version 1.5.0.

setDistanceMeasure(value)
    Sets the value of distanceMeasure.

    New in version 2.4.0.

setInitMode(value)
    Sets the value of initMode.

    New in version 1.5.0.

setInitSteps(value)
    Sets the value of initSteps.

    New in version 1.5.0.

setK(value)
    Sets the value of k.

    New in version 1.5.0.

setParams(self, featuresCol="features", predictionCol="prediction", k=2, initMode="k-means||", initSteps=2, tol=1e-4, maxIter=20, seed=None, distanceMeasure="euclidean")
    Sets params for KMeans.

    New in version 1.5.0.

class pyspark.ml.clustering.KMeansModel(java_model=None)
    Model fitted by KMeans.

    New in version 1.5.0.

clusterCenters()
    Get the cluster centers, represented as a list of NumPy arrays.

    New in version 1.5.0.

computeCost(dataset)
    Return the K-means cost (sum of squared distances of points to their nearest center) for this model on the given data.

..note:: Deprecated in 2.4.0. It will be removed in 3.0.0. Use ClusteringEvaluator instead.
    You can also get the cost on the training dataset in the summary.

    New in version 2.0.0.

hasSummary
    Indicates whether a training summary exists for this model instance.
```

New in version 2.1.0.

summary

Gets summary (e.g. cluster assignments, cluster sizes) of the model trained on the training set. An exception is thrown if no summary exists.

New in version 2.1.0.

```
class pyspark.ml.clustering.GaussianMixture(featuresCol='features', predictionCol='prediction', k=2, probabilityCol='probability', tol=0.01, maxIter=100, seed=None)
```

GaussianMixture clustering. This class performs expectation maximization for multivariate Gaussian Mixture Models (GMMs). A GMM represents a composite distribution of independent Gaussian distributions with associated “mixing” weights specifying each’s contribution to the composite.

Given a set of sample points, this class will maximize the log-likelihood for a mixture of k Gaussians, iterating until the log-likelihood changes by less than convergenceTol, or until it has reached the max number of iterations. While this process is generally guaranteed to converge, it is not guaranteed to find a global optimum.

Note: For high-dimensional data (with many features), this algorithm may perform poorly. This is due to high-dimensional data (a) making it difficult to cluster at all (based on statistical/theoretical arguments) and (b) numerical issues with Gaussian distributions.

```
>>> from pyspark.ml.linalg import Vectors
```

```
>>> data = [(Vectors.dense([-0.1, -0.05])), ,  
...           (Vectors.dense([-0.01, -0.1])), ,  
...           (Vectors.dense([0.9, 0.8])), ,  
...           (Vectors.dense([0.75, 0.935])), ,  
...           (Vectors.dense([-0.83, -0.68])), ,  
...           (Vectors.dense([-0.91, -0.76])), ]  
>>> df = spark.createDataFrame(data, ["features"])  
>>> gm = GaussianMixture(k=3, tol=0.0001,  
...                         maxIter=10, seed=10)  
>>> model = gm.fit(df)  
>>> model.hasSummary  
True  
>>> summary = model.summary  
>>> summary.k  
3  
>>> summary.clusterSizes  
[2, 2, 2]  
>>> summary.logLikelihood  
8.14636...  
>>> weights = model.weights  
>>> len(weights)  
3  
>>> model.gaussiansDF.select("mean").head()
```

(continues on next page)

(continued from previous page)

```

Row(mean=DenseVector([0.825, 0.8675]))
>>> model.gaussiansDF.select("cov").head()
Row(cov=DenseMatrix(2, 2, [0.0056, -0.0051, -0.0051, 0.0046], False))
>>> transformed = model.transform(df).select("features", "prediction")
>>> rows = transformed.collect()
>>> rows[4].prediction == rows[5].prediction
True
>>> rows[2].prediction == rows[3].prediction
True
>>> gmm_path = temp_path + "/gmm"
>>> gm.save(gmm_path)
>>> gm2 = GaussianMixture.load(gmm_path)
>>> gm2.getK()
3
>>> model_path = temp_path + "/gmm_model"
>>> model.save(model_path)
>>> model2 = GaussianMixtureModel.load(model_path)
>>> model2.hasSummary
False
>>> model2.weights == model.weights
True
>>> model2.gaussiansDF.select("mean").head()
Row(mean=DenseVector([0.825, 0.8675]))
>>> model2.gaussiansDF.select("cov").head()
Row(cov=DenseMatrix(2, 2, [0.0056, -0.0051, -0.0051, 0.0046], False))

```

New in version 2.0.0.

getK()

Gets the value of k

New in version 2.0.0.

setK(*value*)

Sets the value of k .

New in version 2.0.0.

setParams(*self*, *featuresCol*=*"features"*, *predictionCol*=*"prediction"*, *k*=2, *probabilityCol*=*"probability"*, *tol*=0.01, *maxIter*=100, *seed*=None)

Sets params for GaussianMixture.

New in version 2.0.0.

class pyspark.ml.clustering.GaussianMixtureModel(*java_model*=None)

Model fitted by GaussianMixture.

New in version 2.0.0.

gaussiansDF

Retrieve Gaussian distributions as a DataFrame. Each row represents a Gaussian Distribution. The DataFrame has two columns: mean (Vector) and cov (Matrix).

New in version 2.0.0.

hasSummary

Indicates whether a training summary exists for this model instance.

New in version 2.1.0.

summary

Gets summary (e.g. cluster assignments, cluster sizes) of the model trained on the training set. An exception is thrown if no summary exists.

New in version 2.1.0.

weights

Weight for each Gaussian distribution in the mixture. This is a multinomial probability distribution over the k Gaussians, where weights[i] is the weight for Gaussian i, and weights sum to 1.

New in version 2.0.0.

```
class pyspark.ml.clustering.GaussianMixtureSummary (java_obj=None)
```

Note: Experimental

Gaussian mixture clustering results for a given model.

New in version 2.1.0.

logLikelihood

Total log-likelihood for this model on the given data.

New in version 2.2.0.

probability

DataFrame of probabilities of each cluster for each training data point.

New in version 2.1.0.

probabilityCol

Name for column of predicted probability of each cluster in *predictions*.

New in version 2.1.0.

```
class pyspark.ml.clustering.LDA (featuresCol='features', maxIter=20, seed=None,
                                  checkpointInterval=10, k=10, optimizer='online',
                                  learningOffset=1024.0, learningDecay=0.51,
                                  subsamplingRate=0.05, optimizeDocConcen-
                                  tration=True, docConcentration=None, top-
                                  icConcentration=None, topicDistribu-
                                  tionCol='topicDistribution', keepLastCheck-
                                  point=True)
```

Latent Dirichlet Allocation (LDA), a topic model designed for text documents.

Terminology:

- “term” = “word”: an element of the vocabulary

- “token”: instance of a term appearing in a document
- “topic”: multinomial distribution over terms representing some concept
- “document”: one piece of text, corresponding to one row in the input data

Original LDA paper (journal version): Blei, Ng, and Jordan. “Latent Dirichlet Allocation.” JMLR, 2003.

Input data (featuresCol): LDA is given a collection of documents as input data, via the featuresCol parameter. Each document is specified as a Vector of length vocabSize, where each entry is the count for the corresponding term (word) in the document. Feature transformers such as pyspark.ml.feature.Tokenizer and pyspark.ml.feature.CountVectorizer can be useful for converting text to word count vectors.

```
>>> from pyspark.ml.linalg import Vectors, SparseVector
>>> from pyspark.ml.clustering import LDA
>>> df = spark.createDataFrame([[1, Vectors.dense([0.0, 1.0])],
...     [2, SparseVector(2, {0: 1.0})]], ["id", "features"])
>>> lda = LDA(k=2, seed=1, optimizer="em")
>>> model = lda.fit(df)
>>> model.isDistributed()
True
>>> localModel = model.toLocal()
>>> localModel.isDistributed()
False
>>> model.vocabSize()
2
>>> model.describeTopics().show()
+-----+-----+
|topic|termIndices|      termWeights|
+-----+-----+
|    0|[1, 0]| [0.50401530077160...|
|    1|[0, 1]| [0.50401530077160...|
+-----+-----+
...
>>> model.topicsMatrix()
DenseMatrix(2, 2, [0.496, 0.504, 0.504, 0.496], 0)
>>> lda_path = temp_path + "/lda"
>>> lda.save(lda_path)
>>> sameLDA = LDA.load(lda_path)
>>> distributed_model_path = temp_path + "/lda_distributed_model"
>>> model.save(distributed_model_path)
>>> sameModel = DistributedLDAModel.load(distributed_model_path)
>>> local_model_path = temp_path + "/lda_local_model"
>>> localModel.save(local_model_path)
>>> sameLocalModel = LocalLDAModel.load(local_model_path)
```

New in version 2.0.0.

getDocConcentration()

Gets the value of docConcentration or its default value.

New in version 2.0.0.

getK()

Gets the value of k or its default value.

New in version 2.0.0.

getKeepLastCheckpoint()

Gets the value of keepLastCheckpoint or its default value.

New in version 2.0.0.

getLearningDecay()

Gets the value of learningDecay or its default value.

New in version 2.0.0.

getLearningOffset()

Gets the value of learningOffset or its default value.

New in version 2.0.0.

getOptimizeDocConcentration()

Gets the value of optimizeDocConcentration or its default value.

New in version 2.0.0.

getOptimizer()

Gets the value of optimizer or its default value.

New in version 2.0.0.

getSubsamplingRate()

Gets the value of subsamplingRate or its default value.

New in version 2.0.0.

getTopicConcentration()

Gets the value of topicConcentration or its default value.

New in version 2.0.0.

getTopicDistributionCol()

Gets the value of topicDistributionCol or its default value.

New in version 2.0.0.

setDocConcentration(*value*)

Sets the value of docConcentration.

```
>>> algo = LDA().setDocConcentration([0.1, 0.2])
>>> algo.getDocConcentration()
[0.1..., 0.2...]
```

New in version 2.0.0.

setK(*value*)

Sets the value of k.

```
>>> algo = LDA().setK(10)
>>> algo.getK()
10
```

New in version 2.0.0.

setKeepLastCheckpoint (value)

Sets the value of keepLastCheckpoint.

```
>>> algo = LDA().setKeepLastCheckpoint(False)
>>> algo.getKeepLastCheckpoint()
False
```

New in version 2.0.0.

setLearningDecay (value)

Sets the value of learningDecay.

```
>>> algo = LDA().setLearningDecay(0.1)
>>> algo.getLearningDecay()
0.1...
```

New in version 2.0.0.

setLearningOffset (value)

Sets the value of learningOffset.

```
>>> algo = LDA().setLearningOffset(100)
>>> algo.getLearningOffset()
100.0
```

New in version 2.0.0.

setOptimizeDocConcentration (value)

Sets the value of optimizeDocConcentration.

```
>>> algo = LDA().setOptimizeDocConcentration(True)
>>> algo.getOptimizeDocConcentration()
True
```

New in version 2.0.0.

setOptimizer (value)

Sets the value of optimizer. Currently only support ‘em’ and ‘online’.

```
>>> algo = LDA().setOptimizer("em")
>>> algo.getOptimizer()
'em'
```

New in version 2.0.0.

```
setParams(self, featuresCol="features", maxIter=20, seed=None, checkpointInterval=10, k=10, optimizer="online", learningOffset=1024.0, learningDecay=0.51, subsamplingRate=0.05, optimizeDocConcentration=True, docConcentration=None, topicConcentration=None, topicDistributionCol="topicDistribution", keepLastCheckpoint=True)
```

Sets params for LDA.

New in version 2.0.0.

