CSE440: Natural Language Processing II

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Lecture 6: Neural Nets and RNN

Outline

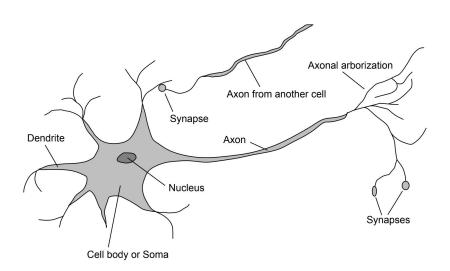
- Neural Networks (SLP 7 and lecture)
- Recurrent neural networks (SLP 9 and lecture)

Before starting learning sequence

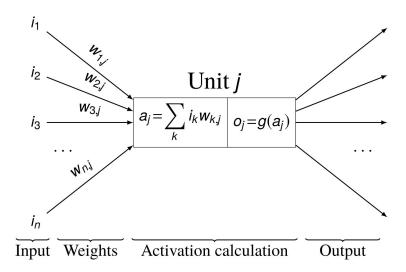
We need to remember some neural network basics.

Neural Networks

Neuron in a human brain

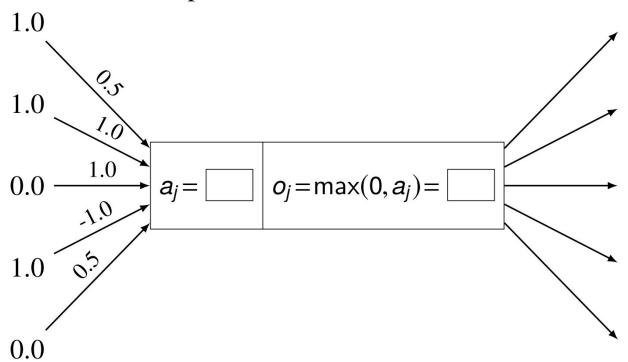


Neuron in an ML model



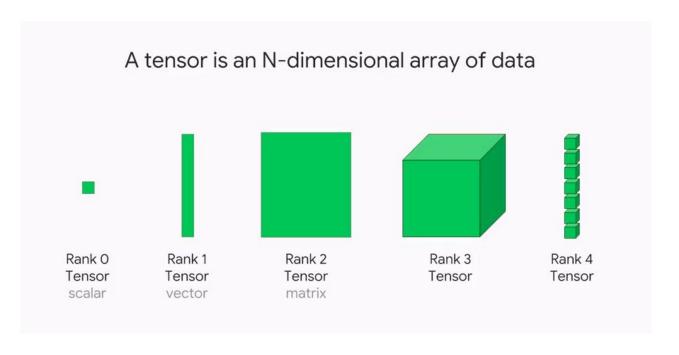
Class work

Calculate the output of this unit:



Unit calculations as tensor arithmetic

What is a tensor?



Unit calculations as tensor arithmetic

Summation for a single unit:

$$o_j = g\left(\sum_k i_k w_{k,j}\right)$$

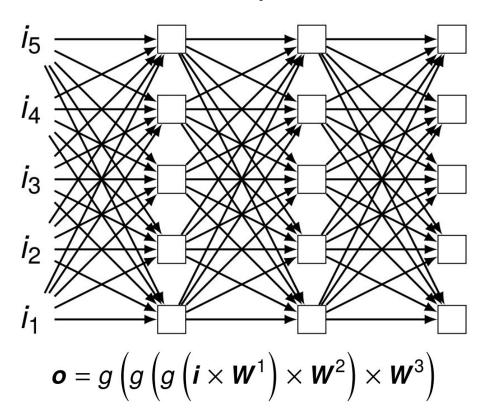
Vector arithmetic for a single unit:

$$o_j = g \left[\begin{bmatrix} i_1 & i_2 & \dots & i_n \end{bmatrix} \begin{bmatrix} w_{1,j} \\ w_{2,j} \\ \dots \\ w_{n,j} \end{bmatrix} \right] = g \left(\mathbf{i} \times \mathbf{w}_{*,j} \right)$$

Matrix arithmetic for multiple units:

$$o = g(i \times W)$$

A feedforward network as composition



Activation functions

- Why do we need activation functions?
- What types of activation functions do we have?

