

An Introduction to Biological Significance Analysis

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Outline

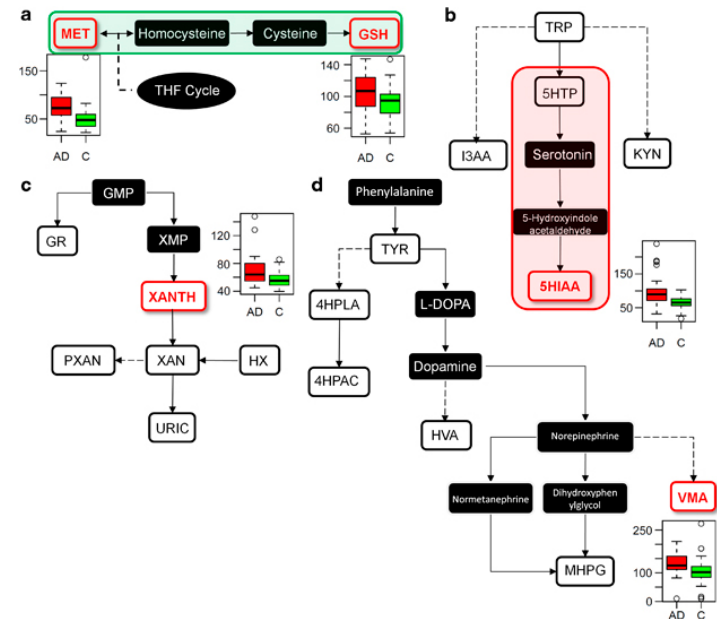
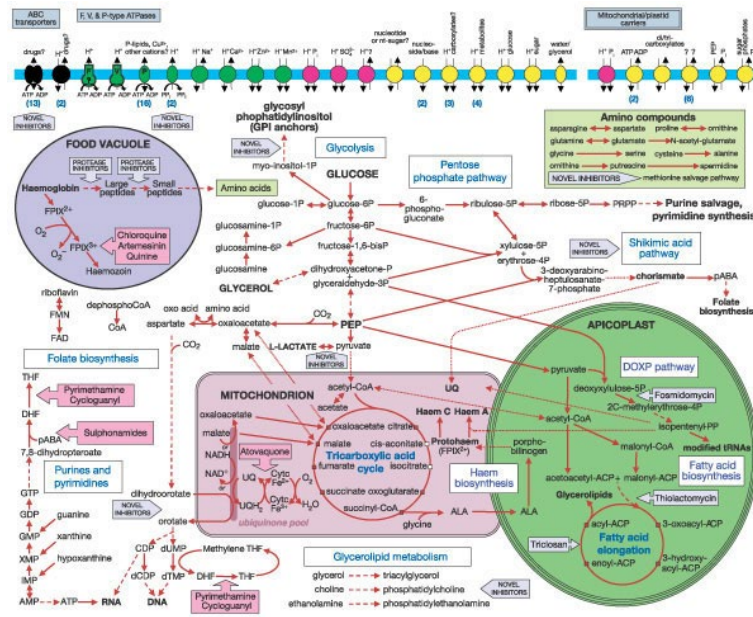
- Presentation
- Introduction and Background
 - Gene lists, Identifiers and Pathway databases
- Pathway Analysis: Methods and Tools
 - Overrepresentation analysis
 - GSEA: Gene Set Enrichment Analysis
 - Multiple Testing Adjustments
- Examples with R and Bioconductor

Introduction & Background

Health, disease and pathways

Metabolism is a complex network of chemical reactions within the confines of a cell that can be analyzed in self-contained parts called **pathways**

One can generally assume that “normal” metabolism is what happens in healthy state or, reciprocally, that disease can *be associated with some type of alteration in metabolism*.



Pathways altered in ALZHEIMER disease

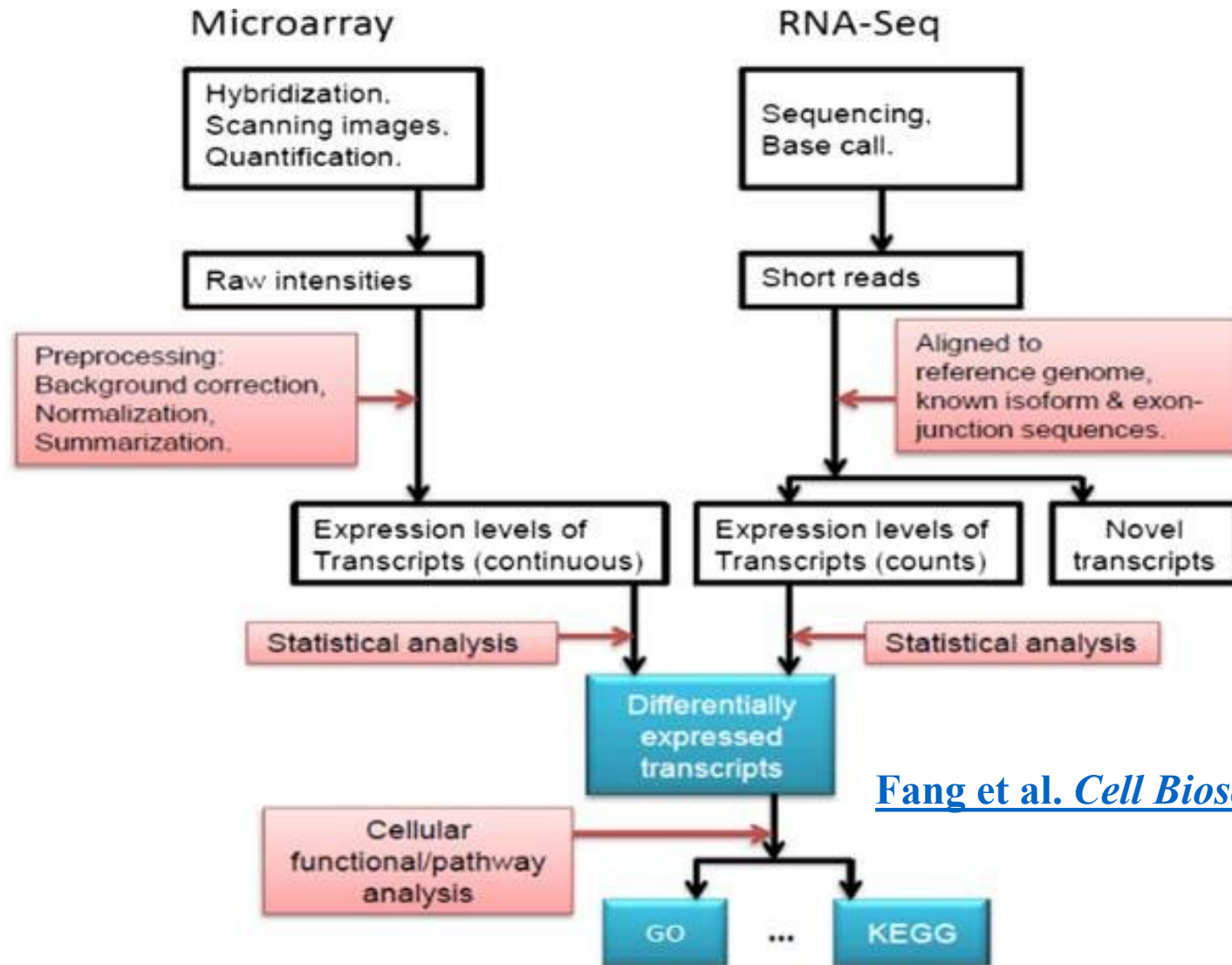
Characterization of disease can be attempted by studying how this affects or disrupts pathways
That's what Pathway Analysis is about (more or less)

Pathway Analysis

- The term Pathway Analysis denotes *any analytic technique that benefits from biological pathway or molecular network information to gain insight into a biological system*. (Creixell et al., Nature Methods 2015 (12 (7)))
- To be more specific, Pathway Analysis methods rely on high throughput information provided by omics technologies to:
 - Contextualize findings to help understand the mechanism of disease
 - Identify genes/proteins associated with the aetiology of a disease
 - Predict drug targets
 - Understand how to therapeutically intervene in disease processes
 - Conduct target literature searches
 - Integrate diverse biological information

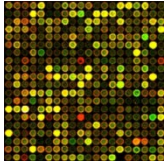
The beginning: *Gene Lists*

The life-cycle of an omics-based study



Fang et al. *Cell Biosci.* 2012; 2: 26.

The (in)famous “*where to now?*” question



- You obtained a list of features. What's next?
 - Select some genes for validation?
 - Follow up experiments on some genes/proteins/...?
 - Publish a huge table with all results?
 - Try to learn about **all** features in the list?

GNAQ
GNAS
DGKZ
GUCY1A3
PDE4B
PDE4D
ATP2A2
ATP2A3
NOS1
CNN1
GSTO1
NOS3
CNN2
MYLK2
CALD1
ACTA1
MYL2



GNAQ
GNAS
DGKZ
GUCY1A3
PDE4B
PDE4D
ATP2A2
ATP2A3
NOS1
CNN1
GSTO1
NOS3
CNN2
MYLK2
CALD1
ACTA1
MYL2

my favorite gene

NCBI Resources How To

PubMed GNAQ

US National Library of Medicine
National Institutes of Health

RSS Save search Advanced

Show additional filters

Display Settings: ☒ Summary, 20 per page, Sorted by Recently A

Article types
Review
More ...

