

mlmc_transport

April 8, 2020

\$ Notebook MLMC Transport \$

```
[1]: %matplotlib inline
import subprocess
import os
import sys
sys.path.append('../tools')
from plot_statistics import *
sys.path.append('../notebooks')
from tp_utilities import *
from vtk_utilities import *
import matplotlib.pyplot as plt
from starter import *
from mlmc_solution import *
sys.path.append('.')
from python.mlmc_mppy import mpp
```

```
[2]: mpp.build()
mpp.mute=True
kernels = 32
```

```
===== build sprng5 =====
```

```
-- libsprng.a found.
```

```
===== running cmake =====
```

```
-- Compiler option -Ofast
-- A library with BLAS API found.
-- A library with BLAS API found.
-- A library with LAPACK API found.
-- Using SuperLU 4.0
-- Time dependent problem
-- 3 dimensional problem
-- General transformations
-- Configuring done
-- Generating done
```

```
-- Build files have been written to: /home2/buchholz/mlmc/build
```

```
===== running make =====
```

```
[ 3%] Built target LIB_PS
[ 5%] Built target gtest
[11%] Built target gtest_main
[14%] Built target gmock
[36%] Built target MLMC
[46%] Built target gmock_main
[98%] Built target SRC
[100%] Built target MLMC-M++
```

```
$ Konvergenz Test $
```

```
[ ]: mpp.clean_data()
     mpp.run(kernels, config='mlmc_transport_ct')
     save("MLMCConvergenceTest/")
```

```
[ ]: mpp.print_convergence_table()
```

```
[ ]: mpp.show_convergence_table()
```

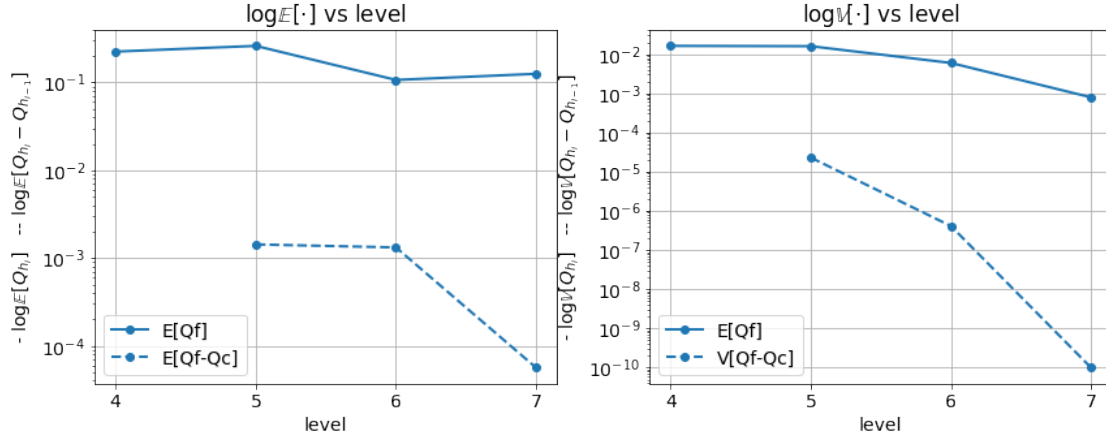
```
$ MLMC Experiment epsilon = 0.01 $
```

```
[ ]: mpp.clean_data()
     kwargs = {'epsilon': '0.01', 'initLevels': '4,5,6', 'initSampleAmount': '8,4,2'}
     mpp.run(kernels, config='mlmc_transport', kwargs=kwargs)
     save("MLMCExperiment/"+kwargs['epsilon']+"/")
```

```
[12]: statistics = read_log('../results/MLMCExperiment/0.01/log')
      display(statistics)
```

| | M | E[Qf-Qc] | E[Qf] | V[Qf-Qc] | V[Qf] | kurtosis | cost |
|---|-----|----------|----------|--------------|----------|----------|-----------|
| 1 | | | | | | | |
| 4 | 378 | 0.225017 | 0.225017 | 1.610760e-02 | 0.016108 | 2.991300 | 294912 |
| 5 | 6 | 0.001429 | 0.261486 | 2.279820e-05 | 0.015813 | 3.923450 | 2359300 |
| 6 | 2 | 0.001321 | 0.106957 | 4.096720e-07 | 0.005909 | 1.000000 | 18874400 |
| 7 | 2 | 0.000056 | 0.125627 | 1.000000e-10 | 0.000784 | 0.110661 | 150995000 |

```
[13]: plot_statistics(statistics, ['E[Qf]', 'V[Qf]'], None)
```



