# ACM TEMPLATE



UESTC\_Jungle

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## $\overline{\text{Contents}}$

1	Dat		3
	1.1	Fenwick	3
	1.2	BST in pb_ds	4
	1.3	Segment Tree	4
	1.4		7
	1.5	<u>.</u>	7
	1.6		0
	1.7	1	1
	1.8	- v	.5
	1.0	reisistent segment free	.J
2	Dyr	namic Programming 1	5
-	2.1		5
		· · · · · · · · · · · · · · · · · · ·	
	2.2	( 0 )	5
	2.3		6
	2.4	1 , 1	7
	2.5	Steiner Tree	.8
3	~		_
			9
	3.1		.9
		3.1.1 Point	.9
		3.1.2 Circle	21
		3.1.3 Convex hull	27
		3.1.4 Intersect Area	27
		3.1.5 Universe	80
4	Gra	$_{ m ph}$	6
	4.1	Tree	86
		4.1.1 Universe	86
			37
		1	4
	4.2	V I	16
	4.3		17
		8	18 18
	4.4		
	4.5		19
		y .	19
			0
		1	52
	4.6	Maxflow	64
	4.7	Strongly Connected Component	8
	4.8	Perfect elimination ordering	i1
5	Mat	h	3
	5.1	Euler Function	3
	F 0	Möbius Function	3
	5.2	N. 1 (77)	
	5.3	Number Theory Inverse	i4
	5.3		
	5.3 5.4	Chinese Remainder Theorem	64
	5.3 5.4 5.5	Chinese Remainder Theorem	54 55
	5.3 5.4 5.5 5.6	Chinese Remainder Theorem6Linear congruences6FFT6	54 55 56
	5.3 5.4 5.5 5.6 5.7	Chinese Remainder Theorem 6 Linear congruences 6 FFT 6 NTT 6	54 55 56 59
	5.3 5.4 5.5 5.6 5.7 5.8	Chinese Remainder Theorem6Linear congruences6FFT6NTT6Fast Walsh-Hadamard transform7	54 55 56 59 71
	5.3 5.4 5.5 5.6 5.7	Chinese Remainder Theorem6Linear congruences6FFT6NTT6Fast Walsh-Hadamard transform7Lucas7	54 55 56 59

	UESTC_Jun	gle
	5.11 Big Prime Test	76
	5.11.1 Miller Rabin	77
	5.11.2 Pollard's rho	79
	5.12 Montgomery modular multiplication	80
	5.13 Berlekamp Massey	81
6	String	82
	6.1 Hash	82
	3.2 KMP	83
	3.3 exKMP	83
	3.4 Suffix Array	85
	3.5 Aho-Corasick Automata	87
	6.6 Manacher	89

## 1 Datastructure

## 1.1 Fenwick

```
//* Fenwick Tree (Binary Indexed Tree), by Abreto <m@abreto.net>. */
 2
   #include <cstring>
 3
 4
   using namespace std;
 5
   template <class T = int, int MAXN = 100001>
 6
 7
   struct fenwick {
 8
      static inline int lowbit(int x) {
 9
        return (x&(-x));
10
11
      int N;
12
      T f[MAXN]; /* 1=based. */
13
      fenwick(void):N(MAXN) {
14
        init();
15
16
      fenwick(int n):N(n) {
17
        init();
18
19
      void init(void) {
20
        memset(f,0,sizeof(f));
21
      void upd(int i, T dx) {
22
        while(i <= N) {</pre>
23
24
          f[i] += dx;
25
          i += lowbit(i);
        }
26
27
      T sum(int i) {
28
29
        T ret = 0;
30
        while(i) {
31
          ret += f[i];
32
          i -= lowbit(i);
33
34
        return ret;
35
      }
36
   |};
   /* Fenwick Tree (Binary Indexed Tree), by Abreto <m@abreto.net>. */
 2
 3
   #define MAXN 100001
 4
   #define LOWBIT(x)
                         ((x)&(-(x)))
 5
 6
   int N;
 7
   int fen[MAXN];
 8
 9
   void update(int i, int dx) {
10
      while(i <= N) {</pre>
        fen[i] += dx;
11
12
        i += LOWBIT(i);
13
14
15
16
   int sum(int i) {
      int s = 0;
17
18
      while(i > 0) {
19
        s += fen[i];
20
        i -= LOWBIT(i);
21
22
      return s;
23 |}
```

## 1.2 BST in pb\_ds

```
/* Red_Black tree via pb_ds. */
   #include<bits/stdc++.h>
   #include<ext/pb_ds/assoc_container.hpp>
   #include<ext/pb_ds/tree_policy.hpp>
 5
   using namespace __gnu_pbds;
 6
   using namespace std;
 7
   template <typename T>
 8
   using ordered_set = tree<T, null_type, less<T>, rb_tree_tag,
       tree_order_statistics_node_update>;
 9
10
   int main() {
11
     ordered_set<int> s;
12
     s.insert(1);
13
     s.insert(3);
     cout << s.order_of_key(2) << endl; // the number of elements in the s less than 2
14
     cout << *s.find_by_order(0) << endl; // print the 0-th smallest number in s(0-based
15
16
```

## 1.3 Segment Tree

```
1
   //* Segment tree (Interval tree, range tree), by Abreto <m@abreto.net>. */
 2
 3
    template <int STMAX = 1000000>
 4
    struct segment_tree {
 5
      struct node_t {
 6
        static inline node_t merge(node_t n1, node_t n2) {
 7
          node_t ans;
 8
          ans.l = n1.l;
 9
          ans.r = n2.r;
10
          /* merge n1 and n2 to ans. */
11
          return ans;
12
        }
13
14
        /* Data field */
15
        int l,r:
16
      } nodes[(STMAX+1)<<2];</pre>
17
18
      struct lazy_t {
        int marked; /* Optional */
19
20
        /* lazy mark. */
21
22
        lazy_t(void) {
23
          clear();
24
25
        void clear(void) {
26
          marked=0;
27
28
      } marks[(STMAX+1)<<2];</pre>
29
30
      inline void maintain_leaf(int o, int idx) {
31
        nodes[o].l = nodes[o].r = idx;
32
        /* Operations to single elements ... */
33
34
      inline void maintain(int o) {
35
        nodes[o] = node_t::merge(nodes[o<<1], nodes[o<<1|1]);</pre>
36
      }
37
38
      /* Usage: build(1,1,n); */
39
      void build(int o, int l, int r) \{ /* [l,r] */
```

```
40
         if( r <= l ) {
 41
           maintain_leaf(o, 1);
 42
         } else {
 43
           int mid = 1+r>>1;
 44
           build(o<<1, 1, mid);
           build(o<<1|1, mid+1, r);
 45
 46
           maintain(o);
 47
       }
 48
 49
 50
       /* Modify all elements in [l,r] */
 51
       void mark(lazy_t act, int o) {
 52
         /* do something .. */
 53
         marks[o].marked = 1;
 54
 55
 56
       /* Pass cached updates. */
 57
       void pushdown(int o) {
 58
         if( marks[o].marked ) {
 59
           mark(marks[o], o<<1);</pre>
 60
           mark(marks[o], o<<1|1);
 61
           marks[o].clear();
 62
 63
       }
 64
 65
       /* Do act on all elements in [L,R] */
 66
       void upd(int L, int R, lazy_t act, int o, int l, int r) {
 67
         if(L \le l \& r \le R)
 68
           mark(act, o);
         } else if (L <= R) {</pre>
 69
           int mid = (l+r)>>1;
 70
 71
           pushdown(o);
           if( L <= mid ) upd(L, R, act, o<<1, l, mid);
 72
 73
           if( R > mid ) upd(L, R, act, o<<1|1, mid+1, r);
 74
           maintain(o);
 75
 76
       }
 77
 78
       node_t qry(int L, int R, int o, int l, int r) {
 79
         if(L \ll 1 \& r \ll R)
 80
           return nodes[o];
 81
         else if (L \ll R) {
 82
           int mid = (l+r)>>1;
 83
           pushdown(o);
 84
           if(R <= mid) return qry(L,R,o<<1,1,mid);</pre>
 85
           if(L > mid) return qry(L,R,o<<1|1,mid+1,r);
 86
           return node_t::merge(qry(L,R,o<<1,l,mid),qry(L,R,o<<1|1,mid+1,r));</pre>
 87
         }
 88
       }
 89
 90
       int N;
 91
 92
       segment_tree(void):N(STMAX) {}
93
       segment_tree(int n):N(n) {}
 94
       void build(int n) {
 95
         N = n;
 96
         build(1,1,N);
 97
       }
 98
       void update(int L, int R, lazy_t act) {
 99
         upd(L,R,act,1,1,N);
100
       node_t query(int L, int R) {
101
102
         return qry(L,R,1,1,N);
103
       }
```

```
104 | };
    |/* Segment tree (Interval tree, range tree), by Abreto <m@abreto.net>. */
  1
  3
    #define MAXN
                      1000001
  4
  5
     typedef struct {
       int l,r;
  6
       /* Data field */
  7
  8
    } node_t;
  9
 10
    node_t merge(node_t n1, node_t n2) {
 11
       node_t ans;
 12
       ans.l = n1.l;
 13
       ans.r = n2.r;
 14
       /* merge n1 and n2 to ans. */
 15
       return ans;
 16
    }
 17
     typedef struct {
 18
 19
       int marked; /* Optional */
 20
       /* lazy mark. */
 21
    } lazy_t;
 22
 23
    int A[MAXN];
 24
    node_t nodes[MAXN<<2];</pre>
 25
    lazy_t marks[MAXN<<2];</pre>
 26
 27
    void maintain_leaf(int o, int idx) {
 28
       nodes[o].l = nodes[o].r = idx;
 29
       /* Operations to single elements ... */
 30
 31
    void maintain(int o) {
       nodes[o] = merge(nodes[o << 1], nodes[o << 1|1]);
 32
 33
    }
 34
 35
     /* Usage: build(1,1,n); */
 36
    void build(int o, int l, int r) { /* [l,r] */
 37
       if( r <= l ) {
 38
         maintain_leaf(o, 1);
 39
       } else {
 40
         int mid = 1+r>>1;
 41
         build(o<<1, 1, mid);
         build(o<<1|1, mid+1, r);
 42
 43
         maintain(o);
 44
 45
       marks[o].marked = 0;
 46
 47
 48
    /* Modify all elements in [l,r] */
 49
    void mark(lazy_t act, int o) {
       /* do something .. */
 50
 51
       marks[o].marked = 1;
 52
 53
 54
    /* Pass cached updates. */
 55
    void pushdown(int o) {
 56
       if( marks[o].marked ) {
 57
         mark(marks[o], o<<1);</pre>
 58
         mark(marks[o], o<<1|1);
 59
         marks[o].marked = 0;
 60
       }
    }
 61
 62
```

```
63
   /* **DISCARDED** */
64
   /* Set A[p]=v. Usage: modify(p, v, 1, 1, n);
65
   void modify(int p, int v, int o, int l, int r)
66
        if(r-1 < 2)
67
68
69
            maintain_leaf(o, v);
70
        } else {
71
            int mid = (1+r)/2;
72
            pushdown(o);
73
            if( p \le mid ) modify(p, v, o*2, l, mid);
74
            else modify(p, v, o*2+1, mid, r);
75
            maintain(o);
76
   }*/
77
78
79
   /* Do act on all elements in [L,R] */
80
   void update(int L, int R, lazy_t act, int o, int l, int r) {
81
      if( L <= 1 && r <= R ) {
82
        mark(act, o);
83
      } else if (L <= R) {</pre>
84
        int mid = (l+r)>>1;
85
        pushdown(o);
86
        if( L <= mid ) update(L, R, act, o<<1, l, mid);</pre>
87
        if( R > mid ) update(L, R, act, o<<1|1, mid+1, r);
88
        maintain(o);
89
      }
90 | }
   1.4 Sparse Table
   |/* RMQ with Sparse Table, by Abreto <m@abreto.net>. */
 1
 2
 3
   int min(int a, int b) {
 4
      return (a<b)?a:b;
 5
 6
 7
   #define MAXN
                     100001
 8
   #define MAXLOG 32
 9
10
    int N;
11
   int A[MAXN];
                   /* indexed from 0. */
12
   int st[MAXN][MAXLOG];
13
    void st_init() {
14
      int i = 0, j = 0, t = 0;
for(i = 0; i < N; ++i) st[i][0] = A[i];
15
16
17
      for(j = 1; (t=(1<< j)) <= N; ++j)
        for(i = 0; (i+t-1) < N; ++i)
18
19
          st[i][j] = min(st[i][j-1], st[i+(t>>1)][j-1]);
20
      /* st(i,j) = min(st(i,j-1), st(i+2^(j-1),j-1)). */
21
22
23
   int st_query(int l, int r) {
24
      int k = 0;
25
      while((1 << (k+1)) <= (r-l+1)) k++;
26
      return min(st[l][k], st[r-(1<k)+1][k]);
27 |}
```

#### 1.5 Treap

```
|#include <bits/stdc++.h>
 1
 2
 3
   using namespace std;
 5
   #define MAXN (2560000)
 6
 7
   int __treap_mem[MAXN];
 8
   void init_treap_mem(void) {
9
      for( int i = 1; i < MAXN; i++)
10
       \_treap\_mem[i-1] = i;
11
12
   int alloc_address(void) {
13
     int ret = __treap_mem[0];
14
      __treap_mem[0] = __treap_mem[ret];
15
      return ret;
16
17
   void free_address(int p) {
18
     _{\text{treap\_mem}[p]} = _{\text{treap\_mem}[0]};
19
      \_treap_mem[0] = p;
20
21
22
   typedef int key_t;
23
   typedef int val_t;
24
   struct treap {
25
     key_t x;
26
     val_t v;
27
               /* random priority */
     int r;
     int eq, s; /* number of equal ones, size of subtree (include root itself) */
28
     treap *fa; /* point to its father */
29
     treap *ch[2]; /* 0 for left child, 1 for right child. */
30
31
32
     treap(void);
33
     inline void maintain(void); /* update s */
34
     inline void set_child(int d, treap *child);
35
     inline int which(void); /* determine which child this is of its father */
36
     inline int cmp(key_t ox); /* determine which child to insert ox */
37
     treap *rotate(void); /* rotate this to its father, return this */
38
   } treap_nodes[MAXN];
39
40
   treap *new_treap(key_t x, val_t v, treap *f) {
41
     treap *ret = treap_nodes + alloc_address();
42
      ret->x = x;
43
      ret -> v = v;
44
      ret->eq = ret->s = 1;
45
      ret->fa=f;
46
      ret->ch[0] = ret->ch[1] = NULL;
47
48
   void free_treap(treap *p) {
49
      free_address( p - treap_nodes );
50
51
   void treap_clear(void) {
52
     init_treap_mem();
53
54
55
   treap::treap(void) {
56
     r = rand();
57
     eq = s = 0;
58
     fa = ch[0] = ch[1] = NULL;
59
60
   inline void treap::maintain(void) {
61
      s = eq;
     for( int i = 0 ; i < 2 ; i++ )
62
63
       if( ch[i] )
64
          s += ch[i]->s;
```

```
65
 66
    inline void treap::set_child(int d, treap *child) {
 67
       ch[d] = child;
 68
       maintain();
 69
       if( child ) child->fa = this;
 70
 71
    inline int treap::which(void) {
 72
       if( NULL == fa ) return -1; /* this is not a child */
 73
       else return ( fa->ch[1] == this );
 74
 75
    inline int treap::cmp(key_t ox) {
 76
       if( ox == x ) return -1; /* equal */
 77
       else return ( ox > x ); /* left less, right more */
 78
 79
     treap *treap::rotate(void) {
 80
       if ( NULL == fa ) return this; /* no father, already global root. */
       int d = which();
 81
 82
       fa->set_child(d, ch[d^1]);
 83
       set_child(d^1, fa);
 84
       return this;
 85
 86
 87
     // --- deprecated |
 88
    typedef int T;
 89
 90
    struct node {
91
       T v; /* value of this node */
 92
       int r; /* random priority */
 93
       int eq; /* the number of equal things */
 94
       int s; /* the size of subtree rooted at this */
       node *ch[2]; /* 0 for left child, 1 for right child. */
 95
       node(void) {
 96
 97
         r = rand();
 98
         ch[0] = ch[1] = NULL;
 99
100
      /* return where to insert x */
101
       int cmp(T x) {
102
         if(v == x) return -1;
103
         else return (x < v) ? 0 : 1;
104
105
       /* return 1 if this node is prior to other */
106
       int pri(node *o) {
107
         return (r > (o->r));
108
109
       /* maintain the s field */
110
       void maintain(void) {
111
         s = eq;
112
         if(NULL != ch[0]) s += ch[0]->s;
113
         if(NULL != ch[1]) s += ch[1]->s;
      }
114
115
116
117
     /* move o to ch[d] of o->ch[d^1] */
118
    void rotate(node *&o, int d) {
       node *k = o\rightarrow ch[d^1];
119
120
       o\rightarrow ch[d^1] = k\rightarrow ch[d];
121
       o->maintain();
122
       k\rightarrow ch[d] = o;
123
       k->maintain();
124
       o = k;
125
```

