

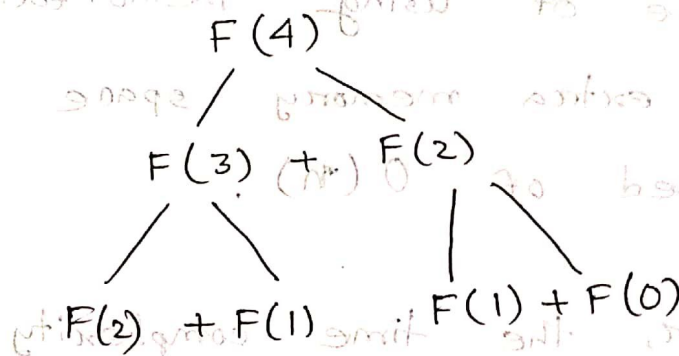
# Task 2 (a) :-

⇒ Implementation 1 :-

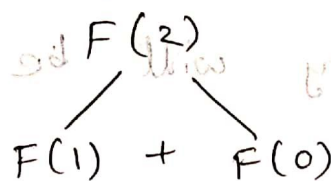
Here the recurrence relation is,

$$F(n) = F(n-1) + F(n-2) + c$$

For visualization, let,  $n=4$ ,



And, for  $n=2$ ,



For any case, the time complexity is,

$$O(2^{n-1} - 1)$$

$$= O\left(\frac{2^n}{2}\right)$$

$$= O(2^n)$$

And, the space complexity will be  $O(1)$ .

⇒ Implementation 2:-

Because of using memoization technique, some extra memory space would be consumed of  $O(n)$ .

However, the time complexity will reduce drastically. we are using a single loop in this implementation. That's why, the time complexity will be  $O(n)$ .

Between implementation 1 and 2, the faster code execution will be of implementation 2. Because, exponential (time) algorithms are much slower than linear (time) algorithms.

$$\left(\frac{n}{2}\right) O$$