

# Curs bàsic d'Anàlisi de dades amb Stata

# Sessió 3

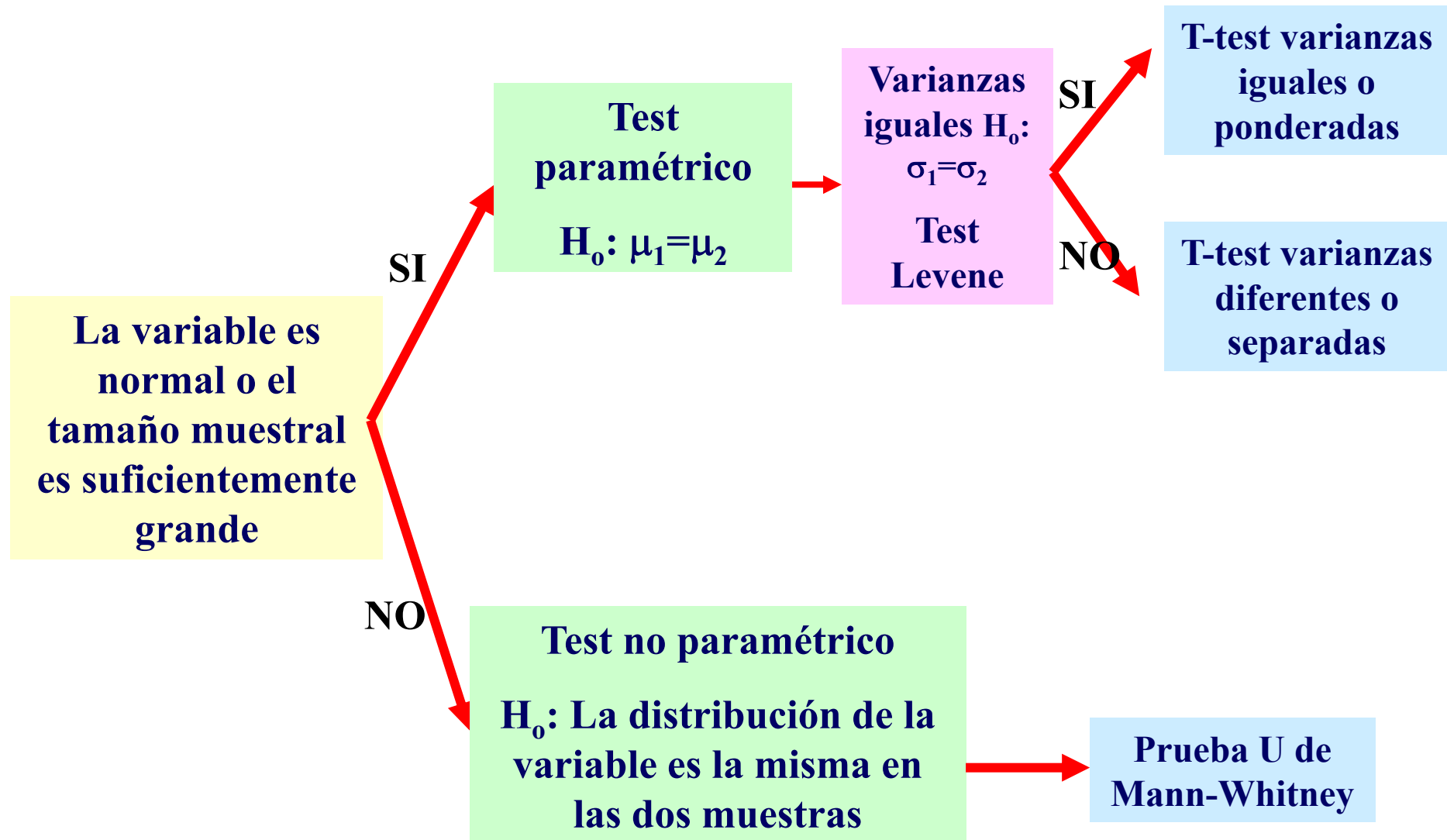
- Estimació i contrast d'hipòtesi
  - Test per una mostra t-test
  - Test per 2 mostres. T-test- Mann-Whitney
  - Test per 3 o mes mostres: Anova, Kruskal Wallis
  - Probes de Normalitat
  - Test per variables qualitatives: Ji-cuadrat
- Correlació i Regressió
  - Gràfics de dispersió
  - Introducció a la Correlació
  - Introducció a la regressió lineal simple
  - Exercici Pràctic

## Base dades MUNS mortalitat en UCI

- Quants morts hi ha, quin percentatge
- Quina es la mitjana d'edat dels vius i dels morts
- Quina es la mediana de la gravetat TISS i SAPS en els morts
- Es el % de universitaris en la mostra mes gran en els morts que en els vius

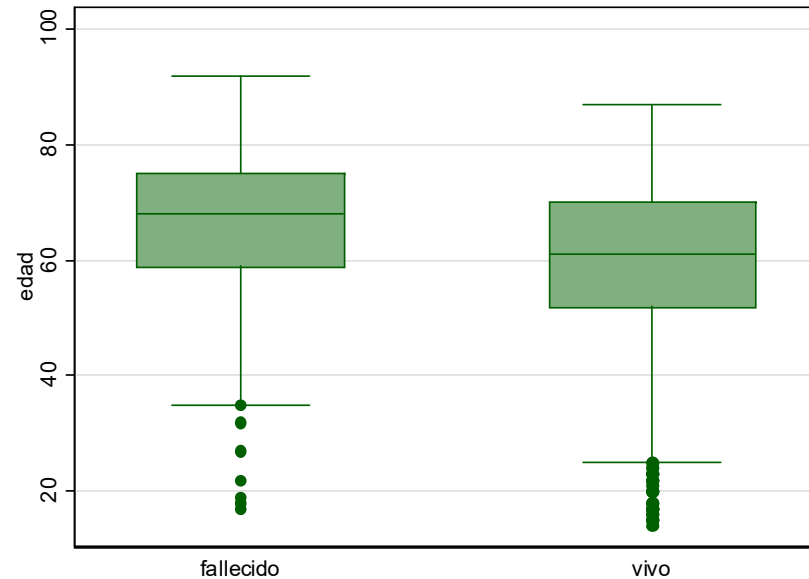
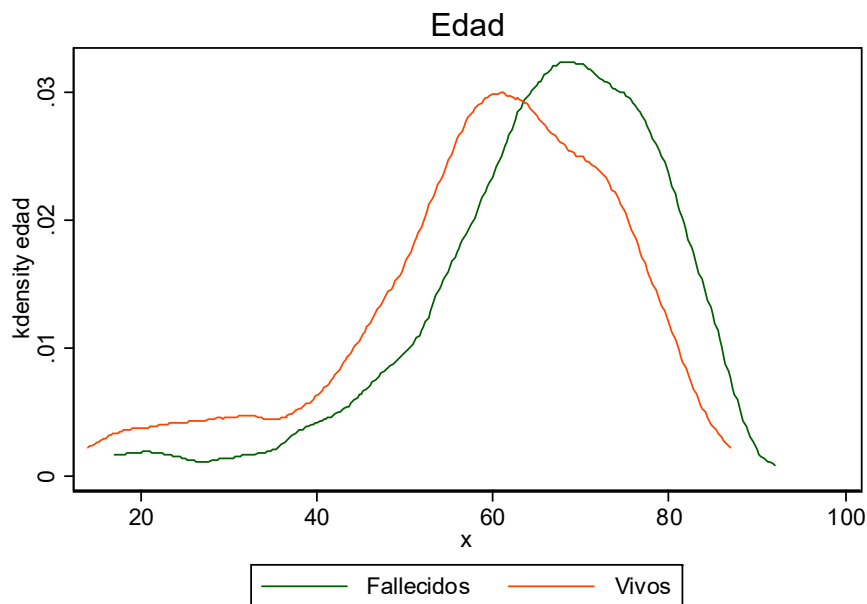
# Relación entre variable cuantitativa según los niveles de una variable cualitativa