Learning the XOR

$$\mathbf{X} = \begin{bmatrix} 0 & 0 \\ 0 & 1 \\ 1 & 0 \\ 1 & 1 \end{bmatrix}$$

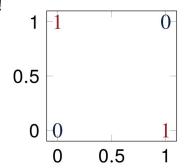
$$\mathbf{y} = \begin{bmatrix} 0 \\ 1 \\ 1 \\ 0 \end{bmatrix}$$

Can you solve it with linear regression?

$$y = XW + b$$

$$\mathbf{X} = \begin{bmatrix} 0 & 0 \\ 0 & 1 \\ 1 & 0 \\ 1 & 1 \end{bmatrix} \qquad \mathbf{y} = \begin{bmatrix} 0 \\ 1 \\ 1 \\ 0 \end{bmatrix} \qquad \begin{bmatrix} \mathbf{y} = \mathbf{X}\mathbf{W} + \mathbf{b} \\ 0 \\ 1 \\ 1 \end{bmatrix} \qquad \begin{bmatrix} 0 \\ 0 \\ 1 \\ 1 \end{bmatrix} = \begin{bmatrix} 0 & 0 \\ 0 & 1 \\ 1 & 0 \\ 1 & 1 \end{bmatrix} \mathbf{W} + \mathbf{b}$$
No such weights exist!

No such weights exist!



$$\begin{bmatrix} 0 \\ 1 \\ 1 \\ 0 \end{bmatrix} = \begin{bmatrix} 0 & 0 \\ 0 & 1 \\ 1 & 0 \\ 1 & 1 \end{bmatrix} \begin{bmatrix} ? \\ ? \end{bmatrix} + ?$$

Solving XOR with NNs

$$f(\boldsymbol{X}; \boldsymbol{W}, \boldsymbol{c}, \boldsymbol{w}, b) = \max(0, \boldsymbol{X}\boldsymbol{W} + \boldsymbol{c}) \boldsymbol{w} + b$$

$$\begin{bmatrix} 0 \\ 1 \\ 1 \\ 0 \end{bmatrix} = \max \left(0, \begin{bmatrix} 0 & 0 \\ 0 & 1 \\ 1 & 0 \\ 1 & 1 \end{bmatrix} \mathbf{W} + \mathbf{c} \right) \mathbf{W} + \mathbf{b}$$

$$\begin{bmatrix} 0 \\ 1 \\ 1 \\ 0 \end{bmatrix} = \max \left(0, \begin{bmatrix} 0 & 0 \\ 0 & 1 \\ 1 & 0 \\ 1 & 1 \end{bmatrix} \begin{bmatrix} ? & ? \\ ? & ? \end{bmatrix} + \begin{bmatrix} ? & ? \end{bmatrix} \right) \begin{bmatrix} ? \\ ? \end{bmatrix} + ?$$

Solving XOR with NNs

$$\begin{bmatrix} 0 \\ 1 \\ 1 \\ 0 \end{bmatrix} = \max \left(0, \begin{bmatrix} 0 & 0 \\ 0 & 1 \\ 1 & 0 \\ 1 & 1 \end{bmatrix} \begin{bmatrix} 1 & 1 \\ 1 & 1 \end{bmatrix} + \begin{bmatrix} 0 & -1 \end{bmatrix} \right) \begin{bmatrix} 1 \\ -2 \end{bmatrix} + 0$$

$$\begin{bmatrix} 0 \\ 1 \\ 1 \\ 0 \end{bmatrix} = \begin{bmatrix} 0 & 0 \\ 1 & 0 \\ 1 & 0 \\ 2 & 1 \end{bmatrix} \begin{bmatrix} 1 \\ -2 \end{bmatrix} + 0$$

Common activation functions in hidden units

We have: affine transformation of input x, followed by nonlinear activation function

$$\boldsymbol{h} = g(\boldsymbol{W}^{\mathsf{T}}\boldsymbol{x} + \boldsymbol{b})$$

g could be just about anything! It can be linear, but a linear function is not preferred. Why?