## 1.6 Leftist Heap

```
|/* HDU 1512 Monkey King(左偏树模板题) */
   #include<iostream>
3
   #include<cstdio>
4
   using namespace std;
5
   const int maxn = 100000+5;
6
7
   int n, m;
8
9
   struct Heap {
10
     int l,r,fa,val,dis;
11
   } t[maxn];
12
13
   int finds(int x) {
14
15
     return t[x].fa == -1? x:t[x].fa = finds(t[x].fa);
16
   }
17
   int merge(int x, int y) {
18
                            //如果为0的话,就说明是空子树,根节点当然就是另一节点了
19
     if(x == 0) return y;
     if(y == 0) return x;
20
21
     if(t[y].val>t[x].val)
                          swap(x,y); //始终往右子树进行插入
22
     t[x].r = merge(t[x].r,y);
23
     t[t[x].r].fa = x;
24
     if(t[t[x].l].dis < t[t[x].r].dis) swap(t[x].l,t[x].r); //是否需要左右子树的对换,
        这样是为了右子树尽量短
25
     if(t[x].r == 0) t[x].dis = 0;
                                   //距离的重新分配
26
     else t[x].dis = t[t[x].r].dis + 1;
27
     return x;
   }
28
29
30
   int pop(int &root) {
31
     int l = t[root].l;
32
     int r = t[root].r;
33
     t[root].l = t[root].r = t[root].dis = 0;
34
     t[root].fa = -1;
35
     t[1].fa = t[r].fa = -1; //删除root根节点
     return merge(l,r);
36
                             //这样一来相当于分裂成了两棵子树,重新进行合并,最后返回值
        为合并后的根节点
37
38
39
   int push(int x, int y) {
40
     return merge(x,y);
41
42
43
   int main() {
     //freopen("in.txt","r",stdin);
44
45
     while(~scanf("%d",&n)) {
46
       for(int i=1; i<=n; i++) {
47
         t[i].l=t[i].r=t[i].dis=0;
48
         t[i].fa=-1;
         scanf("%d",&t[i].val);
49
50
51
       scanf("%d",&m);
       while(m—) {
52
53
         int a,b;
         scanf("%d%d",&a,&b);
54
55
         int x=finds(a);
56
         int y=finds(b);
         if(x!=y) {
57
58
           t[x].val/=2;
59
           int xx = push(pop(x),x);
60
           t[y].val/=2;
```

```
61
            int yy = push(pop(y),y);
            printf("%d\n",t[merge(xx,yy)].val);
62
63
          } else puts("-1");
64
65
66
      return 0;
67
   1.7 Splay
   /* splay, by Abreto<m@abreto.net>. */
 2
 3
   #ifndef NULL
 4
   #define NULL 0
 5
   #endif
 6
 7
   struct node {
 8
      node *f, *ch[2];
 9
      int sz;
10
      node(node *fa = NULL, node *lc = NULL, node *rc = NULL) {
11
        f = fa;
12
        ch[0] = lc;
        ch[1] = rc;
13
14
        maintain();
15
16
      inline int szof(const int d) const {
17
        return ch[d] ? ch[d]->sz : 0;
18
19
      inline void maintain(void) {
20
        sz = szof(0) + szof(1) + 1;
21
22
      inline int which(void) {
23
        if (NULL == f) return 0;
24
        return (f->ch[1] == this); /* f[which()] == this */
25
      inline node *setf(node *fa, int d = 0) {
26
27
        f = fa;
28
        if (f) {
29
          f->ch[d] = this;
30
          f->maintain();
31
        }
32
        return f;
33
34
      inline node *setc(node *son, int d = 0) {
35
        ch[d] = son;
36
        if (son) son—>f = this;
37
        maintain();
38
        return this;
39
40
      /* rotate this to its fater, return this. */
41
      inline node *rotate(void) {
        if (f != NULL) {
42
          node *ff = f \rightarrow f;
43
44
          int d = which(), fd = f->which();
45
          setc(f->setc(ch[d ^ 1], d), d ^ 1);
46
          setf(ff, fd);
47
        }
48
        return this;
49
      /* splay this to child of target */
50
51
      inline node *splay(node * const target = NULL) {
52
        while (f != target) {
53
          if (target != f \rightarrow f) {
```

```
54
            ( (which() == f->which()) ? f : this )->rotate();
55
56
          rotate();
57
58
        return this;
59
60
      /* 0-based rank */
61
      inline node *get_k_th(unsigned k) {
62
        node *p = this;
63
        int rank;
64
        while (k != (rank = (p\rightarrow szof(0))))  {
65
          if (k < rank) {
66
            p = p - sh[0];
67
          } else {
            k = (rank + 1);
68
69
            p = p \rightarrow ch[1];
70
71
72
        return p->splay(f);
73
74
   };
   /* HDU 3487 - Play with Chain, by Abreto<m@abreto.net>. */
 2
   #include <bits/stdc++.h>
 3
 4
   using namespace std;
 5
 6
   #define MAXN
                     300300
 7
 8
   int n, m;
9
10
   #define LC(p)
                     ch[p][0]
11
   #define RC(p)
                     ch[p][1]
   #define TARGET(p) LC(RC(p))
12
13
14
   int nodes;
    int val[MAXN], ch[MAXN][2], fa[MAXN], sz[MAXN];
15
16
    int rev[MAXN];
17
18
   inline int new_node(int v, int f) {
19
      int p = (++nodes);
20
      val[p] = v;
      fa[p] = f;
21
22
      ch[p][0] = ch[p][1] = rev[p] = 0;
23
      sz[p] = 1;
24
      return p;
25
26
   inline void maintain(int p) {
27
      if (p) {
28
        sz[p] = sz[LC(p)] + sz[RC(p)] + 1;
29
30
    inline void make_child(int f, int d, int p) { /* make p the d-th ch of f */
31
32
      ch[f][d] = p;
33
      if(p) fa[p] = f;
34
35
   inline void myrev(int p) {
36
      if (p) {
37
        rev[p] ^= 1;
38
        swap(LC(p), RC(p));
39
40
41
   inline void pushdown(int p) {
     if(p && rev[p]) {
```

```
43
         if(LC(p)) myrev(LC(p));
         if(RC(p)) myrev(RC(p));
44
45
         rev[p] = 0;
 46
47
48
    int build(int f = 0, int l = 0, int r = n+1) {
49
      if(r < l) return 0;
 50
      if(l == r) return new_node(l, f);
      int mid = 1+r>>1;
51
52
      int p = new_node(mid, f);
53
      LC(p) = build(p, l, mid-1);
54
      RC(p) = build(p, mid+1, r);
      maintain(p);
55
56
      return p;
57
58
    inline int which(int p) { /* return 1 if p is a right child or 0 if p is a left
        child. */
59
      return (RC(fa[p]) == p);
 60
61
    inline int rotate(int p) { /* rotate p to its father. [!] make sure p is not global
        root. */
62
       int f = fa[p], ff = fa[f];
63
      if(0 == f) return p; /* p is global root */
64
      pushdown(f);
65
      pushdown(p);
66
      int d = which(p), df = which(f);
67
      make\_child(f, d, ch[p][d^1]);
68
      make\_child(p, d^1, f);
69
      maintain(f);
70
      maintain(p);
71
      fa[p] = ff
 72
      if(ff) ch[ff][df] = p;
73
       return p;
74
75
    inline int splay(int p, int fr) \{ /* \text{ splay p to the son of fr, return p. }*/
      pushdown(p);
76
77
      while(fa[p] != fr) {
78
         int f = fa[p], dp = which(p);
79
         if(fa[f] == fr) {
80
           return rotate(p);
81
         } else {
 82
           int df = which(f);
83
           if(dp == df) {
84
             rotate(f);
 85
           } else {
 86
             rotate(p);
87
88
           rotate(p);
89
         }
90
91
      return p;
92
93
    inline int get_k_th(int root, int k) {
94
       int p = root;
95
       int rank;
96
      while(k != (rank = (sz[LC(p)] + 1))) {
97
         pushdown(p);
         if(k < rank) p = LC(p);
98
99
         else {
100
           k = rank;
101
           p = RC(p);
         }
102
103
      return splay(p, fa[root]);
104
```

```
105
106
    inline int merge(int left, int right) {
107
       pushdown(left);
108
       if(RC(left)) left = get_k_th(left, sz[left]);
109
       RC(left) = right;
110
       maintain(left);
111
       fa[right] = left;
112
       return left;
113
114
    inline int split(int root, int d) { /* split ch[root][d], return the root of splited
        out. */
115
       pushdown(root);
       int child = ch[root][d];
116
       ch[root][d] = 0;
117
118
       maintain(root);
119
       fa[child] = 0;
120
       return child;
121
122
    inline int concat(int root, int d, int p) { /* make p be ch[root][d], return root */
123
       pushdown(root);
124
       ch[root][d] = p;
125
       fa[p] = root;
126
       maintain(root);
127
       return root;
128
129
130
    void myclear(void) {
131
       nodes = 0;
132
133
134
     int ans[MAXN]:
     void inorder(int p, int &pos) {
135
136
       if(0 == p) return;
137
       pushdown(p);
138
       inorder(LC(p), pos);
139
       if( (0 < val[p]) && (val[p] < n+1) ) ans[pos++] = val[p];
140
       inorder(RC(p), pos);
141
142
143
     void handle() {
144
       int i;
145
       int root;
146
       myclear();
147
       root = build(0);
148
       while(m——) {
149
         char command[8];
150
         int a, b, c;
151
         int tar;
         scanf("%s%d%d", command, &a, &b);
152
         if('C' == command\lceil 0 \rceil) {
153
           scanf("%d", &c);
154
155
           root = get_k_th(root, a);
156
           RC(root) = get_k_t(RC(root), b-a+2);
157
           tar = split(RC(root), 0);
158
           maintain(root);
159
           root = get_k_th(root, c+1);
160
           RC(root) = get_k_t(RC(root), 1);
161
           RC(root) = concat(RC(root), 0, tar);
162
           maintain(root);
163
         } else {
164
           root = get_k_th(root, a);
165
           RC(root) = get_k_th(RC(root), b-a+2);
166
           myrev(TARGET(root));
         }
167
```

```
168
169
       int pos = 0;
170
       inorder(root, pos);
       for(i = 0; i < n; i++) printf("%s%d", i ? "_{\bot}":"", ans[i]);
171
172
       puts("");
173
174
175
     int main(void) {
  while( scanf("%d%d", &n, &m) && (n > 0) && (m > 0) )
176
          handle();
177
178
        return 0;
179 | }
```

## 1.8 Persistent Segment Tree

- 1. 首先, 给你一颗值为横坐标的线段树, 每个节点上存着该值出现了多少次, 这样的一颗线段树 你会求区间 k 大值吧. 二分即可.
- 2. 然后, 假设区间是数组 arr[n], 区间长度是 n, 那么给你 n 颗线段树, 第 i 颗线段树是第 i-1 颗线段树插入 arr[i] 得到.
- 3. 如果你有了这 n 颗线段树, 想求区间 [l,r] 中的第 k 大值, 那么你需要在第 r 颗和第 l-1 颗 线段树的差线段树上作二分, 就可以求得区间第 k 大值.
- 4. 差线段树很好理解, 比如你有一个部分和数组 sum, sum[r] sum[l-1] 就是部分和的差, 代表区间 [l,r] 的和, 差线段树同理.
- 5. 现在, 可持久化线段树出现为你解决最后一个问题, 空间问题. 内存很小, 不能够存下 n 颗线段树. 但是, 第 2 条中提到, 由于第 i 颗线段是是第 i-1 颗线段是插入仅一个值得到的, 两颗线段树的区别不大, 仅有  $\log(n)$  个节点发生了改变, 我们仅仅需要记录这  $\log(n)$  的数据就可以记录这个增量, 这就是可持久化线段树.

## 2 Dynamic Programming

## **2.1** LIS $O(n \log n)$

```
1
 2
   int top = 0;
   for( int i=1; i<=n; i++ ) {
 3
     if( ap[i] > dp[top] ) { // 如果大于 "模拟栈" 的栈顶元素直接 入栈 长度加 1
 4
 5
 6
       dp[top] = ap[i];
 7
       continue;
 8
 9
     int m = ap[i];
10
     // lower_bound 前闭后开 返回不小于 m 的最小值的位置
11
     pos = lower_bound(dp,dp+top,m)-dp; // 注意减去dp
12
     if(dp[pos] > ap[i])
       dp[pos] = ap[i];
13
14 | }
```

## 2.2 LCS $O(n \log n)$

总的来说,就是把 LCS 转化成 LIS,然后用 LIS 的  $\mathcal{O}(N \log N)$  算法来求解。 实现如下:(引用) 假设有两个序列  $s_1[1 \dots 6] = abcadc, s_2[1 \dots 7] = cabedab.$ 记录  $s_1$  中每个元素在  $s_2$  中出现的位置,再将位置按降序排列,则上面的例子可表示为:  $loc(a) = \{6,2\}, loc(b) = \{7,3\}, loc(c) = \{1\}, loc(d) = \{5\}.$  (倒着扫一遍  $s_2$  即可把位置扔进 vector). 将  $s_1$  中每个元素的位置按  $s_1$  中元素的顺序排列成一个序列  $s_3 = \{6, 2, 7, 3, 1, 6, 2, 5, 1\}$ . 在对  $s_3$  求 LIS 得到的值即为求 LCS 的答案。

## 2.3 Improved by quadrilateral inequality

```
1
   /*
 2
    * 四边形不等式
 3
 4
    * 如果 dp(i,j) 满足 dp(i,j)<=dp(i,j+1)<=dp(i+1,j+1)
 5
    * 那么决策 S(i,j) 满足 S(i,j)<=S(i,j+1)<=S(i+1,j+1)
 6
     * 可以变形为:
 7
            s(i-1,j) \le s(i,j) \le s(i,j+1) // dp方向: i增j减
 8
       或
    *
            s(i,j-1) \Leftarrow s(i,j) \Leftarrow s(i+1,j) // dp方向: 区间长度L增
 9
    *
10
11
   #include <bits/stdc++.h>
12
   using namespace std;
13
14
15
   #define MAXN
                    1024
16
   #define inf
                    (0x3fffffff)
17
   int n, m;
18
19
   int v[MAXN];
20
   int s[MAXN];
21
   int w[MAXN][MAXN];
22
   int dp[MAXN][MAXN];
23
   int c[MAXN][MAXN];
24
25
   int wa(void) {
     int i, j, k;
26
      for(i = 1; i \le n; ++i) {
27
        scanf("%d", v+i);
28
        s[i] = v[i] + s[i-1];
29
30
31
     for(i = 1; i <= n; ++i) {
32
        w[i][i] = 0;
        for(j = i+1; j \le n; ++j)
33
34
          w[i][j] = w[i][j-1] + v[j] * (s[j-1] - s[i-1]);
35
36
     /* doing dp */
37
     for(i = 1; i <= n; ++i) {
38
        dp[i][0] = w[1][i];
39
        c[i][0] = 1;
40
        c[i][i] = i-1;
41
        for(j = i-1; j > 0; j---) {
42
          dp[i][j] = inf;
43
          for(k = c[i-1][j]; k \le c[i][j+1]; ++k)
44
            if(dp[k][j-1]+w[k+1][i] \leftarrow dp[i][j]) {
45
              dp[i][j] = dp[k][j-1] + w[k+1][i];
46
              c[i][j] = k;
            }
47
48
        }
49
50
     /* dp done */
51
     return dp[n][m];
52
53
54
   int main(void) {
     while(EOF != scanf("%d%d", &n, &m) && n && m) {
55
        printf("%d\n", wa());
56
57
58
     return 0;
```

## 2.4 Improved by Slope

```
1 |/* type 1: */
   /* bzoj 1010 */
 2
 3
   #include <bits/stdc++.h>
 5
   using namespace std;
   typedef long double 11;
 6
 7
   #define MAXN
                    50050
 8
   #define eps
                    (1e-8)
 9
10
   int N;
11
   11 L;
   11 S[MAXN];
12
13
   11 f[MAXN];
   11 dp[MAXN];
14
15
16
   inline ll k(int j) {
17
     return (-2.0) * (f[j] + L);
18
19
   inline ll b(int j) {
      return dp[j] + f[j]*f[j] + 2ll*f[j]*L;
20
21
22
   inline ll g(int j, int i) {
23
      return k(j) * f[i] + b(j);
24
25
26
   /* check if l1 & l3 <= l2 */
   inline int check(int l1, int l2, int l3) {
27
28
     /*ll\ left = b(l3)*k(l1)+b(l1)*k(l2)+b(l2)*k(l3);
29
     ll right = b(l1)*k(l3)*b(l3)*k(l2)*b(l2)*k(l1);*/
30
     ll\ left = b(l3)*k(l1)-b(l1)*k(l3);
31
     ll right = k(l2)*(b(l3)-b(l1))+b(l2)*(k(l1)-k(l3));
32
      return (left <= right);</pre>
33
34
35
   int Q[MAXN], ql, qr;
36
37
   int main(void) {
     int i;
38
39
     scanf("%d%Lf", &N, &L);
40
     L += 1.0;
41
      for(i = 1; i \le N; ++i) 
        scanf("%Lf", S+i);
42
        S[i] += S[i-1];
43
44
        f[i] = S[i] + (double)i;
45
46
     Q[qr++] = 0;
47
     for(i = 1; i <= N; ++i) {
48
        /* <!-- STARED */
49
        for(; ql+1 < qr && g(Q[ql],i) >= g(Q[ql+1],i); ql++);
50
        dp[i] = g(Q[ql], i) + f[i]*f[i] + L*L; //printf("%d: %lld,%lld\n", i, dp[i], dp[i])
           ]_f[i]*f[i]);
51
        for(; ql+1 < qr \& check(Q[qr-2], Q[qr-1], i); qr--);
52
        Q[qr++] = i;
53
        /* --> */
54
55
     printf("%lld\n", (long long int)round(dp[N]));
56
      return 0;
57
```

## 2.5 Steiner Tree

令 f[i][sta] 表示 i 号节点,与其他节点的连通性为 sta 时的最小代价,这里 sta 是一个二进制数,在它二进制下的每一位中,0 表示不连通,1 表示联通 状态转移:

• 由子集转移而来

$$f[i][sta] = \min_{s \subseteq sta} \{f[i][s] + f[i][sta \setminus s] - val[i]\}$$

