# ACM TEMPLATE



UESTC\_Jungle

Last build at October 24, 2018

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#### 1 Datastructure

#### 1.1 Fenwick

```
//* Fenwick Tree (Binary Indexed Tree), by Abreto <m@abreto.net>. */
 2
   #include <cstring>
 3
 4
   using namespace std;
 5
   template <class T = int, int MAXN = 100001>
 6
 7
   struct fenwick {
 8
      static inline int lowbit(int x) {
 9
        return (x&(-x));
10
11
      int N;
12
      T f[MAXN]; /* 1=based. */
13
      fenwick(void):N(MAXN) {
14
        init();
15
16
      fenwick(int n):N(n) {
17
        init();
18
19
      void init(void) {
20
        memset(f,0,sizeof(f));
21
      void upd(int i, T dx) {
22
        while(i <= N) {</pre>
23
24
          f[i] += dx;
25
          i += lowbit(i);
        }
26
27
      T sum(int i) {
28
29
        T ret = 0;
30
        while(i) {
31
          ret += f[i];
32
          i -= lowbit(i);
33
34
        return ret;
35
      }
36
   |};
   /* Fenwick Tree (Binary Indexed Tree), by Abreto <m@abreto.net>. */
 2
 3
   #define MAXN 100001
 4
   #define LOWBIT(x)
                         ((x)&(-(x)))
 5
 6
   int N;
 7
   int fen[MAXN];
 8
 9
   void update(int i, int dx) {
10
      while(i <= N) {</pre>
        fen[i] += dx;
11
12
        i += LOWBIT(i);
13
14
15
16
   int sum(int i) {
      int s = 0;
17
18
      while(i > 0) {
19
        s += fen[i];
20
        i -= LOWBIT(i);
21
22
      return s;
23 |}
```

#### 1.2 BST in pb\_ds

```
/* Red_Black tree via pb_ds. */
   #include<bits/stdc++.h>
   #include<ext/pb_ds/assoc_container.hpp>
   #include<ext/pb_ds/tree_policy.hpp>
 5
   using namespace __gnu_pbds;
 6
   using namespace std;
 7
   template <typename T>
 8
   using ordered_set = tree<T, null_type, less<T>, rb_tree_tag,
       tree_order_statistics_node_update>;
 9
10
   int main() {
11
     ordered_set<int> s;
12
     s.insert(1);
13
     s.insert(3);
     cout << s.order_of_key(2) << endl; // the number of elements in the s less than 2
14
     cout << *s.find_by_order(0) << endl; // print the 0-th smallest number in s(0-based
15
16
```

#### 1.3 Segment Tree

```
1
   //* Segment tree (Interval tree, range tree), by Abreto <m@abreto.net>. */
 2
 3
    template <int STMAX = 1000000>
 4
    struct segment_tree {
 5
      struct node_t {
 6
        static inline node_t merge(node_t n1, node_t n2) {
 7
          node_t ans;
 8
          ans.l = n1.l;
 9
          ans.r = n2.r;
10
          /* merge n1 and n2 to ans. */
11
          return ans;
12
        }
13
14
        /* Data field */
15
        int l,r:
16
      } nodes[(STMAX+1)<<2];</pre>
17
18
      struct lazy_t {
        int marked; /* Optional */
19
20
        /* lazy mark. */
21
22
        lazy_t(void) {
23
          clear();
24
25
        void clear(void) {
26
          marked=0;
27
28
      } marks[(STMAX+1)<<2];</pre>
29
30
      inline void maintain_leaf(int o, int idx) {
31
        nodes[o].l = nodes[o].r = idx;
32
        /* Operations to single elements ... */
33
34
      inline void maintain(int o) {
35
        nodes[o] = node_t::merge(nodes[o<<1], nodes[o<<1|1]);</pre>
36
      }
37
38
      /* Usage: build(1,1,n); */
39
      void build(int o, int l, int r) \{ /* [l,r] */
```

```
40
         if( r <= l ) {
 41
           maintain_leaf(o, 1);
 42
         } else {
 43
           int mid = 1+r>>1;
 44
           build(o<<1, 1, mid);
           build(o<<1|1, mid+1, r);
 45
 46
           maintain(o);
 47
       }
 48
 49
 50
       /* Modify all elements in [l,r] */
 51
       void mark(lazy_t act, int o) {
 52
         /* do something .. */
 53
         marks[o].marked = 1;
 54
 55
 56
       /* Pass cached updates. */
 57
       void pushdown(int o) {
 58
         if( marks[o].marked ) {
 59
           mark(marks[o], o<<1);</pre>
 60
           mark(marks[o], o<<1|1);
 61
           marks[o].clear();
 62
 63
       }
 64
 65
       /* Do act on all elements in [L,R] */
 66
       void upd(int L, int R, lazy_t act, int o, int l, int r) {
 67
         if( L <= 1 && r <= R ) {
 68
           mark(act, o);
         } else if (L <= R) {</pre>
 69
           int mid = (l+r)>>1;
 70
 71
           pushdown(o);
           if( L <= mid ) upd(L, R, act, o<<1, l, mid);
 72
 73
           if( R > mid ) upd(L, R, act, o<<1|1, mid+1, r);
 74
           maintain(o);
 75
 76
       }
 77
 78
       node_t qry(int L, int R, int o, int l, int r) {
 79
         if(L \le 1 \& r \le R)
 80
           return nodes[o];
 81
         else if (L \ll R) {
 82
           int mid = (l+r)>>1;
 83
           pushdown(o);
 84
           if(R <= mid) return qry(L,R,o<<1,l,mid);</pre>
 85
           if(L > mid) return qry(L,R,o<<1|1,mid+1,r);
 86
           return node_t::merge(qry(L,R,o<<1,l,mid),qry(L,R,o<<1|1,mid+1,r));</pre>
 87
         }
 88
       }
 89
 90
       int N;
 91
 92
       segment_tree(void):N(STMAX) {}
93
       segment_tree(int n):N(n) {}
 94
       void build(int n) {
 95
         N = n;
 96
         build(1,1,N);
 97
       }
 98
       void update(int L, int R, lazy_t act) {
 99
         upd(L,R,act,1,1,N);
100
       node_t query(int L, int R) {
101
102
         return qry(L,R,1,1,N);
103
       }
```

```
104 | };
    |/* Segment tree (Interval tree, range tree), by Abreto <m@abreto.net>. */
  1
  3
    #define MAXN
                      1000001
  4
  5
     typedef struct {
       int l,r;
  6
       /* Data field */
  7
  8
    } node_t;
  9
 10
    node_t merge(node_t n1, node_t n2) {
 11
       node_t ans;
 12
       ans.l = n1.l;
 13
       ans.r = n2.r;
 14
       /* merge n1 and n2 to ans. */
 15
       return ans;
 16
    }
 17
     typedef struct {
 18
 19
       int marked; /* Optional */
 20
       /* lazy mark. */
 21
    } lazy_t;
 22
 23
    int A[MAXN];
 24
    node_t nodes[MAXN<<2];</pre>
 25
    lazy_t marks[MAXN<<2];</pre>
 26
 27
    void maintain_leaf(int o, int idx) {
 28
       nodes[o].l = nodes[o].r = idx;
 29
       /* Operations to single elements ... */
 30
 31
    void maintain(int o) {
       nodes[o] = merge(nodes[o << 1], nodes[o << 1|1]);
 32
 33
    }
 34
 35
     /* Usage: build(1,1,n); */
 36
    void build(int o, int l, int r) { /* [l,r] */
 37
       if( r <= l ) {
 38
         maintain_leaf(o, 1);
 39
       } else {
 40
         int mid = 1+r>>1;
 41
         build(o<<1, 1, mid);
         build(o<<1|1, mid+1, r);
 42
 43
         maintain(o);
 44
 45
       marks[o].marked = 0;
 46
 47
 48
    /* Modify all elements in [l,r] */
 49
    void mark(lazy_t act, int o) {
       /* do something .. */
 50
 51
       marks[o].marked = 1;
 52
 53
 54
    /* Pass cached updates. */
 55
    void pushdown(int o) {
 56
       if( marks[o].marked ) {
 57
         mark(marks[o], o<<1);</pre>
 58
         mark(marks[o], o<<1|1);
 59
         marks[o].marked = 0;
 60
       }
    }
 61
 62
```

```
63
   /* **DISCARDED** */
64
   /* Set A[p]=v. Usage: modify(p, v, 1, 1, n);
65
   void modify(int p, int v, int o, int l, int r)
66
        if(r-1 < 2)
67
68
69
            maintain_leaf(o, v);
70
        } else {
71
            int mid = (1+r)/2;
72
            pushdown(o);
73
            if( p \le mid ) modify(p, v, o*2, l, mid);
74
            else modify(p, v, o*2+1, mid, r);
75
            maintain(o);
76
   }*/
77
78
79
   /* Do act on all elements in [L,R] */
80
   void update(int L, int R, lazy_t act, int o, int l, int r) {
81
      if( L <= 1 && r <= R ) {
82
        mark(act, o);
83
      } else if (L <= R) {</pre>
84
        int mid = (l+r)>>1;
85
        pushdown(o);
86
        if( L <= mid ) update(L, R, act, o<<1, l, mid);</pre>
87
        if( R > mid ) update(L, R, act, o<<1|1, mid+1, r);
88
        maintain(o);
89
      }
90 | }
   1.4 Sparse Table
   |/* RMQ with Sparse Table, by Abreto <m@abreto.net>. */
 1
 2
 3
   int min(int a, int b) {
 4
      return (a<b)?a:b;
 5
 6
 7
   #define MAXN
                     100001
 8
   #define MAXLOG 32
 9
10
    int N;
11
   int A[MAXN];
                   /* indexed from 0. */
12
   int st[MAXN][MAXLOG];
13
    void st_init() {
14
      int i = 0, j = 0, t = 0;
for(i = 0; i < N; ++i) st[i][0] = A[i];
15
16
17
      for(j = 1; (t=(1<< j)) <= N; ++j)
        for(i = 0; (i+t-1) < N; ++i)
18
19
          st[i][j] = min(st[i][j-1], st[i+(t>>1)][j-1]);
20
      /* st(i,j) = min(st(i,j-1), st(i+2^(j-1),j-1)). */
21
22
23
   int st_query(int l, int r) {
24
      int k = 0;
25
      while((1 << (k+1)) <= (r-l+1)) k++;
26
      return min(st[l][k], st[r-(1<k)+1][k]);
27 |}
```

#### 1.5 Treap

```
|#include <bits/stdc++.h>
 1
 2
 3
   using namespace std;
 5
   #define MAXN (2560000)
 6
 7
   int __treap_mem[MAXN];
 8
   void init_treap_mem(void) {
9
      for( int i = 1; i < MAXN; i++)
10
       \_treap\_mem[i-1] = i;
11
12
   int alloc_address(void) {
13
     int ret = __treap_mem[0];
14
      __treap_mem[0] = __treap_mem[ret];
15
      return ret;
16
17
   void free_address(int p) {
18
     _{\text{treap\_mem}[p]} = _{\text{treap\_mem}[0]};
19
      \_treap_mem[0] = p;
20
21
22
   typedef int key_t;
23
   typedef int val_t;
24
   struct treap {
25
     key_t x;
26
     val_t v;
27
               /* random priority */
     int r;
     int eq, s; /* number of equal ones, size of subtree (include root itself) */
28
     treap *fa; /* point to its father */
29
     treap *ch[2]; /* 0 for left child, 1 for right child. */
30
31
32
     treap(void);
33
     inline void maintain(void); /* update s */
34
     inline void set_child(int d, treap *child);
35
     inline int which(void); /* determine which child this is of its father */
36
     inline int cmp(key_t ox); /* determine which child to insert ox */
37
     treap *rotate(void); /* rotate this to its father, return this */
38
   } treap_nodes[MAXN];
39
40
   treap *new_treap(key_t x, val_t v, treap *f) {
41
     treap *ret = treap_nodes + alloc_address();
42
      ret->x = x;
43
      ret -> v = v;
44
      ret->eq = ret->s = 1;
45
      ret->fa=f;
46
      ret->ch[0] = ret->ch[1] = NULL;
47
48
   void free_treap(treap *p) {
49
      free_address( p - treap_nodes );
50
51
   void treap_clear(void) {
52
     init_treap_mem();
53
54
55
   treap::treap(void) {
56
     r = rand();
57
     eq = s = 0;
58
     fa = ch[0] = ch[1] = NULL;
59
60
   inline void treap::maintain(void) {
61
      s = eq;
     for( int i = 0 ; i < 2 ; i++ )
62
63
       if( ch[i] )
64
          s += ch[i]->s;
```

```
65
 66
    inline void treap::set_child(int d, treap *child) {
 67
       ch[d] = child;
 68
       maintain();
 69
       if( child ) child->fa = this;
 70
 71
    inline int treap::which(void) {
 72
       if( NULL == fa ) return -1; /* this is not a child */
 73
       else return ( fa->ch[1] == this );
 74
 75
    inline int treap::cmp(key_t ox) {
 76
       if( ox == x ) return -1; /* equal */
 77
       else return ( ox > x ); /* left less, right more */
 78
 79
     treap *treap::rotate(void) {
 80
       if ( NULL == fa ) return this; /* no father, already global root. */
       int d = which();
 81
 82
       fa->set_child(d, ch[d^1]);
 83
       set_child(d^1, fa);
 84
       return this;
 85
 86
 87
     // --- deprecated |
 88
    typedef int T;
 89
 90
    struct node {
91
       T v; /* value of this node */
 92
       int r; /* random priority */
 93
       int eq; /* the number of equal things */
 94
       int s; /* the size of subtree rooted at this */
       node *ch[2]; /* 0 for left child, 1 for right child. */
 95
       node(void) {
 96
 97
         r = rand();
 98
         ch[0] = ch[1] = NULL;
 99
100
      /* return where to insert x */
101
       int cmp(T x) {
102
         if(v == x) return -1;
103
         else return (x < v) ? 0 : 1;
104
105
       /* return 1 if this node is prior to other */
106
       int pri(node *o) {
107
         return (r > (o->r));
108
109
       /* maintain the s field */
110
       void maintain(void) {
111
         s = eq;
112
         if(NULL != ch[0]) s += ch[0]->s;
113
         if(NULL != ch[1]) s += ch[1]->s;
      }
114
115
116
117
     /* move o to ch[d] of o->ch[d^1] */
118
    void rotate(node *&o, int d) {
       node *k = o\rightarrow ch[d^1];
119
120
       o\rightarrow ch[d^1] = k\rightarrow ch[d];
121
       o->maintain();
122
       k\rightarrow ch[d] = o;
123
       k->maintain();
124
       o = k;
125
```

#### 1.6 Leftist Heap

```
|/* HDU 1512 Monkey King(左偏树模板题) */
   #include<iostream>
3
   #include<cstdio>
4
   using namespace std;
5
   const int maxn = 100000+5;
6
7
   int n, m;
8
9
   struct Heap {
10
     int l,r,fa,val,dis;
11
   } t[maxn];
12
13
   int finds(int x) {
14
15
     return t[x].fa == -1? x:t[x].fa = finds(t[x].fa);
16
   }
17
   int merge(int x, int y) {
18
                            //如果为0的话,就说明是空子树,根节点当然就是另一节点了
19
     if(x == 0) return y;
     if(y == 0) return x;
20
21
     if(t[y].val>t[x].val)
                          swap(x,y); //始终往右子树进行插入
22
     t[x].r = merge(t[x].r,y);
23
     t[t[x].r].fa = x;
24
     if(t[t[x].l].dis < t[t[x].r].dis) swap(t[x].l,t[x].r); //是否需要左右子树的对换,
        这样是为了右子树尽量短
25
     if(t[x].r == 0) t[x].dis = 0;
                                   //距离的重新分配
26
     else t[x].dis = t[t[x].r].dis + 1;
27
     return x;
   }
28
29
30
   int pop(int &root) {
31
     int l = t[root].l;
32
     int r = t[root].r;
33
     t[root].l = t[root].r = t[root].dis = 0;
34
     t[root].fa = -1;
35
     t[1].fa = t[r].fa = -1; //删除root根节点
     return merge(l,r);
36
                             //这样一来相当于分裂成了两棵子树,重新进行合并,最后返回值
        为合并后的根节点
37
38
39
   int push(int x, int y) {
40
     return merge(x,y);
41
42
43
   int main() {
     //freopen("in.txt","r",stdin);
44
45
     while(~scanf("%d",&n)) {
46
       for(int i=1; i<=n; i++) {
47
         t[i].l=t[i].r=t[i].dis=0;
48
         t[i].fa=-1;
         scanf("%d",&t[i].val);
49
50
51
       scanf("%d",&m);
       while(m—) {
52
53
         int a,b;
         scanf("%d%d",&a,&b);
54
55
         int x=finds(a);
56
         int y=finds(b);
         if(x!=y) {
57
58
           t[x].val/=2;
59
           int xx = push(pop(x),x);
60
           t[y].val/=2;
```

```
61
            int yy = push(pop(y),y);
            printf("%d\n",t[merge(xx,yy)].val);
62
63
          } else puts("-1");
64
65
66
      return 0;
67
   1.7 Splay
   /* splay, by Abreto<m@abreto.net>. */
 2
 3
   #ifndef NULL
 4
   #define NULL 0
 5
   #endif
 6
 7
   struct node {
 8
      node *f, *ch[2];
 9
      int sz;
10
      node(node *fa = NULL, node *lc = NULL, node *rc = NULL) {
11
        f = fa;
12
        ch[0] = lc;
        ch[1] = rc;
13
14
        maintain();
15
16
      inline int szof(const int d) const {
17
        return ch[d] ? ch[d]->sz : 0;
18
19
      inline void maintain(void) {
20
        sz = szof(0) + szof(1) + 1;
21
22
      inline int which(void) {
23
        if (NULL == f) return 0;
24
        return (f->ch[1] == this); /* f[which()] == this */
25
      inline node *setf(node *fa, int d = 0) {
26
27
        f = fa;
28
        if (f) {
29
          f->ch[d] = this;
30
          f->maintain();
31
        }
32
        return f;
33
34
      inline node *setc(node *son, int d = 0) {
35
        ch[d] = son;
36
        if (son) son—>f = this;
37
        maintain();
38
        return this;
39
40
      /* rotate this to its fater, return this. */
41
      inline node *rotate(void) {
        if (f != NULL) {
42
          node *ff = f \rightarrow f;
43
44
          int d = which(), fd = f->which();
45
          setc(f->setc(ch[d ^ 1], d), d ^ 1);
46
          setf(ff, fd);
47
        }
48
        return this;
49
      /* splay this to child of target */
50
51
      inline node *splay(node * const target = NULL) {
52
        while (f != target) {
53
          if (target != f \rightarrow f) {
```

```
54
            ( (which() == f->which()) ? f : this )->rotate();
55
56
          rotate();
57
58
        return this;
59
60
      /* 0-based rank */
61
      inline node *get_k_th(unsigned k) {
62
        node *p = this;
63
        int rank;
64
        while (k != (rank = (p\rightarrow szof(0))))  {
65
          if (k < rank) {
66
            p = p - sh[0];
67
          } else {
            k = (rank + 1);
68
69
            p = p \rightarrow ch[1];
70
71
72
        return p->splay(f);
73
74
   };
   /* HDU 3487 - Play with Chain, by Abreto<m@abreto.net>. */
 2
   #include <bits/stdc++.h>
 3
 4
   using namespace std;
 5
 6
   #define MAXN
                     300300
 7
 8
   int n, m;
9
10
   #define LC(p)
                     ch[p][0]
11
   #define RC(p)
                     ch[p][1]
   #define TARGET(p) LC(RC(p))
12
13
14
   int nodes;
    int val[MAXN], ch[MAXN][2], fa[MAXN], sz[MAXN];
15
16
    int rev[MAXN];
17
18
   inline int new_node(int v, int f) {
19
      int p = (++nodes);
20
      val[p] = v;
      fa[p] = f;
21
22
      ch[p][0] = ch[p][1] = rev[p] = 0;
23
      sz[p] = 1;
24
      return p;
25
26
   inline void maintain(int p) {
27
      if (p) {
28
        sz[p] = sz[LC(p)] + sz[RC(p)] + 1;
29
30
    inline void make_child(int f, int d, int p) { /* make p the d-th ch of f */
31
32
      ch[f][d] = p;
33
      if(p) fa[p] = f;
34
35
   inline void myrev(int p) {
36
      if (p) {
37
        rev[p] ^= 1;
38
        swap(LC(p), RC(p));
39
40
41
   inline void pushdown(int p) {
     if(p && rev[p]) {
```

```
43
         if(LC(p)) myrev(LC(p));
         if(RC(p)) myrev(RC(p));
44
45
         rev[p] = 0;
 46
47
48
    int build(int f = 0, int l = 0, int r = n+1) {
49
      if(r < l) return 0;
 50
      if(l == r) return new_node(l, f);
      int mid = 1+r>>1;
51
52
      int p = new_node(mid, f);
53
      LC(p) = build(p, l, mid-1);
54
      RC(p) = build(p, mid+1, r);
      maintain(p);
55
56
      return p;
57
58
    inline int which(int p) { /* return 1 if p is a right child or 0 if p is a left
        child. */
59
      return (RC(fa[p]) == p);
 60
61
    inline int rotate(int p) { /* rotate p to its father. [!] make sure p is not global
        root. */
62
       int f = fa[p], ff = fa[f];
63
      if(0 == f) return p; /* p is global root */
64
      pushdown(f);
65
      pushdown(p);
66
      int d = which(p), df = which(f);
67
      make\_child(f, d, ch[p][d^1]);
68
      make\_child(p, d^1, f);
69
      maintain(f);
70
      maintain(p);
71
      fa[p] = ff
 72
      if(ff) ch[ff][df] = p;
73
       return p;
74
75
    inline int splay(int p, int fr) \{ /* \text{ splay p to the son of fr, return p. }*/
      pushdown(p);
76
77
      while(fa[p] != fr) {
78
         int f = fa[p], dp = which(p);
79
         if(fa[f] == fr) {
80
           return rotate(p);
81
         } else {
 82
           int df = which(f);
83
           if(dp == df) {
84
             rotate(f);
 85
           } else {
 86
             rotate(p);
87
88
           rotate(p);
89
         }
90
91
      return p;
92
93
    inline int get_k_th(int root, int k) {
94
       int p = root;
95
       int rank;
96
      while(k != (rank = (sz[LC(p)] + 1))) {
97
         pushdown(p);
         if(k < rank) p = LC(p);
98
99
         else {
100
           k = rank;
101
           p = RC(p);
         }
102
103
      return splay(p, fa[root]);
104
```

```
105
106
    inline int merge(int left, int right) {
107
       pushdown(left);
108
       if(RC(left)) left = get_k_th(left, sz[left]);
109
       RC(left) = right;
110
       maintain(left);
111
       fa[right] = left;
112
       return left;
113
114
    inline int split(int root, int d) { /* split ch[root][d], return the root of splited
        out. */
115
       pushdown(root);
       int child = ch[root][d];
116
       ch[root][d] = 0;
117
118
       maintain(root);
119
       fa[child] = 0;
120
       return child;
121
122
    inline int concat(int root, int d, int p) { /* make p be ch[root][d], return root */
123
       pushdown(root);
124
       ch[root][d] = p;
125
       fa[p] = root;
126
       maintain(root);
127
       return root;
128
129
130
    void myclear(void) {
131
       nodes = 0;
132
133
134
     int ans[MAXN]:
     void inorder(int p, int &pos) {
135
136
       if(0 == p) return;
137
       pushdown(p);
138
       inorder(LC(p), pos);
139
       if( (0 < val[p]) && (val[p] < n+1) ) ans[pos++] = val[p];
140
       inorder(RC(p), pos);
141
142
143
     void handle() {
144
       int i;
145
       int root;
146
       myclear();
147
       root = build(0);
148
       while(m——) {
149
         char command[8];
150
         int a, b, c;
151
         int tar;
         scanf("%s%d%d", command, &a, &b);
152
         if('C' == command\lceil 0 \rceil) {
153
           scanf("%d", &c);
154
155
           root = get_k_th(root, a);
156
           RC(root) = get_k_t(RC(root), b-a+2);
157
           tar = split(RC(root), 0);
158
           maintain(root);
159
           root = get_k_th(root, c+1);
160
           RC(root) = get_k_t(RC(root), 1);
161
           RC(root) = concat(RC(root), 0, tar);
162
           maintain(root);
163
         } else {
164
           root = get_k_th(root, a);
165
           RC(root) = get_k_t(RC(root), b-a+2);
166
           myrev(TARGET(root));
         }
167
```

```
168
169
       int pos = 0;
170
       inorder(root, pos);
       for(i = 0; i < n; i++) printf("%s%d", i ? "_{\bot}":"", ans[i]);
171
172
       puts("");
173
174
175
     int main(void) {
  while( scanf("%d%d", &n, &m) && (n > 0) && (m > 0) )
176
          handle();
177
178
        return 0;
179 | }
```

#### 1.8 Persistent Segment Tree

- 1. 首先, 给你一颗值为横坐标的线段树, 每个节点上存着该值出现了多少次, 这样的一颗线段树 你会求区间 k 大值吧. 二分即可.
- 2. 然后, 假设区间是数组 arr[n], 区间长度是 n, 那么给你 n 颗线段树, 第 i 颗线段树是第 i-1 颗线段树插入 arr[i] 得到.
- 3. 如果你有了这 n 颗线段树, 想求区间 [l,r] 中的第 k 大值, 那么你需要在第 r 颗和第 l-1 颗 线段树的差线段树上作二分, 就可以求得区间第 k 大值.
- 4. 差线段树很好理解, 比如你有一个部分和数组 sum, sum[r] sum[l-1] 就是部分和的差, 代表区间 [l,r] 的和, 差线段树同理.
- 5. 现在, 可持久化线段树出现为你解决最后一个问题, 空间问题. 内存很小, 不能够存下 n 颗线段树. 但是, 第 2 条中提到, 由于第 i 颗线段是是第 i-1 颗线段是插入仅一个值得到的, 两颗线段树的区别不大, 仅有  $\log(n)$  个节点发生了改变, 我们仅仅需要记录这  $\log(n)$  的数据就可以记录这个增量, 这就是可持久化线段树.