Considerations:

- What specific behavior is needed?
- How will the gradients behave?

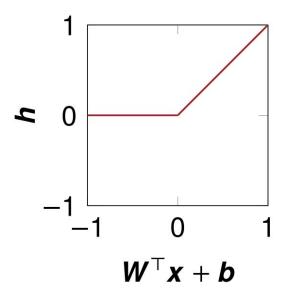
Why linear functions are not preferred?

Because of the considerations.

- We need complex mappings between the inputs and the outputs
- All linear layers will translate the input linearly to output
 — that is, multiple linear transformation
- Cannot use backpropagation as the derivative is constant

ReLU

$$\boldsymbol{h} = \max(0, \boldsymbol{W}^{\top} \boldsymbol{x} + \boldsymbol{b})$$



Behavior?

- Active only when input is positive Gradients?
 - 1 when positive
 - 0 when negative

ReLU is non-differentiable

ReLU at z = 0:

- left derivative = 0
- right derivative = 1

So ReLU is not differentiable at z = 0!

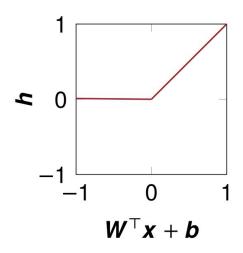
A few non-differentiable points are not a problem:

- Training rarely reaches a point with gradient 0 anyway
- Software simply returns either left or right derivative

Leaky ReLU

$$f(x) = max(0.1x, x)$$

$$h = \max(0, W^{T}x + b) + 0.01 \min(0, W^{T}x + b)$$



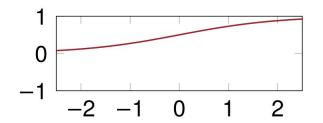
ReLU has a "dead neuron" problem!

Behavior?

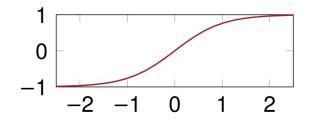
- Strong positive activation when positive
- Very weak negative activation when negative Gradients?
 - 1 when positive
 - 0.1 when negative

Sigmoid and tanh

Sigmoid:
$$f(x) = \frac{1}{1 + e^{-x}}$$



Tanh:
$$f(x) = \frac{(e^x - e^{-x})^2}{(e^x + e^{-x})^2}$$



Behavior?

- Sigmoid: 0/1 switch
- Tanh: -1/+1 switch

Gradients?

- Saturate across most of their domain
- Tanh optimizes slightly better since it is similar to the identity function near 0

Hyperparameters

- Network parameters are the ones that are being learned throughout the training process (e.g. weights)
- There are parameters that we can control to facilitate this learning: they are called hyperparameters
- Activation function is one such hyperparameter
- We have others ...

Optimizers

- Algorithms used to update the learnable parameters in order to reduce loss
- Common optimizers:
 - Gradient descent
 - Stochastic gradient descent
 - Mini-batch gradient descent
 - Momentum
 - Adagrad
 - RMSProp
 - AdaDelta
 - Adaptive moment estimation
- GD methods maintain a single learning rate (with/without decay for all parameters and are known as first order optimizers (works with the first order derivative)
- Adaptive methods like Adagrad provide learning rates for each parameter, thus improving the learnability, but are computationally expensive
- RMSProp not only provides LR for each parameter, it adapts based on the mean of recent magnitudes of the gradients for the weight → first order. AdaDelta is similar but works with squared gradients (second order)

Adaptive moment estimation

- Popularly known as Adam (not ADAM)
- Came out of OpenAl and University of Toronto
- Most likely the highest cited <u>paper</u> in recent history
- Why is it so popular?
 - Straightforward to implement
 - Little memory requirements
 - Well suited for problems that are large in terms of data and/or parameters
 - Needs little to no manual tuning