```
setSubsamplingRate(value)
```

Sets the value of subsamplingRate.

```
>>> algo = LDA().setSubsamplingRate(0.1)
>>> algo.getSubsamplingRate()
0.1...
```

New in version 2.0.0.

```
setTopicConcentration(value)
```

Sets the value of topicConcentration.

```
>>> algo = LDA().setTopicConcentration(0.5)
>>> algo.getTopicConcentration()
0.5...
```

New in version 2.0.0.

```
setTopicDistributionCol(value)
```

Sets the value of topicDistributionCol.

```
>>> algo = LDA().setTopicDistributionCol("topicDistributionCol")
>>> algo.getTopicDistributionCol()
'topicDistributionCol'
```

New in version 2.0.0.

```
class pyspark.ml.clustering.LDAModel(java_model=None)
```

Latent Dirichlet Allocation (LDA) model. This abstraction permits for different underlying representations, including local and distributed data structures.

New in version 2.0.0.

```
describeTopics(maxTermsPerTopic=10)
```

Return the topics described by their top-weighted terms.

New in version 2.0.0.

```
estimatedDocConcentration()
```

Value for LDA.docConcentration estimated from data. If Online LDA was used and LDA.optimizeDocConcentration was set to false, then this returns the fixed (given) value for the LDA.docConcentration parameter.

New in version 2.0.0.

isDistributed()

Indicates whether this instance is of type `DistributedLDAModel`

New in version 2.0.0.

logLikelihood(*dataset*)

Calculates a lower bound on the log likelihood of the entire corpus. See Equation (16) in the Online LDA paper (Hoffman et al., 2010).

WARNING: If this model is an instance of `DistributedLDAModel` (produced when `optimizer` is set to “em”), this involves collecting a large `topicsMatrix()` to the driver. This implementation may be changed in the future.

New in version 2.0.0.

logPerplexity(*dataset*)

Calculate an upper bound on perplexity. (Lower is better.) See Equation (16) in the Online LDA paper (Hoffman et al., 2010).

WARNING: If this model is an instance of `DistributedLDAModel` (produced when `optimizer` is set to “em”), this involves collecting a large `topicsMatrix()` to the driver. This implementation may be changed in the future.

New in version 2.0.0.

topicsMatrix()

Inferred topics, where each topic is represented by a distribution over terms. This is a matrix of size `vocabSize` x `k`, where each column is a topic. No guarantees are given about the ordering of the topics.

WARNING: If this model is actually a `DistributedLDAModel` instance produced by the Expectation-Maximization (“em”) `optimizer`, then this method could involve collecting a large amount of data to the driver (on the order of `vocabSize` x `k`).

New in version 2.0.0.

vocabSize()

Vocabulary size (number of terms or words in the vocabulary)

New in version 2.0.0.

class pyspark.ml.clustering.`LocalLDAModel`(*java_model=None*)

Local (non-distributed) model fitted by `LDA`. This model stores the inferred topics only; it does not store info about the training dataset.

New in version 2.0.0.

class pyspark.ml.clustering.`DistributedLDAModel`(*java_model=None*)

Distributed model fitted by `LDA`. This type of model is currently only produced by Expectation-Maximization (EM).

This model stores the inferred topics, the full training dataset, and the topic distribution for each training document.

New in version 2.0.0.

`getCheckpointFiles()`

If using checkpointing and `LDA.keepLastCheckpoint` is set to true, then there may be saved checkpoint files. This method is provided so that users can manage those files.

Note: Removing the checkpoints can cause failures if a partition is lost and is needed by certain `DistributedLDAModel` methods. Reference counting will clean up the checkpoints when this model and derivative data go out of scope.

:return List of checkpoint files from training

New in version 2.0.0.

`logPrior()`

Log probability of the current parameter estimate: $\log P(\text{topics}, \text{topic distributions for docs} | \alpha, \eta)$

New in version 2.0.0.

`toLocal()`

Convert this distributed model to a local representation. This discards info about the training dataset.

WARNING: This involves collecting a large `topicsMatrix()` to the driver.

New in version 2.0.0.

`trainingLogLikelihood()`

Log likelihood of the observed tokens in the training set, given the current parameter estimates: $\log P(\text{docs} | \text{topics}, \text{topic distributions for docs, Dirichlet hyperparameters})$

Notes:

- This excludes the prior; for that, use `logPrior()`.
- Even with `logPrior()`, this is NOT the same as the data log likelihood given the hyperparameters.
- This is computed from the topic distributions computed during training. If you call `logLikelihood()` on the same training dataset, the topic distributions will be computed again, possibly giving different results.

New in version 2.0.0.

```
class pyspark.ml.clustering.PowerIterationClustering(k=2,    maxIter=20,
                                                       initMode='random',
                                                       srcCol='src',    dst-
                                                       Col='dst',    weight-
                                                       Col=None)
```

Note: Experimental

Power Iteration Clustering (PIC), a scalable graph clustering algorithm developed by Lin and Cohen. From the abstract: PIC finds a very low-dimensional embedding of a dataset using truncated power iteration on a normalized pair-wise similarity matrix of the data.

This class is not yet an Estimator/Transformer, use `assignClusters()` method to run the PowerIterationClustering algorithm.

See also:

[Wikipedia on Spectral clustering](#)

```
>>> data = [(1, 0, 0.5),
...           (2, 0, 0.5), (2, 1, 0.7),
...           (3, 0, 0.5), (3, 1, 0.7), (3, 2, 0.9),
...           (4, 0, 0.5), (4, 1, 0.7), (4, 2, 0.9), (4, 3, 1.1),
...           (5, 0, 0.5), (5, 1, 0.7), (5, 2, 0.9), (5, 3, 1.1), (5, 4, 1.
...           ↵3)]
>>> df = spark.createDataFrame(data).toDF("src", "dst", "weight")
>>> pic = PowerIterationClustering(k=2, maxIter=40, weightCol="weight")
>>> assignments = pic.assignClusters(df)
>>> assignments.sort(assignments.id).show(truncate=False)
+---+-----+
|id |cluster|
+---+-----+
|0  |1      |
|1  |1      |
|2  |1      |
|3  |1      |
|4  |1      |
|5  |0      |
+---+-----+
...
>>> pic_path = temp_path + "/pic"
>>> pic.save(pic_path)
>>> pic2 = PowerIterationClustering.load(pic_path)
>>> pic2.getK()
2
>>> pic2.getMaxIter()
40
```

New in version 2.4.0.

`assignClusters(dataset)`

Run the PIC algorithm and returns a cluster assignment for each input vertex.

Parameters `dataset` – A dataset with columns `src`, `dst`, `weight` representing the affinity matrix, which is the matrix A in the PIC paper. Suppose the `src` column value is i , the `dst` column value is j , the `weight` column value is similarity s_{ij} , which must be nonnegative. This is a symmetric matrix and hence $s_{ij} = s_{ji}$. For any (i, j) with nonzero similarity, there should be either (i, j, s_{ij}) or (j, i, s_{ji}) in the input. Rows with $i = j$ are ignored, because we assume $s_{ii} = 0.0$.

Returns A dataset that contains columns of vertex `id` and the corresponding cluster for the `id`. The schema of it will be: - `id`: Long - `cluster`: Int

New in version 2.4.0.

New in version 2.4.0.

getDstCol()

Gets the value of `dstCol` or its default value.

New in version 2.4.0.

getInitMode()

Gets the value of `initMode` or its default value.

New in version 2.4.0.

getK()

Gets the value of `k` or its default value.

New in version 2.4.0.

getSrcCol()

Gets the value of `srcCol` or its default value.

New in version 2.4.0.

setDstCol(*value*)

Sets the value of `dstCol`.

New in version 2.4.0.

setInitMode(*value*)

Sets the value of `initMode`.

New in version 2.4.0.

setK(*value*)

Sets the value of `k`.

New in version 2.4.0.

setParams(*self*, *k*=2, *maxIter*=20, *initMode*="random", *srcCol*="src", *dstCol*="dst", *weightCol*=None)

Sets params for PowerIterationClustering.

New in version 2.4.0.

setSrcCol(*value*)

Sets the value of `srcCol`.

New in version 2.4.0.

23.5 Recommendation API

```
class pyspark.ml.recommendation.ALS(rank=10, maxIter=10, regParam=0.1, numUserBlocks=10, numItemBlocks=10, implicitPrefs=False, alpha=1.0, userCol='user', itemCol='item', seed=None, ratingCol='rating', nonnegative=False, checkpointInterval=10, intermediateStorageLevel='MEMORY_AND_DISK', finalStorageLevel='MEMORY_AND_DISK', coldStartStrategy='nan')
```

Alternating Least Squares (ALS) matrix factorization.

ALS attempts to estimate the ratings matrix R as the product of two lower-rank matrices, X and Y , i.e. $X * Y^T = R$. Typically these approximations are called ‘factor’ matrices. The general approach is iterative. During each iteration, one of the factor matrices is held constant, while the other is solved for using least squares. The newly-solved factor matrix is then held constant while solving for the other factor matrix.

This is a blocked implementation of the ALS factorization algorithm that groups the two sets of factors (referred to as “users” and “products”) into blocks and reduces communication by only sending one copy of each user vector to each product block on each iteration, and only for the product blocks that need that user’s feature vector. This is achieved by pre-computing some information about the ratings matrix to determine the “out-links” of each user (which blocks of products it will contribute to) and “in-link” information for each product (which of the feature vectors it receives from each user block it will depend on). This allows us to send only an array of feature vectors between each user block and product block, and have the product block find the users’ ratings and update the products based on these messages.

For implicit preference data, the algorithm used is based on “[Collaborative Filtering for Implicit Feedback Datasets](#)”, adapted for the blocked approach used here.

Essentially instead of finding the low-rank approximations to the rating matrix R , this finds the approximations for a preference matrix P where the elements of P are 1 if $r > 0$ and 0 if $r \leq 0$. The ratings then act as ‘confidence’ values related to strength of indicated user preferences rather than explicit ratings given to items.

