## Inductive Types II: Examples

CAS CS 320: Principles of Programming Languages

Thursday, February 8, 2024

# Administrivia

- Homework 2 is due today by 11:59 pm.
- Homework 3 is posted today and due on Thursday, Feb 15, by 11:59 pm.

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# Reading Assignment

- OCP, Section 3.9.5, 3.9.7: Algebraic Data Types
- OCP, Section 3.11: Trees

## recursive variant types (OCP 3.9.4)

instead of using type constructor **list** to define intlist1, as in:

```
type intlist1 = int list ;;
let rec sum1 (lst : intlist1) : int =
  match lst with
  | [] -> 0
  | h :: t -> h + sum1 t
```

### recursive variant types (OCP 3.9.4)

instead of using type constructor list to define intlist1, as in:

```
type intlist1 = int list ;;
let rec sum1 (lst : intlist1) : int =
   match lst with
   | [] -> 0
   | h :: t -> h + sum1 t
```

we can use recursive variant types, as in:

```
type intlist2 = Nil | Cons of int * intlist2
let rec sum2 (lst : intlist2) : int =
  match lst with
  | Nil -> 0
  | Cons (h, t) -> h + sum2 t
```

### parametrized recursive variant types(OCP 3.9.5)

instead of recursive variant types, as in:

```
type intlist2 = Nil | Cons of int * intlist2
let rec length2 (lst : intlist2) : int =
  match lst with
  | Nil -> 0
  | Cons (_, t) -> 1 + length2 t
```

#### parametrized recursive variant types(OCP 3.9.5)

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type intlist2 = Nil | Cons of int * intlist2
let rec length2 (lst : intlist2) : int =
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```

we can use parametrized recursive variant types, as in:

```
type 'a mylist = Nil | Cons of 'a * 'a mylist
let rec length3 (lst : 'a mylist) : int =
  match lst with
  | Nil -> 0
  | Cons (_, t) -> 1 + length3 t
```

# types with polymorphic variants (OCP 3.9.6)

Skip - this section is not part of the posted schedule.

# built-in parametrized recursive variant types(OCP 3.9.7)

OCaml's list datatype is an example of a built-in parametrized recursive variant type, defined as follows:

```
type 'a list = [] | ( :: ) of 'a * 'a list
```

Note how our definition of 'a mylist (two slides earlier) mimics that of 'a list.

# built-in parametrized recursive variant types(OCP 3.9.7)

OCaml's list datatype is an example of a built-in parametrized recursive variant type, defined as follows:

```
type 'a list = [] | ( :: ) of 'a * 'a list
```

Note how our definition of 'a mylist (on the previous slide) mimics that of 'a list.

Another of Ocaml's built-in parametrized (non-recursive) variant types is the option datatype:

```
type 'a option = None | Some of 'a
```

once again, user-defined 'a mylist followed by 'a tree:

```
type 'a mylist =
  | Nil
  | Cons of 'a * 'a mylist
type 'a tree =
  | Leaf
  | Node of 'a * 'a tree * 'a tree
```

once again, user-defined 'a mylist followed by 'a tree:

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```

function preord constructs a list of tree nodes in preorder:

```
let rec myapp (l1 : 'a mylist) (l2 : 'a mylist) : 'a mylist =
  match l1 with
  | Nil -> l2
  | Cons (hd,tl) -> Cons (hd, myapp tl l2)
let rec preord (t : 'a tree) : 'a mylist =
  match t with
  | Leaf -> Nil
  | Node (x,lt,rt) -> Cons(x, myapp (preord lt) (preord rt))
```

once again, user-defined 'a mylist followed by 'a tree:

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type 'a mylist =
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  | Cons of 'a * 'a mylist
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function postord constructs a list of tree nodes in postorder:

```
let rec myapp (l1 : 'a mylist) (l2 : 'a mylist) : 'a mylist =
  match l1 with
  |Nil -> l2
  |Cons (hd,tl) -> Cons (hd, myapp tl l2)
let rec postord (t : 'a tree) : 'a mylist =
  match t with
  |Leaf -> Nil
  |Node(x,lt,rt) -> myapp(myapp(preord lt)(preord rt)))(Cons(x,Nil))
```

using record types to represent binary trees:

```
type 'a tree = Leaf | Node of 'a node
and 'a node = {value : 'a; left : 'a tree; right : 'a tree}
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membership mem function using record-type representation:

```
(* (mem x t) is true/false x is/is not a value in t. *)
let rec mem x = function
   |Leaf -> false
   |Node {value; left; right} -> value = x || mem x left || mem x right
```

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