### 2 Dynamic Programming

#### **2.1** LIS $O(n \log n)$

```
1
 2
   int top = 0;
   for( int i=1; i<=n; i++ ) {
 3
     if( ap[i] > dp[top] ) { // 如果大于 "模拟栈" 的栈顶元素直接 入栈 长度加 1
 4
 5
 6
       dp[top] = ap[i];
 7
       continue;
 8
 9
     int m = ap[i];
10
     // lower_bound 前闭后开 返回不小于 m 的最小值的位置
11
     pos = lower_bound(dp,dp+top,m)-dp; // 注意减去dp
12
     if(dp[pos] > ap[i])
       dp[pos] = ap[i];
13
14 | }
```

#### 2.2 LCS $O(n \log n)$

总的来说,就是把 LCS 转化成 LIS,然后用 LIS 的  $\mathcal{O}(N \log N)$  算法来求解。 实现如下:(引用) 假设有两个序列  $s_1[1 \dots 6] = abcadc, s_2[1 \dots 7] = cabedab.$ 记录  $s_1$  中每个元素在  $s_2$  中出现的位置,再将位置按降序排列,则上面的例子可表示为:  $loc(a) = \{6,2\}, loc(b) = \{7,3\}, loc(c) = \{1\}, loc(d) = \{5\}.$  (倒着扫一遍  $s_2$  即可把位置扔进 vector). 将  $s_1$  中每个元素的位置按  $s_1$  中元素的顺序排列成一个序列  $s_3 = \{6, 2, 7, 3, 1, 6, 2, 5, 1\}$ . 在对  $s_3$  求 LIS 得到的值即为求 LCS 的答案。

#### 2.3 Improved by quadrilateral inequality

```
1
   /*
 2
    * 四边形不等式
 3
 4
    * 如果 dp(i,j) 满足 dp(i,j)<=dp(i,j+1)<=dp(i+1,j+1)
 5
    * 那么决策 S(i,j) 满足 S(i,j)<=S(i,j+1)<=S(i+1,j+1)
 6
     * 可以变形为:
 7
            s(i-1,j) \le s(i,j) \le s(i,j+1) // dp方向: i增j减
 8
       或
    *
            s(i,j-1) \Leftarrow s(i,j) \Leftarrow s(i+1,j) // dp方向: 区间长度L增
 9
    *
10
11
   #include <bits/stdc++.h>
12
   using namespace std;
13
14
15
   #define MAXN
                    1024
16
   #define inf
                    (0x3fffffff)
17
   int n, m;
18
19
   int v[MAXN];
20
   int s[MAXN];
21
   int w[MAXN][MAXN];
22
   int dp[MAXN][MAXN];
23
   int c[MAXN][MAXN];
24
25
   int wa(void) {
     int i, j, k;
26
      for(i = 1; i \le n; ++i) {
27
        scanf("%d", v+i);
28
        s[i] = v[i] + s[i-1];
29
30
31
     for(i = 1; i <= n; ++i) {
32
        w[i][i] = 0;
        for(j = i+1; j \le n; ++j)
33
34
          w[i][j] = w[i][j-1] + v[j] * (s[j-1] - s[i-1]);
35
36
     /* doing dp */
37
     for(i = 1; i <= n; ++i) {
38
        dp[i][0] = w[1][i];
39
        c[i][0] = 1;
40
        c[i][i] = i-1;
41
        for(j = i-1; j > 0; j---) {
42
          dp[i][j] = inf;
43
          for(k = c[i-1][j]; k \le c[i][j+1]; ++k)
44
            if(dp[k][j-1]+w[k+1][i] \leftarrow dp[i][j]) {
45
              dp[i][j] = dp[k][j-1] + w[k+1][i];
46
              c[i][j] = k;
            }
47
48
        }
49
50
     /* dp done */
51
     return dp[n][m];
52
53
54
   int main(void) {
     while(EOF != scanf("%d%d", &n, &m) && n && m) {
55
        printf("%d\n", wa());
56
57
58
     return 0;
```

#### 2.4 Improved by Slope

```
1 |/* type 1: */
   /* bzoj 1010 */
 2
 3
   #include <bits/stdc++.h>
 5
   using namespace std;
   typedef long double 11;
 6
 7
   #define MAXN
                    50050
 8
   #define eps
                    (1e-8)
 9
10
   int N;
11
   11 L;
   11 S[MAXN];
12
13
   11 f[MAXN];
   11 dp[MAXN];
14
15
16
   inline ll k(int j) {
17
     return (-2.0) * (f[j] + L);
18
19
   inline ll b(int j) {
      return dp[j] + f[j]*f[j] + 2ll*f[j]*L;
20
21
22
   inline ll g(int j, int i) {
23
      return k(j) * f[i] + b(j);
24
25
26
   /* check if l1 & l3 <= l2 */
   inline int check(int l1, int l2, int l3) {
27
28
     /*ll\ left = b(l3)*k(l1)+b(l1)*k(l2)+b(l2)*k(l3);
29
     ll right = b(l1)*k(l3)*b(l3)*k(l2)*b(l2)*k(l1);*/
30
     ll\ left = b(l3)*k(l1)-b(l1)*k(l3);
31
     ll right = k(l2)*(b(l3)-b(l1))+b(l2)*(k(l1)-k(l3));
32
      return (left <= right);</pre>
33
34
35
   int Q[MAXN], ql, qr;
36
37
   int main(void) {
     int i;
38
39
     scanf("%d%Lf", &N, &L);
40
     L += 1.0;
41
      for(i = 1; i \le N; ++i) 
        scanf("%Lf", S+i);
42
        S[i] += S[i-1];
43
44
        f[i] = S[i] + (double)i;
45
46
     Q[qr++] = 0;
47
     for(i = 1; i <= N; ++i) {
48
        /* <!-- STARED */
49
        for(; ql+1 < qr && g(Q[ql],i) >= g(Q[ql+1],i); ql++);
50
        dp[i] = g(Q[ql], i) + f[i]*f[i] + L*L; //printf("%d: %lld,%lld\n", i, dp[i], dp[i])
           ]_f[i]*f[i]);
51
        for(; ql+1 < qr \& check(Q[qr-2], Q[qr-1], i); qr--);
52
        Q[qr++] = i;
53
        /* --> */
54
55
     printf("%1ld\n", (long long int)round(dp[N]));
56
      return 0;
57
```

#### 2.5 Steiner Tree

令 f[i][sta] 表示 i 号节点,与其他节点的连通性为 sta 时的最小代价,这里 sta 是一个二进制数,在它二进制下的每一位中,0 表示不连通,1 表示联通 状态转移:

• 由子集转移而来

$$f[i][sta] = \min_{s \subseteq sta} \{f[i][s] + f[i][sta \setminus s] - val[i]\}$$