## 2 Muestras independientes



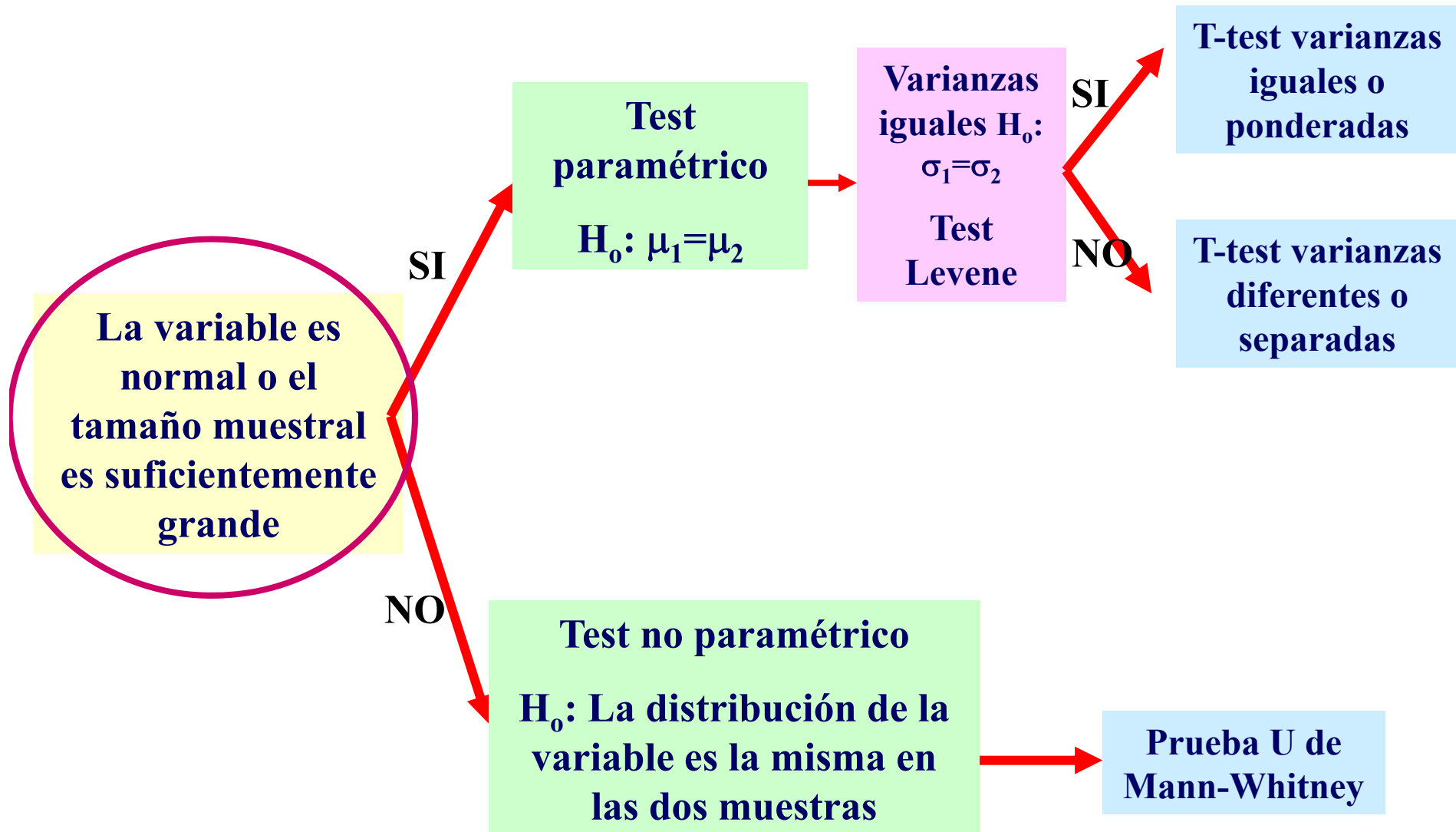
# Ejemplo: Comparación de edad en mortalidad a las dos semanas de salir en UCI

```
graph box edad, over(mortdos1)
```



```
twoway kdensity edad if mortdos1==1 ///  
    || kdensity edad if mortdos1==2 ///  
    ||, legend( label( 1 Fallecidos ) ///  
        label(2 Vivos) ) title(Edad)
```

## 2 Muestras independientes



# Comparación de normalidad

- Test de normalidad (Saphiro-Wilk, Shaphiro-Francia, Skeness/Kurtosis)

**swilk var**

**sfrancia var**

**sktest var**

```
. swilk edad
```

Shapiro-Wilk W test for normal data

| Variable | Obs | W       | V      | z     | Prob>z  |
|----------|-----|---------|--------|-------|---------|
| edad     | 844 | 0.94565 | 29.377 | 8.312 | 0.00000 |

```
. sfrancia edad
```

Shapiro-Francia W' test for normal data

| Variable | Obs | W'      | V'     | z     | Prob>z  |
|----------|-----|---------|--------|-------|---------|
| edad     | 844 | 0.94628 | 30.985 | 7.080 | 0.00001 |

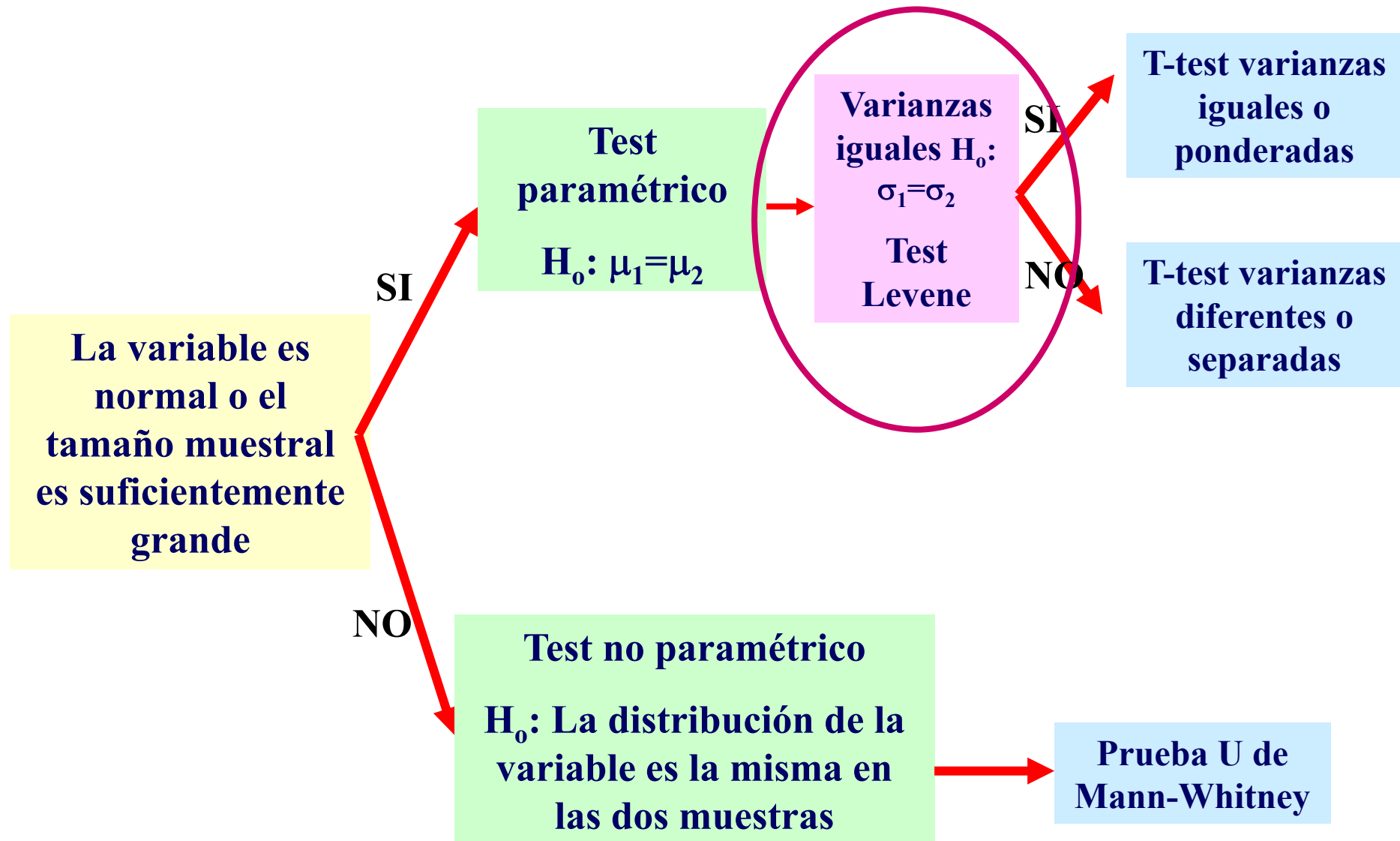
```
. sktest edad
```

Skewness/Kurtosis tests for Normality

| Variable | Obs | Pr(Skewness) | Pr(Kurtosis) | adj chi2(2) | joint Prob>chi2 |
|----------|-----|--------------|--------------|-------------|-----------------|
| edad     | 844 | 0.0000       | 0.0020       | .           | 0.0000          |



## 2 Muestras independientes



# Comparación de varianzas

- Test de Barlett

**sdtest** *var1*,by(*vargrupo*)

```
. sdtest edad,by(mortdos1)
```

Variance ratio test

| Group    | Obs | Mean     | Std. Err. | Std. Dev. | [95% Conf. Interval] |          |
|----------|-----|----------|-----------|-----------|----------------------|----------|
| fallecid | 189 | 65.66138 | .9846041  | 13.53607  | 63.71908             | 67.60367 |
| vivo     | 554 | 58.87365 | .6462106  | 15.20999  | 57.60432             | 60.14297 |
| combined | 743 | 60.60027 | .5534556  | 15.08611  | 59.51374             | 61.68679 |

ratio = sd(fallecid) / sd(vivo) f = 0.7920  
Ho: ratio = 1 degrees of freedom = 188, 553

Ha: ratio < 1  
Pr(F < f) = 0.0291

Ha: ratio != 1  
**2\*Pr(F < f) = 0.0583**

Ha: ratio > 1  
Pr(F > f) = 0.9709

# Comparación de varianzas

- Test de Levene y variaciones (+ 2 grupos)

