

Edge Detection

Audiovisual Processing CMP-6026A

Dr. David Greenwood

david.greenwood@uea.ac.uk

SCI 2.16a University of East Anglia

December 01 2021

Content

- Edges from image derivatives
- Laplacian matrices
- Line detection operators
- Canny edge detector

Edge Detection

Convert an image into a set of **curves**.

- Extracts salient *features* of the image.
- Far more *compact* than pixels.

Edges

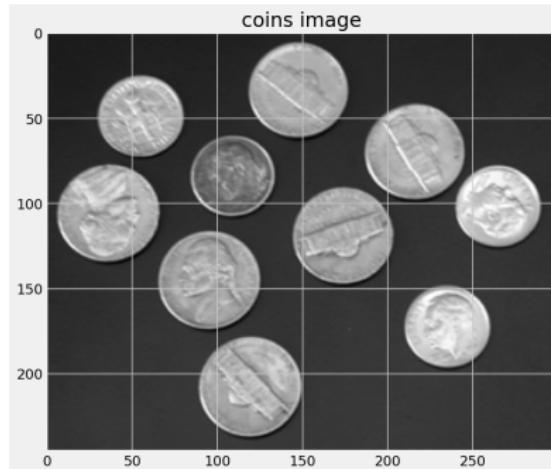
An *edge* in an image is a significant local change or discontinuity in the image intensity.

Edges

Edges come from discontinuity in:

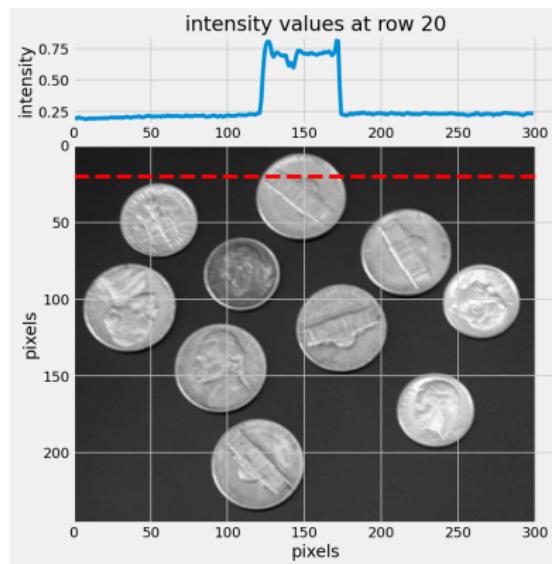
- surface normal
- depth
- surface color
- illumination

Edges



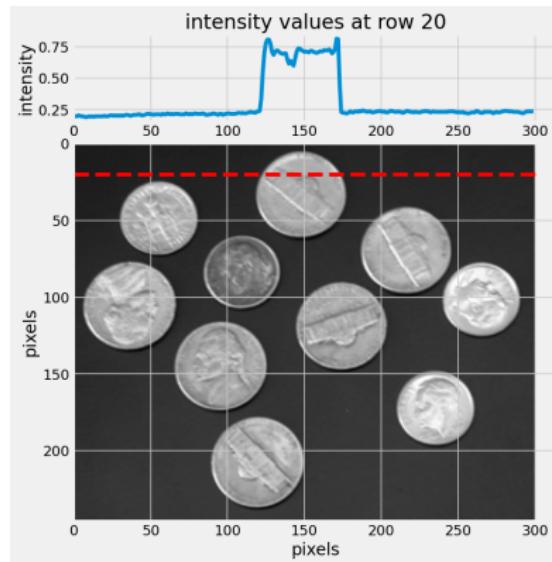
An image is a 2D matrix of intensities.

Edges



We can look at those intensities in a single row.

Edges



We can see how edges are defined by these changes in intensity.

Derivatives

The derivative is the rate of change of a function.

- 1D *first* order derivative: **difference** in consecutive pixels:

$$\frac{\delta f}{\delta x} \approx f(x + 1) - f(x)$$

Derivatives

The derivative is the rate of change of a function.

- 1D *second* order derivative: **acceleration** of pixel intensity change:

$$\frac{\delta^2 f}{\delta x^2} \approx f(x+1) + f(x-1) - 2f(x)$$

Derivatives

Required properties of first derivatives:

- Zero in regions of constant intensity
- Non-zero at onset of a ramp or step
- Non-zero along intensity ramps

Derivatives

Required properties of second derivatives:

- Zero in regions of constant intensity
- Non-zero at the onset **and** end of an intensity step or ramp.
- Zero along intensity ramps.