• 由不含该节点的状态转移而来

$$f[i][j] = \min\{f[k][j] + val[i]\}$$

```
1
   |#include<cstdio>
 2
   #include<queue>
   #include<cstring>
   usina namespace std;
   const int limit = 1050;
 6
    const int INF = 1e9;
 7
    inline int read() {
 8
      char c = getchar();
      int x = 0, f = 1;
 9
      while(c < '0' || c > '9') {
10
        if(c == '-') f = -1;
11
12
        c = getchar();
13
      }
      while(c >= '0' && c <= '9') {
14
        x = x * 10 + c - '0';
15
16
        c = getchar();
17
18
      return x * f;
19
   #define MP(i,j) make_pair(i,j)
21
   #define se second
   #define fi first
22
    #define Pair pair<int,int>
23
24
    int N, M, tot = 0;
    int a[12][12], f[12][12][limit];
25
26
   int xx[5] = \{-1, +1, 0, 0\};
    int yy[5] = \{0, 0, -1, +1\};
27
28
   int vis[12][12];
29
   struct PRE {
30
      int x, y, S;
    } Pre[12][12][limit];
31
32
    queue<Pair>q;
33
    void SPFA(int cur) {
34
      while(q.size() != 0) {
35
        Pair p = q.front();
36
        q.pop();
        vis[p.fi][p.se] = 0;
37
        for(int i = 0; i <4; i++) {
38
          int wx = p.fi + xx[i], wy = p.se + yy[i]; if(wx < 1 \mid \mid wx > N \mid \mid wy < 1 \mid \mid wy > M) continue;
39
40
41
           if(f[wx][wy][cur] > f[p.fi][p.se][cur] + a[wx][wy]) {
42
             f[wx][wy][cur] = f[p.fi][p.se][cur] + a[wx][wy];
43
            Pre[wx][wy][cur] = (PRE) {
44
               p.fi, p.se, cur
45
46
             if(!vis[wx][wy])
47
               vis[wx][wy] = 1, q.push(MP(wx,wy));
48
49
        }
```

```
50
       }
 51
    }
 52
     void dfs(int x, int y, int now) {
 53
       vis[x][y] = 1;
 54
       PRE tmp = Pre[x][y][now];
 55
       if(tmp.x == 0 \&\& tmp.y == 0) return;
 56
       dfs(tmp.x, tmp.y, tmp.S);
 57
       if(tmp.x == x \& tmp.y == y) dfs(tmp.x, tmp.y, now - tmp.S);
 58
 59
     int main() {
       //freopen("a.in", "r", stdin);
 60
 61
       N = read();
 62
       M = read();
       memset(f, 0x3f, sizeof(f));
 63
 64
       for(int i = 1; i <= N; i++)
 65
         for(int j = 1; j <= M; j++) {
 66
           a[i][j] = read();
 67
           if(a[i][j] == 0)
 68
             f[i][j][1 << tot] = 0, tot++;
 69
 70
       int limit = (1 \ll tot) - 1;
 71
       for(int sta = 0; sta <= limit; sta++) {</pre>
 72
         for(int i = 1; i <= N; i++)
 73
           for(int j = 1; j <= M; j++) {
 74
             for(int s = sta; s; s = (s - 1) \& sta) {
 75
                if(f[i][j][s] + f[i][j][sta - s] - a[i][j] < f[i][j][sta])
 76
                  f[i][j][sta] = f[i][j][s] + f[i][j][sta - s] - a[i][j],
 77
                  Pre[i][j][sta] = (PRE) {
 78
                  i,j,s
 79
               };
 80
 81
             if(f[i][j][sta] < INF) q.push(MP(i,j)), vis[i][j] = 1;
 82
         SPFA(sta);
 83
 84
 85
       int ansx, ansy, flag = 0;
       for(int i = 1; i <= N && !flag; i++)
for(int j = 1; j <= M; j++)</pre>
 86
 87
 88
           if(!a[i][j]) {
 89
             ansx = i, ansy = j;
 90
             flag = 1;
 91
             break;
 92
 93
       printf("%d\n",f[ansx][ansy][limit]);
 94
       memset(vis, 0, sizeof(vis));
 95
       dfs(ansx, ansy, limit);
 96
       for(int i = 1; i <= N; i++, puts("")) {
 97
         for(int j = 1; j <= M; j++) {
 98
           if(a[i][j] == 0) putchar('x');
           else if(vis[i][j]) putchar('o');
 99
100
           else putchar('_');
101
102
103
       return 0;
104 | }
```

