## Copyright Notice

These slides are distributed under the Creative Commons License.

<u>DeepLearning.Al</u> makes these slides available for educational purposes. You may not use or distribute these slides for commercial purposes. You may make copies of these slides and use or distribute them for educational purposes as long as you cite <u>DeepLearning.Al</u> as the source of the slides.

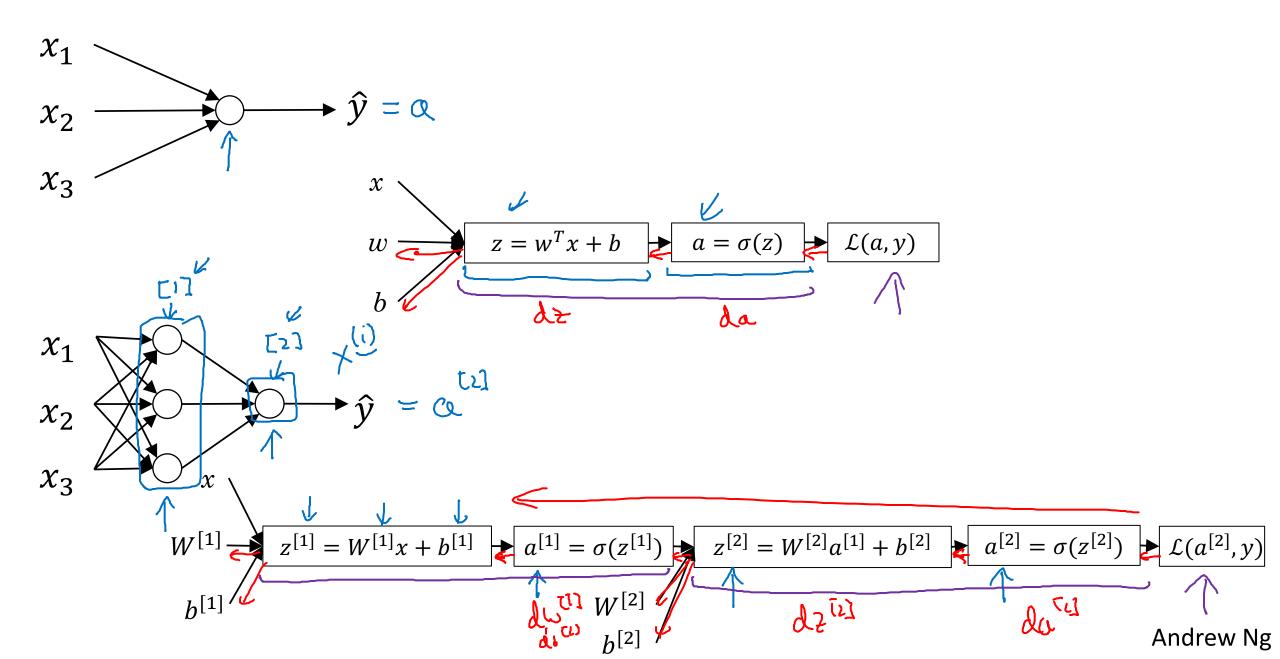
For the rest of the details of the license, see <a href="https://creativecommons.org/licenses/by-sa/2.0/legalcode">https://creativecommons.org/licenses/by-sa/2.0/legalcode</a>



## One hidden layer Neural Network

# Neural Networks Overview

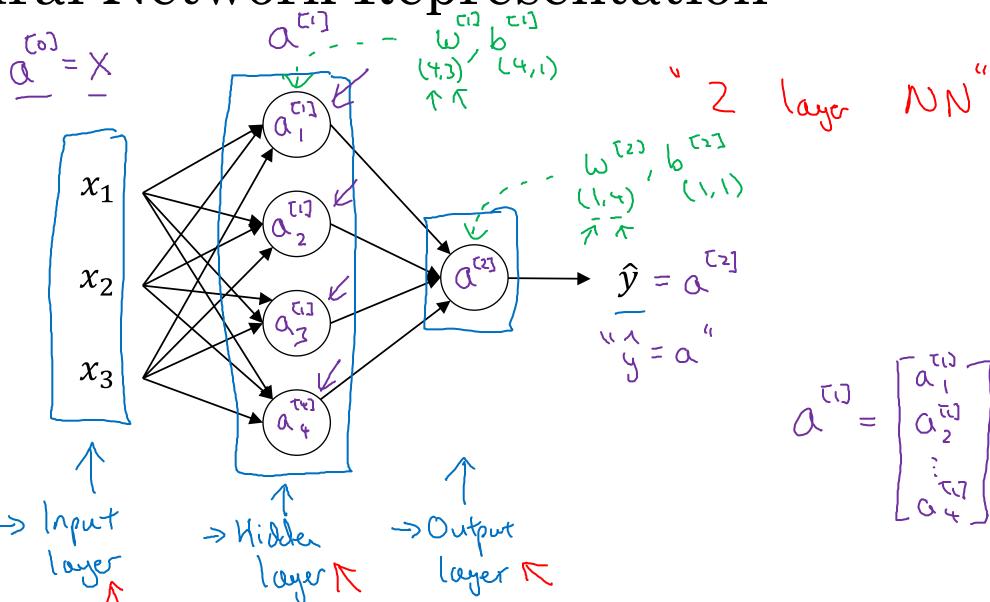
#### What is a Neural Network?