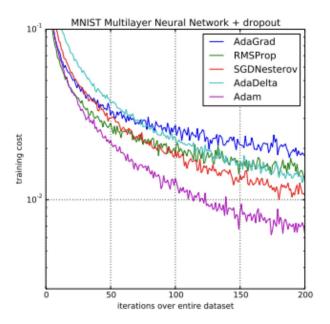
Adam

- Adam works with momentums of first and **second** order
- Instead of adapting the parameter learning rates based on the average first moment (the mean), m_t as in RMSProp, Adam also makes use of the average of the second moments of the gradients (the uncentered variance) v_t

$$\hat{m}_t = rac{m_t}{1-eta_1^t}. \ \hat{v}_t = rac{v_t}{1-eta_2^t}. \ eta_{t+1} = eta_t - rac{\eta}{\sqrt{\hat{v}_t} + \epsilon} \hat{m}_t.$$

 The values for β1 is 0.9, 0.999 for β2 and epsilon is an extremely small number to avoid zero division

Adam's popularity



Sebastian Ruder: "... RMSprop, Adadelta, and Adam are very similar algorithms that do well in similar circumstances. Adam might be the best overall choice."

Andrej Karpathy: "In practice Adam is currently recommended as the default algorithm to use, and often works slightly better than RMSProp."

Regularization

- A set of strategies used in Machine Learning to reduce the generalization error
- Why?
- Bias-variance tradeoff
- Bias: error from wrong assumptions in the learning algorithm
 - High bias can cause an algorithm to miss the relevant relations between features and target outputs → Observations don't matter
 - Underfitting
- Variance: error from sensitivity to small fluctuations in the training set
 - High variance may result in modeling the random noise in the training data → focusing too much on observations
 - Overfitting

Regularization

- A good model needs to balance bias and variance
- Regularization helps us do that

Regularization techniques

- Introduce regularization term to the loss function
 - Introduces a small amount of bias to counter variance → reduce overfitting
 - Loss function: negative log likelihood or binary cross entropy
 - Most common terms:
 - L2 regularizer: Ridge regression → adds the "squared magnitude" of the coefficient as the penalty term to the loss function
 - L1 regularizer: Lasso regression → adds the "absolute value of magnitude" of the coefficient as a penalty term to the loss function
 - Uses λ that controls the sensitivity of the model to the input → less sensitive, less likely to overfit
 - L2 focuses on larger weights, so higher λ means L2 penalizes higher value weights more than lower ones → no feature essentially goes away
 - L1 has equal focus, so, higher $\lambda \to low$ weight features go away \to feature selection

Regularization techniques

- Dropout: Drops out (ignore) a layer's output with a probability p
 - Choice of p depends on the architecture
- Early stopping: Stops when performance gets saturated
 - Stops model from being overfit
 - Returns the best current model
- Data augmentation
 - Introduce new training data with variation
 - Injects noise

Other common hyperparameters

- Learning rate: how quickly a network updates its parameters
 - Low learning rate slows down the learning process but converges smoothly
 - Larger learning rate speeds up the learning but may not converge
 - Decaying learning rate is preferred
- Epochs: How many times the entire training dataset has passed through the model
- Batch size: (Mini) batch size refers to a subset of the training data. Weights are updated after each mini batch training
 - Small mini batch → too many updates
 - Large mini batch → too few updates, too many epochs to converge

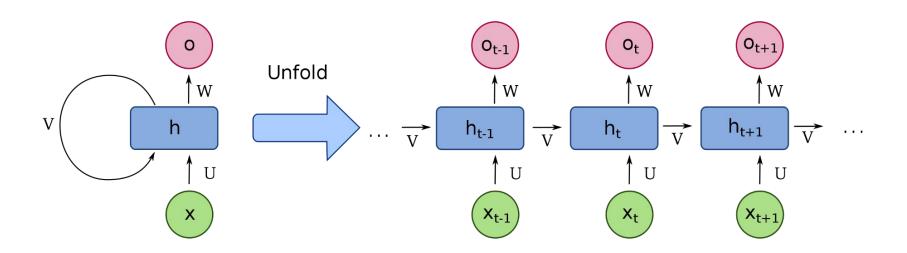
Recurrent Neural Networks (RNN)

- Simple recurrent networks
- Bidirectional and gated recurrent networks
- Recurrent architectures
- Seq2Seq models
- Attention