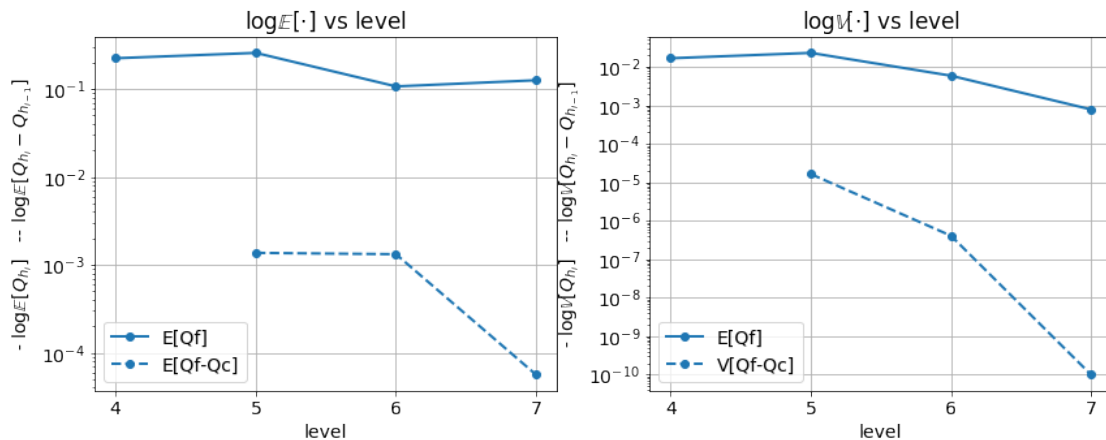
\$ MLMC Experiment epsilon = 0.005 \$

```
[ ]: mpp.clean_data()
kwargs = {'epsilon': '0.005', 'initLevels': '4,5,6', 'initSampleAmount': '8,4,2'}
mpp.run(kernels, config='mlmc_transport', kwargs=kwargs)
save("MLMCExperiment/"+kwargs['epsilon']+"/")
```

```
[14]: statistics = read_log('../results/MLMCExperiment/0.005/log')
display(statistics)
```

| | M | E[Qf-Qc] | E[Qf] | V[Qf-Qc] | V[Qf] | kurtosis | cost |
|---|------|----------|----------|--------------|----------|----------|-----------|
| 1 | | | | | | | |
| 4 | 1539 | 0.223618 | 0.223618 | 1.678900e-02 | 0.016789 | 2.863540 | 294912 |
| 5 | 22 | 0.001368 | 0.257407 | 1.640940e-05 | 0.023179 | 3.119730 | 2359300 |
| 6 | 2 | 0.001321 | 0.106957 | 4.096720e-07 | 0.005909 | 1.000000 | 18874400 |
| 7 | 2 | 0.000056 | 0.125627 | 1.000000e-10 | 0.000784 | 0.110661 | 150995000 |

```
[15]: plot_statistics(statistics, ['E[Qf]', 'V[Qf]'], None)
```



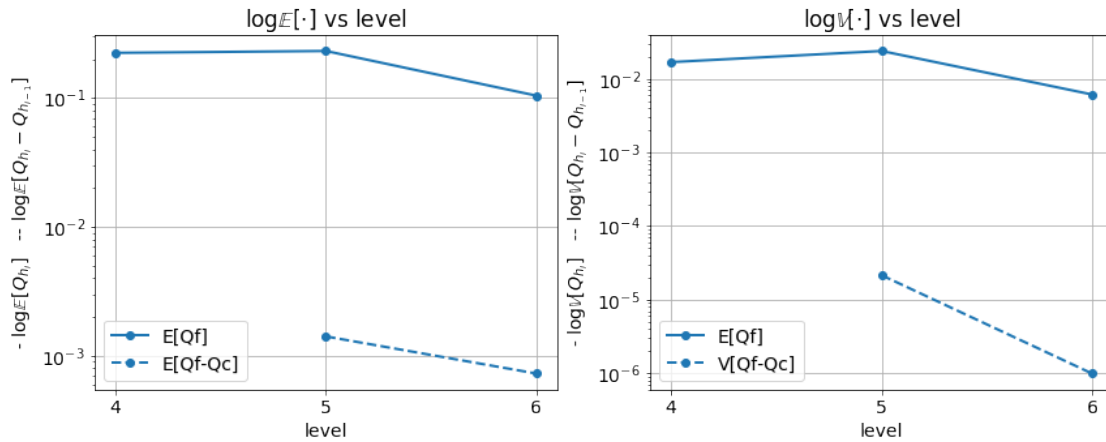
\$ MLMC Experiment epsilon = 0.003 \$

```
[ ]: mpp.clean_data()
      kwargs = {'epsilon': '0.003', 'initLevels': '4,5,6', 'initSampleAmount': '8,4,2'}
      mpp.run(kernels, config='mlmc_transport', kwargs=kwargs)
      save("MLMCExperiment/"+kwargs['epsilon']+"/")
```

```
[16]: statistics = read_log('../results/MLMCExperiment/0.003/log')
      display(statistics)
```