• 由不含该节点的状态转移而来

$$f[i][j] = \min\{f[k][j] + val[i]\}$$

```
流程:
   枚举状态集S
 1
 2
   {
 3
         枚举S的子集s
 4
 5
             更新f[S][1~n]
 6
 7
         将 f[S][x]<inf 的x入队
 8
         spfa(S)
 9
   代码:
   |int f[1<<M][N];
 1
 2
   queue<int> q;
 3
   bool in[N];
 4
 5
   void spfa(int S) {
     while (!q.empty()) {
 6
 7
        int now=q.front();
 8
        q.pop();
 9
        in[now]=0;
10
        for (int i=st[now]; i; i=way[i].nxt) {
11
          int y=way[i].y;
          if (f[S][y]>f[S][now]+val[y]) {
12
13
            f[S][y]=f[S][now]+val[y];
14
            if (!in[y]) q.push(y),in[y]=1;
15
16
        }
17
     }
18
19
20
   void work() {
21
      int cnt=0;
     memset(f,0x7f,sizeof(f));
22
23
24
     for (int i=1; i<=n; i++)
25
        if (!val[i]) f[1<<cnt][i]=0,cnt++;
      for (int S=1; S<(1<<cnt); S++) {
26
27
        for (s=(S-1)\&S; s; s=(s-1)\&S)
          for (int i=1; i<=n; i++)
28
            f[S][i]=min(f[S][i],f[s][i]+f[S^s][i]-val[i]);
29
30
        for (int i=1; i<=n; i++)
31
          if (f[S][i]<INF&&!in[i])</pre>
32
            q.push(i),in[i]=1;
33
        spfa(S);
34
35
36
     int ans=INF;
```

```
for (int i=1; i<=n; i++) ans=min(ans,f[(1<<cnt)-1][i]);
37
38
     printf("%d\n",ans);
39
   }
   //
40
41
   // 作者: Coco_T_
   // 来源: CSDN
42
   // 原文: https://blog.csdn.net/wu_tongtong/article/details/78992913
43
   // 版权声明: 本文为博主原创文章, 转载请附上博文链接!
   3
       Geometry
   3.1
       2\mathrm{D}
   3.1.1 Point
   /* 2D Point Class, by Abreto<m@abreto.net> */
 2
   #include <cmath>
 3
 4
   /**
 5
    * Define ABG2d_USE_LL if you want to use long long int for cordnates.
 6
 7
 8
   namespace ab_geometry_2d {
 9
10
   using namespace std;
11
12
   typedef double ab_float;
13
14
   const ab_float pi = acos(-1.);
15
16
   #ifdef ABG2d_USE_LL
17
   typedef long long int T;
18
   #else
   typedef ab_float T;
19
20
   const ab_float eps = 1e-8;
   #endif
21
22
23
   inline T myabs(T x) \{
24
     if(x < 0) return (-x);
25
      return x;
26
27
   inline int sgn(T x) {
  /* no difference' in fact */
28
29
30
   #ifdef ABG2d_USE_LL
31
     if (0 == x) return 0;
32
   #else
33
     if (myabs(x) < eps) return 0;</pre>
34
   #endif
35
     return (x > 0) ? 1 : -1;
36
37
38
   inline T sqr(T x) {
39
     return (x * x);
40
41
42
   struct point {
43
     T x, y;
44
     point(void):x(T()),y(T()) {}
45
     point(T xx, T yy):x(xx),y(yy) {}
46
     inline T norm2(void) {
47
        return sqr(x) + sqr(y);
```

```
48
49
     inline ab_float norm(void) {
50
        return sqrt((ab_float)(norm2()));
51
     inline point rotate(const ab_float &cost, const ab_float &sint) {} // TODO:
52
     inline point operator-(void) const {
53
54
        return point(-x,-y);
55
56
     inline point operator+(const point& b) const {
57
        return point(x+b.x,y+b.y);
58
59
     inline point operator—(const point& b) const {
60
        return point(x-b.x,y-b.y);
61
     inline point operator->*(const point &b) const {
62
63
        return (b-(*this));
64
65
     inline T operator*(const point& b) const {
        return ((x)*(b.x))+((y)*(b.y)); /* inner product */
66
67
68
     inline T operator^(const point& b) const {
69
        return ((x)*(b.y))-((b.x)*(y)); /* outter product */
70
71
     inline point& operator+=(const point& b) {
72
       point tmp=(*this)+b;
73
       (*this)=tmp;
74
        return (*this);
75
76
     inline point& operator=(const point& b) {
77
        point tmp=(*this)-b;
78
        (*this)=tmp;
79
        return (*this);
80
81
     inline bool operator==(const point& b) const {
82
        return (0==sgn(x-b.x))&(0==sgn(y-b.y));
83
84
     inline bool operator!=(const point& b) const {
85
        return !((*this)==b);
86
87
     inline point operator<<(const ab_float& theta) const {
88
        ab_float ct = cos(theta), st = sin(theta); /* rotate counter-clockwise in radian
89
        return point(ct*x - st*y, st*x + ct*y);
90
     }
91
   };
92
93
   typedef point vec;
94
95
96 | }
       // namespace ab_geometry_2d
   3.1.2 Circle
   Base
  /* 2D Circle Base Class, by Abreto<m@abreto.net>. */
 1
 2
 3
   /* requirement: point.cc */
   #include "point.cc"
 6
   #include <utility>
   namespace ab_geometry_2d {
```

```
9
10
   using namespace std;
11
12
    struct circle {
13
      point o;
14
      Tr;
15
      circle(void) : r(T()) {}
      circle(point center, T radius) : o(center), r(radius) {}
16
17
18
      inline ab_float arclen(ab_float theta) {
19
        return theta * r;
20
      inline ab_float circumference(void) {
21
22
        return 2. * pi * r;
23
24
      inline ab_float area(void) {
25
        return pi * r * r;
26
      }
27
28
     /* bool contain(const circle &C, const bool including_touch = false) const
29
30
          T dis2 = (o \rightarrow *(C.o)).norm2();
31
          T raw_diff = r - C.r;
32
          if ( -1 == sgn(raw_diff) ) return false;
33
          T dr2 = sqr(raw_diff);
34
          return (dis2 < dr2) || (including_touch && (dis2 == dr2));
35
36
      inline bool in(const circle &C, const bool including_touch = false) const
37
38
        return C.contain(*this, including_touch);
39
      } */
40
      enum relation_t {
41
        same = 0 \times 00000,
42
        contain = 0 \times 00001,
43
        intouch = 0 \times 00010,
44
        intersect = 0x00100,
45
        outtouch = 0x01000,
46
        separate = 0x10000,
47
        unknow_relation = 0xfffff
48
      };
49
      relation_t with(const circle &C) const {
50
        T dis2 = (o->*(C.o)).norm2();
51
        T dr2 = sqr(r - C.r), rs2 = sqr(r + C.r);
52
        if (0 == sgn(dis2) \&\& 0 == sgn(dr2)) return same;
             -1 == sgn(dis2 - dr2) ) return contain;
53
        if ( \emptyset == sgn(dis2 - dr2) ) return intouch;
54
55
        if (-1 == sgn(dr2 - dis2) \&\& -1 == sgn(dis2 - rs2)) return intersect;
56
        if (0 == sgn(dis2 - rs2)) return outtouch;
57
        if (-1 == sgn(rs2 - dis2)) return separate;
58
        return unknow_relation;
59
      }
60
61
      enum point_relation_t {
        in = 0x001,
62
63
        on = 0x010,
64
        out = 0x100,
65
        unknow_point_relation = 0xfff
66
      };
67
      point_relation_t with(const point &P) const {
68
        T dis2 = (o\rightarrow *P).norm2();
69
        T r2 = sqr(r);
        int type = sgn(dis2 - r2);
70
71
        if (-1 == type) return in;
72
        if (0 == type) return on;
```

```
73
        if (+1 == type) return out;
74
        return unknow_point_relation;
75
     }
76
77
     ab_float central_angle(const point &A, const point &B, const bool reflex = false)
         const {
78
        T dot = (A * B);
79
        if (0 == sqn(dot)) return 1. * (A != B) * pi;
        ab_float angle = ((ab_float)(dot)) / r / r;
80
81
        if (reflex) angle = 2. * pi - angle;
82
        return angle;
83
     }
84
85
     /* be sure (*this) intersect with C */
86
     pair<point, point> crosspoint(const circle &C) const {
87
        ab_float d = (o \rightarrow * (C.o)).norm();
88
        // TODO:
89
     }
90
   };
91
92 |}
   k 次圆交
   //china no.1
 2
   #pragma comment(linker, "/STACK:1024000000,1024000000")
 3
   #include <vector>
 4
   |#include <iostream>
 5
   |#include <strina>
   #include <map>
 6
   #include <stack>
 7
 8
   #include <cstring>
 9
   #include <queue>
   #include <list>
10
   #include <stdio.h>
11
   |#include <set>
13
   #include <algorithm>
   #include <cstdlib>
14
15
   #include <cmath>
16
   #include <iomanip>
   #include <cctype>
17
18 #include <sstream>
19 |#include <functional>
20
   |#include <stdlib.h>
21
   #include <time.h>
22
   #include <bitset>
23
   using namespace std;
24
25
   #define pi acos(-1)
   #define PI acos(-1)
26
   #define endl '\n'
27
   #define srand() srand(time(0));
28
   #define me(x,y) memset(x,y,sizeof(x));
29
   #define foreach(it,a) for(__typeof((a).begin()) it=(a).begin();it!=(a).end();it++)
30
31
   #define close() ios::sync_with_stdio(0); cin.tie(0);
32
   #define FOR(x,n,i) for(int i=x;i<=n;i++)</pre>
33
   #define F0r(x,n,i) for(int i=x;i<n;i++)</pre>
34
   #define W while
35
   #define sgn(x) ((x) < 0 ? -1 : (x) > 0)
36
   #define bug printf("********\n");
37
   #define db double
   typedef long long LL:
38
   const int INF=0x3f3f3f3f3f;
39
40
   const LL LINF=0x3f3f3f3f3f3f3f3f3f1LL;
41 | const int dx[] = \{-1,0,1,0,1,-1,-1,1\};
```

```
42
    |const int dy[] = {0,1,0,-1,-1,1,-1,1};
 43
    const int maxn=1e3+10;
    const int maxx=1e6+100;
    const double EPS=1e-8;
 46
    const double eps=1e-8;
 47
    const int mod=10000007;
     template<class T>inline T min(T a,T b,T c) {
 48
 49
       return min(min(a,b),c);
 50
 51
    template<class T>inline T max(T a,T b,T c) {
 52
      return max(max(a,b),c);
 53
    template<class T>inline T min(T a,T b,T c,T d) {
 54
 55
      return min(min(a,b),min(c,d));
 56
 57
     template<class T>inline T max(T a,T b,T c,T d) {
 58
      return max(max(a,b),max(c,d));
 59
 60
    template <class T>
 61
    inline bool scan_d(T &ret) {
 62
      char c;
 63
       int sgn;
      if (c = getchar(), c == EOF) {
 64
 65
         return 0;
 66
 67
      while (c != '-' && (c < '0' || c > '9')) {
 68
         c = getchar();
 69
      sqn = (c == '-') ? -1 : 1;
 70
      ret = (c == '-')? 0 : (c - '0');
 71
      while (c = getchar(), c >= '0' && c <= '9') {
 72
 73
         ret = ret * 10 + (c - '0');
 74
      }
 75
      ret *= sgn;
 76
       return 1;
 77
 78
 79
     inline bool scan_lf(double &num) {
 80
       char in:
 81
      double Dec=0.1;
 82
      bool IsN=false,IsD=false;
 83
      in=getchar();
 84
      if(in==EOF) return false;
      while(in!='-'&&in!='.'&&(in<'0'||in>'9'))in=getchar();
 85
      if(in=='-') {
 86
 87
         IsN=true;
 88
         num=0;
 89
      } else if(in=='.') {
 90
         IsD=true;
 91
         num=0;
 92
       } else num=in-'0';
      if(!IsD) {
 93
 94
         while(in=getchar(),in>='0'&&in<='9') {
 95
           num*=10;
 96
           num+=in-'0';
 97
         }
98
      if(in!='.') {
 99
         if(IsN) num=-num;
100
101
         return true;
102
      } else {
103
         while(in=getchar(),in>='0'&&in<='9') {
104
           num+=Dec*(in-'0');
105
           Dec*=0.1;
```

```
106
         }
107
108
       if(IsN) num=-num;
109
       return true;
110
111
112
     void Out(LL a) {
       if(a < 0) {
  putchar('-');</pre>
113
114
115
         a = -a;
116
117
       if(a >= 10) Out(a / 10);
118
       putchar(a % 10 + '0');
119
120
     void print(LL a) {
121
       Out(a), puts("");
122
     //freopen( "in.txt" , "r" , stdin );
//freopen( "data.txt" , "w" , stdout );
//cerr << "run time is " << clock() << endl;</pre>
123
124
125
126
     /*struct Point
127
128
         double x, y;
129
         Point(const Point& rhs): x(rhs.x), y(rhs.y) { } //拷贝构造函数
130
         Point(double x = 0, double y = 0) : x(x), y(y) { }
131
         inline void input()
132
          {
133
              scanf("%lf%lf",&x,&y);
134
135
         inline void print()
136
137
              printf("%.6lf %.6lf\n",x,y);
138
         }
     };*/
139
140
     db sqr(db x) {
141
       return x*x;
142
143
     int dcmp(double x) {
144
       if(fabs(x) < EPS) return 0;
145
       else return x < 0 ? -1 : 1;
146
147
     struct Circle {
148
       double x, y, r, angle;
149
       int d;
150
       Circle() {}
151
       Circle(double xx, double yy, double ang = 0, int t = 0) {
152
         X = XX;
153
         y = yy;
154
         angle = ang;
155
         d = t;
156
157
       void get() {
         scanf("%lf%lf%lf", &x, &y, &r);
158
159
         d = 1;
160
161
162
     Circle cir[maxn],tp[maxn*2];
163
     double area[maxn];
164
     double dis(Circle a,Circle b) {
165
       return sqrt(sqr(a.x - b.x) + sqr(a.y - b.y));
166
167
     double cross(Circle p0,Circle p1,Circle p2) {
168
       return (p1.x - p0.x) * (p2.y - p0.y) - (p1.y - p0.y) * (p2.x - p0.x);
169 |}
```

```
170
    │//圆相交
171
    int CirCrossCir(Circle p1, double r1, Circle p2, double r2, Circle &cp1, Circle &cp2) {
172
      double mx = p2.x - p1.x, sx = p2.x + p1.x, mx2 = mx * mx;
173
      double my = p2.y - p1.y, sy = p2.y + p1.y, my2 = my * my;
174
      double sq = mx^2 + my^2, d = -(sq - sqr(r^1 - r^2)) * (sq - sqr(r^1 + r^2));
175
      if (d + eps < 0) return 0;
176
      if (d < eps) d = 0;
177
      else d = sqrt(d);
178
      double x = mx * ((r1 + r2) * (r1 - r2) + mx * sx) + sx * my2;
179
      double y = my * ((r1 + r2) * (r1 - r2) + my * sy) + sy * mx2;
      double dx = mx * d, dy = my * d;
180
      sq *= 2;
181
      cp1.x = (x - dy) / sq;
182
183
       cp1.y = (y + dx) / sq;
184
       cp2.x = (x + dy) / sq;
185
       cp2.y = (y - dx) / sq;
186
      if (d > eps) return 2;
187
      else return 1;
188
189
    bool circmp(const Circle& u, const Circle& v) {
190
       return dcmp(u.r - v.r) < 0;
191
192
    bool cmp(const Circle& u, const Circle& v) {
193
      if (dcmp(u.angle - v.angle)) return u.angle < v.angle;</pre>
194
       return u.d > v.d;
195
196
    //0.5*r*r*(K-sin(K))
197
    double calc(Circle cir,Circle cp1,Circle cp2) {
198
      double ans = (cp2.angle - cp1.angle) * sqr(cir.r)
199
                    - cross(cir, cp1, cp2) + cross(Circle(0, 0), cp1, cp2);
200
       return ans / 2;
201
202
203
    void CirUnion(Circle cir[], int n) {
204
      Circle cp1, cp2;
205
       sort(cir, cir + n, circmp);
206
      for (int i = 0; i < n; ++i)
207
         for (int j = i + 1; j < n; ++j)
           if (dcmp(dis(cir[i], cir[j]) + cir[i].r - cir[j].r) <= 0)</pre>
208
209
             cir[i].d++;
210
      for (int i = 0; i < n; ++i) {
211
         int tn = 0, cnt = 0;
212
         for (int j = 0; j < n; ++j) {
213
           if (i == j) continue;
214
           if (CirCrossCir(cir[i], cir[i].r, cir[j], cir[j].r,
215
                            cp2, cp1) < 2) continue;
216
           cp1.angle = atan2(cp1.y - cir[i].y, cp1.x - cir[i].x);
217
           cp2.angle = atan2(cp2.y - cir[i].y, cp2.x - cir[i].x);
218
           cp1.d = 1;
219
           tp[tn++] = cp1;
220
           cp2.d = -1;
221
           tp[tn++] = cp2;
222
           if (dcmp(cp1.angle - cp2.angle) > 0) cnt++;
223
224
         tp[tn++] = Circle(cir[i].x - cir[i].r, cir[i].y, pi, -cnt);
         tp[tn++] = Circle(cir[i].x - cir[i].r, cir[i].y, -pi, cnt);
225
226
         sort(tp, tp + tn, cmp);
227
         int p, s = cir[i].d + tp[0].d;
228
         for (int j = 1; j < tn; ++j) {
229
           p = s;
230
           s += tp[j].d;
231
           area[p] += calc(cir[i], tp[j - 1], tp[j]);
232
233
      }
```

```
234
235
    int n;
236
    void solve() {
237
       for(int i=0; i<n; i++)
238
         cir[i].get();
239
       me(area, 0);
240
       CirUnion(cir,n);
241
       for(int i=1; i<=n; i++) {
242
         area[i]=area[i+1];
         printf("[%d]_{\square}=_{\square}%.3f\n", i, area[i]);
243
244
245
246
    int main() {
       while(scanf("%d",&n)!=EOF)
247
248
         solve();
249 |}
     universe
  2
    Point CircumCenter(Point a, Point b, Point c) { //三角形的外心
  3
       Point cp;
  4
       double a1 = b.x-a.x,b1 = b.y-a.y,c1 = (a1*a1 + b1*b1)/2;
  5
       double a2 = c.x-a.x,b2 = c.y-a.y,c2 = (a2*a2 + b2*b2)/2;
  6
       double d = a1*b2 - a2*b1;
  7
       cp.x = a.x + (c1*b2-c2*b1)/d;
  8
       cp.y = a.y + (a1*c2-a2*c1)/d;
  9
       return cp;
 10
     3.1.3 Convex hull
  1 | /* 2D Convex Hull, by Abreto <m@abreto.net>. */
  2
    #include "2d_base.hh"
  3
    #include <cmath>
  4
    |#include <algorithm>
  5
  6
    using namespace std;
  7
  8
    point 0;
  9
 10
    bool comp_angle(point_t a, point_t b) {
 11
       double t = (a-0).X(b-0);
 12
       if(fe(t,0.0)) return fl((b-0).mag2(),(a-0).mag2());
 13
       else return fl(0.0,t);
 14
 15
 16
     void convex_hull_graham(vp& convex, vp src) {
 17
       int i = 0, top = 0;
 18
       0 = src[0];
 19
       for(auto pt : src)
 20
         if( pt.x < 0.x | | (pt.x == 0.x \& pt.y < 0.y))
 21
           0 = pt;
 22
       sort(src.begin(), src.end(), comp_angle);
 23
       convex.push_back(src[0]);
 24
       convex.push_back(src[1]);
 25
       top = 1;
 26
       for(i = 2; i < src.size(); ++i) {
         while(top>1 && fle((convex[top]-convex[top-1]).X(src[i]-convex[top]),0.0)) {
 27
 28
           convex.pop_back();
 29
           --top;
 30
 31
         convex.push_back(src[i]);
```

```
32
       ++top;
33
     }
34 | }
   3.1.4 Intersect Area
   #include <cstdio>
 2
   #include <cmath>
 3
   #include <algorithm>
 4
 5
   using namespace std;
 6
 7
   //#define inf 1000000000000
 8
   #define M 8
 9
   #define LL long long
10
   #define eps 1e-12
11
   #define PI acos(-1.0)
   using namespace std;
13
   struct node {
14
      double x,y;
15
     node() {}
16
     node(double xx,double yy) {
17
       X=XX;
18
       y=yy;
19
     }
20
     node operator –(node s) {
21
        return node(x-s.x,y-s.y);
22
23
     node operator +(node s) {
24
        return node(x+s.x,y+s.y);
25
26
     double operator *(node s) {
27
        return x*s.x+y*s.y;
28
29
     double operator ^(node s) {
30
        return x*s.y-y*s.x;
31
32
33
   double max(double a,double b) {
34
     return a>b?a:b;
35
36
   double min(double a,double b) {
37
      return a<b?a:b;
38
39
   double len(node a) {
40
      return sqrt(a*a);
41
42
   double dis(node a, node b) { //两点之间的距离
43
      return len(b-a);
44
   double cross(node a,node b,node c) { //叉乘
45
46
      return (b-a)^(c-a);
47
48
   double dot(node a, node b, node c) { //点成
49
     return (b-a)*(c-a);
50
51
   int judge(node a, node b, node c) { //判断c是否在ab线段上(前提是c在直线ab上)
52
      if(c.x > = min(a.x, b.x)
53
          \&c.x \le max(a.x,b.x)
54
          \&c.y = min(a.y,b.y)
55
          &&c.y<=max(a.y,b.y))
56
        return 1;
57
      return 0;
```

```
58
 59
    double area(node b,node c,double r) {
 60
      node a(0.0,0.0);
 61
      if(dis(b,c)<eps)
 62
        return 0.0;
      double h=fabs(cross(a,b,c))/dis(b,c);
 63
      if(dis(a,b)>r-eps&&dis(a,c)>r-eps) { //两个端点都在圆的外面则分为两种情况
 64
 65
        double angle=acos(dot(a,b,c)/dis(a,b)/dis(a,c));
        if(h>r-eps) {
 66
 67
          return 0.5*r*r*angle;
 68
        } else if(dot(b,a,c)>0&&dot(c,a,b)>0) {
 69
          double angle1=2*acos(h/r);
 70
          return 0.5*r*r*fabs(angle-angle1)+0.5*r*r*sin(angle1);
 71
        } else {
 72
          return 0.5*r*r*angle;
 73
 74
      } else if(dis(a,b)<r+eps&dis(a,c)<r+eps) { //两个端点都在圆内的情况
 75
        return 0.5*fabs(cross(a,b,c));
 76
      } else { //一个端点在圆上一个端点在圆内的情况
 77
        if(dis(a,b)>dis(a,c)) { //默认b在圆内
 78
          swap(b,c);
 79
 80
        if(fabs(dis(a,b))<eps) { //ab距离为0直接返回0
 81
          return 0.0;
 82
 83
        if(dot(b,a,c)<eps) {
 84
          double angle1=acos(h/dis(a,b));
 85
          double angle2=acos(h/r)-angle1;
 86
          double angle3=acos(h/dis(a,c))-acos(h/r);
 87
          return 0.5*dis(a,b)*r*sin(angle2)+0.5*r*r*angle3;
 88
 89
        } else {
 90
          double angle1=acos(h/dis(a,b));
 91
          double angle2=acos(h/r);
 92
          double angle3=acos(h/dis(a,c))-angle2;
 93
          return 0.5*r*dis(a,b)*sin(angle1+angle2)+0.5*r*r*angle3;
 94
        }
 95
 96
    }
 97
 98
    node A, B, C;
 99
    int R;
100
101
    bool compar(node &p1, node &p2) {
102
      return (p1^p2)>eps;
103
104
105
    double f(double x, double y) {
106
      node 0(x,y);
107
      node p[8];
      p[0] = A-0;
108
109
      p[1] = B-0;
      p[2] = C-0;
110
111
      sort(p, p+3, compar);
112
      p[3] = p[0];
113
      0 = node(0,0);
114
      double sum=0;
115
      /* <!-- 求面积交部分 */
116
      for(int i=0; i<3; i++) { /* 按顺或逆时针顺序最后取绝对值就好 */
117
        int j=i+1;
        double s=area(p[i],p[j],(double)R);
118
119
        if(cross(0,p[i],p[j])>0)
120
          sum+=s;
        else
121
```

```
122
           sum-=s;
123
       if(sum < -eps) sum = -sum;
124
125
       /* --> */
126
       return sum;
127
128
129
     double trifind(double x, double y1, double y2) {
130
       double l = y1, r = y2;
131
       while(r-l>eps) {
132
         double mid = (1+r)/2.0;
         double mmid = (mid+r)/2.0;
133
         if( f(x,mmid) > f(x,mid) + eps )
134
135
           l = mid;
136
         else
137
           r = mmid;
138
139
       return f(x,l);
140
    }
141
142
     double findmin(double x1, double x2, double y1, double y2) {
143
       double l = x1, r = x2;
144
       while(r-l>eps) {
145
         double mid = (1+r)/2.0;
146
         double mmid = (mid+r)/2.0;
147
         if( trifind(mmid,y1,y2) > trifind(mid,y1,y2)+eps )
148
           l = mid;
149
         else
150
           r = mmid;
151
152
       return trifind(l,y1,y2);
153
154
155
     double ans(int a, int b, int c, int r) {
156
       A = node(0,0);
157
       B = node((double)c,0);
158
       R = r;
159
       double da = a, db = b, dc = c;
       double cosa = (db*db+dc*dc-da*da)/(2.0*db*dc);
160
161
       double alpha = acos(cosa);
162
       C = node(db*cosa, db*sin(alpha));
163
       return findmin(0.0, c, 0.0, db*sin(alpha));
164
165
166
    int main(void) {
       int a = 0, b = 0, c = 0, r = 0;
167
       while(EOF != scanf("%d%d%d%d",&a,&b,&c,&r) && (allbliclir))
168
169
         printf("%.8lf\n", ans(a,b,c,r));
170
       return 0;
171 | }
     3.1.5 Universe
    |#include <bits/stdc++.h>
  1
    using namespace std;
  2
  3
  4
    struct Point {
  5
       double x, y;
       Point(double x = 0, double y = 0) : x(x), y(y) {}
  6
  7
    };
  8
  9
    typedef Point Vector;
 10
```

```
| Vector operator + (Vector A, Vector B) {
11
12
     return Vector(A.x + B.x, A.y + B.y);
13
14
   Vector operator – (Vector A, Vector B) {
15
     return Vector(A.x - B.x, A.y - B.y);
16
17
   Vector operator * (Vector A, double p) {
18
     return Vector(A.x*p, A.x*p);
19
20
   Vector operator / (Vector A, double p) {
21
     return Vector(A.x/p, A.x/p);
22
23
24
   bool operator < (const Point& a, const Point b) {</pre>
25
     return a.x < b.x | | (a.x == b.x && a.y < b.y);
26
27
28
   const double EPS = 1e-10;
29
30
   int dcmp(double x) {
31
     if(fabs(x) < EPS) return 0;
32
     else return x < 0 ? -1 : 1;
33
34
35
   bool operator == (const Point& a, const Point& b) {
36
     return dcmp(a.x-b.x) == 0 \&\& dcmp(a.y-b.y);
37
38
39
   //向量a的极角
40
   double Angle(const Vector& v) {
41
     return atan2(v.y, v.x);//\share\CodeBlocks\templates\wizard\console\cpp
42
43
44
   //向量点积
45
   double Dot(Vector A, Vector B) {
46
     return A.x*B.x + A.y*B.y;
47
48
49
   //向量长度\share\CodeBlocks\templates\wizard\console\cpp
50
   double Length(Vector A) {
51
     return sqrt(Dot(A, A));
52
53
54
   //向量夹角
55
   double Angle(Vector A, Vector B) {
56
     return acos(Dot(A, B) / Length(A) / Length(B));
57
58
59
   //向量叉积
   double Cross(Vector A, Vector B) {
61
     return A.x*B.y - A.y*B.x;
62
63
64
   //三角形有向面积的二倍
65
   double Area2(Point A, Point B, Point C) {
66
     return Cross(B-A, C-A);
67
68
69
   //向量逆时针旋转rad度(弧度)
70
   Vector Rotate(Vector A, double rad) {
71
     return Vector(A.x*cos(rad)-A.y*sin(rad), A.x*sin(rad)+A.y*cos(rad));
72
73
   |// 计 算 向 量 A 的 单 位 法 向 量 。 左 转 90 ° , 把 长 度 归 一 。 调 用 前 确 保 A 不 是 零 向 量 。
```

```
75
   | Vector Normal(Vector A) {
76
     double L = Length(A);
77
     return Vector(-A.y/L, A.x/L);
78
   }
79
80
   使用复数类实现点及向量的简单操作
81
82
83
   #include <complex>
84
   typedef complex<double> Point;
85
   typedef Point Vector;
86
87
   double Dot(Vector A, Vector B) { return real(conj(A)*B)}
   double Cross(Vector A, Vector B) { return imag(conj(A)*B);}
88
89
   Vector Rotate(Vector A, double rad) { return A*exp(Point(0, rad)); }
90
91
   92
93
   94
   * 用直线上的一点p0和方向向量v表示一条指向。直线上的所有点P满足P = P0+t*v;
95
   * 如果知道直线上的两个点则方向向量为B-A, 所以参数方程为A+(B-A)*t;
96
   * 当t 无限制时, 该参数方程表示直线。
   * 当t > 0时, 该参数方程表示射线。
97
98
   * 当 0 < t < 1时, 该参数方程表示线段。
99
   100
101
   //直线交点,须确保两直线有唯一交点。
102
   Point GetLineIntersection(Point P, Vector v, Point Q, Vector w) {
103
     Vector u = P - Q;
104
     double t = Cross(w, u)/Cross(v, w);
105
     return P+v*t;
106
107
108
   //点到直线距离
   double DistanceToLine(Point P, Point A, Point B) {
109
110
     Vector v1 = B - A, v2 = P - A;
111
     return fabs(Cross(v1, v2) / Length(v1)); //不取绝对值, 得到的是有向距离
112
113
114
   //点到线段的距离
115
   double DistanceToSegmentS(Point P, Point A, Point B) {
116
     if(A == B) return Length(P-A);
117
     Vector v1 = B-A, v2 = P-A, v3 = P-B;
     if(dcmp(Dot(v1, v2)) < 0) return Length(v2);</pre>
118
     else if(dcmp(Dot(v1, v3)) > 0) return Length(v3);
119
     else return fabs(Cross(v1, v2)) / Length(v1);
120
121
122
123
   //点在直线上的投影
124
   Point GetLineProjection(Point P, Point A, Point B) {
125
     Vector v = B - A;
126
     return A+v*(Dot(v, P-A)/Dot(v, v));
127
128
   //线段相交判定,交点不在一条线段的端点
129
   bool SegmentProperIntersection(Point a1, Point a2, Point b1, Point b2) {
130
131
     double c1 = Cross(a2-a1, b1-a1), c2 = Cross(a2-a1, b2-a1);
132
     double c3 = Cross(b2-b1, a1-b1), c4 = Cross(b2-b1, a2-b1);
133
     return dcmp(c1)*dcmp(c2) < 0 && dcmp(c3)*dcmp(c4) < 0;
134
135
   //判断点是否在点段上,不包含端点
136
   bool OnSegment(Point P, Point a1, Point a2) {
137
     return dcmp(Cross(a1-P, a2-P) == 0 \&\& dcmp((Dot(a1-P, a2-P)) < 0));
138
```

```
139 |}
140
141
    //计算凸多边形面积
142
    double ConvexPolygonArea(Point *p, int n) {
143
     double area = 0;
144
     for(int i = 1; i < n-1; i++)
145
       area += Cross(p[i] - p[0], p[i+1] - p[0]);
146
      return area/2;
147
148
149
    // 计 算 多 边 形 的 有 向 面 积
150
    double PolygonArea(Point *p, int n) {
151
     double area = 0;
152
      for(int i = 1; i < n-1; i++)
153
       area += Cross(p[i] - p[0], p[i+1] - p[0]);
154
      return area/2;
155
156
157
    158
    * Morley定理: 三角形每个内角的三等分线, 相交成的三角形是等边三角形。
159
    * 欧拉定理: 设平面图的定点数, 边数和面数分别为V,E,F。则V+F-E = 2;
160
    161
162
    struct Circle {
163
     Point c;
164
     double r;
165
166
     Circle(Point c, double r) : c(c), r(r) {}
167
     //通过圆心角确定圆上坐标
     Point point(double a) {
168
169
       return Point(c.x + cos(a)*r, c.y + sin(a)*r);
170
     }
171
    };
172
173
    struct Line {
174
     Point p;
175
     Vector v;
176
     double ang;
     Line() {}
177
178
     Line(Point p, Vector v) : p(p), v(v) {}
179
     bool operator < (const Line& L) const {</pre>
180
       return ang < L.ang;
181
     }
182
    };
183
184
    //直线和圆的交点,返回交点个数,结果存在sol中。
185
    //该代码没有清空sol。
    int getLineCircleIntersecion(Line L, Circle C, double& t1, double& t2, vector<Point>&
186
        sol) {
187
     double a = L.v.x, b = L.p.x - C.c.x, c = L.v.y, d = L.p.y - C.c.y;
188
     double e = a*a + c*c, f = 2*(a*b + c*d), g = b*b + d*d - C.r*C.r;
189
     double delta = f*f - 4*e*g;
     if(dcmp(delta) < 0) return 0; //相离
190
191
     if(dcmp(delta) == 0) {
                                 //相切
192
       t1 = t2 = -f / (2*e);
193
       sol.push_back(C.point(t1));
194
       return 1;
195
     }
196
     //相交
197
     t1 = (-f - sqrt(delta)) / (2*e);
198
      sol.push_back(C.point(t1));
199
     t2 = (-f + sqrt(delta)) / (2*e);
200
      sol.push_back(C.point(t2));
201
     return 2;
```

```
202
   |}
203
204
    //两圆相交
205
    int getCircleCircleIntersection(Circle C1, Circle C2, vector<Point>& sol) {
206
      double d = Length(C1.c - C2.c);
207
      if(dcmp(d) == 0) {
208
        if(dcmp(C1.r - C2.r == 0)) return -1;
                                                 //两圆完全重合
209
        return 0:
                                                 //同心圆,半径不一样
210
211
      if(dcmp(C1.r + C2.r - d) < 0) return 0;
      if(dcmp(fabs(C1.r - C2.r) == 0)) return -1;
212
213
      double a = Angle(C2.c - C1.c);
214
                                                   //向量C1C2的极角
215
      double da = a\cos((C1.r*C1.r + d*d - C2.r*C2.r) / (2*C1.r*d));
216
      //C1C2到C1P1的角
217
      Point p1 = C1.point(a-da), p2 = C1.point(a+da);
218
      sol.push_back(p1);
219
      if(p1 == p2) return 1;
220
      sol.push_back(p2);
221
      return 2;
222
223
224
    const double PI = acos(-1);
225
    //过定点做圆的切线
226
    //过点p做圆C的切线,返回切线个数。v[i]表示第i条切线
227
    int getTangents(Point p, Circle C, Vector* v) {
228
      Vector u = C.c - p;
229
      double dist = Length(u);
230
      if(dist < C.r) return 0;
231
      else if(dcmp(dist - C.r) == 0) {
        v[0] = Rotate(u, PI/2);
232
233
        return 1;
234
      } else {
235
        double ang = asin(C.r / dist);
236
        v[0] = Rotate(u, -ang);
237
        v[1] = Rotate(u, +ang);
238
        return 2;
239
240
    }
241
242
    //两圆的公切线
243
    //返回切线的个数, -1表示有无数条公切线。
244
    //a[i], b[i] 表示第i条切线在圆A,圆B上的切点
245
    int getTangents(Circle A, Circle B, Point *a, Point *b) {
246
      int cnt = 0;
247
      if(A.r < B.r) {
248
        swap(A, B);
249
        swap(a, b);
250
251
      int d2 = (A.c.x - B.c.x)*(A.c.x - B.c.x) + (A.c.y - B.c.y)*(A.c.y - B.c.y);
252
      int rdiff = A.r - B.r;
253
      int rsum = A.r + B.r;
254
      if(d2 < rdiff*rdiff) return 0;</pre>
                                      //内含
255
      double base = atan2(B.c.y - A.c.y, B.c.x - A.c.x);
256
      if(d2 == 0 \&\& A.r == B.r) return -1;
                                            // 无限多条切线
                                      //内切一条切线
257
      if(d2 == rdiff*rdiff) {
258
        a[cnt] = A.point(base);
259
        b[cnt] = B.point(base);
260
        cnt++;
261
        return 1;
262
263
      //有外共切线
264
      double ang = acos((A.r-B.r) / sqrt(d2));
265
      a[cnt] = A.point(base+ang);
```

```
266
      b[cnt] = B.point(base+ang);
267
      cnt++;
268
      a[cnt] = A.point(base-ang);
269
      b[cnt] = B.point(base-ang);
270
      cnt++;
271
      if(d2 == rsum*rsum) { //一条公切线
272
       a[cnt] = A.point(base);
       b[cnt] = B.point(PI+base);
273
       cnt++;
274
275
      } else if(d2 > rsum*rsum) {
                               //两条公切线
276
       double ang = acos((A.r + B.r) / sqrt(d2));
       a[cnt] = A.point(base+ang);
277
278
       b[cnt] = B.point(PI+base+ang);
279
       cnt++;
       a[cnt] = A.point(base-ang);
280
281
       b[cnt] = B.point(PI+base-ang);
282
       cnt++:
283
284
      return cnt;
285
286
287
    typedef vector<Point> Polygon;
288
289
    //点在多边形内的判定
290
    int isPointInPolygon(Point p, Polygon poly) {
291
      int wn = 0;
292
      int n = poly.size();
293
      for(int i = 0; i < n; i++) {
294
        if(OnSegment(p, poly[i], poly[(i+1)%n])) return -1; //在边界上
295
       int k = dcmp(Cross(poly[(i+1)%n]-poly[i], p-poly[i]));
       int d1 = dcmp(poly[i].y - p.y);
296
297
       int d2 = dcmp(poly[(i+1)%n].y - p.y);
298
       if(k > 0 \&\& d1 <= 0 \&\& d2 > 0) wn++;
299
       if(k < 0 \&\& d2 <= 0 \&\& d1 > 0) wn++;
300
      if(wn != 0) return 1;
301
                               //内部
302
      return 0;
                               //外部
303
304
305
    //凸包
306
    307
    * 输入点数组p,
                  个数为p, 输出点数组ch。 返回凸包顶点数
308
    * 不希望凸包的边上有输入点, 把两个<= 改成 <
309
    * 高精度要求时建议用dcmp比较
310
    * 输入点不能有重复点。函数执行完以后输入点的顺序被破坏
311
    int ConvexHull(Point *p, int n, Point* ch) {
312
313
      sort(p, p+n);
                      // 先 比 较 x 坐 标 , 再 比 较 y 坐 标
314
      int m = 0;
      for(int i = 0; i < n; i++) {
315
316
       while(m > 1 && Cross(ch[m-1] - ch[m-2], p[i]-ch[m-2]) <= 0) m--;
317
       ch\lceil m++\rceil = p\lceil i\rceil;
318
319
      int k = m;
320
      for(int i = n-2; i >= 0; i++) {
       while(m > k && Cross(ch[m-1] - ch[m-2], p[i]-ch[m-2]) <= 0) m--;
321
322
       ch[m++] = p[i];
323
324
      if(n > 1) m--;
325
      return m;
326
327
328
    //用有向直线A->B切割多边形poly, 返回"左侧"。 如果退化,可能会返回一个单点或者线段
329 //复杂度0(n2);
```

```
330
   |Polygon CutPolygon(Polygon poly, Point A, Point B) {
331
      Polygon newpoly;
332
      int n = poly.size();
333
      for(int i = 0; i < n; i++) {
334
        Point C = poly[i];
335
        Point D = poly[(i+1)\%n];
336
        if(dcmp(Cross(B-A, C-A)) >= 0) newpoly.push_back(C);
        if(dcmp(Cross(B-A, C-D)) != 0) {
337
338
          Point ip = GetLineIntersection(A, B-A, C, D-C);
339
          if(OnSegment(ip, C, D)) newpoly.push_back(ip);
340
        }
341
342
      return newpoly;
343
344
345
    //半平面交
346
347
    // 点p再 有 向 直 线 L 的 左 边 。 ( 线 上 不 算 )
348
    bool Onleft(Line L, Point p) {
349
      return Cross(L.v, p-L.p) > 0;
350
351
352
    //两直线交点,假定交点唯一存在
    Point GetIntersection(Line a, Line b) {
353
354
      Vector u = a.p - b.p;
355
      double t = Cross(b.v, u) / Cross(a.v, b.v);
356
      return a.p+a.v*t;
357
358
359
    int HalfplaneIntersection(Line* L, int n, Point* poly) {
360
      sort(L, L+n);
                                   //按极角排序
361
362
      int first, last;
                                   //双端队列的第一个元素和最后一个元素
363
      Point *p = new Point[n];
                                   //p[i]为q[i]和q[i+1]的交点
      Line *q = new Line[n];
364
                                   //双端队列
365
      q[first = last = 0] = L[0]; //队列初始化为只有一个半平面L[0]
366
      for(int i = 0; i < n; i++) {
367
        while(first < last && !Onleft(L[i], p[last-1])) last--;</pre>
368
        while(first < last && !Onleft(L[i], p[first])) first++;</pre>
369
        q[++last] = L[i];
        if(fabs(Cross(q[last].v, q[last-1].v)) < EPS) {</pre>
370
371
372
          if(Onleft(q[last], L[i].p)) q[last] = L[i];
373
374
        if(first < last) p[last-1] = GetIntersection(q[last-1], q[last]);</pre>
375
376
      while(first < last && !Onleft(q[first], p[last-1])) last--;</pre>
377
      //删除无用平面
378
      if(last-first <= 1) return 0;</pre>
379
      p[last] = GetIntersection(q[last], q[first]);
380
381
      //从deque复制到输出中
382
      int m = 0;
383
      for(int i = first; i \le last; i++) poly[m++] = p[i];
384
      return m;
385 | }
```

