Session 5. Introduction to statistical inference

Example 1

- Read the Osteoporosis dataset and turn factors into variables automatically with Rbase function read delim
- Take a sample of size 100 from the original file. Call it 'osteo 100' and work with this file from now on.
- Compute the mean value of the variable containing bone density values BUA
- Split the computation between all subgroups from variable classific and variable menop
- Compute the percentage of menopausic women from variable menop

```
library(dplyr)
## Attaching package: 'dplyr'
## The following objects are masked from 'package:stats':
##
##
       filter, lag
## The following objects are masked from 'package:base':
##
##
       intersect, setdiff, setequal, union
# Read data
osteoporosis <- read.delim2("datasets/osteoporosis.csv", stringsAsFactors=TRUE)
# Take subsample
osteo100 <- sample_n(osteoporosis, 100)</pre>
# mean bone density
buaMean <- mean(osteo100$bua)
print(buaMean)
## [1] 72.39
# Mean bone density ny groups
osteo100 %>%
  group_by(menop) %>%
 summarize(m = mean(bua))
## `summarise()` ungrouping output (override with `.groups` argument)
## # A tibble: 2 x 2
##
    menop
     <fct> <dbl>
##
## 1 NO
            82.9
## 2 SI
# Proportion of menop women (Proportion is a mean of 0-1 values)
mean(ifelse(osteo100$menop=="SI",1,0))
## [1] 0.71
```

Exercise 1

- Read the diabetes dataset. Convert characters into factors before continuing.
- Provide an estimate of
 - The distribution of a numerical variable.
 - a proportion of at least one categorical variable and
 - the mean value of at least one numerical variable.
- Could you have used different estimators?
- How would you decide?

First we read data and recode character values into factors.

```
library(readxl)
library(dplyr)
library(magrittr)
diabetes <- read_excel("datasets/diabetes.xls")</pre>
sapply(diabetes, class)
##
                                tempsviu
                                                                       edatdiag
      numpacie
                       mort
                                                 edat
                                                               bmi
     "numeric" "character"
                                                         "numeric"
##
                               "numeric"
                                            "numeric"
                                                                     "numeric"
##
         tabac
                        sbp
                                     dbp
                                                  ecg
                               "numeric" "character"
## "character"
                  "numeric"
                                                      "character"
diabetes_factor <- diabetes %>%
  mutate_if(sapply(diabetes, is.character), as.factor) %>%
  select (-numpacie)
sapply(diabetes_factor, class)
##
        mort tempsviu
                              edat
                                         bmi
                                              edatdiag
                                                             tabac
    "factor" "numeric" "numeric" "numeric" "numeric"
                                                         "factor" "numeric" "numeric"
##
##
         ecg
                    chd
##
    "factor"
               "factor"
Next provide a quick summary of each variable
```

```
summary(diabetes_factor)
```