| | M | E[Qf-Qc] | E[Qf] | V[Qf-Qc] | V[Qf] | kurtosis | cost |
|---|------|----------|----------|--------------|----------|----------|----------|
| 1 | | | | | | | |
| 4 | 4374 | 0.224298 | 0.224298 | 1.693870e-02 | 0.016939 | 2.75002 | 294912 |
| 5 | 59 | 0.001411 | 0.231847 | 2.145810e-05 | 0.023991 | 2.59309 | 2359300 |
| 6 | 5 | 0.000727 | 0.104317 | 9.886560e-07 | 0.006146 | 1.66323 | 18874400 |

```
[17]: plot_statistics(statistics, ['E[Qf]', 'V[Qf]'], None)
```



\$ MLMC Experiment epsilon = 0.001 \$

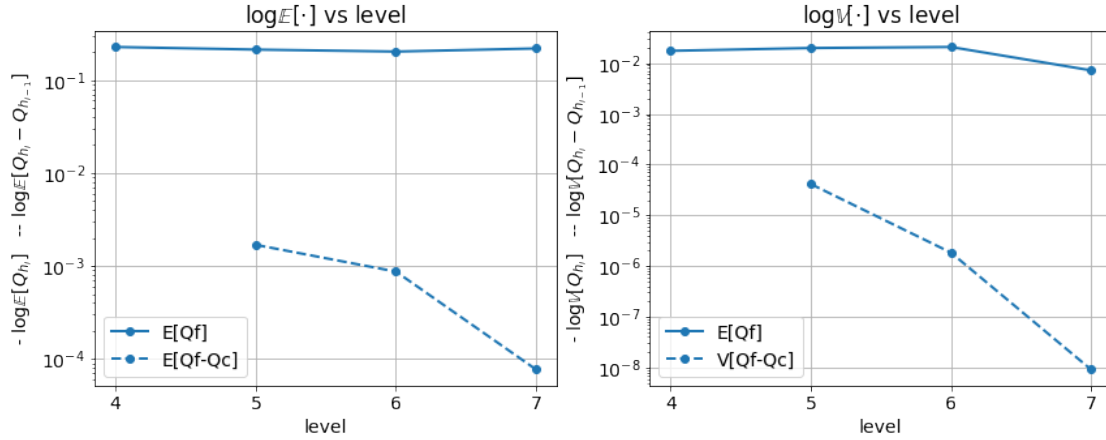
```
[ ]: mpp.clean_data()
      kwargs = {'epsilon': '0.001', 'initLevels': '4,5,6', 'initSampleAmount': '8,4,2'}
      mpp.run(kernels, config='mlmc_transport', kwargs=kwargs)
      save("MLMCExperiment/"+kwargs['epsilon']+"/")
```

```
[18]: statistics = read_log('../results/MLMCExperiment/0.001/log')
      display(statistics)
```

