

Assignment

1.) Consider array Exam $[-3:2, 4:7]$. Find address of Exam $[-1, 7]$. If array is row major and column major. Base address = 4000. $w = 4$ bytes

An Base Address = 4000

$w = 4$ bytes

Exam $[L_1: U_1, L_2: U_2]$

$$L_1 = -3 \quad U_1 = 2$$

$$L_2 = 4 \quad U_2 = 7$$

To Find Exam[i][j]. $i = -1, j = 7$

(1) Row Major

$$\begin{aligned} \text{Exam}[-1][7] &= 4000 + ((i - L_1) \times (U_2 - L_2 + 1) + (j - L_2)) \times w \\ &= 4000 + (((-1 + 3) \times (7 - 4 + 1) + (7 - 4)) \times 4) \\ &= 4000 + 11 \times 4 \\ &= 4000 + 44 \\ &= 4044 \end{aligned}$$

(2) Column major

$$\begin{aligned} \text{Exam}[-1][7] &= 4000 + ((j - L_2) \times (U_1 - L_1 + 1) + (i - L_1)) \times w \\ &= 4000 + ((7 - 4) \times (2 + 3 + 1) + (-1 + 3)) \times 4 \\ &= 4000 + 20 \times 4 \\ &= 4000 + 80 \\ &= 4080 \end{aligned}$$

2) Given 2d array $z_1[3:10, 10:20]$ stored in row major order. Base address = 200, w=4. Find address $z_1[5, 15]$

Ans Base Address = 200
w = 4 bytes

$z_1[L_1:U_1, L_2:U_2]$

$$L_1 = 3 \quad U_1 = 10$$

$$L_2 = 10 \quad U_2 = 20$$

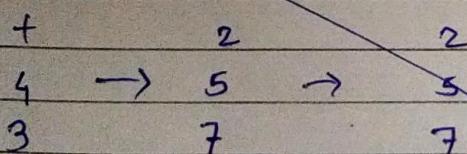
To find $z_1[i][j]$. $i = 5, j = 15$

(a) Row Major

$$\begin{aligned} z_1[5][15] &= 200 + ((i-L_1) \times (U_2-L_2+1) + (j-L_2)) \times w \\ &= 200 + ((15-3) \times (20-10+1) + (15-10)) \times 4 \\ &= 200 + (12 \times 11 + 5) \times 4 \\ &= 200 + 27 \times 4 \\ &= 200 + 108 \\ &= 308 \end{aligned}$$

(b) Evaluate with the help of stack.

~~34 + 52 * 2 * 2 / 2 / 2 - 9 +~~



3.] Evaluate with the help of stack

$$3 \ 4 + 5 \ 2 / 2 * 2 / 2 / 2 / - 9 +$$

$$\begin{array}{ccccccccc}
 & / & * & / & / & / \\
 + & 2 & 2 & 2 & 2 & 2 & 2 & - \\
 4 & \rightarrow & 5 & \rightarrow & 2 & \rightarrow & 4 & \rightarrow & 2 \rightarrow 1 \rightarrow 0 \\
 3 & & 7 & & 7 & & 7 & & 7 \\
 & + & & & & & & & \\
 \rightarrow & 9 & = & \underline{\underline{16}} & & & & & \\
 & 7 & & & & & & &
 \end{array}$$

4.] Convert infix to prefix using stack

$$(A^B) / D * E / (F + A)^* (D^E) - C$$

stack

C

-

) - ,)

F

* - ,) , *

D

(- , * ,

↑

) - , * ,) -

prefix exp.

C E D * A F + E D B A A / * / * -

A

+ - , * ,) , +

F

(

/ - , * , /

E

* - , * , 1 , *

D

/ - , * , 1 , * , /

) - , * , 1 , * , 1 ,)

B

^ - , * , / , * , 1 ,) , ^

(

* Final Prefix expression

-* / * / ^ A B D E + F A * D E C

5) Evaluate with the help of stack.

A B C + * C B A - + *

$$A = 6, B = 12, C = -2$$

6 12 -2 + * -2 12 6 - + *

-

+

6

+

-2

*

6

*

12

→

10

12

60

4

6

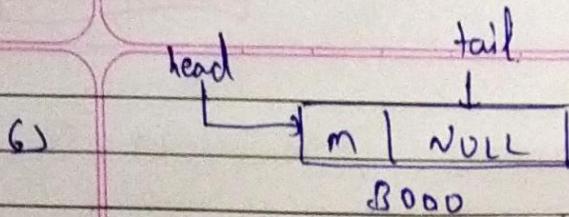
6

60

60

60

240

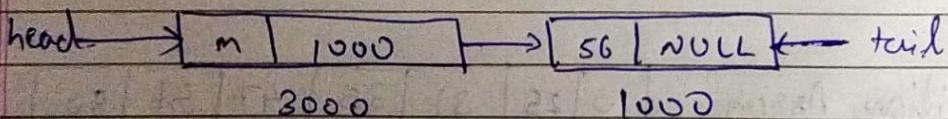


→ For inserting a new node at end.

- We insert a new node which contains data 56 and address 1000 after first node.
- Suppose we have two pointer head and tail. They are pointing at the first node.
- For inserting a new node at end, first of all we create a new node.

