



## Midterm Examination : Questions for CSE330. All Sections.

Department of Computer Science & Engineering

BRAC University

Fall Semester

Date : November 08, 2022

Time : One hour 10 minutes

Faculty Name (Initial) : \_\_\_\_\_ Student ID# : \_\_\_\_\_ Section#: \_\_\_\_\_

### Instructions:

- There are four questions. **Answer any three questions.** Total marks 30.
- Use pencil for your answers. No break for bathroom/freshroom is allowed. **Must use your own calculator.** Cell phones must be turned off (Not in vibration mode). We assume that you know how to use scientific calculator of model CASIO fx-991 ES or equivalent.
- Return this question along with your answer script.
- All examinees must abide by the 'Regulations of Students Conduct' of Brac university.

### Read carefully the questions below and answer properly (All are CO1 and CO2):

1. Answer the following questions:

- (5 marks) [CO-1, CO-2] Consider the quadratic equation  $x^2 - 16x + 3 = 0$ . Explain how the loss of significance occurs in finding the roots of the quadratic equation if we restrict to 4 significant figures. Discuss how to avoid this and find the roots.
- [CO-3, CO-4] Given  $\beta = 2$ ,  $m = 3$ ,  $e_{\min} = -2$  and  $e_{\max} = 1$ . Using the denormalized convention, answer the following:
  - (2 marks) Evaluate the Machine Epsilon.
  - (3 marks) Calculate the minimum and maximum positive number representable by this system.

2. Consider the function  $f(x) = e^x - e^{-x}$  and the nodes at  $-1$ ,  $0$ , and  $1$ . Now answer the following using 3 significant figures:

- (1 mark) [CO-1] Write down the matrices  $b$  and  $V$  used in Vandermonde method.
- (2 marks) [CO-3] Compute the determinant of the Vandermonde matrix  $V$ .
- (3 marks) [CO-3] Using The results of the previous two parts, calculate the Taylor coefficients  $a_0$ ,  $a_1$  and  $a_2$ ; and finally find the interpolation polynomial.
- (4 marks) [CO-4] Evaluate the upper bound of the error for the given function for the interval  $[-2.1, 2.1]$ .

3. Consider the function  $f(x) = e^x - e^{-x}$  and the nodes at  $-2$ ,  $0$ , and  $2$ . Now answer the following using 3 significant figures:

- (4.5 marks) [CO-4] Evaluate the Newton coefficients  $a_k = f[x_0, \dots, x_k]$  using Newton's divided-difference method for the given function and nodes.
- (2.5 marks) [CO-3] Compute the Newton interpolation polynomial for the given function, and express the result in the natural basis.
- (3 marks) [CO-4] Evaluate the relative error in percentage form at  $x = 1.5$ .

4. Consider the following data set:

$x$	2.1	2.3	2.5	2.7
$f(x)$	14.25	18.64	20.90	24.00

Using these data values, answer the following questions:

- (2 marks) [CO-3] Compute  $f'(2.3)$  using the central difference method.
- (2 marks) [CO-4] Evaluate the truncation error for  $f(x) = 12 \ln x$  at  $2.4$  using  $h = 0.1$  in forward difference method.
- (4+2 marks) [CO-3] Deduce an expression for  $D_h^{(1)}$  from  $D_h$  by replacing  $h$  with  $h/3$  using the Richardson extrapolation method. Then calculate the upper bound of error of  $D_h^{(1)}$ , if  $f(x) = \sin x$ ,  $x_0 = 1$  and  $h = 0.1$ .