**robvar** *var1*, **by**(*vargrupo*)

```
. robvar edad,by(mortdos1)
```

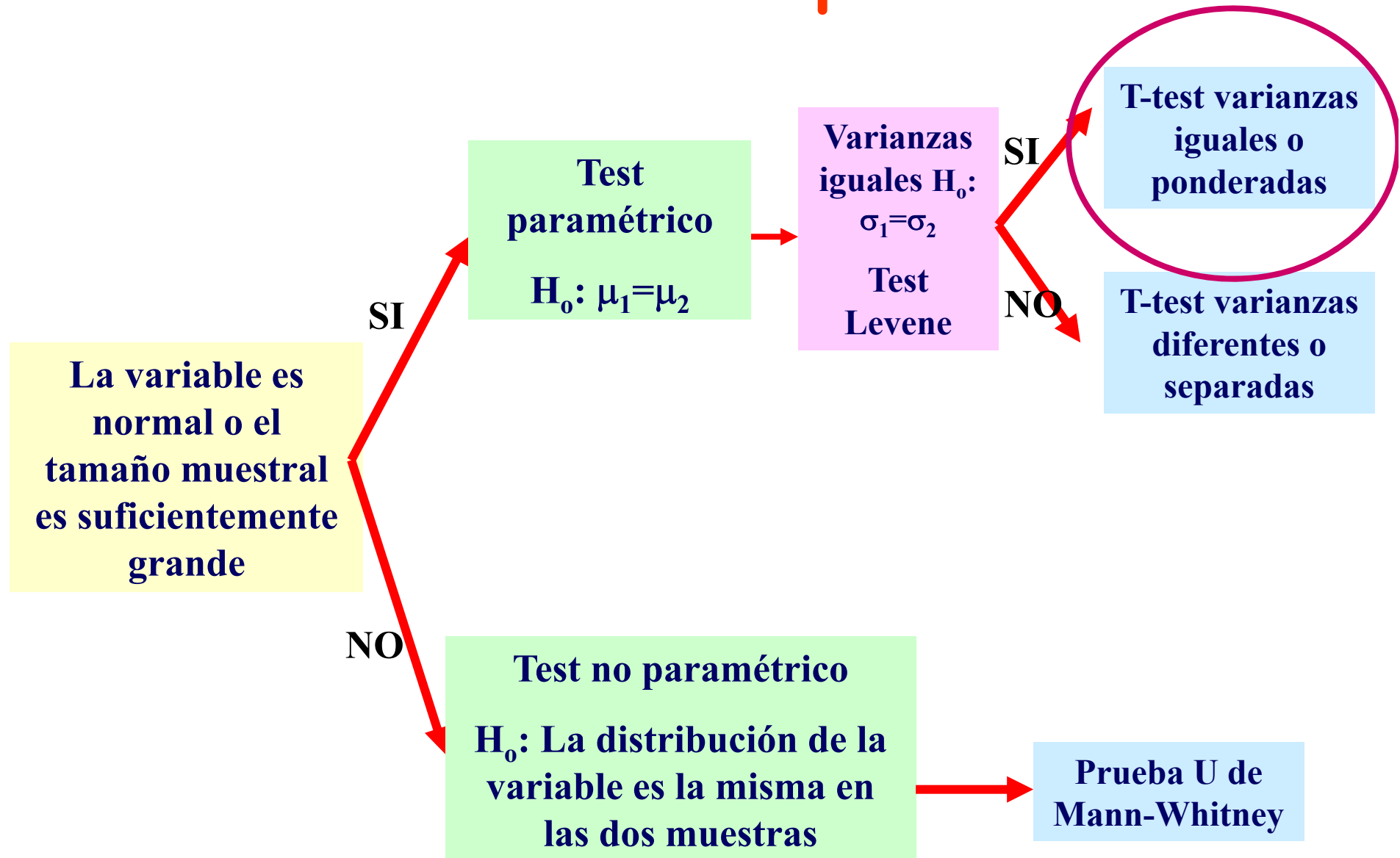
|             |                 |           |       |
|-------------|-----------------|-----------|-------|
| mortalidad  |                 |           |       |
| tras dos    | Summary of edad |           |       |
| meses       | Mean            | Std. Dev. | Freq. |
| -----+----- |                 |           |       |
| fallecido   | 65.661376       | 13.536068 | 189   |
| vivo        | 58.873646       | 15.209992 | 554   |
| -----+----- |                 |           |       |
| Total       | 60.600269       | 15.086109 | 743   |

**W0** = 1.6295302 df(2, 841) Pr > F = **.19663994**

W50 = 1.5424108 df(2, 841) Pr > F = .21446926

W10 = 1.5807144 df(2, 841) Pr > F = .20643891

## 2 Muestras independientes



# Comparación de medias

- T-test para varianzas iguales

```
ttest var1, by (vargrupo)
```

```
ttest edad,by (mortdos1)
```

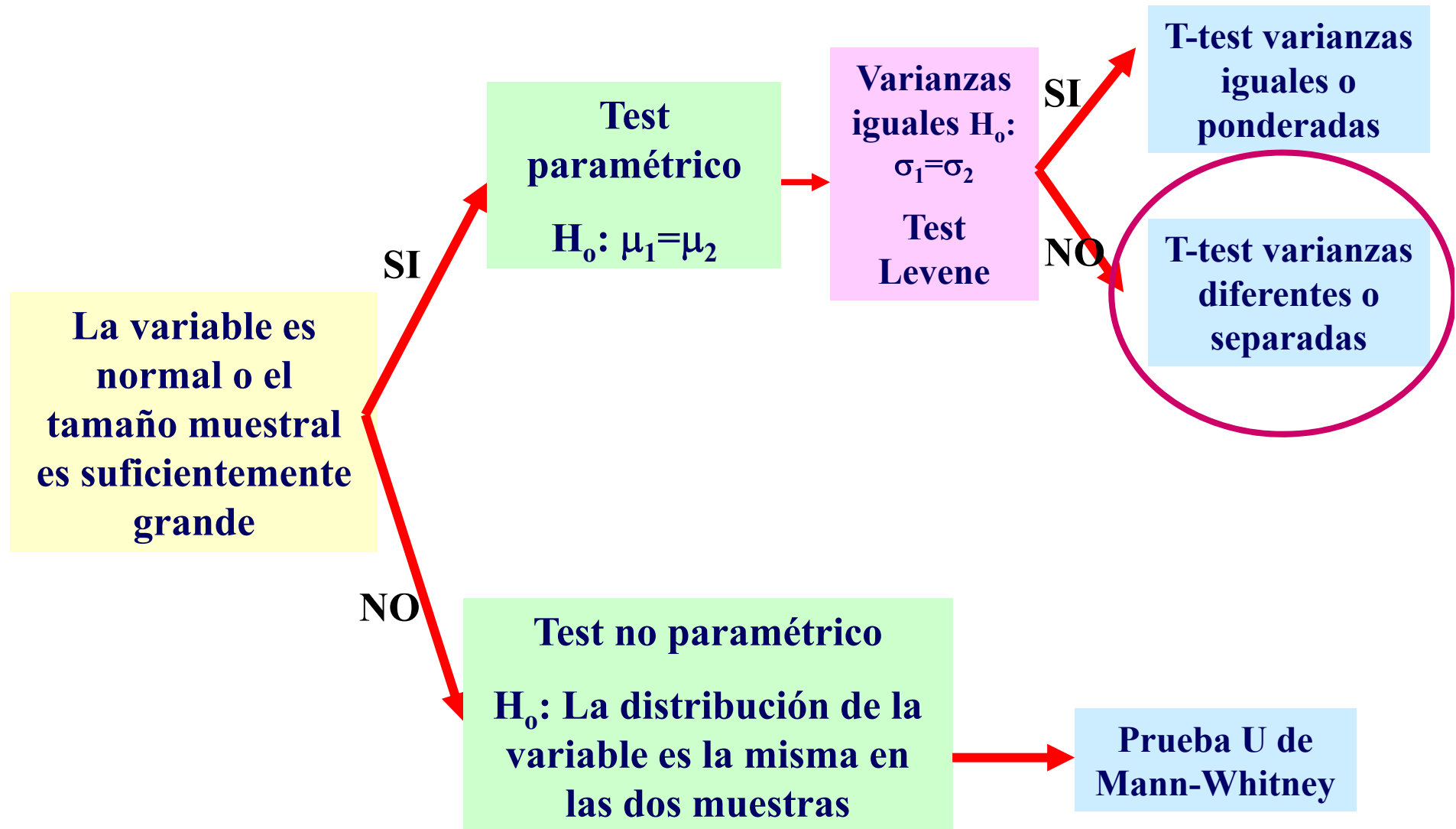
## Two-sample t test with equal variances

| Group    | Obs | Mean     | Std. Err. | Std. Dev. | [95% Conf. Interval] |          |
|----------|-----|----------|-----------|-----------|----------------------|----------|
| fallecid | 189 | 65.66138 | .9846041  | 13.53607  | 63.71908             | 67.60367 |
| vivo     | 554 | 58.87365 | .6462106  | 15.20999  | 57.60432             | 60.14297 |
| combined | 743 | 60.60027 | .5534556  | 15.08611  | 59.51374             | 61.68679 |
| diff     |     | 6.787729 | 1.246996  |           | 4.339663             | 9.235796 |

[illegible]

| Ha: diff < 0       | Ha: diff != 0          | Ha: diff > 0       |
|--------------------|------------------------|--------------------|
| Pr(T < t) = 1.0000 | Pr( T  >  t ) = 0.0000 | Pr(T > t) = 0.0000 |