## 4 Graph

- 4.1 Tree
- 4.1.1 Universe

```
2
    /* find root(重心) */
 3
 4
    void findroot(int u, int fa) {
 5
      int i;
 6
      size[u] = 1;
 7
      f[u] = 0;
      for (i = last[u]; i; i = e[i][2]) {
 8
 9
        if (!vis[e[i][0]] && e[i][0] != fa) {
10
          findroot(e[i][0], u);
11
          size[u] += size[e[i][0]];
12
          if (f[u] < size[e[i][0]])
13
            f[u] = size[e[i][0]];
14
        }
15
      if (f[u] < ALL - size[u])
16
17
        f[u] = ALL - size[u];
18
      if (f[u] < f[root]) root = u;
19
20
21
   /* ---- da ---- */
22
23
    int dep[MAXN+1];
24
    int ancestor[MAXN+1][MAXLGN];
25
   int minw[MAXN+1][MAXLGN];
26
27
    void dfs(int u, int fa) {
28
      ancestor[u][0] = fa;
29
      dep[u] = dep[fa] + 1;
30
      for(int e = u[front]; e; e = E[e].n) {
31
        int v = E[e].v, w = E[e].w;
        if(v != fa) {
32
33
          minw[v][0] = w;
34
          dfs(v, u);
35
        }
36
      }
37
38
39
    void init_system(void) {
40
      int i = 0, w = 0;
41
      int t = 0;
42
      dep[0] = -1;
43
      dfs(1,0);
44
      for(w = 1; (t=(1 << w)) < N; ++w)
45
        for(i = 1; i \le N; ++i) if(dep[i] >= t) {
            ancestor[i][w] = ancestor[ancestor[i][w-1]][w-1];
46
47
            minw[i][w] = min(minw[i][w-1], minw[ancestor[i][w-1]][w-1]);
48
          }
49
50
    int query(int a, int b) {
51
52
      if(dep[a] < dep[b]) return query(b,a);</pre>
      else { /* now dep[s] > dep[t] */
53
        int i = 0;
54
55
        int maxbit = MAXLGN-1;
56
        int ret = INF;
57
        //while((1<<maxbit) <= dep[a]) maxbit++;</pre>
58
        /* first up a to same dep with b. */
59
        for(i = maxbit; i >= 0; i--)
60
          if(dep[a] - (1 << i) >= dep[b]) {
            ret = min(ret, minw[a][i]);
61
62
            a = ancestor[a][i];
63
64
        if(a == b) return ret;
```

```
65
        for(i = maxbit; i \ge 0; i - )
          if(dep[a] - (1 << i) >= 0 \& ancestor[a][i] != ancestor[b][i]) {
66
67
            ret = min(ret, min(minw[a][i], minw[b][i]));
68
            a = ancestor[a][i];
69
            b = ancestor[b][i];
70
71
        ret = min(ret, min(minw[a][0], minw[b][0]));
72
        return ret;
73
74
   4.1.2 Point Divide and Conquer
    Version 1
 1 |/* Tree::Point divide and conquer, by Abreto<m@abreto.net>. */
   #include <bits/stdc++.h>
 3
 4
   using namespace std;
 5
   typedef long long int ll;
 6
 7
   #define MAXN
                     (100001)
 8
   #define MAXV
                     (MAXN+1)
   #define MAXE
 9
                     (MAXN << 1)
10
   struct edge {
11
      int v;
12
      edge *n;
13
      edge(void):v(0),n(NULL) {}
14
      edge(int vv,edge *nn):v(vv),n(nn) {}
15
16
   int nE;
17
   edge E[MAXE];
   edge *front[MAXV];
18
   int label[MAXV];
19
                        /* 0 for '(', 1 for ')' */
20
   void add_edge(int u, int v) {
21
      int ne = ++nE;
22
      E[ne] = edge(v, u[front]);
23
      u[front] = \&(E[ne]);
24
   }
25
26
   int n;
27
   ll ans;
28
29
   char del[MAXV];
30
   namespace findroot {
31
   int ALL;
32
   int nfind;
33
   int vis[MAXV];
   int size[MAXV];
34
35
   int f[MAXV];
36
   int root;
37
    void __find(int u, int fa) {
38
      vis[u] = nfind;
39
      size[u] = 1;
40
      f[u] = 0;
41
      for(edge *e=u[front]; e; e = e->n) {
42
        int v = e \rightarrow v;
43
        if((!del[v]) && (vis[v] != nfind) && (v != fa)) {
44
          __find(v, u);
45
          size[u] += size[v];
46
          if(f[u] < size[v]) f[u] = size[v];
47
      }
48
```

```
49
       if(f[u] < ALL - size[u]) f[u] = ALL - size[u];
 50
       if(f[u] < f[root]) root = u;
 51
 52
    int find(int u, int all) {
 53
       ++nfind;
 54
       ALL = all;
 55
       f[root = 0] = MAXV;
 56
       __find(u,0);
 57
       return root;
 58
 59
 60
 61
    namespace workspaces {
 62
    int maxdep;
     int dep[MAXV];
 63
 64
    11 cntin[MAXV], cntout[MAXV];
 65
    int in[2][MAXV];
                          /* 0 for '(', 1 for ')' */
    int out[2][MAXV];
 66
 67
    void getdeep(int u, int fa) {
 68
       dep[u] = dep[fa] + 1;
 69
       if(dep[u] > maxdep) maxdep = dep[u];
 70
       for(edge *e = u[front]; e; e = e->n)
         if((!del[e->v]) \& (fa != e->v))
 71
 72
           getdeep(e->v, u);
 73
 74
    void dfs(int u, int fa) {
 75
       {
 76
         /* out from root */
 77
         out[0][u] = out[0][fa];
         out[1][u] = out[1][fa];
 78
 79
         if(0 == label[u]) { /* meet '(' */
 80
           out[0][u]++;
                    /* meet ')' */
 81
         } else {
           if(out[0][u]) out[0][u]--;
 82
 83
           else out[1][u]++;
 84
 85
         if(out[0][u] == 0)
 86
           cntout[out[1][u]]++;
 87
       }
 88
 89
         /* in to root */
 90
         in[0][u] = in[0][fa];
 91
         in[1][u] = in[1][fa];
 92
         if(0 == label[u]) { /* meet '(' */
 93
           if(in[1][u]) in[1][u]--;
 94
           else in[0][u]++;
 95
         } else { /* meet ')' */
 96
           in[1][u]++;
 97
 98
         if(0 == in[1][u])
 99
           cntin[in[0][u]]++;
100
101
       /* do something */
       for(edge *e = u[front]; e; e = e \rightarrow n) {
102
         int v = e \rightarrow v;
103
104
         if((!del[v]) \& (v != fa)) {
105
           dfs(v, u);
106
107
108
109
    inline void init_maxdep(void) {
110
       maxdep = 0;
111
112 | inline void update_maxdep(int u) {
```

```
113
       dep[u] = 1;
114
       if(dep[u] > maxdep) maxdep = dep[u];
115
       for(edge *e = u[front]; e; e = e->n)
116
         if((!del[e->v]))
117
           getdeep(e->v, u);
118
119
     inline void clear(void) {
120
       for(int i = 0; i \le maxdep+1; ++i)
121
         cntin[i] = cntout[i] = 0;
122
123
     inline void work(int u) {
       in[0][u] = in[1][u] = out[0][u] = out[1][u] = 0;
124
125
       in[label[u]][u] = out[label[u]][u] = 1;
126
       if(out[0][u] == 0) cntout[out[1][u]]++;
       if(0 == in[1][u]) cntin[in[0][u]]++;
127
128
       /* update in and out if neccessary */
129
       for(edge *e = u[front]; e; e = e->n)
130
         if(!(del[e->v]))
131
           dfs(e\rightarrow v, u);
132
133
    };
134
     11 count(int u, int p) {
135
       ll ret = 0;
136
137
       workspace::init_maxdep();
138
       workspace::update_maxdep(u);
139
       workspace::clear();
140
       if(-1 == p) {
141
         for(edge *e = u[front]; e; e = e->n)
142
           if((!(del[e->v])))
143
             workspace::work(e->v);
         p = label[u];
144
145
         /* single end */
146
         if(0 == p) ret = workspace::cntout[1];
147
         else ret = workspace::cntin[1];
148
       } else {
149
         workspace::work(u);
150
151
       if(0 == p) { /* p is '(' */
152
         for(int i = 0; i < workspace::maxdep; ++i) /* concatenation */
153
           ret += workspace::cntin[i] * workspace::cntout[i+1];
154
                  /* p is ')' */
155
         for(int i = 0; i < workspace::maxdep; ++i) /* concatenation */
156
           ret += workspace::cntin[i+1] * workspace::cntout[i];
157
158
       return ret;
159
160
161
    void handle(int u) {
162
       del[u] = 1; /* delete current root. */
       ans += count(u, -1);
163
164
       /* do something */
165
       for(edge *e = u[front]; e; e = e \rightarrow n) {
166
         int v = e \rightarrow v;
167
         if(!del[v]) {
168
           ans -= count(v, label[u]);
169
           /* do something */
170
           int r = findroot::find(v, findroot::size[v]);
171
           handle(r);
172
         }
173
       }
    }
174
175
176 | void proc(void) {
```

```
177
       int r = findroot::find(1,n);
178
       handle(r);
179
     }
180
181
     char ls[MAXV+1];
182
     int main(void) {
183
       int i = 0;
       scanf("%d", &n);
scanf("%s", ls);
for(i = 0; i < n; ++i)</pre>
184
185
186
         label[i+1] = ls[i] - '(';
187
188
       for(i = 1; i < n; ++i) {
         int ai, bi;
189
         scanf("%d<sub>\\\\</sub>%d", &ai, &bi);
190
191
         add_edge(ai, bi);
192
         add_edge(bi, ai);
193
       }
194
       proc();
       printf("%lld\n", ans);
195
196
       return 0;
197 |}
     Version 2
    //* 2016 ACM/ICPC Asia Regional Dalian. Problem , by Abreto<m@abreto.net>. */
  2
     #include <bits/stdc++.h>
  3
  4
     using namespace std;
  5
     typedef long long int 11;
  6
  7
     /* offset in [1,k] */
  8
     #define GET(i,offset)
                               (((i)>>((offset)-1))&1)
     #define SET(i,offset)
  9
                               ((i)|(1<<((offset)-1)))
 10
     #define REV(i,offset)
                               ((i)^(1<<((offset)-1)))
 11
 12
     #define MAXN
                       (50005)
 13
     #define MAXV
                       (MAXN+1)
     #define MAXE
                       (MAXN << 1)
 14
 15
     struct edge {
 16
       int v;
 17
       edge *n;
 18
       edge(void):v(0),n(NULL) {}
 19
       edge(int vv,edge *nn):v(vv),n(nn) {}
 20
     };
     int nE;
 21
     edge E[MAXE];
 22
 23
     edge *front[MAXV];
     int label[MAXV];
 24
                           /* each kind */
 25
     void add_edge(int u, int v) {
 26
       int ne = ++nE;
 27
       E[ne] = edge(v, u[front]);
 28
       u[front] = \&(E[ne]);
 29
 30
 31
     int n, k;
 32
     ll ans;
 33
     int all_kind;
 34
 35
     int ndel;
 36
    int del[MAXV];
    namespace findroot {
 37
 38
     int ALL;
 39
     ll nfind;
     ll vis[MAXV];
 40
 41 | int size[MAXV];
```

```
42
     int f[MAXV];
 43
     int root;
 44
     void __find(int u, int fa) {
 45
       vis[u] = nfind;
 46
       size[u] = 1;
 47
       f[u] = 0;
 48
       for(edge *e=u[front]; e; e = e->n) {
          int v = e \rightarrow v;
 49
 50
         if((del[v] != ndel) && (vis[v] != nfind) && (v != fa)) {
 51
           __find(v, u);
 52
           size[u] += size[v];
 53
           if(f[u] < size[v]) f[u] = size[v];
 54
         }
 55
       if(f[u] < ALL - size[u]) f[u] = ALL - size[u];
 56
 57
       if(f[u] < f[root]) root = u;
 58
 59
     int find(int u, int all) {
 60
       ++nfind;
       ALL = all;
 61
 62
       f[root = 0] = MAXV;
 63
       __find(u,0);
 64
       return root;
 65
 66
 67
 68
     namespace workspace {
 69
     ll cnt[1024];
 70
     int dp[MAXV];
 71
     void dfs(int u, int fa) {
 72
       dp[u] = dp[fa] \mid label[u];
       cnt[dp[u]] ++;
 73
 74
       /* dig into children */
 75
       for(edge *e = u[front]; e; e = e->n) {
 76
         int v = e \rightarrow v;
 77
         if((del[v] != ndel) && (v != fa)) {
 78
           dfs(v, u);
 79
 80
       }
 81
 82
     inline void clear(void) {
 83
       for(int i = 1; i \leftarrow all_kind; ++i)
 84
         cnt[i] = 0;
 85
     inline void work(int u) {
 86
       dp[u] = label[u];
 87
 88
       cnt[dp[u]] ++;
 89
       for(edge *e = u[front]; e; e = e \rightarrow n)
 90
         if((del[e->v] != ndel))
 91
           dfs(e\rightarrow v, u);
 92
 93
     inline void show(void) {
       for(int i = 0; i \leftarrow all_kind; ++i)
 94
 95
         printf("cnt[%d]_{\square}=_{\square}%lld\n", i, cnt[i]);
 96
       for(int i = 1; i <= n; ++i)
 97
         printf("dp[%d]_{\square}=_{\square}%d\n", i, dp[i]);
 98
 99
     };
100
101
102
     ll count(int u, int p) {
103
       ll ret = 0;
104
       workspace::clear();
105
       //printf("%d,%d :\n", u, p);
```

```
106
       if(-1 == p) {
107
         for(edge *e = u[front]; e; e = e->n)
108
           if(((del[e->v]) != ndel))
109
             workspace::work(e->v);
         p = label[u];
110
111
         /* single end */
112
         for(int i = 1; i <= all_kind; i++)
113
           if(all\_kind == (i|p))
              ret += (workspace::cnt[i]<<1);</pre>
114
115
       } else {
116
         workspace::work(u);
117
118
       //workspace::show();
119
       for(int i = 1; i \leftarrow all_kind; ++i)
120
         if( workspace::cnt[i] > 0 )
121
           for(int j = 1; j \leftarrow all_kind; ++j)
122
              if(all\_kind == (i|p|j))
123
                ret += workspace::cnt[i] * workspace::cnt[j];
124
       //printf("%lld\n", ret);
125
       return ret;
126
127
     void handle(int u) {
128
129
       //printf("proccessing %d\n", u);
130
       del[u] = ndel; /* delete current root. */
131
       ans += count(u, -1);
132
       /* do something */
133
       for(edge *e = u[front]; e; e = e \rightarrow n) {
134
         int v = e \rightarrow v;
135
         if(del[v] != ndel) {
           ans -= count(v, label[u]);
136
           /* do something */
137
138
           int r = findroot::find(v, findroot::size[v]);
139
           handle(r);
140
         }
141
142
143
     void proc(void) {
144
145
       int r = findroot::find(1,n);
146
       handle(r);
147
148
149
     void clear(void) {
150
       int i;
151
       ans = 0;
152
       nE = 0;
       for(i = 0; i \le n; ++i) {
153
154
         front[i] = NULL;
155
156
       //findroot::nfind = 0;
       ndel++;
157
158
159
160
     void mozhu(void) {
161
       int i = 0;
162
       int li;
163
       for(i = 1; i <= n; ++i) {
164
         scanf("%d", &li);
165
         label[i] = 1 << (li-1);
166
       for(i = 1; i < n; ++i) {
167
168
         int ai, bi;
169
         scanf("%d<sub>\\\\</sub>%d", &ai, &bi);
```

```
170
         add_edge(ai, bi);
171
         add_edge(bi, ai);
172
173
       all_kind = (1 << k)-1;
174
       proc();
175
       if(1 == k) ans += n;
176
       printf("%lld\n", ans);
177
178
179
     int main(void) {
       while( EOF != scanf("%d%d", &n, &k) ) {
180
         clear();
181
182
         mozhu();
183
184
       return 0;
185
     4.1.3 Hevay chain decompostion
    /* bzoj 1036 */
  2
     /* 树链剖分 */
  3
    #include <bits/stdc++.h>
  5
     using namespace std;
  6
  7
     #define MAXN
                      30030
  8
    #define MAXM
                      (MAXN << 1)
    struct edge {
  9
 10
       int v;
 11
       edge *n;
 12
       edge(void) {}
 13
       edge(int vv, edge *nn):v(vv),n(nn) {}
 14
 15
    typedef edge *ep;
 16
     int nE;
     edge E[MAXM];
 17
 18
     ep front[MAXN]:
 19
     void add_edge(int u, int v) {
 20
       int ne = ++nE;
 21
       E[ne] = edge(v, u[front]);
 22
       u[front] = \&(E[ne]);
 23
    }
 24
 25
     int n;
 26
     int fa[MAXN], son[MAXN], sz[MAXN], dep[MAXN];
 27
     int top[MAXN];
 28
     int id[MAXN];
 29
     int tot;
 30
 31
     void calc(int u, int uf) {
 32
       dep[u] = dep[uf] + 1;
 33
       fa[u] = uf;
 34
       sz[u] = 1;
       son[u] = -1;
 35
       for(ep e = u[front]; e; e = e->n) {
 36
 37
         if(e\rightarrow v != uf) {
 38
           calc(e->v, u);
 39
           sz[u] += sz[e->v];
 40
           if( -1 == son[u] \mid \mid sz[son[u]] < sz[e\rightarrow v])
 41
              son[u] = e \rightarrow v;
 42
         }
 43
       }
 44
    }
```

```
45
    void link(int u, int f) {
 46
       id[u] = (++tot);
 47
       top[u] = f;
 48
       if(son[u] > 0) {
 49
         link(son[u], f);
 50
 51
       for(ep e = u[front]; e; e = e \rightarrow n) {
 52
         if(e->v != fa[u] \&\& e->v != son[u]) {
 53
           link(e->v, e->v);
 54
 55
 56
 57
 58
    /* 其实是树链剖分 */
 59
    void make_link_cut_tree(void) {
 60
       calc(1, 0);
 61
       link(1, 1);
    }
 62
 63
 64
    int w[MAXN];
 65
    int sum[MAXN<<2], mx[MAXN<<2];</pre>
 66
 67
     void maintain(int o, int l, int r) {
 68
       sum[o] = sum[o << 1] + sum[o << 1|1];
 69
       mx[o] = max(mx[o<<1], mx[o<<1|1]);
 70
 71
    void build(int o = 1, int l = 1, int r = n) {
 72
       if(r == 1) {
 73
         sum[o] = w[l];
 74
         mx[o] = w[l];
 75
       } else {
 76
         int mid = 1+r>>1;
 77
         build(o<<1, l, mid);
         build(o<<1|1, mid+1, r);
 78
 79
         maintain(o, l, r);
 80
 81
 82
     void update(int p, int x, int o = 1, int l = 1, int r = n) {
       if(p \ll 1 \& r \ll p) {
 83
         sum[o] = x;
 84
 85
         mx[o] = x;
 86
       } else {
 87
         int mid = 1+r>>1;
 88
         if(p \le mid) update(p,x,o <<1,1,mid);
 89
         else update(p,x,o<<1|1,mid+1,r);
 90
         maintain(o,l,r);
 91
       }
 92
 93
     int qs(int L, int R, int o = 1, int l = 1, int r = n) {
 94
       if(R < 1 | I r < L) return 0;
 95
       else if (L <= 1 \&\& r <= R) {
 96
         return sum[o];
 97
       } else {
98
         int mid = 1+r>>1;
 99
         return qs(L,R,o<<1,l,mid)+qs(L,R,o<<1|1,mid+1,r);
100
101
102
     int qm(int L, int R, int o = 1, int l = 1, int r = n) {
103
       if(L \le 1 \&\& r \le R) {
104
         return mx[o];
105
       } else {
106
         int mid = 1+r>>1;
107
         if(R \le mid) return qm(L, R, o<<1, l, mid);
108
         else if (L > mid) return qm(L, R, o<<1|1, mid+1, r);
```

```
109
         else return max(qm(L, R, o <<1, l, mid), qm(L, R, o <<1|1, mid+1, r));
       }
110
111
    }
112
113
     void change(int u, int t) {
114
       update(id[u], t);
115
116
     int qmax(int u, int v) {
117
       int ret = -10000000000;
118
       while(top[u] != top[v]) {
119
         if( dep[top[u]] > dep[top[v]] ) {
120
           /* jump u */
121
           ret = max(ret, qm(id[top[u]], id[u]));
122
           u = fa[top[u]];
123
         } else {
124
           ret = max(ret, qm(id[top[v]], id[v]));
125
           v = fa[top[v]];
         }
126
       }
127
128
       ret = max(ret, qm(min(id[u],id[v]),max(id[u],id[v])));
129
       return ret;
130
131
     int qsum(int u, int v) {
       int ret = 0;
132
133
       while(top[u] != top[v]) {
134
         if( dep[top[u]] > dep[top[v]] ) {
135
           /* jump u */
136
           ret += qs(id[top[u]], id[u]);
           u = fa[top[u]];
137
138
         } else {
139
           ret += qs(id[top[v]], id[v]);
140
           v = fa[top[v]];
141
         }
       }
142
143
       ret += qs(min(id[u],id[v]),max(id[u],id[v]));
144
       return ret;
145
146
147
     int main(void) {
148
       int i;
       scanf("%d", &n);
149
150
       for(i = 1; i < n; ++i) {
151
         int a, b;
152
         scanf("%d%d", &a, &b);
153
         add_edge(a, b);
154
         add_edge(b, a);
155
156
       make_link_cut_tree();
157
       for(i = 1; i <= n; ++i) {
         scanf("%d", &(w[id[i]]));
158
159
       build();
160
       scanf("%d", &i);
161
       while(i---) {
162
163
         char command[8];
         int a, b;
164
         scanf("%s<sub>\\\\</sub>%d<sub>\\\</sub>%d", command, &a, &b);
165
         if('C' == command[0]) change(a, b);
166
         else if ('M' == command[1]) printf("%d\n", qmax(a, b));
167
         else if ('S' == command[1]) printf("%d\n", qsum(a, b));
168
169
170
       return 0;
171
```

### 4.2 2-SAT

```
|#include <bits/stdc++.h>
 3
   using namespace std;
 4
 5
   namespace two_sat {
    const int maxn = 100000;
 6
 7
    const int maxm = 1000000;
 8
   struct edge {
 9
      int v;
10
      edge *n;
11
      edge(void):v(0),n(NULL) {}
12
      edge(int vv, edge *nn):v(vv),n(nn) {}
13
   typedef edge *ep;
14
15
   int n;
16
   int nE;
17
   edge E[maxm];
18
   ep front[maxn];
19
   void add_edge(int u, int v) {
20
      int ne = ++nE;
21
      E[ne] = edge(v, u[front]);
      u[front] = \&(E[ne]);
22
23
24
   /* (x = xval or y = yval), indexed from 0 */
25
   void add_clause(int x, int xv, int y, int yv) {
26
     x = x*2 + xv;
27
      y = y*2 + yv;
      add_edge(x^1, y);
28
29
      add_edge(y^1, x);
30
   }
31
32
   char mark[maxn<<1];</pre>
33
   int S[maxn << 1], c;
34
   void init(int N) {
35
      n = N;
36
      for(int i = 0; i < n*2; ++i) {
37
        i[front] = NULL;
38
        i[mark] = 0;
39
40
     nE = 0;
41
42
   int dfs(int x) {
43
44
      if(mark[x^1]) return 0;
45
      if(mark[x]) return 1;
46
      mark[x] = 1;
47
      S[c++] = x;
      for(ep e = x[front]; e; e = e->n)
48
49
        if(!dfs(e->v)) return 0;
50
      return 1;
51
52
    int solve(void) {
53
54
      for(int i = 0; i < n*2; i += 2)
55
        if(!mark[i] && !mark[i+1]) {
56
          c = 0;
57
          if(!dfs(i)) {
            while(c > 0) mark[S[--c]] = 0;
58
59
            if(!dfs(i+1)) return 0;
          }
60
        }
61
62
      return 1;
```

```
63 |}
64 |}
```