Derivatives

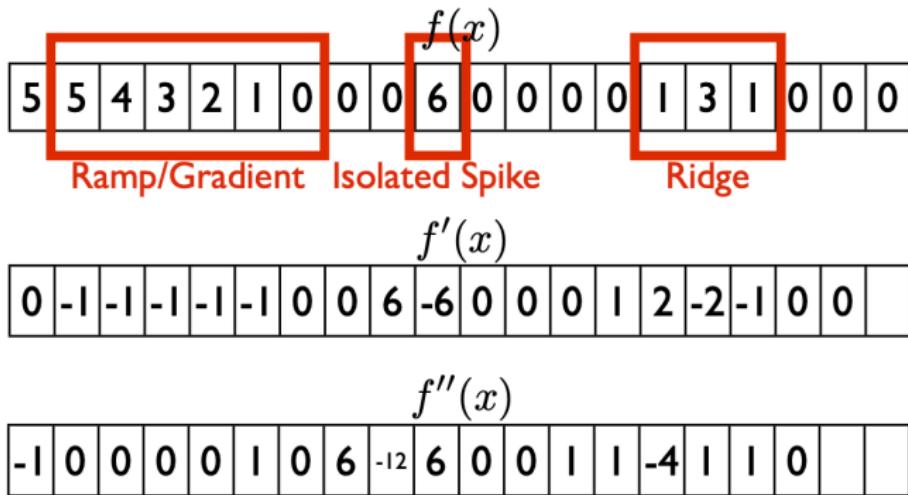


Figure 1: Example from Gonzalez and Woods.

Derivatives

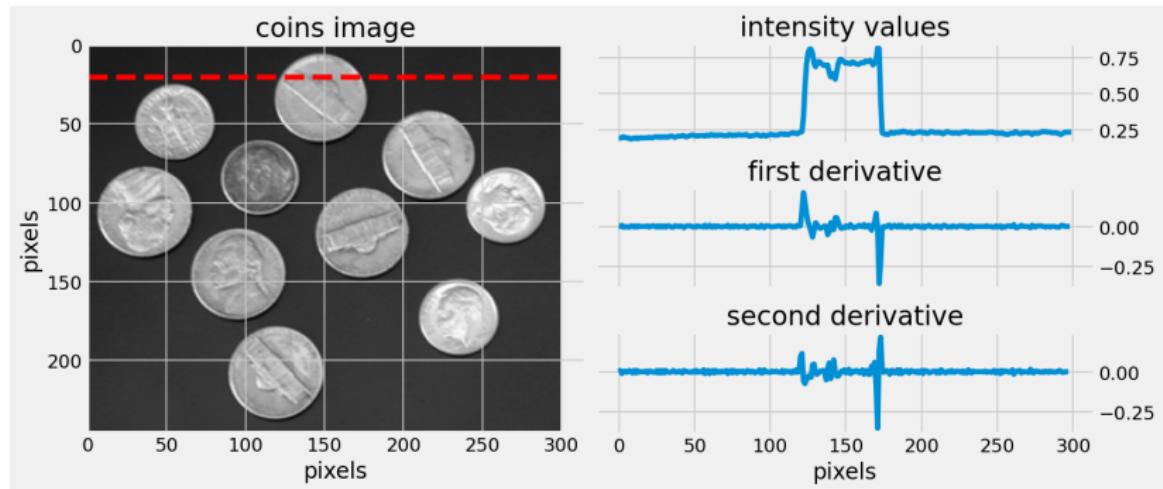


Figure 2: Intensity, first and second derivatives

Image Derivatives

For images, we must consider the derivative in both directions:

$$\frac{\delta f}{\delta x} \approx f(x + 1, y) - f(x, y)$$

$$\frac{\delta f}{\delta y} \approx f(x, y + 1) - f(x, y)$$

Image Derivatives

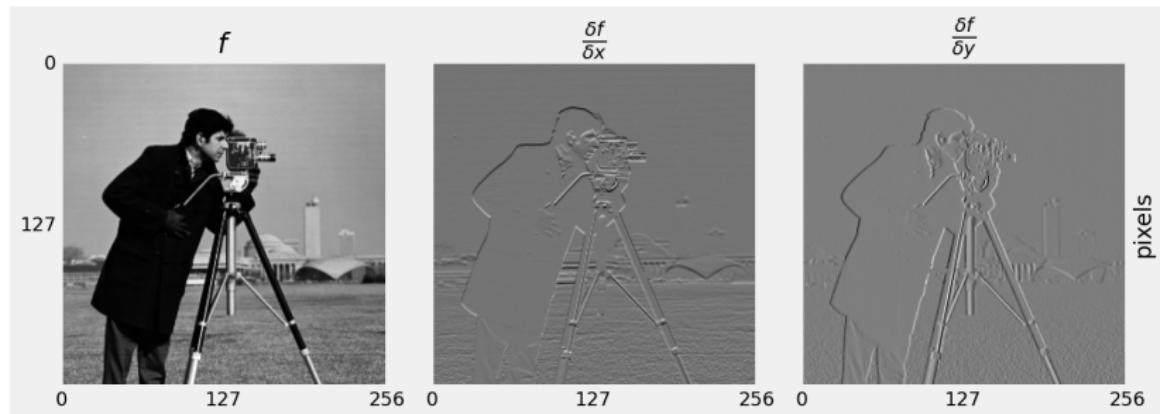


Figure 3: x and y first derivatives

Image Derivatives

An image *gradient* is formed of two components:

$$\nabla f = \left[\frac{\delta f}{\delta x}, \frac{\delta f}{\delta y} \right]$$

Image Derivatives

Image gradient is a vector:

$$\nabla f = \left[\frac{\delta f}{\delta x}, \frac{\delta f}{\delta y} \right]$$

Image Derivatives

A vector has magnitude . . .

$$|\nabla f| = \sqrt{\left(\frac{\delta f}{\delta x}\right)^2 + \left(\frac{\delta f}{\delta y}\right)^2}$$

Magnitude is the *strength* of the edge.