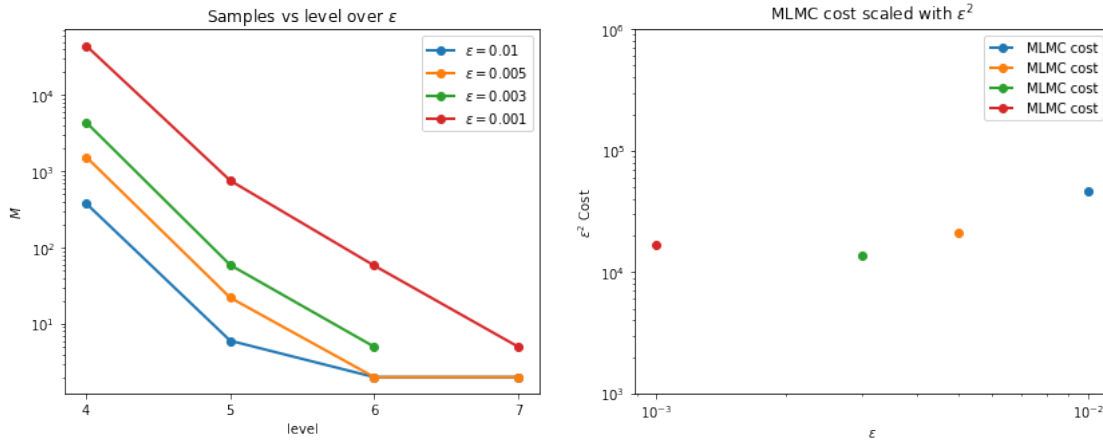
| | M | E[Qf-Qc] | E[Qf] | V[Qf-Qc] | V[Qf] | kurtosis | cost |
|---|---|----------|-------|----------|-------|----------|------|
| 1 | | | | | | | |

| | | | | | | | |
|---|-------|----------|----------|--------------|----------|---------|-----------|
| 4 | 44254 | 0.226394 | 0.226394 | 1.743050e-02 | 0.017431 | 2.65924 | 294912 |
| 5 | 755 | 0.001687 | 0.212340 | 4.127960e-05 | 0.019814 | 3.68994 | 2359300 |
| 6 | 58 | 0.000869 | 0.202110 | 1.839350e-06 | 0.020755 | 3.80032 | 18874400 |
| 7 | 5 | 0.000077 | 0.218324 | 9.122700e-09 | 0.007189 | 2.45257 | 150995000 |

```
[19]: plot_statistics(statistics, ['E[Qf]', 'V[Qf]', None])
```



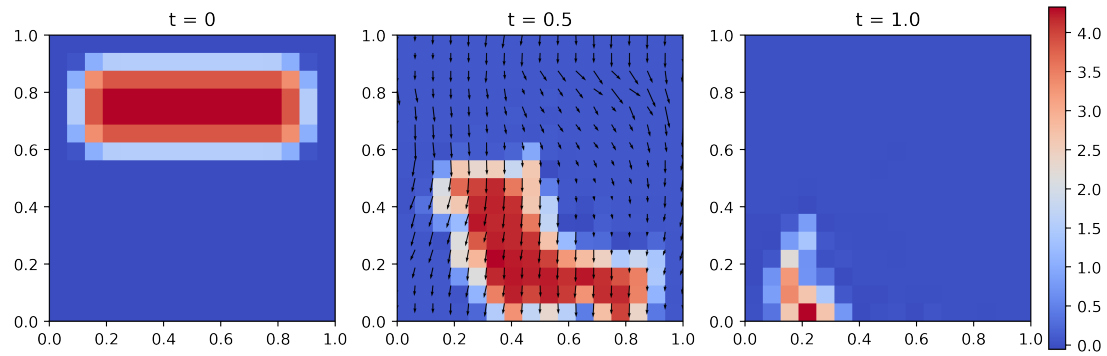
```
[3]: wd = '../results/MLMCExperiment/'
log_files = ['0.01/log', '0.005/log', '0.003/log', '0.001/log']
mpp.show_combined_mlmc_table(log_files= log_files, wd = wd )
```



\$ Beispielsamples\$

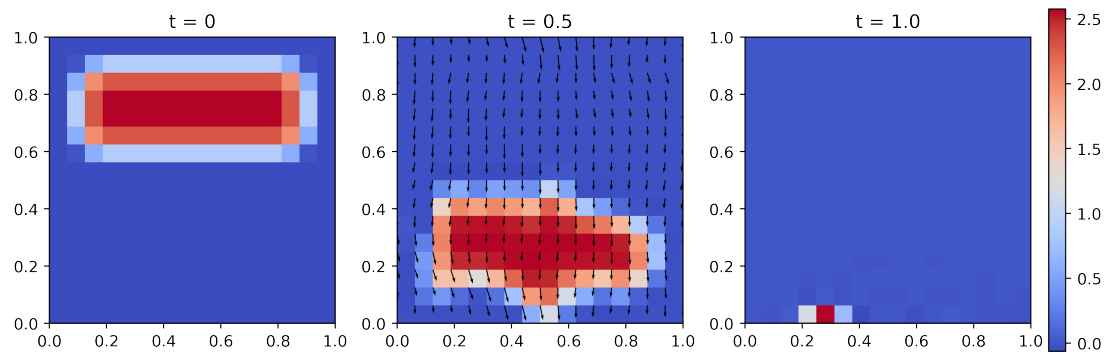
\$ Level 4 (baselevel) \$

```
[4]: solution_3(wd="../results/MLMCEExperiment/0.001/vtk/",sample="sample_4_1/
↪",quiver_filter=1,quiver_scale=0.10)
```