## 2 Muestras independientes



# Comparación de medias

- T-test para varianzas diferentes o separadas

**ttest** *var1*,by(*vargrupo*) **unequal**

```
test edad,by(mortdos1) unequal
```

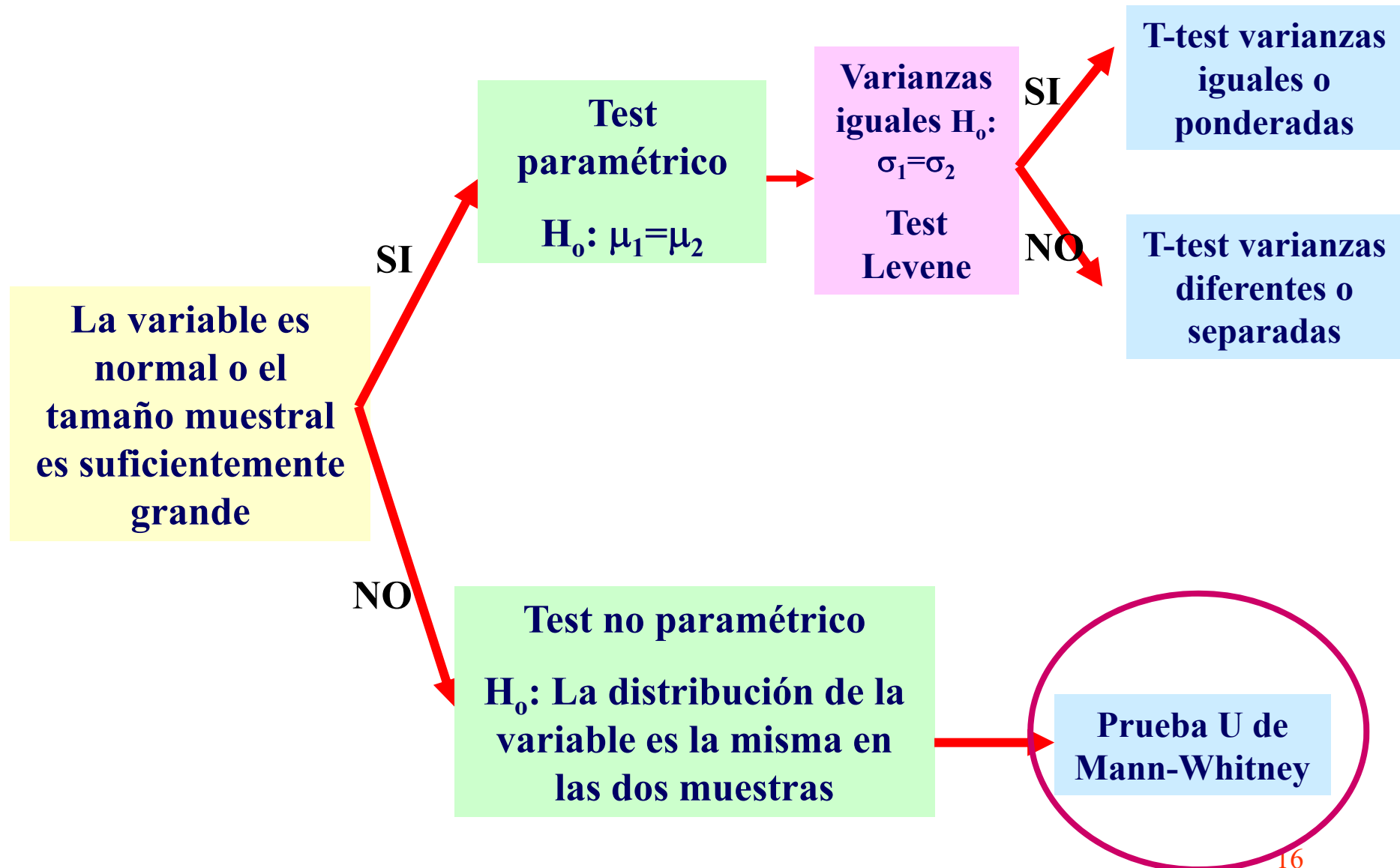
```
Two-sample t test with unequal variances
```

| Group    | Obs | Mean     | Std. Err. | Std. Dev. | [95% Conf. Interval] |          |
|----------|-----|----------|-----------|-----------|----------------------|----------|
| fallecid | 189 | 65.66138 | .9846041  | 13.53607  | 63.71908             | 67.60367 |
| vivo     | 554 | 58.87365 | .6462106  | 15.20999  | 57.60432             | 60.14297 |
| combined | 743 | 60.60027 | .5534556  | 15.08611  | 59.51374             | 61.68679 |
| diff     |     | 6.787729 | 1.177724  |           | 4.47169              | 9.103769 |

```
diff = mean(fallecid) - mean(vivo)          t = 5.7634
Ho: diff = 0          Satterthwaite's degrees of freedom = 362.009
```

|                    |                               |                    |
|--------------------|-------------------------------|--------------------|
| Ha: diff < 0       | Ha: diff != 0                 | Ha: diff > 0       |
| Pr(T < t) = 1.0000 | Pr( T  >  t ) = <b>0.0000</b> | Pr(T > t) = 0.0000 |

## 2 Muestras independientes





# Comparación no paramétrica

- Prueba Suma-rango de Wilcoxon o U de Mann-Witney

**ranksum** *var1*,by(*vargrupo*)

```
ranksum edad,by(mortdos1)
```

Two-sample Wilcoxon rank-sum (Mann-Whitney) test

| mortdos1  | obs | rank sum | expected |
|-----------|-----|----------|----------|
| fallecido | 189 | 85060    | 70308    |
| vivo      | 554 | 191336   | 206088   |
| combined  | 743 | 276396   | 276396   |

unadjusted variance 6491772.00

adjustment for ties -3990.77

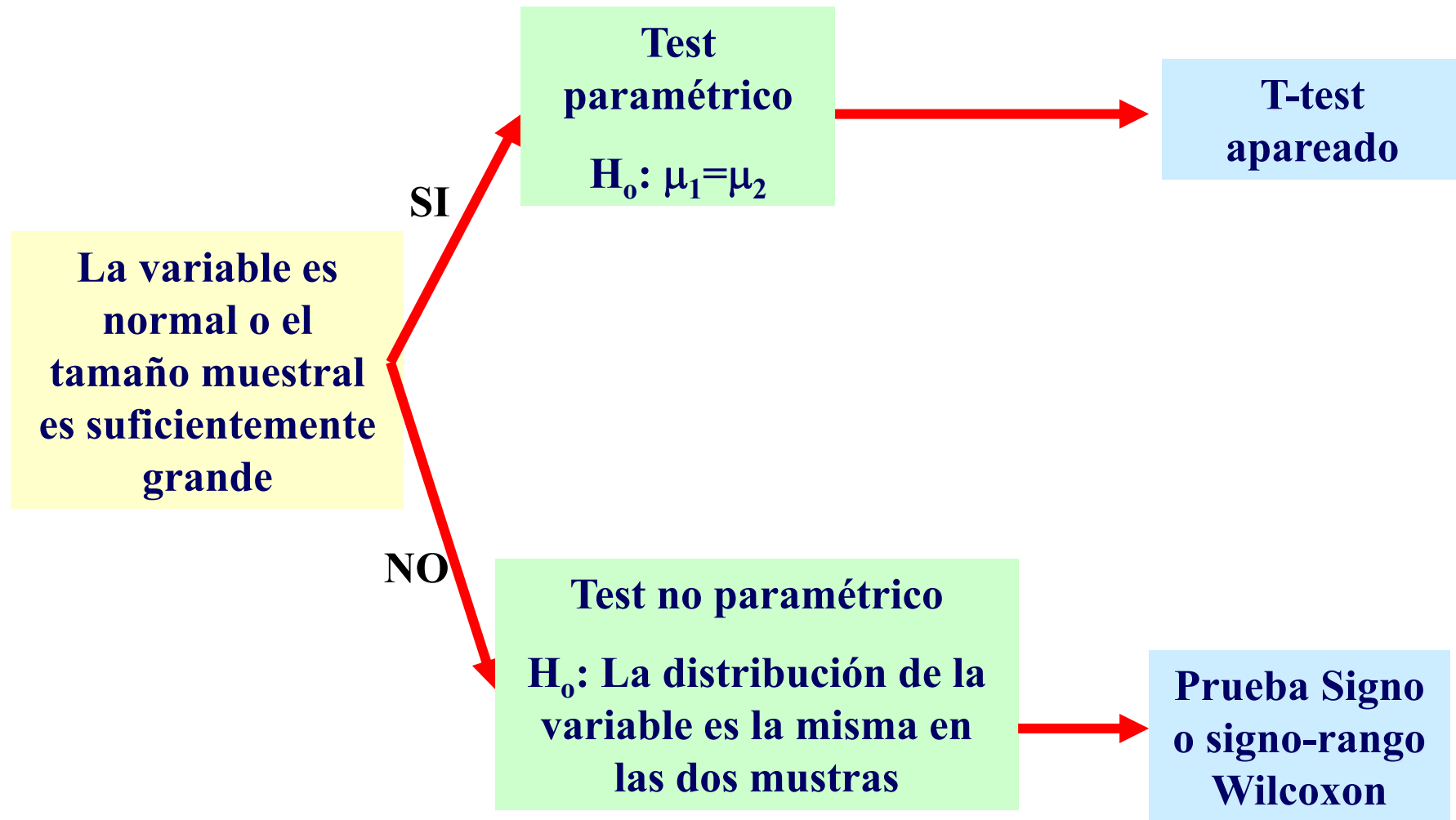
adjusted variance 6487781.23

Ho: edad(mortdos1==fallecido) = edad(mortdos1==vivo)

z = 5.792

**Prob > |z| = 0.0000**

## 2 Muestras dependientes



# Comparación de medias

- T-test apareado

**ttest** *var1=var2*

```
. ttest tiss_20= saps_10
```

Paired t test

| Variable | Obs | Mean      | Std. Err. | Std. Dev. | [95% Conf. Interval] |          |
|----------|-----|-----------|-----------|-----------|----------------------|----------|
| tiss_20  | 828 | -.1763285 | .3729507  | 10.73165  | -.9083699            | .5557129 |
| saps_10  | 828 | -.6400966 | .1660687  | 4.778624  | -.9660623            | -.314131 |
| diff     | 828 | .4637681  | .3000386  | 8.633608  | -.1251587            | 1.052695 |

```
mean(diff) = mean(tiss_20 - saps_10)          t = 1.5457
Ho: mean(diff) = 0                          degrees of freedom = 827

Ha: mean(diff) < 0          Ha: mean(diff) != 0          Ha: mean(diff) > 0
Pr(T < t) = 0.9387          Pr(|T| > |t|) = 0.1226          Pr(T > t) = 0.0613
```

.