Text availability
Abstract available
Free full text available
Full text available

Publication dates
5 years

See 225 articles about GNAQ gene function
See also: GNAQ guanine nucleotide binding protein (G protein), [gnaq](#) in [Homo sapiens](#) | [Mus musculus](#) | [Rattus norvegicus](#) | [All](#)

Results: 1 to 20 of 114

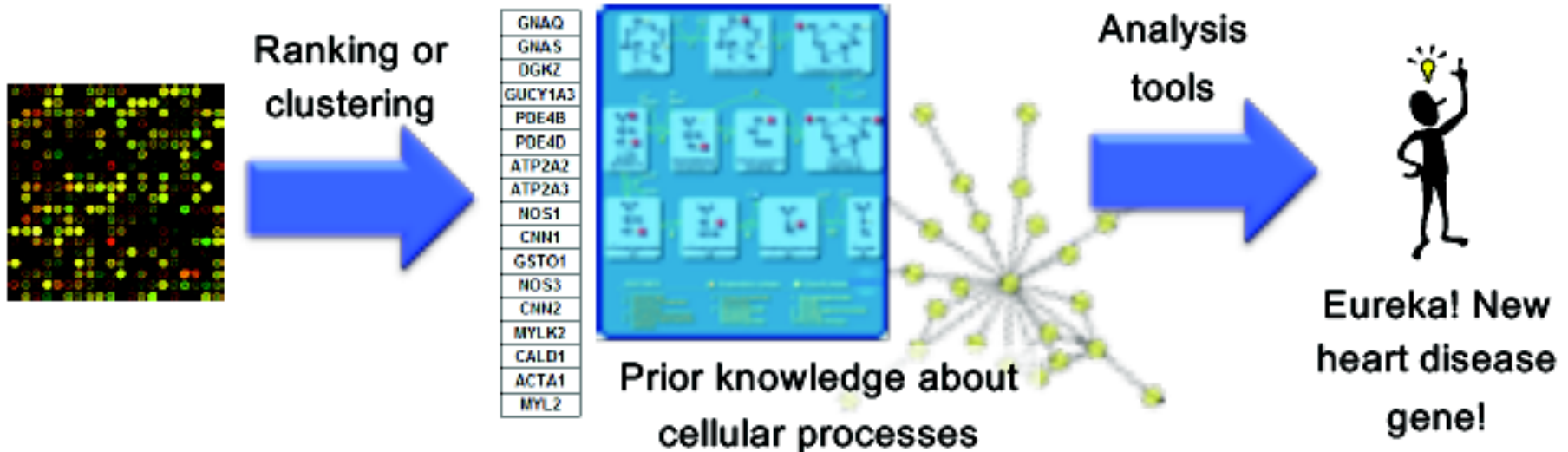
☐ Sturge-Weber Syndrome and Port-Wine Stains Caused by
1. Shirley MD, Tang H, Gallione CJ, Baugher JD, Frelin LP, AM, Pevsner J.
N Engl J Med. 2013 May 8. [Epub ahead of print]
Med - as supplied by publisher

From gene lists to *Pathway Analysis*

- Gene lists are made of individual genes
 - Information about each gene can be extracted from databases.
 - Generically described as ***Gene Annotation***
- Besides, we may obtain information from the analysis of *gene sets*
 - Genes don't act individually, rather in groups
More ***realistic*** approach
 - There are less gene sets than individual genes
Relatively ***simpler*** to manage.
 - Generically described as ***Pathway Analysis***

Pathway Analysis Wishlist

- Tell me what's interesting about these genes
 - Are they enriched in known pathways, complexes, functions



Example 1

- Lists [AvsB](#), [AvsL](#) and [BvsL](#) contain the IDs of genes selected by being differentially expressed between three types of breast cancer tumors.
 - Farmer P, Bonnefoi H, Becette V, Tubiana-Hulin M et al. Identification of molecular apocrine breast tumours by microarray analysis. *Oncogene* 2005 Jul 7;24(29):4660-71. PMID: [15897907](#)
- See the analysis that generates the list in: [https://github.com/alexsanchezpla/Ejemplo de MDA con Bioconductor](https://github.com/alexsanchezpla/Ejemplo_de_MDA_con_Bioconductor)

Example 2

- Genes with frequent somatic SNVs identified in TCGA exome sequencing data of 3,200 tumors of 12 types
- 127 cancer driver genes displaying higher than expected mutation frequencies were detected using the MuSiC software.
- Genes are ranked in decreasing order of significance and mutation frequency

TP53
PIK3CA
PTEN
APC
VHL
KRAS
MLL3
MLL2
ARID1A
PBRM1
NAV3
EGFR
NF1
PIK3R1
CDKN2A
GATA3
RB1
NOTCH1
FBXW7
CTNNB1
DNMT3A
MAP3K1
FLT3
MALAT1
TSHZ3

Example 3

- Third example is a ranked list of genes obtained from TCGA ovarian cancer dataset.
- Two subgroups -immunoreactive and mesenchymal- were compared.
- The list contains **all genes, not only differentially expressed**, ranked by the value of statistic.

rank	GeneName	test statistic
1	IGDCC3	35.5553322839225
2	ANTXR1	35.3770766531836
3	AEBP1	33.0690543534961
4	FBN1	32.1199562790897
5	ANGPTL2	31.8605806216522
6	COL16A1	31.7641267462069
7	BGN	31.533826423921
...
15201	IRF1	-14.7629673442493
15202	CXCL10	-14.982733665643
15203	TAP2	-15.1488606179238
15204	UBE2L6	-15.7162058907796
15205	KIAA0319	-15.7796986548781
15206	PSMB8	-15.7846188665582
15207	PSME1	-16.4510045533584
15208	CSAG3	-16.8014265945244
15209	OVGP1	-17.6903158148446
15210	GBP4	-17.9447602030134
15211	TAP1	-18.0549262210415
15212	PSME2	-18.3639448844986
15213	PSMB9	-18.6614452029879

Gene Lists and Annotations

Gene and Protein Identifiers

- Identifiers (IDs) are ideally unique, stable names or numbers that help track database records
 - E.g. Social Insurance Number, Entrez Gene ID 41232
- But information on features is stored in many databases.
 - The same genes has many distinct IDs
- Records for: Gene, DNA, RNA, Protein
 - Important to recognize the correct record type
 - E.g. Entrez Gene records don't store sequence. They link to DNA regions, RNA transcripts and proteins e.g. in RefSeq, which stores sequence.

TP53
PIK3CA
PTEN
APC
VHL
KRAS
MLL3
MLL2
ARID1A
PBRM1
NAV3
EGFR
NF1
PIK3R1
CDKN2A
GATA3
RB1
NOTCH1
FBXW7
CTNNB1
DNMT3A
MAP3K1
FLT3
MALAT1
TSHZ3

Common Identifiers

Gene

Ensembl [ENSG00000139618](#)

Entrez Gene [675](#)

Unigene [Hs.34012](#)

RNA transcript

GenBank [BC026160.1](#)

RefSeq [NM_000059](#)

Ensembl [ENST00000380152](#)

Protein

Ensembl [ENSP00000369497](#)

RefSeq [NP_000050.2](#)

UniProt [BRCA2_HUMAN](#) or
[A1YBP1_HUMAN](#)

IPI [IPI00412408.1](#)

EMBL [AF309413](#)

PDB [1MIU](#)

Species-specific

HUGO HGNC [BRCA2](#)

MGI [MGI:109337](#)

RGD [2219](#)

ZFIN [ZDB-GENE-060510-3](#)

FlyBase [CG9097](#)

WormBase [WBGene00002299](#) or [ZK1067.1](#)

SGD [S000002187](#) or [YDL029W](#)

Annotations

InterPro [IPR015252](#)

OMIM [600185](#)

Pfam [PF09104](#)

Gene Ontology [GO:0000724](#)

SNPs [rs28897757](#)

Experimental Platform

Affymetrix [208368_3p_s_at](#)

Agilent [A_23_P99452](#)

CodeLink [GE60169](#)

Illumina [GI_4502450-S](#)

Red =

Recommended

Identifier Mapping

- There are many IDs!
 - Software tools recognize only a handful
 - May need to map from your gene list IDs to standard IDs
- Four main uses
 - Searching for a favourite gene name
 - Link to related resources
 - Identifier translation
 - E.g. Proteins to genes, Affy ID to Entrez Gene
 - Merging data from different sources
 - Find equivalent records

ID Challenges

- Avoid errors: map IDs correctly
 - Beware of 1-to-many mappings
- Gene name ambiguity – not a good ID
 - e.g. FLJ92943, LFS1, TRP53, p53
 - Better to use the standard gene symbol: TP53
- Excel error-introduction
 - OCT4 is changed to October-4 (paste as text)
- Problems reaching 100% coverage
 - E.g. due to version issues
 - Use multiple sources to increase coverage

Zeeberg BR et al. *Mistaken identifiers: gene name errors can be introduced inadvertently when using Excel in bioinformatics*
BMC Bioinformatics. 2004 Jun 23;5:80

Use ID converters to prepare list

Option 1: DAVID

DAVID Bioinformatics Resources 2007
National Institute of Allergy and Infectious Diseases (NIAID), NIH

Gene Accession Conversion Tool

Save the results
Submit the converted genes to DAVID for other analytical tools!!