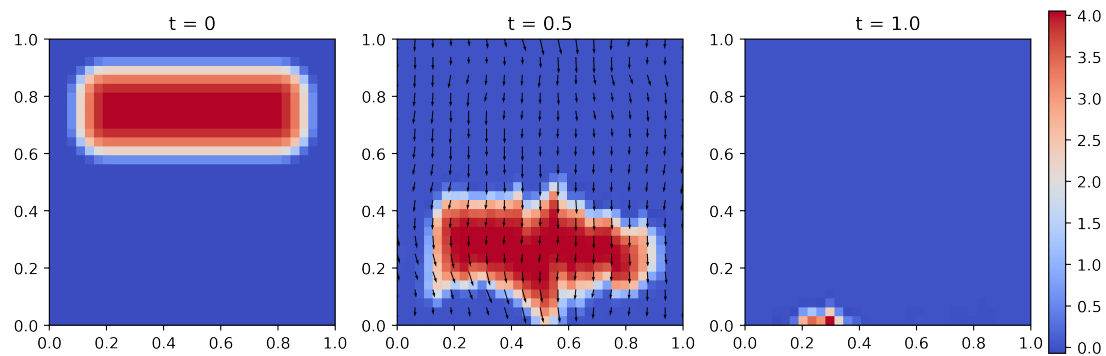


\$ Level 5 (und zugehöriges Vergleichssample auf Level 4) \$

```
[5]: solution_3(wd="../results/MLMCEExperiment/0.001/vtk/",sample="sample_coarse_5_1/
↪",quiver_filter=1,quiver_scale=0.10)
```

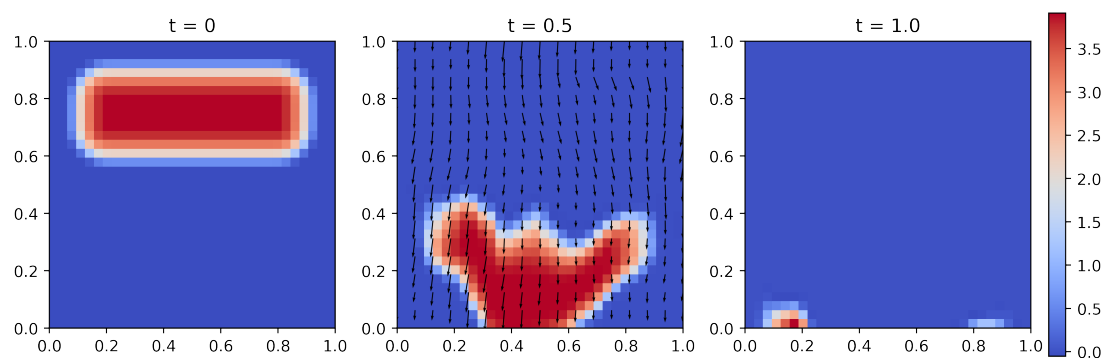


```
[6]: solution_3(wd="../results/MLMCEExperiment/0.001/vtk/",sample="sample_5_1/
↪",quiver_filter=2,quiver_scale=0.10)
```

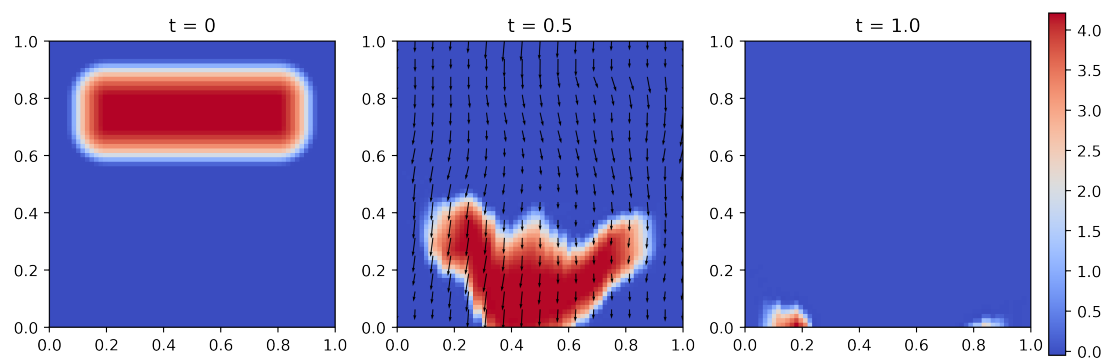


\$ Level 6 (und zugehöriges Vergleichssample auf Level 5) \$

```
[7]: solution_3(wd="../results/MLMCEExperiment/0.01/vtk/",sample="sample_coarse_6_0/
↪",quiver_filter=2,quiver_scale=0.12)
```