```
>>> df = spark.createDataFrame(
...     [(0, 0, 4.0), (0, 1, 2.0), (1, 1, 3.0), (1, 2, 4.0), (2, 1, 1.0),
...     (2, 2, 5.0)],
...     ["user", "item", "rating"])
>>> als = ALS(rank=10, maxIter=5, seed=0)
>>> model = als.fit(df)
>>> model.rank
10
>>> model.userFactors.orderBy("id").collect()
[Row(id=0, features=[...]), Row(id=1, ...), Row(id=2, ...)]
>>> test = spark.createDataFrame([(0, 2), (1, 0), (2, 0)], ["user", "item"])
>>> predictions = sorted(model.transform(test).collect(), key=lambda r:r[0])
```

(continues on next page)

(continued from previous page)

```
>>> predictions[0]
Row(user=0, item=2, prediction=-0.13807615637779236)
>>> predictions[1]
Row(user=1, item=0, prediction=2.6258413791656494)
>>> predictions[2]
Row(user=2, item=0, prediction=-1.5018409490585327)
>>> user_recs = model.recommendForAllUsers(3)
>>> user_recs.where(user_recs.user == 0) .select("recommendations.
˓→item", "recommendations.rating").collect()
[Row(item=[0, 1, 2], rating=[3.910..., 1.992..., -0.138...])]
>>> item_recs = model.recommendForAllItems(3)
>>> item_recs.where(item_recs.item == 2) .select("recommendations.
˓→user", "recommendations.rating").collect()
[Row(user=[2, 1, 0], rating=[4.901..., 3.981..., -0.138...])]
>>> user_subset = df.where(df.user == 2)
>>> user_subset_recs = model.recommendForUserSubset(user_subset, 3)
>>> user_subset_recs.select("recommendations.item", "recommendations.
˓→rating").first()
Row(item=[2, 1, 0], rating=[4.901..., 1.056..., -1.501...])
>>> item_subset = df.where(df.item == 0)
>>> item_subset_recs = model.recommendForItemSubset(item_subset, 3)
>>> item_subset_recs.select("recommendations.user", "recommendations.
˓→rating").first()
Row(user=[0, 1, 2], rating=[3.910..., 2.625..., -1.501...])
>>> als_path = temp_path + "/als"
>>> als.save(als_path)
>>> als2 = ALS.load(als_path)
>>> als.getMaxIter()
5
>>> model_path = temp_path + "/als_model"
>>> model.save(model_path)
>>> model2 = ALSModel.load(model_path)
>>> model.rank == model2.rank
True
>>> sorted(model.userFactors.collect()) == sorted(model2.userFactors.
˓→collect())
True
>>> sorted(model.itemFactors.collect()) == sorted(model2.itemFactors.
˓→collect())
True
```

New in version 1.4.0.

getAlpha()

Gets the value of alpha or its default value.

New in version 1.4.0.

getColdStartStrategy()

Gets the value of coldStartStrategy or its default value.

New in version 2.2.0.

getFinalStorageLevel()
Gets the value of finalStorageLevel or its default value.

New in version 2.0.0.

getImplicitPrefs()
Gets the value of implicitPrefs or its default value.

New in version 1.4.0.

getIntermediateStorageLevel()
Gets the value of intermediateStorageLevel or its default value.

New in version 2.0.0.

getItemCol()
Gets the value of itemCol or its default value.

New in version 1.4.0.

getNonnegative()
Gets the value of nonnegative or its default value.

New in version 1.4.0.

getNumItemBlocks()
Gets the value of numItemBlocks or its default value.

New in version 1.4.0.

getNumUserBlocks()
Gets the value of numUserBlocks or its default value.

New in version 1.4.0.

getRank()
Gets the value of rank or its default value.

New in version 1.4.0.

getRatingCol()
Gets the value of ratingCol or its default value.

New in version 1.4.0.

getUserCol()
Gets the value of userCol or its default value.

New in version 1.4.0.

setAlpha(*value*)
Sets the value of alpha.

New in version 1.4.0.

setColdStartStrategy(*value*)
Sets the value of coldStartStrategy.

New in version 2.2.0.

setFinalStorageLevel (value)

Sets the value of finalStorageLevel.

New in version 2.0.0.

setImplicitPrefs (value)

Sets the value of implicitPrefs.

New in version 1.4.0.

setIntermediateStorageLevel (value)

Sets the value of intermediateStorageLevel.

New in version 2.0.0.

setItemCol (value)

Sets the value of itemCol.

New in version 1.4.0.

setNonnegative (value)

Sets the value of nonnegative.

New in version 1.4.0.

setNumBlocks (value)

Sets both numUserBlocks and numItemBlocks to the specific value.

New in version 1.4.0.

setNumItemBlocks (value)

Sets the value of numItemBlocks.

New in version 1.4.0.

setNumUserBlocks (value)

Sets the value of numUserBlocks.

New in version 1.4.0.

setParams (self, rank=10, maxIter=10, regParam=0.1, numUserBlocks=10, numItemBlocks=10, implicitPrefs=False, alpha=1.0, userCol="user", itemCol="item", seed=None, ratingCol="rating", nonnegative=False, checkpointInterval=10, intermediateStorageLevel="MEMORY_AND_DISK", finalStorageLevel="MEMORY_AND_DISK", coldStartStrategy="nan")

Sets params for ALS.

New in version 1.4.0.

setRank (value)

Sets the value of rank.

New in version 1.4.0.

setRatingCol (value)

Sets the value of ratingCol.

New in version 1.4.0.

setUserCol (*value*)

Sets the value of `userCol`.

New in version 1.4.0.

class pyspark.ml.recommendation.**ALSModel** (*java_model=None*)

Model fitted by ALS.

New in version 1.4.0.

itemFactors

id and *features*

New in version 1.4.0.

Type a DataFrame that stores item factors in two columns

rank

rank of the matrix factorization model

New in version 1.4.0.

recommendForAllItems (*numUsers*)

Returns top *numUsers* users recommended for each item, for all items.

Parameters **numUsers** – max number of recommendations for each item

Returns a DataFrame of (itemCol, recommendations), where recommendations are stored as an array of (userCol, rating) Rows.

New in version 2.2.0.

recommendForAllUsers (*numItems*)

Returns top *numItems* items recommended for each user, for all users.

Parameters **numItems** – max number of recommendations for each user

Returns a DataFrame of (userCol, recommendations), where recommendations are stored as an array of (itemCol, rating) Rows.

New in version 2.2.0.

recommendForItemSubset (*dataset, numUsers*)

Returns top *numUsers* users recommended for each item id in the input data set. Note that if there are duplicate ids in the input dataset, only one set of recommendations per unique id will be returned.

Parameters

- **dataset** – a Dataset containing a column of item ids. The column name must match *itemCol*.
- **numUsers** – max number of recommendations for each item

Returns a DataFrame of (itemCol, recommendations), where recommendations are stored as an array of (userCol, rating) Rows.

New in version 2.3.0.

recommendForUserSubset (*dataset, numItems*)

Returns top *numItems* items recommended for each user id in the input data set. Note that if there are duplicate ids in the input dataset, only one set of recommendations per unique id will be returned.

Parameters

- **dataset** – a Dataset containing a column of user ids. The column name must match *userCol*.
- **numItems** – max number of recommendations for each user

Returns a DataFrame of (*userCol*, recommendations), where recommendations are stored as an array of (*itemCol*, rating) Rows.

New in version 2.3.0.

userFactors

id and *features*

New in version 1.4.0.

Type a DataFrame that stores user factors in two columns

23.6 Pipeline API

class pyspark.ml.pipeline.Pipeline (*stages=None*)

A simple pipeline, which acts as an estimator. A Pipeline consists of a sequence of stages, each of which is either an Estimator or a Transformer. When `Pipeline.fit()` is called, the stages are executed in order. If a stage is an Estimator, its `Estimator.fit()` method will be called on the input dataset to fit a model. Then the model, which is a transformer, will be used to transform the dataset as the input to the next stage. If a stage is a Transformer, its `Transformer.transform()` method will be called to produce the dataset for the next stage. The fitted model from a `Pipeline` is a `PipelineModel`, which consists of fitted models and transformers, corresponding to the pipeline stages. If stages is an empty list, the pipeline acts as an identity transformer.

New in version 1.3.0.

copy (*extra=None*)

Creates a copy of this instance.

Parameters extra – extra parameters

Returns new instance

New in version 1.4.0.

getStages ()

Get pipeline stages.

New in version 1.3.0.

classmethod read ()

Returns an MLReader instance for this class.

New in version 2.0.0.

setParams (*self*, *stages=None*)

Sets params for Pipeline.

New in version 1.3.0.

setStages (*value*)

Set pipeline stages.

Parameters **value** – a list of transformers or estimators

Returns the pipeline instance

New in version 1.3.0.

write ()

Returns an MLWriter instance for this ML instance.

New in version 2.0.0.

class pyspark.ml.pipeline.**PipelineModel** (*stages*)

Represents a compiled pipeline with transformers and fitted models.

New in version 1.3.0.

copy (*extra=None*)

Creates a copy of this instance.

Parameters **extra** – extra parameters

Returns new instance

New in version 1.4.0.

classmethod **read** ()

Returns an MLReader instance for this class.

New in version 2.0.0.

write ()

Returns an MLWriter instance for this ML instance.

New in version 2.0.0.

class pyspark.ml.pipeline.**PipelineModelReader** (*cls*)

(Private) Specialization of MLReader for [PipelineModel](#) types

load (*path*)

Load the ML instance from the input path.

class pyspark.ml.pipeline.**PipelineModelWriter** (*instance*)

(Private) Specialization of MLWriter for [PipelineModel](#) types

saveImpl (*path*)

save() handles overwriting and then calls this method. Subclasses should override this method to implement the actual saving of the instance.

```
class pyspark.ml.pipeline.PipelineReader(cls)
(Private) Specialization of MLReader for Pipeline types

load(path)
Load the ML instance from the input path.

class pyspark.ml.pipeline.PipelineSharedReadWrite
```

Note: DeveloperApi

Functions for MLReader and MLWriter shared between *Pipeline* and *PipelineModel*

New in version 2.3.0.

```
static getStagePath(stageUid, stageIdx, numStages, stagesDir)
Get path for saving the given stage.

static load(metadata, sc, path)
Load metadata and stages for a Pipeline or PipelineModel

Returns (UID, list of stages)

static saveImpl(instance, stages, sc, path)
Save metadata and stages for a Pipeline or PipelineModel - save metadata to
path/metadata - save stages to stages/IDX_UID

static validateStages(stages)
Check that all stages are Writable

class pyspark.ml.pipeline.PipelineWriter(instance)
(Private) Specialization of MLWriter for Pipeline types

saveImpl(path)
save() handles overwriting and then calls this method. Subclasses should override this method
to implement the actual saving of the instance.
```

23.7 Tuning API

```
class pyspark.ml.tuning.ParamGridBuilder
Builder for a param grid used in grid search-based model selection.
```

```
>>> from pyspark.ml.classification import LogisticRegression
>>> lr = LogisticRegression()
>>> output = ParamGridBuilder() \
...     .baseOn({lr.labelCol: 'l'}) \
...     .baseOn([lr.predictionCol, 'p']) \
...     .addGrid(lr.regParam, [1.0, 2.0]) \
...     .addGrid(lr.maxIter, [1, 5]) \
...     .build()
>>> expected = [
```

(continues on next page)

(continued from previous page)

```

...     {lr.regParam: 1.0, lr.maxIter: 1, lr.labelCol: 'l', lr.
↳predictionCol: 'p'},
...     {lr.regParam: 2.0, lr.maxIter: 1, lr.labelCol: 'l', lr.
↳predictionCol: 'p'},
...     {lr.regParam: 1.0, lr.maxIter: 5, lr.labelCol: 'l', lr.
↳predictionCol: 'p'},
...     {lr.regParam: 2.0, lr.maxIter: 5, lr.labelCol: 'l', lr.
↳predictionCol: 'p'}]
>>> len(output) == len(expected)
True
>>> all([m in expected for m in output])
True

```

New in version 1.4.0.

addGrid(*param, values*)

Sets the given parameters in this grid to fixed values.

New in version 1.4.0.

baseOn(*args)

Sets the given parameters in this grid to fixed values. Accepts either a parameter dictionary or a list of (parameter, value) pairs.

New in version 1.4.0.

build()

Builds and returns all combinations of parameters specified by the param grid.

New in version 1.4.0.

```
class pyspark.ml.tuning.CrossValidator(estimator=None, estimator-
                                         ParamMaps=None, evaluator=None,
                                         numFolds=3, seed=None, parallelism=1,
                                         collectSubModels=False)
```

K-fold cross validation performs model selection by splitting the dataset into a set of non-overlapping randomly partitioned folds which are used as separate training and test datasets e.g., with k=3 folds, K-fold cross validation will generate 3 (training, test) dataset pairs, each of which uses 2/3 of the data for training and 1/3 for testing. Each fold is used as the test set exactly once.