# Comparación no paramétrica

- Prueba signo-rango de Wilcoxon

**signrank** *var1*,by(*vargrupo*)

```
signrank tiss_20= saps_10
```

Wilcoxon signed-rank test

| sign     | obs | sum ranks | expected |
|----------|-----|-----------|----------|
| positive | 310 | 155982    | 171015   |
| negative | 470 | 186048    | 171015   |
| zero     | 48  | 1176      | 1176     |
| all      | 828 | 343206    | 343206   |

unadjusted variance      47391029

adjustment for ties    -66284.125

adjustment for zeros      -9506

adjusted variance      47315238

Ho: tiss\_20 = saps\_10

z = -2.185

Prob > |z| = **0.0289**

# Comparación no paramétrica

- Prueba signo

**signtest** *var1* = *var2*

```
signtest tiss_20= saps_10
```

Sign test

| sign     | observed | expected |
|----------|----------|----------|
| positive | 310      | 390      |
| negative | 470      | 390      |
| zero     | 48       | 48       |
| all      | 828      | 828      |

One-sided tests:

Ho: median of tiss\_20 - saps\_10 = 0 vs.

Ha: median of tiss\_20 - saps\_10 > 0

Pr(#positive >= 310) =

Binomial(n = 780, x >= 310, p = 0.5) = 1.0000

Ho: median of tiss\_20 - saps\_10 = 0 vs.

Ha: median of tiss\_20 - saps\_10 < 0

Pr(#negative >= 470) =

Binomial(n = 780, x >= 470, p = 0.5) = 0.0000

Two-sided test:

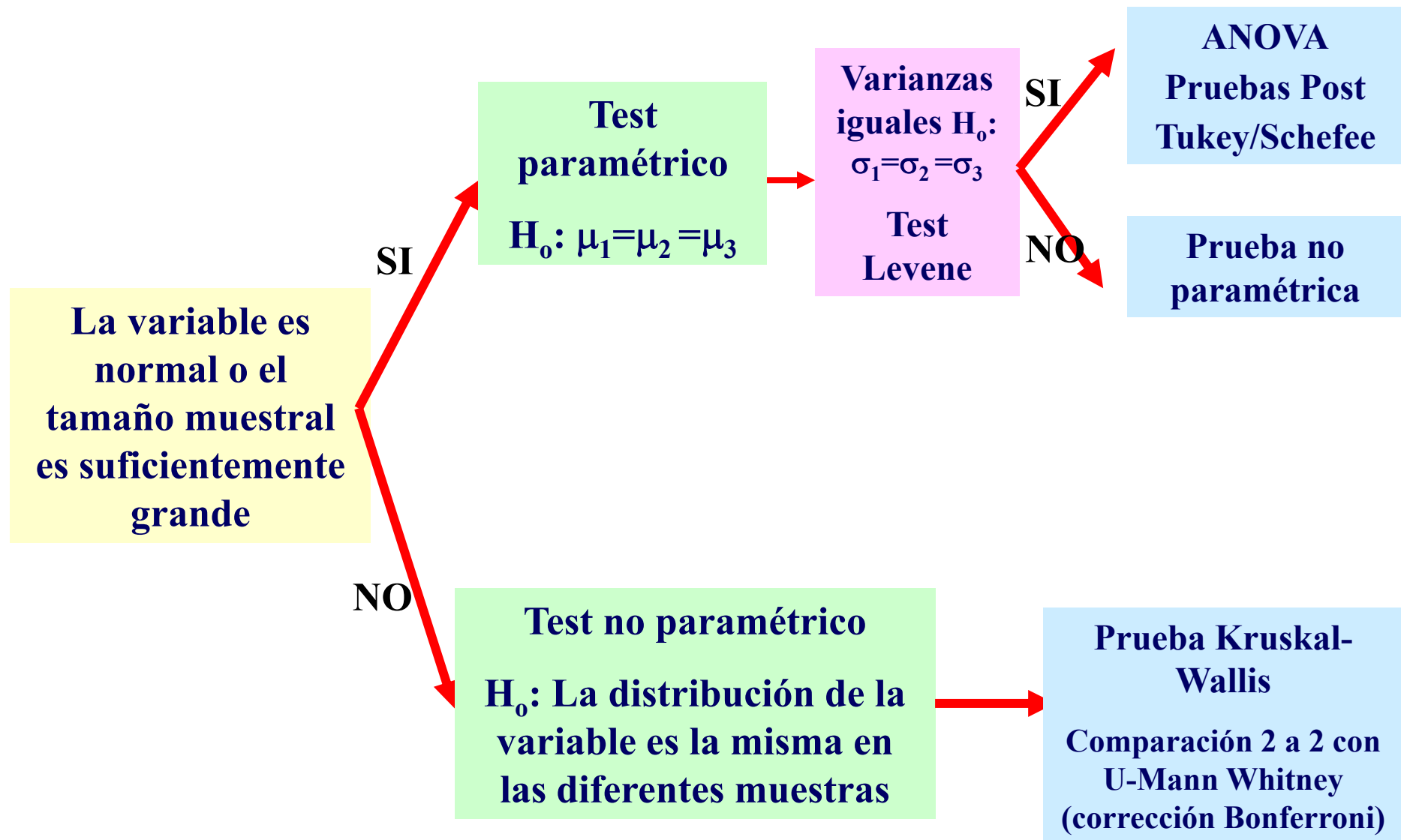
Ho: median of tiss\_20 - saps\_10 = 0 vs.

Ha: median of tiss\_20 - saps\_10 != 0

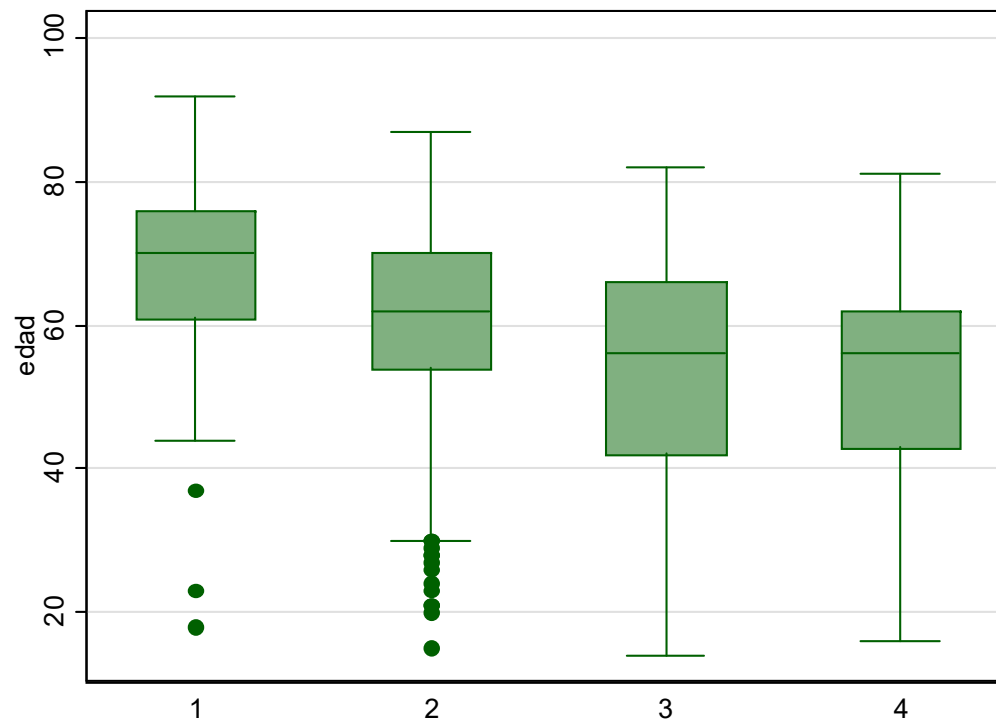
Pr(#positive >= 470 or #negative >= 470) =

min(1, 2\*Binomial(n = 780, x >= 470, p = 0.5)) = 0.0000

## >2 Muestras independientes



# Ejemplo: Comparación de la edad en función del nivel educativo de enfermos en UCI



# Comparación de medias

- ANOVA

**oneway** *var1 vargrupo* ,**tabulate means standard**  
**bonferroni scheffe**

```
. oneway edad educacio, tabulate means standard bonferroni scheffe
```

| nivel de<br>estudios | Summary of edad |           |
|----------------------|-----------------|-----------|
|                      | Mean            | Std. Dev. |
| 1                    | 68.18617        | 11.489238 |
| 2                    | 60.620098       | 12.924095 |
| 3                    | 52.067485       | 18.161528 |
| 4                    | 52.470588       | 15.314507 |
| Total                | 60.141975       | 15.069459 |

| Analysis of Variance |            |     |            |       |          |
|----------------------|------------|-----|------------|-------|----------|
| Source               | SS         | df  | MS         | F     | Prob > F |
| Between groups       | 25887.11   | 3   | 8629.03668 | 44.07 | 0.0000   |
| Within groups        | 157827.563 | 806 | 195.815835 |       |          |
| Total                | 183714.673 | 809 | 227.088594 |       |          |

Bartlett's test for equal variances: chi2(3) = 44.7951 Prob>chi2 = 0.000



# Comparación de medias

- ANOVA

**oneway** *var1 vargrupo* ,**tabulate means estándar**  
**bonferroni scheffe**

```
. oneway edad educacio, tabulate means standard bonferroni scheffe
```