# 4.3 Cut Edge and Point

```
Finding cut edges
 2
   The code below works properly because the lemma above (first lemma):
 3
     h[root] = 0
 4
                par[v] = -1
 5
                         dfs (v):
 6
                          d[v] = h[v]
 7
                                 color[v] = gray
 8
                                          for u in adj[v]:
 9
                                              if color[u] == white
10
                                                 then par[u] = v and dfs(u) and d[v] = min(
                                                    d[v], d[u])
                                                     if d[u] > h[v]
11
12
                                                       then the edge v-u is a cut edge
13
                                                       else if u != par[v])
14
              then d[v] = min(d[v], h[u])
15
                           color[v] = black
16
                                      In this code, h[v] = height of vertex v in the DFS
                                         tree and d[v] = min(h[w] where there is at least
                                         vertex u in subtree of v in the DFS tree where
                                          there is an edge between u and w).
17
18
                                          Finding cut vertices
19
                                          The code below works properly because the lemma
                                              above (first lemma):
20
                                          h[root] = 0
21
                                                     par[v] = -1
                                                         dfs (v):
22
23
                                                         d[v] = h[v]
24
                                                             color[v] = gray
25
                                                       for u in adj[v]:
26
                                                                 if color[u] == white
                                                                   then par[u] = v and dfs(
27
                                                                       u) and d[v] = min(d[v])
                                                                       ], d[u])
28
                                                                          if d[u] >= h[v]
                                                                             and (v != root
                                                                             number_of_children
                                                                             (v) > 1)
29
                                                                            then the edge v
                                                                               is a cut
                                                                               vertex
                                                                            else if u != par
30
                                                                               [v]
31
                    then d[v] = min(d[v], h[u])
32
                                 color[v] = black
33
                                            In this code, h[v] = 1 height of vertex v in
                                                the DFS tree and d[v] = \min(h[w]) where
                                                there is at least vertex u in subtree of v
                                                in the DFS tree where there is an edge
                                                between u and w).
```

## 4.4 Euler Path

```
1 |/* Euler path, by Abreto<m@abreto.net>. */
2 |#define MAXV (1024)
```

```
3
   #define MAXE
                     (MAXV*MAXV)
 4
 5
   typedef struct {
 6
      int id;
 7
      int nxt;
 8
      int del;
 9
    } egde_t;
   int front[MAXV];
10
   egde_t edg[MAXE];
11
12
   int d[MAXV];
13
   int ind[MAXV], outd[MAXV];
14
   int nedges;
15
   void add_edge(int u, int v) {
16
      int newedge = ++nedges;
17
      edg[newedge].id = v;
18
      edg[newedge].nxt = u[front];
19
      edg[newedge].del = 0;
20
      u[front] = newedge;
21
      outd[u]++;
22
      ind[v]++;
23
      d[u]++;
24
      d[v]++;
25
26
   void del_edge(int u, int v) {
27
      int e = 0;
28
      for(e=u[front]; e; e=edg[e].nxt)
29
        if(edg[e].id==v) {
30
          edg[e].del = 1;
          outd[u]--;
31
32
          ind[v]--;
33
          d[u]--;
34
          d[v]=;
35
          return;
36
        }
37
38
39
   int path[MAXV];
40
   int l;
41
42
   void add2path(int u) {
43
      path[l++] = u;
44
45
46
   /* Directed graph */
47
   void euler(int x) {
48
      if(outd[x]) {
49
        int e = 0;
50
        for(e=x[front]; e; e=edg[e].nxt)
51
          if(!edg[e].del) {
52
            int v = edg[e].id;
            del_edge(x,v);
53
54
            euler(v);
55
56
57
      add2path(x);
58
59
60
   /* Undirected graph */
61
   void euler(int x) {
62
      if(d[x]) {
63
        int e = 0;
64
        for(e=x[front]; e; e=edg[e].nxt)
65
          if(!edg[e].del) {
66
            int v = edg[e].id;
```

```
67
            del_edge(x,v);
68
            del_edge(v,x);
69
            euler(v);
70
71
     add2path(x);
72
73
   4.5 Shortest Path
   4.5.1 Dijkstra
   /* Shortest Path Dijstra, by Abreto<m@abreto.net>. */
   #include <cstdio>
 2
 3
   #include <set>
 4
   #include <utility>
 5
   using namespace std;
 7
   typedef set< pair<int,int> > spii;
 8
 9
   #define MAXN
                     512
10
   #define MAXV
                     (MAXN*MAXN)
11
12
   struct egde_t {
13
     int id;
14
     int nxt;
15
16
   int front[MAXV];
17
   egde_t edg[MAXV<<3];
18
   int nedges;
19
   void add_edge(int u, int v) {
20
      int newedge = ++nedges;
21
     edg[newedge].id = v;
22
     edg[newedge].nxt = u[front];
23
     u[front] = newedge;
24
25
26
   int d[MAXV];
27
   int vis[MAXN];
28
   int solid[MAXV];
29
30
   int dijstra(int s, int t) {
31
     int v = s[front];
32
     spii q;
33
     q.insert(make_pair(0, s));
34
     while(!q.empty()) {
35
        auto it = q.begin();
36
        int u = it->second;
37
        int v = u[front];
38
        q.erase(it);
39
        solid[u] = 1;
        if(u == t) break;
40
        while(v) {
41
42
          int w = edg[v].id;
43
          if(!solid[w]) {
44
            if( (0==d[w]) | (d[u] + 1 < d[w]) ) {
45
              q.erase(make_pair(d[w],w));
46
              d[w] = d[u] + 1;
47
              q.insert(make_pair(d[w],w));
            }
48
49
50
          v = edg[v].nxt;
51
```

```
52
53
      return d[t];
54 | }
   4.5.2 Shortest Path Fast Algorithm
   //* Shortest Path Fast Algorithm, by Abreto<m@abreto.net>. */
 2
   #include <cstdio>
 3
   #include <cstring>
 4
   #include <queue>
   #include <utility>
 6
 7
   using namespace std;
 8
 9
   #define MAXN
                     128
10
11
   struct edge {
12
      int v;
13
      int w;
14
      int n;
15
16
   edge edg[MAXN<<1];</pre>
   int nedg;
17
18
   int indegree[MAXN];
19
   int front[MAXN];
20
   int find_edge(int u, int v) {
21
      int e = u[front];
22
      while(e) {
23
        if(edg[e].v == v) return e;
24
        e = edg[e].n;
25
26
      return 0;
27
28
   void add_edge(int u, int v, int w) {
29
      int e = find_edge(u,v);
30
      if(0==e) {
31
        int newnode = ++nedq;
        edg[newnode].v = v;
32
33
        edg[newnode].w = w;
34
        edg[newnode].n = u[front];
35
        u[front] = newnode;
36
        indegree[v]++;
37
      } else {
38
        edg[e].w = (w < edg[e].w)?w:(edg[e].w);
39
40
   }
41
42
   int n;
43
44
   char inq[MAXN];
45
   int vis[MAXN];
46
    int d[MAXN];
    int spfa(int s) { /* return 1 if fuhuan exists. */
47
48
      queue<int> q;
49
      memset(inq, 0, sizeof(inq));
50
      memset(d, -1, sizeof(d));
51
      memset(vis, 0, sizeof(vis));
52
      d[s] = 0;
53
      inq[s] = 1;
54
      q.push(s);
55
      while(!q.empty()) {
        int u = q.front();
56
57
        q.pop();
```

```
58
        printf("proc<sub>\\\\</sub>d..\n", u);
59
        inq[u] = 0;
60
        if(vis[u]++ > n)
61
          return 1;
62
        for(int e = front[u]; e; e = edg[e].n) {
63
          int v = edg[e].v, w = edg[e].w;
          if(-1=d[v] | | d[u] + w < d[v]) {
64
            d[v] = d[u] + w;
65
            if(!inq[v]) {
66
67
              inq[v] = 1;
68
              q.push(v);
69
            }
70
          }
        }
71
72
73
      return 0;
74
    4.5.3 K-th shortest path
 1 |/**
 2
    * poj
 3
    * Problem#2449
 4
    * Accepted
 5
    * Time: 250ms
 6
    * Memory: 9252k
 7
    */
 8
   #include <iostream>
 9
   #include <fstream>
10
   #include <sstream>
11
   #include <algorithm>
   #include <cstdio>
12
13
   #include <cstdlib>
   |#include <cstring>
15
   #include <ctime>
   #include <cctype>
16
17
   #include <cmath>
18
   #include <vector>
19
   #include <queue>
20
   #include <stack>
21
   |#include <map>
22
   #include <set>
23
   #include <bitset>
24
   using namespace std;
25
   typedef bool boolean;
26
27
   typedef class Edge {
28
   public:
29
      int end;
30
      int next;
31
      int w;
32
33
      Edge(int end = 0, int next = -1, int w = 0):end(end), next(next), w(w) {
                                                                                           }
34
   } Edge;
35
36
   const int N = 1e3, M = 1e5;
37
38
   typedef class MapManager {
39
   public:
40
      int cnt;
      int h[N + 5];
41
42
      Edge edge[M + 5];
43
```

```
MapManager() {
 44
 45
       MapManager(int n):cnt(-1) {
 46
    //
                   h = new int[(n + 1)];
 47
    //
                   edge = new Edge[(m + 1)];
 48
         memset(h, -1, sizeof(int) * (n + 1));
 49
 50
 51
       inline void addEdge(int u, int v, int w) {
 52
         edge[++cnt] = (Edge(v, h[u], w));
 53
                   h[u] = (signed)edge.size() - 1;
 54
         h[u] = cnt;
       }
 55
 56
 57
       inline int start(int node) {
 58
         return h[node];
 59
 60
 61
       Edge& operator [] (int pos) {
 62
         return edge[pos];
 63
 64
     } MapManager;
 65
    #define m_endpos -1
 66
 67
     int n, m;
 68
    MapManager g;
 69
    MapManager rg;
 70
    int s, t, k;
 71
    int ds[N + 5];
 72
 73
    inline void init() {
 74
       scanf("%d%d", &n, &m);
       memset(g.h, -1, sizeof(int) * (n + 1));
 75
 76
       memset(rg.h, -1, sizeof(int) * (n + 1));
 77
       for(int i = 1, u, v, w; i \le m; i++) {
         scanf("%d%d%d", &u, &v, &w);
 78
 79
         g.addEdge(u, v, w);
 80
         rg.addEdge(v, u, w);
 81
 82
       scanf("%d%d%d", &s, &t, &k);
 83
           ds = new int[(n + 1)];
 84
    }
 85
 86
    #define g rg
 87
    #define f ds
 88
    #define que que1
 89
    boolean vis[N + 5];
 90
    queue<int> que;
 91
    boolean spfa(int s, int t) {
 92
       memset(f, 0x7f, sizeof(int) * (n + 1));
 93
       memset(vis, false, sizeof(boolean) * (n + 1));
 94
       que.push(s);
 95
       f[s] = 0;
96
       while(!que.empty()) {
 97
         int e = que.front();
 98
         que.pop();
 99
         vis[e] = false;
100
         for(int i = g.start(e); i != m_endpos; i = g[i].next) {
           int& eu = g[i].end;
101
                   cout << e << " " << eu << " " << i <<endl;
102
    //
103
           if(f[e] + g[i].w < f[eu]) {
104
             f[eu] = f[e] + g[i].w;
             if(!vis[eu]) {
105
106
               que.push(eu);
107
               vis[eu] = true;
```

```
108
             }
109
           }
         }
110
111
       return (f[t] != 0x7f7f7f7f);
112
113
114
     #undef g
115
     #undef f
116
    #undef que
117
118
     typedef class Status {
119
    public:
120
       int node;
121
       int dis;
122
       int priority;
123
124
       Status(int node = 0, int dis = 0):node(node), dis(dis), priority(h()) {
                                                                                           }
125
126
       int h() {
127
         return dis + ds[node];
128
129
130
       boolean operator < (Status b) const {</pre>
131
         return priority > b.priority;
132
133
    } Status;
134
135
    int label[N + 5];
136
    priority_queue<Status> que;
137
     int bfs(int s, int t) {
138
       if(s == t)
                     k++;
139
           label = new int[(n + 1)];
140
       memset(label, 0, sizeof(int) * (n + 1));
141
       que.push(Status(s, 0));
142
       while(!que.empty()) {
143
         Status e = que.top();
144
         que.pop();
145
         label[e.node]++;
         if(e.node == t && label[e.node] == k)
146
147
           return e.dis;
148
         for(int i = g.start(e.node); i != m_endpos; i = g[i].next) {
149
           if(label[q[i].end] < k)
150
             que.push(Status(g[i].end, e.dis + g[i].w));
         }
151
       }
152
153
       return -1;
154
155
156
     inline void solve() {
157
       if(!spfa(t, s)) {
158
         puts("-1");
159
         return;
160
       printf("%d", bfs(s, t));
161
162
163
164
    int main() {
165
       init();
166
       solve();
167
       return 0;
168
```

### 4.6 Maxflow

```
/* Max Flow Problem, by Abreto<m@abreto.net> */
 3
   #include <bits/stdc++.h>
 4
   using namespace std;
 5
 6
   #define MAXV
                     (100000)
 7
   #define MAXE
                     (1000000)
 8
   struct edge {
 9
      static int N;
10
      int v, w;
11
      edge *n;
12
      edge(void):v(0),w(0),n(NULL) {}
      edge(int vv, int ww, edge *nn):v(vv),w(ww),n(nn) {}
13
14
15
   int nE;
   edge E[MAXE];
16
17
   edge *front[MAXV];
   void add_edge(int u, int v, int w) {
18
19
      int ne = ++nE;
20
      E[ne] = edge(v, w, u[front]);
21
      u[front] = \&(E[ne]);
22
   edge *find_edge(int u, int v) {
23
24
      for(edge *e = u[front]; e != NULL; e = e->n)
25
        if(e\rightarrow v == v)
26
          return e;
27
      return NULL;
28
29
   void grant_e(int u, int v, int w) {
30
      edge *e = find_edge(u, v);
31
      if(NULL == e) add_edge(u,v,w);
32
      else e\rightarrow w += w;
33
   }
34
35
   int vis[MAXV];
    int path[MAXV];
36
37
    int dfs(int u, int t) {
38
      vis[u] = 1;
39
      if(u == t) return 1;
40
      for(edge *e = u[front]; e != NULL; e = e->n) {
41
        int v = e \rightarrow v;
42
        if(!vis[v] \&\& e->w \&\& dfs(v,t)) {
43
          path[u] = v;
44
          return 1;
45
        }
46
      }
47
      return 0;
48
49
   int find_path(int s, int t) {
50
      memset(vis, 0, sizeof(vis));
51
      return dfs(s,t);
52
    int max_flow(int s, int t) {
53
54
      int flow = 0;
      while(find_path(s,t)) {
55
56
        int i = 0;
57
        int minf = find_edge(s,path[s])->w;
58
        for(i = path[s]; i != t; i = path[i])
          minf = min(minf, find_edge(i,path[i])->w);
59
        for(i = s; i != t; i = path[i]) {
60
61
          grant_e(i, path[i], -minf);
62
          grant_e(path[i], i, minf);
```

```
63
64
        flow += minf;
65
 66
      return flow;
67
    }
68
69
    /* Dinic */
 70
    #define N 1000
 71
    #define INF 100000000
72
73
    struct Edge {
74
      int from, to, cap, flow;
75
      Edge(int u,int v,int c,int f):from(u),to(v),cap(c),flow(f) {}
76
    };
77
 78
    struct Dinic {
79
      int n,m,s,t;//结点数,边数(包括反向弧),源点编号,汇点编号
80
      vector<Edge>edges;//边表, dges[e]和dges[e^1]互为反向弧
81
      vector<int>G[N];//邻接表,G[i][j]表示结点i的第j条边在e数组中的编号
82
      bool vis[N]; //BFS的使用
83
      int d[N]; //从起点到i的距离
84
      int cur[N]; //当前弧下标
85
86
      void addedge(int from,int to,int cap) {
87
        edges.push_back(Edge(from, to, cap, 0));
88
        edges.push_back(Edge(to,from,0,0));
        int m=edges.size();
89
90
        G[from].push_back(m-2);
91
        G[to].push_back(m-1);
92
      }
93
      bool bfs() {
94
95
        memset(vis,0,sizeof(vis));
96
        queue<int>Q;
97
        Q.push(s);
98
        d[s]=0;
99
        vis[s]=1;
100
        while(!Q.empty()) {
101
          int x=Q.front();
102
          Q.pop();
103
          for(int i=0; i<G[x].size(); i++) {
104
            Edge&e=edges[G[x][i]];
105
            if(!vis[e.to]&&e.cap>e.flow) { //只考虑残量网络中的弧
106
              vis[e.to]=1;
107
              d[e.to]=d[x]+1;
108
              Q.push(e.to);
109
            }
          }
110
111
112
113
        return vis[t];
114
115
      int dfs(int x,int a) { //x表示当前结点, a表示目前为止的最小残量
116
117
        if(x==t||a==0)return a;//a等于0时及时退出,此时相当于断路了
118
        int flow=0,f;
119
        for(int&i=cur[x]; i<G[x].size(); i++) { //从上次考虑的弧开始, 注意要使用引用, 同
           时修改cur[x]
120
          Edge&e=edges[G[x][i]];//e是一条边
121
          if(d[x]+1==d[e.to]&&(f=dfs(e.to,min(a,e.cap-e.flow)))>0) {
122
            e.flow+=f;
123
            edges[G[x][i]^1].flow==f;
124
            flow+=f;
125
            a=f;
```

```
126
            if(!a)break;//a等于0及时退出, 当a!=0,说明当前节点还存在另一个曾广路分支。
127
128
          }
        }
129
130
        return flow;
131
132
133
      int Maxflow(int s,int t) { //主过程
134
        this->s=s,this->t=t;
135
        int flow=0;
136
        while(bfs()) { //不停地用bfs构造分层网络, 然后用dfs沿着阻塞流增广
137
          memset(cur,0,sizeof(cur));
          flow+=dfs(s,INF);
138
139
        }
140
        return flow;
141
      }
142
    };
143
    /* ISAP */
144
145
    struct Edge {
146
      int from, to, cap, flow;
147
    };
148
    const int maxn=650;
149
    const int INF=0x3f3f3f3f;
150
    struct ISAP {
151
      int n,m,s,t;//结点数,边数(包括反向弧),源点编号,汇点编号
152
      vector<Edge>edges;
153
      vector<int>G[maxn];
154
      bool vis[maxn];
155
      int d[maxn];
156
      int cur[maxn];
157
      int p[maxn];
158
      int num[maxn];
159
      void AddEdge(int from,int to,int cap) {
160
        edges.push_back((Edge) {
161
          from, to, cap, 0
162
        });
163
        edges.push_back((Edge) {
164
          to, from, 0,0
165
        });
166
        m=edges.size();
167
        G[from].push_back(m-2);
168
        G[to].push_back(m-1);
169
170
      bool RevBFS() {
171
        memset(vis,0,sizeof(vis));
172
        queue<int>Q;
173
        Q.push(t);
174
        d[t]=0;
        vis[t]=1;
175
176
        while(!Q.empty()) {
177
          int x=Q.front();
178
          Q.pop();
           for(int i=0; i<G[x].size(); i++) {
179
180
            Edge &e =edges[G[x][i]^1];
181
            if(!vis[e.from]&&e.cap>e.flow) {
182
              vis[e.from]=1;
183
               d[e.from]=d[x]+1;
184
               Q.push(e.from);
185
            }
186
          }
187
188
        return vis[s];
189
```

```
190
       int Augment() {
191
         int x=t, a=INF;
192
         while(x!=s) {
193
           Edge &e = edges[p[x]];
           a= min(a,e.cap-e.flow);
194
195
           x=edges[p[x]].from;
196
197
         x=t;
         while(x!=s) {
198
199
           edges[p[x]].flow+=a;
200
           edges[p[x]^1].flow=a;
201
           x=edges[p[x]].from;
202
         }
203
         return a;
204
205
       int Maxflow(int s,int t,int n) {
206
         this->s=s,this->t=t,this->n=n;
207
         int flow=0;
208
         RevBFS();
209
         memset(num,0,sizeof(num));
         for(int i=0; i<n; i++) {
210
211
           num[d[i]]++;
212
213
         int x=s;
214
         memset(cur,0,sizeof(cur));
215
         while(d[s]<n) {</pre>
216
           if(x==t) {
217
             flow+=Augment();
218
             X=S;
219
220
           int ok=0;
221
           for(int i=cur[x]; i<G[x].size(); i++) {
222
             Edge &e =edges[G[x][i]];
223
             if(e.cap>e.flow&d[x]==d[e.to]+1) {
224
               ok=1;
225
               p[e.to]=G[x][i];
226
               cur[x]=i;
227
               x=e.to;
228
               break;
229
             }
230
231
           if(!ok) {
232
             int m=n-1;
233
             for(int i=0; i<G[x].size(); i++) {
234
               Edge &e =edges[G[x][i]];
235
               if(e.cap>e.flow)
236
                 m=min(m,d[e.to]);
237
238
             if(--num[d[x]]==0)
239
               break;
240
             num[d[x]=m+1]++;
241
             cur[x]=0;
242
             if(x!=s)
243
               x=edges[p[x]].from;
244
245
246
         return flow;
247
       }
248
249
    int main() {
250
       int n,m,a,b,c,res;
       while(scanf("%d%d",&m,&n)!=EOF) {
251
252
         ISAP tmp;
253
         for(int i=0; i<m; i++) {
```

```
254
           scanf("%d%d%d",&a,&b,&c);
255
           tmp.AddEdge(a,b,c);
256
257
         res=tmp.Maxflow(1,n,n);
258
         printf("%d\n", res);
259
260
       return 0;
261
         Strongly Connected Component
    /* Kosaraju */
  2
     #define MAXN
                      10010
    #define MAXM
  3
                      100010
  4
    struct edge {
  5
       int v;
  6
       edge *n;
  7
       edge(void):v(0),n(NULL) {}
  8
       edge(int vv, edge *nn):v(vv),n(nn) {}
  9
 10
     int nE;
     edge E[MAXM<<1];</pre>
 11
 12
     edge *ori[MAXN];
 13
     edge *inv[MAXN];
 14
     void add_edge(edge *front[], int u, int v) {
 15
       int ne = ++nE;
 16
       E[ne] = edge(v, u[front]);
 17
       u[front] = \&(E[ne]);
 18
 19
     void connect(int u, int v) {
 20
       add_edge(ori, u, v);
 21
       add_edge(inv, v, u);
 22
 23
 24
     int vis[MAXN];
 25
     int vst[MAXN];
     void first_dfs(int u, int &siq) {
 26
 27
       vis[u] = 1;
 28
       for(edge *e = u[ori]; e; e = e \rightarrow n)
 29
         if(!vis[e->v])
 30
           first_dfs(e->v, sig);
 31
       vst[++sig] = u;
 32
 33
     int mark[MAXN];
 34
     void second_dfs(int u, int sig) {
 35
       vis[u] = 1;
 36
       mark[u] = sig;
 37
       for(edge *e = u[inv]; e; e = e \rightarrow n)
 38
         if(!vis[e->v])
 39
           second_dfs(e->v, sig);
 40
 41
 42
     int N, M;
 43
 44
     int kosaraju(void) {
 45
       int i;
 46
       int sig = 0;
 47
       for(i = 0; i \le N; ++i) vis[i] = 0;
       for(i = 1; i \le N; ++i) {
 48
         if(!vis[i])
 49
 50
           first_dfs(i, sig);
 51
 52
       sig = 1;
```

```
53
       for(i = 0; i \le N; ++i) vis[i] = 0;
 54
       for(i = N; i > 0; --i) {
 55
         if(!vis[vst[i]])
 56
           second_dfs(vst[i], sig++);
 57
       for(i = 1; i \le N; ++i)
 58
 59
         if(mark[i] != 1)
 60
           return 0:
       return 1;
 61
 62
 63
 64
     void clear(void) {
 65
 66
       nE = 0;
       for(int i = 0; i <= N; ++i) {
 67
 68
         ori[i] = inv[i] = NULL;
 69
 70
     }
 71
 72
     /* Tarjan */
 73
     #define MAXN
                      10010
 74
     #define MAXM
                      100010
 75
     struct edge {
 76
       int v;
 77
       edge *n;
 78
       edge(void):v(0),n(NULL) {}
 79
       edge(int vv, edge *nn):v(vv),n(nn) {}
 80
 81
    typedef edge *ep;
 82
     int nE;
     edge E[MAXM];
 83
 84
     edge *front[MAXN];
 85
     void add_edge(int u, int v) {
 86
       int ne = ++nE;
 87
       E[ne] = edge(v, u[front]);
 88
       u[front] = \&(E[ne]);
 89
 90
 91
     int mark[MAXN];
 92
     int dfn[MAXN], low[MAXN];
 93
     int stk[MAXN];
 94
     int stk_top;
 95
 96
     void tardfs(int u, int stamp, int &scc) {
 97
       mark[u] = 1;
 98
       dfn[u] = low[u] = stamp;
       stk[stk\_top++] = u;
 99
100
       for(ep e = u[front]; e; e = e->n) {
101
         if(0 == mark[e \rightarrow v]) tardfs(e \rightarrow v, ++stamp, scc);
         if(1 == mark[e\rightarrow v]) low[u] = min(low[u], low[e\rightarrow v]);
102
103
       if(dfn[u] == low[u]) {
104
105
         ++SCC;
106
         do {
           low[stk[stk_top-1]] = scc;
107
           mark[stk[stk\_top-1]] = 2;
108
109
         } while(stk[(stk_top--)-1] != u);
110
111
112
113
     int tarjan(int n) {
       int scc = 0, lay = 1;
114
115
       for(int i = 1; i <= n; ++i)
116
         if(0 == mark[i])
```

```
117
           tardfs(i, lay, scc);
118
       return scc;
119
    }
120
121
    int N, M;
122
123
     void clear(void) {
124
       nE = 0;
125
       for(int i = 0; i <= N; ++i) {
126
         i[front] = NULL;
127
         mark[i] = low[i] = 0;
128
129
       stk\_top = 0;
130
131
132
    /* Garbow */
133
    #define MAXN
                     10010
134
    #define MAXM
                     100010
135
136
    struct edge {
137
       int v;
138
       edge *n;
       edge(void):v(0),n(NULL) {}
139
140
       edge(int vv, edge *nn):v(vv),n(nn) {}
141
142
    typedef edge *ep;
143
144
    int nE;
145
    edge E[MAXM];
146
    edge *front[MAXN];
147
    void add_edge(int u, int v) {
148
       int ne = ++nE;
149
       E[ne] = edge(v, u[front]);
150
       u[front] = \&(E[ne]);
151
    }
152
     int stk1[MAXN], stk1t;
153
154
     int stk2[MAXN], stk2t;
155
    int low[MAXN], belg[MAXN];
156
157
    void garbowdfs(int u, int lay, int &scc) {
158
       stk1[++stk1t] = u;
159
       stk2[++stk2t] = u;
160
       low[u] = ++lay;
161
       for(ep e=u[front]; e; e = e->n) {
162
         if(!low[e->v]) garbowdfs(e->v, lay, scc);
163
         else if (0 == belg[e->v])
164
           while(low[stk2[stk2t]] > low[e->v])
165
             ---stk2t;
166
       if(stk2[stk2t] == u) {
167
         stk2t—;
168
169
         scc++;
170
         do {
           belg[stk1[stk1t]] = scc;
171
172
         } while(stk1[stk1t--] != u);
173
174
175
176
     int grabow(int n) {
177
       int i;
178
       int scc = 0, lay = 0;
179
       for(i = 0; i <= n; ++i) {
180
         belg[i] = low[i] = 0;
```

```
181
182
       for(i = 1; i \le n; ++i)
183
         if(0 == low[i])
184
           garbowdfs(i, lay, scc);
185
       return scc;
186
187
188
    int N, M;
189
190
    void clear(void) {
191
       nE = 0;
192
       for(int i = 0; i <= N; ++i) {
193
         front[i] = NULL;
194
195
```