## 3 Geometry

## 3.1 2D

3.1.1 Point

```
/* 2D Point Class, by Abreto<m@abreto.net> */
 1
 2
   #include <cmath>
 3
 4
    /**
 5
    * Define ABG2d_USE_LL if you want to use long long int for cordnates.
 6
 7
 8
   namespace ab_geometry_2d {
 9
10
   using namespace std;
11
12
   typedef double ab_float;
13
   const ab_float pi = acos(-1.);
14
15
16
   #ifdef ABG2d_USE_LL
17
   typedef long long int T;
18
   #else
19
   typedef ab_float T;
20
   const ab_float eps = 1e-8;
21
   #endif
22
   inline T myabs(T x) {
23
24
      if(x < 0) return (-x);
25
      return x;
26
27
   inline int sgn(T x) {
  /* no difference' in fact */
28
29
30
   #ifdef ABG2d_USE_LL
31
      if (0 == x) return 0;
32
   #else
33
      if (myabs(x) < eps) return 0;
34
   #endif
35
      return (x > 0) ? 1 : -1;
36
37
38
    inline T sqr(T x) {
39
      return (x * x);
40
41
42
    struct point {
43
      T x, y;
44
      point(void):x(T()),y(T()) {}
      point(T xx, T yy):x(xx),y(yy) {}
45
46
      inline T norm2(void) {
        return sqr(x) + sqr(y);
47
48
49
      inline ab_float norm(void) {
        return sqrt((ab_float)(norm2()));
50
51
52
      inline point rotate(const ab_float &cost, const ab_float &sint) {} // TODO:
53
      inline point operator—(void) const {
54
        return point(-x,-y);
55
56
      inline point operator+(const point& b) const {
57
        return point(x+b.x,y+b.y);
58
59
      inline point operator-(const point& b) const {
60
        return point(x-b.x,y-b.y);
61
62
      inline point operator->*(const point &b) const {
63
        return (b-(*this));
64
      }
```

```
65
     inline T operator*(const point& b) const {
66
        return ((x)*(b.x))+((y)*(b.y)); /* inner product */
67
68
     inline T operator^(const point& b) const {
69
        return ((x)*(b.y))-((b.x)*(y)); /* outter product */
70
71
     inline point& operator+=(const point& b) {
72
        point tmp=(*this)+b;
73
        (*this)=tmp;
74
       return (*this);
75
76
     inline point& operator—=(const point& b) {
77
       point tmp=(*this)_b;
78
       (*this)=tmp;
79
        return (*this);
80
81
     inline bool operator==(const point& b) const {
        return (0==sgn(x-b.x))&(0==sgn(y-b.y));
82
83
84
     inline bool operator!=(const point& b) const {
85
        return !((*this)==b);
86
87
     inline point operator<<(const ab_float& theta) const {
       ab_float ct = cos(theta), st = sin(theta); /* rotate counter-clockwise in radian
88
89
        return point(ct*x - st*y, st*x + ct*y);
90
91
   };
92
93
   typedef point vec;
94
95
96 |}
       // namespace ab_geometry_2d
   3.1.2 Circle
   Base
   /* 2D Circle Base Class, by Abreto<m@abreto.net>. */
 1
 2
 3
   /* requirement: point.cc */
 4
   #include "point.cc"
 5
 6
   #include <utility>
 8
   namespace ab_geometry_2d {
 9
10
   using namespace std;
11
12
   struct circle {
13
     point o;
14
     Tr;
15
     circle(void) : r(T()) {}
     circle(point center, T radius) : o(center), r(radius) {}
16
17
     inline ab_float arclen(ab_float theta) {
18
19
       return theta * r;
20
     inline ab_float circumference(void) {
21
22
        return 2. * pi * r;
23
24
      inline ab_float area(void) {
25
        return pi * r * r;
```

```
26
      }
27
28
      /* bool contain(const circle &C, const bool including_touch = false) const
29
30
          T dis2 = (o \rightarrow *(C.o)).norm2();
31
          T raw_diff = r - C.r;
32
          if (-1 == sqn(raw_diff)) return false;
          T dr2 = sqr(raw_diff);
33
          return (dis2 < dr2) || (including_touch && (dis2 == dr2));
34
35
36
      inline bool in(const circle &C, const bool including_touch = false) const
37
      {
        return C.contain(*this, including_touch);
38
39
      } */
40
      enum relation_t {
41
        same = 0 \times 00000,
42
        contain = 0 \times 00001,
43
        intouch = 0 \times 00010,
44
        intersect = 0x00100,
45
        outtouch = 0x01000,
46
        separate = 0x10000,
47
        unknow_relation = 0xfffff
48
      };
49
      relation_t with(const circle &C) const {
50
        T dis2 = (o \rightarrow *(C.o)).norm2();
51
        T dr2 = sqr(r - C.r), rs2 = sqr(r + C.r);
52
        if (0 == sgn(dis2) \&\& 0 == sgn(dr2)) return same;
53
        if (-1 == sgn(dis2 - dr2)) return contain;
54
        if (0 == sgn(dis2 - dr2)) return intouch;
             -1 = sgn(dr2 - dis2) \&\& -1 = sgn(dis2 - rs2)) return intersect;
55
        if ( 0 == sgn(dis2 - rs2) ) return outtouch;
56
        if (-1 == sgn(rs2 - dis2)) return separate;
57
58
        return unknow_relation;
      }
59
60
61
      enum point_relation_t {
62
        in = 0x001,
63
        on = 0x010,
64
        out = 0x100.
65
        unknow_point_relation = 0xfff
66
      };
67
      point_relation_t with(const point &P) const {
68
        T dis2 = (o\rightarrow *P).norm2();
69
        T r2 = sqr(r);
70
        int type = sgn(dis2 - r2);
        if (-1 == type) return in; if (0 == type) return on;
71
72
73
        if (+1 == type) return out;
74
        return unknow_point_relation;
75
      }
76
77
      ab_float central_angle(const point &A, const point &B, const bool reflex = false)
         const {
        T dot = (A * B);
78
        if (0 == sgn(dot)) return 1. * (A != B) * pi;
79
        ab_float angle = ((ab_float)(dot)) / r / r;
80
81
        if (reflex) angle = 2. * pi - angle;
82
        return angle;
83
      }
84
85
      /* be sure (*this) intersect with C */
      pair<point, point> crosspoint(const circle &C) const {
86
87
        ab_float d = (o \rightarrow * (C.o)).norm();
88
        // TODO:
```

```
89
90
   };
91
92 |}
   k 次圆交
 1 | // china no.1
   #pragma comment(linker, "/STACK:1024000000,1024000000")
 3
   #include <vector>
 4
   #include <iostream>
 5
   #include <string>
   |#include <map>
 6
 7
   #include <stack>
 8
   |#include <cstring>
 9
   #include <queue>
10
   #include <list>
11
   #include <stdio.h>
12
   #include <set>
13 |#include <algorithm>
   #include <cstdlib>
15
   |#include <cmath>
   |#include <iomanip>
16
17
   #include <cctype>
18
   |#include <sstream>
19
   |#include <functional>
20
   #include <stdlib.h>
21
   |#include <time.h>
22
   #include <bitset>
23
   using namespace std;
24
25
   #define pi acos(-1)
   #define PI acos(-1)
26
   #define endl '\n'
27
   #define srand() srand(time(0));
   #define me(x,y) memset(x,y,sizeof(x));
   #define foreach(it,a) for(__typeof((a).begin()) it=(a).begin();it!=(a).end();it++)
31
   #define close() ios::sync_with_stdio(0); cin.tie(0);
   #define FOR(x,n,i) for(int i=x;i <=n;i++)
32
33
   #define F0r(x,n,i) for(int i=x;i<n;i++)</pre>
34
   #define W while
35
   #define sgn(x) ((x) < 0 ? -1 : (x) > 0)
   #define bug printf("*********n");
36
37
   #define db double
38
   typedef long long LL;
39
   const int INF=0x3f3f3f3f;
40
   const LL LINF=0x3f3f3f3f3f3f3f3f3f1LL;
   const int dx[] = \{-1,0,1,0,1,-1,-1,1\};
41
42
   const int dy[] = \{0,1,0,-1,-1,1,-1,1\};
43
   const int maxn=1e3+10;
   const int maxx=1e6+100;
45
   const double EPS=1e-8;
46
   const double eps=1e-8;
47
   const int mod=10000007;
48
   template<class T>inline T min(T a,T b,T c) {
49
      return min(min(a,b),c);
50
51
   template<class T>inline T max(T a,T b,T c) {
52
      return max(max(a,b),c);
53
54
   template<class T>inline T min(T a,T b,T c,T d) {
55
      return min(min(a,b),min(c,d));
56
57
   template<class T>inline T max(T a,T b,T c,T d) {
     return max(max(a,b),max(c,d));
```

```
59 |}
 60
    template <class T>
 61
     inline bool scan_d(T &ret) {
 62
       char c;
 63
       int sgn;
 64
       if (c = getchar(), c == EOF) {
 65
         return 0;
 66
       while (c != '-' \&\& (c < '0' || c > '9')) {
 67
 68
         c = getchar();
 69
       sgn = (c == '-') ? -1 : 1;
 70
       ret = (c == '-') ? 0 : (c - '0');
 71
       while (c = getchar(), c >= '0' && c <= '9') {
 72
         ret = ret * 10 + (c - '0');
 73
 74
 75
       ret *= sgn;
 76
       return 1;
 77
     }
 78
 79
     inline bool scan_lf(double &num) {
 80
       char in;
 81
       double Dec=0.1;
 82
       bool IsN=false,IsD=false;
       in=getchar();
 83
 84
       if(in==EOF) return false;
 85
       while(in!='-'&&in!='.'&&(in<'0'||in>'9'))in=getchar();
 86
       if(in=='-') {
 87
         IsN=true;
 88
         num=0;
 89
       } else if(in=='.') {
 90
         IsD=true;
 91
         num=0;
 92
       } else num=in-'0';
 93
       if(!IsD) {
         while(in=getchar(),in>='0'&&in<='9') {</pre>
 94
 95
           num*=10;
 96
           num+=in-'0';
 97
         }
 98
       if(in!='.') {
 99
100
         if(IsN) num=-num;
101
         return true;
       } else {
102
         while(in=getchar(),in>='0'&&in<='9') {
103
104
           num+=Dec*(in-'0');
105
           Dec*=0.1;
         }
106
107
108
       if(IsN) num=-num;
109
       return true;
110
111
     void Out(LL a) {
112
       if(a < 0) {
  putchar('-');</pre>
113
114
115
         a = -a;
116
117
       if(a >= 10) Out(a / 10);
118
       putchar(a % 10 + '0');
119
120
     void print(LL a) {
121
       Out(a), puts("");
122 |}
```

```
//freopen( "in.txt" , "r" , stdin );
//freopen( "data.txt" , "w" , stdout );
//cerr << "run time is " << clock() << endl;</pre>
123
124
125
126
    /*struct Point
127
128
         double x, y;
129
         Point(const Point& rhs): x(rhs.x), y(rhs.y) { } //拷贝构造函数
130
         Point(double x = 0, double y = 0) : x(x), y(y) { }
131
         inline void input()
132
             scanf("%lf%lf",&x,&y);
133
134
         inline void print()
135
136
137
             printf("%.6lf %.6lf\n",x,y);
138
         }
139
     };*/
     db sqr(db x) {
140
141
       return x*x;
142
143
     int dcmp(double x) {
       if(fabs(x) < EPS) return 0;
144
145
       else return x < 0 ? -1 : 1;
146
     struct Circle {
147
148
       double x, y, r, angle;
149
       int d;
150
       Circle() {}
151
       Circle(double xx, double yy, double ang = 0, int t = 0) {
152
153
         y = yy;
154
         angle = ang;
155
         d = t;
156
157
       void get() {
158
         scanf("%lf%lf%lf", &x, &y, &r);
159
         d = 1;
160
161
162
     Circle cir[maxn],tp[maxn*2];
163
     double area[maxn];
164
     double dis(Circle a,Circle b) {
165
       return sqrt(sqr(a.x - b.x) + sqr(a.y - b.y));
166
167
     double cross(Circle p0,Circle p1,Circle p2) {
168
       return (p1.x - p0.x) * (p2.y - p0.y) - (p1.y - p0.y) * (p2.x - p0.x);
169
     //圆相交
170
171
    int CirCrossCir(Circle p1, double r1, Circle p2, double r2, Circle &cp1, Circle &cp2) {
172
       double mx = p2.x - p1.x, sx = p2.x + p1.x, mx2 = mx * mx;
173
       double my = p2.y - p1.y, sy = p2.y + p1.y, my2 = my * my;
174
       double sq = mx^2 + my^2, d = -(sq - sqr(r^1 - r^2)) * (sq - sqr(r^1 + r^2));
175
       if (d + eps < 0) return 0;
       if (d < eps) d = 0;
176
177
       else d = sqrt(d);
178
       double x = mx * ((r1 + r2) * (r1 - r2) + mx * sx) + sx * my2;
179
       double y = my * ((r1 + r2) * (r1 - r2) + my * sy) + sy * mx2;
180
       double dx = mx * d, dy = my * d;
181
       sq *= 2;
182
       cp1.x = (x - dy) / sq;
183
       cp1.y = (y + dx) / sq;
184
       cp2.x = (x + dy) / sq;
185
       cp2.y = (y - dx) / sq;
       if (d > eps) return 2;
186
```

```
187
       else return 1;
188
189
     bool circmp(const Circle& u, const Circle& v) {
190
       return dcmp(u.r - v.r) < 0;
191
192
     bool cmp(const Circle& u, const Circle& v) {
193
       if (dcmp(u.angle - v.angle)) return u.angle < v.angle;</pre>
194
       return u.d > v.d;
195
196
     //0.5*r*r*(K-sin(K))
197
     double calc(Circle cir,Circle cp1,Circle cp2) {
198
       double ans = (cp2.angle - cp1.angle) * sqr(cir.r)
199
                    - cross(cir, cp1, cp2) + cross(Circle(0, 0), cp1, cp2);
200
       return ans / 2;
201
202
203
     void CirUnion(Circle cir□, int n) {
204
       Circle cp1, cp2;
205
       sort(cir, cir + n, circmp);
       for (int i = 0; i < n; ++i)
206
         for (int j = i + 1; j < n; ++j)
207
208
           if (dcmp(dis(cir[i], cir[j]) + cir[i].r - cir[j].r) <= 0)</pre>
209
             cir[i].d++;
210
       for (int i = 0; i < n; ++i) {
211
         int tn = 0, cnt = 0;
212
         for (int j = 0; j < n; ++j) {
213
           if (i == j) continue;
214
           if (CirCrossCir(cir[i], cir[i].r, cir[j], cir[j].r,
215
                            cp2, cp1) < 2) continue;
           cp1.angle = atan2(cp1.y - cir[i].y, cp1.x - cir[i].x);
216
           cp2.angle = atan2(cp2.y - cir[i].y, cp2.x - cir[i].x);
217
218
           cp1.d = 1;
219
           tp[tn++] = cp1;
           cp2.d = -1;
220
221
           tp[tn++] = cp2;
222
           if (dcmp(cp1.angle - cp2.angle) > 0) cnt++;
223
224
         tp[tn++] = Circle(cir[i].x - cir[i].r, cir[i].y, pi, -cnt);
225
         tp[tn++] = Circle(cir[i].x - cir[i].r, cir[i].y, -pi, cnt);
226
         sort(tp, tp + tn, cmp);
227
         int p, s = cir[i].d + tp[0].d;
228
         for (int j = 1; j < tn; ++j) {
229
           p = s;
230
           s += tp[j].d;
231
           area[p] += calc(cir[i], tp[j - 1], tp[j]);
232
         }
233
       }
234
235
     int n;
236
     void solve() {
237
       for(int i=0; i<n; i++)
238
         cir[i].get();
239
       me(area, 0);
240
       CirUnion(cir,n);
241
       for(int i=1; i<=n; i++) {
242
         area[i]=area[i+1];
243
         printf("[%d]_{\perp}=_{\perp}%.3f\n", i, area[i]);
244
245
246
     int main() {
       while(scanf("%d",&n)!=EOF)
247
248
         solve();
249
```

```
universe
 1
 2
   Point CircumCenter(Point a, Point b, Point c) { //三角形的外心
 3
 4
     double a1 = b.x-a.x, b1 = b.y-a.y, c1 = (a1*a1 + b1*b1)/2;
 5
     double a2 = c.x-a.x,b2 = c.y-a.y,c2 = (a2*a2 + b2*b2)/2;
 6
     double d = a1*b2 - a2*b1;
 7
     cp.x = a.x + (c1*b2-c2*b1)/d;
 8
     cp.y = a.y + (a1*c2-a2*c1)/d;
 9
      return cp;
10 | }
   3.1.3 Convex hull
   /* 2D Convex Hull, by Abreto <m@abreto.net>. */
   #include "2d_base.hh"
 3
   #include <cmath>
 4
   #include <algorithm>
 6
   using namespace std;
 7
 8
   point 0;
 9
10
   bool comp_angle(point_t a, point_t b) {
11
     double t = (a-0).X(b-0);
12
     if(fe(t,0.0)) return fl((b-0).mag2(),(a-0).mag2());
13
      else return fl(0.0,t);
14
15
16
   void convex_hull_graham(vp& convex, vp src) {
17
      int i = 0, top = 0;
18
     0 = src[0];
     for(auto pt : src)
19
        if( pt.x < 0.x | | (pt.x == 0.x \&\& pt.y < 0.y))
20
21
          0 = pt;
22
     sort(src.begin(), src.end(), comp_angle);
23
     convex.push_back(src[0]);
24
     convex.push_back(src[1]);
25
     top = 1;
26
     for(i = 2; i < src.size(); ++i) {
        while(top>1 && fle((convex[top]-convex[top-1]).X(src[i]-convex[top]),0.0)) {
27
28
          convex.pop_back();
29
          --top;
30
31
        convex.push_back(src[i]);
32
        ++top;
33
     }
34
   3.1.4 Intersect Area
   |#include <cstdio>
 2
   #include <cmath>
 3
   #include <algorithm>
 4
 5
   using namespace std;
 6
 7
   //#define inf 1000000000000
 8
   #define M 8
   #define LL long long
 9
10 |#define eps 1e-12
```

```
11
   |#define PI acos(-1.0)|
12
   using namespace std;
13
   struct node {
14
     double x,y;
15
     node() {}
16
     node(double xx,double yy) {
17
       X=XX;
18
       y=yy;
19
     }
20
     node operator -(node s) {
21
       return node(x-s.x,y-s.y);
22
23
     node operator +(node s) {
24
       return node(x+s.x,y+s.y);
25
26
     double operator *(node s) {
27
       return x*s.x+y*s.y;
28
29
     double operator ^(node s) {
30
        return x*s.y-y*s.x;
31
32
   };
33
   double max(double a, double b) {
34
     return a>b?a:b;
35
36
   double min(double a,double b) {
37
     return a<b?a:b;
38
39
   double len(node a) {
40
     return sqrt(a*a);
41
42
   double dis(node a, node b) { //两点之间的距离
43
     return len(b-a);
44
45
   double cross(node a,node b,node c) { //叉乘
46
      return (b-a)^(c-a);
47
48
   double dot(node a, node b, node c) { //点成
49
      return (b-a)*(c-a);
50
51
   int judge(node a, node b, node c) { //判断c是否在ab线段上(前提是c在直线ab上)
52
     if(c.x > = min(a.x, b.x)
53
         \&c.x \le max(a.x,b.x)
54
         \&c.y = min(a.y,b.y)
55
         \&c.y \le max(a.y,b.y)
56
       return 1;
57
     return 0;
58
59
   double area(node b, node c, double r) {
60
     node a(0.0,0.0);
61
     if(dis(b,c)<eps)
62
        return 0.0;
     double h=fabs(cross(a,b,c))/dis(b,c);
63
64
     if(dis(a,b)>r-eps&&dis(a,c)>r-eps) { //两个端点都在圆的外面则分为两种情况
65
        double angle=acos(dot(a,b,c)/dis(a,b)/dis(a,c));
66
       if(h>r-eps) {
67
          return 0.5*r*r*angle;
68
       } else if(dot(b,a,c)>0&&dot(c,a,b)>0) {
69
          double angle1=2*acos(h/r);
70
          return 0.5*r*r*fabs(angle-angle1)+0.5*r*r*sin(angle1);
71
       } else {
72
          return 0.5*r*r*angle;
73
74
     } else if(dis(a,b)<r+eps&dis(a,c)<r+eps) { //两个端点都在圆内的情况</p>
```

```
return 0.5*fabs(cross(a,b,c));
 75
 76
      } else { //一个端点在圆上一个端点在圆内的情况
 77
        if(dis(a,b)>dis(a,c)) { //默认b在圆内
 78
           swap(b,c);
 79
 80
        if(fabs(dis(a,b))<eps) { //ab距离为0直接返回0
 81
           return 0.0;
 82
 83
        if(dot(b,a,c)<eps) {
 84
           double angle1=acos(h/dis(a,b));
 85
           double angle2=acos(h/r)-angle1;
 86
           double angle3=acos(h/dis(a,c))-acos(h/r);
           return 0.5*dis(a,b)*r*sin(angle2)+0.5*r*r*angle3;
 87
 88
 89
        } else {
 90
          double angle1=acos(h/dis(a,b));
 91
          double angle2=acos(h/r);
 92
          double angle3=acos(h/dis(a,c))-angle2;
 93
           return 0.5*r*dis(a,b)*sin(angle1+angle2)+0.5*r*r*angle3;
 94
        }
 95
      }
 96
 97
 98
    node A, B, C;
 99
    int R;
100
101
    bool compar(node &p1, node &p2) {
102
      return (p1^p2)>eps;
103
104
105
    double f(double x, double y) {
106
      node 0(x,y);
107
      node p[8];
108
      p[0] = A-0;
109
      p[1] = B-0;
110
      p[2] = C-0;
111
      sort(p, p+3, compar);
112
      p[3] = p[0];
      0 = node(0,0);
113
114
      double sum=0;
      /* <!-- 求面积交部分 */
115
116
      for(int i=0; i<3; i++) { /* 按顺或逆时针顺序最后取绝对值就好 */
117
        int j=i+1;
        double s=area(p[i],p[j],(double)R);
118
119
        if(cross(0,p[i],p[j])>0)
120
           sum+=s;
121
        else
122
          sum-=s;
123
124
      if(sum < -eps) sum = -sum;
125
      /* --> */
126
      return sum;
127
128
129
    double trifind(double x, double y1, double y2) {
130
      double l = y1, r = y2;
131
      while(r-l>eps) {
132
        double mid = (1+r)/2.0;
133
        double mmid = (mid+r)/2.0;
134
        if( f(x,mmid) > f(x,mid) + eps )
135
          l = mid;
136
        else
137
           r = mmid;
138
      }
```

```
139
      return f(x,l);
140
    }
141
142
    double findmin(double x1, double x2, double y1, double y2) {
143
      double l = x1, r = x2;
144
      while(r-l>eps) {
145
         double mid = (1+r)/2.0;
         double mmid = (mid+r)/2.0;
146
147
         if( trifind(mmid,y1,y2) > trifind(mid,y1,y2)+eps )
148
           l = mid;
149
         else
150
           r = mmid;
151
      }
      return trifind(l,y1,y2);
152
153
154
155
    double ans(int a, int b, int c, int r) {
156
      A = node(0,0);
157
      B = node((double)c, 0);
158
      R = r;
159
      double da = a, db = b, dc = c;
160
      double cosa = (db*db+dc*dc-da*da)/(2.0*db*dc);
161
      double alpha = acos(cosa);
162
      C = node(db*cosa, db*sin(alpha));
163
       return findmin(0.0, c, 0.0, db*sin(alpha));
164
165
166
    int main(void) {
167
       int a = 0, b = 0, c = 0, r = 0;
      while(EOF != scanf("%d%d%d%d",&a,&b,&c,&r) && (allbliclir))
168
         printf(%.81f\n, ans(a,b,c,r));
169
170
       return 0;
171 |}
    3.1.5 Universe
    |#include <bits/stdc++.h>
  2
    using namespace std;
  3
  4
    struct Point {
  5
       double x, y;
  6
      Point(double x = 0, double y = 0) : x(x), y(y) {}
  7
  8
 9
    typedef Point Vector;
 10
 11
    Vector operator + (Vector A, Vector B) {
 12
       return Vector(A.x + B.x, A.y + B.y);
 13
 14
    Vector operator – (Vector A, Vector B) {
 15
      return Vector(A.x - B.x, A.y - B.y);
 16
 17
    Vector operator * (Vector A, double p) {
 18
       return Vector(A.x*p, A.x*p);
 19
 20
    Vector operator / (Vector A, double p) {
 21
       return Vector(A.x/p, A.x/p);
 22
 23
    bool operator < (const Point& a, const Point b) {</pre>
 24
 25
       return a.x < b.x | | (a.x == b.x && a.y < b.y);
 26
    }
 27
```

```
28
  |const double EPS = 1e-10;
29
30
   int dcmp(double x) {
31
     if(fabs(x) < EPS) return 0;
32
     else return x < 0 ? -1 : 1;
33
34
35
   bool operator == (const Point& a, const Point& b) {
36
     return dcmp(a.x-b.x) == 0 \&\& dcmp(a.y-b.y);
37
38
39
   //向量a的极角
40
   |double Angle(const Vector& v) {
41
     return atan2(v.y, v.x);//\share\CodeBlocks\templates\wizard\console\cpp
42
43
44
   //向量点积
45
   double Dot(Vector A, Vector B) {
46
     return A.x*B.x + A.y*B.y;
47
   }
48
49
   //向量长度\share\CodeBlocks\templates\wizard\console\cpp
50
   double Length(Vector A) {
51
     return sqrt(Dot(A, A));
52
53
54
   //向量夹角
55
   double Angle(Vector A, Vector B) {
56
     return acos(Dot(A, B) / Length(A) / Length(B));
57
58
59
   //向量叉积
   double Cross(Vector A, Vector B) {
60
61
     return A.x*B.y - A.y*B.x;
62
   }
63
64
   //三角形有向面积的二倍
65
   double Area2(Point A, Point B, Point C) {
66
     return Cross(B-A, C-A);
67
68
69
   //向量逆时针旋转rad度(弧度)
70
   Vector Rotate(Vector A, double rad) {
71
     return Vector(A.x*cos(rad)-A.y*sin(rad), A.x*sin(rad)+A.y*cos(rad));
72
73
74
   //计算向量A的单位法向量。左转90°,把长度归一。调用前确保A不是零向量。
75
   Vector Normal(Vector A) {
76
     double L = Length(A);
77
     return Vector(-A.y/L, A.x/L);
78
79
80
   81
   使用复数类实现点及向量的简单操作
82
83
   #include <complex>
84
   typedef complex<double> Point;
85
   typedef Point Vector;
86
87
   double Dot(Vector A, Vector B) { return real(conj(A)*B)}
   double Cross(Vector A, Vector B) { return imag(conj(A)*B);}
88
89
   Vector Rotate(Vector A, double rad) { return A*exp(Point(0, rad)); }
90
91
```

```
92
93
    94
   * 用直线上的一点p0和方向向量v表示一条指向。直线上的所有点P满足P = P0+t*v;
95
   * 如果知道直线上的两个点则方向向量为B-A, 所以参数方程为A+(B-A)*t;
    * 当t 无限制时, 该参数方程表示直线。
96
97
    * 当t > 0时, 该参数方程表示射线。
    * 当 0 < t < 1时, 该参数方程表示线段。
98
99
    100
101
    //直线交点,须确保两直线有唯一交点。
    Point GetLineIntersection(Point P, Vector v, Point Q, Vector w) {
102
103
     Vector u = P - Q;
104
     double t = Cross(w, u)/Cross(v, w);
105
     return P+v*t;
106
107
108
    //点到直线距离
109
    double DistanceToLine(Point P, Point A, Point B) {
110
     Vector v1 = B - A, v2 = P - A;
111
     return fabs(Cross(v1, v2) / Length(v1)); //不取绝对值, 得到的是有向距离
112
113
114
    //点到线段的距离
115
    double DistanceToSegmentS(Point P, Point A, Point B) {
116
     if(A == B) return Length(P-A);
117
     Vector v1 = B-A, v2 = P-A, v3 = P-B;
118
     if(dcmp(Dot(v1, v2)) < 0) return Length(v2);</pre>
119
     else if(dcmp(Dot(v1, v3)) > 0) return Length(v3);
     else return fabs(Cross(v1, v2)) / Length(v1);
120
121
122
123
    //点在直线上的投影
124
   Point GetLineProjection(Point P, Point A, Point B) {
125
     Vector v = B - A;
126
     return A+v*(Dot(v, P-A)/Dot(v, v));
127
128
129
    //线段相交判定,交点不在一条线段的端点
    bool SegmentProperIntersection(Point a1, Point a2, Point b1, Point b2) {
130
131
     double c1 = Cross(a2-a1, b1-a1), c2 = Cross(a2-a1, b2-a1);
132
     double c3 = Cross(b2-b1, a1-b1), c4 = Cross(b2-b1, a2-b1);
133
     return dcmp(c1)*dcmp(c2) < 0 && dcmp(c3)*dcmp(c4) < 0;
134
135
136
    //判断点是否在点段上,不包含端点
   bool OnSegment(Point P, Point a1, Point a2) {
137
138
     return dcmp(Cross(a1-P, a2-P) == 0 \& dcmp((Dot(a1-P, a2-P)) < 0));
139
    }
140
141
    //计算凸多边形面积
142
    double ConvexPolygonArea(Point *p, int n) {
143
     double area = 0;
144
     for(int i = 1; i < n-1; i++)
145
       area += Cross(p[i] - p[0], p[i+1] - p[0]);
146
     return area/2;
147
148
149
    //计算多边形的有向面积
150
    double PolygonArea(Point *p, int n) {
151
     double area = 0;
152
     for(int i = 1; i < n-1; i++)
153
       area += Cross(p[i] - p[0], p[i+1] - p[0]);
154
     return area/2;
155 |}
```

```
156
157
    158
    * Morley定理: 三角形每个内角的三等分线, 相交成的三角形是等边三角形。
159
    * 欧拉定理: 设平面图的定点数, 边数和面数分别为V,E,F。则V+F-E = 2;
160
    161
162
    struct Circle {
163
     Point c:
164
     double r;
165
166
     Circle(Point c, double r) : c(c), r(r) {}
     //通过圆心角确定圆上坐标
167
168
     Point point(double a) {
169
       return Point(c.x + cos(a)*r, c.y + sin(a)*r);
170
171
    };
172
173
    struct Line {
174
     Point p;
175
     Vector v;
176
     double ang;
177
     Line() {}
     Line(Point p, Vector v) : p(p), v(v) {}
178
179
     bool operator < (const Line& L) const {</pre>
180
        return ang < L.ang;
181
182
    };
183
184
    //直线和圆的交点,返回交点个数,结果存在sol中。
    //该代码没有清空sol。
185
    int getLineCircleIntersecion(Line L, Circle C, double& t1, double& t2, vector<Point>&
186
        sol) {
187
     double a = L.v.x, b = L.p.x - C.c.x, c = L.v.y, d = L.p.y - C.c.y;
188
     double e = a*a + c*c, f = 2*(a*b + c*d), g = b*b + d*d - C.r*C.r;
189
     double delta = f*f - 4*e*a;
190
     if(dcmp(delta) < 0) return 0; //相离
191
     if(dcmp(delta) == 0) {
                                //相切
       t1 = t2 = -f / (2*e);
192
193
        sol.push_back(C.point(t1));
194
       return 1;
195
     }
196
     //相交
197
     t1 = (-f - sqrt(delta)) / (2*e);
198
     sol.push_back(C.point(t1));
199
     t2 = (-f + sqrt(delta)) / (2*e);
200
      sol.push_back(C.point(t2));
201
      return 2;
202
    }
203
204
    //两圆相交
205
    int getCircleCircleIntersection(Circle C1, Circle C2, vector<Point>& sol) {
206
     double d = Length(C1.c - C2.c);
      if(dcmp(d) == 0) {
207
        if(dcmp(C1.r - C2.r == 0)) return -1;
                                            //两圆完全重合
208
209
                                            //同心圆,半径不一样
       return 0;
210
211
     if(dcmp(C1.r + C2.r - d) < 0) return 0;
212
     if(dcmp(fabs(C1.r - C2.r) == 0)) return -1;
213
214
     double a = Angle(C2.c - C1.c);
                                              //向量C1C2的极角
215
     double da = acos((C1.r*C1.r + d*d - C2.r*C2.r) / (2*C1.r*d));
216
     //C1C2到C1P1的角
     Point p1 = C1.point(a-da), p2 = C1.point(a+da);
217
218
     sol.push_back(p1);
```

```
219
      if(p1 == p2) return 1;
220
      sol.push_back(p2);
221
      return 2;
222
    }
223
224
    const double PI = acos(-1);
225
    //过定点做圆的切线
    //过点p做圆C的切线,返回切线个数。v[i]表示第i条切线
226
227
    int getTangents(Point p, Circle C, Vector* v) {
228
      Vector u = C.c - p;
229
      double dist = Length(u);
230
      if(dist < C.r) return 0;
231
      else if(dcmp(dist - C.r) == 0) {
232
        v[0] = Rotate(u, PI/2);
233
        return 1;
      } else {
234
235
        double ang = asin(C.r / dist);
236
        v[0] = Rotate(u, -ang);
237
        v[1] = Rotate(u, +ang);
238
        return 2;
239
      }
240
    }
241
242
    //两圆的公切线
243
    //返回切线的个数,-1表示有无数条公切线。
244
    //a[i], b[i] 表示第i条切线在圆A, 圆B上的切点
245
    int getTangents(Circle A, Circle B, Point *a, Point *b) {
246
      int cnt = 0;
247
      if(A.r < B.r) {
        swap(A, B);
248
249
        swap(a, b);
250
251
      int d2 = (A.c.x - B.c.x)*(A.c.x - B.c.x) + (A.c.y - B.c.y)*(A.c.y - B.c.y);
      int rdiff = A.r - B.r;
252
      int rsum = A.r + B.r;
253
      if(d2 < rdiff*rdiff) return 0;</pre>
254
                                      //内含
      double base = atan2(B.c.y - A.c.y, B.c.x - A.c.x);
255
256
      if(d2 == 0 && A.r == B.r) return -1; //无限多条切线
257
      if(d2 == rdiff*rdiff) {
                                      //内切一条切线
258
        a[cnt] = A.point(base);
259
        b[cnt] = B.point(base);
260
        cnt++;
261
        return 1;
262
      //有外共切线
263
      double ang = acos((A.r-B.r) / sqrt(d2));
264
265
      a[cnt] = A.point(base+ang);
266
      b[cnt] = B.point(base+ang);
267
      cnt++;
268
      a[cnt] = A.point(base-ang);
269
      b[cnt] = B.point(base-ang);
270
      cnt++;
271
      if(d2 == rsum*rsum) { //一条公切线
272
        a[cnt] = A.point(base);
273
        b[cnt] = B.point(PI+base);
274
        cnt++;
275
      } else if(d2 > rsum*rsum) {
                                  //两条公切线
276
        double ang = acos((A.r + B.r) / sqrt(d2));
277
        a[cnt] = A.point(base+ang);
278
        b[cnt] = B.point(PI+base+ang);
279
        cnt++:
        a[cnt] = A.point(base-ang);
280
281
        b[cnt] = B.point(PI+base-ang);
282
        cnt++;
```

```
283
284
      return cnt;
285
    }
286
287
    typedef vector<Point> Polygon;
288
289
    //点在多边形内的判定
290
    int isPointInPolygon(Point p, Polygon poly) {
291
      int wn = 0;
292
      int n = poly.size();
293
      for(int i = 0; i < n; i++) {
294
        if(OnSegment(p, poly[i], poly[(i+1)%n]))    return -1; //在边界上
295
        int k = dcmp(Cross(poly[(i+1)%n]-poly[i], p-poly[i]));
296
        int d1 = dcmp(poly[i].y - p.y);
        int d2 = dcmp(poly[(i+1)%n].y - p.y);
297
298
        if(k > 0 \&\& d1 \le 0 \&\& d2 > 0) wn++;
299
        if(k < 0 \&\& d2 <= 0 \&\& d1 > 0) wn++;
300
301
      if(wn != 0) return 1;
                                //内部
                                //外部
302
      return 0;
303
304
305
    //凸包
306
    个数为p,
307
    * 输入点数组p,
                            输出点数组ch。 返回凸包顶点数
308
    * 不希望凸包的边上有输入点, 把两个<= 改成 <
309
    * 高精度要求时建议用dcmp比较
310
    * 输入点不能有重复点。函数执行完以后输入点的顺序被破坏
311
    312
    int ConvexHull(Point *p, int n, Point* ch) {
                      // 先比较x坐标, 再比较y坐标
313
      sort(p, p+n);
      int m = 0;
314
315
      for(int i = 0; i < n; i++) {
316
        while(m > 1 && Cross(ch[m-1] - ch[m-2], p[i]-ch[m-2]) <= 0) m--;
317
        ch[m++] = p[i];
318
319
      int k = m;
320
      for(int i = n-2; i >= 0; i++) {
321
        while(m > k && Cross(ch[m-1] - ch[m-2], p[i]-ch[m-2]) <= 0) m--;
322
        ch[m++] = p[i];
323
324
      if(n > 1) m--;
325
      return m;
326
327
328
    //用 有 向 直 线 A->B 切 割 多 边 形 poly , 返 回 " 左 侧 " 。 如 果 退 化 , 可 能 会 返 回 一 个 单 点 或 者 线 段
329
    //复杂度0(n2);
330
    Polygon CutPolygon(Polygon poly, Point A, Point B) {
331
      Polygon newpoly;
332
      int n = poly.size();
333
      for(int i = 0; i < n; i++) {
334
        Point C = poly[i];
335
        Point D = poly[(i+1)\%n];
        if(dcmp(Cross(B-A, C-A)) >= 0) newpoly.push_back(C); if(dcmp(Cross(B-A, C-D)) != 0) {
336
337
338
          Point ip = GetLineIntersection(A, B-A, C, D-C);
339
          if(OnSegment(ip, C, D)) newpoly.push_back(ip);
340
        }
341
342
      return newpoly;
343
344
345
    //半平面交
346
```

```
347
    //点p再有向直线L的左边。(线上不算)
348
    bool Onleft(Line L, Point p) {
349
      return Cross(L.v, p-L.p) > 0;
350
    }
351
352
    //两直线交点,假定交点唯一存在
353
    Point GetIntersection(Line a, Line b) {
      Vector u = a.p - b.p;
354
355
      double t = Cross(b.v, u) / Cross(a.v, b.v);
356
      return a.p+a.v*t;
357
358
359
    int HalfplaneIntersection(Line* L, int n, Point* poly) {
360
      sort(L, L+n);
                                  //按极角排序
361
362
      int first, last;
                                  //双端队列的第一个元素和最后一个元素
363
      Point *p = new Point[n];
                                  //p[i]为q[i]和q[i+1]的交点
364
      Line *q = new Line[n];
                                  //双端队列
      q[first = last = 0] = L[0]; //队列初始化为只有一个半平面L[0]
365
366
      for(int i = 0; i < n; i++) {
        while(first < last && !Onleft(L[i], p[last-1])) last-;</pre>
367
368
        while(first < last && !Onleft(L[i], p[first])) first++;</pre>
369
        q[++last] = L[i];
370
        if(fabs(Cross(q[last].v, q[last-1].v)) < EPS) {</pre>
371
372
          if(Onleft(q[last], L[i].p)) q[last] = L[i];
373
374
        if(first < last) p[last-1] = GetIntersection(q[last-1], q[last]);
375
376
      while(first < last && !Onleft(q[first], p[last-1])) last--;</pre>
377
      //删除无用平面
378
      if(last-first <= 1) return 0;</pre>
                                      //空集
379
      p[last] = GetIntersection(q[last], q[first]);
380
381
      //从deque复制到输出中
382
      int m = 0;
383
      for(int i = first; i \le last; i++) poly[m++] = p[i];
384
      return m;
385 | }
    4
        Graph
    4.1
        \operatorname{Tree}
    4.1.1 Universe
 2
    /* find root(重心) */
 3
    void findroot(int u, int fa) {
 4
      int i;
 5
 6
      size[u] = 1;
 7
      f[u] = 0;
      for (i = last[u]; i; i = e[i][2]) {
 8
 9
        if (!vis[e[i][0]] && e[i][0] != fa) {
10
          findroot(e[i][0], u);
          size[u] += size[e[i][0]];
 11
 12
          if (f[u] < size[e[i][0]])
13
            f[u] = size[e[i][0]];
14
        }
15
      if (f[u] < ALL - size[u])
 16
```

```
17
        f[u] = ALL - size[u];
18
     if (f[u] < f[root]) root = u;
19
20
   /* --- da --- */
21
22
23
   int dep[MAXN+1];
   int ancestor[MAXN+1][MAXLGN];
24
25
   int minw[MAXN+1][MAXLGN];
26
27
   void dfs(int u, int fa) {
28
     ancestor[u][0] = fa;
29
     dep[u] = dep[fa] + 1;
30
     for(int e = u[front]; e; e = E[e].n) {
31
        int v = E[e].v, w = E[e].w;
        if(v != fa) {
32
33
          minw[v][0] = w;
34
          dfs(v, u);
35
        }
36
     }
37
38
39
   void init_system(void) {
40
     int i = 0, w = 0;
41
     int t = 0;
42
     dep[0] = -1;
43
     dfs(1,0);
44
     for(w = 1; (t=(1<< w)) < N; ++w)
45
        for(i = 1; i \le N; ++i) if(dep[i] >= t) {
            ancestor[i][w] = ancestor[ancestor[i][w-1]][w-1];
46
47
            minw[i][w] = min(minw[i][w-1], minw[ancestor[i][w-1]][w-1]);
48
49
   }
50
51
   int query(int a, int b) {
52
     if(dep[a] < dep[b]) return query(b,a);</pre>
53
     else { /* now dep[s] > dep[t] */
54
        int i = 0;
55
        int maxbit = MAXLGN-1;
56
        int ret = INF;
57
        //while((1<<maxbit) <= dep[a]) maxbit++;</pre>
58
        /* first up a to same dep with b. */
59
        for(i = maxbit; i >= 0; i--)
          if(dep[a] - (1 << i) >= dep[b]) {
60
            ret = min(ret, minw[a][i]);
61
62
            a = ancestor[a][i];
63
64
        if(a == b) return ret;
65
        for(i = maxbit; i >= 0; i--)
          if(dep[a] - (1 << i) >= 0 \& ancestor[a][i] != ancestor[b][i]) {
66
67
            ret = min(ret, min(minw[a][i], minw[b][i]));
68
            a = ancestor[a][i];
69
            b = ancestor[b][i];
70
71
        ret = min(ret, min(minw[a][0], minw[b][0]));
72
        return ret;
73
74 |}
```