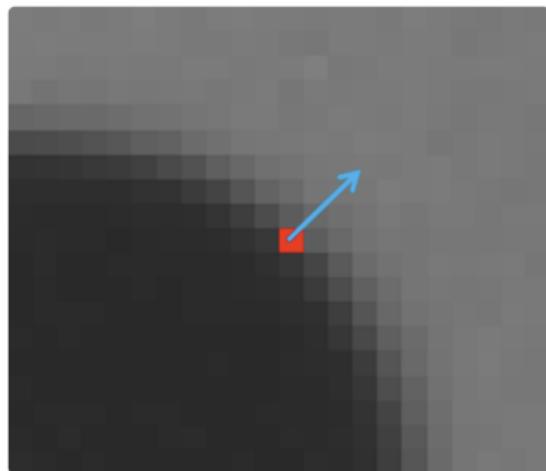
Image Derivatives

A vector has direction...

$$\theta = \tan^{-1} \left(\frac{\delta f}{\delta y} / \frac{\delta f}{\delta x} \right)$$

Direction of an edge is **perpendicular** to the gradient direction.

Image Derivatives



- The gradient points in the direction of most rapid change in intensity.
- **Perpendicular** to the edge direction.

Figure 4: gradient direction

Image Derivatives

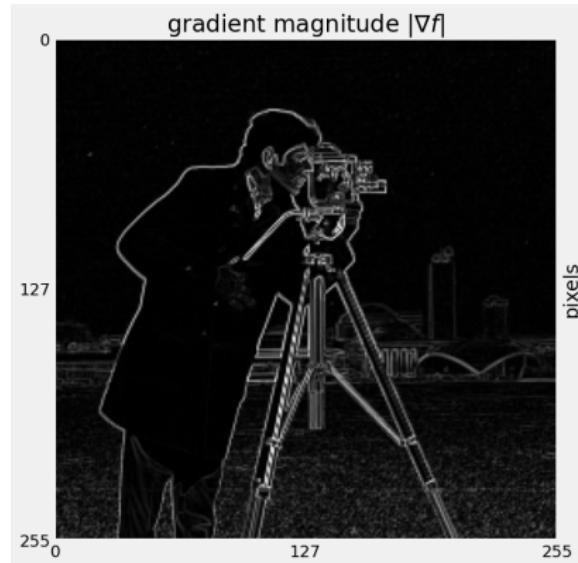


Figure 5: gradient magnitude as greyscale

Image Derivatives

First order derivatives:

- produce thicker edges in images
- have a stronger response to stepped intensity changes

Second Order Derivatives

Second order derivatives:

- have a stronger response to fine detail
- are more aggressive at enhancing detail
- Generally, second-order derivatives are *preferred*.

Second Order Derivatives

$$\nabla^2 f = \frac{\delta^2 f}{\delta x^2} + \frac{\delta^2 f}{\delta y^2}$$

Derivative in this form is known as the **Laplacian**.

Laplacian

We know:

$$\frac{\delta^2 f}{\delta x^2} \approx f(x+1) + f(x-1) - 2f(x)$$

$$\frac{\delta^2 f}{\delta y^2} \approx f(y+1) + f(y-1) - 2f(y)$$

Laplacian

So, the Laplacian is calculated as:

$$\nabla^2 f = f(x+1) + f(x-1) + f(y+1) + f(y-1) - 4f(x, y)$$

Laplacian

$$\begin{bmatrix} 0 & 1 & 0 \\ 1 & -4 & 1 \\ 0 & 1 & 0 \end{bmatrix}$$

The Laplacian can also be calculated by **convolving** the image with this filter.