`struct node *newnode = (struct node *) malloc
(sizeof(struct node))`

- Then for insert we move our tail pointer
 $\text{tail} \rightarrow \text{next} = \text{new node}$
- We assign address of new node in first node
then we move tail pointer to new node
- In last; the scenario is -



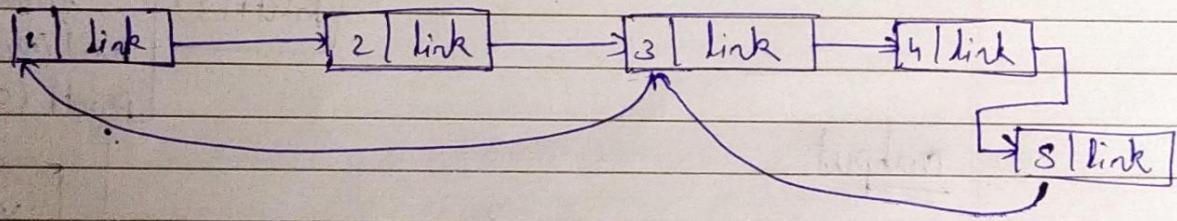
3) void fun1 (struct node * head)

```

{
    if (head == NULL)
        return;
    fun1 (head->next->next);
    printf ("%d", head->data);
}
  
```

So, the given function prints the alternate node (i.e. odd nodes) present in linked list in reverse manner.

For example, we have linked list containing $1 \rightarrow 2 \rightarrow 3 \rightarrow 4 \rightarrow 5$
 then it will give output 5 3 1



Revision for above example

$1 \rightarrow 2 \rightarrow 3 \rightarrow 4 \rightarrow 5$
 head.

```

void fun1(l)
{
    if (head == NULL)
        return;
    fun1(l->next);
    printf ("%d", l->data);
}
  
```

Recursion for above example

```
void fun1()
if (head == NULL)
    return
fun1(3)
printf()
```

return to
printf()

```
fun1() calls fun1(3)
void fun1(3)
if (head == NULL)
    return
fun1(3)
printf(3)
```

return to
printf(3)

```
fun1(3) calls
fun1(5)
void fun1(5)
if (head == NULL)
    return;
fun1(NULL) — calls
fun1(5)
```

```
return to
printf(5)
```

output

5 3 1

Q) what are advantages of circular queue over simple queue ? Explain pseudocode of enqueue() and dequeue() operation

- In circular queue, the front end and the rear end are next to each other. As a result, if the rear end is full even when the front end has space, data can be stored in the later sections until there is an overflow.
- Thus free space is effectively utilized.
- However in normal queue the front and rear ends are at opposite corners. Thus, even if the queue has a full rear end and only partially filled front end, the space cannot be used to store data as insertion starts from rear end which is full.

* Enqueue Algorithm

enqueue(Q, R, F, x, n)

```

1. if (R == n)
    "Overflow"
else
    R = R + 1
  
```

2. Q[R] = x

1 if ($F == -1$)
 $F = 0$

step 1 check if the queue is full.

step 2 If the queue is full, produce overflow error and exit.

step 3 If the queue is not full, increment R to point next empty space.

step 4 Add data element to the queue location where R is pointing.

step 5 Increment F to 0 if F is -1.

* Dequeue Algorithm.

Dequeue (Q, F, R)

1 if ($F == -1$)
 "underflow"
 return,

2 $Y \leftarrow Q[F]$

3 if $F == R$
 then $F \leftarrow R \leftarrow -1$
 else

$F \leftarrow F + 1$

4 return

Step-1 Check if queue is empty

Step-2 If queue is empty, produce underflow and exit.

Step-3 If the queue is not empty, access the data where front element is pointing.

Step-4 Increment the front pointer to next data element.

Step-5 If $F == R$, assign F and R to -1 (critical)

Step-6 Return.

Q1 Sort the following and show each step.

25, 56, 47, 35, 10, 90, 80, 31

(a) Bubble sort

Row 1 25 56 47 35 10 90 80 31
 ↙

25 47 56 35 10 90 80 31
 ↙

25 47 35 56 10 90 80 31
 ↙

25 47 35 10 56 90 80 31
 ↙ ↗

25 47 35 10 56 80 90 31
 ↙ ↗

25 47 25 10 56 80 31 90

Row 2 25 47 35 10 56 80 31 90
 ↙

25 35 47 10 56 80 31 90
 ↙

25 35 10 47 56 80 31 90
 ↙

25 35 10 47 56 31 80 90

Pass 3

25 35 10 47 56 31 80 90
 ↙ ↘
 25 10 35 47 56 31 80 90

25 10 35 47 31 56 80 90

Pass 4

25 10 35 47 31 56 80 90
 ↙ ↘

10 25 35 47 31 56 80 90
 ↙ ↘

10 25 35 31 47 56 80 90

Pass 5

10 25 35 31 47 56 80 90
 ↙ ↘

10 25 31 35 47 56 80 90

Sorted Array :-

10, 25, 31, 35, 47, 56, 80, 90

(b) selection sort

25 56 47 35 10 90 80 31

Step-1 10 56 47 35 25 90 80 31

Step-2 10 25 47 35 56 90 80 31

Step-3 10 25 31 35 56 90 80 47

Step-4 10 25 31 35 47 90 80 56

Step-5 10 25 31 35 47 56 80 90

Sorted Array:-

10, 25, 31, 35, 47, 56, 80, 90

(c) insertion sort

25 56 47 35 10 90 80 31

Step-1 25 56 47 35 10 90 80 31

Step-2 25 47 56 35 10 90 80 31

Step-3 25 47 35 56 10 90 80 31

25 35 47 56 10 90 80 31

Step 4 25 35 47 10 56 90 80 31
 ↙ ↗

25 35 10 47 56 90 80 31
 ↙ ↗

25 10 35 47 56 90 80 31
 ↙ ↗

10 25 35 47 56 90 80 31

Step 5 10 25 35 47 56 90 80 31

Step 6 10 25 35 47 56 80 90 31

Step 7 10 25 35 47 56 80 31 90
 ↙ ↗

10 25 35 47 56 31 80 90
 ↙ ↗

10 25 35 47 31 56 80 90
 ↙ ↗

10 25 35 31 47 56 80 90
 ↙ ↗

10 25 31 35 47 56 80 90

Sorted Array:-

10, 25, 31, 35, 47, 56, 80, 90

(d) Quick Sort

Step-1 25 56 47 ~~35~~²⁵ 10 90 80 31
 Pivot P Q { } { }

Step-2 25 10 47 ~~35~~⁵⁶ 90 80 31
 Pivot P Q { } { }

Step-3 [10] 25 [47 35 56 90 80 31]
 Left sub Array Right sub Array
 Pivot P Q { }