# 4.8 Perfect elimination ordering

求弦图的最大团数/最小色数的时候,只要在完美消除序列上从后往前贪心染色即可。 而求最大独立集/最小团覆盖的时候,只要在完美消除序列上从前往后贪心取点即可。

```
1
   /**
 2
    * BZ0J 1006
 3
    * 「HNOI2008 ] 神奇的国度
    * 最大势法求完美消除序列
 5
    * by Abreto<m@abreto.net>.
    **/
 6
 7
   #include <cassert>
   #include <cstdio>
 8
 9
   #include <vector>
10
   #include <bitset>
11
   |#include <algorithm>
12
13
   using namespace std;
14
   typedef vector<int> vi;
15
   typedef vi::iterator vii;
   #define pb push_back
16
   #define MAXN 10100
17
   #define MAXM 1000100
18
19
20
   int n;
21
   vi g[MAXN];
22
   int ans;
23
24
   struct node_t {
25
      int v;
26
      node_t *nxt;
27
    } node[MAXM << 2];</pre>
28
   |int used;
29
   node_t *new_node(void) {
30
      return node + (used ++);
31
   }
32
33
   node_t *f[MAXN]; /* head */
34
   void lkto(int pos, int item) {
35
      node_t *t = new_node();
36
      t \rightarrow v = item;
37
      t\rightarrow nxt = f[pos];
38
      f[pos] = t;
39
40
41
   |int usedby[MAXN];
42 | int color[MAXN];
```

```
43
   |bitset<MAXN> added;
44
   int label[MAXN], max_label;
45
   void mcs(void) {
46
      for (int i = 1; i \le n; i++) lkto(0, i);
47
     for (int i = n; i > 0; i ---) {
48
        node_t *cur = f[max_label];
49
        assert(cur != NULL);
50
        while (added.test(cur->v)) { /* already added */
51
          cur = cur->nxt;
52
          while (NULL == cur)
53
            cur = f[ --max_label ];
54
55
        f[ max_label ] = cur->nxt;
        while (max_label && NULL == f[max_label]) max_label—;
56
57
        int u = cur->v;
58
        added.set(u);
59
        /* the i-th is u */
        for (vii it = g[u].begin(); it != g[u].end(); it++) {
60
61
          int v = *it;
          if (!added.test(v)) {
62
63
            label[v] ++;
64
            max_label = max(max_label, label[v]);
65
            lkto(label[v], v);
66
67
          usedby[color[v]] = i;
68
69
70
        for (int j = 1; j <= n; j++)
          if (usedby[j] != i) {
71
72
            color[u] = j;
73
            break;
74
75
        ans = max(ans, color[u]);
76
     }
77
   }
78
79
   int main(void) {
80
     int m;
      scanf("%d%d", &n, &m);
81
82
     while (m--) {
83
        int ai, bì;
        scanf("%d%d", &ai, &bi);
84
85
        g[ai].pb(bi);
86
        g[bi].pb(ai);
     }
87
88
     mcs();
     printf("%d\n", ans);
89
90
      return 0;
91 |}
       Math
   5
        Euler Function
   /* Euler function phi(x), by Abreto<m@abreto.net>. */
 1
 2
 3
   #define MAXX
                    3000000
 4
 5
   int phi[MAXX];
 6
   void get_euler(void) {
 7
     int i = 0, j = 0;
     phi[1] = 1;
```

```
9
     for(i = 2; i < MAXX; ++i)
10
        if(!phi[i])
11
          for(j = i; j < MAXX; j += i) {
12
            if(!phi[j]) phi[j] = j;
13
            phi[j] = phi[j]/i * (i-1);
14
15
   }
   5.2 Möbius Function
 1
   void sieve() {
 2
      fill(isPrime, isPrime + maxn, 1);
 3
     mu[1] = 1, num = 0;
     for (int i = 2; i < maxn; ++i) {
 4
 5
        if (isPrime[i]) primes[num++] = i, mu[i] = -1;
 6
        static int d;
 7
        for (int j = 0; j < num && (d = i * primes[j]) < maxn; ++j) {
          isPrime[d] = false;
 8
 9
          if (i % primes[j] == 0) {
            mu[d] = 0;
10
11
            break;
12
          } else mu[d] = -mu[i];
13
14
15
        Number Theory Inverse
   |#include <bits/stdc++.h>
 2
   using namespace std;
 3
 4
   const int n=10000000;
 5
   const long long mod=1e9+7; /* prime required. */
 6
   long long fact[n],fiv[n],inv[n];
 7
 8
   int main() {
9
10
     fact[0]=fact[1]=1;
     fiv[0]=fiv[1]=1;
11
12
     inv[1]=1;
13
     for (int i=2; i<n; i++) {
14
        fact[i]=fact[i-1]*i%mod;
15
        inv[i]=(mod-mod/i)*inv[mod%i]%mod;
16
        fiv[i]=inv[i]*fiv[i-1]%mod;
17
18
      for (int i=1; i<n; i++) {
        if (fact[i]*fiv[i]%mod!=1) printf("fact_wrong:_wd\n",i);
19
                                     printf("intv_wrong: _\%d\n",i);
20
        if (inv[i]*i%mod!=1)
21
22
     cout<<"complete"<<endl;</pre>
23
      return 0;
24
```

## 5.4 Chinese Remainder Theorem

 $x \equiv a_i \pmod{m_i}$ 

```
/* Chinese Remainder Theorem, by Abreto<m@abreto.net>. */
 1
 2
   #include "euler.c"
 3
 4
   #define MAXN
 5
 6
   typedef long long int ll;
 7
 8
   11 quickpow(ll a, ll b, ll mod) {
9
     ll ret = 1, base = a;
10
     while(b > 0) {
11
        if(b & 1) ret = (ret * base) % mod;
12
        base = (base * base) \% mod;
13
        b >>= 1;
14
15
     return ret;
16
   }
17
18
   11 N;
19
   ll a[MAXN], m[MAXN]; /* a and m is indexed from 0. */
20
   11 \times, M;
21
22
   void naive_crt(void) {
23
     int i = 0;
24
     11 Mi[MAXN], nMi[MAXN];
25
     11 t[MAXN];
26
27
     M = 1;
28
     for(i = 0; i < N; ++i)
29
        M *= a[i];
      for(i = 0; i < N; ++i)
30
       Mi[i] = M / a[i];
31
32
     get_euler();
33
     for(i = 0; i < N; ++i)
34
        nMi[i] = quickpow(Mi[i], phi[a[i]]-1, a[i]);
35
      for(i = 0; i < N; ++i)
36
        t[i] = ((a[i] * Mi[i]) % M) * nMi[i] % M;
37
     for(i = 0; i < N; ++i)
38
        x = (x + t[i]) % M;
39 | }
        Linear congruences
   5.5
   |#include <cstdio>
 1
 2
   #include <cassert>
 3
   #include <cstdlib>
 4
 5
   using namespace std;
 6
 7
   class mod_equ_resolver {
 8
     typedef long long int ll;
 9
     11 a, m;
10
     inline void gurantee(void) {
        if (a < 0) {
11
12
          11 k = (-a) / m;
13
          a += (k + 111) * m;
14
          a = (a + m) \% m;
15
        } else {
16
          a \% = m;
17
        // printf("x = %lld (mod %lld)\n",a, m);
18
19
   public:
20
     mod_equ_resolver(void) {
21
```

```
22
        a = 011;
23
        m = 111;
24
25
      11 exgcd(ll m, ll n, ll &x, ll &y) {
26
        if (0 == n) {
          x = 1;
27
28
          y = 0;
29
          return m;
30
31
        ll g = exgcd(n, m % n, x, y);
32
        ll t = x;
        x = y;
33
34
        y = t - m / n * y;
35
        return g;
36
37
      int onemore(ll a2, ll m2) {
38
        11 x, y;
39
        ll g = exgcd(m, m2, x, y);
40
        assert(x*m+y*m2==q);
41
        a2 = (a2 + m2) \% m2;
        if ( abs(a2 - a) \% g ) return -1;
42
        ll newm = m / g * m2;
43
44
        11 newa = a + (a2 - a) / g * x * m;
45
        a = newa;
46
        m = newm;
47
        gurantee();
48
        return 0;
49
50
      ll resolve(void) {
51
        return a;
52
53 | };
    Usage: For
                                          x \equiv a_1 \mod m_1
   run
 1 |mod_equ_resolver solver;
   for (int i = 1; i \le k; i++)
        solver.onemore(a[i], m[i]);
    then the solution is
                                    x \equiv solver.a \mod solver.m
   5.6 FFT
   |#include <cmath>
 2
   using namespace std;
 3
   namespace fft {
   #define eps (1e-9)
   template < typename T = double >
   struct dbl {
 6
 7
      Tx;
 8
      dbl(void):x(0.0) {}
 9
      template <typename U>
10
      dbl(U a):x((T)a) {}
11
      inline char sgn(void) {
12
        return ((x)=-eps)&(x<=eps))?(0):((x>eps)?(1):(-1));
13
```

```
14
     inline T tabs(void) {
15
        return ((x \ge -eps) \& (x \le eps))?(0.0):((x \ge eps)?(x):(-x));
16
17
     inline dbl abs(void) {
18
        return dbl(tabs());
19
20
     template <typename U> inline dbl &operator=(const U b) {
21
        x=(T)b;
22
        return (*this);
23
24
     inline T *operator&(void) {
25
        return &x;
26
27
     inline dbl operator-(void) const {
28
        return dbl(-x);
29
30
     inline dbl operator+(const dbl &b) const {
31
        return dbl(x+b.x);
32
33
     inline dbl operator—(const dbl &b) const {
34
        return dbl(x-b.x);
35
36
     inline dbl operator*(const dbl &b) const {
37
        return dbl(x*b.x);
38
39
     inline dbl operator/(const dbl &b) const {
40
        return dbl(x/b.x);
41
42
     template <typename U> inline dbl operator^(const U &b) const {
43
        T ret=1.0, base=x;
        while(b) {
44
45
          if(b&1)ret*=base;
46
          base*=base;
47
          b>>=1;
48
        }
49
        return dbl(ret);
50
51
     inline dbl operator+=(const dbl &b) {
52
        return dbl(x+=b.x);
53
54
     inline dbl operator—=(const dbl &b) {
55
        return dbl(x-=b.x);
56
57
     inline dbl operator*=(const dbl &b) {
58
        return dbl(x*=b.x);
59
60
     inline dbl operator/=(const dbl &b) {
61
        return dbl(x/=b.x);
62
     template <typename U> inline dbl operator^=(const U &b) {
63
64
        dbl tmp=(*this)^b;
65
        *this=tmp;
66
        return tmp;
67
68
     inline bool operator==(const dbl &b) const {
        return (0 == ((*this)-b).sgn());
69
70
71
     inline bool operator!=(const dbl &b) const {
72
        return (0 != ((*this)-b).sgn());
73
74
     inline bool operator<(const dbl &b) const {
75
        return (-1 == ((*this)-b).sgn());
76
     inline bool operator<=(const dbl &b) const {
77
```

```
78
         return (((*this)==b) || ((*this)<b));
 79
 80
      inline bool operator>(const dbl &b) const {
 81
         return (b < (*this));
 82
 83
      inline bool operator>=(const dbl &b) const {
 84
         return (((*this)==b) || ((*this)>b));
 85
 86
      template <typename U> inline operator U() const {
 87
         return (U)x;
 88
 89
       inline char operator[](unsigned n) {
 90
         if(n >= 0) {
 91
           long long int ret=x;
 92
           while(n--) {
 93
             ret/=10;
 94
 95
           return (ret%10);
 96
         } else {
 97
           T ret=x;
 98
           n=-n;
 99
           while(n-)ret*=10.0;
           return ((long long int)ret)%10;
100
101
102
103
    };
104
    template <typename T>
105
    struct Complex {
106
       T x,y; /* x + iy */
      Complex(void):x(T()),y(T()) {}
107
108
      Complex(T xx):x(xx) {}
      Complex(T xx,T yy):x(xx),y(yy) {}
109
110
       inline Complex operator—(void) const {
111
         return Complex(-x,-y);
112
113
      inline Complex operator+(const Complex& b) const {
114
         return Complex(x+b.x,y+b.y);
115
      inline Complex operator-(const Complex& b) const {
116
117
         return Complex(x-b.x,y-b.y);
118
119
      inline Complex operator*(const Complex& b) const {
120
         return Complex(x*b.x-y*b.y,x*b.y+y*b.x);
121
122
      inline Complex operator/(const Complex& b) const {
123
         T bo=b.x*b.x+b.y*b.y;
124
         return Complex((x*b.x+y*b.y)/bo,(y*b.x-x*b.y)/bo);
125
126
      inline Complex& operator+=(const Complex& b) {
127
         Complex tmp=(*this)+b;
128
         (*this)=tmp;
129
         return (*this);
130
       inline Complex& operator—=(const Complex& b) {
131
132
         Complex tmp=(*this)_b;
133
         (*this)=tmp;
134
         return (*this);
135
136
      inline Complex& operator*=(const Complex& b) {
137
         Complex tmp=(*this)*b;
138
         (*this)=tmp;
139
         return (*this);
140
      inline Complex& operator/=(const Complex& b) {
141
```

```
142
         Complex tmp=(*this)/b;
143
         (*this)=tmp;
144
         return (*this);
145
       inline friend Complex operator+(const T& a, const Complex& b) {
146
147
         return Complex(a)+b;
148
149
       inline friend Complex operator—(const T& a, const Complex& b) {
150
         return Complex(a)-b;
151
152
       inline friend Complex operator*(const T& a, const Complex& b) {
153
         return Complex(a)*b;
154
155
       inline friend Complex operator/(const T& a, const Complex& b) {
156
         return Complex(a)/b;
157
       }
158
     };
159
    typedef dbl<> Double;
160
     typedef Complex<Double> ComplexD;
161
     typedef long long int ll;
162
     const int maxn = 2000000; /* !! */
163
     const Double pi(acos(-1.0));
164
165
     void build(ComplexD _P[], ComplexD P[], int n, int m, int curr, int &cnt) {
166
       if(m == n) {
167
         _P[curr] = P[cnt++];
168
       } else {
169
         build(_P, P, n, m*2, curr, cnt);
170
         build(_P, P, n, m*2, curr+m, cnt);
171
172
    }
173
174
     void FFT(ComplexD P[], int n, int oper) { /* n should be 2^k. */
175
       static ComplexD _P[maxn];
176
       int cnt = 0;
       build(_P, P, n, 1, 0, cnt);
177
       copy(_P, _P+n, P);
for(int d = 0; (1<<d)<n; ++d) {</pre>
178
179
180
         int m = 1 << d;
         int m2 = m*2;
181
182
         Double p0 = pi / m * oper;
183
         ComplexD unit_p0(cos(p0.x), sin(p0.x));
184
         for(int i = 0; i < n; i += m2) {
185
           ComplexD unit(1,0);
           for(int j = 0; j < m; ++j) {
186
187
             ComplexD &P1 = P[i+j+m], &P2 = P[i+j];
188
             ComplexD t = unit * P1;
             P1 = P2 - t;
189
190
             P2 = P2 + t;
191
             unit *= unit_p0;
192
           }
         }
193
194
       if(-1 == oper) {
195
196
         for(int i = 0; i < n; ++i)
197
           P[i] /= Double(n);
198
199
200
```

#### 5.7 NTT

```
2
   |#define ll long long
 3
   const int N=262144;
   const ll MOD=50000000001507329LL;//998244353 1004535809
   using namespace std;
 6
   int n,m;
 7
   ll a[N],b[N],x[N],y[N];
 8
   ll wn[25];
 9
    ll Mul(ll x, ll y) { //乘法超ll用快速乘, 主函数也需要用
10
      ll ans=(x*y-(ll)((long double)x/MOD*y+1e-8)*MOD);
11
      return ans<0?ans+MOD:ans;</pre>
12
13
   ll Qpow(ll a,ll b,ll M) {
14
      ll ans=1;
15
      a%=M;
      while(b) {
16
17
        if(b&1) ans=Mul(ans,a);
18
        a=Mul(a,a);
19
        b>>=1;
20
      }
21
      return ans;
22
    void Getwn() { //主函数预处理getwn()
23
24
      for(int i=0; i<25; i++) {
25
        wn[i]=Qpow(3,(MOD-1)/(1<< i),MOD);
26
27
28
    void NTT(ll *x,int n,int rev) {
29
      int i,j,k,ds;
30
      ll w,u,\vee;
31
      for(i=1, j=n>>1, k=n>>1; i< n-1; i++, k=n>>1) {
        if(i<j) swap(x[i],x[j]);
32
33
        while(j>=k) j==k,k>>=1;
34
        if(j < k) j += k;
35
36
      for(i=2,ds=1; i<=n; i<<=1,ds++) {
37
        for(j=0; j<n; j+=i) {
38
          w=1;
39
          for(k=j; k< j+i/2; k++) {
40
            u=x[k];
41
            v=Mul(w,x[k+i/2]);
42
            x[k]=(u+v)\%MOD;
43
            x[k+i/2]=(u-v+MOD)%MOD;
44
            w=Mul(w,wn[ds]);
          }
45
        }
46
47
      if(rev==-1) {
48
49
        for(i=1; i<n/2; i++) swap(x[i],x[n-i]);
50
        w=Qpow(n,MOD-2,MOD);
51
        for(i=0; i<n; i++) x[i]=Mul(x[i],w);
52
      }
53
54
    int main() {
55
      Getwn();
56
      while(~scanf("%d%d",&n,&m)) {
        for(int i=0; i<n; i++)scanf("%lld",&a[i]);</pre>
57
58
        for(int i=0; i<m; i++)scanf("%lld",&b[i]);
59
        int len=1,s=n+m;
60
        while(len<s)len<<=1;</pre>
61
        for(int i=n; i<len; i++)a[i]=0;
        for(int i=m; i<len; i++)b[i]=0;
62
63
        NTT(a, len, 1);
64
        NTT(b,len,1);
        for(int i=0; i<len; i++)a[i]=Mul(a[i],b[i]);
65
```

```
66
        NTT(a, len, -1);
 67
         68
        puts("");
 69
      }
 70
    }
 71
 72
 73
    #include<cstdio>
 74
    #include<iostream>
 75
    #include<cstring>
 76
    #include<cmath>
 77
    #include<complex>
 78
    using namespace std;
 79
    typedef long long LL;
    const LL MOD=998244353,g=3,gi=332748118;
 80
 81
    const LL N=1000005;
 82
    LL n,m;
 83
    LL a[N],b[N];
 84
    LL pow (LL x,LL y) {
 85
      if (y==1) return x;
 86
      LL lalal=pow(x,y>>1);
 87
      lalal=lalal*lalal%MOD;
 88
      if (y&1) lalal=lalal*x%MOD;
 89
      return lalal;
 90
 91
    void ntt (LL *a,LL n,LL o) {
 92
      if (n==1) return;
 93
      LL k=(n>>1);
 94
      LL w=1, wn=pow(o==1?g:gi, (MOD-1)/n), a0[k], a1[k];
 95
      for (LL u=0; u< k; u++) {
 96
         LL i=u*2
 97
        a0[u]=a[i]:
 98
        a1[u]=a[i+1];
99
100
      ntt(a0,k,o);
101
      ntt(a1,k,o);
102
      for (LL u=0; u< k; u++) {
103
        a[u]=a0[u]+w*a1[u]%MOD;
104
        a[u]=(a[u]\%MOD+MOD)\%MOD;
105
        a[u+k]=a0[u]-w*a1[u];
106
        a[u+k]=(a[u+k]%MOD+MOD)%MOD;
107
        w=w*wn%MOD;
108
      }
109
110
    void ntt(LL *a,LL n,LL op) {
111
      for (LL u=0; u<n; u++) bin[u]=(bin[u>>1]>>1)|((u&1)*(n>>1));
112
      for (LL u=0; u<n; u++) if (u<bin[u]) swap(a[u],a[bin[u]]);
113
      for (LL u=1; u<n; u<<=1) {
114
        LL wn=pow(op==1?g:gi,(MOD-1)/(u<<1)),w,t;
         for (LL i=0; i<n; i=i+(u<<1)) {
115
116
          w=1;
117
           for (LL k=0; k<u; k++) {
118
             t=w*a[u+i+k]%MOD;
             a[u+i+k]=(a[i+k]-t+MOD)%MOD;
119
120
             a[i+k]=(a[i+k]+t)%MOD;
121
             w=w*wn%MOD;
122
        }
123
124
125
      if(op==-1) {
126
         LL Inv=pow(n,MOD-2);
127
         for(LL i=0; i<n; i++) a[i]=a[i]*Inv%MOD;
128
      }
129
```

```
130
131
     int main() {
       scanf("%I64d%I64d",&n,&m);
132
       for (LL u=0; u<=n; u++) scanf("%I64d",&a[u]);
133
134
       for (LL u=0; u<=m; u++) scanf("%I64d",&b[u]);
135
       m=m+n;
136
       n=1;
       while (n <= m) n << = 1;
137
138
       ntt(a,n,1);
139
       ntt(b,n,1);
140
       for (LL u=0; u<=n; u++) a[u]*=b[u];
141
       ntt(a,n,-1);
142
       LL inv=pow(n,MOD-2);
143
       for (LL u=0; u<=m; u++) printf("%I64d_{\perp}",a[u]*inv%MOD);
144
       return 0;
145
    }
```

## 5.8 Fast Walsh-Hadamard transform

异或

$$\mathcal{F}\{A\} = [\mathcal{F}\{A_0\} + \mathcal{F}\{A_1\}, \mathcal{F}\{A_0\} - \mathcal{F}\{A_1\}]$$
$$\mathcal{F}^{-1}\{A\} = \left[\mathcal{F}^{-1}\{\frac{A_0 + A_1}{2}\}, \mathcal{F}^{-1}\{\frac{A_0 - A_1}{2}\}\right]$$

