

Ans to the ques no:- C

Given that,  $L = \{w \in \{0,1,2\}^* : 0^n 1^n 2^n \text{ where } n \geq 0\}$

Say  $L_3$  is regular.  $P$  is the pumping length.

Assume,  $w = 0^P 1^P 2^P$

Here,  $|w| \geq P$

$$w = xyz$$

$$|xy| \leq P$$

$$y \neq \epsilon$$

$$xy^iz \in L_3, \text{ where } i \geq 0$$

So, after decomposing  $w$  into  $xyz$ ,

$$x = 0^d$$

$$y = 0^f \quad [f \geq 1]$$

$$z = 0^{P-d-f} 1^P 2^P \quad [d+f \leq P]$$

Lets say,  $i = 2$

$$\therefore xy^iz = 0^d (0^f)^2 0^{P-d-f} 1^P 2^P$$

$$= O^d O^{2f} O^{p-d-f} 1^p 2^p$$

$$= O^{d+2f+p-d-f} 1^p 2^p$$

$$= O^{p+f} 1^p 2^p$$

If,  $O^{p+f} 1^p 2^p \in L_3$ ,

then,  $p+f = p$

$$\Rightarrow f = 0$$

However, the precondition was  $f \geq 1$ .

So, this is a contradiction.

Therefore,  $L_3$  is not regular.