# One hidden layer Neural Network

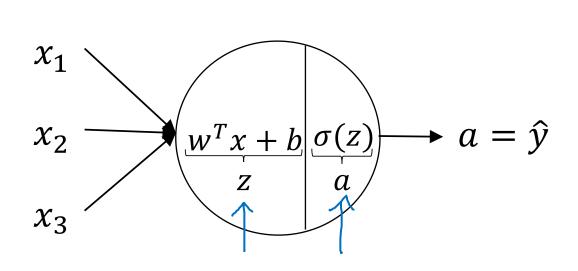
Neural Network Representation



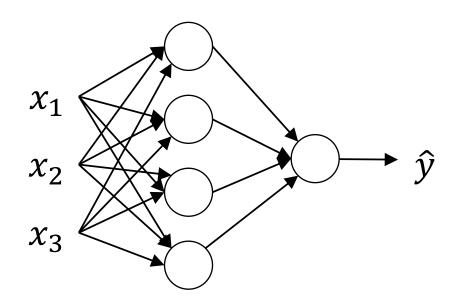


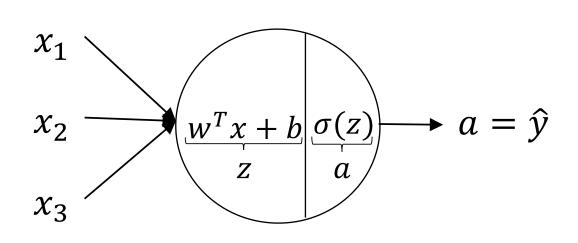
## One hidden layer Neural Network

Computing a Neural Network's Output

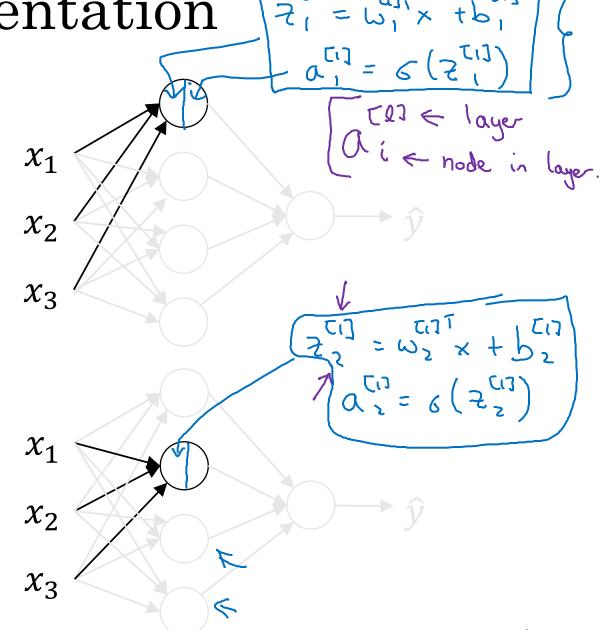


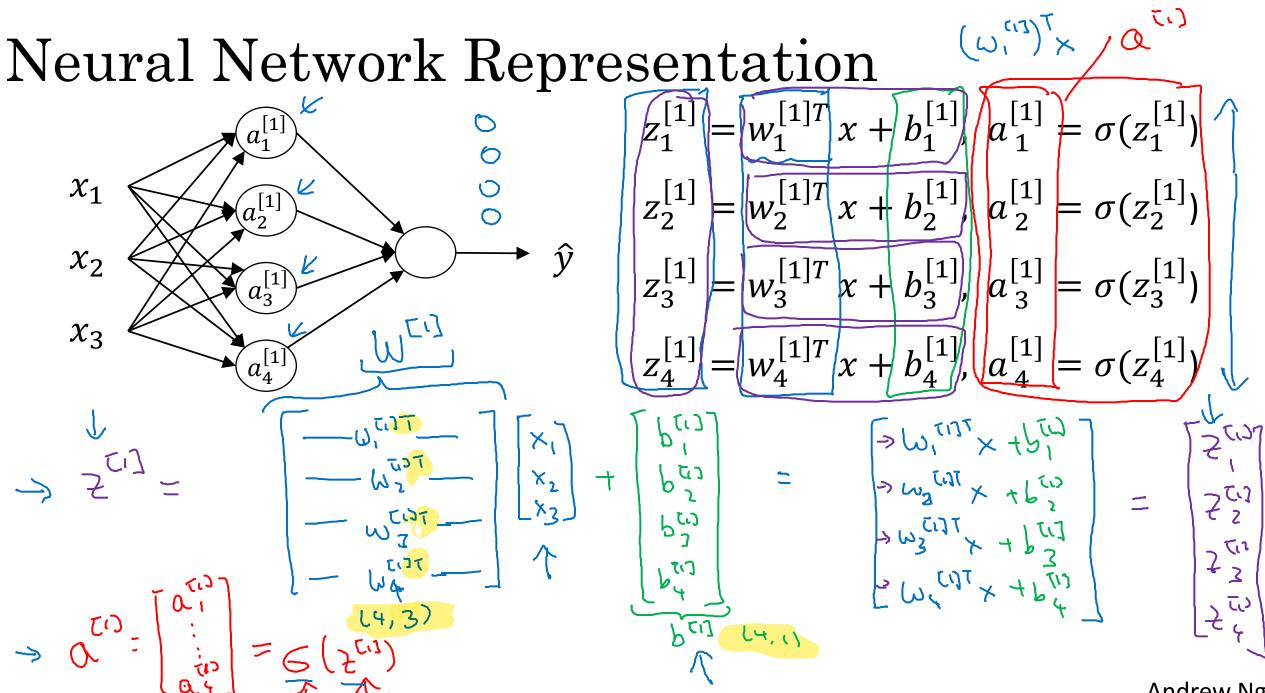
$$z = w^T x + b$$
$$a = \sigma(z)$$





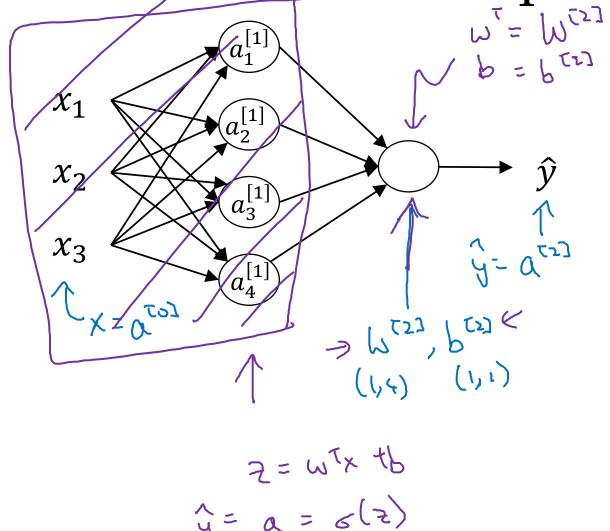