• 按位与

$$\mathcal{F}\{A\} = [\mathcal{F}\{A_0\} + \mathcal{F}\{A_1\}, \mathcal{F}\{A_1\}]$$
$$\mathcal{F}^{-1}\{A\} = [\mathcal{F}^{-1}\{A_0\} - \mathcal{F}^{-1}\{A_1\}, \mathcal{F}^{-1}\{A_1\}]$$

• 按位或

$$\mathcal{F}\{A\} = [\mathcal{F}\{A_0\}, \mathcal{F}\{A_1\} + \mathcal{F}\{A_0\}]$$
$$\mathcal{F}^{-1}\{A\} = [\mathcal{F}^{-1}\{A_0\}, \mathcal{F}^{-1}\{A_1\} - \mathcal{F}^{-1}\{A_0\}]$$

```
void FWT(int a[],int n) {
 1
 2
      for(int d=1; d<n; d<<=1)
 3
        for(int m=d<<1,i=0; i<n; i+=m)
 4
           for(int j=0; j<d; j++) {
 5
             int x=a[i+j], y=a[i+j+d];
 6
             a[i+j]=(x+y) \mod , a[i+j+d]=(x-y+mod) \mod ;
 7
             //xor:a[i+j]=x+y,a[i+j+d]=(x-y+mod)%mod;
 8
             //and:a[i+j]=x+y;
 9
             //or:a[i+j+d]=x+y;
10
11
12
13
    void UFWT(int a[],int n) {
      for(int d=1; d<n; d<<=1)
14
        for(int m=d << 1, i=0; i < n; i+=m)
15
          for(int j=0; j<d; j++) {
  int x=a[i+j],y=a[i+j+d];</pre>
16
17
             a[i+j]=1LL*(x+y)*rev%mod, a[i+j+d]=(1LL*(x-y)*rev%mod+mod)%mod;
18
19
             //xor:a[i+j]=(x+y)/2,a[i+j+d]=(x-y)/2;
20
             //and:a[i+j]=x-y;
21
             //or:a[i+j+d]=y-x;
22
23
24
    void solve(int a[],int b[],int n) {
25
      FWT(a,n);
26
      FWT(b,n);
27
      for(int i=0; i<n; i++) a[i]=1LL*a[i]*b[i]%mod;
```

```
28
     UFWT(a,n);
29 }
   5.9 Lucas
   /* Lucas, by Abreto<m@abreto.net>. */
 3
   struct __lucas {
 4
      static const int maxp = 100000;
 5
      typedef long long int ll;
 6
      int p;
 7
     int f[maxp]; // fiv[maxp], inv[maxp];
 8
     inline int mul(const int a, const int b) {
 9
        ll z = 1ll * a * b;
        z = z / p * p;
10
11
        return z;
12
13
     int qow(int a, int x) {
        int ret = 1;
14
15
        while (x) {
16
          if (1 & x) ret = mul(ret, a);
17
          a = mul(a, a);
18
         x >>= 1;
        }
19
20
        return ret;
21
22
     void init(int np) {
23
        p = np;
24
        // return; // uncomment this line if use binom()
25
        f[0] = f[1] = 1;
        // fiv[0] = fiv[1] = 1;
26
        // inv[1] = 1;
27
28
        for (int i = 2; i < p; i++) {
          f[i] = mul(f[i - 1], i);
29
30
          // inv[i] = mul(p - p / i, inv[p % i]);
31
          // fiv[i] = mul(fiv[i - 1], inv[i]);
32
33
34
     int C(int n, int k) {
35
        if (n < k) return 0;
        return mul(f[n], qow(mul(f[k], f[n - k]), p - 2));
36
37
38
     /** use following if get TLE { */
39
     int binom(int n, int k) {
40
        if (n < k) return 0;
41
        if (k > n - k) k = n - k;
        int a = 1, b = 1;
42
        while (k) {
43
          a = mul(a, n);
44
45
          b = mul(b, k);
46
         n--;
47
         k---;
48
        }
49
        return mul(a, qow(b, p - 2));
50
51
      /** } ___ */
52
     int operator()(int n, int k) {
53
        if (0 == k) return 1;
54
        if (n  return <math>C(n, k);
55
        return mul(C(n % p, k % p), (*this)(n / p, k / p));
57
   |} lucas;
```

## 5.10 Linear Programming

```
|/* 线性规划 */
   #include<bits/stdc++.h>
3
4
   using namespace std;
5
   const int Maxn=110, Maxm=59;
6
   class Simplex {
7
     /*
8
        功能:
9
        接受有n个约束, m个基本变量的方程组a[0~n][0~m]
10
        a [0] [] 存放需要最大化的目标函数, a [] [0] 存放常数
11
        Base [] 存放基本变量的id, 初始为1~m
12
        Rest □ 存放松弛变量的id,初始为m+1~m+n
13
        返 回 此 线 性 规 划 的 最 小 值 ans
14
        要求方案的话, Base[]中的变量值为0,Rest[]中的变量值为相应行的[0]
15
        如果solve
16
        返回1,说明运行正常ans是它的最大值
17
        返回0,说明无可行解
18
        返回-1,说明解没有最大值
19
        测试:
20
        m=2, n=3
        double a[4][3] = {
21
22
        {0,1,3},
23
        \{8,-1,1\},
24
        \{-3,1,1\},
25
        \{2,1,-4\}
26
        };
27
        solve=1, ans=64/3;
28
        注意ac不了可能是eps的问题
29
   public:
30
31
     static const double Inf;
32
     static const double eps;
33
     int n,m;
     double a[Maxn][Maxm];
34
35
     int Base[Maxm], Rest[Maxn];
36
     double val[Maxm];
37
     double ans;
     void pt() {
38
39
       for(int i=0; i<=n; i++) {
40
         for(int j=0; j<=m; j++)printf(\%.2f_{\square},a[i][j]);
41
         puts("");
42
       }
43
     }
44
     void pivot(int x,int y) { //将第x个非基本变量和第y个基本变量调换
45
       swap(Rest[x],Base[y]);
46
       double tmp=-1./a[x][y];
47
       a[x][y] = -1.;
48
       for(int j=0; j<=m; j++)a[x][j]*=tmp;
       for(int i=0; i<=n; i++) {
49
50
         if(i==x||fabs(a[i][y])<eps)continue;</pre>
51
         tmp=a[i][y];
52
         a[i][y]=0;
         for(int j=0; j<=m; j++)a[i][j]+=tmp*a[x][j];
53
54
       }
55
56
     bool opt() {
57
       while(1) {
58
         int csi=0;
59
         for(int i=1; i<=m; i++)if(a[0][i]>eps&&(!csi||Base[i]<Base[csi]))csi=i;
60
         if(!csi)break;
61
         int csj=0;
         double cur;
62
```

```
63
           for(int j=1; j<=n; j++) {
 64
             if(a[j][csi]>-eps)continue;
 65
             double tmp=-a[j][0]/a[j][csi];
 66
             if(!csj||tmp+eps<cur||(fabs(tmp-cur)<eps&&Rest[j]<Rest[csj]))csj=j,cur=tmp;
 67
 68
           if(!csj)return 0;
 69
           pivot(csj,csi);
 70
 71
         ans=a[0][0];
 72
         return 1;
 73
 74
       bool init() {
 75
         ans=0;
 76
         for(int i=1; i<=m; i++)Base[i]=i;
 77
         for(int i=1; i<=n; i++)Rest[i]=m+i;</pre>
 78
         int cs=1;
         for(int i=2; i<=n; i++)if(a[i][0]<a[cs][0])cs=i;
 79
 80
         if(a[cs][0]>=-eps)return 1;
 81
         static double tmp[Maxm];
 82
         for(int i=0; i<=m; i++)tmp[i]=a[0][i],a[0][i]=0;
 83
         for(int i=1; i<=n; i++)a[i][m+1]=1.;
 84
         a[0][m+1]=-1.;
 85
         Base[m+1]=m+n+1;
 86
         pivot(cs,++m);
 87
         opt();
 88
         m--;
 89
         if(a[0][0] \leftarrow eps) return 0;
 90
         cs=-1:
 91
         for(int i=1; i<=n; i++) {
 92
           if(Rest[i]>m+n) {
 93
             cs=i;
 94
             break;
 95
           }
 96
         if(cs>=1) {
 97
 98
           int nxt=-1;
 99
           m++;
100
           for(int i=1; i<=m; i++)if(a[cs][i]>eps||a[cs][i]<-eps) {
101
               nxt=i;
102
               break;
103
104
           pivot(cs,nxt);
105
           m--;
106
107
         for(int i=1; i<=m; i++) {
108
           if(Base[i]>m+n) {
109
             swap(Base[i],Base[m+1]);
110
             for(int j=0; j<=n; j++)a[j][i]=a[j][m+1];
111
             break;
           }
112
113
114
         for(int i=1; i<=m; i++)a[0][i]=0;
115
         a[0][0]=tmp[0];
         for(int i=1; i<=m; i++)if(Base[i]<=m)a[0][i]=tmp[Base[i]];
116
117
         for(int i=1; i<=n; i++) {
118
           if(Rest[i]<=m) {
119
             for(int j=0; j<=m; j++)a[0][j]+=tmp[Rest[i]]*a[i][j];
120
           }
121
         }
122
         return 1;
123
124
       void getval() {
125
         for(int i=1; i<=m; i++)val[i]=0;
126
         for(int i=1; i<=n; i++)if(Rest[i]<=m)val[Rest[i]]=a[i][0];
```

```
127
        //for(int i=1;i<=m;i++)printf("%.2f ",val[i]);puts("");</pre>
128
129
      int solve() {
130
        if(!init())return 0;
131
        if(!opt())return -1;
132
         getval();
133
         return 1;
134
135
    } solver;
136
    const double Simplex:: Inf=1e80;
137
    const double Simplex:: eps=1e-8;
138
    int main() {
139
       int m,n,type;
       scanf("%d%d%d",&m,&n,&type);
140
141
       solver.a[0][0]=0;
142
      for(int i=1; i<=m; i++)scanf("%lf",&solver.a[0][i]);
143
      for(int i=1; i<=n; i++) {
144
        for(int j=1; j<=m+1; j++) {
           if(j==m+1)scanf("%lf",&solver.a[i][0]);
145
146
           else {
             scanf("%lf",&solver.a[i][j]);
147
148
             solver.a[i][j]=-solver.a[i][j];
149
150
        }
151
      }
152
      solver.m=m, solver.n=n;
153
      int rep=solver.solve();
154
      if(rep==0)puts("Infeasible");
155
      else if(rep==-1)puts("Unbounded");
156
      else {
         printf("%.12f\n", solver.ans);
157
158
        if(type==1) {
159
           for(int i=1; i<=m; i++)printf("%.12f%c",solver.val[i],i==m?'\n':'u');
160
161
      }
162
    |}
    5.11 Big Prime Test
  1 |#include <iostream>
    |#include <cstdlib>
  3
    using namespace std;
  4
    typedef long long LL;
    LL minfactor, p[11] = \{2, 3, 5, 7, 11, 13, 17, 19, 23, 29\};
  5
  6
    LL gcd(LL a, LL b) {
  7
       return b ? gcd(b, a % b) : a;
  8
  9
    LL qmult(LL a, LL b, LL mod) { // 快速乘模
 10
      LL sum = 0;
 11
      while (b) {
 12
        if (b & 1) {
 13
           sum += a;
           if (sum >= mod) sum -= mod; // 此处无需用%, %运算比减法慢很多
 14
 15
 16
        b >>= 1, a <<= 1;
 17
        if (a >= mod) a -= mod;
 18
      }
 19
      return sum;
 20
 21
    LL qpow(LL a, LL b, LL mod) { // 快速幂模
 22
       LL res = 1;
 23
      while (b) {
 24
        if (b & 1) res = qmult(res, a, mod);
```

```
25
       b >>= 1;
26
       a = qmult(a, a, mod);
27
28
     return res;
29
   bool prime_test(LL n, LL a) { // 对整数n,底数a进行测试,返回true表示通过测试
30
31
     LL p = qpow(a, n - 1, n);
     if (p!= 1) return false;
32
33
     else { // 二次探测
34
       LL s = n - 1;
35
       while (!(s & 1) && p == 1) {
36
         s >>= 1;
37
         p = qpow(a, s, n);
38
39
       if (p == 1 \mid | p == n - 1) return true;
40
       else return false;
41
     }
42
   bool Miller_Rabin(LL n) { // 对整数n进行Miller_Rabin素数测试,返回true表示通过测试
43
     if (n <= 29) {
44
                    // if这一块其实可以不用
       for (int i = 0; i < 10; i++) {
45
46
         if (n == p[i]) return true;
47
48
       return false;
49
     }
50
     for (int i = 0; i < 10; i++) { // 利用前10个素数作为底数测试的正确率已经非常高
51
       if (qcd(n, p[i]) == 1 \&\& !prime_test(n, p[i])) return false;
52
53
     return true;
54
   LL randf(LL x, LL n, LL c) { // 满足要求的产生伪随机数函数
55
56
     return (qmult(x, x, n) + c) \% n;
57
58
   LL pollard_rho(LL n, LL c) { // 查找n的因数, c为上面函数要用的随机数, c也可自己指定
       ( 但 要 有 变 化 )
59
     LL x = rand() % n, y = x, i = 1, k = 2, p; // 随机生成随机数的初始值,也可自己指定
60
     while (true) {
61
       i++;
       x = randf(x, n, c);
62
63
       p = gcd(y - x + n, n);
       if (p > 1 \& p < n) return p;
64
65
       if (y == x) return n;
                            // 判 圈, 返 回n表 示 查 找 失 败, 要 更 新 随 机 种 子 重 新 查 找
66
       if (i == k) {
67
         y = x; // 更新范围和记录的数
68
         k <<= 1;
69
       }
70
     }
71
72
   void find_factor(LL n) { // 查找所有因数
73
     if (Miller_Rabin(n)) {
74
       minfactor = min(minfactor, n);
75
       return ;
76
77
     LL p = n;
     while (p == n) p = pollard_rho(n, rand()% (n - 1) + 1); // 查找失败则更新随机种子
78
        重 新 查 找 , 直 到 找 到 因 子
79
     find_factor(p);
                       // 递归查找更小因子
     find_factor(n / p);
80
81
82
83
   int main() {
84
     int t;
85
     cin >> t;
     while (t--) {
86
```

```
87
        LL N;
88
        cin >> N;
89
        if (Miller_Rabin(N)) cout << "Prime" << endl;</pre>
90
91
          minfactor = N;
92
          find_factor(N);
93
          cout << minfactor << endl;</pre>
94
95
96
      return 0;
97 | }
    5.11.1 Miller Rabin
 1
   /* Miller-Rabin Prime Test, by Abreto<m@abreto.net>. */
 2
 3
   namespace miller_rabin {
 4
 5
    typedef long long int ll;
 6
 7
    inline ll add(const ll a, const ll b, const ll mod) {
 8
      11 z = a + b;
 9
      if (z \ge mod) z = mod;
10
      return z;
11
12
    inline ll mul(ll a, ll b, const ll mod) {
13
      11 z = 0;
14
      if (a >= mod) a %= mod;
15
      if (b \ge mod) b mod;
      while (b) {
16
17
        if (1 \& b) z = add(z, a, mod);
18
        a = add(a, a, mod);
19
        b >>= 1;
20
      }
21
      return z;
22
23
24
    ll qow(ll a, ll x, ll mod) {
25
      ll ret = 1ll;
26
      while (x) {
27
        if (1 \& x) ret = mul(ret, a, mod);
28
        a = mul(a, a, mod);
29
        x >>= 1;
      }
30
31
      return ret;
32
33
34
    const int K = 5;
35
    const int p[] = {
      2, 3, 7, 61, 24251
36
37
38
    const ll strong = 4685624825598111;
39
    /* 46 856 248 255 981 in (0, 1e16) */
40
41
    bool mr(ll n, int k) {
42
      11 d = n - 1;
43
      int s = 0;
44
      while (d > 1 \&\& 0 == (d \& 1))  {
45
        S++;
46
        d >>= 1;
47
48
      for (int i = 0; i < k; i++) {
49
        ll a = (i < K) ? p[i] : (1 + rand() % (n - 1));
```

```
50
        11 x = qow(a, d, n);
51
        for (int j = 0; j < s; j++) {
52
          ll xp = mul(x, x, n);
53
          if (1 == xp \&\& x != 1 \&\& x != n-1) return false;
54
          x = xp;
55
56
        if (x != 1) return false;
57
58
      return true;
59
60
61
   /* 2,3,5,7,11,13 */
    const int pre[] = \{3, 5, 7, 11, 13\};
62
   bool test(ll n, int k = 5) {
63
      if (2 == n) return true;
64
65
      if (0 == (n \& 1)) return false;
66
      if (strong == n) return false;
67
      for (int i = 0; i < 5; i++) {
68
        if (n == pre[i]) return true;
        if (n == n / pre[i] * pre[i])
69
70
          return false;
71
72
      return mr(n, k);
73
74
75 |}
    5.11.2 Pollard's rho
 1
   /* Pollard's rho, by Abreto<m@abreto.net>. */
 2
 3
   namespace pollards_rho {
 5
   typedef long long int ll;
 6
 7
    inline ll add(const ll a, const ll b, ll mod) {
 8
      11 z = a + b;
 9
      if (z >= mod) z -= mod;
10
      return z;
11
    inline ll mul(ll a, ll b, ll mod) {
12
13
      11 z = 011;
14
      if (a >= mod) a -= a / mod * mod;
15
      if (b \ge mod) b = b / mod * mod;
16
      while (b) {
        if (1 \& b) z = add(z, a, mod);
17
18
        a = add(a, a, mod);
19
        b >>= 1;
20
21
      return z;
22
23
24
    ll gcd(ll m, ll n) {
25
      return (0 == n)? m : gcd(n, m % n);
26
27
    ll find(ll n, int c = -1) {
28
29
      ll x = rand() % n;
30
      11 y = x, k = 2;
      for (int i = 2; i++) {
31
32
        x = add(mul(x, x, n), (n + c) % n, n);
33
        ll d = gcd(y - x + n, n); // change to abs(y - x) if get WA
34
        if (1 != d && n != d) return d;
```

```
35
        if (y == x) return n;
        if (i == k) {
36
37
          y = x;
38
          k <<= 1;
39
40
41
    }
42
43
    /** usage:
44
     * void find(ll n, int c = 107)
45
     * {
46
         if (1 == n) return;
     *
         if ( miller-rabin(n) )
47
48
     *
49
     *
           n is a prime;
50
     *
           return;
51
     *
52
         ll p = n, k = c;
     *
53
         while (p \ge n) p = pollards_rho(p, k--);
         find(p, c);
54
     *
55
         find(n/p, c);
     *
56
     * }
57
     **/
58
59 |}
```

# 5.12 Montgomery modular multiplication

```
1
 2
   /* -- Montgomery modular algorithm { -- */
 3
   struct Mod64 {
 4
     typedef long long ll;
 5
     typedef unsigned long long u64;
 6
     typedef __int128_t i128;
     typedef __uint128_t u128;
 7
 8
     Mod64() :n_(0) {}
9
     Mod64(u64 n) :n_(init(n)) {}
     static u64 init(u64 w) {
10
11
        return reduce(u128(w) * r2);
12
13
     static void set_mod(u64 m) {
14
        mod = m;
15
        assert(mod & 1);
16
        inv = m;
17
        for (int i = 0; i < 5; ++i) inv *= 2 - inv * m;
18
        r2 = -u128(m) \% m;
19
     }
20
     static u64 reduce(u128 x) {
21
        u64 y = u64(x >> 64) - u64((u128(u64(x)*inv)*mod) >> 64);
22
        return ll(y)<0 ? y + mod : y;
23
24
     Mod64& operator += (Mod64 rhs) {
25
        n_ += rhs.n_ - mod;
26
        if (ll(n_)<0) n_+=mod;
27
        return *this;
28
29
     Mod64 operator + (Mod64 rhs) const {
30
        return Mod64(*this) += rhs;
31
     Mod64& operator -= (Mod64 rhs) {
32
        n_ -= rhs.n_;
33
34
        if (ll(n_{-})<0) n_{-} += mod;
35
        return *this;
```

```
36
37
     Mod64 operator - (Mod64 rhs) const {
38
        return Mod64(*this) -= rhs;
39
40
     Mod64& operator *= (Mod64 rhs) {
41
        n_{-} = reduce(u128(n_{-})*rhs.n_{-});
42
        return *this;
43
44
     Mod64 operator * (Mod64 rhs) const {
45
        return Mod64(*this) *= rhs;
46
47
     u64 get() const {
48
        return reduce(n_);
49
50
     static u64 mod, inv, r2;
51
     u64 n_;
52
53
54
   Mod64::u64 Mod64::mod, Mod64::inv, Mod64::r2;
55
   /* -- } Montgomery modular algorithm -- */
56
57
   /**
58
    * usage:
    * First, Mod64::set_mod();
59
60
    * Mod64 a, b, c(init_val);
61
    *a = b * c;
62
     * printf("%llu\n", a.get());
63
    **/
   5.13
         Berlekamp Massey
   /* Berlekamp Massey by HoldZhu. */
 1
   #include <cstdio>
 3
   #include <vector>
 5
   using namespace std;
 7
   namespace BerlekampMassey {
 8
   const int mod = 1e9 + 7;
9
   int L, m, b, n;
10
   vector<int> s, C, B;
11
   void init() {
12
      s.clear();
13
     C.clear();
14
     B.clear();
15
     C.push_back(1);
16
     B.push_back(1);
17
     L = n = 0;
18
     m = b = 1;
19
20
   int pow_mod(int a, int k) {
21
     int s = 1;
22
     while (k) {
23
        if (k & 1)
24
          s = 111 * s * a % mod;
25
        a = 111 * a * a % mod;
26
        k >>= 1;
27
     }
28
     return s;
29
30
   void update(int d) {
31
      s.push_back(d);
     for (int i = 1; i <= L; ++i)
```

```
33
        d = (d + 111 * C[i] * s[n - i] % mod) % mod;
34
     if (d == 0)
35
        ++m;
     else if (2 * L <= n) {
36
37
        vector<int> T = C;
38
        C.resize(n + 1 - L + 1);
39
        for (int i = L + 1; i \le n + 1 - L; ++i)
40
          C[i] = 0;
41
        for (int i = 0; i < B.size(); ++i)
42
          C[i + m] = (C[i + m] + mod - 111 * d * pow_mod(b, mod - 2) % mod * B[i] % mod)
             % mod;
43
        L = n + 1 - L;
44
        B = T;
        b = d;
45
46
        m = 1;
47
     } else {
48
        for (int i = 0; i < B.size(); ++i)
49
          C[i + m] = (C[i + m] + mod - 1ll * d * pow_mod(b, mod - 2) % mod * B[i] % mod)
50
        ++m;
51
     }
52
     ++n;
53
   void output() {
54
     printf("F(n)=");
55
56
     for (int i = 1; i < C.size(); ++i) {
57
        int output = (mod - C[i]) \% mod;
58
        if (output > mod / 2)
59
          output -= mod;
        printf("%s%d*F(n-%d)", (output < 0 \mid i == 1)? "" : "+", output, i);
60
61
62
     puts("");
63
   void output_code_for() {
64
     static const char *name = "dp";
65
     static const char *index = "i";
66
     static const char *upperbound = "maxn";
67
68
     puts("//_Generated_by_Berlekamp_Massey_algorithm");
69
     for (int i = 1; i < C.size(); ++i) {
70
        printf("%s[%d]=%d;\n", name, i - 1, s[i - 1]);
71
     printf("for(int<sub>\(\)</sub>i=\(\)d;i<\(\)s;++i)\\n", (int)C.size() - 1, upperbound);</pre>
72
     printf("⊔∪%s[%s]=((", name, index);
73
74
     for (int i = 1; i < C.size(); ++i) {
75
        int output = (mod - C[i]) % mod;
76
        if (output > mod / 2)
77
          output -= mod;
        printf("%s%d*%s[%s-%d]%mod", (output < 0 | | i == 1) ? "" : "+", output, name,
78
           index, i);
79
80
     puts(")%mod+mod)%mod;");
81
82
   void output_code_matrix() {
     // TODO
83
84
85
   };
86
87
   /** usage */
88
   int usage() {
      // int arr[12] = {2, 24, 96, 416, 1536, 5504, 18944, 64000, 212992, 702464,
89
         2301952, 7512064};
     int arr[] = {3, 20, 119, 696, 4059, 23660, 137903, 803760, 4684659};
90
91
     BerlekampMassey::init();
92
     for (auto ai : arr) {
```

### 5.14 Lindström-Gessel-Viennot lemma

对于一张无边权的 DAG 图,给定 n 个起点和对应的 n 个终点,这 n 条不相交路径的方案数为

```
 \begin{vmatrix} e(a_1,b_1) & e(a_1,b_2) & \cdots & e(a_1,b_n) \\ e(a_2,b_1) & e(a_2,b_2) & \cdots & e(a_2,b_n) \\ \vdots & \vdots & \ddots & \vdots \\ e(a_n,b_1) & e(a_n,b_2) & \cdots & e(a_n,b_n) \end{vmatrix}  (该矩阵的行列式)
```

其中 e(a,b) 为图上 a 到 b 的方案数.