#### 4.1.2 Point Divide and Conquer

Version 1

```
/* Tree::Point divide and conquer, by Abreto<m@abreto.net>. */
 2
   #include <bits/stdc++.h>
 3
 4
   using namespace std;
 5
   typedef long long int 11;
 6
 7
   #define MAXN
                     (100001)
 8
   #define MAXV
                     (MAXN+1)
9
   #define MAXE
                     (MAXN << 1)
10
   struct edge {
11
      int v;
12
      edge *n;
13
      edge(void):v(0),n(NULL) {}
14
      edge(int vv,edge *nn):v(vv),n(nn) {}
15
16
   int nE;
17
   edge E[MAXE];
   edge *front[MAXV];
18
                        /* 0 for '(', 1 for ')' */
19
   int label[MAXV];
20
   void add_edge(int u, int v) {
21
      int ne = ++nE;
22
      E[ne] = edge(v, u[front]);
23
      u[front] = \&(E[ne]);
24
25
26
   int n;
27
   ll ans;
28
29
   char del[MAXV];
30
   namespace findroot {
31
   int ALL;
32
   int nfind;
   int vis[MAXV]
33
34
   int size[MAXV];
35
   int f[MAXV];
36
   int root;
37
    void __find(int u, int fa) {
38
      vis[u] = nfind;
39
      size[u] = 1;
40
      f[u] = 0;
      for(edge *e=u[front]; e; e = e->n) {
41
42
        int v = e \rightarrow v;
43
        if((!del[v]) && (vis[v] != nfind) && (v != fa)) {
44
          __find(v, u);
45
          size[u] += size[v];
46
          if(f[u] < size[v]) f[u] = size[v];
47
        }
48
49
      if(f[u] < ALL - size[u]) f[u] = ALL - size[u];
50
      if(f[u] < f[root]) root = u;
51
    int find(int u, int all) {
52
53
      ++nfind;
54
      ALL = all:
55
      f[root = 0] = MAXV;
56
      __find(u,0);
57
      return root;
58
59
60
   namespace workspaces {
61
62
   int maxdep;
   int dep[MAXV];
63
64 | Il cntin[MAXV], cntout[MAXV];
```

```
65
                          /* 0 for '(', 1 for ')' */
    int in[2][MAXV];
    int out[2][MAXV];
 66
 67
    void getdeep(int u, int fa) {
 68
       dep[u] = dep[fa] + 1;
 69
       if(dep[u] > maxdep) maxdep = dep[u];
 70
       for(edge *e = u[front]; e; e = e \rightarrow n)
 71
         if((!del[e->v]) \& (fa != e->v))
 72
           getdeep(e->v, u);
 73
    void dfs(int u, int fa) {
 74
 75
 76
         /* out from root */
 77
         out[0][u] = out[0][fa];
 78
         out[1][u] = out[1][fa];
 79
         if(0 == label[u]) { /* meet '(' */
 80
           out[0][u]++;
                     /* meet ')' */
 81
         } else {
 82
           if(out[0][u]) out[0][u]--;
 83
           else out[1][u]++;
 84
 85
         if(out[0][u] == 0)
 86
           cntout[out[1][u]]++;
 87
 88
 89
         /* in to root */
 90
         in[0][u] = in[0][fa];
 91
         in[1][u] = in[1][fa];
 92
         if(0 == label[u]) { /* meet '(' */
 93
           if(in[1][u]) in[1][u]--;
 94
           else in[0][u]++;
 95
                    /* meet ')' */
         } else {
 96
           in[1][u]++;
 97
 98
         if(0 == in[1][u])
 99
           cntin[in[0][u]]++;
100
101
       /* do something */
102
       for(edge *e = u[front]; e; e = e \rightarrow n) {
103
         int v = e \rightarrow v;
104
         if((!del[v]) \&\& (v != fa)) {
105
           dfs(v, u);
106
107
       }
108
109
     inline void init_maxdep(void) {
110
       maxdep = 0;
111
112
    inline void update_maxdep(int u) {
113
       dep[u] = 1;
114
       if(dep[u] > maxdep) maxdep = dep[u];
       for(edge *e = u[front]; e; e = e->n)
115
116
         if((!del[e->v]))
117
           getdeep(e->v, u);
118
119
     inline void clear(void) {
120
       for(int i = 0; i \le maxdep+1; ++i)
121
         cntin[i] = cntout[i] = 0;
122
123
    inline void work(int u) {
124
       in[0][u] = in[1][u] = out[0][u] = out[1][u] = 0;
125
       in[label[u]][u] = out[label[u]][u] = 1;
126
       if(out[0][u] == 0) cntout[out[1][u]]++;
127
       if(0 == in[1][u]) cntin[in[0][u]]++;
128
       /* update in and out if neccessary */
```

```
129
       for(edge *e = u[front]; e; e = e \rightarrow n)
130
         if(!(del[e->v]))
131
           dfs(e\rightarrow v, u);
132
133
     };
134
135
     11 count(int u, int p) {
136
       ll ret = 0;
137
       workspace::init_maxdep();
138
       workspace::update_maxdep(u);
139
       workspace::clear();
140
       if(-1 == p)  {
141
         for(edge *e = u[front]; e; e = e->n)
142
           if((!(del[e->v])))
143
             workspace::work(e->v);
144
         p = label[u];
145
         /* single end */
146
         if(0 == p) ret = workspace::cntout[1];
147
         else ret = workspace::cntin[1];
148
       } else {
149
         workspace::work(u);
150
151
       if(0 == p) { /* p is '(' */
152
         for(int i = 0; i < workspace::maxdep; ++i) /* concatenation */</pre>
153
           ret += workspace::cntin[i] * workspace::cntout[i+1];
154
       } else {
                  /* p is ')' */
155
         for(int i = 0; i < workspace::maxdep; ++i) /* concatenation */
156
           ret += workspace::cntin[i+1] * workspace::cntout[i];
157
158
       return ret;
159
160
161
     void handle(int u) {
162
       del[u] = 1; /* delete current root. */
163
       ans += count(u, -1);
       /* do something */
164
165
       for(edge *e = u[front]; e; e = e \rightarrow n) {
166
         int v = e \rightarrow v;
167
         if(!del[v]) {
           ans -= count(v, label[u]);
168
169
           /* do something */
170
           int r = findroot::find(v, findroot::size[v]);
171
           handle(r);
172
         }
173
       }
174
175
     void proc(void) {
176
177
       int r = findroot::find(1,n);
178
       handle(r);
179
     }
180
181
     char ls[MAXV+1];
182
     int main(void) {
       int i = 0;
183
       scanf("%d", &n);
184
185
       scanf("%s", ls);
186
       for(i = 0; i < n; ++i)
187
         label[i+1] = ls[i] - '(';
188
       for(i = 1; i < n; ++i) {
189
         int ai, bi;
         scanf("%d<sub>\u00e4</sub>%d", &ai, &bi);
190
191
         add_edge(ai, bi);
192
         add_edge(bi, ai);
```

```
193
       }
194
       proc();
195
       printf("%lld\n", ans);
196
       return 0;
197 |}
     Version 2
    //* 2016 ACM/ICPC Asia Regional Dalian. Problem , by Abreto<m@abreto.net>. */
  2
    #include <bits/stdc++.h>
  3
  4
    using namespace std;
  5
    typedef long long int 11;
  6
  7
     /* offset in [1,k] */
  8
    #define GET(i,offset)
                              (((i)>>((offset)-1))&1)
  9
    #define SET(i,offset)
                              ((i)|(1<<((offset)-1)))
 10
    #define REV(i,offset)
                              ((i)^{(1<<((offset)-1))})
 11
    #define MAXN
 12
                      (50005)
 13
    #define MAXV
                      (MAXN+1)
 14
    #define MAXE
                      (MAXN << 1)
 15
    struct edge {
       int v;
 16
 17
       edge *n;
 18
       edge(void):v(0),n(NULL) {}
 19
       edge(int vv,edge *nn):v(vv),n(nn) {}
 20
    |};
 21
    int nE;
    edge E[MAXE];
 22
 23
    edge *front[MAXV];
    int label[MAXV];
 24
                          /* each kind */
 25
    void add_edge(int u, int v) {
 26
       int ne = ++nE;
 27
       E[ne] = edge(v, u[front]);
 28
       u[front] = \&(E[ne]);
 29
 30
 31
    int n, k;
 32
     ll ans;
 33
    int all_kind;
 34
 35
    int ndel;
 36
    int del[MAXV];
 37
    namespace findroot {
 38
    int ALL;
 39
    ll nfind;
 40
    ll vis[MAXV];
 41
    int size[MAXV];
 42
    int f[MAXV];
 43
    int root:
     void __find(int u, int fa) {
 44
 45
       vis[u] = nfind;
       size[u] = 1;
 46
 47
       f[u] = 0;
 48
       for(edge *e=u[front]; e; e = e->n) {
 49
         int v = e \rightarrow v;
 50
         if((del[v] != ndel) && (vis[v] != nfind) && (v != fa)) {
 51
            _find(v, u);
 52
           size[u] += size[v];
 53
           if(f[u] < size[v]) f[u] = size[v];
         }
 54
 55
 56
       if(f[u] < ALL - size[u]) f[u] = ALL - size[u];
 57
       if(f[u] < f[root]) root = u;
```

```
58
 59
     int find(int u, int all) {
 60
       ++nfind;
 61
       ALL = all;
 62
       f[root = 0] = MAXV;
 63
       __find(u,0);
 64
       return root;
 65
 66
 67
 68
     namespace workspace {
 69
     ll cnt[1024];
 70
     int dp[MAXV];
     void dfs(int u, int fa) {
 71
 72
       dp[u] = dp[fa] \mid label[u];
       cnt[dp[u]] ++;
 73
 74
       /* dig into children */
 75
       for(edge *e = u[front]; e; e = e \rightarrow n) {
 76
         int v = e \rightarrow v;
 77
         if((del[v] != ndel) && (v != fa)) {
 78
            dfs(v, u);
 79
 80
 81
 82
     inline void clear(void) {
 83
       for(int i = 1; i \leftarrow all_kind; ++i)
 84
         cnt[i] = 0;
 85
 86
     inline void work(int u) {
 87
       dp[u] = label[u];
       cnt[dp[u]] ++;
 88
 89
       for(edge *e = u[front]; e; e = e->n)
 90
         if((del[e\rightarrow v] != ndel))
 91
            dfs(e\rightarrow v, u);
 92
 93
     inline void show(void) {
 94
       for(int i = 0; i <= all_kind; ++i)</pre>
         printf("cnt[%d]_{\square}=_{\square}%lld\n", i, cnt[i]);
 95
 96
       for(int i = 1; i <= n; ++i)
 97
         printf("dp[%d]_{\square}=_{\square}%d\n", i, dp[i]);
 98
 99
     };
100
101
102
     11 count(int u, int p) {
103
       ll ret = 0;
       workspace::clear();
104
       //printf("%d,%d :\n", u, p);
105
106
       if(-1 == p) {
         for(edge *e = u[front]; e; e = e->n)
107
            if(((del[e->v]) != ndel))
108
109
              workspace::work(e->v);
110
         p = label[u];
111
         /* single end */
112
         for(int i = 1; i <= all_kind; i++)
113
            if(all\_kind == (i|p))
114
              ret += (workspace::cnt[i]<<1);
115
       } else {
116
         workspace::work(u);
117
       //workspace::show();
118
119
       for(int i = 1; i \leftarrow all_kind; ++i)
120
         if( workspace::cnt[i] > 0 )
121
            for(int j = 1; j \le all_kind; ++j)
```

```
122
             if(all\_kind == (i|p|j))
123
                ret += workspace::cnt[i] * workspace::cnt[j];
124
       //printf("%lld\n", ret);
125
       return ret;
126
127
128
     void handle(int u) {
129
       //printf("proccessing %d\n", u);
130
       del[u] = ndel; /* delete current root. */
       ans += count(u, -1);
131
132
       /* do something */
133
       for(edge *e = u[front]; e; e = e \rightarrow n) {
134
         int v = e \rightarrow v;
135
         if(del[v] != ndel) {
136
           ans -= count(v, label[u]);
137
           /* do something */
138
           int r = findroot::find(v, findroot::size[v]);
139
           handle(r);
140
         }
141
       }
142
143
144
     void proc(void) {
145
       int r = findroot::find(1,n);
146
       handle(r);
147
148
149
     void clear(void) {
       int i;
150
       ans = 0;
151
152
       nE = 0;
       for(i = 0; i \le n; ++i) {
153
154
         front[i] = NULL;
155
       //findroot::nfind = 0;
156
157
       ndel++;
158
159
160
     void mozhu(void) {
161
       int i = 0;
162
       int li;
163
       for(i = 1; i \le n; ++i) {
164
         scanf("%d", &li);
         label[i] = 1 << (li-1);
165
166
       for(i = 1; i < n; ++i) {
167
168
         int ai, bi;
         scanf("%d<sub>\\\\</sub>%d", &ai, &bi);
169
170
         add_edge(ai, bi);
171
         add_edge(bi, ai);
172
173
       all_kind = (1 << k)-1;
174
       proc();
175
       if(1 == k) ans += n;
176
       printf("%lld\n", ans);
177
178
179
     int main(void) {
180
       while( EOF != scanf("%d%d", &n, &k) ) {
181
         clear();
182
         mozhu();
183
184
       return 0;
185 | }
```