Step-4 [10] 25 [47 35 31 90 80 56]
 Pivot P Q { } { }

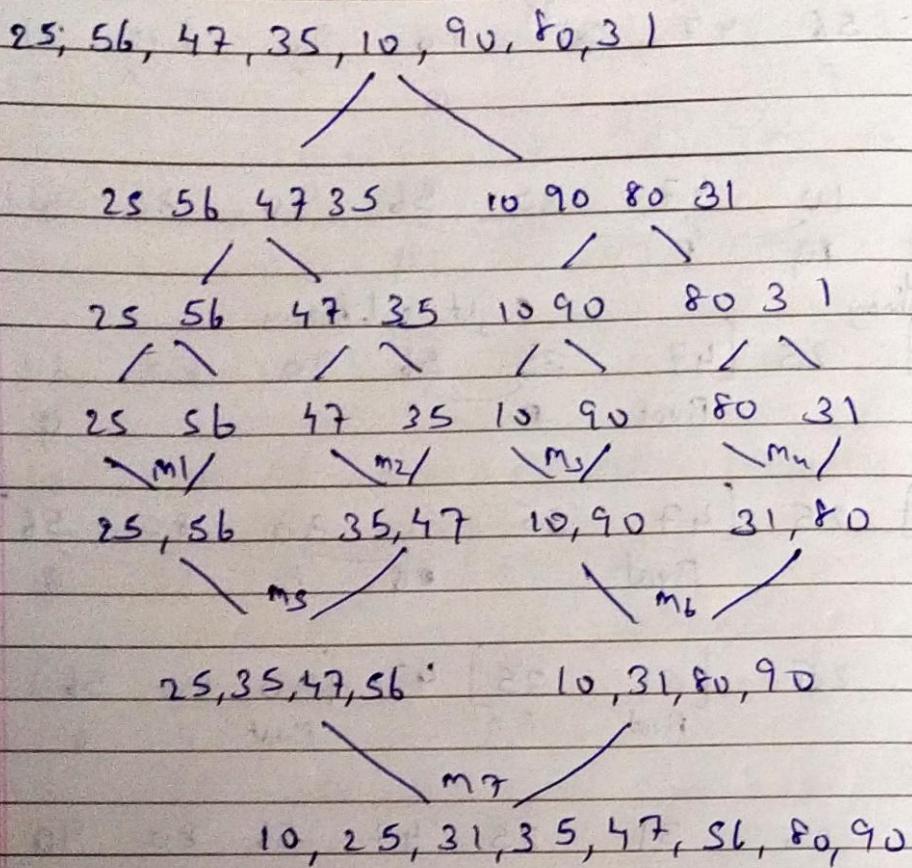
Step-5 10 25 [31 35] 47 [90 80 56]
 Pivot P Q { } { }