```

>>> from pyspark.ml.classification import LogisticRegression
>>> from pyspark.ml.evaluation import BinaryClassificationEvaluator
>>> from pyspark.ml.linalg import Vectors
>>> dataset = spark.createDataFrame(
...     [(Vectors.dense([0.0]), 0.0),
...      (Vectors.dense([0.4]), 1.0),
...      (Vectors.dense([0.5]), 0.0),
...      (Vectors.dense([0.6]), 1.0),
...      (Vectors.dense([1.0]), 1.0)] * 10,
...     ["features", "label"])
>>> lr = LogisticRegression()
>>> grid = ParamGridBuilder().addGrid(lr.maxIter, [0, 1]).build()

```

(continues on next page)

(continued from previous page)

```
>>> evaluator = BinaryClassificationEvaluator()
>>> cv = CrossValidator(estimator=lr, estimatorParamMaps=grid,
-> evaluator=evaluator,
...     parallelism=2)
>>> cvModel = cv.fit(dataset)
>>> cvModel.avgMetrics[0]
0.5
>>> evaluator.evaluate(cvModel.transform(dataset))
0.8333...
```

New in version 1.4.0.

copy (extra=None)

Creates a copy of this instance with a randomly generated uid and some extra params. This copies creates a deep copy of the embedded paramMap, and copies the embedded and extra parameters over.

Parameters extra – Extra parameters to copy to the new instance

Returns Copy of this instance

New in version 1.4.0.

getNumFolds ()

Gets the value of numFolds or its default value.

New in version 1.4.0.

classmethod read ()

Returns an MLReader instance for this class.

New in version 2.3.0.

setNumFolds (value)

Sets the value of numFolds.

New in version 1.4.0.

setParams (estimator=None, estimatorParamMaps=None, evaluator=None, numFolds=3,

seed=None, parallelism=1, collectSubModels=False)

setParams(self, estimator=None, estimatorParamMaps=None, evaluator=None, numFolds=3, seed=None, parallelism=1, collectSubModels=False): Sets params for cross validator.

New in version 1.4.0.

write ()

Returns an MLWriter instance for this ML instance.

New in version 2.3.0.

**class pyspark.ml.tuning.CrossValidatorModel (bestModel, avgMetrics=[], sub-
Models=None)**

CrossValidatorModel contains the model with the highest average cross-validation metric across folds and uses this model to transform input data. CrossValidatorModel also tracks the metrics for each param map evaluated.

New in version 1.4.0.

avgMetrics = None

Average cross-validation metrics for each paramMap in CrossValidator.estimatorParamMaps, in the corresponding order.

bestModel = None

best model from cross validation

copy(extra=None)

Creates a copy of this instance with a randomly generated uid and some extra params. This copies the underlying bestModel, creates a deep copy of the embedded paramMap, and copies the embedded and extra parameters over. It does not copy the extra Params into the subModels.

Parameters extra – Extra parameters to copy to the new instance

Returns Copy of this instance

New in version 1.4.0.

classmethod read()

Returns an MLReader instance for this class.

New in version 2.3.0.

subModels = None

sub model list from cross validation

write()

Returns an MLWriter instance for this ML instance.

New in version 2.3.0.

```
class pyspark.ml.tuning.TrainValidationSplit(estimator=None, estimatorParamMaps=None, evaluator=None, trainRatio=0.75, parallelism=1, collectSubModels=False, seed=None)
```

Note: Experimental

Validation for hyper-parameter tuning. Randomly splits the input dataset into train and validation sets, and uses evaluation metric on the validation set to select the best model. Similar to *CrossValidator*, but only splits the set once.

```
>>> from pyspark.ml.classification import LogisticRegression
>>> from pyspark.ml.evaluation import BinaryClassificationEvaluator
>>> from pyspark.ml.linalg import Vectors
>>> dataset = spark.createDataFrame(
...     [ (Vectors.dense([0.0]), 0.0),
...      (Vectors.dense([0.4]), 1.0),
...      (Vectors.dense([0.5]), 0.0),
...      (Vectors.dense([0.6]), 1.0),
```

(continues on next page)

(continued from previous page)

```
...     (Vectors.dense([1.0]), 1.0)] * 10,
...     ["features", "label"])
>>> lr = LogisticRegression()
>>> grid = ParamGridBuilder().addGrid(lr.maxIter, [0, 1]).build()
>>> evaluator = BinaryClassificationEvaluator()
>>> tvs = TrainValidationSplit(estimator=lr, estimatorParamMaps=grid, 
  ↵evaluator=evaluator,
...     parallelism=2)
>>> tvsModel = tvs.fit(dataset)
>>> evaluator.evaluate(tvsModel.transform(dataset))
0.8333...
```

New in version 2.0.0.

`copy(extra=None)`

Creates a copy of this instance with a randomly generated uid and some extra params. This copies creates a deep copy of the embedded paramMap, and copies the embedded and extra parameters over.

Parameters `extra` – Extra parameters to copy to the new instance

Returns Copy of this instance

New in version 2.0.0.

`getTrainRatio()`

Gets the value of trainRatio or its default value.

New in version 2.0.0.

`classmethod read()`

Returns an MLReader instance for this class.

New in version 2.3.0.

setParams (`estimator=None, estimatorParamMaps=None, evaluator=None, trainRatio=0.75, parallelism=1, collectSubModels=False, seed=None`)
setParams(self, estimator=None, estimatorParamMaps=None, evaluator=None, trainRatio=0.75, parallelism=1, collectSubModels=False, seed=None): Sets params for the train validation split.

New in version 2.0.0.

`setTrainRatio(value)`

Sets the value of trainRatio.

New in version 2.0.0.

`write()`

Returns an MLWriter instance for this ML instance.

New in version 2.3.0.

```
class pyspark.ml.tuning.TrainValidationSplitModel (bestModel, validation-
                                                 Metrics=[], subMod-
                                                 els=None)
```

Note: Experimental

Model from train validation split.

New in version 2.0.0.

bestModel = None

best model from train validation split

copy (extra=None)

Creates a copy of this instance with a randomly generated uid and some extra params. This copies the underlying bestModel, creates a deep copy of the embedded paramMap, and copies the embedded and extra parameters over. And, this creates a shallow copy of the validationMetrics. It does not copy the extra Params into the subModels.

Parameters extra – Extra parameters to copy to the new instance

Returns Copy of this instance

New in version 2.0.0.

classmethod read()

Returns an MLReader instance for this class.

New in version 2.3.0.

subModels = None

sub models from train validation split

validationMetrics = None

evaluated validation metrics

write()

Returns an MLWriter instance for this ML instance.

New in version 2.3.0.

23.8 Evaluation API

```
class pyspark.ml.evaluation.Evaluator
```

Base class for evaluators that compute metrics from predictions.

New in version 1.4.0.

evaluate (dataset, params=None)

Evaluates the output with optional parameters.

Parameters

- **dataset** – a dataset that contains labels/observations and predictions
- **params** – an optional param map that overrides embedded params

Returns metric

New in version 1.4.0.

isLargerBetter()

Indicates whether the metric returned by `evaluate()` should be maximized (True, default) or minimized (False). A given evaluator may support multiple metrics which may be maximized or minimized.

New in version 1.5.0.

```
class pyspark.ml.evaluation.BinaryClassificationEvaluator(rawPredictionCol='rawPrediction',
                                                       label-
                                                       Col='label',
                                                       metric-
                                                       Name='areaUnderROC')
```

Note: Experimental

Evaluator for binary classification, which expects two input columns: rawPrediction and label. The rawPrediction column can be of type double (binary 0/1 prediction, or probability of label 1) or of type vector (length-2 vector of raw predictions, scores, or label probabilities).

```
>>> from pyspark.ml.linalg import Vectors
>>> scoreAndLabels = map(lambda x: (Vectors.dense([1.0 - x[0], x[0]]), x[1]),
...     [(0.1, 0.0), (0.1, 1.0), (0.4, 0.0), (0.6, 0.0), (0.6, 1.0), (0.6,
...     1.0), (0.8, 1.0)])
>>> dataset = spark.createDataFrame(scoreAndLabels, ["raw", "label"])
...
>>> evaluator = BinaryClassificationEvaluator(rawPredictionCol="raw")
>>> evaluator.evaluate(dataset)
0.70...
>>> evaluator.evaluate(dataset, {evaluator.metricName: "areaUnderPR"})
0.83...
>>> bce_path = temp_path + "/bce"
>>> evaluator.save(bce_path)
>>> evaluator2 = BinaryClassificationEvaluator.load(bce_path)
>>> str(evaluator2.getRawPredictionCol())
'raw'
```

New in version 1.4.0.

getMetricName()

Gets the value of metricName or its default value.

New in version 1.4.0.

setMetricName (*value*)

Sets the value of metricName.

New in version 1.4.0.

setParams (*self*, *rawPredictionCol="rawPrediction"*, *labelCol="label"*, *metricName="areaUnderROC"*)

Sets params for binary classification evaluator.

New in version 1.4.0.

```
class pyspark.ml.evaluation.RegressionEvaluator(predictionCol='prediction',
                                                labelCol='label',
                                                metricName='rmse')
```

Note: Experimental

Evaluator for Regression, which expects two input columns: prediction and label.

```
>>> scoreAndLabels = [(-28.98343821, -27.0), (20.21491975, 21.5),
...      (-25.98418959, -22.0), (30.69731842, 33.0), (74.69283752, 71.0)]
>>> dataset = spark.createDataFrame(scoreAndLabels, ["raw", "label"])
...
>>> evaluator = RegressionEvaluator(predictionCol="raw")
>>> evaluator.evaluate(dataset)
2.842...
>>> evaluator.evaluate(dataset, {evaluator.metricName: "r2"})
0.993...
>>> evaluator.evaluate(dataset, {evaluator.metricName: "mae"})
2.649...
>>> re_path = temp_path + "/re"
>>> evaluator.save(re_path)
>>> evaluator2 = RegressionEvaluator.load(re_path)
>>> str(evaluator2.getPredictionCol())
'raw'
```

New in version 1.4.0.

getMetricName ()

Gets the value of metricName or its default value.

New in version 1.4.0.

setMetricName (*value*)

Sets the value of metricName.

New in version 1.4.0.

setParams (*self*, *predictionCol="prediction"*, *labelCol="label"*, *metricName="rmse"*)

Sets params for regression evaluator.

New in version 1.4.0.

```
class pyspark.ml.evaluation.MulticlassClassificationEvaluator(predictionCol='prediction',
                                                               labelCol='label',
                                                               metricName='f1')
```

Note: Experimental

Evaluator for Multiclass Classification, which expects two input columns: prediction and label.

```
>>> scoreAndLabels = [(0.0, 0.0), (0.0, 1.0), (0.0, 0.0),
...         (1.0, 0.0), (1.0, 1.0), (1.0, 1.0), (1.0, 1.0), (2.0, 2.0), (2.0,
...         0.0)]
>>> dataset = spark.createDataFrame(scoreAndLabels, ["prediction", "label"])
...
>>> evaluator = MulticlassClassificationEvaluator(predictionCol=
...         "prediction")
>>> evaluator.evaluate(dataset)
0.66...
>>> evaluator.evaluate(dataset, {evaluator.metricName: "accuracy"})
0.66...
>>> mce_path = temp_path + "/mce"
>>> evaluator.save(mce_path)
>>> evaluator2 = MulticlassClassificationEvaluator.load(mce_path)
>>> str(evaluator2.getPredictionCol())
'prediction'
```

New in version 1.5.0.

getMetricName()

Gets the value of metricName or its default value.

New in version 1.5.0.

setMetricName(value)

Sets the value of metricName.

New in version 1.5.0.

setParams(self, predictionCol="prediction", labelCol="label", metricName="f1")

Sets params for multiclass classification evaluator.

New in version 1.5.0.