# 6 String

#### 6.1 Hash

```
/* Common hash for any substrings. */
 1
 2
   typedef unsigned long long int llu;
 3
   #define MAXN 1000000
 5
   int n;
   char s[MAXN];
 6
   llu H[MAXN], xP[MAXN], P = 9999111;
 7
   void init(void) {
 8
 9
     int i = 0;
     xP[0] = 111;
10
11
     for(i = 1; i < MAXN; ++i) xP[i] = xP[i-1] * P;
12
     H[n] = 0;
13
     for(i = n-1; i >= 0; --i) H[i] = H[i+1]*P + s[i];
14
15 |\# define HASH(i,l) (H[i] - H[i+l]*xP[l])
```

## 6.2 KMP

```
1
   /* KMP, by Abreto<m@abreto.net>. */
 2
   #include <string.h>
 3
 4
   /* !!NEED IMPROVING!! */
 5
   #define MAXL (1000010)
 6
 7
 8
   char W[MAXL], T[MAXL];
9
   int f[MAXL];
10
   int lW, lT;
11
12
   int count(void) {
13
     int cnt = 0;
14
     int i, j;
15
     lW = strlen(W);
     lT = strlen(T);
16
     // -- self-matching
```

```
18
     f[0] = j = -1;
19
     for(i = 1; i < lW; i++) {
20
        while( j \ge 0 \& W[j+1] != W[i] )
21
          j = f[j];
22
        if(W[j+1] == W[i]) j++;
23
        f[i] = j;
24
     }
25
     // -
      j = -1;
26
     for(i = 0; i < lT; i++) {
27
28
        while( j \ge 0 \& W[j+1] != T[i] )
29
          j = f[j];
30
        if(W[j+1] == T[i]) j++;
        if( j == lW-1 ) {
31
32
          cnt++;
33
          j = f[j];
34
        }
35
36
      return cnt;
37
   6.3 \text{ exKMP}
 1
   #include <bits/stdc++.h>
 2
   using namespace std;
 3
 4
   namespace exkmp {
 5
   const int maxn = 1000100, maxm = 1000100;
 6
 7
 8
   int n, m;
9
   char S[maxn], T[maxm];
10
   /* the length of longest prefix between T[i..m-1] and T[0..m-1] */
11
12
   int nxt[maxm];
   /* the length of longest prefix between S[i..n-1] and T[0..m-1] */
13
14
   int ex[maxn];
15
16
   void getsize() {
17
     n = strlen(S);
18
     m = strlen(T);
19
20
21
   void self(void) {
22
     int q = 1, p = 0;
23
     nxt[0] = m;
24
     while (1 + p < m \&\& T[1 + p] == T[p]) p++;
25
     nxt[1] = p;
     for (int i = 2; i < m; i++) {
26
27
        int l = nxt[i - q];
        if (i + l - 1 < p) {
28
29
          nxt[i] = 1;
        } else {
30
31
          int j = max(0, p - i + 1);
          while (i + j < m \& T[i + j] == T[j]) j++;
32
33
          nxt[i] = j;
34
          p = i + j - 1;
35
          q = i;
36
37
     }
   }
38
39
40 void run(void) {
```

```
41
      int q = 0, p = 0;
42
      self();
43
      while (p < n \&\& p < m \&\& S[p] == T[p]) p++;
44
      ex[0] = p;
45
46
      for (int i = 1; i < n; i++) {
47
        int l = nxt[i - q];
48
        if (i + l - 1 < p) {
49
          ex[i] = 1;
        } else {
50
51
          int j = max(0, p - i + 1);
52
          while (i + j < n \&\& S[i + j] == T[j]) j++;
53
          ex[i] = j;
54
          p = i + j - 1;
55
          q = i;
56
        }
57
      }
58
59
60
   void inspect(void) {
      printf("S:□");
61
62
      for (int i = 0; i < n; i++) putchar(S[i]);
      puts("")
63
      printf("T:⊔");
64
65
      for (int i = 0; i < m; i++) putchar(T[i]);
      puts("");
66
67
      printf("next:");
68
      for (int i = 0; i < m; i++) printf("\lfloor \%d", nxt[i]);
      puts("");
69
      printf("extend:");
70
      for (int i = 0; i < n; i++) printf("\lfloor \%d", ex[i]);
71
72
      puts("");
73
   }
74
75 |} // exkmp
   6.4 Suffix Array
   /* Suffix Array, copied. */
 1
 2
 3
   #define MAXN
                     (200010)
   namespace mzry_sa {
 5
   int wx[MAXN], wy[MAXN], *x, *y, wss[MAXN], wv[MAXN];
 6
 7
    bool dacmp(int *r,int n,int a,int b,int l) {
 8
      return a+1 < n \&\& b+1 < n \&\& r[a]==r[b]\&\&r[a+1]==r[b+1];
9
10
   void da(int str[],int sa[],int rank[],int height[],int n,int m) {
11
      int *s = str;
12
      int *x=wx,*y=wy,*t,p;
      int i,j;
13
14
      for(i=0; i<m; i++)wss[i]=0;
15
      for(i=0; i<n; i++)wss[x[i]=s[i]]++;
16
      for(i=1; i<m; i++)wss[i]+=wss[i-1];
17
      for(i=n-1; i>=0; i--)sa[--wss[x[i]]]=i;
18
      for(j=1,p=1; p<n && j<n; j*=2,m=p) {
19
        for(i=n-j,p=0; i< n; i++)y[p++]=i;
20
        for(i=0; i<n; i++)if(sa[i]-j>=0)y[p++]=sa[i]-j;
        for(i=0; i<n; i++)wv[i]=x[y[i]];
21
        for(i=0; i<m; i++)wss[i]=0;
22
        for(i=0; i<n; i++)wss[wv[i]]++;
23
24
        for(i=1; i<m; i++)wss[i]+=wss[i-1];
25
        for(i=n-1; i>=0; i--)sa[--wss[wv[i]]]=y[i];
```

```
26
       for(t=x,x=y,y=t,p=1,i=1,x[sa[0]]=0; i<n; i++)
27
          x[sa[i]]=dacmp(y,n,sa[i-1],sa[i],j)?p-1:p++;
28
29
     for(int i=0; i<n; i++) rank[sa[i]]=i;
30
     for(int i=0, j=0, k=0; i< n; height[rank[i++]]=k)
31
        if(rank[i]>0)
32
          for(k?k-:0, j=sa[rank[i]-1];
33
              i+k < n && j+k < n && str[i+k]==str[j+k];
34
              k++);
35
36
   }
37
38
   /*
39
   Suffix array 0(n lg^2 n)
40
   LCP table O(n)
41
   */
42
   #include <cstdio>
43
   #include <algorithm>
44
   #include <cstring>
45
46
   using namespace std;
47
48
   #define REP(i, n) for (int i = 0; i < (int)(n); ++i)
49
50
   namespace SuffixArray {
51
   const int MAXN = 1 \ll 21;
52
   char * S;
53
   int N, gap;
54
   int sa[MAXN], pos[MAXN], tmp[MAXN], lcp[MAXN];
55
56
   bool sufCmp(int i, int j) {
57
     if (pos[i] != pos[j])
58
       return pos[i] < pos[j];
59
     i += gap;
60
      j += gap;
61
      return (i < N && j < N) ? pos[i] < pos[j] : i > j;
62
63
   void buildSA() {
64
65
     N = strlen(S);
66
     REP(i, N) sa[i] = i, pos[i] = S[i];
67
     for (gap = 1;; gap <<= 1) {
68
        sort(sa, sa + N, sufCmp);
69
       REP(i, N-1) tmp[i+1] = tmp[i] + sufCmp(sa[i], sa[i+1]);
       REP(i, N) pos[sa[i]] = tmp[i];
70
71
        if (tmp[N-1] == N-1) break;
72
     }
73
74
75
   void buildLCP() {
76
     for (int i = 0, k = 0; i < N; ++i) if (pos[i] != N - 1) {
77
          for (int j = sa[pos[i] + 1]; S[i + k] == S[j + k];)
78
            ++k;
          lcp[pos[i]] = k;
79
80
          if (k)—k;
81
82
   } // end namespace SuffixArray
83
84
85
   namespace HashSuffixArray {
86
   const int
87
   MAXN = 1 << 21;
88
89 typedef unsigned long long hash;
```

```
90
 91
    const hash BASE = 137;
 92
 93
    int N;
 94
    char * S;
 95
    int sa[MAXN];
 96
    hash h[MAXN], hPow[MAXN];
 97
 98
    \#define getHash(lo, size) (h[lo] - h[(lo) + (size)] * hPow[size])
 99
100
    inline bool sufCmp(int i, int j) {
101
      int lo = 1, hi = min(N - i, N - j);
102
      while (lo <= hi) {
103
         int mid = (lo + hi) >> 1;
104
         if (getHash(i, mid) == getHash(j, mid))
105
          lo = mid + 1;
106
        else
107
          hi = mid - 1;
108
109
      return S[i + hi] < S[j + hi];</pre>
110
111
112
    void buildSA() {
113
      N = strlen(S);
114
      hPow[0] = 1;
115
      for (int i = 1; i <= N; ++i)
116
        hPow[i] = hPow[i - 1] * BASE;
117
      h[N] = 0;
118
      for (int i = N - 1; i >= 0; —i)
119
        h[i] = h[i + 1] * BASE + S[i], sa[i] = i;
120
121
      stable_sort(sa, sa + N, sufCmp);
122
123
124
    } // end namespace HashSuffixArray
125
126
    namespace lrj_sa {
127
    const int MAXN = 1000;
    char s[MAXN]; /* 原始字符数组 (最后一个字符应必须是0,而前面的字符必须非0) */
128
129
    int sa[MAXN], t[MAXN], t2[MAXN], c[MAXN], n; /* n seems to be the length of s. */
130
    /* every charactor is in [0,m-1] */
131
    void build_sa(int m) {
132
      int i, *x = t, *y = t2;
133
      for(i = 0; i < m; ++i) c[i] = 0;
134
      for(i = 0; i < n; i++) c[x[i]=s[i]]++;
      for(i = 1; i < m; ++i) c[i] += c[i-1]
135
136
      for(i = n-1; i >= 0; --i) sa[--c[x[i]]] = i;
      for(int k = 1; k <= n; k <<= 1) {
137
138
         int p = 0;
139
         for(i = n-k; i < n; ++i) y[p++] = i;
         for(i = 0; i < n; ++i) if(sa[i] >= k) y[p++] = sa[i]-k;
140
         for(i = 0; i < m; i++) c[i] = 0;
141
142
         for(i = 0; i < n; i++) c[x[y[i]]]++;
143
         for(i = 0; i < m; ++i) c[i]+=c[i-1];
144
         for(i = n-1; i >= 0; --i) sa[--c[x[y[i]]]] = y[i];
145
         swap(x,y);
146
        p = 1;
147
        x[sa[0]] = 0;
148
         for(i = 1; i < n; ++i)
149
          x[sa[i]] = y[sa[i-1]] = y[sa[i]] & y[sa[i-1]+k] = y[sa[i]+k] ? p-1:p++;
150
        if(p >= n) break;
151
        m = p;
152
      }
153 |}
```

```
154
    int rank[MAXN], height[MAXN];
155
    void get_height(void) {
156
       int i,j,k = 0;
157
       for(i = 0; i < n; ++i) rank[sa[i]] = i;
158
      for(i = 0; i < n; ++i) {
159
         if(k) k-;
         j = sa[rank[i]-1];
160
161
         while(s[i+k]==s[j+k]) k++;
162
         height[rank[i]] = k;
163
164
165 |} // end namespace lrj_sa
         Aho-Corasick Automata
    //* Aho-Corasick automaton algorithm, by Abreto<m@abreto.net>. */
  1
  2
  3
    #define MAXN 500500
    #define NALPHA
  5
    #define FIRSTA
                    'a'
  7
     /* pointer version => { */
  8
    struct vtx {
  9
      vtx *nxt[NALPHA];
 10
      vtx *fail;
 11
      int end;
 12
     } vtxs[MAXN];
 13
    int nvtxs;
    void myclr(void) {
 14
 15
      nvtxs = 0;
 16
 17
    vtx *new_vtx(void) {
 18
      vtx *ret = vtxs+(nvtxs++);
 19
      for(int i = 0; i < NALPHA; i++)
         ret->nxt[i] = NULL;
 20
 21
       ret->fail = NULL;
 22
       ret->end = 0;
 23
      return ret;
 24
 25
    void myins(vtx *root, char const *s) {
 26
      for(; *s; s++) {
 27
         int of = (*s) – FIRSTA;
 28
         if ( NULL == root->nxt[of] ) {
 29
           root->nxt[of] = new_vtx();
 30
 31
         root = root->nxt[of];
 32
 33
       root->end++;
 34
 35
    void build_ac(vtx *root) {
 36
      queue<vtx *> q;
 37
      q.push(root);
 38
      while(!q.empty()) {
 39
         vtx *p = q.front();
 40
         q.pop();
 41
         for(int i = 0; i < NALPHA; i++) {
 42
           if( NULL == p->nxt[i] ) continue;
 43
           if( root == p ) p->nxt[i]->fail = root;
 44
           else {
 45
             vtx *t = p->fail;
             while ( t && NULL == t->nxt[i] ) {
 46
 47
               t = t \rightarrow fail;
 48
             }
```

```
49
             if (t) p->nxt[i]->fail = t->nxt[i];
50
             else p->nxt[i]->fail = root;
51
52
           /* version[1] { */
           p->nxt[i]->end += p->nxt[i]->fail->end; /* update this sum, add its existing
53
               prefix to this. */
           /* } */
54
55
           q.push(p->nxt[i]);
56
57
58
59
     int qry(vtx *root, char const *s) {
60
       vtx *p = root;
       int cnt = 0;
61
       for(; *s; s++) {
62
63
         int of = (*s) - FIRSTA;
64
         while( p != root && NULL == p->nxt[of] ) {
65
           p = p \rightarrow fail;
66
         if (p->nxt[of]) p = p->nxt[of];
67
         cnt += p->end; // correct when version[1] exists.
68
         // if version[1] not exists, you need to add all ends from this vertex up.
69
70
         //for( vtx *t = p ; t ; t = t->fail )
71
         // cnt += t->end;
72
73
      return cnt;
74
75
    /* } */
76
     /* — usage (of pointer version) — */
77
 78
    #include <bits/stdc++.h>
79
    using namespace std;
80
81
    char S[1000100];
82
    char pat[64];
83
84
    int main(void) {
85
       int T, N;
86
       vtx *root = NULL;
87
       scanf("%d", &T);
88
       while(T---) {
89
         myclr();
         root = new_vtx();
90
         scanf("%s", S);
scanf("%d", &N);
91
92
93
         while(N---) {
           scanf("%s", pat);
94
95
           myins(root, pat);
96
97
         build_ac(root);
98
         printf("%d\n", qry(root, S));
99
100
       return 0;
101
    6.6 Manacher
    |char t[MAXL<<1];</pre>
    int p[MAXL<<1];</pre>
  2
  3
    int manacher(char *s) {
  4
       int i;
  5
       int sl = strlen(s);
       int pos = 0, mxr = 0;
```

```
7
     int ret = 0;
 8
     t[0] = '^;
 9
     for(i = 0; i < sl; ++i) {
        t[i*2+1] = '#';
10
        t[i*2+2] = s[i];
11
12
     t[sl*2+1] = '#';
13
     t[sl*2+2] = '$';
14
15
     sl = sl*2+2;
16
     for(i = 1; i < sl; ++i) {
17
        if(i <= mxr) {
18
          p[i] = min(p[2*pos - i], mxr-i+1);
19
        } else {
20
          p[i] = 1;
21
22
        while( t[i-p[i]] == t[i+p[i]] ) p[i]++;
23
        if(i + p[i] - 1 > mxr) {
24
          mxr = i+p[i]-1;
25
          pos = i;
26
27
        ret = max(ret, p[i]-1);
28
29
     return ret;
30
   7
```

# Utility

# 7.1 IO plug-in

```
/* I/O Plug-in, by Abreto <m@abreto.net>. */
 2
   #include <stdio.h>
 3
 4
   #if ( _WIN32 || __WIN32__ || _WIN64 || __WIN64__ )
 5
   #define INT64 "%I64d"
 6
   #else
 7
   #define INT64 "%lld"
 8
   #endif
9
   #if ( _WIN32 || __WIN32__ || _WIN64 || __WIN64__ )
10
11
   #define UNS64 "%I64u"
12
   #else
   #define UNS64 "%llu"
13
14
   #endif
15
   #define ISDIGIT(x) ((x>='0')\&\&(x<='9'))
16
   int readn(int *n) {
17
18
     int c=0;
19
     *n=0;
20
     for(; !ISDIGIT(c); c=getchar());
21
     for(; ISDIGIT(c); c=getchar())*n=(*n)*10+c-'0';
22
     return (*n);
23
24
   void putn(int n) {
25
     int ns[16]= {0,n%10},nd=1;
26
     while(n/=10)ns[++nd]=n%10;
     while(nd)putchar(ns[nd--]+'0');
27
28 | }
 1
   |#include <cstdio>
 2
 3
   class abio {
     static const unsigned BUF_SZ = 65536;
```

```
5
      FILE *istream, *ostream;
      char ibuf[BUF_SZ], obuf[BUF_SZ];
 6
 7
      bool reached_eof;
 8
      size_t ip, isz;
 9
      size_t op, osz;
10
      inline void clear_ibuf(void) {
11
        ip = isz = 0u;
12
13
      inline void clear_obuf(void) {
14
        op = osz = 0u;
15
16
      inline void clear_buffer(void) {
        reached_eof = false;
17
18
        clear_ibuf();
        clear_obuf();
19
20
21
      inline size_t read_buffer(void) {
        isz = std::fread(ibuf, sizeof(char), BUF_SZ, istream);
22
23
        ip = 0;
24
        return isz;
25
26
      inline size_t write_buffer(void) {
27
        if(osz) {
28
          size_t ret = std::fwrite(obuf+op, sizeof(char), osz-op, ostream);
29
          op += ret;
30
          if(op == osz) clear_obuf();
31
          return ret;
32
        }
33
        return 0;
34
35
      inline abio &reach_eof(void) {
        reached_eof = true;
36
37
        return (*this);
38
39
   public:
40
      static const char endl = '\n';
      abio(FILE *input = stdin, FILE *output = stdout) {
41
42
        this->istream = input;
        this->ostream = output;
43
44
        clear_buffer();
45
      }
46
      abio(const char *input, const char *output) {
47
        this->istream = std::fopen(input, "r");
        this->istream = std::fopen(output, "w+");
48
49
        clear_buffer();
50
      ~abio(void) {
51
52
        write_buffer();
53
        std::fclose(istream);
54
        std::fclose(ostream);
55
56
      operator bool() const {
57
        return (!reached_eof);
58
59
      inline int getchar(void) {
60
        if(isz == ip) read_buffer();
61
        if(isz == ip) return EOF;
62
        return ibuf[ip++];
63
64
      inline int putchar(int ch) {
        if(osz == BUF_SZ) write_buffer();
if(osz == BUF_SZ) return EOF;
65
66
67
        return (obuf[osz++] = ch);
68
      }
```

```
69
      abio &read_int(int &x) {
 70
         int flag = 0, ch = getchar();
         for (; (EOF!=ch)\&\&((ch<'0')||(ch>'9')); ch=getchar()) if ('-'==ch) flag = 1;
 71
 72
         if (EOF == ch) return (this->reach_eof());
 73
         x = 0;
         for (; (ch>='0')\&\&(ch<='9'); ch=getchar()) x = x * 10 + (ch - '0');
 74
 75
         if (flag) x *= (-1);
 76
         return (*this);
 77
 78
      abio &read_ll(long long int &x) {
 79
         int flag = 0, ch = getchar();
         for (; (EOF!=ch)\&((ch<'0')||(ch>'9')); ch=qetchar()) if ('-' == ch) flag = 1;
 80
         if (EOF == ch) return (this->reach_eof());
 81
 82
         x = 011;
 83
         for (; (ch>='0')&&(ch<='9'); ch=getchar()) x = x * 10ll + (ch - '0');
 84
         if ( flag ) x *= (-111);
 85
         return (*this);
 86
 87
      abio &read_unsigned(unsigned &x) {
 88
         int ch = aetchar();
 89
         for(; (EOF != ch) && ((ch < '0') || (ch > '9')); ch = getchar());
 90
         if (EOF == ch) return (this->reach_eof());
 91
 92
         for(; (ch >= '0') && (ch <= '9'); ch = getchar()) x = x * 10u + (ch - '0');
 93
         return (*this);
 94
 95
      abio &read_ull(unsigned long long int &x) {
 96
         int ch = getchar();
         for(; (EOF != ch) && ((ch < '0') || (ch > '9')); ch = getchar());
 97
 98
         if (EOF == ch) return (this->reach_eof());
 99
         x = 0ull:
100
         for(; (ch >= '0') && (ch <= '9'); ch = getchar()) x = x * 10ull + (ch - '0');
101
         return (*this);
102
      /* set interrupt as '\n' to read a whole line. */
103
      abio &read_s(char *s, const char interrupt = '□') {
104
105
         int ch = getchar();
         while((EOF!=ch)&&(ch<'!'||ch>'~'))ch=getchar();
106
107
         if(EOF==ch) return (this->reach_eof());
108
         for(; (EOF!=ch)&&(interrupt!=ch)&&(ch>='\_''&&ch<='\~'); ch=getchar())(*s++)=ch;
109
         (*s)=0;
110
         return (*this);
111
112
      abio &write_int(int x, char append = 0) {
113
         int d[20], nd=0;
114
         if(0==x) putchar('0');
115
         if(x<0) {
116
           putchar('-');
117
           X=-X;
118
119
         while(x) {
           d[nd++]=x%10;
120
121
           x/=10;
122
         while(nd—)putchar('0'+d[nd]);
123
124
         if(append)putchar(append);
         return (*this);
125
126
127
      abio &write_ll(long long int x, char append = 0) {
128
         int d[20], nd=0;
129
         if(0==x) putchar('0');
130
         if(x<0) {
131
           putchar('-');
132
           X=-X;
```

```
133
134
         while(x) {
135
           d[nd++]=x%10;
136
           x/=10;
137
138
         while(nd—)putchar('0'+d[nd]);
139
         if(append)putchar(append);
         return (*this);
140
141
142
       abio \&write\_unsigned(unsigned x, char append = 0) {
143
         int d[20], nd=0;
144
         if(0==x) putchar('0');
145
         while(x) {
146
           d[nd++]=x%10;
147
           x/=10;
148
149
         while(nd—)putchar('0'+d[nd]);
150
         if(append)putchar(append);
151
         return (*this);
152
153
       abio &write_ull(unsigned long long int x, char append = 0) {
154
         int d[20],nd=0;
         if(0==x) putchar('0');
155
         while(x) {
156
157
           d[nd++]=x%10;
158
           x/=10;
159
160
         while(nd—)putchar('0'+d[nd]);
161
         if(append)putchar(append);
162
         return (*this);
163
164
       abio &write_s(const char *s, char append = 0) {
165
         while(*s) putchar(*s++);
166
         if(append) putchar(append);
167
         return (*this);
168
169
       abio &operator>>(char &ch) {
170
         ch = getchar();
171
         if(EOF==ch) return (this->reach_eof());
172
         return (*this);
173
       }
174
       abio &operator>>(int &x) {
175
         return read_int(x);
176
177
       abio &operator>>(long long int &x) {
178
         return read_ll(x);
179
       abio &operator>>(unsigned &x) {
180
181
         return read_unsigned(x);
182
       abio &operator>>(unsigned long long int &x) {
183
184
         return read_ull(x);
185
       abio &operator>>(char *s) {
186
187
         return read_s(s);
188
189
       abio &operator<<(const char ch) {
190
         putchar(ch);
191
         return (*this);
192
193
       abio &operator<<(const int x) {
194
         return write_int(x);
195
       abio &operator<<(const long long int x) {
196
```

```
197
         return write_ll(x);
       }
198
199
       abio &operator<<(const unsigned x) {</pre>
         return write_unsigned(x);
200
201
202
       abio &operator<<(const unsigned long long int x) {
203
         return write_ull(x);
204
       abio &operator<<(const char *s) {</pre>
205
         return write_s(s);
206
207
208 |} io;
```