Gene Accession Conversion Statistics

Conversion Summary

ID Count	In DAVID DB	Conversion
157 IDs	Yes	Successful
8 IDs	Yes	None
0 IDs	No	NA
1 IDs	Ambiguous	Pending
Total Unique User IDs: 166		

Summary

The possible choices for ambiguous genes

The possible choices for each individual ambiguous genes

Summary of Ambiguous Gene IDs

ID Count	Possible Source	Convert All
1	ENTREZ_GENE_ID	<input type="checkbox"/>
1	GI_ACCESSION	<input type="checkbox"/>

Possible Sources For Ambiguous IDs

Ambiguous ID	Possibility	Convert
3538	ENTREZ_GENE_ID	<input type="checkbox"/>
3538	GI_ACCESSION	<input type="checkbox"/>

Genes that have been converted.

From	To	Species	David Gene Name
*1112_G_AT	4684	HOMO SAPIENS	NEURAL CELL ADHESION MOLECULE 1
*1331_S_AT	8718	HOMO SAPIENS	TUMOR NECROSIS FACTOR RECEPTOR SUPERFAMILY, MEMBER 25
*1355_G_AT	4915	HOMO SAPIENS	NEUROTROPHIC TYROSINE KINASE, RECEPTOR, TYPE 2
*1372_AT	7130	HOMO SAPIENS	TUMOR NECROSIS FACTOR, ALPHA-INDUCED PROTEIN 6
*1391_S_AT	1579	HOMO SAPIENS	CYTOCHROME P450, FAMILY 4, SUBFAMILY A, POLYPEPTIDE 11
*1403_S_AT	6352	HOMO SAPIENS	CHEMOKINE (C-C MOTIF) LIGAND 5
*1419_G_AT	4843	HOMO SAPIENS	NITRIC OXIDE SYNTHASE 2A (INDUCIBLE, HEPATOCYTES)
*1575_AT	5243	HOMO SAPIENS	ATP-BINDING CASSETTE, SUB-FAMILY B (MDR/TAP), MEMBER 1
*1645_AT	2814	HOMO SAPIENS	KISS-1 METASTASIS-SUPPRESSOR
*1786_AT	10461	HOMO SAPIENS	C-MER PROTO-ONCOGENE TYROSINE KINASE
*1855_AT	2248	HOMO SAPIENS	FIBROBLAST GROWTH FACTY INTEGRATION SITE (V-INT-2)
*1890_AT	9518	HOMO SAPIENS	GROWTH DIFFERENTIATION

Species of converted gene IDs

Converted gene IDs

Users' input gene IDs

*Users' decision for ambiguous IDs

g:Profiler

News Archives Beta API R client FAQ Docs Contact Cite g:Profiler Services using g:P List of organisms

g:Profiler has been updated with new data from Ensembl.

Show more... Close

g:GOST Functional profiling

g:Convert Gene ID conversion

g:Orth Orthology search

g:SNPense SNP id to gene name

Query

Options

Organism:

Target namespace:

Numeric IDs treated as:

Run query

Left Panel

Right Panel

Example 1: Gene ID conversion with g:Converter

g:Convert enables to convert between various gene, protein, microarray probe and numerous other types of namespaces. We provide at least 40 types of IDs for more than 60 species. The 98 different namespaces supported for human include Ensembl, Refseq,

Illumina, Entrezgene and Uniprot identifiers. All namespaces are obtained through matching them via Ensembl gene identifiers as a reference.

Example: Gene ID conversion with *g:Convert*

g:Profiler News Archives Beta API R client FAQ Docs Contact Cite g:Profiler Services using g:P List of organisms

g:Profiler has been updated with new data from Ensembl. [Show more...](#) [Close](#)

g:GOST Functional profiling **g:Convert** Gene ID conversion **g:Orth** Orthology search **g:SNPense** SNP id to gene name

Query ⓘ

TP53
PIK3CA
PTEN
APC
VHL
KRAS
MLL3
MLL2
AR1D1A
PBRM1
|

Options

Organism: ⓘ
Homo sapiens (Human)

Target namespace
ENSG

Numeric IDs treated as
|

[Run query](#)

g:Convert enables to convert between various gene, protein, microarray probe and numerous other types of namespaces. We provide at least 40 types of IDs for more than 60 species. The 98 different namespaces supported for human include Ensembl, Refseq,

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Example: Gene ID conversion with *g:Convert*

g:Profiler

NewsArchivesBetaAPIR clientFAQDocsContactCite g:ProfilerServices using g:PList of organisms

g:Profiler has been updated with new data from Ensembl.

Show more...Close

g:GOST
Functional profiling

g:Convert
Gene ID conversion

g:Orth
Orthology search

g:SNPense
SNP id to gene name

Query

TP53
PIK3CA
PTEN
APC
VHL
KRAS
MLL3
MLL2
AR1D1A
PBRM1

Run query

Options

Organism:

Homo sapiens (Human)

Target namespace

ENSG

Numeric IDs treated as

Export to CSV


Show query URL

Show short link

initial alias	converted alias	name	description	namespace
TP53	ENSG00000141510	TP53	tumor protein p53 [Source:HGNC Symbol;Acc:HGNC:11998]	DBASSS, ENTREZGENE, HGNC, U
PIK3CA	ENSG00000121879	PIK3CA	phosphatidylinositol-4,5-bisphosphate 3-kinase catalytic subunit alpha [Source:HGNC ...	ENTREZGENE, HGNC, UNIPROT_
PTEN	ENSG00000171862	PTEN	phosphatase and tensin homolog [Source:HGNC Symbol;Acc:HGNC:9588]	DBASSS, ENTREZGENE, HGNC, U
APC	ENSG00000134982	APC	APC regulator of WNT signaling pathway [Source:HGNC Symbol;Acc:HGNC:583]	ENTREZGENE, HGNC, UNIPROT_
VHL	ENSG00000134086	VHL	von Hippel-Lindau tumor suppressor [Source:HGNC Symbol;Acc:HGNC:12687]	ENTREZGENE, HGNC, UNIPROT_
KRAS	ENSG00000133703	KRAS	KRAS proto-oncogene, GTPase [Source:HGNC Symbol;Acc:HGNC:6407]	ENTREZGENE, HGNC, UNIPROT_
MLL3	None	None	None	
MLL2	None	None	None	
AR1D1A	None	None	None	
PBRM1	ENSG00000163939	PBRM1	polybromo 1 [Source:HGNC Symbol;Acc:HGNC:30064]	ENTREZGENE, HGNC, UNIPROT_

1 to 10 of 10 < > Page 1 of 1 > |

Beware of ambiguous ID mappings



g:Profiler

Welcome! About Contact Beta Archives R

g:GOST Gene Group Functional Profiling

g:Cocoa Compact Compare of Annotations

g:Convert Gene ID Converter

g:Sorter Expression Similarity Search

g:Orth Orthology search

J. Reimand, M. Kull, H. Peterson, J. Hansen, J. Vilo: g:Profiler -- a web-based toolset for functional profiling of gene lists from large-scale experiments (2007) NAR 35 W193-W200 [PDF]

J. Reimand, T. Arak, J. Vilo: g:Profiler -- a web server for functional interpretation of gene lists (2011 update) Nucleic Acids Research 2011; doi: 10.1093/nar/gkr378 [PDF]

[?] Organism

Homo sapiens

[?] Query (genes, proteins, probes, term)

TP53 MDM2 207105_S_AT P60484

[?] or Term ID:

g:Profile! Clear

Example or random query

Options

[?] ☒ Significant only

[?] ☐ Ordered query

[?] ☐ No electronic GO annotations

[?] ☐ Chromosomal regions

[?] ☒ Hierarchical sorting

[?] ☒ Hierarchical filtering

Show all terms (no filtering)

[?] Output type

Graphical (PNG)

Show advanced options

☒ Gene Ontology ☒ Biological process ☒ Cellular component ☒ Molecular function

Inferred from experiment [IDA, IPI, IMP, IGI, IEP]

Direct assay [IDA] / Mutant phenotype [IMP]

Genetic interaction [IGI] / Physical interaction [IPI]

Traceable author [TAS] / Non-traceable author [NAS] / Inferred by curator [IC]

Expression pattern [IEP] / Sequence or structural similarity [ISS] / Genomic context [IGC]

Biological aspect of ancestor [IBA] / Rapid divergence [IRD]

Reviewed computational analysis [RCA] / Electronic annotation [IEA]

No biological data [ND] / Not annotated [NA]

Biological pathways ☒ KEGG ☒ Reactome

Regulatory motifs in DNA ☒ TRANSFAC TFBS ☒ miRBase microRNAs

☒ CORUM protein complexes

☒ Human Phenotype Ontology (sequence homologs in other species)

☒ BioGRID protein-protein interaction

>> g:Convert
Gene ID Converter

>> g:Orth
Orthology Search

>> g:Sorter
Expression Similarity Search

>> g:Cocoa
Compact Compare of Annotations

>> Static URL
Come back later

Warning: Some gene identifiers are ambiguous. Resolve these manually?