Comparison of edad by nivel de estudios  
(Bonferroni)

| Row Mean-<br>Col Mean | 1                 | 2                 | 3                |
|-----------------------|-------------------|-------------------|------------------|
| 2                     | -7.56607<br>0.000 |                   |                  |
| 3                     | -16.1187<br>0.000 | -8.55261<br>0.000 |                  |
| 4                     | -15.7156<br>0.000 | -8.14951<br>0.001 | .403104<br>1.000 |

Comparison of edad by nivel de estudios  
(Scheffe)

| Row Mean-<br>Col Mean | 1                 | 2                 | 3                |
|-----------------------|-------------------|-------------------|------------------|
| 2                     | -7.56607<br>0.000 |                   |                  |
| 3                     | -16.1187<br>0.000 | -8.55261<br>0.000 |                  |
| 4                     | -15.7156<br>0.000 | -8.14951<br>0.002 | .403104<br>0.998 |

# Comparación no paramétrica

- Prueba Kruskal-Wallis

**kwallis** *var1,by(vargrupo)*

```
kwallis edad,by(educacio)
```

Test: Equality of populations (Kruskal-Wallis test)

| educacio | Obs | Rank Sum  |
|----------|-----|-----------|
| 1        | 188 | 101002.50 |
| 2        | 408 | 163864.00 |
| 3        | 163 | 49147.50  |
| 4        | 51  | 14441.00  |

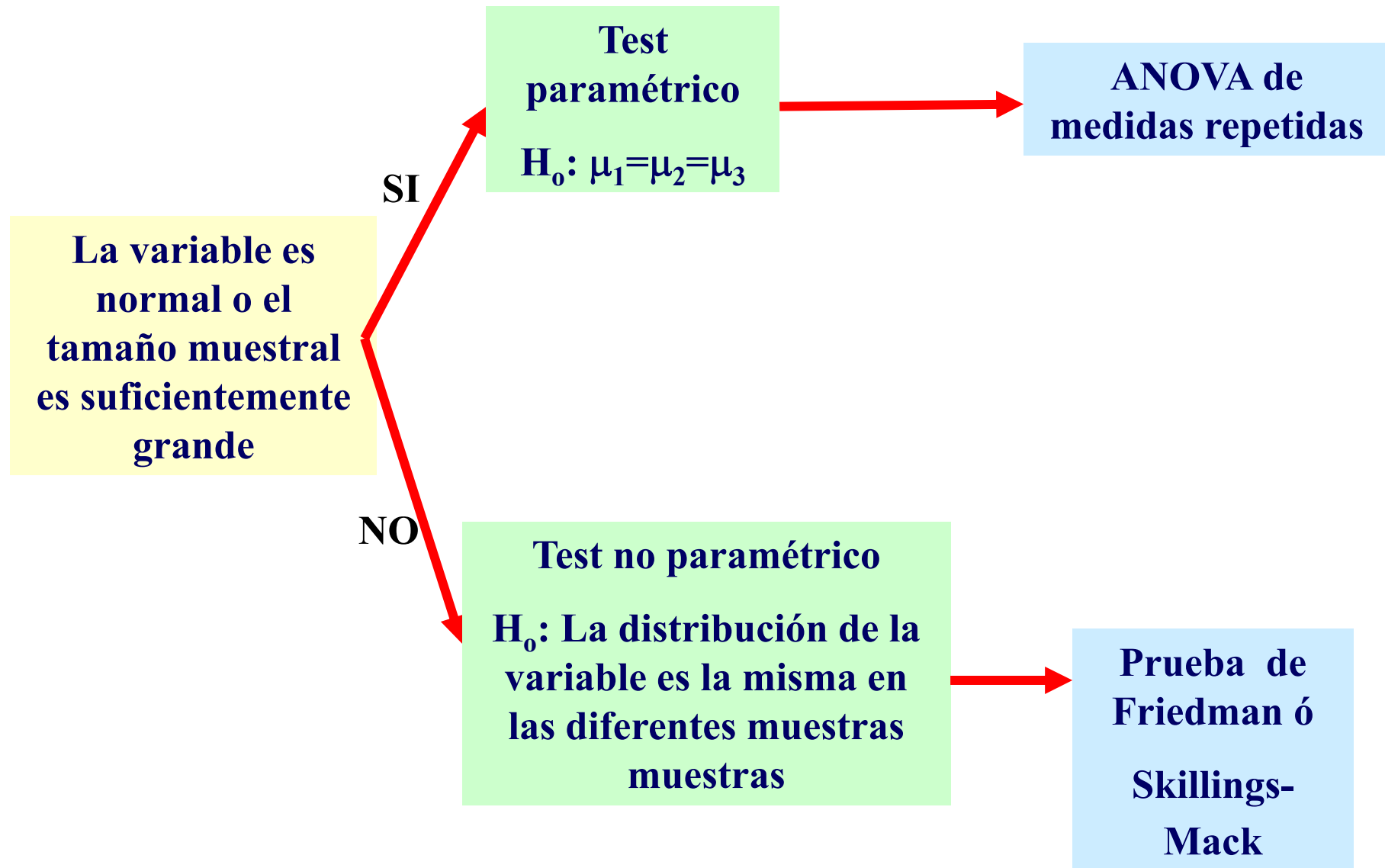
chi-squared = 105.860 with 3 d.f.

probability = 0.0001

chi-squared with ties = 105.923 with 3 d.f.

probability = 0.0001

## >2 Muestras dependientes



# Comparación de medias

- ANOVA de medidas repetidas. Datos “long2

**anova** *var1 varmedicion id, repeated(medicacion)*

```
. anova tas medicion numero, repeated(medicion)
```

```
Number of obs =      639      R-squared      = 0.6067
Root MSE      = 10.4854      Adj R-squared = 0.5582
```

| Source     | Partial SS | df  | MS         | F     | Prob > F |
|------------|------------|-----|------------|-------|----------|
| Model      | 96330.6179 | 70  | 1376.15168 | 12.52 | 0.0000   |
| medicacion | 11716.8386 | 11  | 1065.16714 | 9.69  | 0.0000   |
| numero     | 82921.013  | 59  | 1405.4409  | 12.78 | 0.0000   |
| Residual   | 62448.3054 | 568 | 109.9442   |       |          |
| Total      | 158778.923 | 638 | 248.869786 |       |          |

# Comparación de medias

- ANOVA de medidas repetidas. Datos “long”

**anova** *var1 varmedicion id, repeated(medicion)*

```
. anova tas medicion numero, repeated(medicion)
```

```
.....
```

```
Between-subjects error term: numero
```

```
Levels: 60 (59 df)
```

```
Lowest b.s.e. variable: numero
```

```
Repeated variable: medicion
```

```
Huynh-Feldt epsilon = 0.8579
```

```
Greenhouse-Geisser epsilon = 0.7316
```

```
Box's conservative epsilon = 0.0909
```

|          |     |      | ----- Prob > F ----- |        |        |        |
|----------|-----|------|----------------------|--------|--------|--------|
| Source   | df  | F    | Regular              | H-F    | G-G    | Box    |
| medicion | 11  | 9.69 | 0.0000               | 0.0000 | 0.0000 | 0.0030 |
| Residual | 568 |      |                      |        |        |        |

# Comparación no paramétrica

- Test de Skillings-Mack. Datos “long”

**skilmack** *var1* ,**i**(*ident*) **repeated**(*medicion*)

```
skilmack tas ,id(numero) repeated(medicion)
```

Weighted Sum of Centered Ranks

| medicion | N  | WSumCRank | SE    | WSum/SE |
|----------|----|-----------|-------|---------|
| 1        | 57 | 136.81    | 24.06 | 5.69    |
| 2        | 57 | 102.14    | 24.06 | 4.24    |
| 3        | 55 | 40.97     | 24.02 | 1.71    |
| 4        | 53 | -22.63    | 23.77 | -0.95   |
| 5        | 52 | -11.31    | 23.85 | -0.47   |
| 6        | 52 | -88.39    | 23.85 | -3.71   |
| 7        | 51 | -69.85    | 23.64 | -2.95   |
| 8        | 52 | -25.41    | 23.85 | -1.07   |
| 9        | 52 | -37.92    | 23.85 | -1.59   |
| 10       | 52 | -1.16     | 23.85 | -0.05   |
| 11       | 51 | 10.73     | 23.64 | 0.45    |
| 12       | 52 | -33.97    | 23.85 | -1.42   |
| Total    |    | 0         |       |         |

# Comparación no paramétrica

- Test de Skillings-Mack. Datos “long”

**skilmack** *var1* ,**i**(*ident*) **repeated**(*medicion*)

```
skilmack tas ,id(numero) repeated(medicion)
```

```
.....
```

Note N= 3 not included as only had one observation

Skillings Mack = 76.340

P-value (No ties) = 0.0000

N.B. As P-value <0.02, it is likely to be conservative (unless n large).  
Consider obtaining a p-value from a simulated null  
distribution of SM - see options.

