

week-2-submission-1

January 29, 2024

```
[2]: # Imports
import matplotlib.pyplot as plt
import numpy as np
```

0.0.1 Plot Sine Function (for my reference)

```
[4]: # Define the range of values for x
      # np.linspace creates array of 1000 points evenly spaced between -2 and 2
      # This range is chosen since it covers two full cycles of the sine wave
      # sine waves repeat every 2
      # np.pi is constant for the value of (pi).
x = np.linspace(-2*np.pi, 2*np.pi, 1000)

# Compute the sine of these values
# Computes the sine of all the 1000 points in x and stores the result in y.
y = np.sin(x)

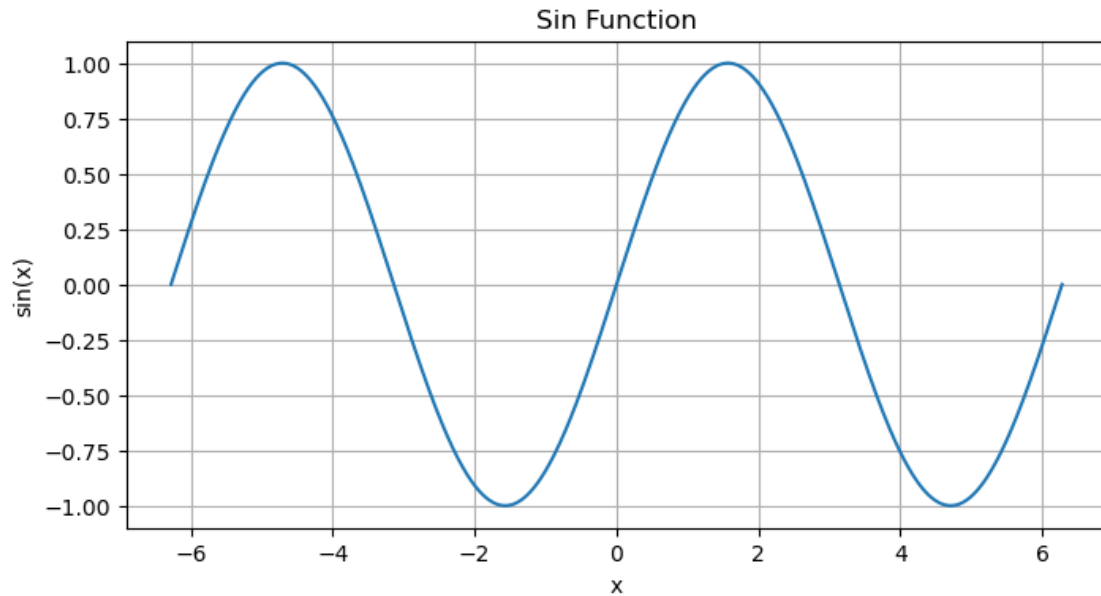
# Create the plot
# Set the size
plt.figure(figsize=(8, 4))

# Set the variables to plot
plt.plot(x, y)

# Title and Labels
plt.title('Sin Function')
plt.xlabel('x')
plt.ylabel('sin(x)')

# Add lines to the plot
plt.grid(True)

# Show the plot
plt.show()
```



0.0.2 Plot Loch Ness Monster Function

```
[6]: # Define the range of values for x
      # This range is chosen to observe the behavior of the function from 0 to 30
      x = np.linspace(0, 30, 100)

      # Compute the Loch Ness Monster function for b = 0.05
      # The function is  $y = 2 + e^{-bx}\sin(x)$ , where b is 0.05
      #  $e^{-bx}$  represents an exponential decay and  $\sin(x)$  is a sine wave
      # The combination of these two creates a wave pattern that decreases in
      ↪ amplitude over time
      y1 = 2 + np.exp(-0.05 * x) * np.sin(x)

      # Compute the Loch Ness Monster function for b = 0.1
      # This leads to a faster decay of the wave pattern
      y2 = 2 + np.exp(-0.1 * x) * np.sin(x)

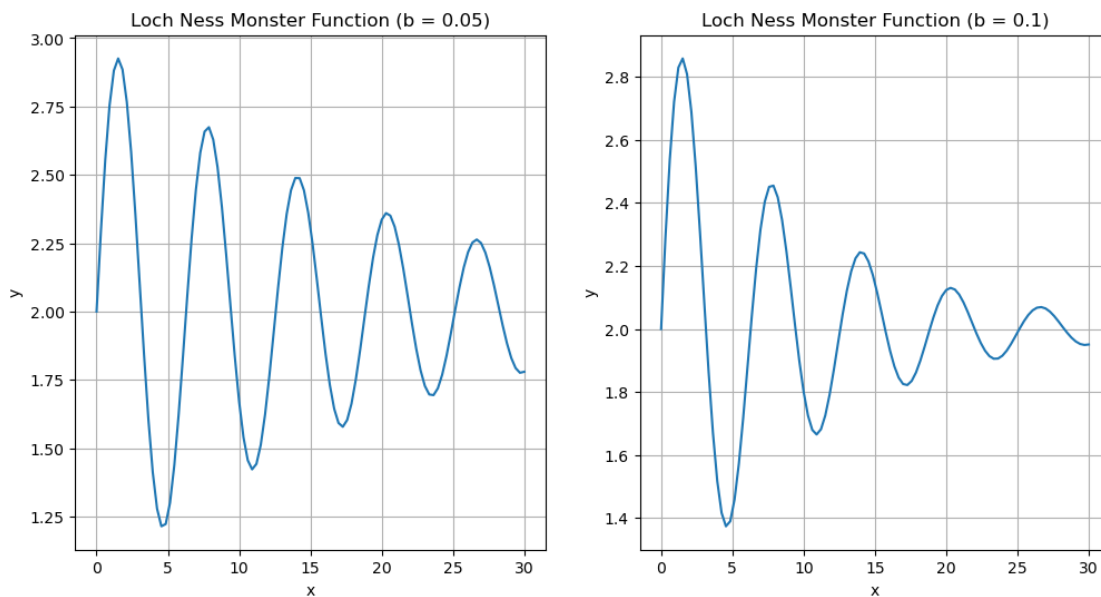
      # Create the plot
      plt.figure(figsize=(12, 6))

      # Plot for b = 0.05
      # Create the subplot on the left
      plt.subplot(1, 2, 1)
      plt.plot(x, y1)
      plt.title('Loch Ness Monster Function (b = 0.05)')
      plt.xlabel('x')
      plt.ylabel('y')
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plt.grid(True)

# Plot for b = 0.1
    # Create the subplot on the right
plt.subplot(1, 2, 2)
plt.plot(x, y2)
plt.title('Loch Ness Monster Function (b = 0.1)')
plt.xlabel('x')
plt.ylabel('y')
plt.grid(True)

# Show the plots
plt.show()
```