Attempt to automatically resolve symbols using a namespace (percentage of ambiguous symbols resolved in brackets):

207105_S_AT

- ☐ ENSG00000268173 (PIK3R2, 26 GO annot.) - phosphoinositide-3-kinase, regulatory subunit 2 (beta) [Source:HGNC Symbol;Acc:HGNC:8980]
- ☐ ENSG00000105647 (PIK3R2, 26 GO annot.) - phosphoinositide-3-kinase, regulatory subunit 2 (beta) [Source:HGNC Symbol;Acc:HGNC:8980]

Resubmit query

Recommendations

- For proteins and genes
 - (doesn't consider splice forms)
 - Map everything to Entrez Gene IDs or Official Gene Symbols using an appropriate tool, such as gProfiler, DAVID or Biomart.
- If 100% coverage desired, manually curate missing mappings using multiple resources
- Be careful of Excel auto conversions – especially when pasting large gene lists!
 - Remember to format cells as 'text' before pasting

Pathway and *Gene Sets* Databases

Where is pathway information? (1)

- Most common sources*
 - Gene Ontology: Biological process,
 - Pathway databases:
 - Reactome : <http://reactome.org>
 - <http://www.pathguide.org>
 - MSigDB:
<http://www.broadinstitute.org/gsea/msigdb/>
 - <http://www.pathwaycommons.org/>

[*Comparison of human cell signaling pathway databases—evolution, drawbacks and challenges](#)

Where is pathway information? (2)

- Other annotations
 - Gene Ontology molecular function, cell location
 - Chromosome position
 - Disease association
 - DNA properties (TF binding sites, gene structure (intron/exon), SNPs, ...)
 - Transcript properties (Splicing, 3' UTR, microRNA binding sites, ...)
 - Protein properties (Domains, 2ry and 3ry structure, PTM sites)
 - Interactions with other genes

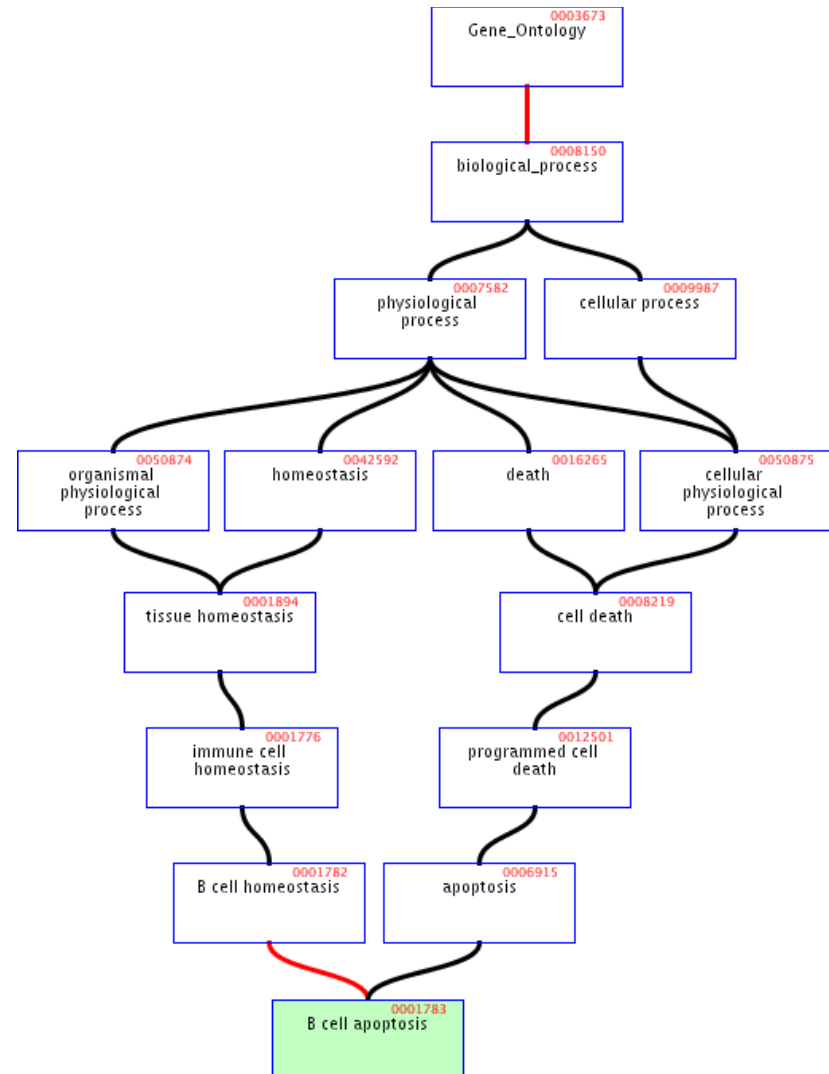
[*Comparison of human cell signaling pathway databases—evolution, drawbacks and challenges](#)

What is the Gene Ontology (GO)?

- Set of biological phrases (terms) which are applied to genes:
 - protein kinase, apoptosis, membrane
- An ontology is not a dictionary
 - Dictionary: A collection of term definitions,
 - Alphabetic organization
 - Ontology: A formal system for describing knowledge
 - Hierarchical organization
- <http://geneontology.org/>

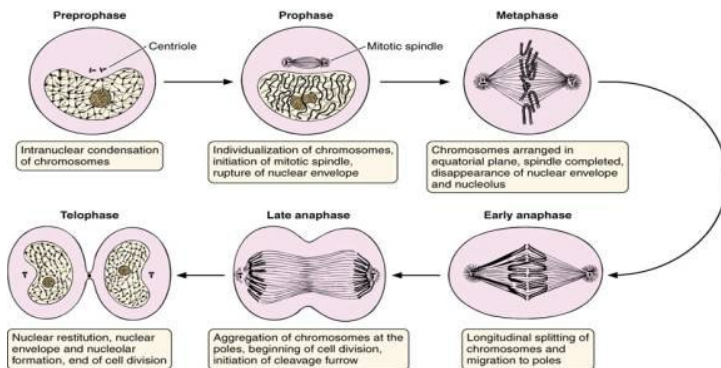
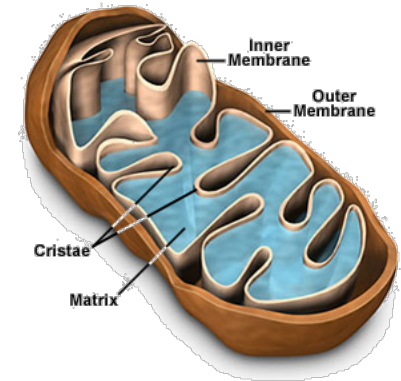
GO Structure

- Terms are related within a hierarchy
 - is-a
 - part-of
- Describes multiple levels of detail of gene function
- Terms can have more than one parent or child

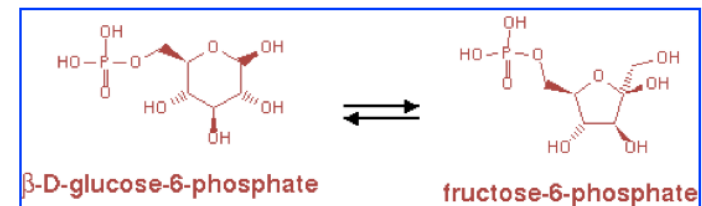


What is covered by the GO?

- GO terms divided into three aspects:
 - cellular component
 - molecular function
 - biological process



**Cell
division**



**glucose-6-phosphate
isomerase activity**

Annotation Sources

- Manual annotation
 - Curated by scientists
 - High quality
 - Small number (time-consuming to create)
 - Reviewed computational analysis
- Electronic annotation
 - Annotation derived without human validation
 - Computational predictions (accuracy varies)
 - Lower 'quality' than manual codes
- Key point: be aware of annotation origin

Evidence Types

- **Experimental Evidence Codes**

- **EXP:** Inferred from Experiment
- **IDA:** Inferred from Direct Assay
- **IPI:** Inferred from Physical Interaction
- **IMP:** Inferred from Mutant Phenotype
- **IGI:** Inferred from Genetic Interaction
- **IEP:** Inferred from Expression Pattern



- **Computational Analysis Evidence Codes**

- **ISS:** Inferred from Sequence or Structural Similarity
- **ISO:** Inferred from Sequence Orthology
- **ISA:** Inferred from Sequence Alignment
- **ISM:** Inferred from Sequence Model
- **IGC:** Inferred from Genomic Context
- **RCA:** inferred from Reviewed Computational Analysis