### 4.1.3 Hevay chain decompostion

```
/* bzoj 1036 */
    /* 树链剖分 */
 3
    #include <bits/stdc++.h>
 5
    using namespace std;
 6
 7
    #define MAXN
                     30030
 8
    #define MAXM
                     (MAXN << 1)
 9
    struct edge {
10
      int v;
11
      edge *n;
      edge(void) {}
12
13
      edge(int vv, edge *nn):v(vv),n(nn) {}
14
15
   typedef edge *ep;
   int nE;
16
    edge E[MAXM];
17
    ep front[MAXN];
18
19
    void add_edge(int u, int v) {
20
      int ne = ++nE;
21
      E[ne] = edge(v, u[front]);
22
      u[front] = \&(E[ne]);
23
24
25
26
    int fa[MAXN], son[MAXN], sz[MAXN], dep[MAXN];
    int top[MAXN];
27
28
    int id[MAXN];
29
    int tot;
30
31
    void calc(int u, int uf) {
32
      dep[u] = dep[uf] + 1;
33
      fa[u] = uf;
34
      sz[u] = 1;
35
      son[u] = -1;
      for (ep \ e = u[front]; \ e; \ e = e \rightarrow n)  {
36
        if(e->v != uf) {
37
38
          calc(e->v, u);
39
          sz[u] += sz[e->v];
          if( -1 == son[u] \mid | sz[son[u]] < sz[e \rightarrow v] )
40
41
             son[u] = e \rightarrow v;
42
        }
43
      }
44
45
    void link(int u, int f) {
46
      id[u] = (++tot);
47
      top[u] = f;
48
      if(son[u] > 0) {
49
        link(son[u], f);
50
51
      for(ep e = u[front]; e; e = e \rightarrow n) {
52
        if(e->v != fa[u] \&\& e->v != son[u]) {
53
          link(e->v, e->v);
54
55
      }
56
57
    /* 其实是树链剖分 */
58
59
    void make_link_cut_tree(void) {
      calc(1, 0);
60
61
      link(1, 1);
62 |}
```

```
63
 64
    int w[MAXN];
 65
    int sum[MAXN<<2], mx[MAXN<<2];</pre>
 66
 67
     void maintain(int o, int l, int r) {
 68
       sum[o] = sum[o << 1] + sum[o << 1|1];
 69
       mx[o] = max(mx[o << 1], mx[o << 1|1]);
 70
 71
    void build(int o = 1, int l = 1, int r = n) {
 72
       if(r == 1) {
 73
         sum[o] = w[l];
 74
         mx[o] = w[l];
 75
       } else {
         int mid = 1+r>>1;
 76
         build(o<<1, l, mid);</pre>
 77
 78
         build(o<<1|1, mid+1, r);
 79
         maintain(o, l, r);
 80
       }
 81
 82
     void update(int p, int x, int o = 1, int l = 1, int r = n) {
 83
       if(p \ll 1 \& r \ll p) {
 84
         sum[o] = x;
 85
         mx[o] = x;
 86
       } else {
 87
         int mid = 1+r>>1;
 88
         if(p \le mid) update(p,x,o \le 1,1,mid);
 89
         else update(p,x,o <<1|1,mid+1,r);
 90
         maintain(o,l,r);
 91
       }
 92
     int qs(int L, int R, int o = 1, int l = 1, int r = n) {
 93
 94
       if(R < l | l | r < L) return 0;
 95
       else if (L \le 1 \& r \le R) \{
 96
         return sum[o];
 97
       } else {
 98
         int mid = 1+r>>1;
 99
         return qs(L,R,o<<1,l,mid)+qs(L,R,o<<1|1,mid+1,r);
100
101
102
     int qm(int L, int R, int o = 1, int l = 1, int r = n) {
103
       if(L <= 1 && r <= R) {
104
         return mx[o];
105
       } else {
106
         int mid = 1+r>>1;
107
         if(R \le mid) return qm(L, R, o<<1, l, mid);
108
         else if (L > mid) return qm(L, R, o<<1|1, mid+1, r);
109
         else return max(qm(L, R, o << 1, l, mid), qm(L, R, o << 1|1, mid+1, r));
110
       }
111
112
     void change(int u, int t) {
113
114
       update(id[u], t);
115
116
     int qmax(int u, int v) {
117
       int ret = -10000000000;
118
       while(top[u] != top[v]) {
119
         if( dep[top[u]] > dep[top[v]] ) {
120
           /* jump u */
121
           ret = max(ret, qm(id[top[u]], id[u]));
122
           u = fa[top[u]];
123
         } else {
124
           ret = max(ret, qm(id[top[v]], id[v]));
125
           v = fa[top[v]];
         }
126
```

```
127
128
       ret = max(ret, qm(min(id[u],id[v]),max(id[u],id[v])));
129
       return ret;
130
131
    int qsum(int u, int v) {
132
       int ret = 0;
133
       while(top[u] != top[v]) {
134
         if( dep[top[u]] > dep[top[v]] ) {
           /* jump u */
135
136
           ret += qs(id[top[u]], id[u]);
137
           u = fa[top[u]];
138
         } else {
139
           ret += qs(id[top[v]], id[v]);
140
           v = fa[top[v]];
141
         }
142
143
       ret += qs(min(id[u],id[v]),max(id[u],id[v]));
144
       return ret;
145
146
147
     int main(void) {
148
       int i;
       scanf("%d", &n);
149
       for(i = 1; i < n; ++i) {
150
         int a, b;
151
152
         scanf("%d%d", &a, &b);
153
         add_edge(a, b);
154
         add_edge(b, a);
155
156
       make_link_cut_tree();
       for(i = 1; i \le n; ++i) {
157
         scanf("%d", &(w[id[i]]));
158
159
       build();
160
       scanf("%d", &i);
161
162
       while(i--) {
163
         char command[8];
164
         int a, b;
               "%s⊔%d⊔%d", command, &a, &b);
165
         if('C' == command[0]) change(a, b);
166
         else if ('M' == command[1]) printf("%d\n", qmax(a, b));
167
168
         else if ('S' == command[1]) printf("%d\n", qsum(a, b));
169
170
       return 0;
171
     4.2 2-SAT
    |#include <bits/stdc++.h>
  3
    using namespace std;
  4
  5
    namespace two_sat {
     const int maxn = 100000;
  6
  7
     const int maxm = 1000000;
  8
    struct edge {
  9
       int v;
 10
       edge *n;
       edge(void):v(0),n(NULL) {}
 11
 12
       edge(int vv, edge *nn):v(vv),n(nn) {}
 13
    };
 14
    typedef edge *ep;
 15 | int n;
```

```
16
   int nE;
17
   edge E[maxm];
18
   ep front[maxn];
19
   void add_edge(int u, int v) {
20
      int ne = ++nE;
21
      E[ne] = edge(v, u[front]);
22
      u[front] = \&(E[ne]);
23
24
   /* (x = xval or y = yval), indexed from 0 */
25
   void add_clause(int x, int xv, int y, int yv) {
26
      x = x*2 + xv;
27
      y = y*2 + yv;
      add_edge(x^1, y);
28
29
      add_edge(y^1, x);
30
31
32
    char mark[maxn<<1];</pre>
33
   int S[maxn << 1], c;
34
   void init(int N) {
35
      n = N;
36
      for(int i = 0; i < n*2; ++i) {
37
        i[front] = NULL;
38
        i[mark] = 0;
39
40
     nE = 0;
41
42
43
   int dfs(int x) {
44
      if(mark[x^1]) return 0;
45
      if(mark[x]) return 1;
46
      mark[x] = 1;
47
      S[c++] = x;
48
      for(ep e = x[front]; e; e = e->n)
49
        if(!dfs(e->v)) return 0;
50
      return 1;
51
52
53
    int solve(void) {
54
      for(int i = 0; i < n*2; i += 2)
55
        if(!mark[i] && !mark[i+1]) {
56
          c = 0;
57
          if(!dfs(i)) {
58
            while(c > 0) mark[S[--c]] = 0;
59
            if(!dfs(i+1)) return 0;
          }
60
61
      return 1;
62
63
64
   }
        Cut Edge and Point
   Finding cut edges
 2
    The code below works properly because the lemma above (first lemma):
 3
      h[root] = 0
 4
                par[v] = -1
 5
                          dfs (v):
 6
                          d[v] = h[v]
 7
                                 color[v] = gray
 8
                                           for u in adj[v]:
 9
                                               if color[u] == white
10
                                                 then par[u] = v and dfs(u) and d[v] = min(
                                                     d[v], d[u]
```

```
11
                                                     if d[u] > h[v]
12
                                                        then the edge v-u is a cut edge
13
                                                        else if u != par[v])
14
              then d[v] = min(d[v], h[u])
15
                           color[v] = black
16
                                       In this code, h[v] = 0 height of vertex v in the DFS
                                          tree and d[\sqrt{y}] = \min(h[w]) where there is at least
                                          vertex u in subtree of v in the DFS tree where
                                          there is an edge between u and w).
17
18
                                           Finding cut vertices
19
                                           The code below works properly because the lemma
                                               above (first lemma):
20
                                           h[root] = 0
21
                                                      par[v] = -1
22
                                                          dfs (v):
23
                                                          d[v] = h[v]
24
                                                              color[v] = gray
25
                                                        for u in adj[v]:
26
                                                                  if color[u] == white
27
                                                                    then par[u] = v and dfs(
                                                                        u) and d[v] = min(d[v])
                                                                        ], d[u])
                                                                           if d[u] >= h[v]
28
                                                                              and (v != root
                                                                              number_of_children
                                                                              (v) > 1)
29
                                                                             then the edge v
                                                                                is a cut
                                                                                vertex
                                                                             else if u != par
30
                                                                                 [v])
31
                    then d[v] = min(d[v], h[u])
32
                                 color[v] = black
33
                                             In this code, h[v] = height of vertex v in
                                                 the DFS tree and d[\sqrt{y}] = \min(h[w]) where
                                                 there is at least vertex u in subtree of v
                                                 in the DFS tree where there is an edge
                                                 between u and w).
```

### 4.4 Euler Path

```
/* Euler path, by Abreto<m@abreto.net>. */
 2
   #define MAXV
                     (1024)
 3
   #define MAXE
                     (MAXV*MAXV)
 4
 5
    typedef struct {
 6
      int id:
 7
      int nxt;
 8
      int del;
 9
    } egde_t;
   int front[MAXV];
10
11
   egde_t edg[MAXE];
   int d[MAXV];
12
13
   int ind[MAXV], outd[MAXV];
14
   int nedges;
15
   void add_edge(int u, int v) {
16
      int newedge = ++nedges;
17
      edg[newedge].id = v;
18
      edg[newedge].nxt = u[front];
19
      edg[newedge].del = 0;
20
      u[front] = newedge;
```

```
21
      outd[u]++;
22
      ind[v]++;
23
      d[u]++;
24
      d[v]++;
25
26
   void del_edge(int u, int v) {
27
      int e = 0;
28
      for(e=u[front]; e; e=edg[e].nxt)
29
        if(edg[e].id==v) {
30
          edg[e].del = 1;
31
          outd[u]--;
32
          ind[v]--;
33
          d[u]--;
34
          d[v]--;
35
          return;
36
        }
37
38
39
   int path[MAXV];
40
   int l;
41
42
   void add2path(int u) {
43
      path[l++] = u;
44
45
46
   /* Directed graph */
47
   void euler(int x) {
48
      if(outd[x]) {
49
        int e = 0;
        for(e=x[front]; e; e=edg[e].nxt)
50
51
          if(!edg[e].del) {
52
            int v = edg[e].id;
53
            del_edge(x,v);
54
            euler(v);
55
          }
56
57
      add2path(x);
58
59
60
   /* Undirected graph */
61
   void euler(int x) {
62
      if(d[x]) {
63
        int e = 0;
        for(e=x[front]; e; e=edg[e].nxt)
64
65
          if(!edg[e].del) {
66
            int v = edg[e].id;
67
            del_edge(x,v);
68
            del_edge(v,x);
69
            euler(v);
70
          }
71
72
      add2path(x);
73
    4.5 Shortest Path
   4.5.1 Dijkstra
 1 | /* Shortest Path Dijstra, by Abreto<m@abreto.net>. */
 2
   #include <cstdio>
 3
   #include <set>
 4
   #include <utility>
 5
```

```
6
   using namespace std;
 7
   typedef set< pair<int,int> > spii;
 8
 9
   #define MAXN
                     512
10
   #define MAXV
                     (MAXN*MAXN)
11
12
    struct egde_t {
13
      int id;
14
      int nxt;
15
   };
16
   int front[MAXV];
17
   egde_t edg[MAXV<<3];
18
   int nedges;
19
   void add_edge(int u, int v) {
20
      int newedge = ++nedges;
21
      edg[newedge].id = v;
22
      edg[newedge].nxt = u[front];
23
      u[front] = newedge;
24
   }
25
26
   int d[MAXV];
27
    int vis[MAXN];
28
   int solid[MAXV];
29
30
    int dijstra(int s, int t) {
31
      int v = s[front];
32
      spii q;
33
      q.insert(make_pair(0, s));
34
      while(!q.empty()) {
35
        auto it = q.begin();
36
        int u = it->second;
        int v = u[front];
37
38
        q.erase(it);
39
        solid[u] = 1;
40
        if(u == t) break;
41
        while(v) {
42
          int w = edg[v].id;
43
          if(!solid[w]) {
44
            if( (0==d[w]) | (d[u] + 1 < d[w]) ) {
45
              q.erase(make_pair(d[w],w));
46
              d[w] = d[u] + 1;
47
              q.insert(make_pair(d[w],w));
48
            }
49
50
          v = edg[v].nxt;
51
52
53
      return d[t];
54
   4.5.2 Shortest Path Fast Algorithm
 1 |/* Shortest Path Fast Algorithm, by Abreto<m@abreto.net>. */
 2
   #include <cstdio>
   #include <cstring>
 3
   #include <queue>
   #include <utility>
 6
 7
   using namespace std;
 8
 9
   #define MAXN
                     128
10
   struct edge {
11
```

```
12
      int v;
13
      int w;
14
      int n;
15
16
   edge edg[MAXN<<1];</pre>
17
   int nedg;
18
   int indegree[MAXN];
    int front[MAXN];
19
20
   int find_edge(int u, int v) {
21
      int e = u[front];
22
      while(e) {
23
        if(edg[e].v == v) return e;
24
        e = edg[e].n;
25
26
      return 0;
27
28
   void add_edge(int u, int v, int w) {
29
      int e = find_edge(u,v);
30
      if(0==e) {
31
        int newnode = ++nedg;
32
        edg[newnode].v = v;
33
        edg[newnode].w = w;
34
        edg[newnode].n = u[front];
35
        u[front] = newnode;
36
        indegree[v]++;
37
      } else {
38
        edg[e].w = (w < edg[e].w)?w:(edg[e].w);
39
40
41
42
   int n;
43
44
   char inq[MAXN];
45
   int vis[MAXN];
46
   int d[MAXN];
47
    int spfa(int s) { /* return 1 if fuhuan exists. */
48
      queue<int> q;
     memset(inq, 0, sizeof(inq));
49
50
      memset(d, -1, sizeof(d));
51
      memset(vis, 0, sizeof(vis));
52
      d[s] = 0;
53
      inq[s] = 1;
54
      q.push(s);
55
      while(!q.empty()) {
56
        int u = q.front();
57
        q.pop();
        printf("proc<sub>\\\</sub>d..\n", u);
58
59
        inq[u] = 0;
60
        if(vis[u]++ > n)
61
          return 1;
62
        for(int e = front[u]; e; e = edg[e].n) {
63
          int v = edg[e].v, w = edg[e].w;
          if( -1 == d[v] || d[u] + w < d[v]) {
64
            d[v] = d[u] + w;
65
66
            if(!inq[v]) {
67
              inq[v] = 1;
68
              q.push(v);
69
            }
70
          }
71
        }
72
73
      return 0;
74
```