The 0.1 graph is decaying faster than the 0.05 graph since when b is larger, the value of $-bx$ becomes more negative which in return makes e^{-bx} smaller. Therefore making the y smaller as well.

0.0.3 Bell Function

```
[9]: # Define the range of values for x
x = np.linspace(0, 30, 100)

# Define the center of the Bell curve
a = 15.0

# Compute the Bell function
    # The function is defined as  $y = \exp(-(x-a)^2)$ 
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y_bell = np.exp(-(x - a)**2)

# Compute the Inverse Bell function
y_inverse_bell = 1 - np.exp(-(x - a)**2)

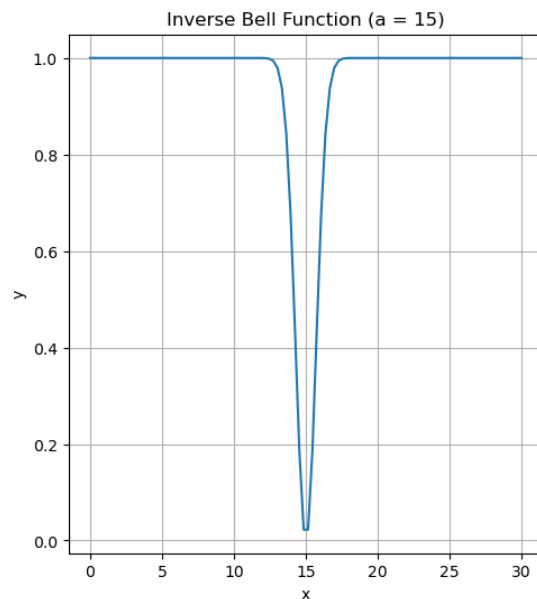
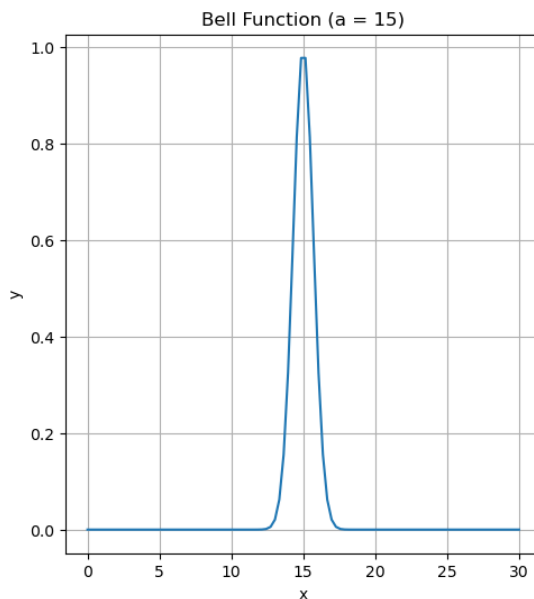
# Create the plot
plt.figure(figsize=(12, 6))

# Plot for the Bell function
plt.subplot(1, 2, 1)
plt.plot(x, y_bell)
plt.title('Bell Function (a = 15)')
plt.xlabel('x')
plt.ylabel('y')
plt.grid(True)

# Plot for the Inverse Bell function
plt.subplot(1, 2, 2)
plt.plot(x, y_inverse_bell)
plt.title('Inverse Bell Function (a = 15)')
plt.xlabel('x')
plt.ylabel('y')
plt.grid(True)

# Show the plots
plt.show()

```



The reason why the graphs look the way they do because it is a bell-shaped curve centered at $x = a$ (here $a = 15$). The initial function value increases as x approaches a , and decreases as x moves away from a . The inverse does the opposite so the function value decreases towards 0 as x approaches a , and increases towards 1 as x moves away from a .