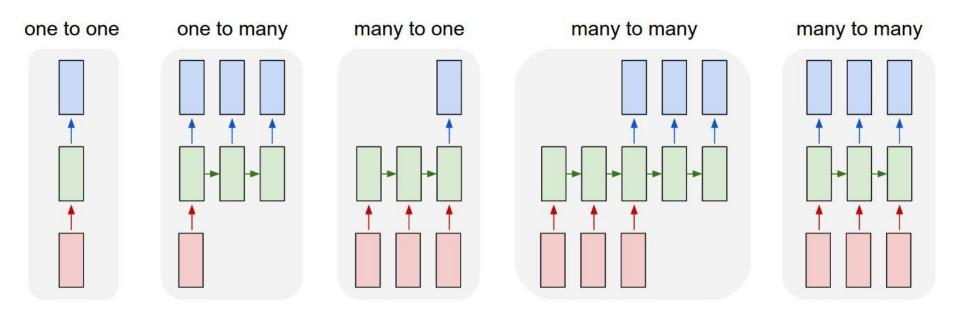
Short history of RNN

- 1986: RNNs are Introduced by David Rumelhart
- 1995: LSTMs are introduced by Sepp Hochreiter and Jürgen Schmidhuber based on Hochreiter's 1991 research on vanishing gradient problem
- 2001: Gers and Schmidhuber trained LSTMs to learn language models (unlearnable by HMMs)
- 2009: Graves et al. won ICDAR handwriting recognition competition using LSTMs
- 2013: Hinton and his team destroyed previous record for speech recognition using LSTM
- 2014: GRU is introduced by Cho et al.
- 2015: Widespread use in both academia and industry due to Google's adaptation of LSTM in their Google Voice speech recognition system

Structure of an RNN

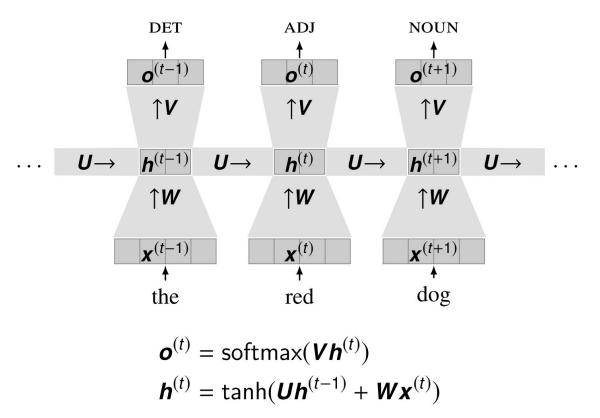


Types of RNNs



https://karpathy.github.io/2015/05/21/rnn-effectiveness/

A completely unrolled Simple RNN



Simple RNN

Intuitions:

- Each step combines the current input with the history
- Each prediction is made based on this combination Observations:
 - The input and hidden state change at each time step
- The parameters W, U, V are the same at each step Equations:

$$\mathbf{h}^{(t)} = \tanh(\mathbf{U}\mathbf{h}^{(t-1)} + \mathbf{W}\mathbf{x}^{(t)})$$

 $\mathbf{o}^{(t)} = \operatorname{softmax}(\mathbf{V}\mathbf{h}^{(t)})$

Classwork

Consider an RNN that predicts as:

$$\mathbf{o}^{(t)} = \operatorname{softmax}(\mathbf{V}\mathbf{h}^{(t)})$$

$$h^{(t)} = Uh^{(t-1)} + Wx^{(t)}$$

whose parameters have been set to:

$$\boldsymbol{U} = \begin{bmatrix} 2 & 0 \\ 1 & 2 \end{bmatrix} \quad \boldsymbol{W} = \begin{bmatrix} 2 & 0 & -1 \\ 1 & -1 & 1 \end{bmatrix} \quad \boldsymbol{V} = \begin{bmatrix} 1 & 0 \\ -1 & 1 \\ 0 & 3 \end{bmatrix}$$

If you are given the following input:

$$h^{(0)} = \begin{bmatrix} 1 \\ -1 \end{bmatrix} \quad x^{(1)} = \begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix} \quad x^{(2)} = \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix}$$

Which label will be predicted for each word if in the final softmax, index 0=ADJ, index 1=DET, and index 2=NOUN?