- **Author Statement Evidence Codes**

- **TAS:** Traceable Author Statement
- **NAS:** Non-traceable Author Statement

- **Curator Statement Evidence Codes**

- **IC:** Inferred by Curator
- **ND:** No biological Data available



- **IEA:** Inferred from electronic annotation

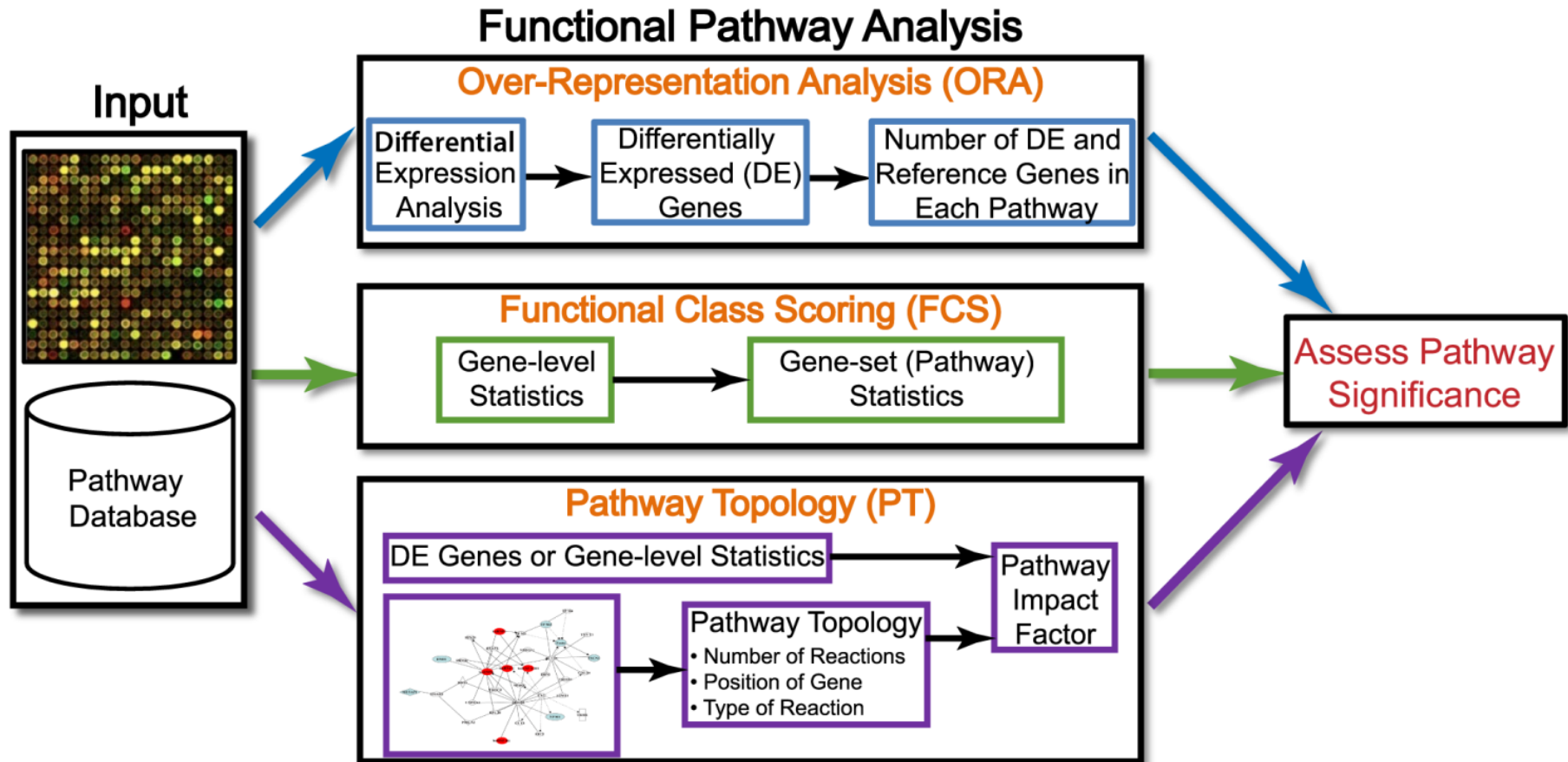


<http://www.geneontology.org/GO.evidence.shtml>

Pathway Analysis Methods

Overrepresentation Analysis
Gene Set Enrichment Analysis

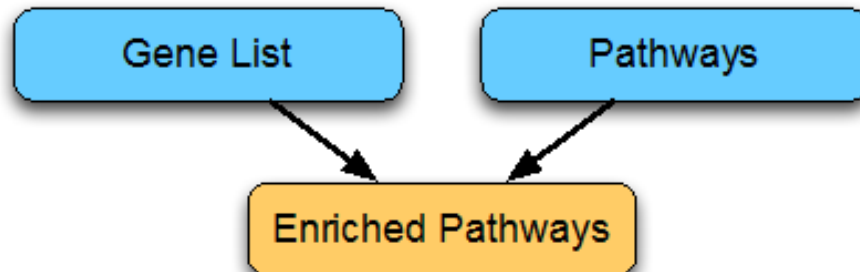
Types of Pathway Analysis



Analysis of *thresholded* lists with
Enrichment Analysis
(also called Overrepresentation A.)

Over-representation analysis

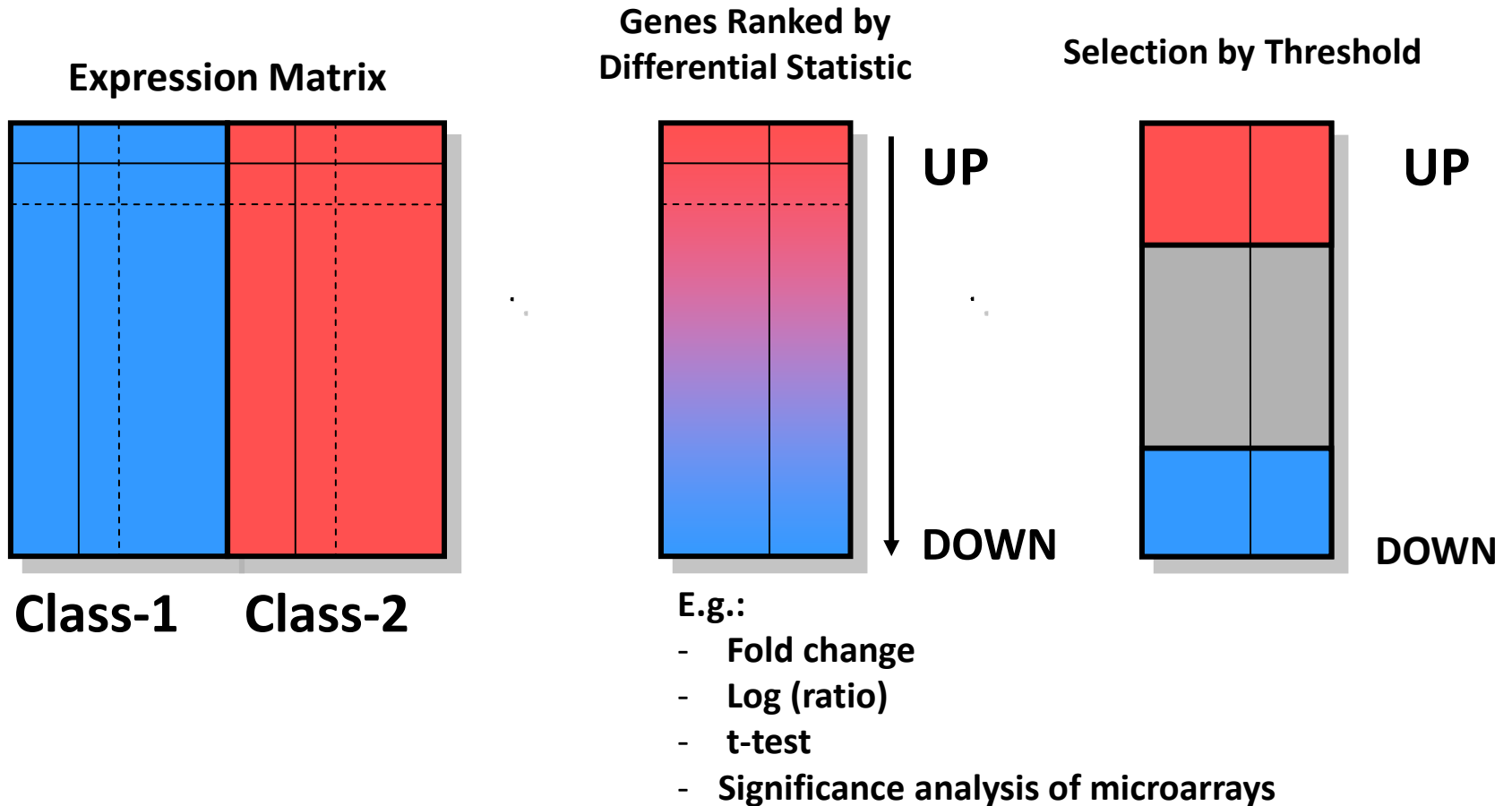
- Combines
 - Gene (feature) lists \leftarrow (Gen)omic experiment
 - Pathways and other gene annotations
 - Gene Ontology
 - Reactome
 - Pathway commons