Laplacian

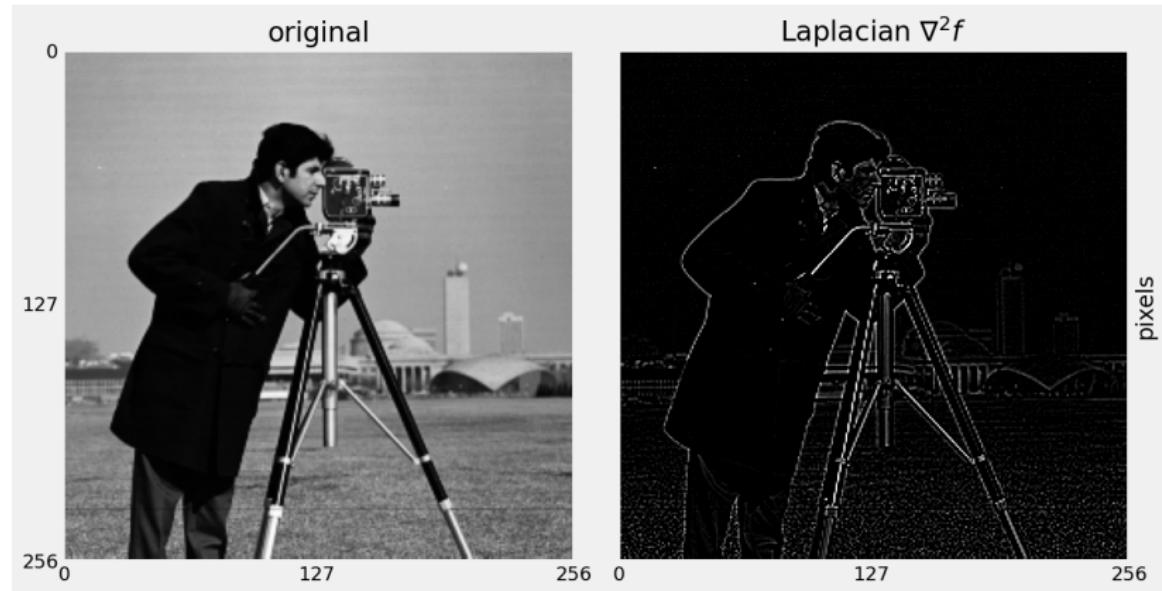


Figure 6: Laplacian

Laplacian

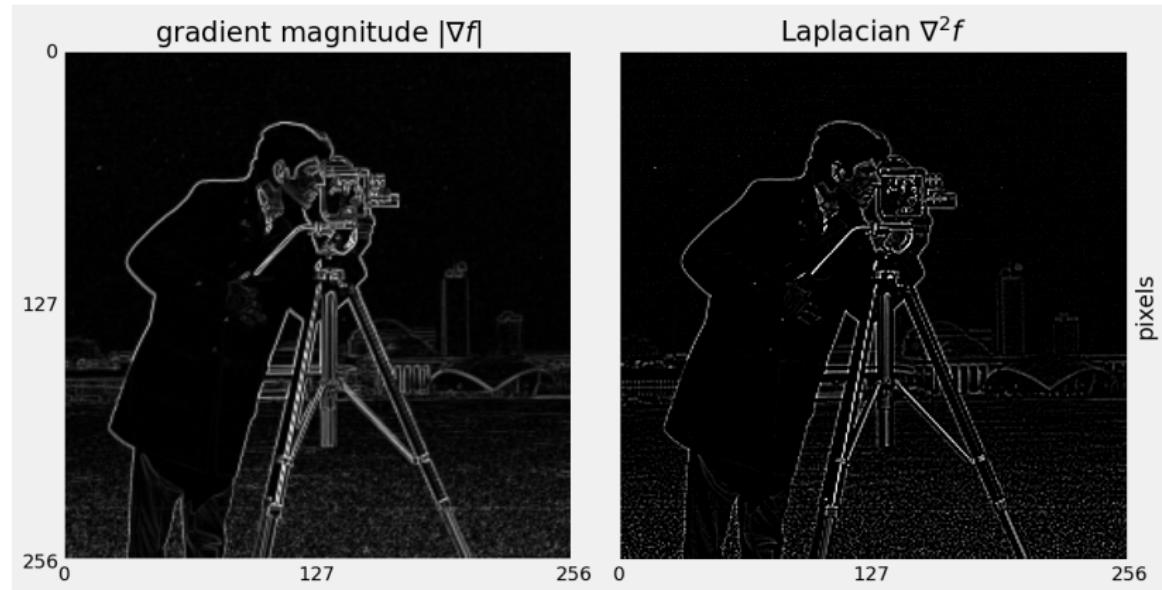


Figure 7: Gradient magnitude and Laplacian

Line Detection

The Laplacian responds strongly to *any* detail in the image.

Line Detection

What if we only wanted to detect lines that point in a certain direction?

