# mlmc\_transport

# April 12, 2020

## \$ Notebook MLMC Transport \$

```
[1]: %matplotlib inline
    import subprocess
    import os
    import sys
    sys.path.append('../tools')
    from plot_statistics import *
    sys.path.append('../notebooks')
    from tp_utilities import *
    from vtk_utilities import *
    import matplotlib.pyplot as plt
    from starter import *
    from mlmc_solution import *
    sys.path.append('..')
    from python.mlmc_mppy import mpp
[2]: mpp.build()
    mpp.mute=True
    kernels = 32
    ======= build sprng5 ========
    -- libsprng.a found.
    ======== running cmake =========
    -- Compiler option -Ofast
    -- A library with BLAS API found.
    -- A library with BLAS API found.
    -- A library with LAPACK API found.
    -- Using SuperLU 4.0
    -- Time dependent problem
    -- 3 dimensional problem
    -- General transformations
    -- Configuring done
    -- Generating done
```

#### -- Build files have been written to: /home2/buchholz/mlmc/build

```
[ 5%] Built target gtest
[ 5%] Built target LIB_PS
[ 16%] Built target gtest_main
[ 19%] Built target gmock
[ 31%] Built target MLMC
[ 49%] Built target gmock_main
[ 98%] Built target SRC
[100%] Built target MLMC-M++
```

## \$ Konvergenz Test \$

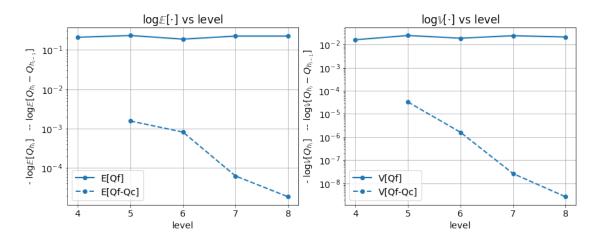
```
[3]: mpp.clean_data()
    mpp.run(kernels, config='mlmc_transport_ct')
    save("MLMCConvergenceTest/")
```

## Created Folder

# [4]: mpp.print\_convergence\_table()

```
E[Qf-Qc]
                     E[Qf]
                                V[Qf-Qc]
                                             V[Qf]
                                                    kurtosis
                                                                       cost
1
4
  100
       0.206865 0.206865
                            1.594270e-02
                                          0.015943
                                                      2.49970
                                                               2.949120e+05
5
  100
       0.001558 0.229484
                            3.282100e-05
                                          0.024385
                                                      4.00513
                                                               2.359300e+06
       0.000817 0.185469
6
  100
                            1.615470e-06
                                          0.018631
                                                      3.99497
                                                               1.887440e+07
7
       0.000063 0.221811
                            2.657520e-08
                                                               1.509950e+08
  100
                                          0.023902
                                                      2.75915
       0.000019 0.221853
                            2.636770e-09
                                                               1.207960e+09
  100
                                          0.020987
                                                      3.37952
```

## [5]: mpp.show\_convergence\_table()



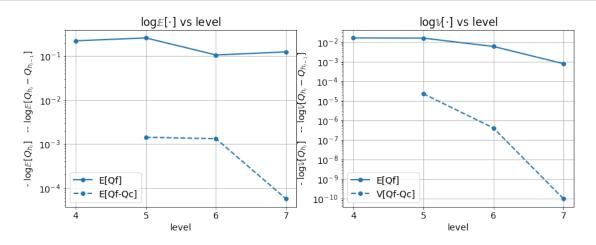
## MLMC Experiment epsilon = 0.01

```
[6]: mpp.clean_data()
   kwargs = {'epsilon':'0.01','initLevels':'4,5,6','initSampleAmount':'8,4,2'}
   mpp.run(kernels, config='mlmc_transport',kwargs=kwargs)
   save("MLMCExperiment/"+kwargs['epsilon']+"/")
```

```
[7]: statistics = read_log('../results/MLMCExperiment/0.01/log') display(statistics)
```

	M	E[Qf-Qc]	E[Qf]	V[Qf-Qc]	V[Qf]	kurtosis	cost
1							
4	378	0.225017	0.225017	1.610760e-02	0.016108	2.991300	294912
5	6	0.001429	0.261486	2.279820e-05	0.015813	3.923450	2359300
6	2	0.001321	0.106957	4.096720e-07	0.005909	1.000000	18874400
7	2	0.000056	0.125627	1.000000e-10	0.000784	0.110661	150995000