$$z = w^T x + b$$
$$a = \sigma(z)$$





Andrew Ng

Neural Network Representation learning



Given input x:

$$z^{[1]} = W^{[1]} + b^{[1]}$$

$$a^{[1]} = \sigma(z^{[1]})$$

$$a^{[1]} = w^{[2]} a^{[1]} + b^{[2]}$$

$$a^{[2]} = w^{[2]} a^{[1]} + b^{[2]}$$

$$a^{[2]} = \sigma(z^{[2]})$$

$$a^{[2]} = \sigma(z^{[2]})$$

$$a^{[2]} = \sigma(z^{[2]})$$

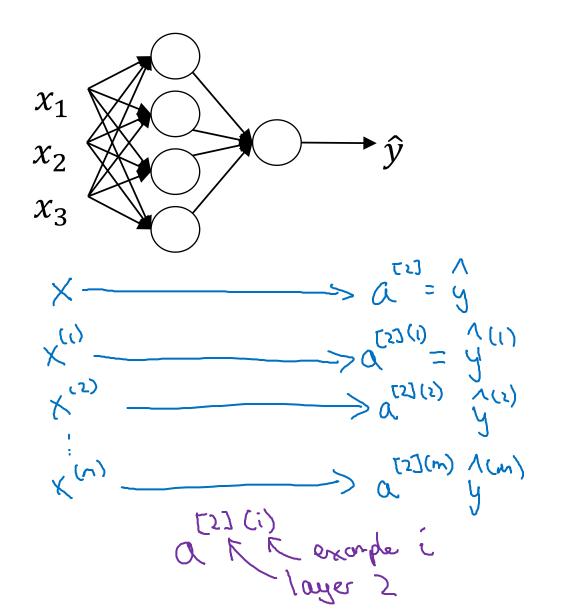
Changed:

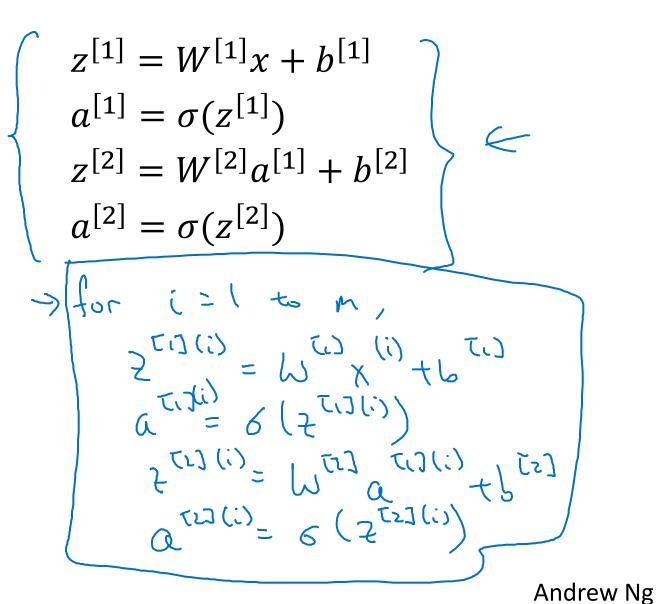


# One hidden layer Neural Network

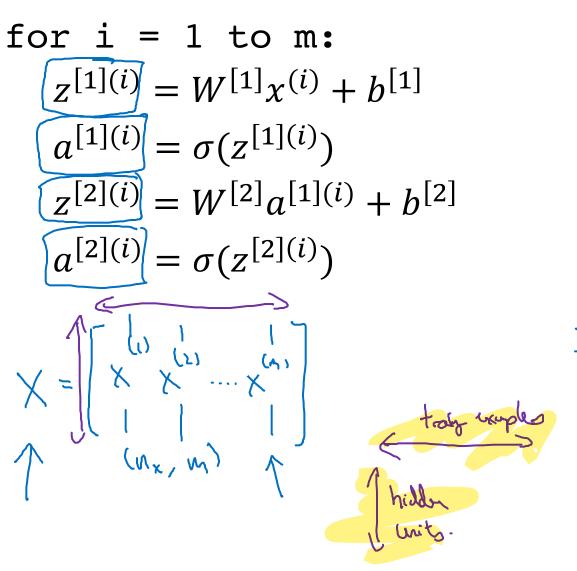
Vectorizing across multiple examples

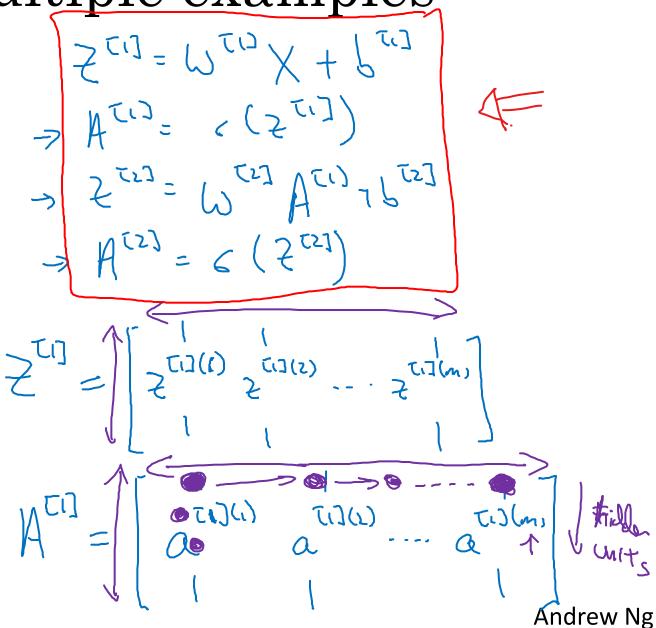
### Vectorizing across multiple examples