```
class pyspark.ml.evaluation.ClusteringEvaluator(predictionCol='prediction',
                                                 featuresCol='features', metricName='silhouette',
                                                 distanceMeasure='squaredEuclidean')
```

Note: Experimental

Evaluator for Clustering results, which expects two input columns: prediction and features. The metric computes the Silhouette measure using the squared Euclidean distance.

The Silhouette is a measure for the validation of the consistency within clusters. It ranges between 1 and -1, where a value close to 1 means that the points in a cluster are close to the other points in the same cluster and far from the points of the other clusters.

```
>>> from pyspark.ml.linalg import Vectors
>>> featureAndPredictions = map(lambda x: (Vectors.dense(x[0]), x[1]),
...     [[[0.0, 0.5], 0.0), ([0.5, 0.0], 0.0), ([10.0, 11.0], 1.0),
...     ([10.5, 11.5], 1.0), ([1.0, 1.0], 0.0), ([8.0, 6.0], 1.0)])
>>> dataset = spark.createDataFrame(featureAndPredictions, ["features",
... "prediction"])
...
>>> evaluator = ClusteringEvaluator(predictionCol="prediction")
>>> evaluator.evaluate(dataset)
0.9079...
>>> ce_path = temp_path + "/ce"
>>> evaluator.save(ce_path)
>>> evaluator2 = ClusteringEvaluator.load(ce_path)
>>> str(evaluator2.getPredictionCol())
'prediction'
```

New in version 2.3.0.

getDistanceMeasure()

Gets the value of *distanceMeasure*

New in version 2.4.0.

getMetricName()

Gets the value of *metricName* or its default value.

New in version 2.3.0.

setDistanceMeasure(*value*)

Sets the value of *distanceMeasure*.

New in version 2.4.0.

setMetricName(*value*)

Sets the value of *metricName*.

New in version 2.3.0.

**setParams(*self*, *predictionCol*="prediction", *featuresCol*="features", *metric-*
Name="silhouette", *distanceMeasure*="squaredEuclidean")**

Sets params for clustering evaluator.

New in version 2.3.0.

**CHAPTER
TWENTYFOUR**

MAIN REFERENCE

BIBLIOGRAPHY

- [Feng2017] W. Feng and M. Chen. [Learning Apache Spark](#), Github 2017.
- [Feng2016PSD] W. Feng, A. J. Salgado, C. Wang, S. M. Wise. Preconditioned Steepest Descent Methods for some Nonlinear Elliptic Equations Involving p-Laplacian Terms. *J. Comput. Phys.*, 334:45–67, 2016.
- [Feng2014] W. Feng. [Prelim Notes for Numerical Analysis](#), The University of Tennessee, Knoxville.
- [Karau2015] H. Karau, A. Konwinski, P. Wendell and M. Zaharia. [Learning Spark: Lightning-Fast Big Data Analysis](#). O'Reilly Media, Inc., 2015
- [Kirillov2016] Anton Kirillov. Apache Spark: core concepts, architecture and internals. <http://datastrophic.io/core-concepts-architecture-and-internals-of-apache-spark/>
- [zeppelin2nb] Wenqiang Feng and Ryan Blue. [Zeppelin notebook to jupyter notebook Library API](#), 2019.
- [jupyter-zeppelin] Ryan Blue. [Jupyter/Zeppelin conversion](#), 2017.

PYTHON MODULE INDEX

p

`pyspark.ml.classification`, 346
`pyspark.ml.clustering`, 369
`pyspark.ml.evaluation`, 397
`pyspark.ml.pipeline`, 390
`pyspark.ml.recommendation`, 385
`pyspark.ml.regression`, 325
`pyspark.ml.stat`, 319
`pyspark.ml.tuning`, 392

INDEX

A

accuracy (*pyspark.ml.classification.LogisticRegressionSummary* attribute), 352
addGrid() (*pyspark.ml.tuning.ParamGridBuilder* method), 393
AFTSurvivalRegression (*class in pyspark.ml.regression*), 325
AFTSurvivalRegressionModel (*class in pyspark.ml.regression*), 327
aic (*pyspark.ml.regression.GeneralizedLinearRegressionSummary* attribute), 335
ALS (*class in pyspark.ml.recommendation*), 385
ALSModel (*class in pyspark.ml.recommendation*), 389
areaUnderROC (*pyspark.ml.classification.BinaryLogisticRegressionSummary* attribute), 354
assignClusters () (*pyspark.ml.clustering.PowerIterationClustering* method), 383
avgMetrics (*pyspark.ml.tuning.CrossValidatorModel* attribute), 395

B

baseOn () (*pyspark.ml.tuning.ParamGridBuilder* method), 393
bestModel (*pyspark.ml.tuning.CrossValidatorModel* attribute), 395
bestModel (*pyspark.ml.tuning.TrainValidationSplitModel* attribute), 397
BinaryClassificationEvaluator (*class in pyspark.ml.evaluation*), 398
BinaryLogisticRegressionSummary (*class in pyspark.ml.classification*), 354

BinaryLogisticRegressionTrainingSummary (*class in pyspark.ml.classification*), 355
BisectingKMeans (*class in pyspark.ml.clustering*), 369
BisectingKMeansModel (*class in pyspark.ml.clustering*), 371
BisectingKMeansSummary (*class in pyspark.ml.clustering*), 371
boundaries (*pyspark.ml.regression.IsotonicRegressionModel* attribute), 338
build () (*pyspark.ml.tuning.ParamGridBuilder* method), 393

C

ChiSquareTest (*class in pyspark.ml.stat*), 319
clusterCenters () (*pyspark.ml.clustering.BisectingKMeansModel* method), 371
clusterCenters () (*pyspark.ml.clustering.KMeansModel* method), 373
ClusteringEvaluator (*class in pyspark.ml.evaluation*), 400
coefficientMatrix (*pyspark.ml.classification.LogisticRegressionModel* attribute), 351
coefficients (*pyspark.ml.classification.LinearSVCModel* attribute), 347
coefficients (*pyspark.ml.classification.LogisticRegressionModel* attribute), 351
coefficients (*pyspark.ml.regression.AFTSurvivalRegressionModel* attribute), 327

| | | |
|--|--|--|
| coefficients | (pys- | D |
| park.ml.regression.GeneralizedLinearRegressionModel
attribute), 334 | DecisionTreeClassificationModel
(class in pyspark.ml.classification), 357 | |
| coefficients | (pys- | DecisionTreeClassifier (class in pys-
park.ml.classification), 355 |
| park.ml.regression.LinearRegressionModel
attribute), 340 | DecisionTreeRegressionModel (class in
pyspark.ml.regression), 328 | |
| coefficientStandardErrors | (pys- | DecisionTreeRegressor (class in pys-
park.ml.regression), 327 |
| park.ml.regression.GeneralizedLinearRegressionTrainingSummary
attribute), 336 | degreesOfFreedom | (pys- |
| coefficientStandardErrors | (pys- | park.ml.regression.GeneralizedLinearRegressionSummary
attribute), 335 |
| computeCost() | (pys- | degreesOfFreedom |
| park.ml.clustering.BisectingKMeansModel
method), 371 | park.ml.regression.LinearRegressionSummary
attribute), 341 | (pys- |
| computeCost() | (pys- | describeTopics() |
| park.ml.clustering.KMeansModel method),
373 | park.ml.clustering.LDAModel
method),
380 | (pys- |
| Configure Spark on Mac and Ubuntu,
16 | | deviance (pyspark.ml.regression.GeneralizedLinearRegressionSum-
attribute), 335 |
| copy() | (pyspark.ml.classification.OneVsRest
method), 368 | devianceResiduals |
| copy() | (pyspark.ml.classification.OneVsRestModel
method), 369 | (pys-
park.ml.regression.LinearRegressionSummary
attribute), 341 |
| copy() | (pyspark.ml.pipeline.Pipeline
method), 390 | dispersion |
| copy() | (pyspark.ml.pipeline.PipelineModel
method), 391 | (pys-
park.ml.regression.GeneralizedLinearRegressionSummary
attribute), 335 |
| copy() | (pyspark.ml.tuning.CrossValidator
method), 394 | DistributedLDAModel (class in pys-
park.ml.clustering), 381 |
| copy() | (pyspark.ml.tuning.CrossValidatorModel
method), 395 | |
| copy() | (pyspark.ml.tuning.TrainValidationSplit
method), 396 | E |
| copy() | (pyspark.ml.tuning.TrainValidationSplitModel
method), 397 | |
| corr() | (pyspark.ml.stat.Correlation
method), 320 | estimatedDocConcentration() |
| Correlation (class in pyspark.ml.stat), 320 | | (pys-
park.ml.clustering.LDAModel
method), 380 |
| count() | (pyspark.ml.stat.Summarizer
method), 323 | evaluate() |
| CrossValidator (class in pyspark.ml.tuning),
393 | static | (pys-
park.ml.classification.LogisticRegressionModel
method), 351 |
| CrossValidatorModel (class in pys-
park.ml.tuning), 394 | static | evaluate() |
| | | (pys-
park.ml.evaluation.Evaluator
method), 397 |
| | | evaluate() |
| | | (pys-
park.ml.regression.GeneralizedLinearRegressionModel
method), 334 |
| | | evaluate() |
| | | (pys-
park.ml.regression.LinearRegressionModel
method), 340 |
| | | evaluateEachIteration() |
| | | (pys-
park.ml.classification.GBTClassificationModel
method), 360 |

| | | |
|---|--|---|
| evaluateEachIteration() | (pyspark.ml.regression.GBTRegressionModel method), 330 | GaussianMixtureSummary (class in pyspark.ml.clustering), 376 |
| Evaluator (class in pyspark.ml.evaluation), 397 | | gaussiansDF (pyspark.ml.clustering.GaussianMixtureModel attribute), 375 |
| explainedVariance | (pyspark.ml.regression.LinearRegressionSummary attribute), 341 | GBTClassificationModel (class in pyspark.ml.classification), 360 |
| | | GBTClassifier (class in pyspark.ml.classification), 358 |
| F | | GBTRegressionModel (class in pyspark.ml.regression), 330 |
| falsePositiveRateByLabel | (pyspark.ml.classification.LogisticRegressionSummary attribute), 352 | GBTRegressor (class in pyspark.ml.regression), 329 |
| featureImportances | (pyspark.ml.classification.DecisionTreeClassificationModel attribute), 357 | GeneralizedLinearRegression (class in pyspark.ml.regression), 331 |
| featureImportances | (pyspark.ml.classificationGBTClassificationModel attribute), 360 | GeneralizedLinearRegressionModel (class in pyspark.ml.regression), 334 |
| featureImportances | (pyspark.ml.classification.RandomForestClassificationModel attribute), 362 | GeneralizedLinearRegressionSummary (class in pyspark.ml.regression), 335 |
