## 1.

(a) To find k, we know that the sum of all probabilities in a PMF should equal 1. We have an infinite geometric series where the first term a=k and the common ratio r=(3/4), so the sum S of this series is S=a/(1-r)=1. Solving this equation, we get:

$$k/(1 - 3/4) = 1$$
  
 $k = 1 - 3/4 = 1/4$ 

(b) The cumulative distribution function (CDF) is the sum of the probabilities up to a certain value of x. So, for x = 1, 2, 3, ... we have:

$$F(x) = P(1) + P(2) + \dots + P(x)$$

$$F(x) = k * [(3/4)^{1} + (3/4)^{2} + \dots + (3/4)^{x}]$$

$$F(x) = k * [1 - (3/4)^{x}] / [1 - (3/4)]$$

$$F(x) = 1 - (3/4)^{x}$$

## 2.

We will use the z-score formula  $z=(x-\mu)/\sigma$  to standardize each score, where x is the individual score,  $\mu$  is the mean, and  $\sigma$  is the standard deviation.

(a)  $z=(70-80.5)/9.9\approx-1.06$ . Looking up this z-score in a standard normal distribution table or using software gives a cumulative probability of  $\approx 0.1441$ .

(b)  $z_1 = (75 - 80.5) / 9.9 \approx -0.56$  and  $z_2 = (90 - 80.5) / 9.9 \approx 0.96$ . The proportion is  $P(z_2) - P(z_1) \approx 0.8315 - 0.2877 \approx 0.5438$ .

(c) 
$$z = (90 - 80.5) / 9.9 \approx 0.96$$
.

The proportion with hypertension is  $1 - P(z) \approx 1 - 0.8315 = 0.1685$ .

(d) 
$$z = (65 - 80.5) / 9.9 \approx -1.56$$
.

The proportion is  $P(z) \approx 0.0594$ , which is above 5%, so it's not considered unusual.

3.

(a) Using z-score, z=1.96 for the heaviest 2.5%. The weight that determines the overweight classification is  $\mu+z\sigma=10+1.96*0.2\approx10.392$  lbs.

(b) 
$$z_1 = (9.8 - 10) / 0.2 = -1$$
 and  $z_2 = (10.4 - 10) / 0.2 = 2$ . The proportion lost is  $P(z_2) - P(z_1) \approx 0.9772 - 0.1587 \approx 0.8185$ .

4.

(a) The sampling distribution of the mean is normally distributed with mean  $\mu$  = 50 and standard error  $\sigma = 6/sqrt(40) = 0.94868$ .

(b) 
$$z = (51 - 50) / (6/sqrt(40)) \approx 1.0541$$
  
The probability is  $1 - P(z) \approx 1 - 0.8543 = 0.1457$ .

(c) The probability is more than 5%, so it's not considered unusual.

5.

(a) According to the Central Limit Theorem, the sampling distribution of X is approximately normally distributed with mean  $\mu$  = 1 and standard error  $\sigma = 1/sqrt(70) = 0.119522$ .

(b) 
$$z = (1.1 - 1) / (1/sqrt(70)) \approx 0.8375$$
.  
The probability is  $1 - P(z) \approx 1 - 0.7985 = 0.2015$ .

(c) 
$$z = (1.25 - 1) / (1/sqrt(70)) \approx 2.0948$$

The probability is  $1 - P(z) \approx 1 - 0.9818 = 0.0182$ .