$$\begin{bmatrix} -1 & 2 & -1 \\ -1 & 2 & -1 \\ -1 & 2 & -1 \end{bmatrix}$$

Line Detection

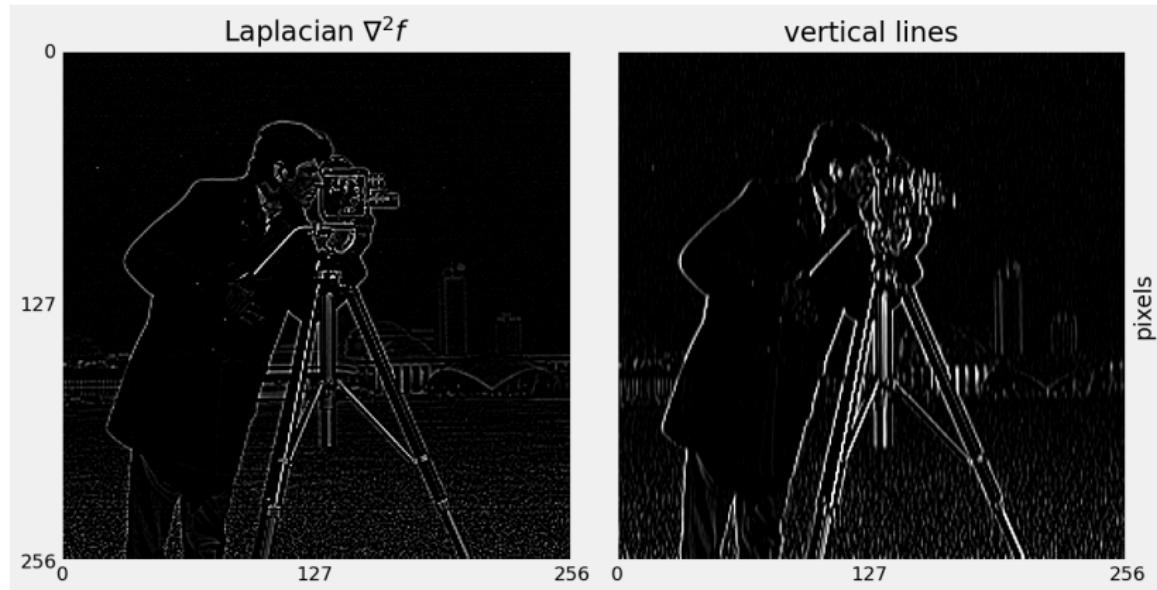


Figure 8: Line Detection

Line Detection

What about detecting edges in other directions?

vertical	forward diagonal	horizontal	backward diagonal
-1 2 -1	-1 -1 2	-1 -1 -1	2 -1 -1
-1 2 -1	-1 2 -1	2 2 2	-1 2 -1
-1 2 -1	2 -1 -1	-1 -1 -1	-1 -1 2

Figure 9: Line directions

Line Detection

What about detecting edges in other directions?

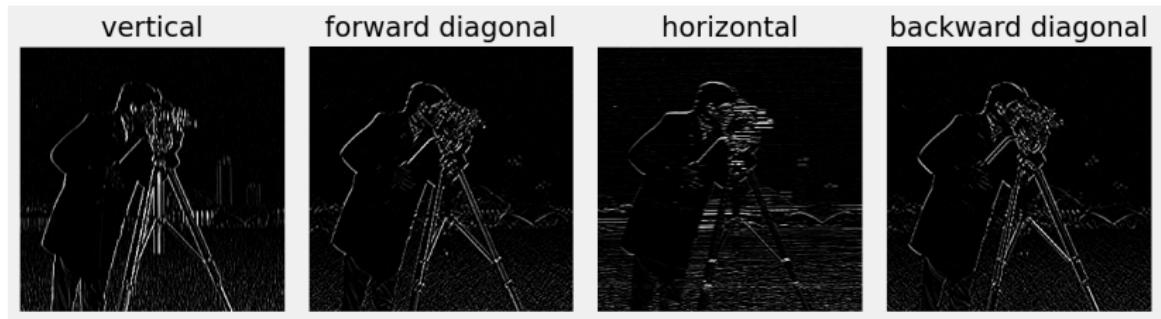


Figure 10: Line directions

Line Detection

Previous filter gives strong response along a line.

- **But...** also responds at isolated pixels.
- Edge detector should respond *only* to edges

Line Detection

Look either side of candidate pixel...

- but ignore the pixel itself.

Line Detection

Two popular *first-order* operators are **Prewitt** and **Sobel**.

Both provide approximations of derivatives.

Line Detection

Prewitt operators		
1	1	1
0	0	0
-1	-1	-1
0	1	1
-1	0	1
-1	-1	0
-1	0	1
-1	0	1
0	1	1
-1	-1	-1
0	0	0
1	1	1
0	-1	-1
1	0	-1
1	1	0
1	0	-1
1	0	-1
1	1	0
1	0	-1
0	-1	-1

Figure 11: Prewitt, J.M.S. (1970). "Object Enhancement and Extraction"