Step-6 10 25 31 35 47 56 80 90

Sorted Array:-

10, 25, 31, 35, 47, 56, 80, 90

(e) merge sort



Sorted Array :-

10, 25, 31, 35, 47, 56, 80, 90

(F) Radix Sort

Pass-1 Input Array

25	56	47	35	10	90	80	31
0	1	2	3	4	5	6	7

Count Array

3	1	0	0	0	2	1	1	0	0
0	1	2	3	4	5	6	7	8	9

0	1	2	3	3	3	0	3	6	5	6	7	7
0	1	2	3	4	5	6	7	8	9			

Auxiliary Array

10	90	80	31	25	35	56	47
0	1	2	3	4	5	6	7

Pass-2 Input Array

10	90	80	31	25	35	56	47
0	1	2	3	4	5	6	7

Count Array

0	1	1	2	1	1	0	0	1	1
0	1	2	3	4	5	6	7	8	9

-1	0	0	1	0	3	0	4	5	5	0	5	6
0	1	2	3	4	5	6	7	8	9			

Auxiliary Array

10	25	31	35	47	56	80	90
0	1	2	3	4	5	6	7

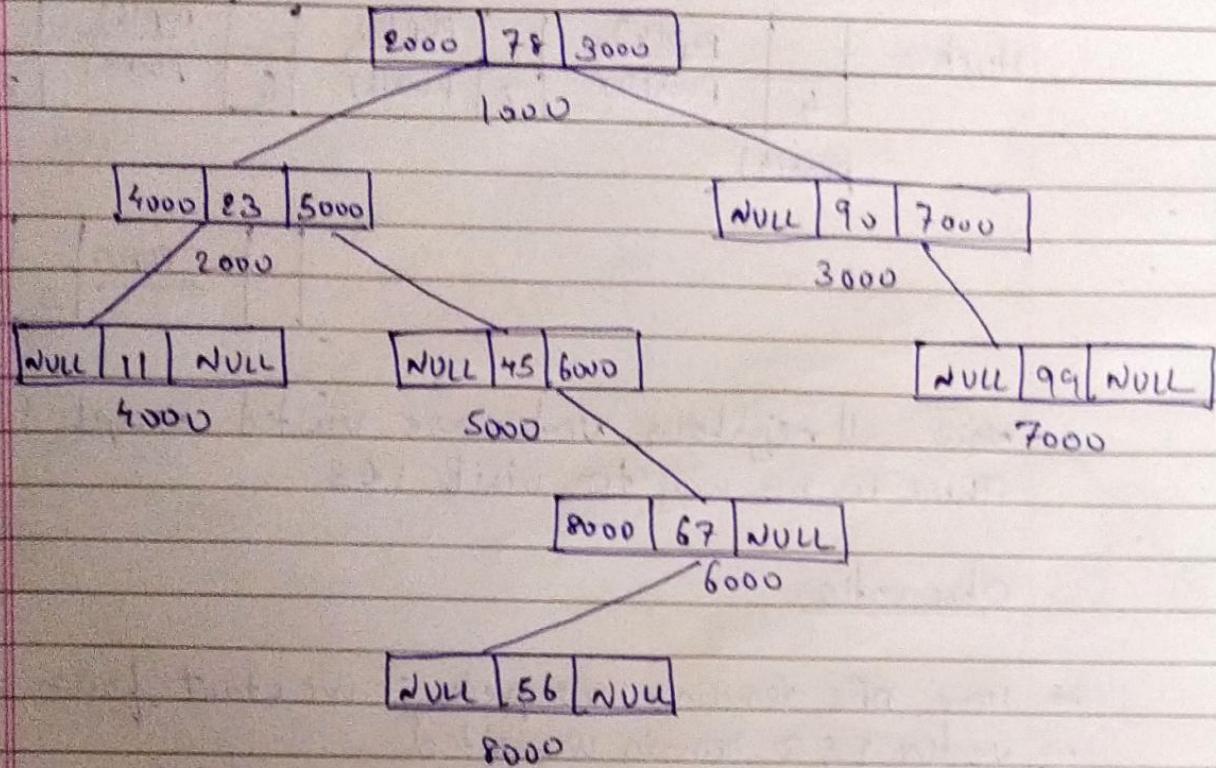
Pass-3 Input Array

10	25	31	35	47	56	80	90
0	1	2	3	4	5	6	7

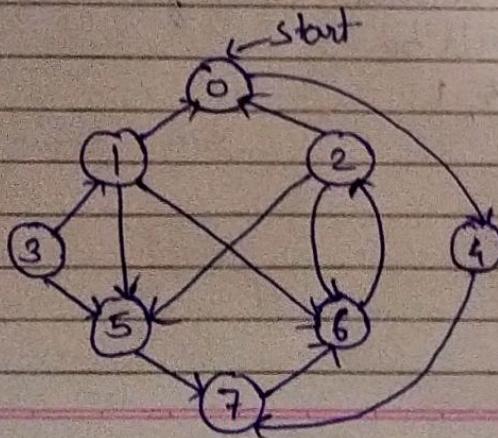
Sorted Array:- 10, 25, 31, 35, 47, 56, 80, 90

10) BST

78, 23, 11, 45, 67, 90, 99, 56



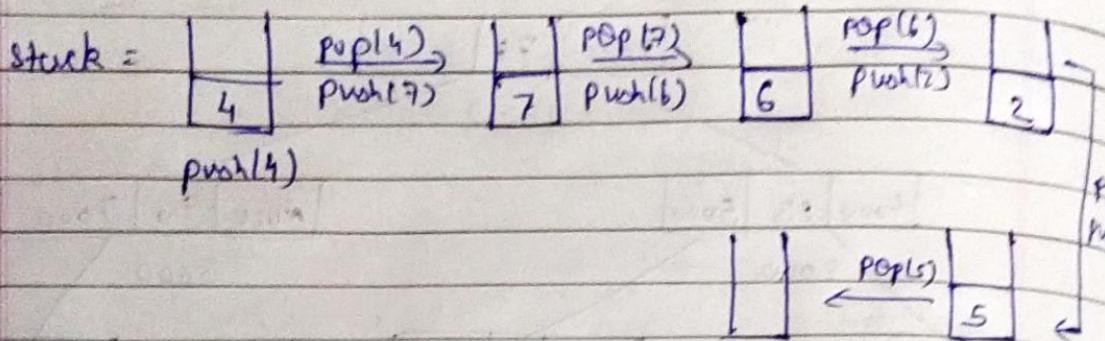
ii) DFS sequence (start vertex is 0)



vertex	Visited
0	✓
1	✗
2	✓
3	✗
4	✓
5	✓
6	✓
7	✓

DFS uses stack data structure.