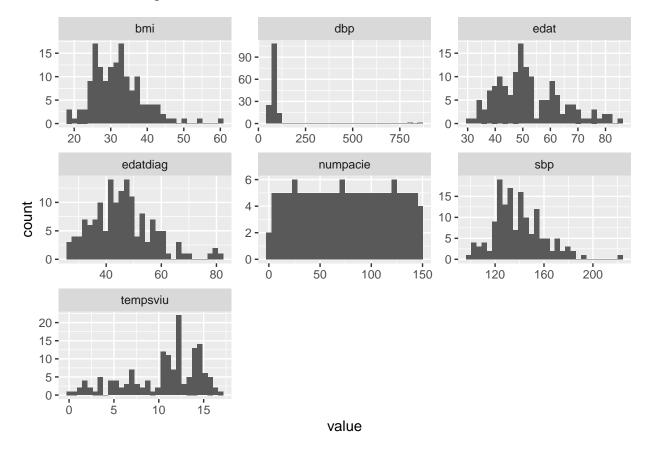
```
edatdiag
                                         edat
##
        mort
                     tempsviu
                                                          bmi
                                                             :18.20
                                                                              :26.00
##
    Muerto: 25
                  Min.
                         : 0.00
                                   Min.
                                           :31.00
                                                     Min.
                                                                      Min.
                                                     1st Qu.:26.60
                                                                      1st Qu.:38.00
##
    Vivo :124
                  1st Qu.: 7.30
                                    1st Qu.:43.00
                  Median :11.60
                                   Median :50.00
##
                                                     Median :31.20
                                                                      Median :45.00
##
                  Mean
                          :10.52
                                   Mean
                                           :52.17
                                                     Mean
                                                             :31.78
                                                                      Mean
                                                                              :45.99
##
                  3rd Qu.:13.90
                                    3rd Qu.:60.00
                                                     3rd Qu.:35.20
                                                                      3rd Qu.:53.00
##
                  Max.
                          :16.90
                                   Max.
                                           :86.00
                                                     Max.
                                                             :59.70
                                                                      Max.
                                                                              :81.00
##
           tabac
                           sbp
                                            dbp
                                                                ecg
                                                                          chd
##
    Ex fumador:41
                             : 98.0
                                              : 58.00
                                                                         No:99
                     Min.
                                       Min.
                                                         Anormal: 11
##
    Fumador
               :51
                     1st Qu.:124.0
                                       1st Qu.: 74.00
                                                         Frontera: 27
                                                                         Si:50
##
    No fumador:57
                     Median :138.0
                                       Median : 80.00
                                                         Normal:111
##
                     Mean
                             :139.1
                                       Mean
                                              : 90.04
                                       3rd Qu.: 88.00
##
                     3rd Qu.:152.0
##
                     Max.
                             :222.0
                                       Max.
                                              :862.00
```

Plotting all variables with an instruction is a bit tricky. May be easier to plot separately numerical and categorical variables.

```
library(ggplot2)
library(tidyr)
```

```
## Attaching package: 'tidyr'
## The following object is masked from 'package:magrittr':
##
##
       extract
library(purrr)
##
## Attaching package: 'purrr'
  The following object is masked from 'package:magrittr':
##
##
##
       set_names
diabetes %>%
  keep(is.numeric) %>%
  gather() %>%
  ggplot(aes(value)) +
    facet_wrap(~ key, scales = "free") +
    geom_histogram()
```

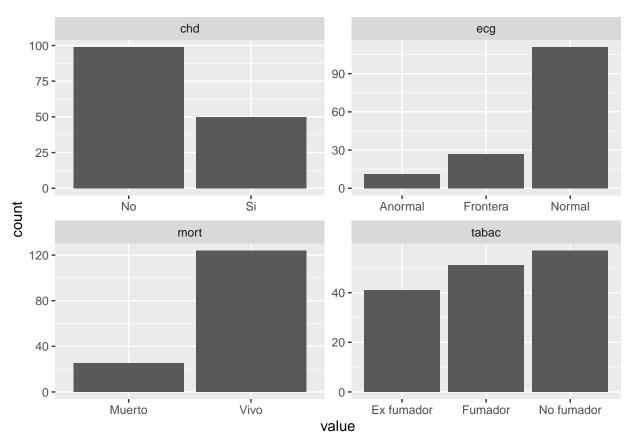
`stat_bin()` using `bins = 30`. Pick better value with `binwidth`.



Proceed similarly with categorical variables

```
diabetes %>%
  keep(is.character) %>%
  gather() %>%
```

```
ggplot(aes(value)) +
  facet_wrap(~ key, scales = "free") +
  geom_bar()
```



You may notice -or not- that the dataset has some outlier values.

Before removing them consider estimating the mean nvalue of SBP and DBP with distinct estimators

```
with(diabetes_factor, {
    print("DBP")
    show(summary(dbp))
    print("SBP")
    show(summary(sbp))
}
```

```
## [1] "DBP"
##
      Min. 1st Qu.
                     Median
                               Mean 3rd Qu.
                                                 Max.
                                       88.00
##
     58.00
             74.00
                      80.00
                               90.04
                                              862.00
## [1] "SBP"
                               Mean 3rd Qu.
##
      Min. 1st Qu.
                     Median
                                                 Max.
##
      98.0
             124.0
                      138.0
                               139.1
                                       152.0
                                                222.0
```

What is prefereable to estimate the mean SBP or DBP?