Drawbacks of simple RNN

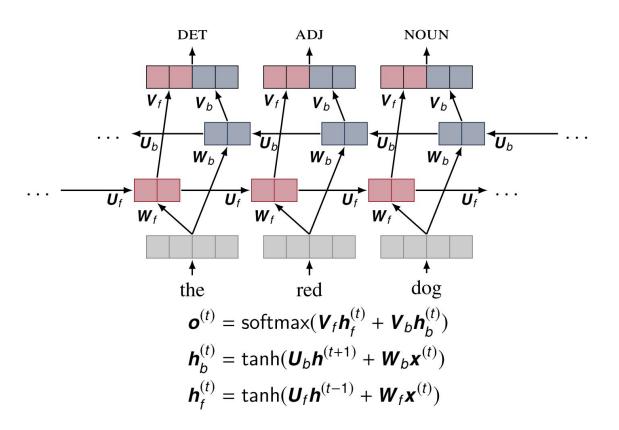
- They can only see the past, not the future
- They must forget the same amount of history at each time step.
 - Theoretically, they don't have to
 - Maintaining long term memory is difficult

Bidirectional RNNs

Intuition:

- Run one forward RNN
- Run one backward RNN
- Combine their outputs

Bidirectional RNNs

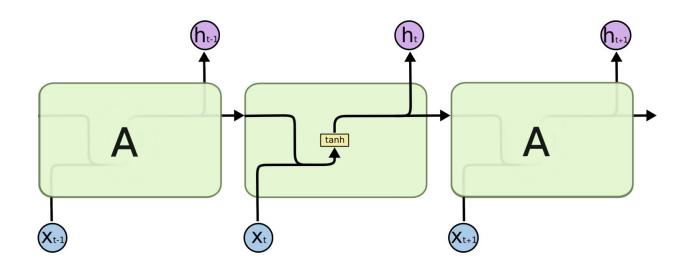


Gated RNNs

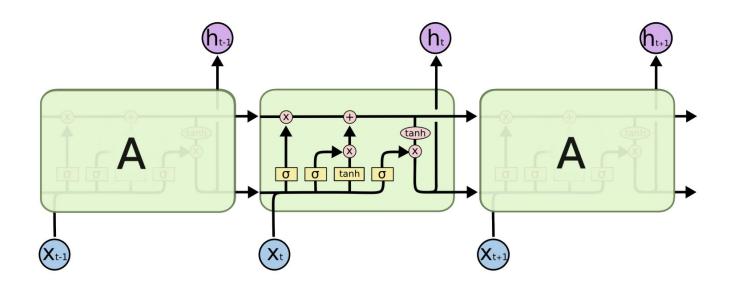
Intuition:

- Simple RNNs forget the same amount at each time step
- Look at the previous hidden state and the current input
- Decide how much to forget based on those
- Two gated RNNs
 - Long Short-Term Memory (LSTM)
 - Gated Recurrent Units (GRU)

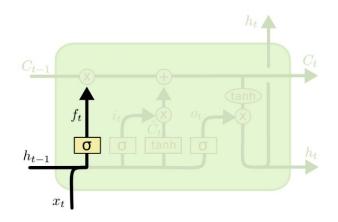
Simple RNN



LSTM

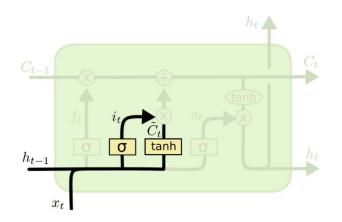


Forget gate



$$f_t = \sigma\left(W_f \cdot [h_{t-1}, x_t] + b_f\right)$$

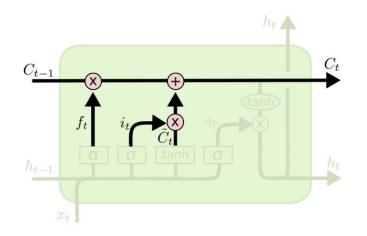
Input gate



$$i_t = \sigma (W_i \cdot [h_{t-1}, x_t] + b_i)$$

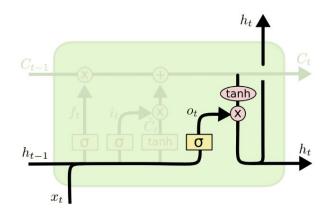
$$\tilde{C}_t = \tanh(W_C \cdot [h_{t-1}, x_t] + b_C)$$