Line Detection

Prewitt responses

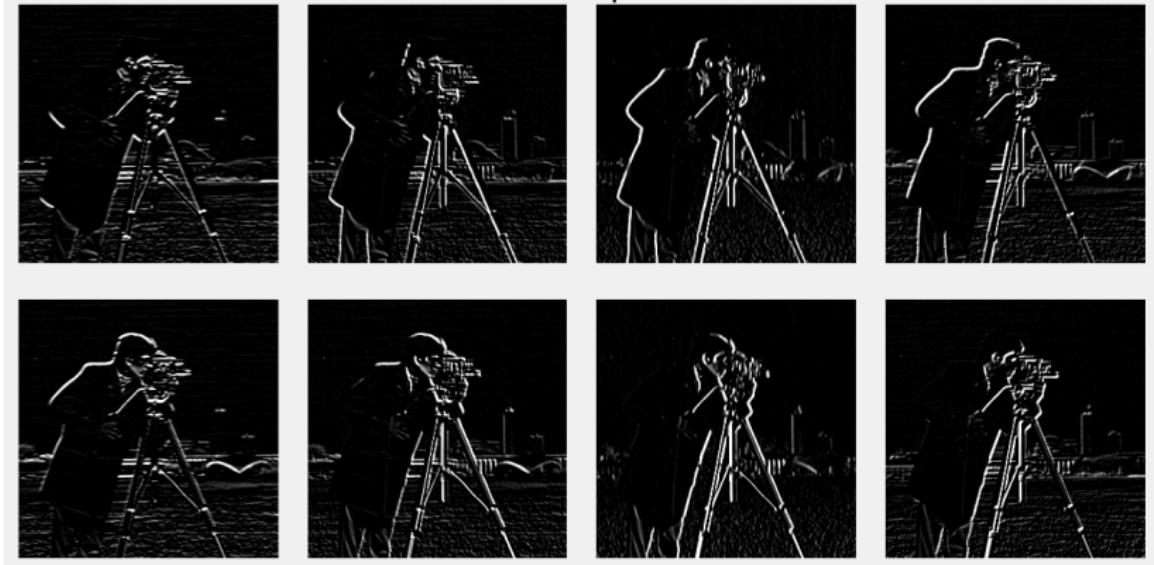


Figure 12: Prewitt responses

Line Detection

Sobel operators		
1 2 1	0 1 2	-1 0 1
0 0 0	-1 0 1	-2 0 2
-1 -2 -1	-2 -1 0	-1 0 1
-1 -2 -1	0 -1 -2	1 0 -1
0 0 0	1 0 -1	2 0 -2
1 2 1	2 1 0	1 0 -1
2 1 0	1 0 -1	0 -1 -2
1 0 -1	0 -1 -2	
0 -1 -2		

Figure 13: Sobel, I. (1968) “An Isotropic 3x3 Image Gradient Operator”

Line Detection

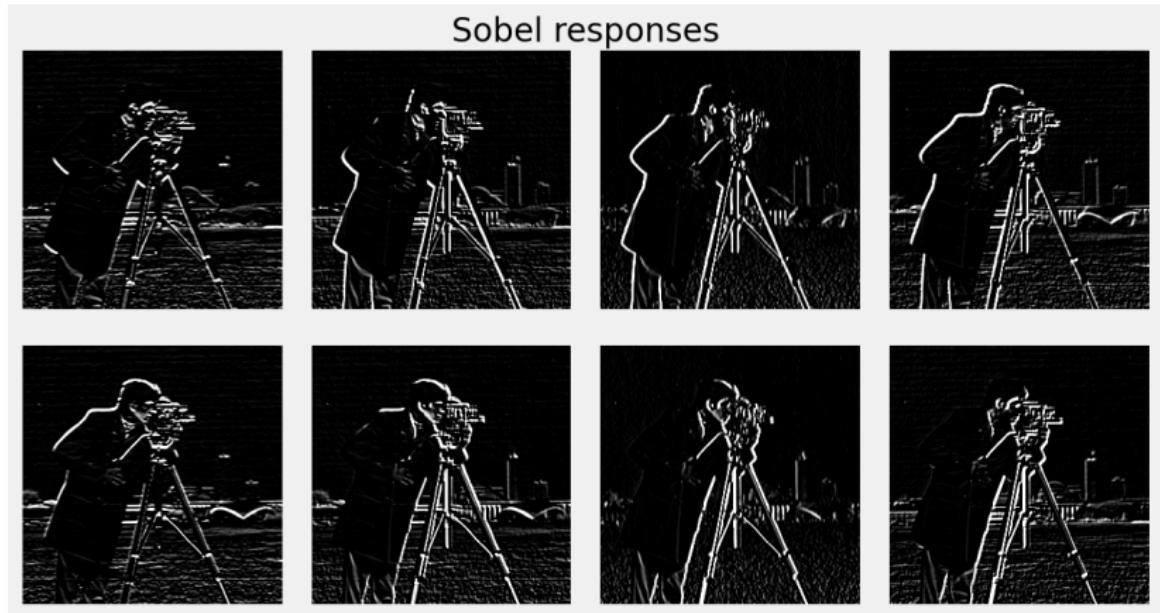


Figure 14: Sobel responses

For each pixel, find the maximum value from all of the filter responses, and then threshold.