Example 2. Computing Confidence Intervals with R (2)

```
t.test(osteo100[["bua"]])

##

## One Sample t-test

##

## data: osteo100[["bua"]]

## t = 39.783, df = 99, p-value < 2.2e-16

## alternative hypothesis: true mean is not equal to 0

## 95 percent confidence interval:

## 68.77944 76.00056

## sample estimates:

## mean of x

## 72.39</pre>
```

Example 2. Computing Confidence Intervals with R (3)

```
cntMenop <- table(osteo100[["menop"]])["SI"]</pre>
ssize <- length(osteo100[["menop"]])</pre>
prop.test (x=cntMenop, n=ssize)
##
   1-sample proportions test with continuity correction
##
##
## data: cntMenop out of ssize, null probability 0.5
## X-squared = 16.81, df = 1, p-value = 4.132e-05
## alternative hypothesis: true p is not equal to 0.5
## 95 percent confidence interval:
## 0.6093752 0.7942336
## sample estimates:
##
      р
## 0.71
```

Exercise 2.1 Computing Confidence intervals

- Read the file "osteoporosis.csv" into a dataset and call it "osteoporosis"
- Compute confidence intervals for the BUA mean and for the percentage of menopausic women with all the individuals in the dataset.
- Compare these confidence intervals with those that you obtained in example 2. How do they differ?

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Exercise 2.2 Computing Confidence intervals

• Read the diabetes dataset. Convert characters into factors before continuing.

```
library(readxl)
library(dplyr)
library(magrittr)
```

```
diabetes <- read_excel("datasets/diabetes.xls")</pre>
sapply(diabetes, class)
##
      numpacie
                                tempsviu
                                                 edat
                                                                      edatdiag
                       mort
                                                               bmi
     "numeric" "character"
                                                                     "numeric"
##
                               "numeric"
                                            "numeric"
                                                        "numeric"
##
         tabac
                        sbp
                                     dbp
                                                  ecg
## "character"
                  "numeric"
                               "numeric" "character" "character"
diabetes_factor <- diabetes %>%
  mutate_if(sapply(diabetes, is.character), as.factor) %>%
  select (-numpacie)
sapply(diabetes_factor, class)
##
        mort tempsviu
                             edat
                                         bmi edatdiag
                                                            tabac
                                                                                    dbp
##
    "factor" "numeric" "numeric" "numeric"
                                                         "factor" "numeric" "numeric"
##
         ecg
                    chd
    "factor"
               "factor"
  • Provide a confidence interval for:

    a proportion of at least one categorical variable and

    the mean value of at least one numerical variable.

cnt <- table(diabetes[["mort"]])["Muerto"]</pre>
ssize <- length(diabetes[["mort"]])</pre>
prop.test (x=cnt, n=ssize)
##
##
    1-sample proportions test with continuity correction
##
## data: cnt out of ssize, null probability 0.5
## X-squared = 64.456, df = 1, p-value = 9.869e-16
## alternative hypothesis: true p is not equal to 0.5
## 95 percent confidence interval:
## 0.1134978 0.2396854
## sample estimates:
##
## 0.1677852
t.test(diabetes[["edat"]])
##
##
    One Sample t-test
##
## data: diabetes[["edat"]]
## t = 54.09, df = 148, p-value < 2.2e-16
## alternative hypothesis: true mean is not equal to 0
## 95 percent confidence interval:
## 50.26188 54.07370
## sample estimates:
## mean of x
## 52.16779

    How would you find alternative approaches to compute these confidence intervals?
```

Using formulas directly calculating from $\bar{x} \pm t_{\alpha/2} \frac{s}{\sqrt{x}}$