Ties exist. Above SEs and P-value approximate, if not too many ties;  
639 rows of [numero, tas]; 308 different combinations; n(numero) = 60

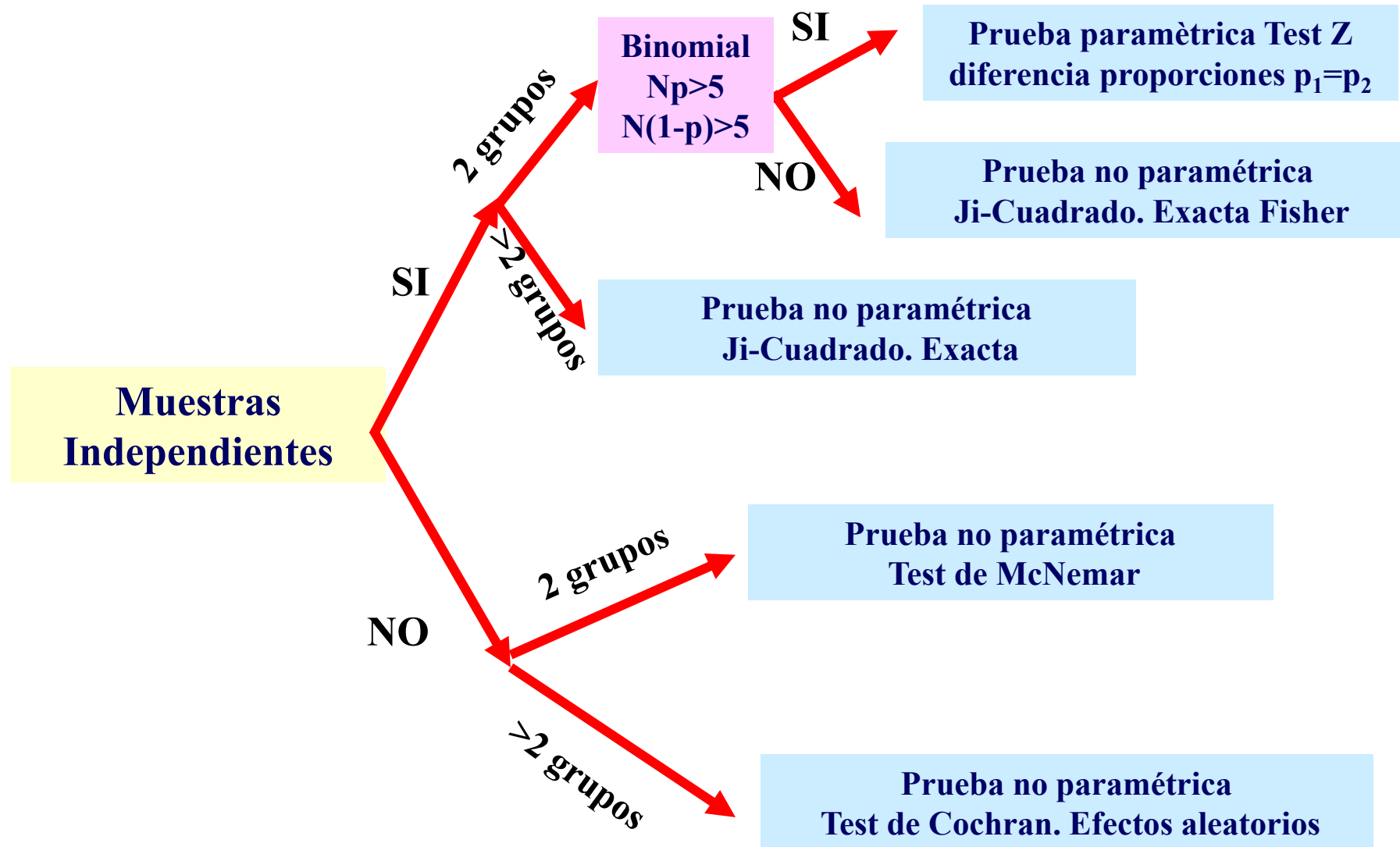
Consider using the p-value below, (which is found from a simulated  
conditional null distribution of SM - see options -  
simulating .....)

Empirical P-value (Ties) ~ 0.0000

**Relación entre variable  
cualitativa (2 niveles) según los  
niveles de una variable cualitativa**



# Relación variables categóricas



# Muestras Independientes

- Prueba Ji cuadrado, Exacta de Fisher

**tabulate** *variable1 variable2* , **chi exact exp**

```
. tabulate expcateg aids, chi exact exp
```

```
+-----+
| Key      |
+-----+
| frequency|
| expected frequency|
+-----+
```

| exposure<br>category | aids diagnosis |       | Total |
|----------------------|----------------|-------|-------|
|                      | yes            | no    |       |
| HSH                  | 20             | 63    | 83    |
|                      | 18.7           | 64.3  | 83.0  |
| UDI                  | 74             | 260   | 334   |
|                      | 75.3           | 258.7 | 334.0 |
| Total                | 94             | 323   | 417   |
|                      | 94.0           | 323.0 | 417.0 |

```

Pearson chi2(1) = 0.1434   Pr = 0.705
Fisher's exact = 0.769
1-sided Fisher's exact = 0.402

```

## 2 Muestras Independientes

- Test z paramétrico para diferencia proporciones (variable codificada como 0 y 1)

**prtest** *variable1* ,by(*variable2*)

```
. prtest aids, by(expcateg)
```

Two-sample test of proportion

HSH: Number of obs = 83

UDI: Number of obs = 334

| Variable | Mean      | Std. Err. | z    | P> z  | [95% Conf. Interval] |          |
|----------|-----------|-----------|------|-------|----------------------|----------|
| HSH      | .2409639  | .0469427  |      |       | .1489578             | .3329699 |
| UDI      | .2215569  | .0227239  |      |       | .1770189             | .2660949 |
| diff     | .019407   | .0521536  |      |       | -.0828121            | .1216261 |
|          | under Ho: | .0512489  | 0.38 | 0.705 |                      |          |

diff = prop(HSH) - prop(UDI) z = 0.3787  
Ho: diff = 0

|                    |                        |                  |
|--------------------|------------------------|------------------|
| Ha: diff < 0       | Ha: diff != 0          | Ha: diff > 0     |
| Pr(Z < z) = 0.6475 | Pr( Z  <  z ) = 0.7049 | Pr(Z > z) = 0.35 |

## 2 Muestras Dependientes

- Test McNemar (2 mediciones variables (0,1) a través de un estudio casos control apareado

**mcc** var1 var2

**. mcc rtas1 rtas12**

|           | Controls          |       |
|-----------|-------------------|-------|
| Cases     | Exposed Unexposed | Total |
| Exposed   | 12 19             | 31    |
| Unexposed | 3 18              | 21    |
| Total     | 15 37             | 52    |

**McNemar's** chi2(1) = 11.64 Prob > chi2 = **0.0006**

Exact McNemar significance probability = 0.0009

Proportion with factor

Cases .5961538

Controls .2884615

[95% Conf. Interval]

difference .3076923

.1327038 .4826808

ratio 2.066667

1.349346 3.16532

rel. diff. .4324324

.2452494 .6196155

odds ratio 6.333333

1.864327 33.41648

(exact)

## 2 Muestras Dependientes

- Test de simetria ( útil para 2 niveles de la variable)

**symmetry** *var1 var2*

```
. symmetry rtas1 rtas12
```

|          |          |                 |       |
|----------|----------|-----------------|-------|
| TAS      |          |                 |       |
| medicion |          | TAS medicion 12 |       |
| 1        | <140mmHg | >140mmHg        | Total |
| <140mmHg | 18       | 3               | 21    |
| >140mmHg | 19       | 12              | 31    |
| Total    | 37       | 15              | 52    |

|                                       |       |    |        |
|---------------------------------------|-------|----|--------|
|                                       | chi2  | df |        |
| Prob>chi2                             |       |    |        |
| Symmetry (asymptotic)                 | 11.64 | 1  | 0.0006 |
| Marginal homogeneity (Stuart-Maxwell) | 11.64 | 1  | 0.0006 |

```
symmi 18 3 \ 19 12
```

## >2 Muestras Dependientes

- Test de Cochran (variable respuesta de 2 niveles de la variable)

**cochran** *var1 var2 ...varN*

```
. cochran rtas1 rtas2 rtas12, detail
```

Test for equality of proportions of nonzero  
outcomes in matched samples (Cochran's Q):

| Variable    | Proportion | Count |
|-------------|------------|-------|
| -----+----- |            |       |
| rtas1       | .5961538   | 31    |
| rtas2       | .4615385   | 24    |
| rtas12      | .2884615   | 15    |
| -----       |            |       |

```
Number of obs      =          52  
Cochran's chi2(2)  =    13.78571  
Prob > chi2        =    0.0010
```

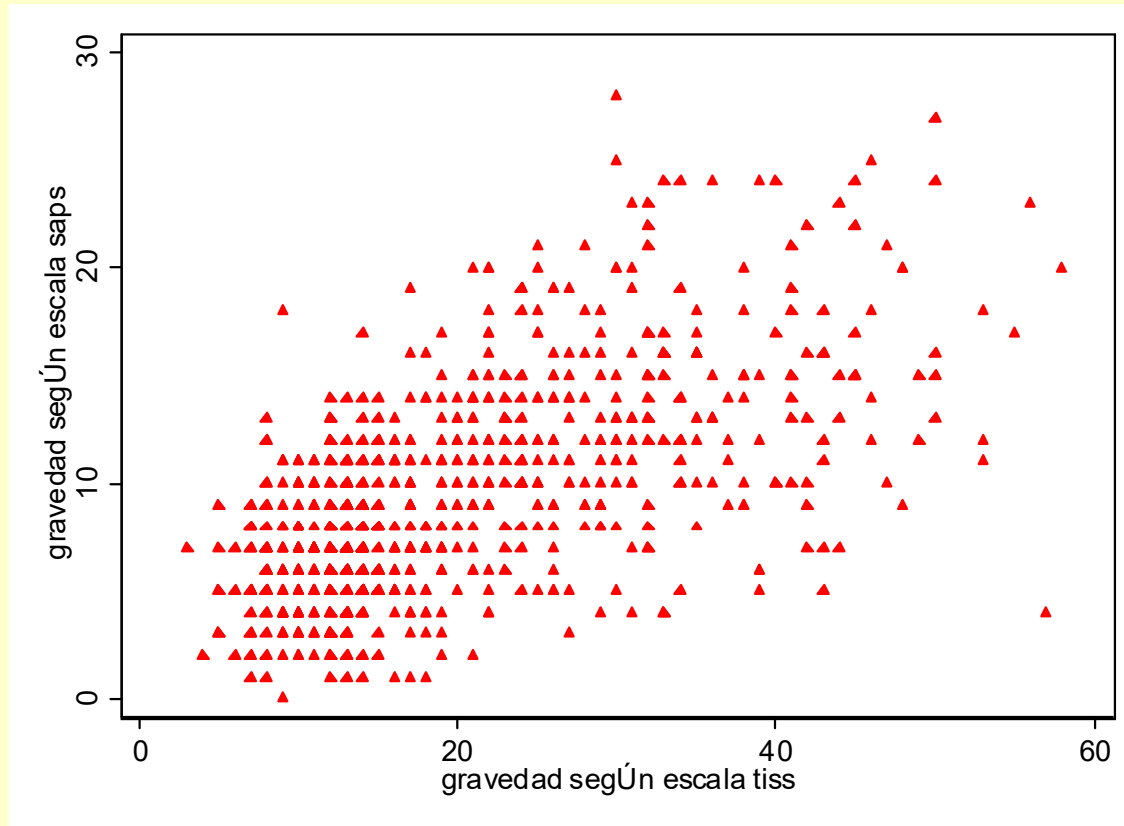
# Relación entre 2 variables cuantitativas (correlación y regresión)