Over-representation analysis

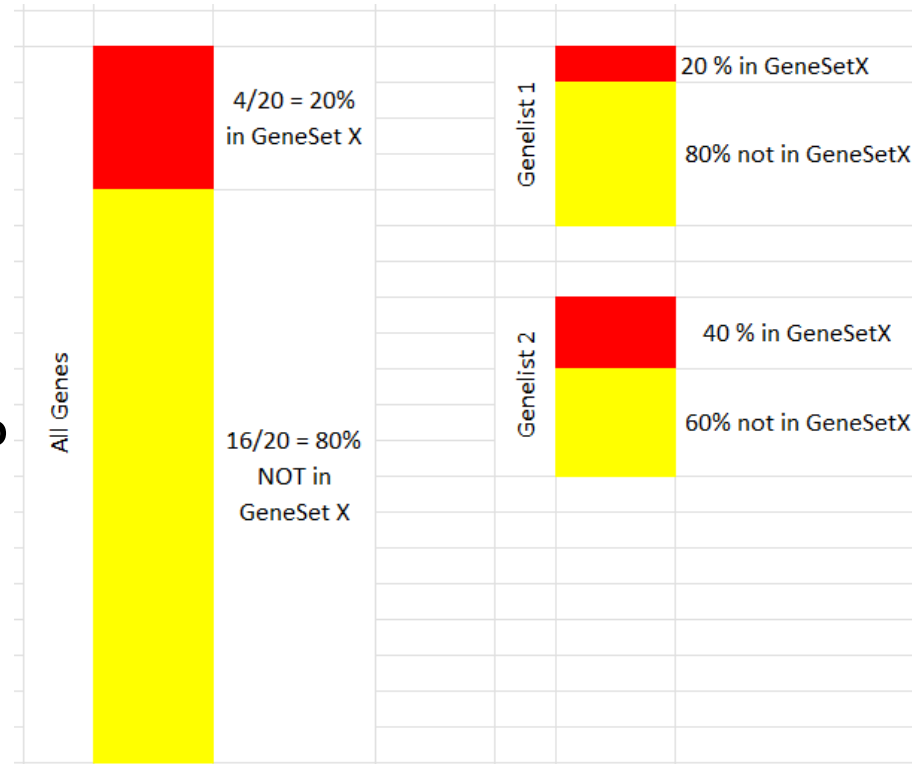
- Given:
 1. Gene list: e.g. RRP6, MRD1, RRP7, RRP43, RRP42 (yeast)
 2. Gene sets or annotations: e.g. Gene ontology, transcription factor binding sites in promoter
- Question: *Are any of the gene annotations surprisingly enriched in the gene list?*
- Details:
 1. Where do the gene lists come from?
 2. How to assess “surprisingly” (statistics)
 3. How to adjust for test multiplicity?

Obtaining the gene lists



Assessing “surprisingly”

- Given a gene list, “gl”, and a gene set, “GS”, check:
- Is the % of genes in “gl” annotated in “GS” the same as the % of genes globally annotated in “GS”?
 - If both percentages are similar --> *No Enrichment*
 - If the % of genes annotated in “GS” is greater in “gl” than in the rest of genes --> *“gl” is enriched in “GS”*



Examples

	Differentially expressed (gl_1)	Not differentially expressed	TOTAL
In Gene Set (GS1)	10	30	40
Not In Gene Set	390	3570	3960
TOTAL	400	3600	4000
% of gl_1 in GS1	$10/400=0.025$	$30/3600=0.00833$	

$0.025 \gg 0.00833$: “ gl_1 ” is enriched in “GS₁”

	Differentially expressed (gl_2)	Not differentially expressed	TOTAL
In Gene Set (GS2)	10	30	40
Not In Gene Set	390	1220	1610
TOTAL	400	1500	1650
% of gl_2 in GS ₂	$10/400=0.025$	$30/1500=0.02$	

$0.025 \approx 0.02$: Can't say that “ gl_2 ” is enriched in “GS₂”

Assessing significance: Fisher test

- The examples shows two cases
 - One where percentages are quite different
 - Another where percentages are similar
- How can we set a threshold to decide that the difference is “big enough” to call it “Enriched”
 - Use Fisher Test or, equivalently,
 - a test to compare proportions or
 - a hypergeometric test.

Assessing significance: Fisher test (1)

```
> GOnnnnnCounts<- matrix(c(10, 30, 390, 3570),
+       nrow = 2, byrow=TRUE,
+       dimnames = list(GeneSet = c("In Gene Set", "Not in Gene Set"),
+       Test =c("Differentially expressed", "Not Dif. Expr.")))
> GOnnnnnCounts
```

GeneSet	Test	
	Differentially expressed	Not Dif. Expr.
In Gene Set	10	30
Not in Gene Set	390	3570

```
> fisher.test(GOnnnnnCounts, alternative = "greater")
```

Fisher's Exact Test for Count Data

```
data: GOnnnnnCounts
p-value = 0.004836
alternative hypothesis: true odds ratio is greater than 1
95 percent confidence interval:
 1.508343      Inf
sample estimates:
odds ratio
 3.049831
```

P-value small, odds-ratio high → List is *surprisingly* enriched in Gene Set

Assessing significance: Fisher test (2)

```
> GOnnnnnCounts<-matrix(c(10,30,390,1220), nrow=2, byrow=TRUE,
+                         dimnames=list(
+                           GeneSet=c("In Gene Set", "Not in Gene Set"),
+                           Test=c("Diff.expressed", "Not diff.expr.")))
> GOnnnnnCounts
```

	Test	
GeneSet	Diff.expressed	Not diff.expr.
In Gene Set	10	30
Not in Gene Set	390	1220

```
> fisher.test(GOnnnnnCounts, alternative="greater")

      Fisher's Exact Test for Count Data

data:  GOnnnnnCounts
p-value = 0.517
alternative hypothesis: true odds ratio is greater than 1
95 percent confidence interval:
 0.5149828      Inf
sample estimates:
odds ratio
 1.042711
```

P-value not small, odds-ratio approx. 1 : List is not *surprisingly* enriched in Gene Set



Recipe for gene list enrichment test

- **Step 1:** Define **gene list** (e.g. thresholding analyzed list) and **background list**,
- **Step 2:** Select gene sets to test for enrichment,
- **Step 3:** Run enrichment tests and correct for multiple testing, if necessary,
- **Step 4:** Interpret your enrichments
- **Step 5:** Publish! ;)

Possible problems with gene list tests

- No “natural” value for the threshold
- Possible loss of statistical power due to thresholding
 - No resolution between significant signals with different strengths
 - Weak signals neglected
- Different results at different threshold settings
- Based on the wrong assumption of independent gene (or gene group) sampling, which increases false positive predictions

An example of ORA using Bioconductor (1)

```
# Get Genelist and expression marix
topTabAvsB <- read.table ("datasets/Top_AvsB.csv2", head=T, sep=";", dec=".", row.names=1)
expresAvsB <- read.table ("datasets/expres_AvsB.csv2", head=T, sep=";", dec=".", row.names=1)

# Define Gene list using arbitrary though reasonable cutoffs
probesUniverse <- rownames(topTabAvsB)
whichGenesInTop<- topTab["adj.P.Val"]<0.05 & topTab["logFC"] > 1
# Annotate Gene Universe and Gene list
entrezUniverse<- select(hgu133a.db, probesUniverse, "ENTREZID")
entrezUniverse <- entrezUniverse$ENTREZID
topGenes <- entrezUniverse[whichGenesInTop]
entrezUniverse <- entrezUniverse[!duplicated(entrezUniverse)]
topGenes <- topGenes[!duplicated(topGenes)]
```

An example of ORA using Bioconductor (2)

```
library(GOstats)
```

```
GOparams = new("GOHyperGParams",
```

```
    genelds=topGenes, universeGenelds=entrezUniverse,
```

```
    annotation="hgu133a.db", ontology="BP", pvalueCutoff=0.001)
```

```
GOhyper = hyperGTest(GOparams)
```

```
head(summary(GOhyper))
```

	GOBPID	Pvalue	OddsRatio	ExpCount	Count	Size	Term
1	GO:0019370	0.0000917494	31.294444	0.2904762	4	7	leukotriene biosynthetic process
2	GO:0046395	0.0004796855	3.282433	4.4816327	13	108	carboxylic acid catabolic process
3	GO:0016054	0.0005736863	3.213594	4.5646259	13	110	organic acid catabolic process
4	GO:0072329	0.0007287196	4.193992	2.4897959	9	60	monocarboxylic acid catabolic process
5	GO:0006691	0.0007580159	13.402381	0.4564626	4	11	leukotriene metabolic process
6	GO:0045109	0.0008510094	8.401076	0.7884354	5	19	intermediate filament organization

Analysis of ranked gene lists with
Gene Set Enrichment Analysis
(also called Functional Class Scoring)

Gene Sets

- A gene set
 - a group of genes with related functions.
 - sets of genes or pathways, for their association with a phenotype.
 - Examples: metabolic pathway, protein complex, or GO (gene ontology) category.
- Identified from a prior biological knowledge.
- May better reflect the true underlying biology.
- May be more appropriate units for analysis.