• Why would you want to do such a thing?

```
mostra<-diabetes[["edat"]]
m<-mean(mostra) # Calculate mean
sd<-sd(mostra) # Calculate standard deviation</pre>
se<-sd/sqrt(length(mostra)) # Calculate standard Error</pre>
li<- m-qt(.975,length(mostra)-1)*se # Calculate 95% CI lower bound
ls<- m+qt(.975,length(mostra)-1)*se # Calculate 95%CI upper bound
cat("Mean=",m,"\n")
## Mean= 52.16779
cat("Standard deviation=",sd,"\n")
## Standard deviation= 11.77285
cat("Standard error=",se,"\n")
## Standard error= 0.9644696
cat("95% Confidence interval=(",li,";",ls,")","\n")
## 95% Confidence interval=( 50.26188 ; 54.0737 )
Se calcula el intervalo de confianza como \overline{p} \pm z_{1-\alpha/2} \sqrt{\frac{\overline{p}(\overline{1-\overline{p}})}{n}}
cnt <- table(diabetes[["mort"]])["Muerto"]</pre>
ssize <- length(diabetes[["mort"]])</pre>
p<-cnt/ssize
n<-ssize
z<-qnorm(.975)
ee < -sqrt((p*(1-p))/n)
lowerli<- p-z*ee
upperli<- p+z*ee
cat("95% confidence interval for ", p ,"=(",lowerli,";",upperli,")","\n")
## 95\% confidence interval for 0.1677852 = (0.1077855; 0.227785)
```

Example 3. Sample size calculation

- Using the osteoporosis dataset, assume that the standard deviation is a good approximation to σ .
- Find the sample size needed to achieve a margin of error equal to 5 with a 95% confidence interval.

Function is the solution sample.size.mean(e, S, N = Inf, level = 0.95)

```
library(samplingbook)

## Loading required package: pps

## Loading required package: sampling

## Loading required package: survey

## Loading required package: grid
```

```
## Loading required package: Matrix
##
## Attaching package: 'Matrix'
##
  The following objects are masked from 'package:tidyr':
##
       expand, pack, unpack
##
## Loading required package: survival
##
## Attaching package: 'survival'
## The following objects are masked from 'package:sampling':
##
##
       cluster, strata
##
## Attaching package: 'survey'
## The following object is masked from 'package:graphics':
##
       dotchart
osteoporosis <- read.delim2("datasets/osteoporosis.csv", stringsAsFactors=TRUE)
sdbua<-sd(osteoporosis$bua)</pre>
merror<-5
sample.size.mean(merror,sdbua)
##
## sample.size.mean object: Sample size for mean estimate
## Without finite population correction: N=Inf, precision e=5 and standard deviation S=16.8093
## Sample size needed: 44
```

Exercise 3. Sample size calculation

Sample size formula is

$$n = \frac{\overline{p}(1-\overline{p})z_{1-\alpha/2}^2}{marginerror^2}$$

- Write a function to compute the sample size for proportions in the worst case (p=q=0.5) or assuming p is known.
 - Using a 50% planned proportion estimate, find the sample size needed to achieve 5 margin of error for a survey at 95 confidence level.
 - How would this result change if we are told that a pilot study suggests that p = 10%?

```
alpha<-1-.95
z<-qnorm(1-alpha/2)
merror<-0.05
p<-0.5 # Worst proportion
nsample<- (p*(1-p) * z^2)/0.05^2
cat("Sample size for 95% CI and 5% margin error s ",round(nsample))</pre>
```

Sample size for 95% CI and 5% margin error s 384

```
p<-.1 # Worst proportion</pre>
nsample < (p*(1-p) * z^2)/0.05^2
cat("Sample size for 95% CI and 10% margin error s ",round(nsample))
## Sample size for 95% CI and 10% margin error s \, 138 \,
t.test(osteoporosis$bua,mu=72.5
      )
##
## One Sample t-test
##
## data: osteoporosis$bua
## t = 1.4994, df = 999, p-value = 0.1341
## alternative hypothesis: true mean is not equal to 72.5
## 95 percent confidence interval:
## 72.2539 74.3401
## sample estimates:
## mean of x
      73.297
##
```