| featureImportances | (pyspark.ml.regression.DecisionTreeRegressionModel attribute), 328 | getAlpha() (pyspark.ml.recommendation.ALS method), 386 |
| featureImportances | (pyspark.ml.regression.GBTRegressionModel attribute), 331 | getBlockSize() (pyspark.ml.classification.MultilayerPerceptronClassifier method), 366 |
| featureImportances | (pyspark.ml.regression.RandomForestRegressionModel attribute), 345 | getCensorCol() (pyspark.ml.regression.AFTSurvivalRegression method), 326 |
| featuresCol | (pyspark.ml.classification.LogisticRegressionSummary attribute), 352 | getCheckpointFiles() (pyspark.ml.clustering.DistributedLDAModel method), 381 |
| featuresCol | (pyspark.ml.regression.LinearRegressionSummary attribute), 341 | getColdStartStrategy() (pyspark.ml.recommendation.ALS method), 386 |
| fMeasureByLabel() | (pyspark.ml.classification.LogisticRegressionSummary method), 352 | getDistanceMeasure() (pyspark.ml.clustering.BisectingKMeans method), 370 |
| fMeasureByThreshold | (pyspark.ml.classification.BinaryLogisticRegressionSummary attribute), 354 | getDistanceMeasure() (pyspark.ml.clustering.KMeans method), 372 |
| G | | getDistanceMeasure() (pyspark.ml.evaluation.ClusteringEvaluator method), 401 |
| GaussianMixture | (class in pyspark.ml.clustering), 374 | getDocConcentration() (pyspark.ml.clustering.LDA method), 377 |
| GaussianMixtureModel | (class in pyspark.ml.clustering), 375 | getDstCol() (pyspark.ml.clustering.PowerIterationClustering |

| | | |
|---|--|---|
| <i>method), 384</i> | <i>(pys-</i> | <i>getKeepLastCheckpoint () (pys-</i> |
| <code>getEpsilon()</code> (<i>pys-</i> | <i>park.ml.regression.LinearRegression</i> | <i>park.ml.clustering.LDA method), 378</i> |
| <i>method), 340</i> | | <i>(pys-</i> |
| <code>getFamily()</code> (<i>pys-</i> | <i>park.ml.classification.MultilayerPerceptronClassifier</i> | |
| <i>method), 349</i> | | <i>method), 366</i> |
| <code>getFamily()</code> (<i>pys-</i> | <i>park.ml.clustering.LDA method), 378</i> | <i>(pys-</i> |
| <i>method), 333</i> | | <i>getLearningOffset () (pys-</i> |
| <code>getFeatureIndex()</code> (<i>pys-</i> | <i>park.ml.clustering.LDA method), 378</i> | |
| <i>method), 338</i> | | <i>getLink () (pys-</i> |
| <code>getFinalStorageLevel()</code> (<i>pys-</i> | <i>park.ml.regression.GeneralizedLinearRegression</i> | <i>park.ml.regression.GeneralizedLinearRegression</i> |
| <i>method), 386</i> | | <i>method), 333</i> |
| <code>getImplicitPrefs()</code> (<i>pys-</i> | <i>method), 386</i> | <i>method), 333</i> |
| <i>method), 387</i> | | <i>getLinkPredictionCol () (pys-</i> |
| <code>getInitialWeights()</code> (<i>pys-</i> | <i>park.ml.regression.GeneralizedLinearRegression</i> | <i>park.ml.regression.GeneralizedLinearRegression</i> |
| <i>method), 366</i> | | <i>method), 333</i> |
| <code>getInitMode()</code> (<i>pyspark.ml.clustering.KMeans</i> | | <i>getLossType () (pys-</i> |
| <i>method), 372</i> | | <i>park.ml.classification.GBTClassifier</i> |
| <code>getInitMode()</code> (<i>pys-</i> | <i>method), 359</i> | |
| <i>park.ml.clustering.PowerIterationClustering</i> | | <i>getLossType () (pys-</i> |
| <i>method), 384</i> | | <i>park.ml.regression.GBTRegressor method),</i> |
| <code>getInitSteps()</code> (<i>pys-</i> | <i>330</i> | |
| <i>park.ml.clustering.KMeans</i> | | <i>getLowerBoundsOnCoefficients () (pys-</i> |
| <i>method), 372</i> | | <i>park.ml.classification.LogisticRegression</i> |
| <code>getIntermediateStorageLevel()</code> (<i>pys-</i> | | <i>method), 349</i> |
| <i>park.ml.recommendation(ALS</i> | | <i>getLowerBoundsOnIntercepts () (pys-</i> |
| <i>method), 387</i> | | <i>park.ml.classification.LogisticRegression</i> |
| <code>getIsotonic()</code> (<i>pys-</i> | | <i>method), 349</i> |
| <i>park.ml.regression.IsotonicRegression</i> | | <i>getMetricName () (pys-</i> |
| <i>method), 338</i> | | <i>park.ml.evaluation.BinaryClassificationEvaluator</i> |
| <code>getItemCol()</code> (<i>pyspark.ml.recommendation(ALS</i> | | <i>method), 398</i> |
| <i>method), 387</i> | | <i>getMetricName () (pys-</i> |
| <code>getK()</code> (<i>pyspark.ml.clustering.BisectingKMeans</i> | | <i>park.ml.evaluation.MulticlassClassificationEvaluator</i> |
| <i>method), 370</i> | | <i>method), 400</i> |
| <code>getK()</code> (<i>pyspark.ml.clustering.GaussianMixture</i> | | <i>getMetricName () (pys-</i> |
| <i>method), 375</i> | | <i>park.ml.evaluation.RegressionEvaluator</i> |
| <code>getK()</code> (<i>pyspark.ml.clustering.KMeans</i> | | <i>method), 399</i> |
| <i>method), 373</i> | | <i>getMinDivisibleClusterSize () (pys-</i> |
| <code>getK()</code> (<i>pyspark.ml.clustering.LDA</i> | | <i>park.ml.clustering.BisectingKMeans</i> |
| <i>method), 377</i> | | <i>method), 370</i> |
| <code>getK()</code> (<i>pyspark.ml.clustering.PowerIterationClustering</i> | | <i>getModelType () (pys-</i> |
| <i>method), 384</i> | | <i>park.ml.classification.NaiveBayes method),</i> |
| | | <i>364</i> |

| | | | |
|---|--|--|---|
| getNonnegative()
<code>park.ml.recommendation.ALS</code>
387 | (pys-
method), | <i>method)</i> , 349
getThresholds()
<code>park.ml.classification.LogisticRegression</code>
(pys-
method), | (pys-
method), 350 |
| getNumFolds()
<code>park.ml.tuning.CrossValidator</code>
394 | (pys-
method), | getTopicConcentration()
<code>park.ml.clustering.LDA method</code> , 378 | (pys-
method), |
| getNumItemBlocks()
<code>park.ml.recommendation.ALS</code>
387 | (pys-
method), | getTopicDistributionCol()
<code>park.ml.clustering.LDA method</code> , 378 | (pys-
method), |
| getNumUserBlocks()
<code>park.ml.recommendation.ALS</code>
387 | (pys-
method), | getTrainRatio()
<code>park.ml.tuning.TrainValidationSplit</code>
method), 396 | (pys-
method), |
| getOffsetCol()
<code>park.ml.regression.GeneralizedLinearRegression</code>
method), 333 | (pys-
method), | getUpperBoundsOnCoefficients()
<code>park.ml.classification.LogisticRegression</code>
method), 350 | (pys-
method), |
| getOptimizeDocConcentration()
<code>park.ml.clustering.LDA method</code> , 378 | (pys-
method), | getUpperBoundsOnIntercepts()
<code>park.ml.classification.LogisticRegression</code>
method), 350 | (pys-
method), |
| getOptimizer()
<code>pyspark.ml.clustering.LDA</code>
method), 378 | (pyspark.
ml.clustering.LDA
method), | getUserCol()
<code>pyspark.ml.recommendation.ALS</code>
method), 387 | (pys-
park.ml.recommendation.ALS
method), |
| getQuantileProbabilities()
<code>park.ml.regression.AFTSurvivalRegression</code>
method), 326 | (pys-
park.ml.regression.AFTSurvivalRegression
method), | getVariancePower()
<code>park.ml.regression.GeneralizedLinearRegression</code>
method), 333 | (pys-
park.ml.regression.GeneralizedLinearRegression
method), |
| getQuantilesCol()
<code>park.ml.regression.AFTSurvivalRegression</code>
method), 326 | (pys-
park.ml.regression.AFTSurvivalRegression
method), | H | |
| getRank()
<code>pyspark.ml.recommendation.ALS</code>
method), 387 | (pyspark.
ml.recommendation.ALS
method), | hasSummary
<code>park.ml.classification.LogisticRegressionModel</code>
attribute), 351 | (pys-
park.ml.classification.LogisticRegressionModel
attribute), |
| getRatingCol()
<code>park.ml.recommendation.ALS</code>
387 | (pys-
park.ml.recommendation.ALS
method), | hasSummary
<code>park.ml.clustering.BisectingKMeansModel</code>
attribute), 371 | (pys-
park.ml.clustering.BisectingKMeansModel
attribute), |
| getSmoothing()
<code>park.ml.classification.NaiveBayes</code>
method), 364 | (pys-
park.ml.classification.NaiveBayes
method), | hasSummary
<code>park.ml.clustering.GaussianMixtureModel</code>
attribute), 375 | (pys-
park.ml.clustering.GaussianMixtureModel
attribute), |
| getSrcCol()
<code>park.ml.clustering.PowerIterationClustering</code>
method), 384 | (pys-
park.ml.clustering.PowerIterationClustering
method), | hasSummary
<code>park.ml.clustering.KMeansModel</code>
attribute), 373 | (pys-
park.ml.clustering.KMeansModel
attribute), |
| getStagePath()
<code>park.ml.pipeline.PipelineSharedReadWrite</code>
static method), 392 | (pys-
park.ml.pipeline.PipelineSharedReadWrite
static method), | hasSummary
<code>park.ml.regression.GeneralizedLinearRegressionModel</code>
attribute), 335 | (pys-
park.ml.regression.GeneralizedLinearRegressionModel
attribute), |
| getStages()
<code>pyspark.ml.pipeline.Pipeline</code>
method), 390 | (pys-
pyspark.
ml.pipeline.Pipeline
method), | hasSummary
<code>park.ml.regression.LinearRegressionModel</code>
attribute), 340 | (pys-
park.ml.regression.LinearRegressionModel
attribute), |
| getStepSize()
<code>park.ml.classification.MultilayerPerceptronClassifier</code>
method), 366 | (pys-
park.ml.classification.MultilayerPerceptronClassifier
method), | intercept
<code>park.ml.classification.LinearSVCModel</code>
attribute), 347 | (pys-
park.ml.classification.LinearSVCModel
attribute), |
| getSubsamplingRate()
<code>park.ml.clustering.LDA</code>
method), 378 | (pys-
park.ml.clustering.LDA
method), | | |
| getThreshold()
<code>park.ml.classification.LogisticRegression</code> | (pys-
park.ml.classification.LogisticRegression | | |