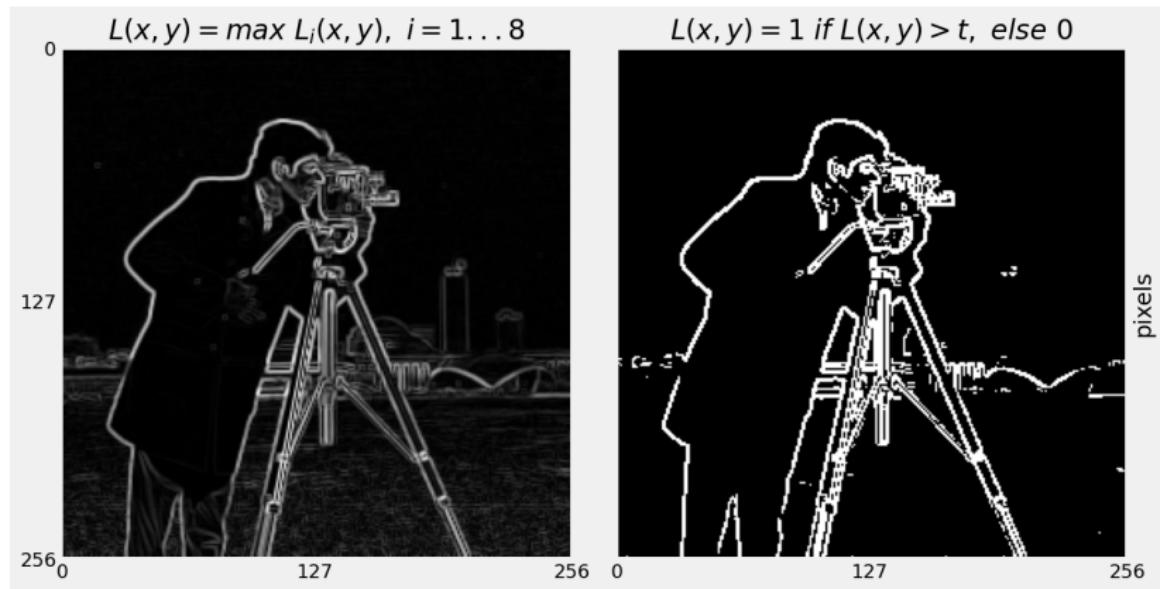


Figure 15: Sobel maximum

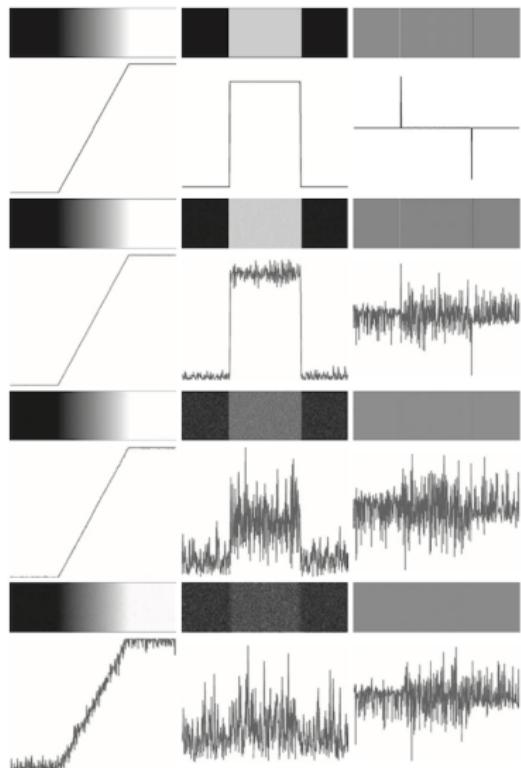


Figure 16: Gonzalez and Woods

We rarely observe *ideal* edges in real images.

- Lens imperfections
- sensor noise, etc.
- Edges appear more like noisy ramps.

Edge Detection

Four limitations with basic gradient-based edge detection:

- Hard to set the optimal value for the threshold.
- Edges are broken (known as streaking)
- Edges can be poorly localised
- An edge might produce more than one response

Canny Edge Detector

The **Canny Edge Detector** is *optimal* with respect to gradient-based limitations.

Canny Edge Detector

Requirements for a *good* edge detector:

- Good detection - respond to edges, not noise.
- Good localisation - detected edge near real edge.
- Single response - only one response per edge.

Canny Edge Detector

Canny provides an elegant solution to edge detection.

- Canny provides a *hacky* solution to edge detection!

Canny Edge Detector

Canny Edge Detection is a four step process:

1. Convolve image with Gaussians of particular scales.
2. Compute gradient magnitude and direction.
3. Perform **non-maximal** suppression to thin the edges.
4. Threshold edges with **hysteresis**.

Canny Edge Detector

Step 1: Convolve image with Gaussians of particular scales.

- Smoothing helps ensure robustness to noise.
- The size of the Gaussian kernel affects the performance of the detector.

Canny Edge Detector

Step 2: Compute gradient *magnitude* and *direction*:

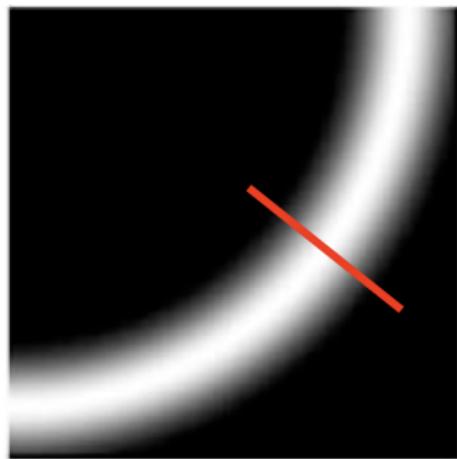
- Using Sobel operators.

Quantise the angle of the gradient:

- Discrete nature of image limits the possible angle.
- Angle can only be $\{0, 45, 90, 135\}$ degrees.

Canny Edge Detector

Step 3: Perform **non-maximal** suppression.



- An edge-thinning technique.
- Searches for maximum value along direction of gradient and sets all others to zero.
- Result is a one pixel wide curve.

Figure 17: direction of gradient

Canny Edge Detector

Step 4: Threshold edges with **hysteresis**.

- Hysteresis is the dependence of the state of a system on its history.

Canny Edge Detector

Step 4: Threshold edges with **hysteresis**.