Vectorizing across multiple examples



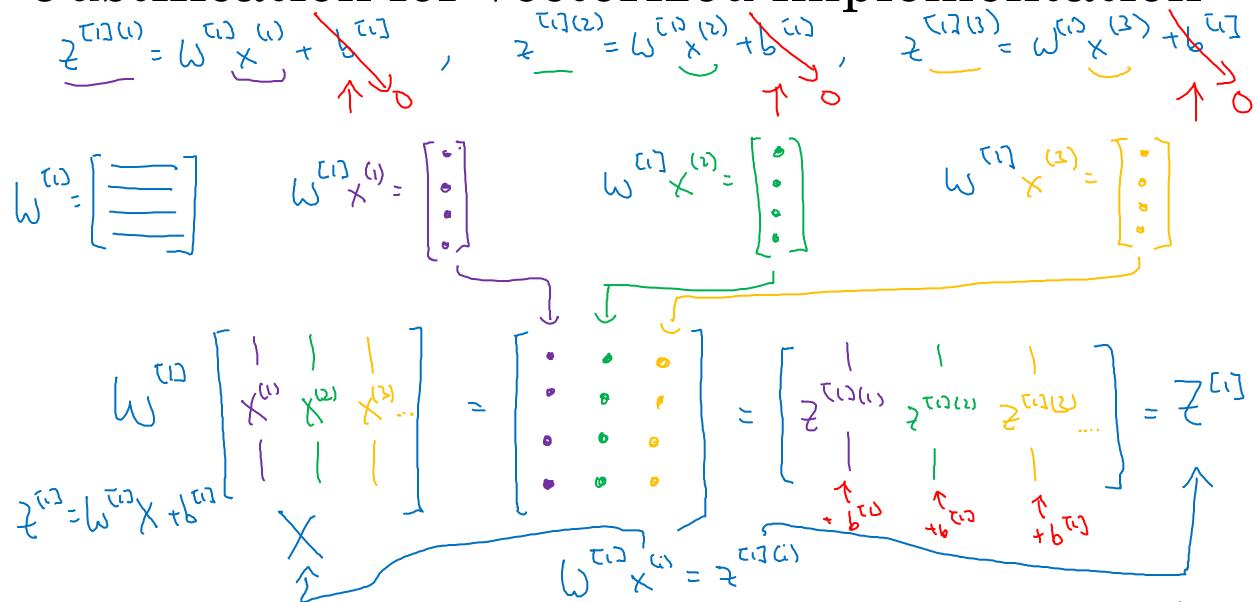




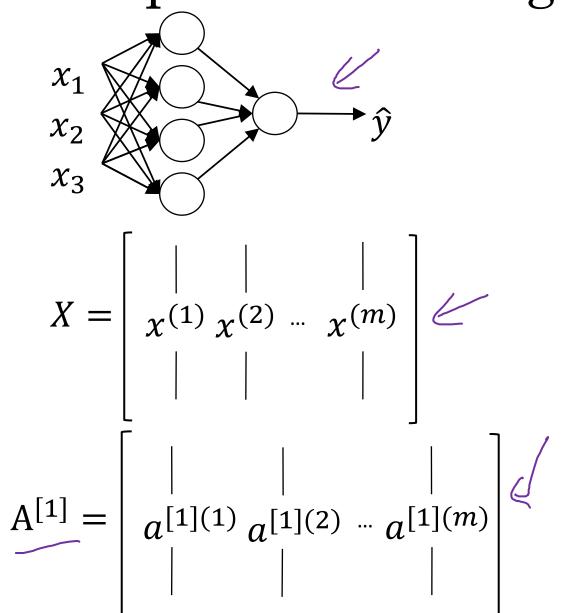
# One hidden layer Neural Network

Explanation for vectorized implementation

Justification for vectorized implementation



## Recap of vectorizing across multiple examples



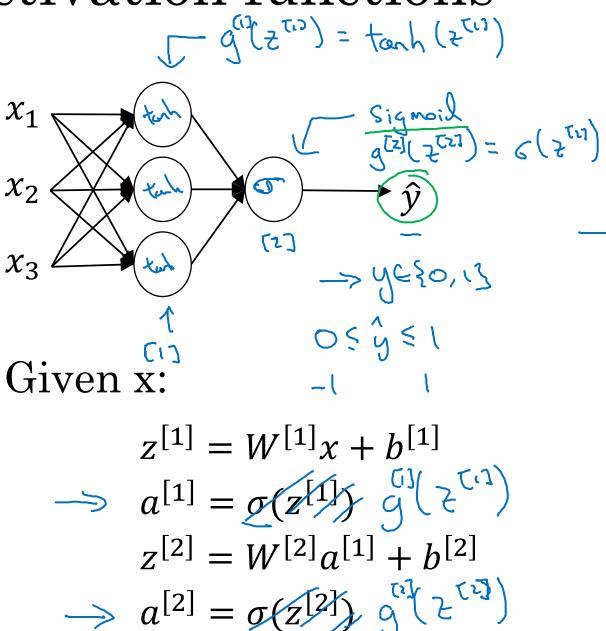
```
for i = 1 to m
                                     + z^{[1](i)} = W^{[1]}x^{(i)} + b^{[1]}
                                    \Rightarrow a^{[1](i)} = \sigma(z^{[1](i)})
                                  \Rightarrow z^{[2](i)} = W^{[2]}a^{[1](i)} + b^{[2]}
                            \Rightarrow a^{[2](i)} = \sigma(z^{[2](i)})
                                                                                                                                                                                                                      \chi = \alpha^{(0)} \quad \chi = \alpha^{(0)} \quad \chi^{(0)} = \alpha^{(0)
 Z^{[1]} = W^{[1]}X + b^{[1]} \leftarrow W^{[1]}X^{(0)} + b^{[1]}
         A^{[1]} = \sigma(Z^{[1]})
Z^{[2]} = W^{[2]}A^{[1]} + b^{[2]}
     A^{[2]} = \sigma(Z^{[2]})
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               Andrew Ng
```