Gene Sets

Each row represents one gene set

	A	B	C	D	E	F	G
1	chr10q24	Cytogenetic band	PITX3	SPFH1	NEURL	C10orf12	NDUFB8
2	chr5q23	Cytogenetic band	ALDH7A1	IL13	8-Sep	IRF1	ACSL6
3	chr8q24	Cytogenetic band	HAS2	LRRC14	TSTA3	DGAT1	RECQL4
4	chr16q24	Cytogenetic band	RPL13	GALNS	FANCA	CPNE7	COTL1
5	chr13q14	Cytogenetic band	AKAP11	ARL11	ATP7B	C13orf1	C13orf9
6	chr7p21	Cytogenetic band	ARL4A	SCIN	GLCC1	SP8	SOSTDC1
7	chr10q23	Cytogenetic band	SNCG	FER1L3	C10orf116	HHEX	TNKS2
8	chr14q12	Cytogenetic band	C14orf125	FOXG1C	HECTD1	SCFD1	AP4S1
9	chr13q13	Cytogenetic band	ALG5	RFXAP	DCAMKL1	MAB21L1	STOML3
10	chr1p34	Cytogenetic band	JMJD2A	MRPS15	HIVEP3	GJB3	CDCA8
11	chr10q21	Cytogenetic band	MBL2	C10orf70	DNAJC12	BICC1	CXXC6

If editing in excel, watch out for its tendency to auto-format gene sets (SEP8 becomes 8-Sep)

First column are gene set names. Duplicates are not allowed

Second column contains a brief description. Its optional – you can fill in a dummy field (e.g. “na”)

Unequal lengths (i.e # of genes) is allowed

MSigDB Collection	Subcollection	No. Gene Sets
C1: positional gene sets		326
C2: curated gene sets	CGP: chemical and genetic perturbations	3402
	CP: Canonical pathways	1320
C3: motif gene sets	KEGG/Biocarta/REACTOME	
	MIR: microRNA targets	221
C4: computational gene sets	TFT: transcription factor targets	615
	CGN: cancer gene neighborhoods	427
	CM: cancer modules	431
C5: GO gene sets	BP: GO biological process	825
	CC: GO cellular component	233
	MF: GO molecular function	396
C6: oncogenic signatures		189
C7: immunologic signatures		1910
Total		10295

Gene Set (Enrichment) Analysis

- Mootha (2003) as an alternative to ORA.
- It aims to identify gene sets with *subtle but coordinated expression changes* that cannot be detected by ORA methods.
 - Weak changes in individual genes gathered to large gene sets can show a significant pattern.
- Results not affected by arbitrarily chosen cutoffs.
- It does not provide information as detailed as ORA

The GSEA method

- Original GSEA method is based on comparing, for each gene group, the distribution of the test statistic within the group with the overall distribution of those statistics, i.e. the calculated for all genes.
- To do this, test statistics are ranked (from biggest to smallest) and **for each gene set** a running sum is computed such that
 - If a gene is in the gene set add a certain quantity (moderate)
 - If a gene is not in the gene set, subtract a (small) quantity
- The distribution of the running sum is compared with that of the random walk using a Kolmogorov-Smirnov test (K-S test) statistic
- P-values are computed based on a randomization.



Calculating enrichment score (ES)

Create a running sum statistic based on the following

If gene p is not in set S , then add

$$X_i = -\sqrt{\frac{N_S}{N - N_S}}$$

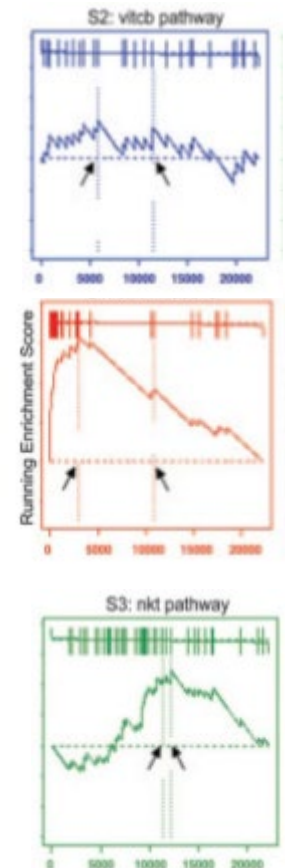
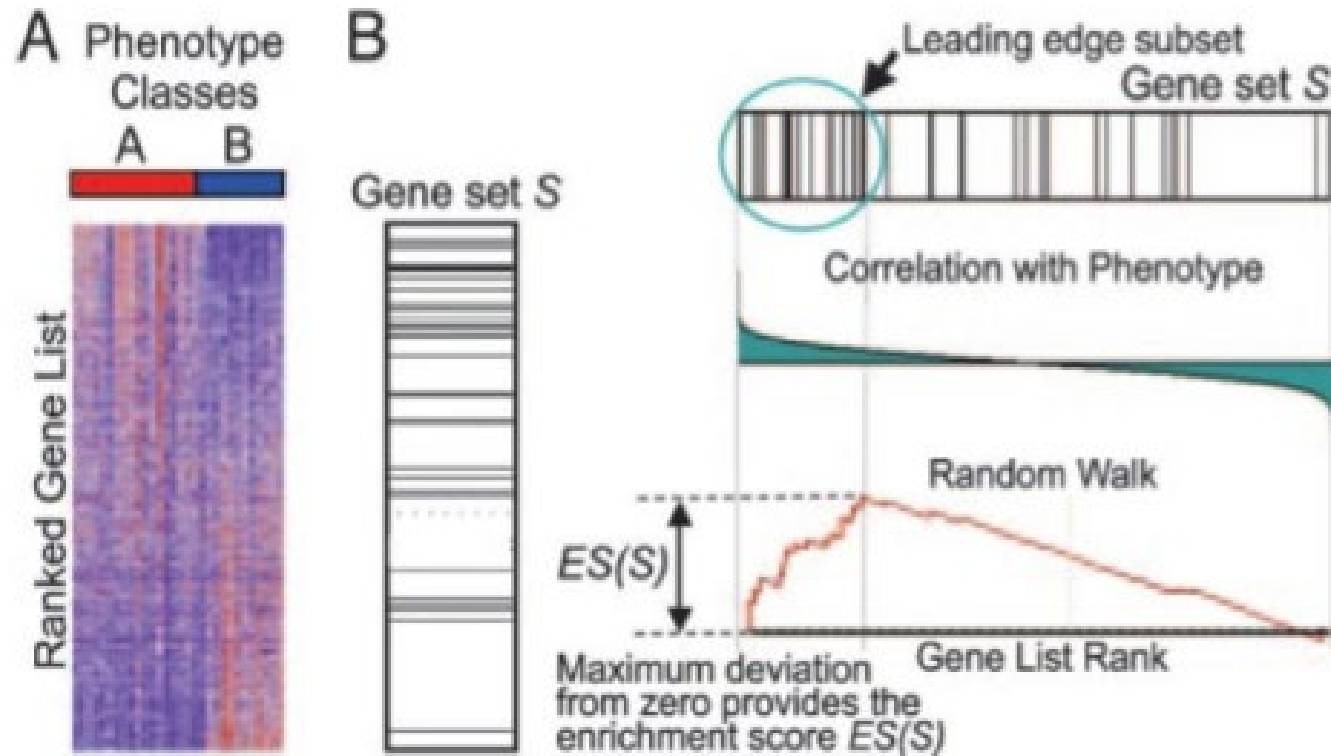
If gene p is in set S , then add

$$X_i = \sqrt{\frac{N - N_S}{N_S}}$$

This creates a running sum

The maximum sum over the whole list L is the Enrichment Score
MES

The GSEA method





Recipe for ranked list enrichment test

- **Step 1:** Rank ALL your genes,
- **Step 2:** Select gene sets to test for enrichment,
- **Step 3:** Run enrichment tests and correct for multiple testing, if necessary,
- **Step 4:** Interpret your enrichments
- **Step 5:** Publish! ;)

GSEA variants

- GSEA is not free from criticisms
 - Use of KS test
 - Null hypothesis is not clear
- Many alternative available
 - Efron's GSA
 - Limma's ROAST
 - Irizarry's simple GSA based on Wilcoxon...

Multiple test adjustments

Why we need to “adjust”

- We use a statistical test to decide if a gene list is “surprisingly” enriched in a Gene Set.
 - We use “surprisingly” instead of “significantly”
- Remember that when doing statistical tests one can be right or wrong differently.
 - Right
 - Rejecting the null hypothesis (H_0) when it is false
 - Not rejecting H_0 when it is true
 - Wrong
 - Rejecting the null hypothesis (H_0) when it is true
 - Not rejecting H_0 when it is false

Errors and Successes in tests: Type I and type II errors

Actual Situation “Truth”		
		Decision
H₀ True	H₀ False	
Do Not Reject H₀	Correct Decision $1 - \alpha$	Incorrect Decision Type II Error β
Rejct H₀	Incorrect Decision Type I Error α	Correct Decision $1 - \beta$

$$\alpha = P(\text{Type I Error}) \quad \beta = P(\text{Type II Error})$$

Testing repeatedly

- Omics studies are “high throughput”
 - Selecting genes: One test per each gene
 - Finding enriched gene sets: One test per each gene set
- Doing many tests means facing repeatedly the probability of making one false positive.
 - As the number of tests increases →
 - The chance of observing at least one false positive is going to increase too.