#### 4.5.3 *K*-th shortest path

```
1
   /**
 2
    * poj
 3
     * Problem#2449
 4
    * Accepted
 5
    * Time: 250ms
 6
    * Memory: 9252k
 7
    */
 8
   #include <iostream>
 9
   #include <fstream>
10
   |#include <sstream>
   |#include <algorithm>
11
12
   #include <cstdio>
   #include <cstdlib>
13
14
   #include <cstring>
15
   #include <ctime>
   #include <cctype>
16
17
   #include <cmath>
   |#include <vector>
18
19
   #include <queue>
20
   #include <stack>
21
   #include <map>
22
   #include <set>
23
   #include <bitset>
24
   using namespace std;
25
   typedef bool boolean;
26
27
   typedef class Edge {
28
   public:
29
      int end;
30
     int next;
31
     int w;
32
33
      Edge(int end = 0, int next = -1, int w = 0):end(end), next(next), w(w) {
                                                                                          }
34
   } Edge;
35
36
   const int N = 1e3, M = 1e5;
37
38
   typedef class MapManager {
39
   public:
40
      int cnt;
41
      int h[N + 5];
42
     Edge edge[M + 5];
43
     MapManager() {
44
45
     MapManager(int n):cnt(-1) {
46
   //
                  h = new int[(n + 1)];
47
   //
                  edge = new Edge[(m + 1)];
48
        memset(h, -1, sizeof(int) * (n + 1));
49
50
51
     inline void addEdge(int u, int v, int w) {
52
        edge[++cnt] = (Edge(v, h[u], w));
53
                  h[u] = (signed)edge.size() - 1;
54
        h[u] = cnt;
55
     }
56
57
     inline int start(int node) {
58
        return h[node];
59
     }
60
61
     Edge& operator [] (int pos) {
62
        return edge[pos];
```

```
63
 64
    } MapManager;
    #define m_endpos -1
 65
 66
 67
    int n, m;
 68
    MapManager q;
 69
    MapManager rg;
    int s, t, k;
 70
 71
    int ds[N + 5];
 72
 73
    inline void init() {
 74
       scanf("%d%d", &n, &m);
 75
       memset(g.h, -1, sizeof(int) * (n + 1));
 76
       memset(rg.h, -1, sizeof(int) * (n + 1));
 77
       for(int i = 1, u, v, w; i \le m; i++) {
         scanf("%d%d%d", &u, &v, &w);
 78
 79
         g.addEdge(u, v, w);
 80
         rg.addEdge(v, u, w);
 81
       }
 82
       scanf("%d%d%d", &s, &t, &k);
 83
           ds = new int[(n + 1)];
 84
    }
 85
    #define g rg
 86
 87
    #define f ds
 88
    #define que que1
 89
    boolean vis[N + 5];
 90
    queue<int> que;
 91
    boolean spfa(int s, int t) {
 92
       memset(f, 0x7f, sizeof(int) * (n + 1));
 93
       memset(vis, false, sizeof(boolean) * (n + 1));
 94
       que.push(s);
 95
       f[s] = 0;
 96
       while(!que.empty()) {
 97
         int e = que.front();
 98
         que.pop();
 99
         vis[e] = false;
100
         for(int i = g.start(e); i != m_endpos; i = g[i].next) {
           int& eu = g[i].end;
101
                   cout << e << " " << eu << " " << i <<endl;
102
     //
103
           if(f[e] + g[i].w < f[eu]) {
104
             f[eu] = f[e] + g[i].w;
105
             if(!vis[eu]) {
106
               que.push(eu);
107
               vis[eu] = true;
108
             }
109
           }
         }
110
111
       return (f[t] != 0x7f7f7f7f);
112
113
114
    #undef g
115
    #undef f
    #undef que
116
117
118
     typedef class Status {
119
    public:
120
       int node;
121
       int dis;
122
       int priority;
123
124
       Status(int node = 0, int dis = 0):node(node), dis(dis), priority(h()) {
                                                                                          }
125
126
       int h() {
```

```
127
         return dis + ds[node];
128
       }
129
130
       boolean operator < (Status b) const {
131
         return priority > b.priority;
132
133
     } Status;
134
135
     int label[N + 5];
    priority_queue<Status> que;
136
137
     int bfs(int s, int t) {
138
       if(s == t)
                     k++;
           label = new int[(n + 1)];
139
140
       memset(label, 0, sizeof(int) * (n + 1));
       que.push(Status(s, 0));
141
142
       while(!que.empty()) {
143
         Status e = que.top();
144
         que.pop();
145
         label[e.node]++;
146
         if(e.node == t && label[e.node] == k)
147
           return e.dis;
148
         for(int i = g.start(e.node); i != m_endpos; i = g[i].next) {
149
           if(label[q[i].end] < k)
             que.push(Status(g[i].end, e.dis + g[i].w));
150
151
         }
152
153
       return -1;
154
155
156
    inline void solve() {
157
       if(!spfa(t, s)) {
158
         puts("-1");
159
         return;
160
       printf("%d", bfs(s, t));
161
162
163
164
    int main() {
       init();
165
166
       solve();
167
       return 0;
168
    |}
     4.6 Maxflow
    /* Max Flow Problem, by Abreto<m@abreto.net> */
  1
  2
  3
    #include <bits/stdc++.h>
    using namespace std;
  5
    #define MAXV
  6
                     (100000)
  7
    #define MAXE
                     (1000000)
  8
    struct edge {
  9
       static int N;
 10
       int v, w;
 11
       edge *n;
 12
       edge(void):v(0),w(0),n(NULL) {}
 13
       edge(int vv, int ww, edge *nn):v(vv),w(ww),n(nn) {}
 14
 15
    int nE;
 16
    edge E[MAXE];
 17
    edge *front[MAXV];
 18 | void add_edge(int u, int v, int w) {
```

```
19
     int ne = ++nE;
20
     E[ne] = edge(v, w, u[front]);
21
     u[front] = \&(E[ne]);
22
23
   edge *find_edge(int u, int v) {
24
      for(edge *e = u[front]; e != NULL; e = e->n)
25
        if(e\rightarrow v == v)
26
          return e:
27
      return NULL;
28
29
   void grant_e(int u, int v, int w) {
30
     edge *e = find_edge(u, v);
31
     if(NULL == e) add_edge(u,v,w);
32
     else e\rightarrow w += w;
33
34
35
   int vis[MAXV]
36
   int path[MAXV];
37
   int dfs(int u, int t) {
38
     vis[u] = 1;
39
     if(u == t) return 1;
40
     for(edge *e = u[front]; e != NULL; e = e->n) {
41
        int v = e \rightarrow v;
       if(!vis[v] \&\& e->w \&\& dfs(v,t)) {
42
43
          path[u] = v;
44
          return 1;
45
       }
46
     }
47
     return 0;
48
49
   int find_path(int s, int t) {
50
     memset(vis, 0, sizeof(vis));
51
     return dfs(s,t);
52
53
   int max_flow(int s, int t) {
54
     int flow = 0;
55
     while(find_path(s,t)) {
56
        int i = 0;
57
        int minf = find_edge(s,path[s])->w;
58
        for(i = path[s]; i != t; i = path[i])
59
          minf = min(minf, find_edge(i,path[i])->w);
60
        for(i = s; i != t; i = path[i]) {
61
          grant_e(i, path[i], -minf);
          grant_e(path[i], i, minf);
62
63
64
       flow += minf;
65
66
     return flow;
67
68
69
   /* Dinic */
70
   #define N 1000
71
   #define INF 100000000
72
73
   struct Edge {
     int from, to, cap, flow;
74
75
     Edge(int u,int v,int c,int f):from(u),to(v),cap(c),flow(f) {}
76
   };
77
78
   struct Dinic {
79
     int n,m,s,t;//结点数, 边数 (包括反向弧), 源点编号, 汇点编号
80
     vector<Edge>edges;//边表, dges[e]和dges[e^1]互为反向弧
81
     vector<int>G[N];//邻接表,G[i][j]表示结点i的第j条边在e数组中的编号
82
     bool vis[N]; //BFS的使用
```

```
83
      int d[N]; //从起点到i的距离
84
      int cur[N]; //当前弧下标
85
86
      void addedge(int from,int to,int cap) {
87
        edges.push_back(Edge(from, to, cap, 0));
88
        edges.push_back(Edge(to,from,0,0));
89
        int m=edges.size();
90
        G[from].push_back(m-2);
91
        G[to].push_back(m-1);
92
93
94
      bool bfs() {
95
        memset(vis,0,sizeof(vis));
96
        queue<int>Q;
97
        Q.push(s);
98
        d[s]=0;
99
        vis[s]=1;
100
        while(!Q.empty()) {
101
          int x=Q.front();
          Q.pop();
102
103
          for(int i=0; i<G[x].size(); i++) {</pre>
104
            Edge&e=edges[G[x][i]];
105
            if(!vis[e.to]&&e.cap>e.flow) { //只考虑残量网络中的弧
              vis[e.to]=1;
106
107
              d[e.to]=d[x]+1;
108
              Q.push(e.to);
109
            }
110
          }
111
112
113
        return vis[t];
114
115
116
      int dfs(int x,int a) { //x表示当前结点, a表示目前为止的最小残量
117
        if(x==t||a==0)return a;//a等于0时及时退出,此时相当于断路了
118
        int flow=0,f;
119
        for(int&i=cur[x]; i < G[x].size(); i++) { //从上次考虑的弧开始, 注意要使用引用, 同
           时修改cur[x]
120
          Edge&e=edges[G[x][i]];//e是一条边
121
          if(d[x]+1==d[e.to]&&(f=dfs(e.to,min(a,e.cap-e.flow)))>0) {
122
            e.flow+=f;
123
            edges[G[x][i]^1].flow==f;
124
            flow+=f;
125
            a=f;
            if(!a)break;//a等于0及时退出, 当a!=0,说明当前节点还存在另一个曾广路分支。
126
127
128
          }
129
        }
130
        return flow;
131
      }
132
133
      int Maxflow(int s,int t) { //主过程
134
        this->s=s,this->t=t;
135
        int flow=0;
136
        while(bfs()) { //不停地用bfs构造分层网络, 然后用dfs沿着阻塞流增广
137
          memset(cur,0,sizeof(cur));
138
          flow+=dfs(s,INF);
139
        }
140
        return flow;
141
      }
142
    };
143
    /* ISAP */
144
145 | struct Edge {
```

```
146
      int from, to, cap, flow;
    };
147
148
    const int maxn=650;
149
    const int INF=0x3f3f3f3f3f;
    struct ISAP {
150
151
       int n,m,s,t;//结点数,边数(包括反向弧),源点编号,汇点编号
152
       vector<Edge>edges;
153
       vector<int>G[maxn];
154
       bool vis[maxn];
155
       int d[maxn];
156
       int cur[maxn];
157
       int p[maxn];
158
       int num[maxn];
159
       void AddEdge(int from,int to,int cap) {
160
         edges.push_back((Edge) {
161
           from, to, cap, 0
162
         });
163
         edges.push_back((Edge) {
164
           to, from, 0,0
165
         });
166
         m=edges.size();
167
         G[from].push_back(m-2);
168
         G[to].push_back(m-1);
169
       }
170
       bool RevBFS() {
171
         memset(vis,0,sizeof(vis));
172
         queue<int>Q;
173
         Q.push(t);
174
         d[t]=0;
         vis[t]=1;
175
176
         while(!Q.empty()) {
177
           int x=Q.front();
178
           Q.pop();
179
           for(int i=0; i<G[x].size(); i++) {
180
             Edge &e =edges[G[x][i]^1;
181
             if(!vis[e.from]&&e.cap>e.flow) {
182
               vis[e.from]=1;
183
               d[e.from]=d[x]+1;
               Q.push(e.from);
184
185
186
           }
187
188
         return vis[s];
189
190
       int Augment() {
191
         int x=t, a=INF;
         while(x!=s) {
192
193
           Edge &e = edges[p[x]];
194
           a= min(a,e.cap-e.flow);
195
           x=edges[p[x]].from;
196
         }
197
         x=t;
         while(x!=s) {
198
199
           edges[p[x]].flow+=a;
200
           edges[p[x]^1].flow=a;
201
           x=edges[p[x]].from;
202
         }
203
         return a;
204
205
       int Maxflow(int s,int t,int n) {
206
         this->s=s,this->t=t,this->n=n;
207
         int flow=0:
         RevBFS();
208
209
         memset(num,0,sizeof(num));
```

```
210
         for(int i=0; i<n; i++) {
211
           num[d[i]]++;
212
213
         int x=s;
214
         memset(cur,0,sizeof(cur));
         while(d[s]<n) {</pre>
215
216
           if(x==t) {
217
             flow+=Augment();
218
             x=s;
219
220
           int ok=0;
221
           for(int i=cur[x]; i<G[x].size(); i++) {
222
             Edge &e =edges[G[x][i]];
             if(e.cap>e.flow&d[x]==d[e.to]+1) {
223
224
               ok=1;
225
               p[e.to]=G[x][i];
226
               cur[x]=i;
227
               x=e.to;
228
               break;
             }
229
230
231
           if(!ok) {
232
             int m=n-1;
233
             for(int i=0; i<G[x].size(); i++) {
               Edge &e =edges[G[x][i]];
234
235
               if(e.cap>e.flow)
236
                 m=min(m,d[e.to]);
237
238
             if(--num[d[x]]==0)
239
               break;
240
             num[d[x]=m+1]++;
             cur[x]=0;
241
242
             if(x!=s)
243
               x=edges[p[x]].from;
244
           }
245
246
         return flow;
247
248
    };
249
    int main() {
250
       int n,m,a,b,c,res;
251
       while(scanf("%d%d",&m,&n)!=EOF) {
252
         ISAP tmp;
253
         for(int i=0; i<m; i++) {
           scanf("%d%d%d",&a,&b,&c);
254
255
           tmp.AddEdge(a,b,c);
256
257
         res=tmp.Maxflow(1,n,n);
258
         printf("%d\n", res);
259
260
       return 0;
261
          Strongly Connected Component
    /* Kosaraju */
  2
    #define MAXN
                      10010
  3
    #define MAXM
                      100010
  4
    struct edge {
  5
       int v;
  6
       edge *n;
  7
       edge(void):v(0),n(NULL) {}
       edge(int vv, edge *nn):v(vv),n(nn) {}
```

```
9 | };
10
   int nE;
11
   edge E[MAXM<<1];</pre>
   edge *ori[MAXN];
13
   edge *inv[MAXN];
14
   void add_edge(edge *front[], int u, int v) {
15
      int ne = ++nE;
16
      E[ne] = edge(v, u[front]);
      u[front] = \&(E[ne]);
17
18
19
   void connect(int u, int v) {
20
      add_edge(ori, u, v);
21
      add_edge(inv, v, u);
22
23
24
   int vis[MAXN];
25
   int vst[MAXN];
   void first_dfs(int u, int &sig) {
26
27
      vis[u] = 1;
28
      for(edge *e = u[ori]; e; e = e \rightarrow n)
29
        if(!vis[e->v])
30
          first_dfs(e->v, sig);
31
      vst[++sig] = u;
32
33
   int mark[MAXN];
34
   void second_dfs(int u, int sig) {
35
      vis[u] = 1;
36
      mark[u] = sig;
      for(edge *e = u[inv]; e; e = e \rightarrow n)
37
38
        if(!vis[e->v])
39
          second_dfs(e->v, sig);
40
41
42
   int N, M;
43
44
    int kosaraju(void) {
45
      int i;
46
      int sig = 0;
47
      for(i = 0; i \le N; ++i) vis[i] = 0;
48
      for(i = 1; i \le N; ++i) {
49
        if(!vis[i])
50
          first_dfs(i, sig);
51
      }
52
      sig = 1;
53
      for(i = 0; i \le N; ++i) vis[i] = 0;
54
      for(i = N; i > 0; --i) {
55
        if(!vis[vst[i]])
56
          second_dfs(vst[i], sig++);
57
      for(i = 1; i \le N; ++i)
58
59
        if(mark[i] != 1)
60
          return 0;
61
      return 1;
62
63
64
65
   void clear(void) {
66
      nE = 0;
      for(int i = 0; i <= N; ++i) {
67
68
        ori[i] = inv[i] = NULL;
69
   }
70
71
72 |/* Tarjan */
```

```
73
    #define MAXN
                      10010
 74
     #define MAXM
                       100010
 75
     struct edge {
 76
       int v;
 77
       edge *n;
 78
       edge(void):v(0),n(NULL) {}
 79
       edge(int vv, edge *nn):v(vv),n(nn) {}
 80
 81
     typedef edge *ep;
 82
     int nE;
 83
     edge E[MAXM];
 84
     edge *front[MAXN];
     void add_edge(int u, int v) {
 85
 86
       int ne = ++nE;
 87
       E[ne] = edge(v, u[front]);
 88
       u[front] = \&(E[ne]);
 89
     }
 90
 91
     int mark[MAXN];
 92
     int dfn[MAXN], low[MAXN];
 93
     int stk[MAXN];
 94
     int stk_top;
 95
 96
     void tardfs(int u, int stamp, int &scc) {
 97
       mark[u] = 1;
98
       dfn[u] = low[u] = stamp;
 99
       stk[stk\_top++] = u;
100
       for(ep e = u[front]; e; e = e\rightarrown) {
         if(0 == mark[e \rightarrow v]) tardfs(e \rightarrow v, ++stamp, scc);
101
         if(1 == mark[e \rightarrow v]) low[u] = min(low[u], low[e \rightarrow v]);
102
103
104
       if(dfn[u] == low[u]) {
105
         ++SCC;
106
         do {
107
           low[stk[stk_top-1]] = scc;
108
           mark[stk[stk\_top-1]] = 2;
109
         } while(stk[(stk_top--)-1] != u);
110
111
112
113
     int tarjan(int n) {
114
       int scc = 0, lay = 1;
115
       for(int i = 1; i <= n; ++i)
116
         if(0 == mark[i])
117
           tardfs(i, lay, scc);
118
       return scc;
119
     }
120
121
     int N, M;
122
123
     void clear(void) {
124
       nE = 0;
125
       for(int i = 0; i <= N; ++i) {
126
         i[front] = NULL;
         mark[i] = low[i] = 0;
127
128
129
       stk\_top = 0;
130
131
132
     /* Garbow */
133
     #define MAXN
                       10010
134
    #define MAXM
                       100010
135
136 | struct edge {
```

```
137
       int v;
138
       edge *n;
139
       edge(void):v(0),n(NULL) {}
140
       edge(int vv, edge *nn):v(vv),n(nn) {}
141
142
    typedef edge *ep;
143
144
     int nE;
145
     edge E[MAXM];
     edge *front[MAXN];
146
147
     void add_edge(int u, int v) {
148
       int ne = ++nE;
       E[ne] = edge(v, u[front]);
149
150
       u[front] = \&(E[ne]);
151
152
153
    int stk1[MAXN], stk1t;
154
    int stk2[MAXN], stk2t;
155
     int low[MAXN], belg[MAXN];
156
157
     void garbowdfs(int u, int lay, int &scc) {
158
       stk1[++stk1t] = u;
159
       stk2[++stk2t] = u;
160
       low[u] = ++lay;
       for(ep e=u[front]; e; e = e\rightarrown) {
161
162
         if(!low[e->v]) garbowdfs(e->v, lay, scc);
163
         else if (0 == belg[e->v])
164
           while(low[stk2[stk2t]] > low[e->v])
165
             ---stk2t;
166
       if(stk2[stk2t] == u) {
167
168
         stk2t—;
169
         SCC++;
170
         do {
171
           belg[stk1[stk1t]] = scc;
172
         } while(stk1[stk1t--] != u);
173
       }
174
175
176
    int grabow(int n) {
177
       int i;
178
       int scc = 0, lay = 0;
179
       for(i = 0; i \le n; ++i) {
180
         belg[i] = low[i] = 0;
181
182
       for(i = 1; i \le n; ++i)
183
         if(0 == low[i])
184
           garbowdfs(i, lay, scc);
185
       return scc;
    }
186
187
188
    int N, M;
189
     void clear(void) {
190
191
       nE = 0;
192
       for(int i = 0; i <= N; ++i) {
193
         front[i] = NULL;
194
195
    }
```