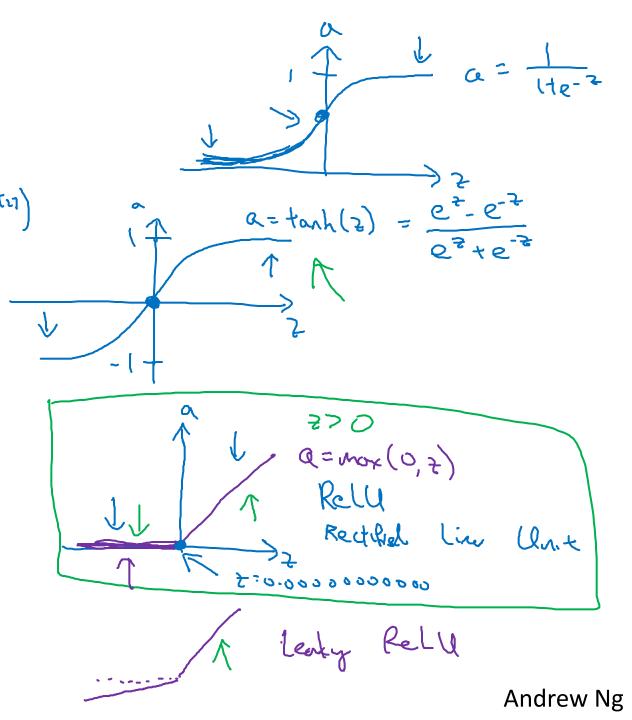


## One hidden layer Neural Network

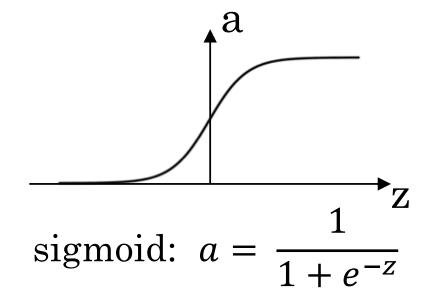
#### Activation functions

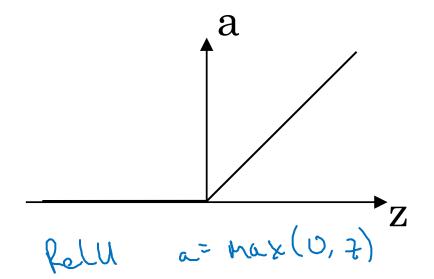
#### Activation functions

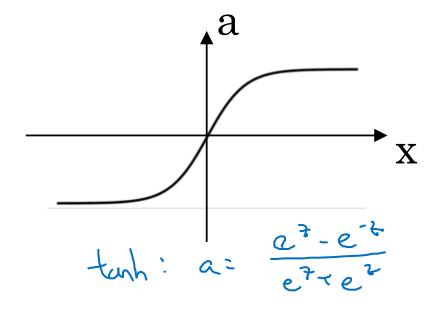


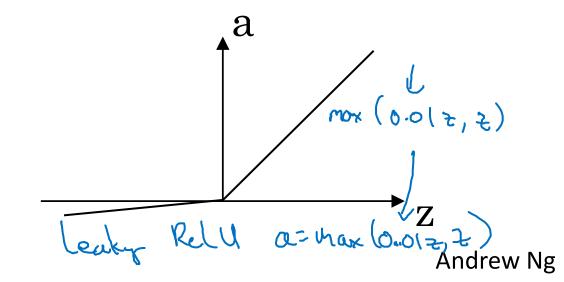


#### Pros and cons of activation functions







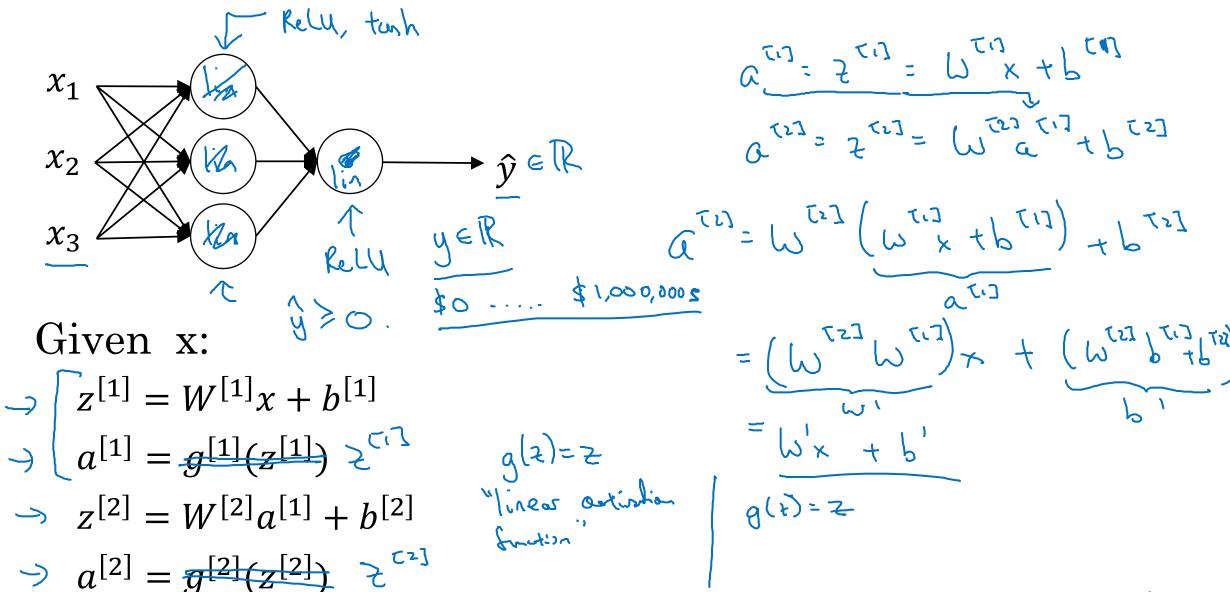




# One hidden layer Neural Network

Why do you need non-linear activation functions?