Sequence $\rightarrow 0 \ 4 \ 7 \ 6 \ 2 \ 5$



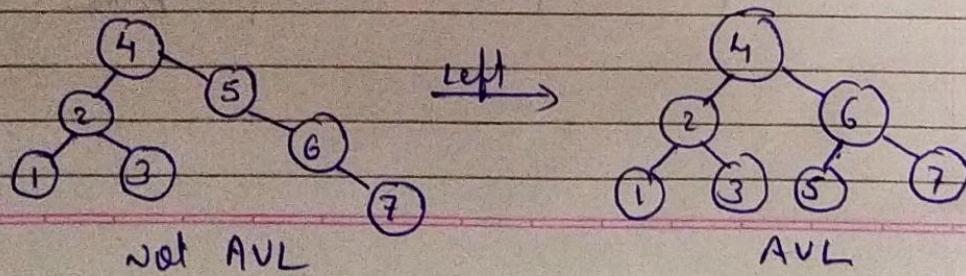
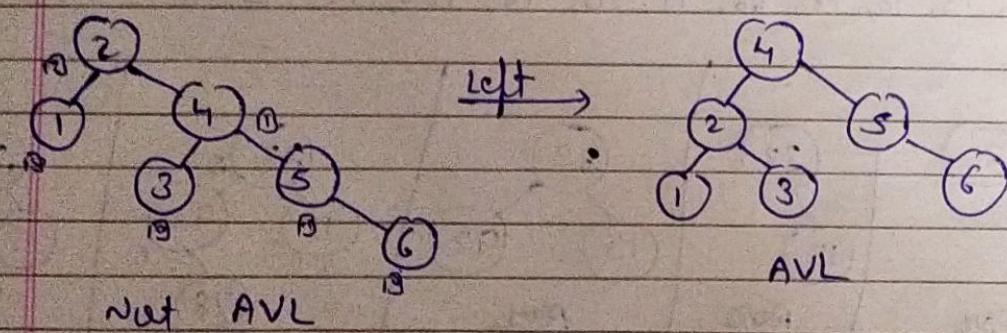
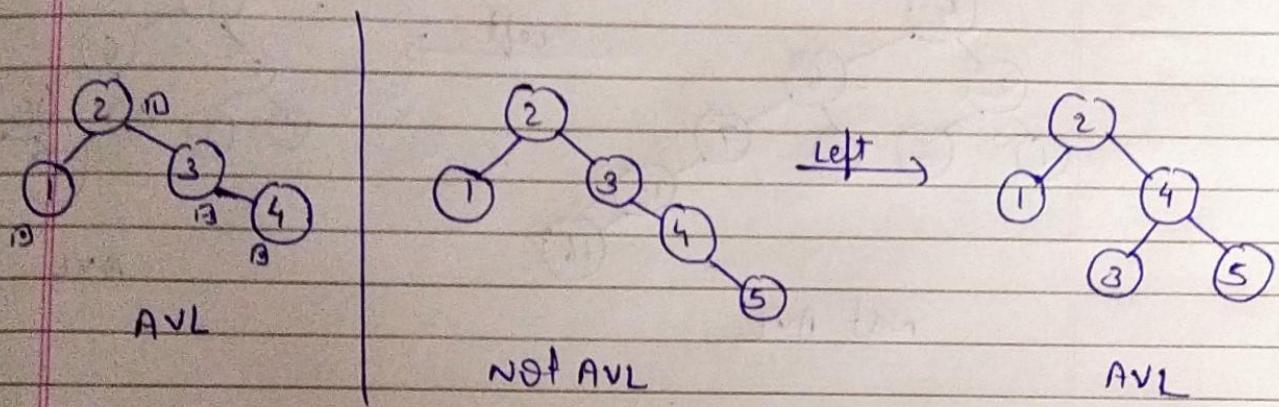
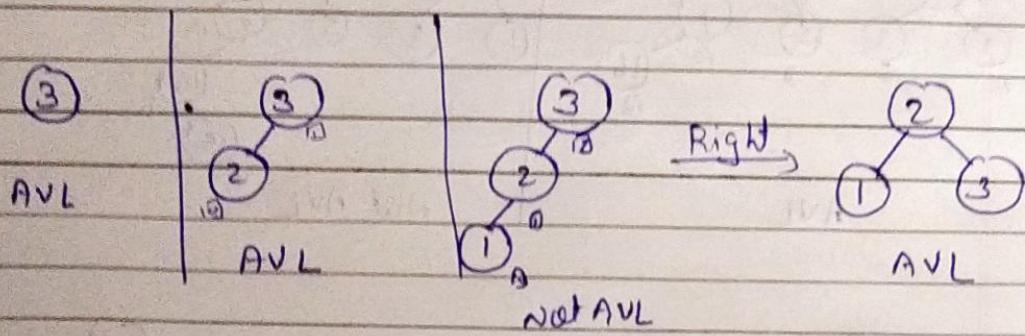
Now, all neighbour vertex are visited except 1 & 3.
There is no way to visit 1 & 3.

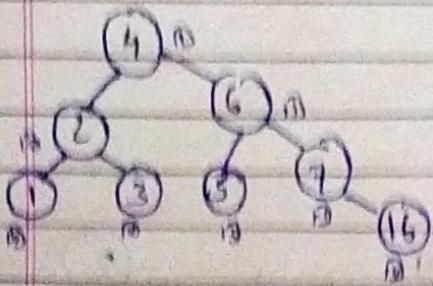
Observation

- Here DFS remains incomplete if we start from vertex 0
- vertex 1 & 3 remain unvisited
- In this graph, there is loop of $(5 \rightarrow 7 \rightarrow 6 \rightarrow 2 \rightarrow 0 \rightarrow 4 \rightarrow 7)$
so, there is no way to visit 1 & 3 if we start from vertex 0.
- For complete DFS, we should start from vertex 3
then DFS sequence will be
 $3, 5, 7, 6, 2, 0, 4, 1$