```

intercept          (pys- LinearRegression (class      in      pys-
    park.ml.classification.LogisticRegressionModel      park.ml.regression), 338
    attribute), 351                                     LinearRegressionModel (class      in      pys-
                                                               LinearRegressionSummary (class      in      pys-
                                                               park.ml.regression), 341
intercept          (pys-      park.ml.regression), 340
    park.ml.regression.AFTSurvivalRegressionModel      AFTSurvivalRegressionSummary (class      in      pys-
    attribute), 327                                     park.ml.regression), 341
intercept          (pys-      LinearRegressionTrainingSummary
    park.ml.regression.GeneralizedLinearRegressionModel      (class      in      pyspark.ml.regression), 343
    attribute), 335                                     LinearSVC (class      in      pyspark.ml.classification),
                                                               346
intercept          (pys-      LinearSVCModel (class      in      pys-
    park.ml.regression.LinearRegressionModel      park.ml.classification), 347
    attribute), 340
interceptVector     (pys-      load () (pyspark.ml.pipeline.PipelineModelReader
    park.ml.classification.LogisticRegressionModel      method), 391
    attribute), 351                                     load () (pyspark.ml.pipeline.PipelineReader
                                                               method), 392
isDistributed()     (pys-      load () (pyspark.ml.pipeline.PipelineSharedReadWrite
    park.ml.clustering.LDAModel      static method), 392
    380
isLargerBetter()    (pys-      LocalLDAModel (class      in      pyspark.ml.clustering),
    park.ml.evaluation.Evaluator      method), 381
    398
IsotonicRegression (class      in      pys-
    park.ml.regression), 337
IsotonicRegressionModel (class      in      pys-
    park.ml.regression), 338
itemFactors         (pys-
    park.ml.recommendation(ALSModel
    attribute), 389
K
KMeans (class      in      pyspark.ml.clustering), 371
KMeansModel (class      in      pyspark.ml.clustering), 373
KolmogorovSmirnovTest (class      in      pys-
    park.ml.stat), 321
L
labelCol (pyspark.ml.classification.LogisticRegressionSummary()
    attribute), 352
labelCol (pyspark.ml.regression.LinearRegressionSummary
    attribute), 341
labels (pyspark.ml.classification.LogisticRegressionSummary
    attribute), 352
layers (pyspark.ml.classification.MultilayerPerceptronClassificationModel
    attribute), 367
LDA (class      in      pyspark.ml.clustering), 376
LDAModel (class      in      pyspark.ml.clustering), 380
M
max () (pyspark.ml.stat.Summarizer static method), 322
mean () (pyspark.ml.stat.Summarizer      static
    method), 323
meanAbsoluteError (pyspark.ml.regression.LinearRegressionSummary
    attribute), 343

```

| | |
|--|--|
| <i>attribute), 342</i> | <i>OneVsRestModel (class in pyspark.ml.classification), 369</i> |
| <i>meanSquaredError (pyspark.ml.regression.LinearRegressionSummary attribute), 342</i> | P |
| <i>metrics () (pyspark.ml.stat.Summarizer static method), 323</i> | <i>ParamGridBuilder (class in pyspark.ml.tuning), 392</i> |
| <i>min () (pyspark.ml.stat.Summarizer static method), 324</i> | <i>pi (pyspark.ml.classification.NaiveBayesModel attribute), 364</i> |
| <i>MulticlassClassificationEvaluator (class in pyspark.ml.evaluation), 399</i> | <i>Pipeline (class in pyspark.ml.pipeline), 390</i> |
| <i>MultilayerPerceptronClassificationModel (class in pyspark.ml.classification), 367</i> | <i>PipelineModel (class in pyspark.ml.pipeline), 391</i> |
| <i>MultilayerPerceptronClassifier (class in pyspark.ml.classification), 365</i> | <i>PipelineModelReader (class in pyspark.ml.pipeline), 391</i> |
| N | <i>PipelineModelWriter (class in pyspark.ml.pipeline), 391</i> |
| <i>NaiveBayes (class in pyspark.ml.classification), 363</i> | <i>PipelineReader (class in pyspark.ml.pipeline), 391</i> |
| <i>NaiveBayesModel (class in pyspark.ml.classification), 364</i> | <i>PipelineSharedReadWrite (class in pyspark.ml.pipeline), 392</i> |
| <i>normL1 () (pyspark.ml.stat.Summarizer static method), 324</i> | <i>PipelineWriter (class in pyspark.ml.pipeline), 392</i> |
| <i>normL2 () (pyspark.ml.stat.Summarizer static method), 324</i> | <i>PowerIterationClustering (class in pyspark.ml.clustering), 382</i> |
| <i>nullDeviance (pyspark.ml.regression.GeneralizedLinearRegressionSummary attribute), 335</i> | <i>pr (pyspark.ml.classification.BinaryLogisticRegressionSummary attribute), 354</i> |
| <i>numInstances (pyspark.ml.regression.GeneralizedLinearRegressionSummary attribute), 336</i> | <i>psm (pyspark.ml.classification.LogisticRegressionSummary attribute), 352</i> |
| <i>numInstances (pyspark.ml.regression.LinearRegressionSummary attribute), 342</i> | <i>psmByLabel (pyspark.ml.classification.LogisticRegressionSummary attribute), 352</i> |
| <i>numIterations (pyspark.ml.regression.GeneralizedLinearRegressionSummary attribute), 337</i> | <i>psmByThreshold (pyspark.ml.classification.BinaryLogisticRegressionSummary attribute), 354</i> |
| <i>numNonZeros () (pyspark.ml.stat.Summarizer static method), 324</i> | <i>predict () (pyspark.ml.regression.AFTSurvivalRegressionModel method), 327</i> |
| O | <i>predictionCol (pyspark.ml.regression.GeneralizedLinearRegressionSummary attribute), 336</i> |
| <i>objectiveHistory (pyspark.ml.classification.LogisticRegressionTrainingSummary attribute), 353</i> | <i>predictionCol (pyspark.ml.regression.LinearRegressionSummary attribute), 342</i> |
| <i>objectiveHistory (pyspark.ml.regression.LinearRegressionTrainingSummary attribute), 344</i> | <i>predictions (pyspark.ml.classification.LogisticRegressionSummary attribute), 352</i> |
| <i>OneVsRest (class in pyspark.ml.classification), 367</i> | <i>predictions (pyspark.ml.regression.GeneralizedLinearRegressionSummary attribute), 354</i> |

attribute), 336
predictions (pyspark.ml.regression.IsotonicRegressionModel attribute), 338
predictions (pyspark.ml.regression.LinearRegressionSummary attribute), 342
predictQuantiles () (pyspark.ml.regression.AFTSurvivalRegressionModel method), 327
probability (pyspark.ml.clustering.GaussianMixtureSummary attribute), 376
probabilityCol (pyspark.ml.classification.LogisticRegressionSummary attribute), 353
probabilityCol (pyspark.ml.clustering.GaussianMixtureSummary attribute), 376
pValues (pyspark.ml.regression.GeneralizedLinearRegressionSummary attribute), 337
pValues (pyspark.ml.regression.LinearRegressionSummary attribute), 342
pyspark.ml.classification (module), 346
pyspark.ml.clustering (module), 369
pyspark.ml.evaluation (module), 397
pyspark.ml.pipeline (module), 390
pyspark.ml.recommendation (module), 385
pyspark.ml.regression (module), 325
pyspark.ml.stat (module), 319
pyspark.ml.tuning (module), 392

R

r2 (pyspark.ml.regression.LinearRegressionSummary attribute), 342
r2adj (pyspark.ml.regression.LinearRegressionSummary attribute), 343
RandomForestClassificationModel (class in pyspark.ml.classification), 362
RandomForestClassifier (class in pyspark.ml.classification), 360
RandomForestRegressionModel (class in pyspark.ml.regression), 345
RandomForestRegressor (class in pyspark.ml.regression), 344
rank (pyspark.ml.recommendation(ALSModel attribute), 389

rank (pyspark.ml.regression.GeneralizedLinearRegressionSummary attribute), 336
read () (pyspark.ml.pipeline.Pipeline class method), 390
read () (pyspark.ml.pipeline.PipelineModel class method), 391
read () (pyspark.ml.tuning.CrossValidator class method), 394
read () (pyspark.ml.tuning.CrossValidatorModel class method), 395
read () (pyspark.ml.tuning.TrainValidationSplit class method), 396
read () (pyspark.ml.tuning.TrainValidationSplitModel class method), 397
recallByLabel (pyspark.ml.classification.LogisticRegressionSummary attribute), 353
recallByThreshold (pyspark.ml.classification.BinaryLogisticRegressionSummary attribute), 355
recommendForAllItems () (pyspark.ml.recommendation(ALSModel method), 389
recommendForAllUsers () (pyspark.ml.recommendation(ALSModel method), 389
recommendForItemSubset () (pyspark.ml.recommendation(ALSModel method), 389
recommendForUserSubset () (pyspark.ml.recommendation(ALSModel method), 389
RegressionEvaluator (class in pyspark.ml.evaluation), 399
residualDegreeOfFreedom (pyspark.ml.regression.GeneralizedLinearRegressionSummary attribute), 336
residualDegreeOfFreedomNull (pyspark.ml.regression.GeneralizedLinearRegressionSummary attribute), 336
residuals (pyspark.ml.regression.LinearRegressionSummary attribute), 343
residuals () (pyspark.ml.regression.GeneralizedLinearRegressionSummary method), 336
roc (pyspark.ml.classification.BinaryLogisticRegressionSummary attribute), 355

rootMeanSquaredError (pyspark.ml.regression.LinearRegressionSummary attribute), 343

Run on Databricks Community Cloud, 11

S

saveImpl () (pyspark.ml.pipeline.PipelineModelWriter method), 391

saveImpl () (pyspark.ml.pipeline.PipelineSharedReadWrite static method), 392

saveImpl () (pyspark.ml.pipeline.PipelineWriter method), 392

scale (pyspark.ml.regression.AFTSurvivalRegressionModel attribute), 327

scale (pyspark.ml.regression.LinearRegressionModel attribute), 340

Set up Spark on Cloud, 26

setAlpha () (pyspark.ml.recommendation.ALS method), 387

setBlockSize () (pyspark.ml.classification.MultilayerPerceptronClassifier method), 366

setCensorCol () (pyspark.ml.regression.AFTSurvivalRegression method), 326

setColdStartStrategy () (pyspark.ml.recommendation.ALS method), 387

setDistanceMeasure () (pyspark.ml.clustering.BisectingKMeans method), 370

setDistanceMeasure () (pyspark.ml.clustering.KMeans method), 373

setDistanceMeasure () (pyspark.ml.evaluation.ClusteringEvaluator method), 401

setDocConcentration () (pyspark.ml.clustering.LDA method), 378

setDstCol () (pyspark.ml.clustering.PowerIterationClustering method), 384

setEpsilon () (pyspark.ml.regression.LinearRegression method), 340

setFamily () (pyspark.ml.classification.LogisticRegression method), 350

setFamily () (pyspark.ml.regression.GeneralizedLinearRegression method), 334

setFeatureIndex () (pyspark.ml.regression.IsotonicRegression method), 338

setFeatureSubsetStrategy () (pyspark.ml.classificationGBTClassifier method), 359

setFeatureSubsetStrategy () (pyspark.ml.classification.RandomForestClassifier method), 362

setFeatureSubsetStrategy () (pyspark.ml.regression.GBTRegressor method), 330