# [8]: plot\_statistics(statistics, ['E[Qf]','V[Qf]'], None)



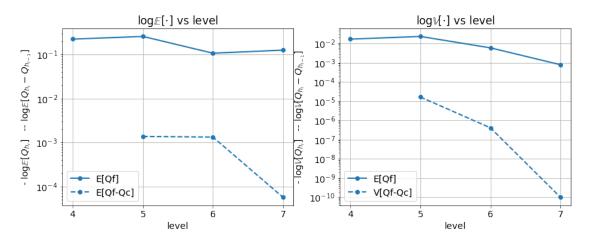
## \$ MLMC Experiment epsilon = 0.005 \$

```
[9]: mpp.clean_data()
   kwargs = {'epsilon':'0.005','initLevels':'4,5,6','initSampleAmount':'8,4,2'}
   mpp.run(kernels, config='mlmc_transport',kwargs=kwargs)
   save("MLMCExperiment/"+kwargs['epsilon']+"/")
```

```
M E[Qf-Qc] E[Qf] V[Qf-Qc] V[Qf] kurtosis cost
1
4 1539 0.223618 0.223618 1.678900e-02 0.016789 2.863540 294912
```

```
5
     22 0.001368
                   0.257407
                             1.640940e-05
                                           0.023179
                                                     3.119730
                                                                 2359300
6
      2 0.001321
                   0.106957
                             4.096720e-07
                                           0.005909
                                                     1.000000
                                                                18874400
7
        0.000056
                   0.125627
                             1.000000e-10
                                           0.000784
                                                     0.110661
                                                               150995000
```

# [11]: plot\_statistics(statistics, ['E[Qf]','V[Qf]'], None)



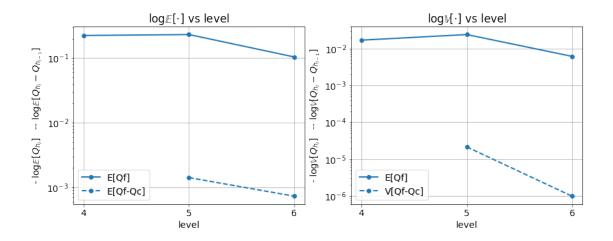
# MLMC Experiment epsilon = 0.003

```
[12]: mpp.clean_data()
   kwargs = {'epsilon':'0.003','initLevels':'4,5,6','initSampleAmount':'8,4,2'}
   mpp.run(kernels, config='mlmc_transport',kwargs=kwargs)
   save("MLMCExperiment/"+kwargs['epsilon']+"/")
```

```
[13]: statistics = read_log('../results/MLMCExperiment/0.003/log') display(statistics)
```

```
M E[Qf-Qc]
                      E[Qf]
                                 V[Qf-Qc]
                                               V[Qf]
                                                      kurtosis
                                                                    cost
1
4
  4374
         0.224298
                   0.224298
                             1.693870e-02
                                           0.016939
                                                       2.75002
                                                                  294912
5
                                                       2.59309
     59
         0.001411
                   0.231847
                             2.145810e-05
                                            0.023991
                                                                 2359300
6
      5 0.000727 0.104317 9.886560e-07
                                           0.006146
                                                       1.66323
                                                                18874400
```

```
[14]: plot_statistics(statistics, ['E[Qf]','V[Qf]'], None)
```



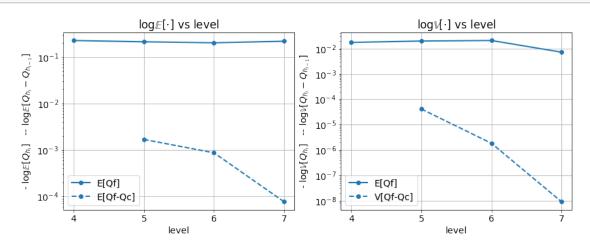
# MLMC Experiment epsilon = 0.001 \$

```
[15]: mpp.clean_data()
   kwargs = {'epsilon':'0.001','initLevels':'4,5,6','initSampleAmount':'8,4,2'}
   mpp.run(kernels, config='mlmc_transport',kwargs=kwargs)
   save("MLMCExperiment/"+kwargs['epsilon']+"/")
```

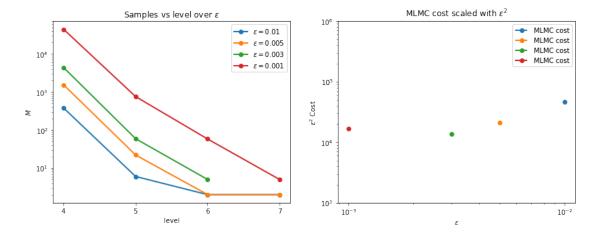
```
[16]: statistics = read_log('../results/MLMCExperiment/0.001/log')
display(statistics)
```

```
E[Qf-Qc]
                        E[Qf]
                                   V[Qf-Qc]
                                                 V[Qf]
                                                        kurtosis
                                                                         cost
1
4
   44254
          0.226394
                     0.226394
                               1.743050e-02
                                              0.017431
                                                          2.65924
                                                                      294912
5
     755
          0.001687
                     0.212340
                               4.127960e-05
                                              0.019814
                                                          3.68994
                                                                     2359300
6
      58
          0.000869
                     0.202110
                               1.839350e-06
                                              0.020755
                                                          3.80032
                                                                    18874400
7
          0.000077
                     0.218324
                               9.122700e-09
                                              0.007189
                                                          2.45257
                                                                   150995000
```