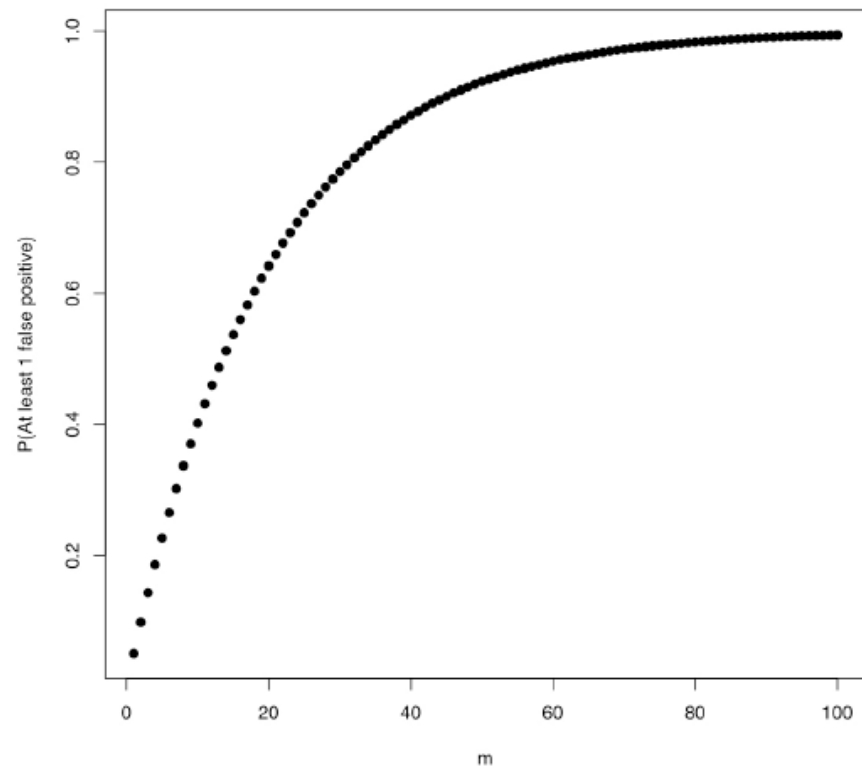
Why multiple testing matters

- The probability of observing one false positive if testing once is:
 - $P(\text{Making a type I error}) = \alpha$
 - $P(\text{not making a type I error}) = 1 - \alpha$
- Now imagine we perform m tests independently
 - $P(\text{not making a type I error in } m \text{ tests}) = (1 - \alpha)^m$
 - $P(\text{making at least a type I error in } m \text{ tests}) = 1 - (1 - \alpha)^m$
- As m increases the probability of having at least one type error tends to increase

Type I error not useful in multiple testing

Probability of At Least 1 False Positive

Number of tests: m	P(making at least a type I error) = $1-(1-\alpha)^m$
1	0.050000
2	0.097500
3	0.142625
4	0.185494
5	0.226219
6	0.264908
7	0.301663
8	0.336580



How can we deal with this issue?

- Controlling for type I error is not feasible if many tests.
- Idea: Modify α (or alternatively the p-value) so the error probability is ***controlled overall***
- This may mean different things:
 1. The probability of *at least one error* in m tests is $< \alpha$
 2. The expected number of false positives is below a fixed threshold.
- ...

Controlling the FWER: *Bonferroni*

If M = # of annotations tested:

Adjusted P-value = $M \times$ original P-value

Adjusted P-value is greater than or equal to the probability that ***one or more of the observed enrichments*** are due to random draws.

The jargon for this correction is “controlling for the *Family-Wise Error Rate (FWER)*”

Bonferroni correction caveats

- Bonferroni correction is very stringent and can “wash away” real enrichments leading to false negatives,
- Often one is willing to accept a less stringent condition, the “false discovery rate” (FDR), which leads to a gentler correction when there are real enrichments.

False discovery rate (FDR)

- FDR is *the expected **proportion** of “False Positives” that is of the observed enrichments due to random chance.*
- Compare to Bonferroni correction which is a bound on *the probability that **any one** of the observed enrichments could be due to random chance.*
- Typically, FDR adjustments are calculated using the Benjamini-Hochberg procedure.
- FDR threshold is often called the “q-value”

Benjamini-Hochberg example I

Rank	Category	(Nominal) P-value
1	<i>Transcriptional</i>	0.001
2	<i>regulation</i>	0.002
3	<i>Transcription factor</i>	0.003
4	<i>Initiation of</i>	0.0031
5	<i>transcription</i>	0.005
...	<i>Nuclear localization</i>	...
	<i>Chromatin modification</i>	
52	...	0.97
53	<i>Cytoplasmic localization</i>	0.99
	<i>Translation</i>	

Sort P-values of all tests in decreasing order

Benjamini-Hochberg example II

Rank	Category	(Nominal) P-value	Adjusted P-value
1	<i>Transcriptional regulation</i>	0.001	0.001 x 53/1 = 0.053
2	<i>Transcription factor</i>	0.002	0.002 x 53/2 = 0.053
3	<i>Initiation of transcription</i>	0.003	0.003 x 53/3 = 0.053
4	<i>Nuclear localization</i>	0.0031	0.0031 x 53/4 = 0.040
5	<i>Chromatin modification</i>	0.005	0.005 x 53/5 = 0.053
...
52	<i>Cytoplasmic localization</i>	0.97	0.985 x 53/52 = 1.004
53	<i>Translation</i>	0.99	0.99 x 53/53 = 0.99

Adjusted P-value is “nominal” P-value times # of tests divided by the rank of the P-value in sorted list: $AdjP\text{-value} = P\text{-value} \times [\# \text{ of tests}] / Rank$

Benjamini-Hochberg example III

Rank	Category	(Nominal) P-value	Adjusted P-value	FDR / Q-value
1	<i>Transcriptional regulation</i>	0.001	0.001 x 53/1 = 0.053	0.040
2	<i>Transcription factor</i>	0.002	0.002 x 53/2 = 0.053	0.040
3	<i>Initiation of transcription</i>	0.003	0.003 x 53/3 = 0.053	0.040
4	<i>Nuclear localization</i>	0.0031	0.0031 x 53/4 = 0.040	0.040
5	<i>Chromatin modification</i>	0.005	0.005 x 53/5 = 0.053	0.053
...
52	<i>Cytoplasmic localization</i>	0.97	0.985 x 53/52 = 1.004	0.99
53	<i>Translation</i>	0.99	0.99 x 53/53 = 0.99	0.99

Adjusted P-value is “nominal” P-value times # of tests divided by the rank of the P-value in sorted list: $AdjP\text{-value} = P\text{-value} \times [\# \text{ of tests}] / Rank$

Q-value (or FDR) corresponding to a nominal P-value is the smallest adjusted P-value assigned to P-values with the same or larger ranks.

Benjamini-Hochberg example III

Rank	Category	P-value threshold for FDR < 0.05 (Nominal)		Adjusted P-value	FDR / Q-value
		P-value			
1	<i>Transcriptional regulation</i>	0.001		0.001 x 53/1 = 0.053	0.040
2	<i>Transcription factor</i>	0.002		0.002 x 53/2 = 0.053	0.040
3	<i>Initiation of transcription</i>	0.003		0.003 x 53/3 = 0.053	0.040
4	<i>Nuclear localization</i>	0.0031		0.0031 x 53/4 = 0.040	0.040
5	<i>Chromatin modification</i>	0.005		0.005 x 53/5 = 0.053	0.053
...
				Red: non-significant	
				Green: significant at FDR < 0.05	
52	<i>Cytoplasmic localization</i>	0.97		0.985 x 53/52 = 1.004	0.99
53	<i>Translation</i>	0.99		0.99 x 53/53 = 0.99	0.99

Adjusted P-value is “nominal” P-value times # of tests divided by the rank of the P-value in sorted list: $AdjP\text{-value} = P\text{-value} \times [\# \text{ of tests}] / Rank$

Q-value (or FDR) corresponding to a nominal P-value is the smallest adjusted P-value assigned to P-values with the same or larger ranks.

P-value threshold is highest ranking P-value for which corresponding Q-value is below desired significance threshold

Reducing adjustment stringency

- The adjustment to the P-value threshold depends on the # of tests that you do,
- So, no matter what, *the more tests you do, the more sensitive the test needs to be*
- Can control the stringency by ***reducing the number of tests:***
 - Don't use all collections of Gene Sets available
 - Restrict testing to the appropriate GO annotations;
 - Filter gene sets by size

Summary

- Pathway Analysis is a useful approach to help gain biological understanding from omics-based studies.
- There are many ways, many methods, many tools
- Choice of the method should be guided by
 - a combination of availability, ease of use and usefulness ,
 - Usually obtained from a good understanding of how it
- Different methods may yield different results
 - Worth checking!

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