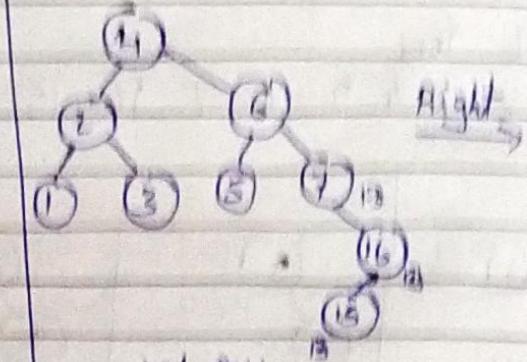
(2) AVL Tree

3 2 1 4 5 6 7 16 15

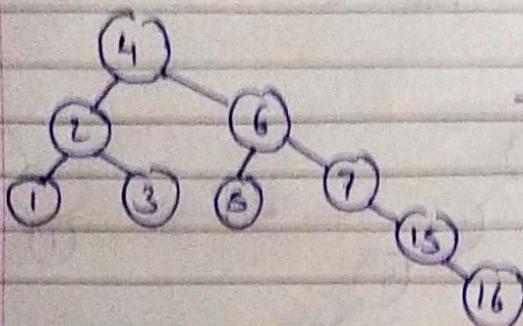




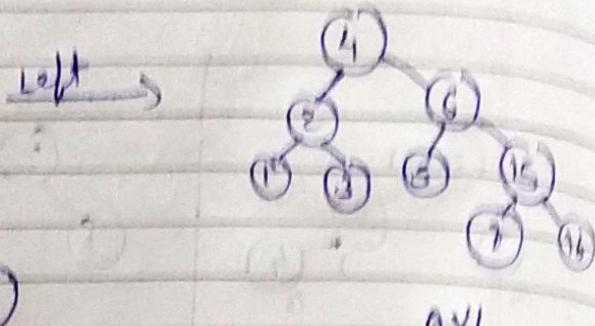
AVL



Not AVL

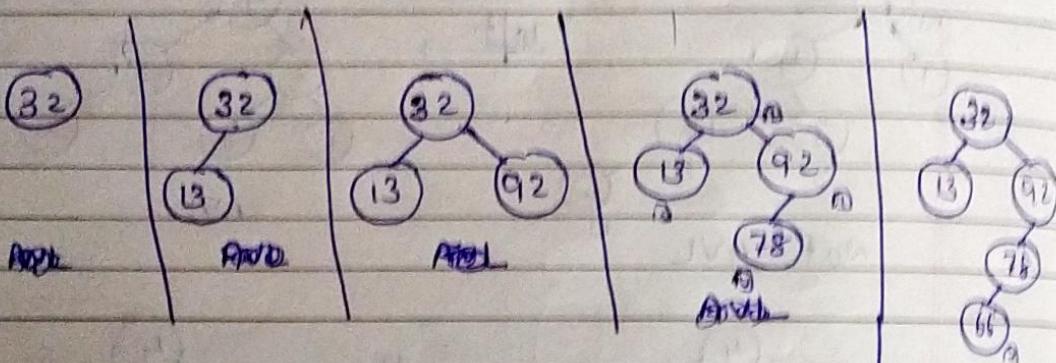


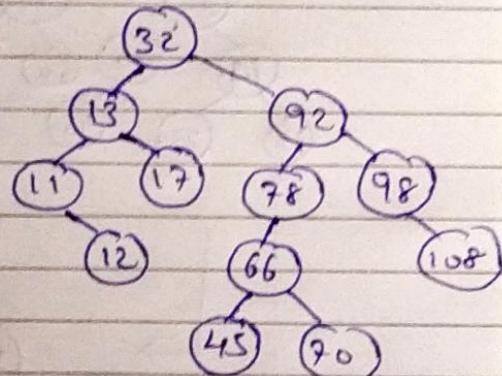
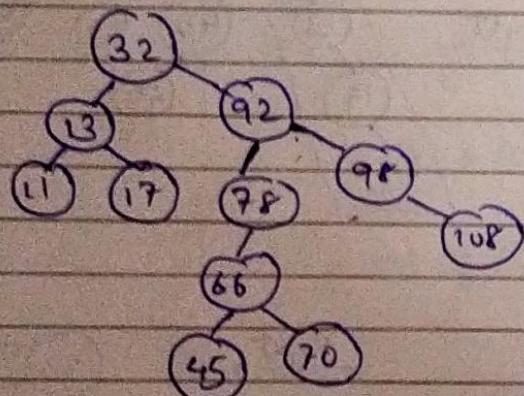
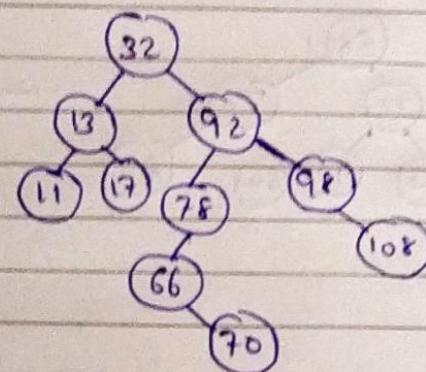
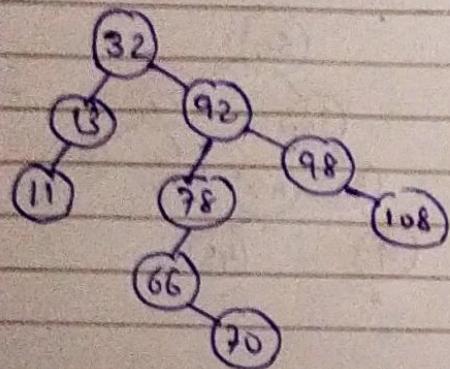
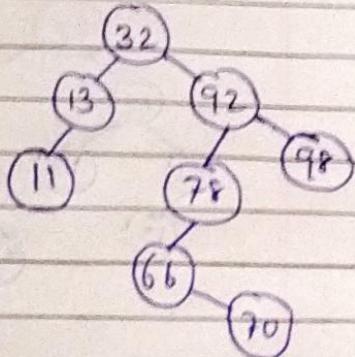
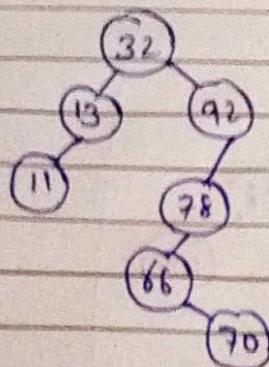
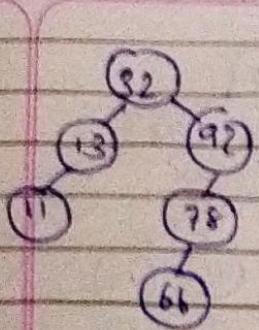
Not AVL