Use **two** thresholds: T_{min} and T_{max} .

$$E(x, y) = \begin{cases} 1 & E(x, y) \geq T_{max} \\ 0 & E(x, y) < T_{min} \end{cases}$$

Canny Edge Detector

Step 4: Threshold edges with **hysteresis**.

$$E(x, y) = \begin{cases} 1 & T_{min} \leq E(x, y) < T_{max} \iff \text{linked to an edge} \\ 0 & T_{min} \leq E(x, y) < T_{max} \text{ otherwise} \end{cases}$$

Canny Edge Detector

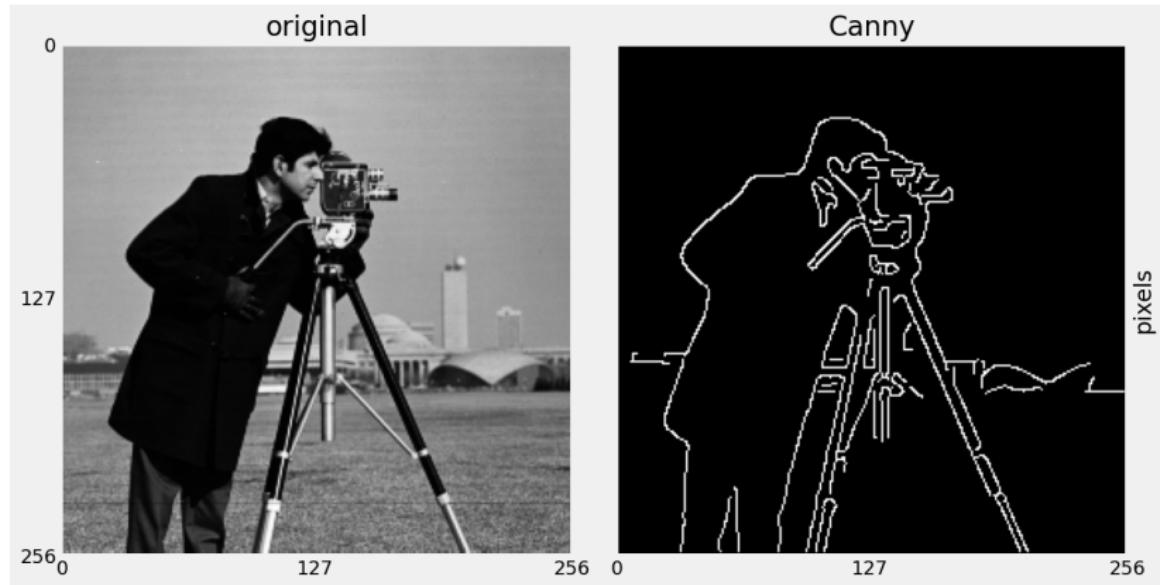


Figure 18: Canny edge detection

Canny Edge Detector

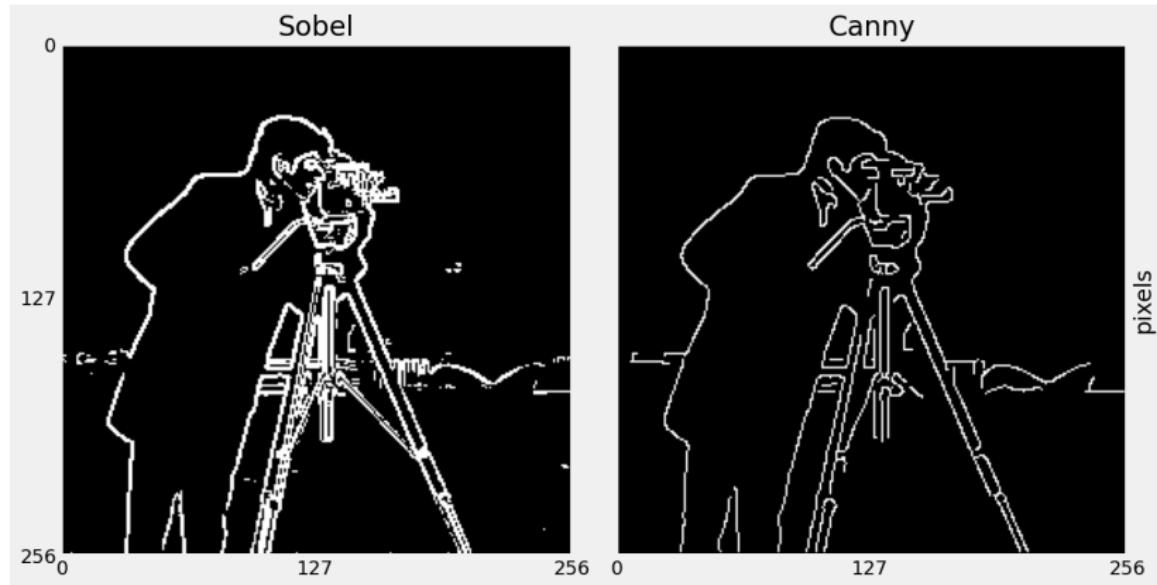


Figure 19: Max Sobel compared to Canny

Summary

- Image derivatives
- Laplacian operator
- Line detection kernels
- Canny Edge Detector