#### Activation function





## One hidden layer Neural Network

# Derivatives of activation functions

## Sigmoid activation function

$$g(z) = \frac{1}{1 + e^{-z}}$$

$$g(z) = \frac{1}{1 + e^{-z}}$$

$$a = g(z) = \frac{1}{1 + e^{-z}}$$

$$\frac{1}{1 + e^{-z}}$$

$$= \frac{1}{1 + e^{-z}}$$

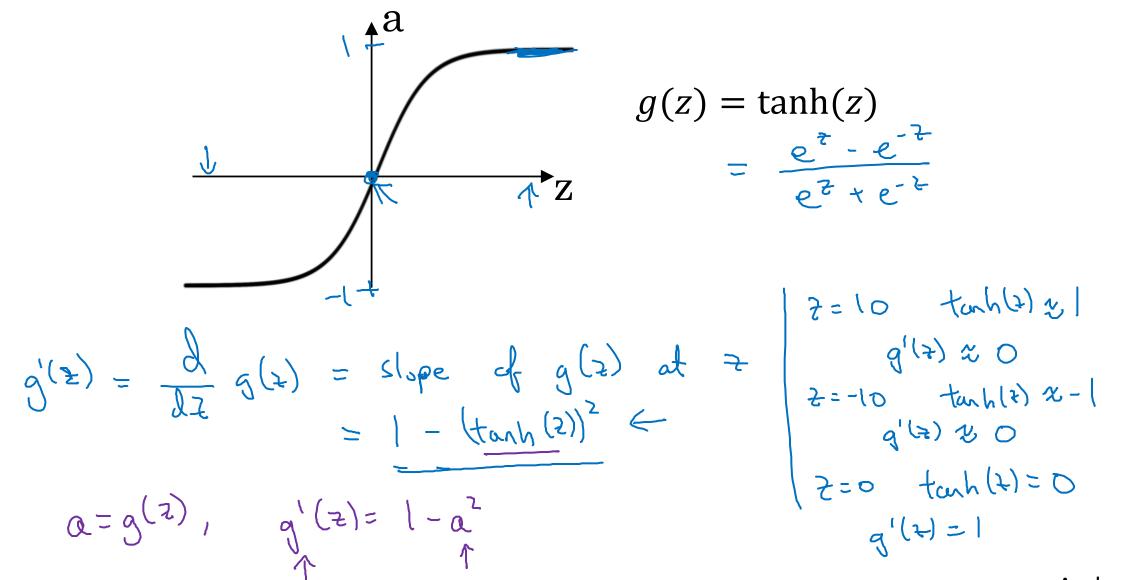
$$\frac{1}{1 + e^{-z}}$$

$$= \frac{1}{1 + e^{-z}}$$

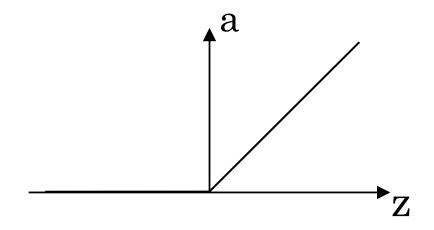
$$\frac{1}{1 + e^{-z}}$$

$$\frac$$

#### Tanh activation function



#### ReLU and Leaky ReLU

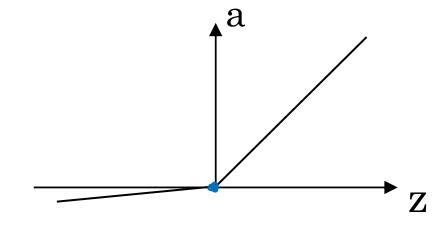


#### ReLU

$$g(t) = mox(0, 2)$$

$$\Rightarrow g'(t) = \begin{cases} 0 & \text{if } 2 < 0 \\ 1 & \text{if } t > 0 \end{cases}$$

$$\Rightarrow \frac{1}{2} = 0.0000...00$$



#### Leaky ReLU

$$g(z) = \max(0.01z, z)$$
 $g'(z) = \{0.01 \text{ if } z > 0\}$ 



# One hidden layer Neural Network

# Gradient descent for neural networks

#### Gradient descent for neural networks

Parameters: 
$$(\sqrt{12})$$
  $(\sqrt{12})$   $(\sqrt$ 

### Formulas for computing derivatives

Formal propagation!  $Z_{(1)} = P_{(1)}(S_{(1)}) + P_{(1)}$   $Y_{(2)} = P_{(2)}(S_{(2)}) + P_{(2)}$   $Y_{(2)} = P_{(2)}(S_{(2)}) + P_{(2)}$ 

A-Y: derivation shown in Logistic case Back propagation. 1= [ 4", A(3) --- \ (100)] 95[5] = U[5]- X dw [1] = In dz [1] A [1] T 2 b T2] = In np. Sun (d2 T2), anis= 1, keepdons = True) 12til = Wizzit dzizz \* gtil (Ztil)
(nti), m)

(nti), m) dw = = 42 TIX X T ab [1] = In np.sum (d2[1], oni) = 1, keeplin = True (ntiz) ) restaure 1 Andrew Ng