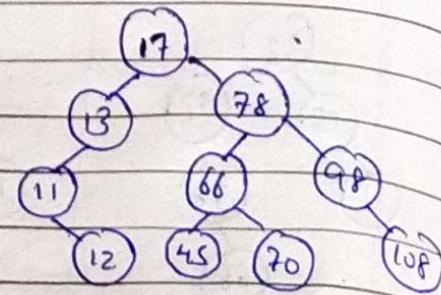
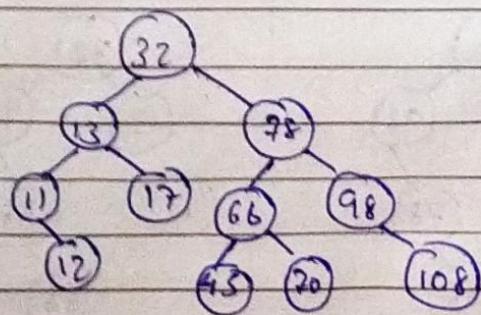


AVL

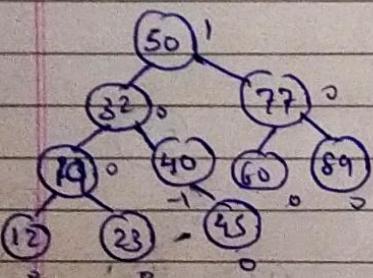
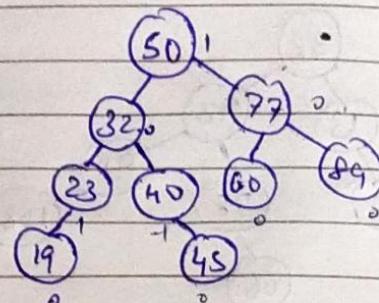
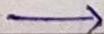
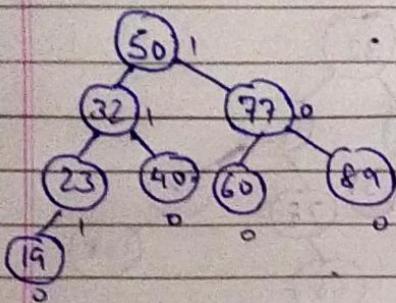
13) 32, 13, 92, 78, 66, 11, 70, 98, 108, 17, 45, 12



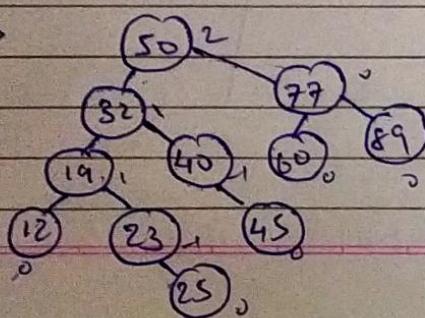
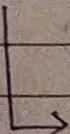
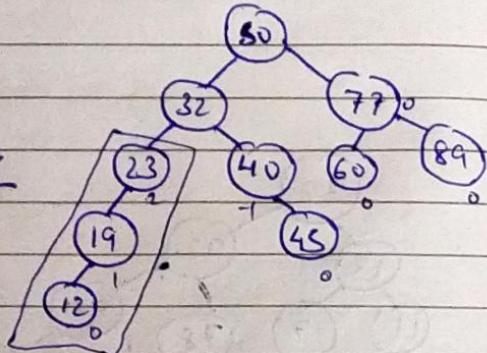




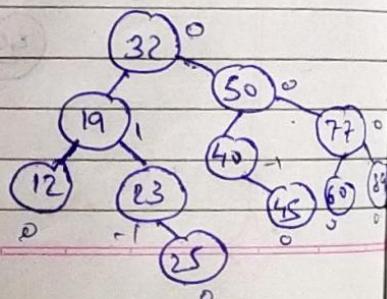
14)

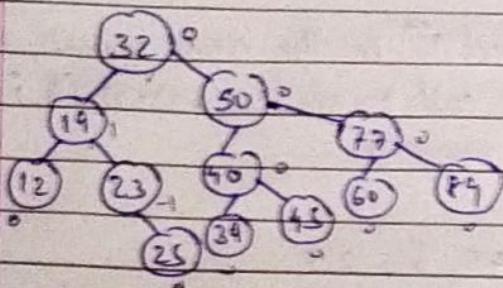


Right



Right





15) Suppose you are given an implementation of a queue of integers. The operations that can be performed on the queue are:

- (i) `isEmpty(Q)`: return true if the queue is empty, false otherwise
 - (ii) `delete(Q)`: delete the element at the front of the queue and returns its value.
 - (iii) `insert(Q, i)`: inserts the integer i at the rear of the queue.
- Consider the following function:

```
void f(queue Q)
{
```

```
    int i;
    if (!isEmpty(Q))
    {
        i = delete(Q);
        f(Q);
        insert(Q, i);
    }
}
```

}

What operation is performed by the above function f ?