# [17]: plot\_statistics(statistics, ['E[Qf]','V[Qf]'], None)

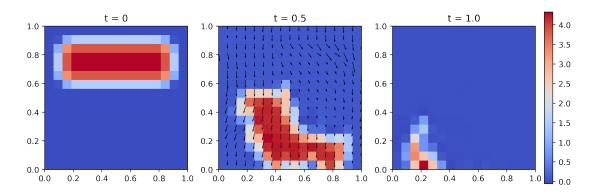


```
[18]: wd = '/../.results/MLMCExperiment/'
log_files = ['0.01/log','0.005/log','0.003/log','0.001/log']
mpp.show_combined_mlmc_table(log_files= log_files, wd = wd )
```

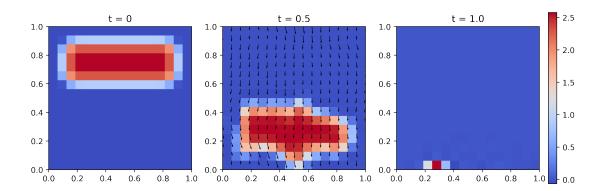


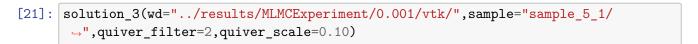
# \$ Beispielsamples\$

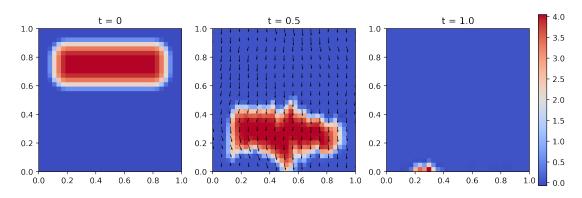
# \$ Level 4 (baselevel) \$



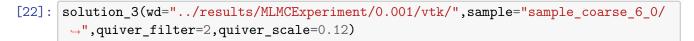
# \$ Level 5 (und zugehöriges Vergleichssample auf Level 4) \$

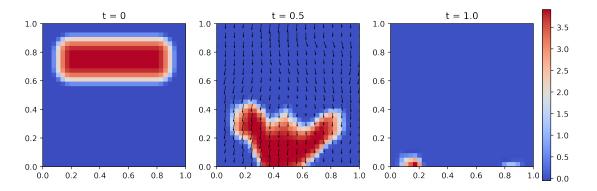


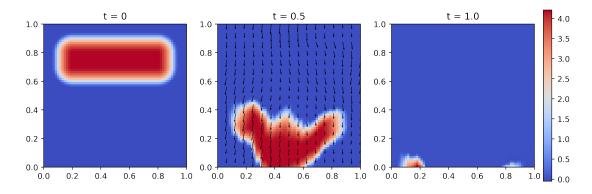




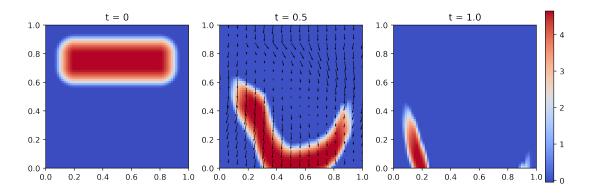
# \$ Level 6 (und zugehöriges Vergleichssample auf Level 5) \$

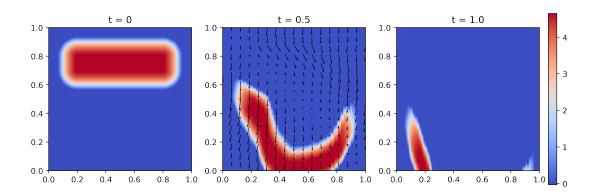






# \$ Level 7 (und zugehöriges Vergleichssample auf Level 6) \$



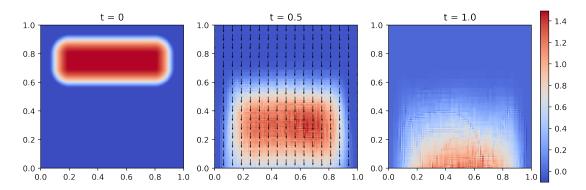


# \$ Lösung im MLMC Sinne basierend auf gegegebem Zielfunktional (hier Masse zum Zeitpunkt t = 1.0)\$

```
[26]: result = tail("../results/MLMCExperiment/0.001/log",n=22)
levels, sample_amount = parse_nofsamples(result)
mlmcmeshes(working_dir="../results/MLMCExperiment/0.001/vtk/

\[ \to ", levels=levels, sample_amount=sample_amount) \]
```





[28]: