

Descriptive Statistics: Summaries and Graphs

Curs d'Estadística Bàsica per a la Recerca Biomèdica

UEB - VHIR

Santiago Pérez-Hoyos and Jordi Cortés

santi.perezhoyos@vhir.org





















- Make an approach to key concepts of **Statistics** and in particular to **Biostatistics**.
- Explain the different types of **analysis**, **variables** and other relevant **concepts**.
- Learn how to make a **statistical summary** of some descriptive data.
- ➤ Learn how to implement a descriptive statistics analysis with R and R-Commander.





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- 1. INTRODUCTION. ANALYSIS STRATEGY
- 2. VARIABLES CLASSIFICATION
- 3. SUMMARY MEASURES
 - 1. Measures of location/central tendency
 - 2. Measures of variability/dispersion
- 4. SUMMARY OF VARIABLES
 - 1. Contingency Tables
 - 2. Graphs
- 5. Examples & exercises





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GENERAL CONCEPTS



- Population: It represents the largest group of individuals who want to study and generally usually inaccessible.
- Sample: Subset of the population in which measurements are done. This sample should be representative of the original population (any individual has equal opportunity to be selected).
- Variable: Feature measurable and observable that represents a concept of study
- **Measure:** Procedure for assign quantitative or qualitative values to the characteristics of objects, people or events. If these procedures are not well measured the validity of the results is not guaranteed.





STEPS IN A STATISTICAL STUDY ANALSYIS

1. Make hypothesis about a population

2. Decide which data collect (Experimental design)

- Which individuals will be part of the study (samples)
- Which data must be collected for each individual (variables)

3. Collect Data

4. Describe (summarize) collected data

- Summary measures and graphs
- Point estimations and confidence intervals

5. Establish relations between two variables

- Set up Statistical Hypothesis test
- Check application conditions
- Calculate intensity relationship measures

6. Multivariable analysis. Modelling

- Consider effects of several variables on an outcome
- Regression models
- More complex models





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QUALITATIVE NOMINAL

Event of interest

Conceptual definition

Operational Definition

Measure qualities of an individual

Examples: Sex, Treatment, Disease

ORDINAL

Measure qualities but they are ordered

Examples: Educational level, Stage, Severity

QUANTITATIVE

DISCRETE

Take only a finite possible values

Examples: No of admissions, No of programmed visits

CONTINOUS

Can take an infinite number of values. Between two measures always can be another

Example: Stay time, Age, Cholesterol level





Variable classification in a Study

Response, dependent or outcome variable

- One that answer the research question

• Explain, independent or exposure variables

 They are those that are related to the causes of the events we want to study

Confounding or effect modifier variables

 Are those that can affect the relation between exposure and outcome variables

Universal variables

 Are those that can be exposures or confounders that always have to be considered. For example: sex, age, residence location, ethnic, etc.





Descriptive analysis

- Data have to be organized to be useful (frequency or contingency tables)
- Graph data before calculating summary measures
- This actions can help to:
 - Select the **best summary** measure
 - Transform variables
 - Detect outliers





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Quantitative Variables

- We have a new variable (i.e. a biomarker and we want to summarize information)
 - Around which values is the variable?
 - Values vary greatly between different individuals
 - Data are grouped or not





Summary Measures

Location

- Mean
- Median
- Mode

Dispersion

- Range (Maximum-Minimum)
- Variance
- Standard Deviation
- Variation Coefficient
- Percentile
- Interquartile range (IQR) or Interquartile interval

Shape

- Asymmetry
- Kurtosis





Location measures



Mean

Median

Mode

Mean



 μ

- Useful to locate data.
- •Is the **sum** of observed values **over sample size**
- Can be altered by extreme values

$$\bar{x} = \frac{1}{n} \sum_{i=1}^{n} x_i$$

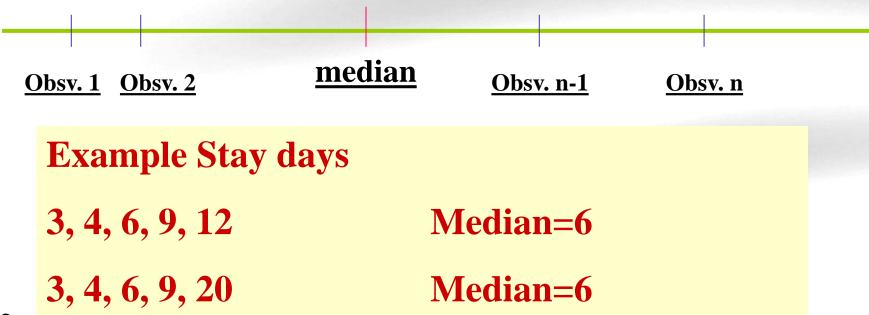
Example Stay days



Mediana



- Is the point that divied in two parts the observations
- Observations are ordered from lowest to highest and median is the central point
- It is not altered by extreme observations





Exemple en R-Commander EID



Exemple de Clase

Your Name

```
> x1 < -c(3,4,6,9,12)
```

$$> x2 < -c(3,4,6,9,20)$$

> mean(x1)

[1] 6.8

> mean(x2)

[1] 8.4

> median(x1)

[1] 6

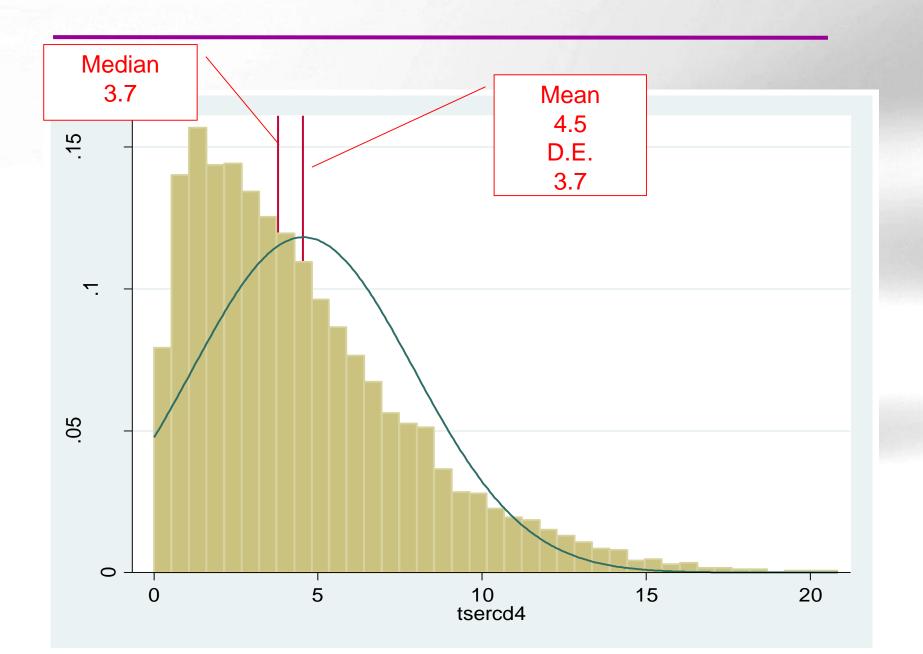
> median(x2)

[1] 6



Mean or Median

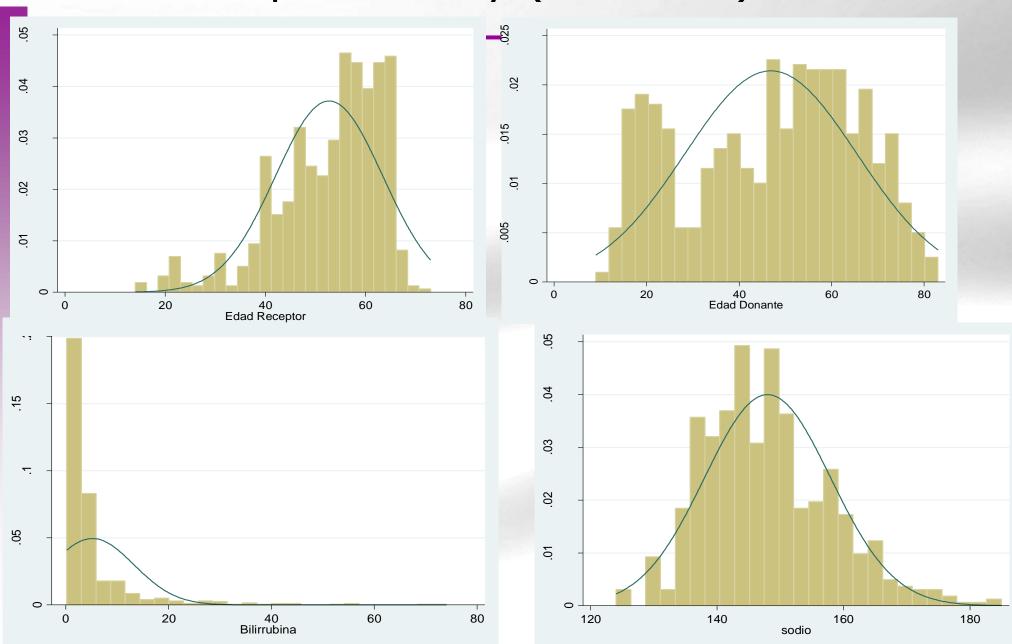






Transplant study (real data)







Geometric mean



- Sometimes data are transformed. For example logarithmic scale
- Mean is recalculated in transformed scale and exponentiated to come back to natural scale
- The calculated value is the geometric mean

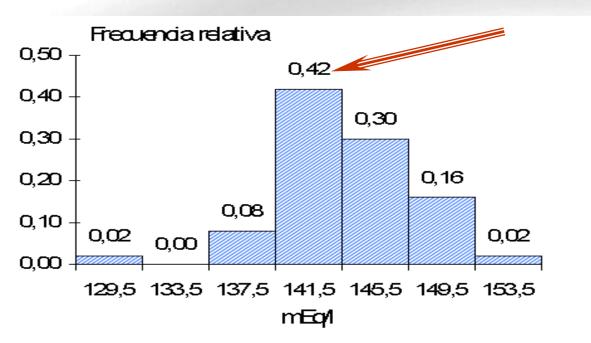
	Days	Ln(Days)	Days	Ln(Days)
	3	1,10	3	1,10
	4	1,39	4	1,39
	6	1,79	6	1,79
	9	2,20	9	2,20
	12	2,48	20	3,00
Mean	6,8	1,79	8,4	1,89
Geometric Mean		6,00		6,65



Mode



- The most frequent value
- May be not unique
- In a quantitative variable is the maximum values of an histogram

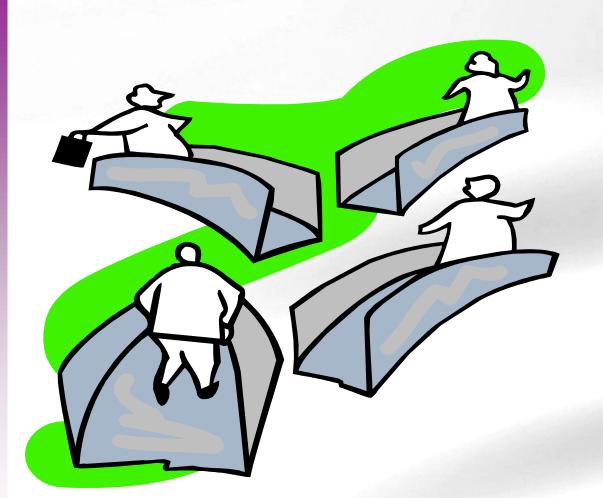


Determinaciones de socio





Dispersion or variability measures



Range (Maximum-Minimum)

Variance

Standard Deviation

Variation Coefficient

Percentile

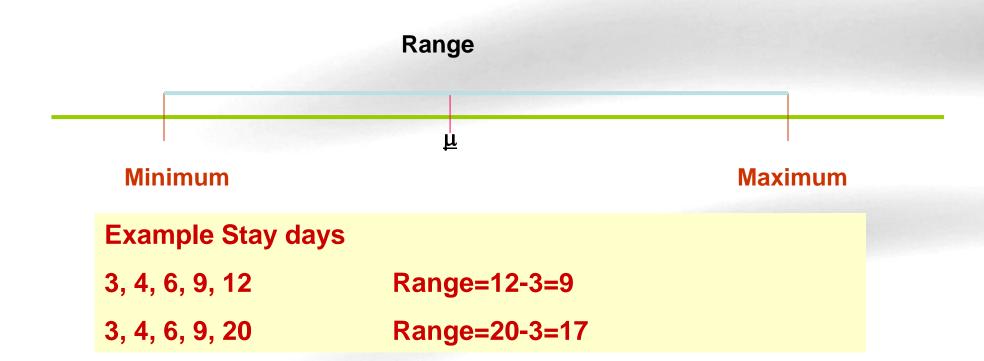
Interquartile Range (IQR)



Range



- Simplest measure of dispersion
- Is the difference between maximum and minimum value of the observations

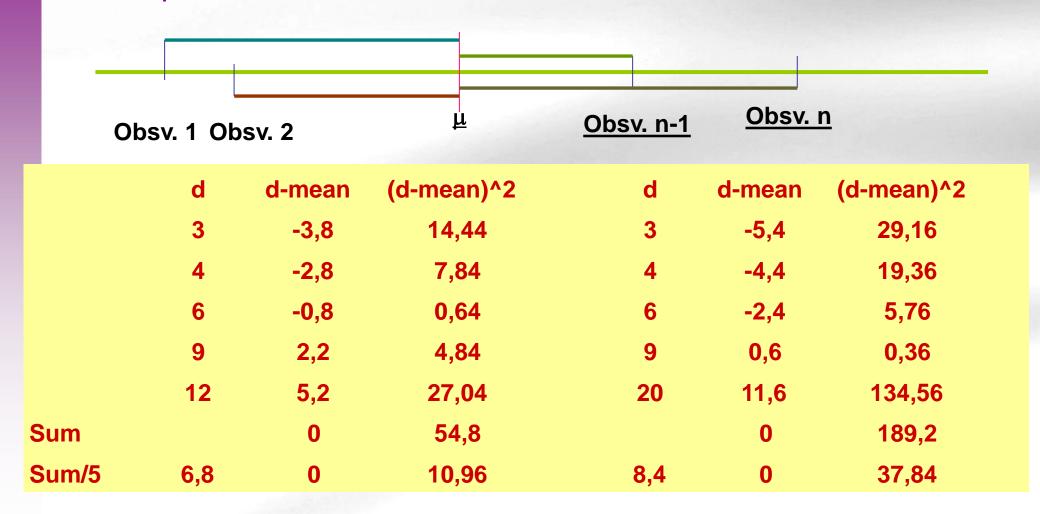




Variance



 Mean difference of observations from mean in squared scale





Standard Deviation



- Squared root of the variance
- It is measured in the same units than the variable

Example Stay days

3, 4, 6, 9, 12 Variance =10.96

Std. Dev.=3.31

3, 4, 6, 9, 20 Variance= 37.84

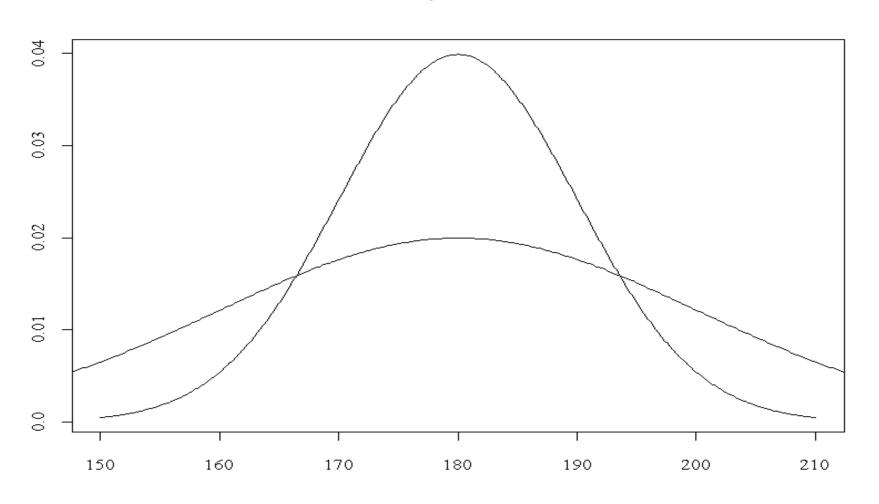
Std. Dev.= 6.15





Same mean, different variances

Mismas medias, diferentes varianzas

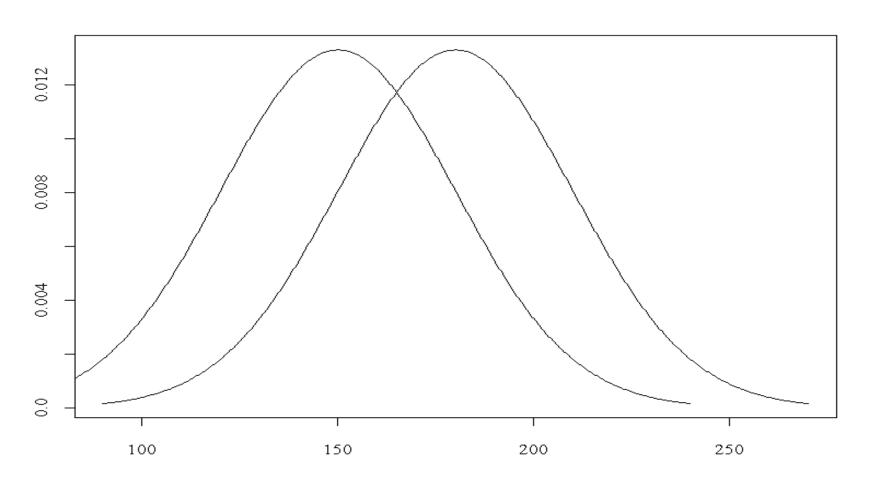






Same variances, different means

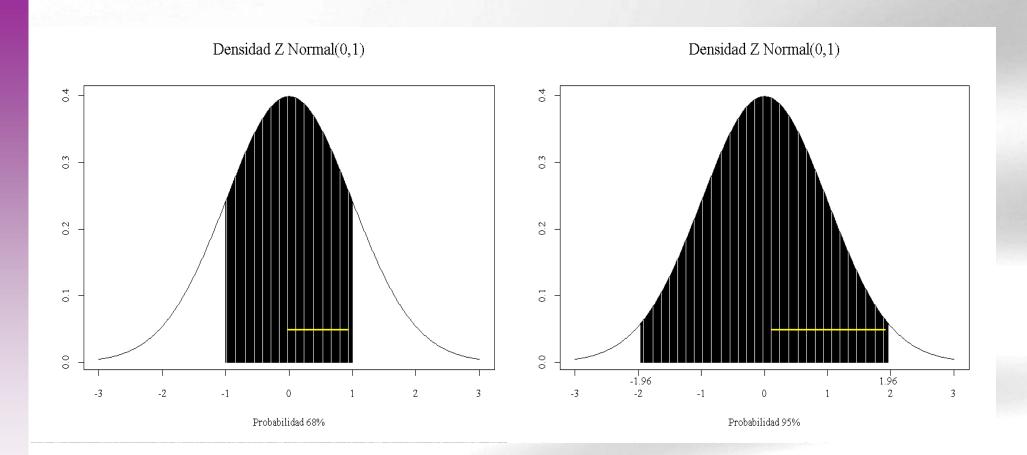
Mismas varianzas, diferentes medias







Normal distribution



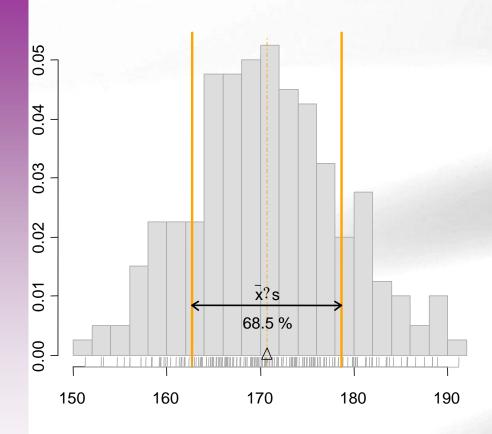
✓ Between µ (mean) ± 1 SD, there are about 68% of the probability.

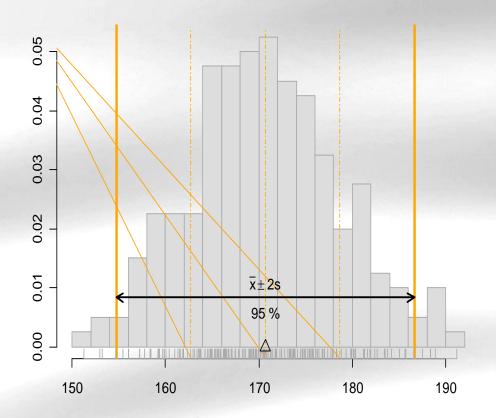
✓ Between µ (mean) ± 2 SD is about 95% of probability.





Symmetric distribution of data





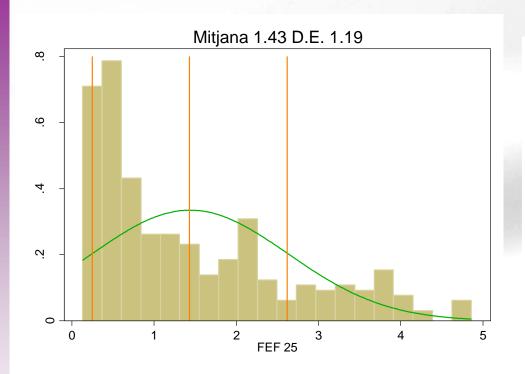
✓ Between \bar{x} (mean) ± 1 SD, there are about 68% of the observations.

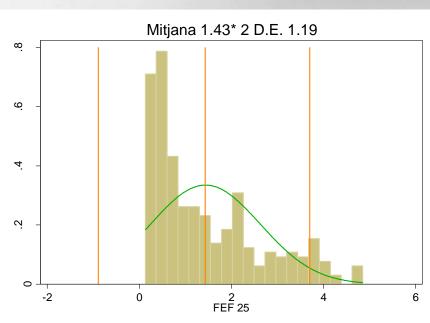
✓ Between \bar{x} (mean) ± 2 SD is about 95% of observations





Asymmetric distribution of data





- ✓ Between \bar{x} (mean) ± 1 SD, there percentage of observations is not 68%
- ✓ Between \bar{x} (mean) ± 2 SD, there percentage of observations is not 95%





Coefficient of Variation (CV)

- It is the ratio between standard deviation and mean
- Allows to compare the variability of variables measured in different scales

Example Stay Days

3, 4, 6, 9, 12 Std. Dev.= 3.31

Mean = 6.8

Variation Coef.= 0.49

3, 4, 6, 9, 20 Std. Dev. = 6.15

Mean = 8.4

Variation Coef.= 0.73



Example Variation Coefficient



Weight (Kg) of 5 patients
$$\rightarrow$$
 (70,60,56,83,79) $\begin{cases} \bar{x} = Kg \\ s = Kg \end{cases}$

Blood Pression (mmHg) \rightarrow 5 patients (150,170,135,180,19) $\begin{cases} \bar{x} = mmHg \\ s = mmHg \end{cases}$

Which variable have more variation? Weight or Pression





Data set:







View data set

R Script R Markdown

```
x1 < -c(70,60,56,83,79)
x2 < -c(150, 170, 135, 180, 195)
dades<-data.frame(x1,x2)
mean(x1)
sd(x1)
mean(x2)
sd (x2)
(sd(x1)/mean(x1))*100
(sd(x2)/mean(x2)*100
```



Example Variation Coefficient



Weight (Kg) of 5 patients
$$\Rightarrow$$
 (70,60,56,83,79) $= x = 69.6 \text{ Kg}$
 $= x = 69.6 \text{ Kg}$
 $= x = 11.67$
Blood Pression (mmHg) 5 patients $= x = 11.67$
 $= x = 166 \text{ mmHg}$
 $= x = 166 \text{ mmHg}$

Which variable have more variation? Weight or Pression



Percentiles



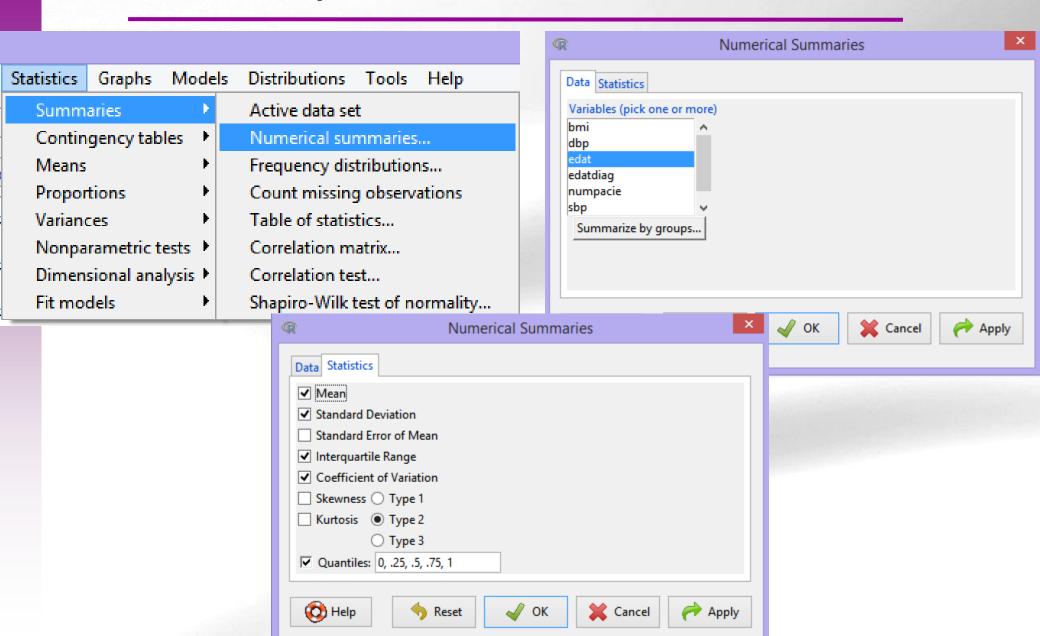
- Observations are ranked from minimum to maximum and the point that leaves below p% of observations is selected
- There are some special percentiles
 - Deciles are percentiles 10, 20, 30, 40, 50, 60, 70, 80, 90
 - Quartiles are percentiles 25, 50, 75
 - Quintiles are percentiles 20,40, 60,80
 - They are not affected by extreme observations
 - Interquartile range is difference between 25 and 75 percentile



Summary meaures in R Commander

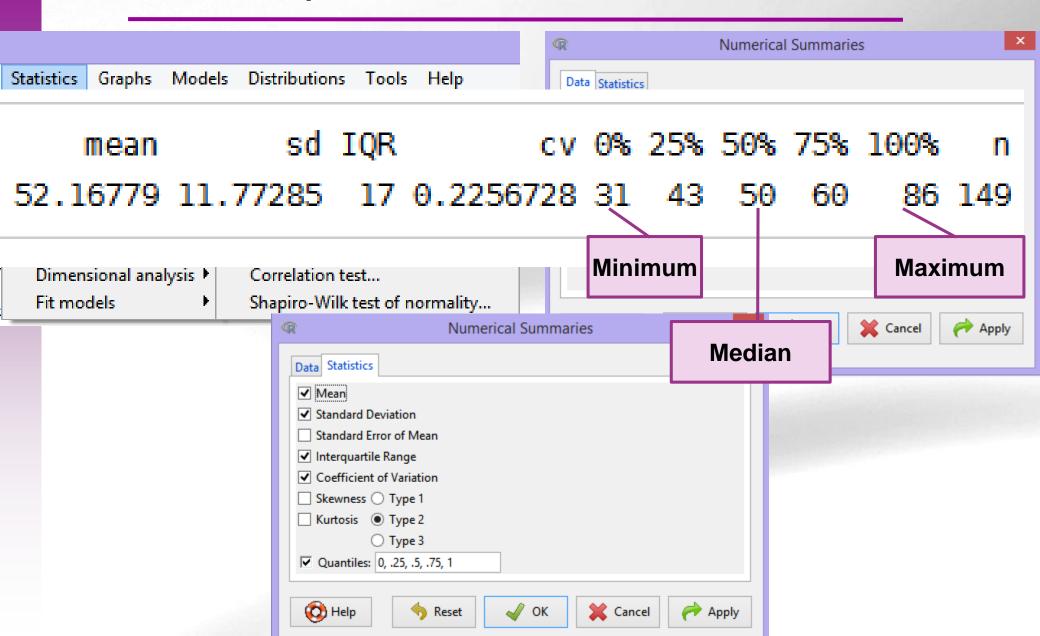
D'ESTADÍSTICA I

BIOINFORMÀTICA





Summary measures in R Commander







Syllabus

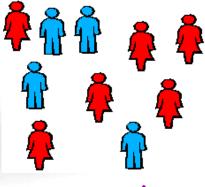
- 1. INTRODUCTION. ANALYSIS STRATEGY
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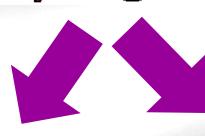


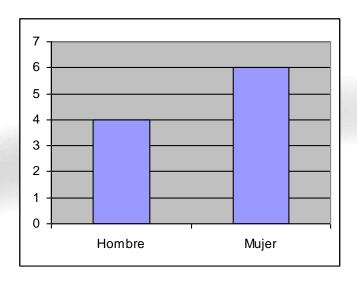
Summary of variables

Frequency tables and graphs are two equivalent ways to present information. Both expose in an ordered way the collected data.a.



Género	Frec.
Hombre	4
Mujer	6









NÚMERO DE HIJOS ENTRE MUJERES DE 20 Y 30 AÑOS

NÚMERO DE HIJOS	Frecuencia Absoluta (f _i)	Frecuencia Relativa (fr _i)	Frecuencia Acumulada (F _i)	Frecuencia Relativa Acumulada (Fr _i)
0	175	0'35	175	0'35
1	225	0'45	400	0'80
2	75	0'15	475	0'95
3 o más	25	0'05	500	1'00
TOTAL	500	1'00	500	1'00





Cate go ries

NÚMERO DE HIJOS ENTRE MUJERES DE 20 Y 30 AÑOS

NÚMERO DE HIJOS	Frecuencia Absoluta			Frecuencia Relativa
	(f _i)	(fr _i)	(F _i)	Acumulada (Fr _i)
0	175	0'35	175	0'35
1	225	0'45	400	0'80
2	75	0'15	475	0'95
3 o más	25	0'05	500	1'00
TOTAL	500	1'00	500	1'00



Cate

go ries

Taula de Frequencia



No of subjects by category

RE MUJERES DE 20 Y 30 AÑOS

NÚMERO DE HIJOS	Frecuencia Absoluta (f _i)	Frecuencia Relativa (fr _i)	Frecuencia Acumulada (F _i)	Frecuencia Relativa Acumulada (Fr _i)
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Percentage of subjects Freq /Total

No of subjects by category

RE MUJERES DE 20 Y 30 AÑOS

Cate go ries

NÚMERO DE HIJOS	Frecuencia Absoluta (f _i)	Frecuencia Relativa (fr _i)	Frecuencia Acumulada (F _i)	Frecuencia Relativa Acumulada (Fr _i)
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Percentage of subjects Freq /Total

Nº of subjects by category

RE MUJERES DE 20 Y 30 AÑOS

Cate go ries

NÚMERO DE HIJOS	Frecuencia Absoluta	Frecuencia Relativa	Frecuencia Acumulada	Frecuencia Relativa
	(f;)	(fr _i)	(F _i)	Acumulada (Fr _i)
0	175	0'35	175	0'35
1	225	0'45	4 00	0'80
2	75	0'15	475	0'95
3 o más	Nº accumi subects up to	ulated category	500	1'00
TOTAL	subects up to (Only ordi discrete vai	nal or riables)	500	1'00





Percentage of subjects Freq /Total

Nº of subjects by category

RE MUJERES DE 20 Y 30 AÑOS

go ries NÚMERO

Cate

NÚMERO DE HIJOS	Frecuencia Absoluta (f _i)	Frecuencia Relativa (fr _i)	Frecuencia Acumulada (F _i)	Frecuencia Relativa Acumulada (Fr _i)
0	175	0'35	175	0'35
1	225	0'45	400	i <mark>8</mark> 9
2	75	0'15	475	0'90

3 o más

TOTAL

Nº accumulated subects up to category (Only ordinal or discrete variables)

500

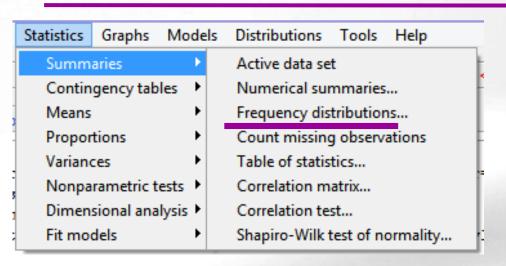
500

Accumulated Frequency up to category Freq Abs/Total





Frequency tables in R Commander

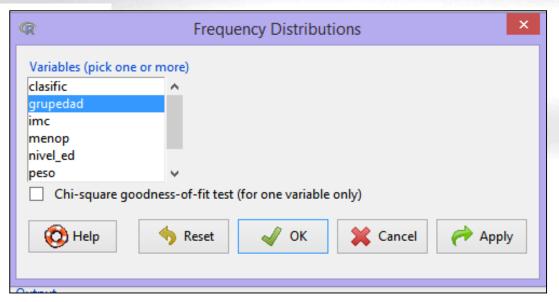


counts:

grupedad

percentages:

grupedad







Frequency tables for quantitative variables

PESO

Marca de Clase	Intervalo de Clase	Frecuencia Absoluta	Frecuencia Relativa	Frecuencia Acumulada	Frecuencia Relativa Acumulada
42'5	x<45	1	0'002	1	0'002
47'5	45<=x<50	3	0'006	4	0'008
52'5	50<=x<55	12	0'024	16	0'032
57'5	55<=x<60	75	0'150	91	0'182
62'5	60<=x<65	103	0'206	194	0'388
67'5	65<=x<70	155	0'310	349	0'698
72'5	70<=x<75	101	0'202	450	0'900
77'5	75<=x<80	29	0'058	479	0'958
82'5	80<=x<85	11	0'022	490	0'980
87'5	85<=x<90	8	0'016	498	0'996
92'5	90<=x<95	2	0'004	500	1'000
		500	1'000	500	1'000

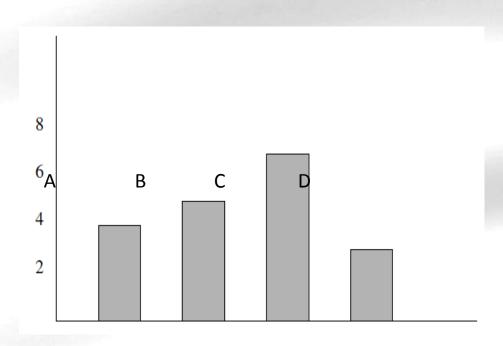




Bar Graph

Categorys are representened in X axis and frequencies in Y axis

freqüències

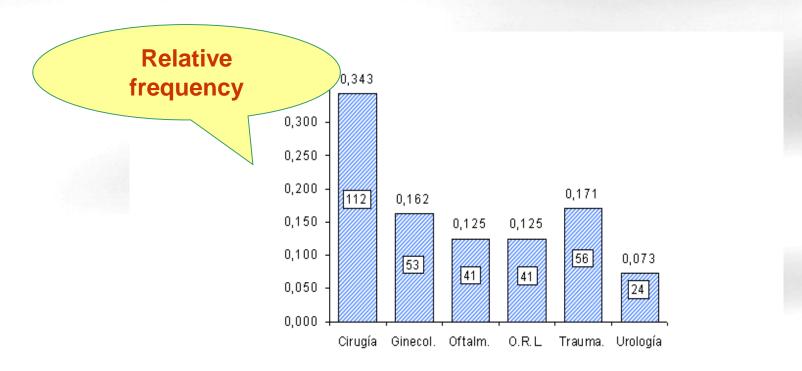






Bar Graph

For comparing two population better use relative frequencies



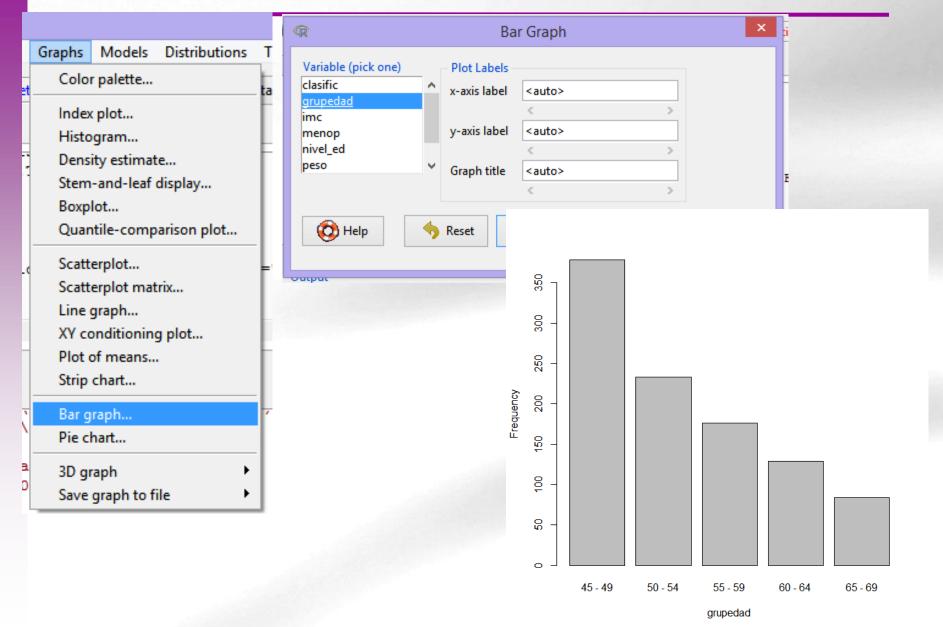
Intervenciones quirúrgicas

Categories





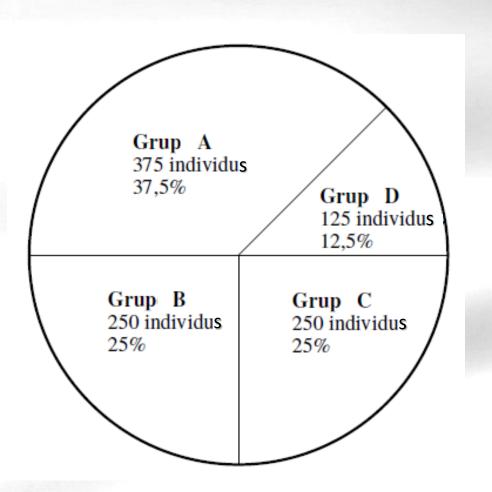
Graphs in R Commander







Pie Graph



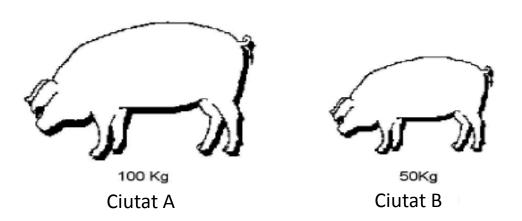


Pictograms



Expressed with drawings alluding to the subject of study frequencies of the modalities of the variable. The scaling of each design should be such that the area of each of them should be proportional to the frequency category representing. Used by the media because they can be quickly understood by a general audience..

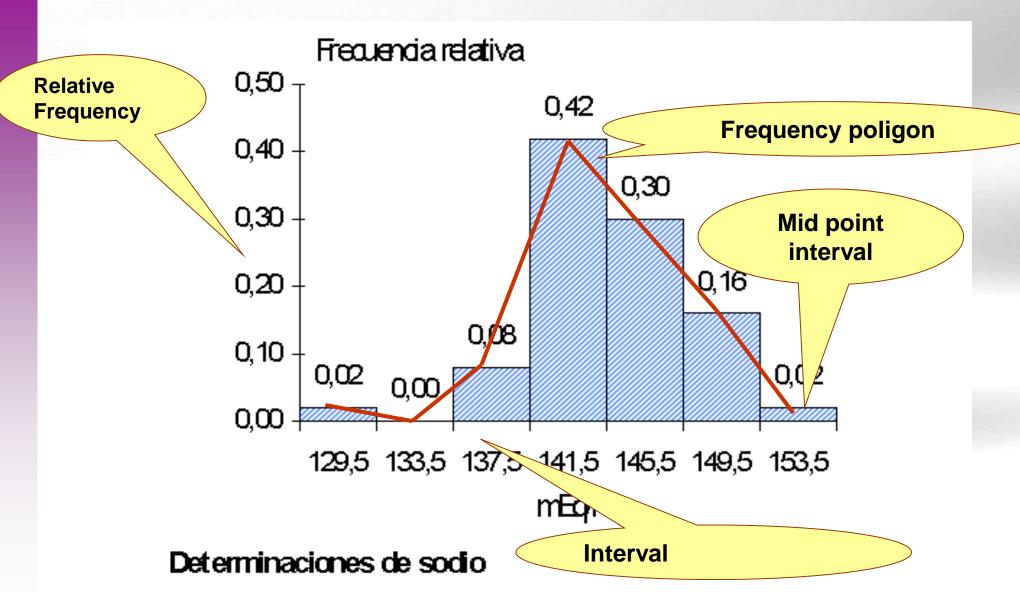
Ampolles de cervesa recollides





Histogram







Steam and Leaf graph EID UNITAT D'ESTADÍSTICA I BIOINFORMÀTICA



128	106	125	108	98	58	118	92	108	132	32	140	138	96	161
133	104	122	124	110	120	86	115	118	95	83	112	128	127	124
133	115	127	135	89	123	134	94	67	124	155	105	100	112	141
121	112	135	115	64	104	132	98	146	132	93	85	94	116	113
104	115	138	105	144	121	68	107	122	126	88	89	108	115	85
87	88	103	108	109	111	121	124	104	125	102	122	137	110	101
					91	122	138	99	115	104	98	89	119	109

```
784
   6358959789
   8 2654834198
   6 8 504784214945389 84
   85822635105950525
8 5 0 743412614 22852471
   284227883355
   0164
15
```





Steam and Leaf graph

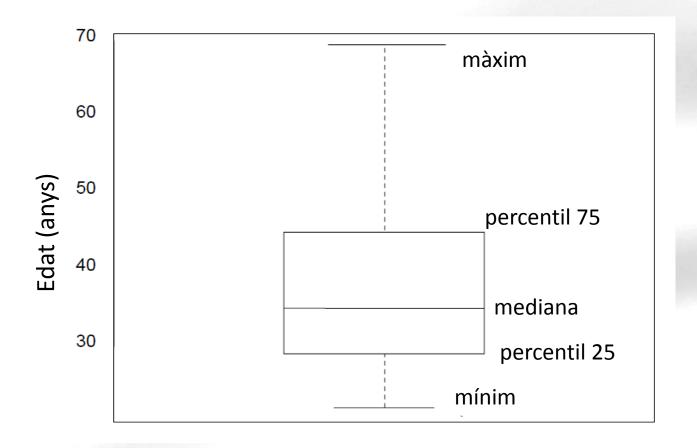
128	106	125	108	98	58	118	92	108	132	32	140	138	96	161
133	104	122	124	110	120	86	115	118	95	83	112	128	127	124
133	115	127	135	89	123	134	94	67	124	155	105	100	112	141
121	112	135	115	64	104	132	98	146	132	93	85	94	116	113
104	115	138	105	144	121	68	107	122	126	88	89	108	115	85
87	88	103	108	109	111	121	124	104	125	102	122	137	110	101
					91	122	138	99	115	104	98	89	119	109



Boxplot



It is graphically represented the "five numbers": box are 25th and 75th percentiles, the middle line is the median (50th percentile) and the ends are the minimum and maximum values.

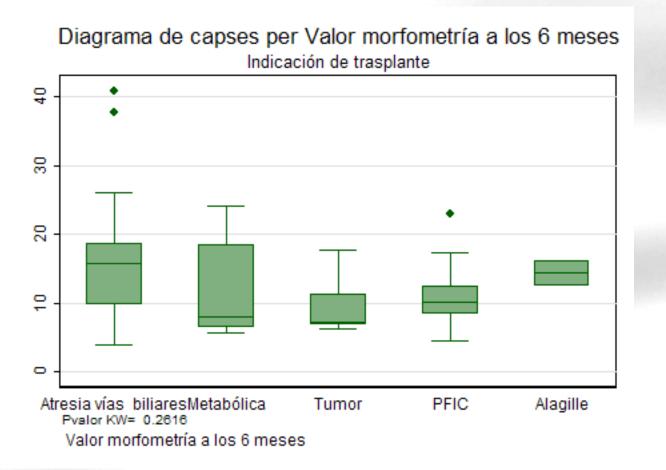








The boxplot is a quick way to identify outliers in the sample (they can not be "outliers")







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