Ans Reverses the order of the elements in the queue Q
 As, it is recursive call, and removing from front while inserting from end, that means last element will be deleted

at last and will be inserted 1^{st} in the new queue. And like it will continue till first call executes insert(0, i) function. So, the queue will be in reverse.

- 16) Data: 50, 47, 19, 21, 11, 45, 6, 25
 Hash F^n $H(x) = (x \bmod 5) + 3$

<u>Index</u>	<u>Data</u>
0	45
1	6
2	25
3	50
4	21
5	47
6	11
7	19

Hashing:

- 1) $(50 \bmod 5) + 3 = 3$
- 2) $(47 \bmod 5) + 3 = 5$
- 3) $(19 \bmod 5) + 3 = 7$
- 4) $(21 \bmod 5) + 3 = 4$
- 5) $(11 \bmod 5) + 3 = 4$ collision
 $(4+0) \bmod 8 = 4$ collision
 $(4+1) \bmod 8 = 4$ collision
 $(4+2) \bmod 8 = 6$ ✓

- 6) $(45 \bmod 5) + 3 = 2$ collision
 $(3+0) \bmod 8 = 3$ collision
 $(3+1) \bmod 8 = 4$ collision
 $(3+2) \bmod 8 = 5$ collision

$$(2+3) \bmod 8 = 6 \quad \text{collision}$$

$$(3+4) \bmod 8 = 7 \quad \text{collision}$$

$$(3+5) \bmod 8 = 0 \quad \checkmark$$

2) $(6 \bmod 5) + 3 = 4 \quad \text{collision}$

$$(4+0) \bmod 8 = 4 \quad \text{collision}$$

$$(4+1) \bmod 8 = 5 \quad \text{collision}$$

$$(4+2) \bmod 8 = 6 \quad \text{collision}$$

$$(4+3) \bmod 8 = 7 \quad \text{collision}$$

$$(4+4) \bmod 8 = 0 \quad \text{collision}$$

$$(4+5) \bmod 8 = 1 \quad \checkmark$$

8) $(25 \bmod 5) + 3 = 3 \quad \text{collision}$

$$(3+0) \bmod 8 = 4 \quad \text{collision}$$

$$(3+1) \bmod 8 = 5 \quad \text{collision}$$

$$(3+2) \bmod 8 = 6 \quad \text{collision}$$

$$(3+3) \bmod 8 = 7 \quad \text{collision}$$

$$(3+4) \bmod 8 = 8 \quad \text{collision}$$

$$(3+5) \bmod 8 = 0 \quad \text{collision}$$

$$(3+6) \bmod 8 = 1 \quad \text{collision}$$

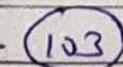
$$(3+7) \bmod 8 = 2 \quad \checkmark$$

so, final array using hashing is

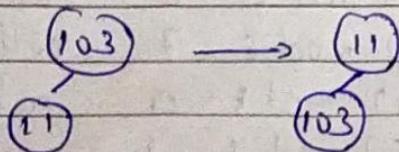
45, 6, 25, 50, 21, 47, 11, 19
 0 1 2 3 4 5 6 7

17) [103, 11, 101, 110, 111, 119, 19, 91]

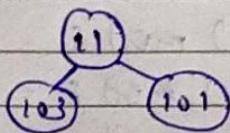
Step 1) Insert 103



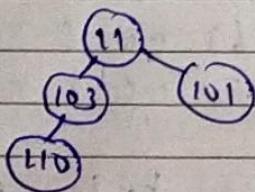
2) Insert 11 ($11 < 103$) so swap 11 & 103



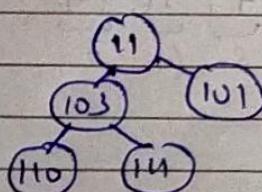
3) Insert 101



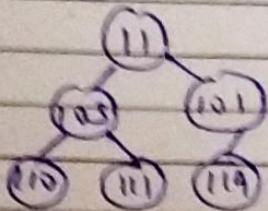
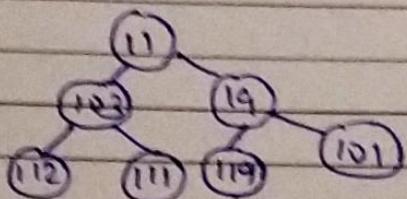
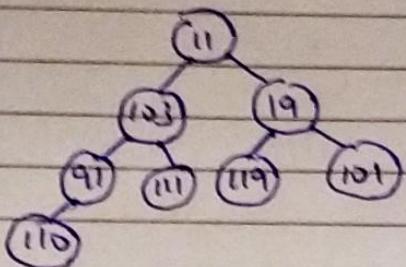
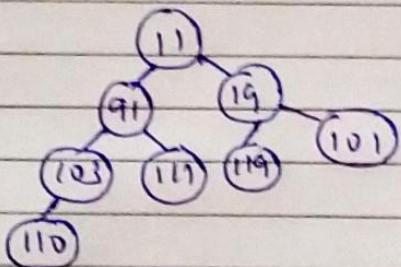
4) Insert 110 at bottom (start from left)



5) Insert 111 (at bottom)



Q) Insert 110

Q) Insert 19 ($19 < 101$) so swap $19 \leftrightarrow 101$ Q) Insert 91 ($91 < 110$) so swap $91 \leftrightarrow 110$ Q) ($91 < 103$) so swap $91 \leftrightarrow 103$ so, min. heap will be $\rightarrow 11, 91, 19, 103, 111, 119, 101, 110$