# Gràfico de Dispersion

- Scatterplot

```
sc var1 var2, msymbol(sym) mcolor(color) msize(size)
```

```
sc saps tiss, mcolor(red) msymbol(triangle) msize(small)
```



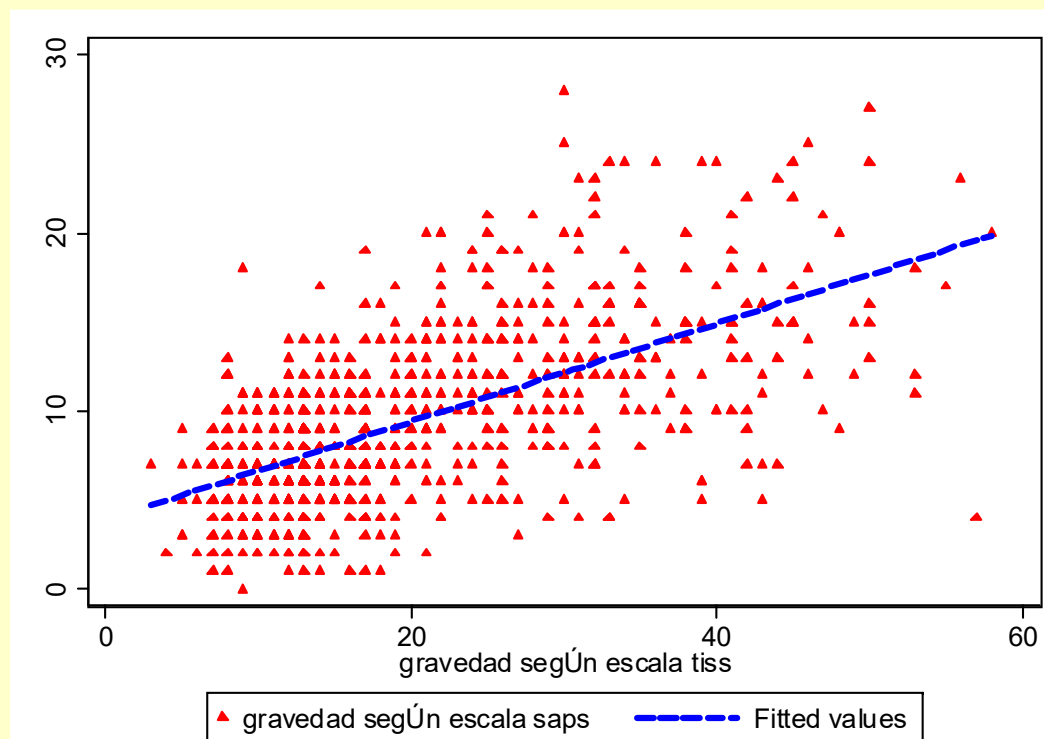


# Añadir gràficos (Twoway)

- Es poden combinar gràficos amb el comando twoway para mirar la forma de la relación entre las dos variables

```
twoway sc var1 var2, msymbol(sym) mcolor(color) msize(size)  
|| lfit var1 var2, lpattern(lp) lwidth(lw) lcolor(lc)
```

```
twoway sc saps tiss, mcolor(red) msymbol(triangle) msize(small)  
|| lfit saps tiss, lpattern(dash) lwidth(thick) lcolor(blue)
```

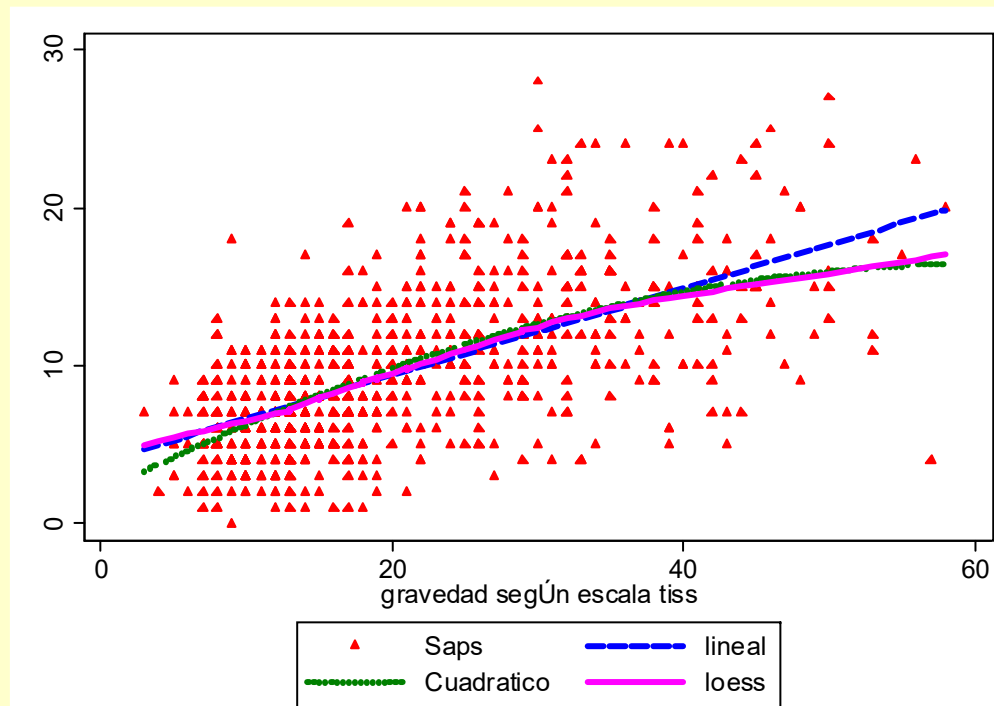


# Añadir gráficos (Twoway)

- Otras opciones para el twoway son

```
||lfit    ||mspline    ||lowess    ||lfit ||qfit  
||fpfit   ||lfitci     ||qfitci   ||fpfitci  
||, title() subtitle() note() legend( label(# eti#) )
```

```
twoway sc saps tiss, mcolor(red) msymbol(triangle) msize(small)  
|| lfit saps tiss, lpattern(dash) lwidth(thick) lcolor(blue)  
|| qfit saps tiss, lpattern(dot) lwidth(thick) lcolor(green)  
|| lowess saps tiss, lpattern(solid) lwidth(thick) lcolor(magenta)  
||, legend( label(1 Saps) label(2 lineal) label(3 Cuadratico) label(4 loess))
```



# Correlación

- Existen dos comandos para obtener la correlación

**corr var1 var2 var3**

**pwcorr var1 var2 var3, sig obs**

```
. corr tiss saps edad
```

```
(obs=827)
```

|      | tiss    | saps   | edad   |
|------|---------|--------|--------|
| tiss | 1.0000  |        |        |
| saps | 0.6183  | 1.0000 |        |
| edad | -0.0579 | 0.2145 | 1.0000 |

```
. pwcorr tiss saps edad, sig obs
```

|      | tiss    | saps   | edad   |
|------|---------|--------|--------|
| tiss | 1.0000  |        |        |
|      | 829     |        |        |
| saps | 0.6188  | 1.0000 |        |
|      | 0.0000  |        |        |
|      | 828     | 837    |        |
| edad | -0.0592 | 0.2118 | 1.0000 |
|      | 0.0889  | 0.0000 |        |
|      | 828     | 836    | 844    |

# Regresión lineal con Stata

- Regresión lineal entre dos variables cuantitativas

**regress** depvar [indepvars] , **opciones**

**regress saps tiss**

| Source   | SS         | df        | MS         | Number of obs = 828    |                      |          |
|----------|------------|-----------|------------|------------------------|----------------------|----------|
| Model    | 7230.58002 | 1         | 7230.58002 | F( 1, 826) = 512.47    |                      |          |
| Residual | 11654.1688 | 826       | 14.1091632 | Prob > F = 0.0000      |                      |          |
| Total    | 18884.7488 | 827       | 22.8352464 | R-squared = 0.3829     |                      |          |
|          |            |           |            | Adj R-squared = 0.3821 |                      |          |
|          |            |           |            | Root MSE = 3.7562      |                      |          |
| saps     | Coef.      | Std. Err. | t          | P> t                   | [95% Conf. Interval] |          |
| tiss     | .2755289   | .0121711  | 22.64      | 0.000                  | .2516389             | .2994189 |
| _cons    | 3.897909   | .2743255  | 14.21      | 0.000                  | 3.359452             | 4.436366 |