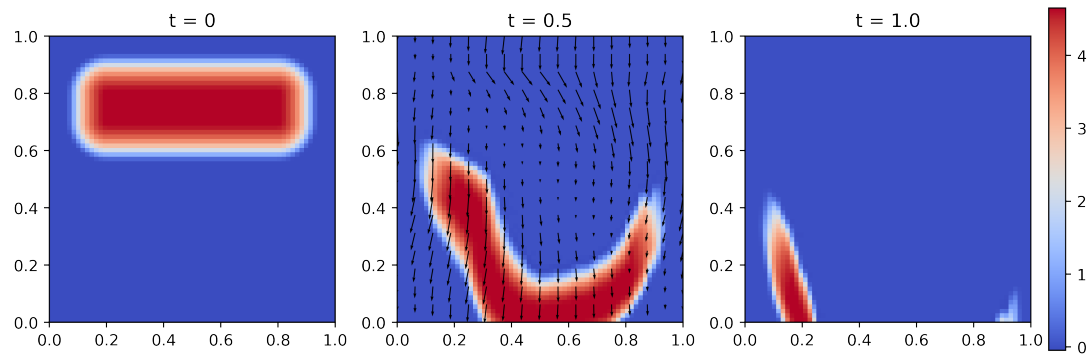


```
[8]: solution_3(wd="../results/MLMCEExperiment/0.01/vtk/",sample="sample_6_0/
↪",quiver_filter=4,quiver_scale=0.12)
```

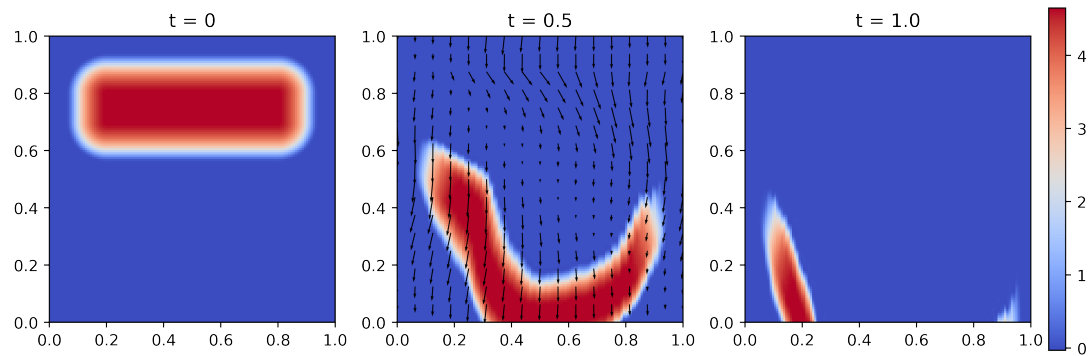


\$ Level 7 (und zugehöriges Vergleichssample auf Level 6) \$

```
[9]: solution_3(wd="../../results/MLMCEExperiment/0.01/vtk/",sample="sample_coarse_7_0/
↪",quiver_filter=4,quiver_scale=0.12)
```



```
[10]: solution_3(wd="../../results/MLMCEExperiment/0.01/vtk/",sample="sample_7_0/
↪",quiver_filter=8,quiver_scale=0.12)
```



```
[ ]: result = tail("../../results/MLMCEExperiment/0.001/log",n=22)
levels, sample_amount = parse_nofsamples(result)
mlmcmeshes(working_dir="../../results/MLMCEExperiment/0.001/vtk/
↪",levels=levels,sample_amount=sample_amount)
```

\$ Lösung im MLMC Sinne basierend auf gegebenem Zielfunktional (hier Masse zum Zeitpunkt $t = 1.0$)\$


```
[ ]: solution_3(wd="../results/MLMCExperiment/0.001/vtk/",sample="mlmc/  
↪",quiver_filter=8,quiver_scale=0.12)
```

```
[ ]:
```