setFeatureSubsetStrategy () (pyspark.ml.regression.RandomForestRegressor method), 345

setFinalStorageLevel () (pyspark.ml.recommendation.ALS method), 387

setImplicitPrefs () (pyspark.ml.recommendation.ALS method), 388

setInitialWeights () (pyspark.ml.classification.MultilayerPerceptronClassifier method), 367

setInitMode () (pyspark.ml.clustering.KMeans method), 373

setInitMode () (pyspark.ml.clustering.PowerIterationClustering method), 384

setInitSteps () (pyspark.ml.clustering.KMeans method), 373

setIntermediateStorageLevel () (pyspark.ml.recommendation.ALS method), 388

setIsotonic () (pyspark.ml.regression.IsotonicRegression method), 338

setItemCol () (pyspark.ml.recommendation.ALS method), 388

setK () (pyspark.ml.clustering.BisectingKMeans method), 370

| | |
|---|--|
| <code>setK()</code> (<i>pyspark.ml.clustering.GaussianMixture method</i>), 375 | <code>method)</code> , 399 |
| <code>setK()</code> (<i>pyspark.ml.clustering.KMeans method</i>), 373 | <code>setMinDivisibleClusterSize()</code> (<i>pyspark.ml.clustering.BisectingKMeans method</i>), 371 |
| <code>setK()</code> (<i>pyspark.ml.clustering.LDA method</i>), 378 | <code>setModelType()</code> (<i>pyspark.ml.classification.NaiveBayes method</i>), 364 |
| <code>setK()</code> (<i>pyspark.ml.clustering.PowerIterationClustering method</i>), 384 | <code>setNonnegative()</code> (<i>pyspark.ml.recommendation.ALS method</i>), 388 |
| <code>setKeepLastCheckpoint()</code> (<i>pyspark.ml.clustering.LDA method</i>), 379 | <code>setNumBlocks()</code> (<i>pyspark.ml.recommendation.ALS method</i>), 388 |
| <code>setLayers()</code> (<i>pyspark.ml.classification.MultilayerPerceptronClassifier method</i>), 367 | <code>setNumFolds()</code> (<i>pyspark.ml.tuning.CrossValidator method</i>), 394 |
| <code>setLearningDecay()</code> (<i>pyspark.ml.clustering.LDA method</i>), 379 | <code>setNumItemBlocks()</code> (<i>pyspark.ml.recommendation.ALS method</i>), 388 |
| <code>setLearningOffset()</code> (<i>pyspark.ml.clustering.LDA method</i>), 379 | <code>setNumUserBlocks()</code> (<i>pyspark.ml.recommendation.ALS method</i>), 388 |
| <code>setLink()</code> (<i>pyspark.ml.regression.GeneralizedLinearRegression method</i>), 334 | <code>setOffsetCol()</code> (<i>pyspark.ml.regression.GeneralizedLinearRegression method</i>), 334 |
| <code>setLinkPower()</code> (<i>pyspark.ml.regression.GeneralizedLinearRegression method</i>), 334 | <code>setOptimizeDocConcentration()</code> (<i>pyspark.ml.clustering.LDA method</i>), 379 |
| <code>setLinkPredictionCol()</code> (<i>pyspark.ml.regression.GeneralizedLinearRegression method</i>), 334 | <code>setOptimizer()</code> (<i>pyspark.ml.clustering.LDA method</i>), 379 |
| <code>setLossType()</code> (<i>pyspark.ml.classificationGBTClassifier method</i>), 359 | <code>setParams()</code> (<i>pyspark.ml.classification.DecisionTreeClassifier method</i>), 357 |
| <code>setLossType()</code> (<i>pyspark.ml.regressionGBTRegressor method</i>), 330 | <code>setParams()</code> (<i>pyspark.ml.classificationGBTClassifier method</i>), 359 |
| <code>setLowerBoundsOnCoefficients()</code> (<i>pyspark.ml.classification.LogisticRegression method</i>), 350 | <code>setParams()</code> (<i>pyspark.ml.classification.LinearSVC method</i>), 347 |
| <code>setLowerBoundsOnIntercepts()</code> (<i>pyspark.ml.classification.LogisticRegression method</i>), 350 | <code>setParams()</code> (<i>pyspark.ml.classification.LogisticRegression method</i>), 350 |
| <code>setMetricName()</code> (<i>pyspark.ml.evaluation.BinaryClassificationEvaluator method</i>), 398 | <code>setParams()</code> (<i>pyspark.ml.classification.MultilayerPerceptronClassifier method</i>), 367 |
| <code>setMetricName()</code> (<i>pyspark.ml.evaluation.ClusteringEvaluator method</i>), 401 | <code>setParams()</code> (<i>pyspark.ml.classification.NaiveBayes method</i>), 364 |
| <code>setMetricName()</code> (<i>pyspark.ml.evaluation.MulticlassClassificationEvaluator method</i>), 400 | <code>setParams()</code> (<i>pyspark.ml.classification.NaiveBayes method</i>), 364 |
| <code>setMetricName()</code> (<i>pyspark.ml.evaluation.RegressionEvaluator</i>) | |

| | | | |
|---|-------|--|-------|
| setParams () | (pys- | setParams () | (pys- |
| <i>park.ml.classification.OneVsRest method),</i> | | <i>park.ml.regression.IsotonicRegression</i> | |
| 368 | | <i>method), 338</i> | |
| setParams () | (pys- | setParams () | (pys- |
| <i>park.ml.classification.RandomForestClassifier</i> | | <i>park.ml.regression.LinearRegression</i> | |
| <i>method), 362</i> | | <i>method), 340</i> | |
| setParams () | (pys- | setParams () | (pys- |
| <i>park.ml.clustering.BisectingKMeans</i> | | <i>park.ml.regression.RandomForestRegressor</i> | |
| <i>method), 371</i> | | <i>method), 345</i> | |
| setParams () | (pys- | setParams () (pyspark.ml.tuning.CrossValidator | |
| <i>park.ml.clustering.GaussianMixture</i> | | <i>method), 394</i> | |
| <i>method), 375</i> | | setParams () | (pys- |
| setParams () (pyspark.ml.clustering.KMeans | | <i>park.ml.tuning.TrainValidationSplit</i> | |
| <i>method), 373</i> | | <i>method), 396</i> | |
| setParams () (pyspark.ml.clustering.LDA | | setQuantileProbabilities () | (pys- |
| <i>method), 379</i> | | <i>park.ml.regression.AFTSurvivalRegression</i> | |
| setParams () (pys- | | <i>method), 326</i> | |
| <i>park.ml.clustering.PowerIterationClustering</i> | | setQuantilesCol () | (pys- |
| <i>method), 384</i> | | <i>park.ml.regression.AFTSurvivalRegression</i> | |
| setParams () (pys- | | <i>method), 326</i> | |
| <i>park.ml.evaluation.BinaryClassificationEvaluator</i> | | setRank () (pyspark.ml.recommendation.ALS | |
| <i>method), 399</i> | | <i>method), 388</i> | |
| setParams () (pys- | | setRatingCol () | (pys- |
| <i>park.ml.evaluation.ClusteringEvaluator</i> | | <i>park.ml.recommendation.ALS</i> | |
| <i>method), 401</i> | | <i>method), 388</i> | |
| setParams () (pys- | | setSmoothing () | (pys- |
| <i>park.ml.evaluation.MulticlassClassificationEvaluator</i> | | <i>park.ml.classification.NaiveBayes</i> | |
| <i>method), 400</i> | | <i>method), 364</i> | |
| setParams () (pys- | | setSrcCol () | (pys- |
| <i>park.ml.evaluation.RegressionEvaluator</i> | | <i>park.ml.clustering.PowerIterationClustering</i> | |
| <i>method), 399</i> | | <i>method), 384</i> | |
| setParams () (pyspark.ml.pipeline.Pipeline | | setStages () (pyspark.ml.pipeline.Pipeline | |
| <i>method), 391</i> | | <i>method), 391</i> | |
| setParams () (pyspark.ml.recommendation.ALS | | setStepSize () | (pys- |
| <i>method), 388</i> | | <i>park.ml.classification.MultilayerPerceptronClassifier</i> | |
| setParams () (pys- | | <i>method), 367</i> | |
| <i>park.ml.regression.AFTSurvivalRegression</i> | | setSubsamplingRate () | (pys- |
| <i>method), 326</i> | | <i>park.ml.clustering.LDA</i> | |
| setParams () (pys- | | <i>method), 380</i> | |
| <i>park.ml.regression.DecisionTreeRegressor</i> | | setThreshold () | (pys- |
| <i>method), 328</i> | | <i>park.ml.classification.LogisticRegression</i> | |
| setParams () (pys- | | <i>method), 350</i> | |
| <i>park.ml.regression.GBTRegressor</i> | | setThresholds () | (pys- |
| <i>method), 330</i> | | <i>park.ml.classification.LogisticRegression</i> | |
| setParams () (pys- | | <i>method), 350</i> | |
| <i>park.ml.regression.GeneralizedLinearRegression</i> | | setTopicConcentration () | (pys- |
| <i>method), 334</i> | | <i>park.ml.clustering.LDA</i> | |
| | | <i>method), 380</i> | |
| | | setTopicDistributionCol () | (pys- |
| | | <i>park.ml.clustering.LDA</i> | |
| | | <i>method), 380</i> | |

T
 setTrainRatio() (pyspark.ml.tuning.TrainValidationSplit method), 396
 setUpperBoundsOnCoefficients() (pyspark.ml.classification.LogisticRegression method), 351
 setUpperBoundsOnIntercepts() (pyspark.ml.classification.LogisticRegression method), 351
 setUserCol() (pyspark.ml.recommendation.ALS method), 388
 setVariancePower() (pyspark.ml.regression.GeneralizedLinearRegression method), 334
 solver (pyspark.ml.regression.GeneralizedLinearRegressionTrainingSummary attribute), 337
 subModels (pyspark.ml.tuning.CrossValidatorModel attribute), 395
 subModels (pyspark.ml.tuning.TrainValidationSplitModel attribute), 397
 Summarizer (class in pyspark.ml.stat), 322
 summary (pyspark.ml.classification.LogisticRegressionModel attribute), 351
 summary (pyspark.ml.clustering.BisectingKMeansModel attribute), 371
 summary (pyspark.ml.clustering.GaussianMixtureModel attribute), 376
 summary (pyspark.ml.clustering.KMeansModel attribute), 374
 summary (pyspark.ml.regression.GeneralizedLinearRegressionModel attribute), 335
 summary (pyspark.ml.regression.LinearRegressionModel attribute), 340
 summary () (pyspark.ml.stat.SummaryBuilder method), 324
 SummaryBuilder (class in pyspark.ml.stat), 324

U
 userFactors (pyspark.ml.recommendation(ALSModel attribute), 390

V
 validateStages() (pyspark.ml.pipeline.PipelineSharedReadWrite static method), 392
 validationMetrics (pyspark.ml.tuning.TrainValidationSplitModel attribute), 397
 variance() (pyspark.ml.stat.Summarizer static method), 324

park.ml.tuning.TrainValidationSplit, 396
park.ml.classification.LogisticRegression, 351
park.ml.classification.GeneralizedLinearRegression, 334
park.ml.tuning.CrossValidatorModel, 395
park.ml.tuning.TrainValidationSplitModel, 397
park.ml.stat.SummaryBuilder, 324
park.ml.recommendation(ALSModel, 390
park.ml.pipeline.PipelineSharedReadWrite, 392
park.ml.tuning.TrainValidationSplitModel, 397
park.ml.stat.Summarizer, 324

vocabSize () (*pyspark.ml.clustering.LDAModel method*), 381

W

weightedFalsePositiveRate (pyspark.ml.classification.LogisticRegressionSummary attribute), 353

weightedFMeasure () (pyspark.ml.classification.LogisticRegressionSummary method), 353

weightedPrecision (pyspark.ml.classification.LogisticRegressionSummary attribute), 353

weightedRecall (pyspark.ml.classification.LogisticRegressionSummary attribute), 353

weightedTruePositiveRate (pyspark.ml.classification.LogisticRegressionSummary attribute), 353

weights (pyspark.ml.classification.MultilayerPerceptronClassificationModel attribute), 367

weights (pyspark.ml.clustering.GaussianMixtureModel attribute), 376

write () (pyspark.ml.pipeline.Pipeline method), 391

write () (pyspark.ml.pipeline.PipelineModel method), 391

write () (pyspark.ml.tuning.CrossValidator method), 394

write () (pyspark.ml.tuning.CrossValidatorModel method), 395

write () (pyspark.ml.tuning.TrainValidationSplit method), 396

write () (pyspark.ml.tuning.TrainValidationSplitModel method), 397