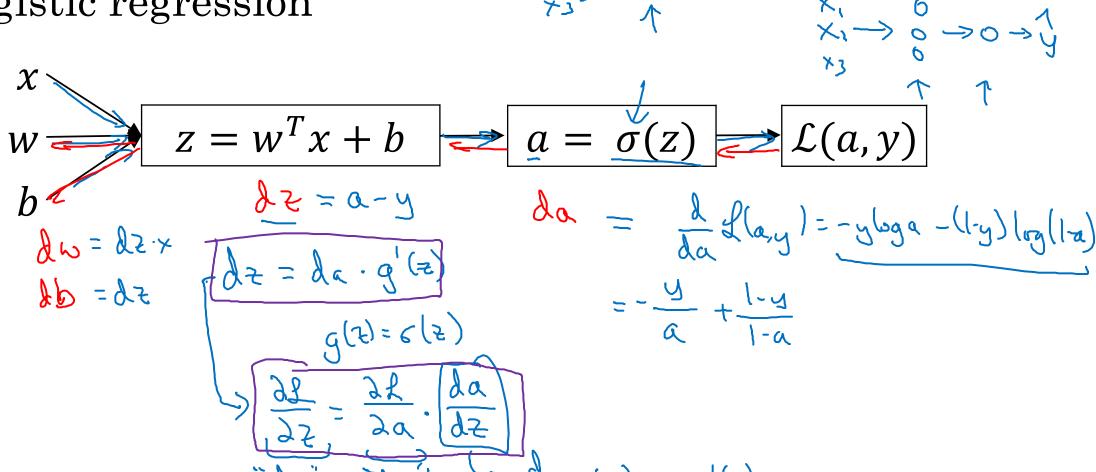


# One hidden layer Neural Network

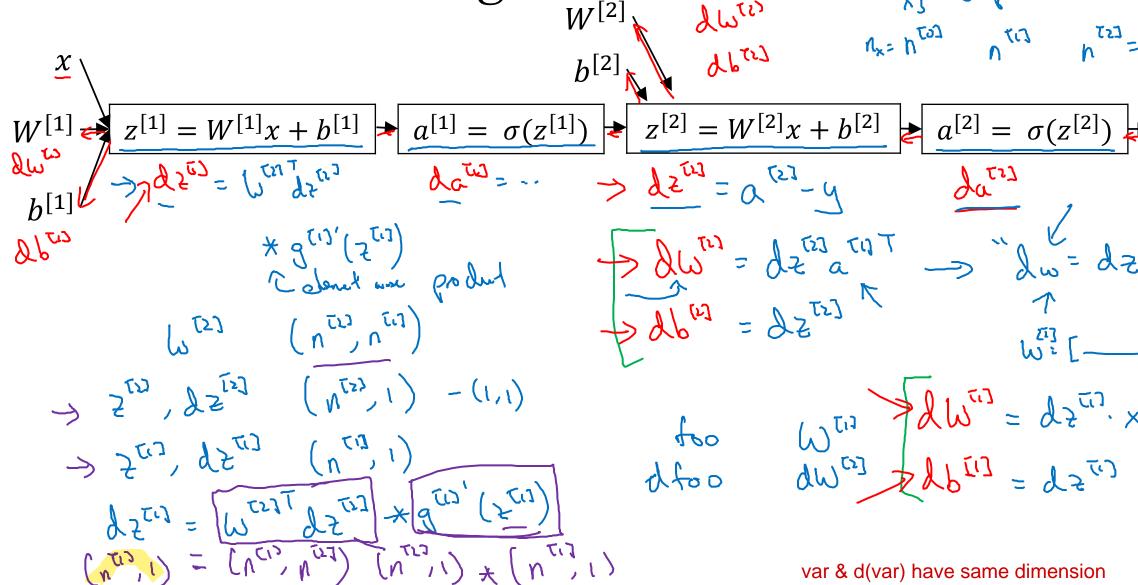
Backpropagation intuition (Optional)

## Computing gradients

Logistic regression



## Neural network gradients



## Summary of gradient descent

$$dz^{[2]} = a^{[2]} - y$$
 $dW^{[2]} = dz^{[2]}a^{[1]^T}$ 
 $db^{[2]} = dz^{[2]}$ 
 $dz^{[1]} = W^{[2]T}dz^{[2]} * g^{[1]'}(z^{[1]})$ 
 $dW^{[1]} = dz^{[1]}x^T$ 
 $db^{[1]} = dz^{[1]}$ 

Vectorized Implementation:

$$z^{(1)} = \omega^{(1)} \times + b^{(1)}$$

$$z^{(1)} = g^{(1)}(z^{(1)})$$

$$z^{(1)} = \left[z^{(1)}(z^{(1)})\right]$$

$$z^{(1)} = \left[z^{(1)}(z^{(1)})\right]$$

$$z^{(1)} = \left[z^{(1)}(z^{(1)})\right]$$

$$z^{(1)} = \left[z^{(1)}(z^{(1)})\right]$$

$$z^{(1)} = g^{(1)}(z^{(1)})$$

## Summary of gradient descent

$$dz^{[2]} = a^{[2]} - y$$

$$dW^{[2]} = dz^{[2]}a^{[1]^T}$$

$$db^{[2]} = dz^{[2]}$$

$$dz^{[1]} = W^{[2]T}dz^{[2]} * g^{[1]'}(z^{[1]})$$

$$dW^{[1]} = dz^{[1]}x^T$$

$$db^{[1]} = dz^{[1]}$$

$$dz^{[2]} = a^{[2]} - y$$

$$dW^{[2]} = dz^{[2]}a^{[1]^T}$$

$$db^{[2]} = dz^{[2]}$$

$$dz^{[2]} = \frac{1}{m}dz^{[2]}A^{[1]^T}$$

$$dz^{[2]} = \frac{1}{m}np. sum(dz^{[2]}, axis = 1, keepdims = True)$$

$$dz^{[1]} = W^{[2]T}dz^{[2]} * g^{[1]'}(z^{[1]})$$

$$dW^{[1]} = dz^{[1]}x^T$$

$$dy^{[1]} = dz^{[1]}x^T$$

$$dy^{[1]} = \frac{1}{m}dz^{[1]}x^T$$

$$dy^{[1]} = \frac{1}{m}dz^{[1]}x^T$$

$$dy^{[1]} = \frac{1}{m}dz^{[1]}x^T$$

$$dy^{[1]} = \frac{1}{m}np. sum(dz^{[1]}, axis = 1, keepdims = True)$$

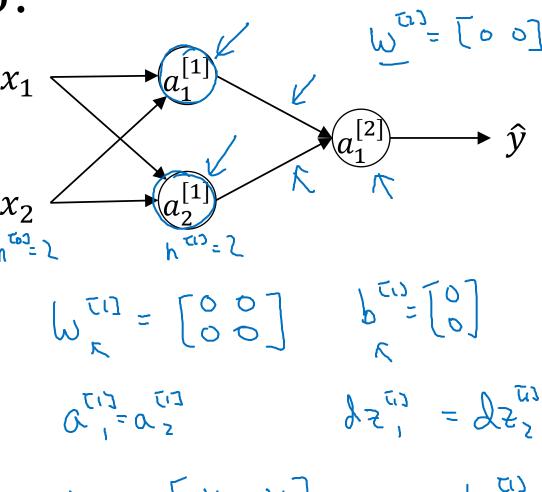


# One hidden layer Neural Network

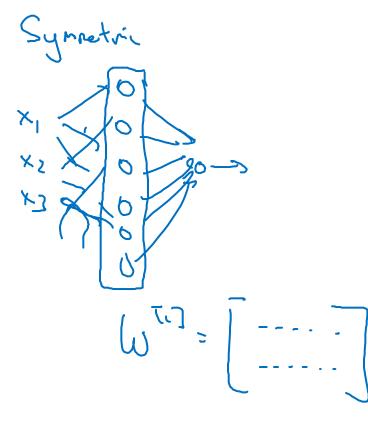
#### Random Initialization

## What happens if you initialize weights to

zero?



Every node in a layer becomes symmetric and changes together at each iteration.



#### Random initialization