Cell update



$$C_t = f_t * C_{t-1} + i_t * \tilde{C}_t$$

Output gate

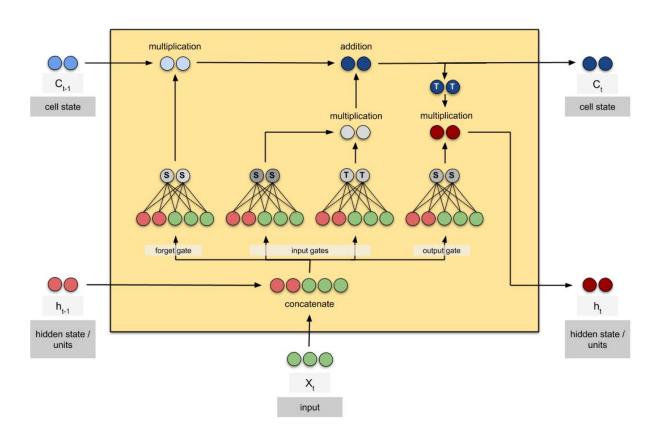


$$o_t = \sigma (W_o [h_{t-1}, x_t] + b_o)$$
$$h_t = o_t * \tanh (C_t)$$

Useful blog from Colah

https://colah.github.io/posts/2015-08-Understanding-LSTMs/

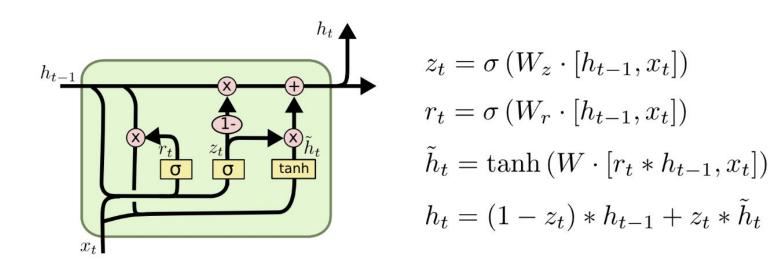
One LSTM cell



LSTM

- Step 1: Calculate forget (f_t), input (i_t) and output gates (o_t)
- Step 2: Calculate cell state update
- Step 3: Update cell state (C_t)
- Step 4: Calculate h,

GRU



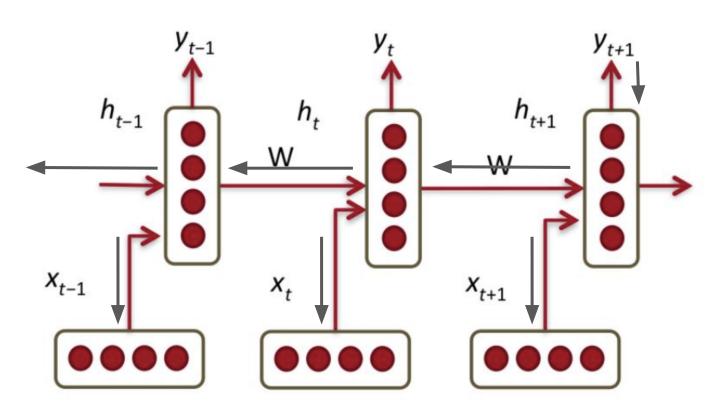
Gated RNNs

Properties:

- Can forget different amounts at each time step
- Much better at using long distance information

A bidirectional GRU is a good starting point for many sequence tagging tasks

Backpropagation through time



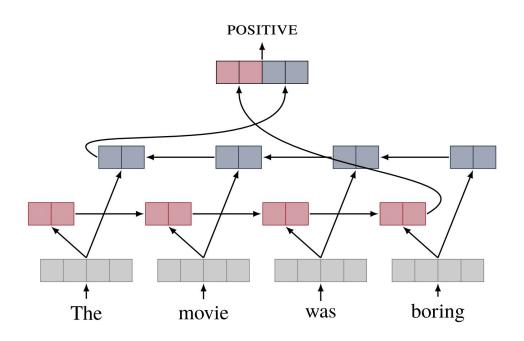
The vanishing gradient problem

- BPTT calculates gradients backward through time, it involves taking derivatives of the loss with respect to the model's parameters at each time step
- These derivatives are multiplied together as they are propagated backward
- Since gradients are multiplied together, if the gradients at each time step are less than 1, this multiplication leads to a compounding effect
 - As you go further back in time, the gradients become increasingly smaller
- The compounding effect causes the gradients for early time steps to become vanishingly small, approaching zero
 - When the gradients are too close to zero, they don't provide meaningful information for parameter updates
 - This makes it challenging for the RNN to learn long-term dependencies in the data

Recurrent architectures for related tasks

RNNs for text classification

- Last hidden state of the RNN represents the entire sentence.



Recurrent architectures for related tasks

What other tasks can RNNs handle?

Practice

Equations for LSTM

```
f_{t} = sigmoid(W_{t}x_{t} + U_{t}h_{t-1} + b_{t})
i_{t} = sigmoid(W_{t}x_{t} + U_{t}h_{t-1} + b_{t})
o_{t} = sigmoid(W_{0}x_{t} + U_{0}h_{t-1} + b_{0})
```

- All the weights (Ws and Us and bs) will be given. You need to calculate f, i
 and o.
- How to calculate sigmoid/tanh for a vector (because the argument for sigmoid in this case will be a vector)
 - sigmoid([1, 2, 0]) = [sigmoid(1), sigmoid(2), sigmoid(0)]
 - tanh([1, 2, 0]) = [tanh(1), tanh(2), tanh(0)]

Practice

How to calculate f_{t} for input $x_{t} = [1 \ 1]^{T}$

- Given: $W_f = [1 \ 1, \ 0 \ 1], \ U_f = [0 \ 0, \ 2 \ 3], \ h_{t-1} = [4 \ 5]^T, \ b_f = [0 \ 0]^T$
- Using this equation: $f_t = sigmoid(W_t x_t + U_t h_{t-1} + b_t)$
 - Multiply W_f with x_f (W_f has a shape of 2x2, xt has a shape of 2x1), output will be a 2x1 vector
 - Multiply U_f with h_{f-1} (U_f has a shape of 2x2, ht-1 has a shape of 2x1), output will be a 2x1 vector
 - b, already is a 2x1 vector
 - So, f, will also be a 2x1 vector

Then calculate i_t and o_t and use these values to calculate the C_t and h_t $h_t = o_t^* tanh(C_t)$ $C_t = f_t^* C_{t-1} + i_t^* \hat{C}_t$ $\hat{C}_t = tanh(W_c x_t + U_c h_{t-1} + b_c)$

P.S. * means element-wise multiplication

Practice

```
W_{f}X_{t} = [2 \ 1]^{T}, U_{f}h_{t-1} = [0 \ 23]^{T} \text{ bf} = [0 \ 0]^{T}, \text{ so } W_{f}X_{t} + U_{f}h_{t-1} + b = [2 \ 24]^{T}
f_{t} = \text{sigmoid}([2 \ 24]^{T}) = [\text{sigmoid}(2) \ \text{sigmoid}(24)]^{T}
Ct = f_{t}^{*}C_{t-1} + i_{t}^{*}\hat{C}_{t}
If C_{t-1} = [1 \ 5]^{T}
f_{t}^{*}C_{t-1} = [\text{sigmoid}(2) \ \text{sigmoid}(6)]^{T} * [1 \ 5]^{T}
= [\text{sigmoid}(2)^{*}1 \ \text{sigmoid}(24)^{*}5]^{T} \text{ which is another } 2x1 \ \text{matrix}
```