### 4.8 Perfect elimination ordering

求弦图的最大团数/最小色数的时候,只要在完美消除序列上从后往前贪心染色即可。

而求最大独立集/最小团覆盖的时候,只要在完美消除序列上从前往后贪心取点即可。

```
1
 2
    * BZOJ 1006
 3
    * [HN0I2008] 神奇的国度
 4
    * 最大势法求完美消除序列
 5
    * by Abreto<m@abreto.net>.
 6
    **/
 7
   #include <cassert>
 8
   #include <cstdio>
 9
   #include <vector>
10
   |#include <bitset>
   #include <algorithm>
11
12
13
   using namespace std;
14
   typedef vector<int> vi;
15
   typedef vi::iterator vii;
   #define pb push_back
16
17
   #define MAXN 10100
18
   |#define MAXM 1000100
19
20
   int n;
21
   vi g[MAXN];
22
   int ans;
23
24
   struct node_t {
25
     int v;
     node_t *nxt;
26
27
   } node[MAXM << 2];</pre>
28
   int used;
29
   node_t *new_node(void) {
      return node + (used ++);
30
31
32
33
   node_t *f[MAXN]; /* head */
34
   void lkto(int pos, int item) {
35
     node_t *t = new_node();
36
     t\rightarrow v = item;
37
      t\rightarrow nxt = f[pos];
38
     f[pos] = t;
39
   }
40
41
   int usedby[MAXN];
42
   int color[MAXN];
   bitset<MAXN> added;
43
44
   int label[MAXN], max_label;
45
   void mcs(void) {
46
      for (int i = 1; i \le n; i++) lkto(0, i);
47
     for (int i = n; i > 0; i---) {
48
        node_t *cur = f[max_label];
49
        assert(cur != NULL);
        while (added.test(cur->v)) { /* already added */
50
51
          cur = cur->nxt;
          while (NULL == cur)
52
53
            cur = f[ --max_label ];
54
55
        f[ max_label ] = cur->nxt;
56
        while (max_label && NULL == f[max_label]) max_label--;
57
        int u = cur -> v;
58
        added.set(u);
59
        /* the i-th is u */
60
        for (vii it = g[u].begin(); it != g[u].end(); it++) {
61
          int v = *it;
          if (!added.test(v)) {
62
```

```
label[v] ++;
63
64
            max_label = max(max_label, label[v]);
65
            lkto(label[v], v);
66
67
68
          usedby[color[v]] = i;
69
        for (int j = 1; j <= n; j++)
  if (usedby[j] != i) {</pre>
70
71
72
            color[u] = j;
73
            break;
74
75
        ans = max(ans, color[u]);
76
77
   }
78
79
   int main(void) {
80
      int m;
      scanf("%d%d", &n, &m);
81
82
      while (m--) {
83
        int ai, bi;
        scanf("%d%d", &ai, &bi);
84
85
        g[ai].pb(bi);
86
        g[bi].pb(ai);
87
      }
88
      mcs();
      printf("%d\n", ans);
89
90
      return 0;
91 | }
    5
        Math
   5.1 Euler Function
   /* Euler function phi(x), by Abreto<m@abreto.net>. */
 1
 3
   #define MAXX
                     3000000
 4
 5
   int phi[MAXX];
 6
    void get_euler(void) {
 7
      int i = 0, j = 0;
 8
      phi[1] = 1;
      for(i = 2; i < MAXX; ++i)
 9
10
        if(!phi[i])
11
          for(j = i; j < MAXX; j += i) {
12
            if(!phi[j]) phi[j] = j;
13
            phi[j] = phi[j]/i * (i-1);
14
15 | }
         Möbius Function
   void sieve() {
 1
 2
      fill(isPrime, isPrime + maxn, 1);
 3
      mu[1] = 1, num = 0;
 4
      for (int i = 2; i < maxn; ++i) {
        if (isPrime[i]) primes[num++] = i, mu[i] = -1;
 5
        static int d;
 6
        for (int j = 0; j < num && (d = i * primes[j]) < maxn; ++j) {
 7
 8
          isPrime[d] = false;
 9
          if (i % primes[j] == 0) {
```

```
10 | mu[d] = 0;

11 | break;

12 | } else mu[d] = -mu[i];

13 | }

14 | }

15 |}
```

# 5.3 Number Theory Inverse

```
|#include <bits/stdc++.h>
 2
   using namespace std;
 3
 4
   const int n=10000000;
                                /* */
   const long long mod=1e9+7; /* prime required. */
 5
 7
   long long fact[n],fiv[n],inv[n];
 8
9
   int main() {
10
     fact[0]=fact[1]=1;
11
     fiv[0]=fiv[1]=1;
12
     inv[1]=1;
13
      for (int i=2; i<n; i++) {
        fact[i]=fact[i-1]*i%mod;
14
15
        inv[i]=(mod-mod/i)*inv[mod%i]%mod;
        fiv[i]=inv[i]*fiv[i-1]%mod;
16
17
18
     for (int i=1; i<n; i++) {
19
        if (fact[i]*fiv[i]%mod!=1) printf("fact_wrong: _\%d\n",i);
20
                                     printf("intv_wrong:_%d\n",i);
        if (inv[i]*i\%mod!=1)
21
22
     cout<<"complete"<<endl;</pre>
23
      return 0;
24
```

## 5.4 Chinese Remainder Theorem

```
x \equiv a_i \pmod{m_i}
```

```
/* Chinese Remainder Theorem, by Abreto<m@abreto.net>. */
   #include "euler.c"
 4
   #define MAXN
 5
 6
   typedef long long int 11;
 7
 8
   11 quickpow(ll a, ll b, ll mod) {
 9
     ll ret = 1, base = a;
     while(b > 0) {
10
11
        if(b \& 1) ret = (ret * base) % mod;
        base = (base * base) % mod;
12
13
        b >>= 1;
14
15
     return ret;
16
17
18
19
   Il a[MAXN], m[MAXN]; /* a and m is indexed from 0. */
20
   ll x, M;
21
22 | void naive_crt(void) {
```

```
23
     int i = 0;
24
     11 Mi[MAXN], nMi[MAXN];
25
     11 t[MAXN];
26
27
     M = 1;
28
     for(i = 0; i < N; ++i)
29
        M *= a[i];
30
      for(i = 0; i < N; ++i)
        Mi[i] = M / a[i];
31
     get_euler();
32
33
     for(i = 0; i < N; ++i)
34
        nMi[i] = quickpow(Mi[i], phi[a[i]]-1, a[i]);
     for(i = 0; i < N; ++i)
35
36
        t[i] = ((a[i] * Mi[i]) % M) * nMi[i] % M;
     for(i = 0; i < N; ++i)
37
38
        x = (x + t[i]) % M;
39
        Linear congruences
   |#include <cstdio>
 2
   #include <cassert>
 3
   #include <cstdlib>
 4
 5
   using namespace std;
 6
 7
   class mod_equ_resolver {
 8
     typedef long long int ll;
 9
     ll a, m;
10
     inline void gurantee(void) {
11
        if (a < 0) {
          11 k = (-a) / m;
12
          a += (k + 111) * m;
13
14
          a = (a + m) \% m;
15
        } else {
16
          a \% = m;
17
18
        // printf("x = \%lld (mod \%lld)\n",a, m);
19
   public:
20
21
     mod_equ_resolver(void) {
22
        a = 011;
23
        m = 111;
24
25
     ll exgcd(ll m, ll n, ll &x, ll &y) {
26
        if (0 == n) {
27
          x = 1;
28
          y = 0;
29
          return m;
30
31
        ll g = exgcd(n, m % n, x, y);
32
        11 t = x;
33
        x = y;
        y = t - m / n * y;
34
35
        return g;
36
37
     int onemore(ll a2, ll m2) {
38
        11 x, y;
39
        ll g = exgcd(m, m2, x, y);
40
        assert(x*m+y*m2==g);
41
        a2 = (a2 + m2) \% m2;
        if ( abs(a2 - a) \% g ) return -1;
42
43
        ll newm = m / g * m2;
```

```
44
        11 newa = a + (a2 - a) / g * x * m;
45
        a = newa;
46
        m = newm;
47
        gurantee();
48
        return 0;
49
50
      ll resolve(void) {
51
        return a;
52
53 |};
    Usage: For
                                           x \equiv a_1
   run
 1 |mod_equ_resolver solver;
   for (int i = 1; i <= k; i++)
 3
        solver.onemore(a[i], m[i]);
    then the solution is
                                     x \equiv solver.a \mod solver.m
   5.6 FFT
   |#include <cmath>
 1
 2
   using namespace std;
 3
   namespace fft {
 4
   #define eps (1e-9)
 5
   template < typename T = double >
   struct dbl {
 6
 7
      Tx;
      dbl(void):x(0.0) {}
 8
 9
      template <typename U>
10
      dbl(U a):x((T)a) {}
11
      inline char sgn(void) {
12
        return ((x \ge -eps) & (x \le -eps))?(0):((x \ge -eps)?(1):(-1));
13
14
      inline T tabs(void) {
15
        return ((x \ge -eps) & (x \le -eps))?(0.0):((x \ge -eps)?(x):(-x));
16
17
      inline dbl abs(void) {
18
        return dbl(tabs());
19
20
      template <typename U> inline dbl &operator=(const U b) {
21
        x=(T)b;
22
        return (*this);
23
24
      inline T *operator&(void) {
25
        return &x;
26
      inline dbl operator—(void) const {
27
28
        return dbl(-x);
29
      inline dbl operator+(const dbl &b) const {
30
31
        return dbl(x+b.x);
32
33
      inline dbl operator-(const dbl &b) const {
34
        return dbl(x-b.x);
35
```

```
inline dbl operator*(const dbl &b) const {
36
37
        return dbl(x*b.x);
38
39
     inline dbl operator/(const dbl &b) const {
40
        return dbl(x/b.x);
41
42
      template <typename U> inline dbl operator^(const U &b) const {
43
        T ret=1.0, base=x;
        while(b) {
44
45
          if(b&1)ret*=base;
46
          base*=base;
47
          b>>=1;
        }
48
49
        return dbl(ret);
50
51
     inline dbl operator+=(const dbl &b) {
52
        return dbl(x+=b.x);
53
54
     inline dbl operator—=(const dbl &b) {
55
        return dbl(x=b.x);
56
57
     inline dbl operator*=(const dbl &b) {
58
        return dbl(x*=b.x);
59
60
     inline dbl operator/=(const dbl &b) {
61
        return dbl(x/=b.x);
62
63
     template <typename U> inline dbl operator^=(const U &b) {
64
        dbl tmp=(*this)^b;
65
        *this=tmp;
66
        return tmp;
67
68
     inline bool operator==(const dbl &b) const {
        return (0 == ((*this)-b).sgn());
69
70
71
     inline bool operator!=(const dbl &b) const {
72
        return (0 != ((*this)-b).sgn());
73
74
     inline bool operator<(const dbl &b) const {
75
        return (-1 == ((*this)-b).sgn());
76
77
     inline bool operator<=(const dbl &b) const {
78
        return (((*this)==b) || ((*this)<b));
79
     inline bool operator>(const dbl &b) const {
80
81
        return (b < (*this));
82
83
     inline bool operator>=(const dbl &b) const {
84
        return (((*this)==b) || ((*this)>b));
85
     template <typename U> inline operator U() const {
86
87
        return (U)x;
88
89
      inline char operator[](unsigned n) {
90
        if(n >= 0) {
91
          long long int ret=x;
92
          while(n--) {
93
            ret/=10;
94
95
          return (ret%10);
96
        } else {
97
          T ret=x;
98
          n=-n;
99
          while(n-)ret*=10.0;
```

```
100
           return ((long long int)ret)%10;
101
102
      }
103
    };
104
    template <typename T>
105
    struct Complex {
106
       T x,y; /* x + iy */
107
      Complex(void):x(T()),y(T())  {}
108
      Complex(T xx):x(xx) {}
      Complex(T xx,T yy):x(xx),y(yy) {}
109
110
       inline Complex operator—(void) const {
111
         return Complex(-x,-y);
112
113
      inline Complex operator+(const Complex& b) const {
114
         return Complex(x+b.x,y+b.y);
115
116
      inline Complex operator—(const Complex& b) const {
117
         return Complex(x-b.x,y-b.y);
118
119
      inline Complex operator*(const Complex& b) const {
120
         return Complex(x*b.x-y*b.y,x*b.y+y*b.x);
121
122
      inline Complex operator/(const Complex& b) const {
         T bo=b.x*b.x+b.y*b.y;
123
124
         return Complex((x*b.x+y*b.y)/bo,(y*b.x-x*b.y)/bo);
125
      }
126
      inline Complex& operator+=(const Complex& b) {
127
         Complex tmp=(*this)+b;
128
         (*this)=tmp;
129
         return (*this);
130
131
       inline Complex& operator—=(const Complex& b) {
132
         Complex tmp=(*this)_b;
133
         (*this)=tmp;
134
         return (*this);
135
136
       inline Complex& operator*=(const Complex& b) {
137
         Complex tmp=(*this)*b;
138
         (*this)=tmp;
139
         return (*this);
140
141
      inline Complex& operator/=(const Complex& b) {
142
         Complex tmp=(*this)/b;
143
         (*this)=tmp;
144
         return (*this);
145
146
      inline friend Complex operator+(const T& a, const Complex& b) {
147
         return Complex(a)+b;
148
149
      inline friend Complex operator—(const T& a, const Complex& b) {
150
         return Complex(a)—b;
151
152
      inline friend Complex operator*(const T& a, const Complex& b) {
153
         return Complex(a)*b;
154
155
      inline friend Complex operator/(const T& a, const Complex& b) {
         return Complex(a)/b;
156
157
158
159
    typedef dbl<> Double;
160
    typedef Complex<Double> ComplexD;
161
    typedef long long int ll;
162
    const int maxn = 2000000; /* !! */
    const Double pi(acos(-1.0));
163
```

```
164
165
    void build(ComplexD _P[], ComplexD P[], int n, int m, int curr, int &cnt) {
166
      if(m == n) {
167
         _P[curr] = P[cnt++];
168
      } else {
169
         build(_P, P, n, m*2, curr, cnt);
170
         build(_P, _P, _n, _m*2, _curr+m, _cnt);
171
172
173
174
    void FFT(ComplexD P[], int n, int oper) { /* n should be 2^k. */
175
      static ComplexD _P[maxn];
      int cnt = 0;
176
177
      build(_P, P, n, 1, 0, cnt);
178
       copy(P, P+n, P);
      for(int d = 0; (1<<d)<n; ++d) {
179
180
         int m = 1 << d;
         int m2 = m*2;
181
182
         Double p0 = pi / m * oper;
183
         ComplexD unit_p0(cos(p0.x), sin(p0.x));
184
         for(int i = 0; i < n; i += m2) {
185
           ComplexD unit(1,0);
186
           for(int j = 0; j < m; ++j) {
187
             ComplexD &P1 = P[i+j+m], &P2 = P[i+j];
188
             ComplexD t = unit * P1;
             P1 = P2 - t;
189
190
             P2 = P2 + t;
191
             unit *= unit_p0;
192
           }
193
         }
194
195
      if(-1 == oper) {
196
         for(int i = 0; i < n; ++i)
197
           P[i] /= Double(n);
198
      }
199
200
        NTT
    |#include<bits/stdc++.h>
    #define ll long long
  3
    const int N=262144;
    const ll MOD=50000000001507329LL;//998244353 1004535809
  4
  5
    using namespace std;
  6
    int n,m;
  7
    ll a[N],b[N],x[N],y[N];
  8
    ll wn[25];
  9
    ll Mul(ll x, ll y) { //乘法超ll用快速乘, 主函数也需要用
 10
      ll ans=(x*y-(ll)((long double)x/MOD*y+1e-8)*MOD);
 11
       return ans<0?ans+MOD:ans;</pre>
 12
 13
    11 Qpow(ll a,ll b,ll M) {
 14
      ll ans=1;
 15
      a%=M;
 16
      while(b) {
 17
         if(b&1) ans=Mul(ans,a);
 18
         a=Mul(a,a);
 19
         b>>=1;
 20
 21
      return ans;
 22
    |void Getwn() { //主函数预处理getwn()
```

```
24
      for(int i=0; i<25; i++) {
25
        wn[i]=Qpow(3,(MOD-1)/(1<< i),MOD);
26
27
28
   void NTT(ll *x,int n,int rev) {
29
      int i,j,k,ds;
30
      ll w,u,∨;
31
      for(i=1, j=n>>1, k=n>>1; i< n-1; i++, k=n>>1) {
32
        if(i<j) swap(x[i],x[j]);
33
        while(j>=k) j==k,k>>=1;
34
        if(j< k) j+=k;
35
36
      for(i=2,ds=1; i<=n; i<<=1,ds++) {
37
        for(j=0; j<n; j+=i) {
38
          w=1;
39
          for(k=j; k< j+i/2; k++) {
40
            u=x[k];
41
            v=Mul(w,x[k+i/2]);
42
            x[k]=(u+v)\%MOD;
43
            x[k+i/2]=(u-v+MOD)%MOD;
44
            w=Mul(w,wn[ds]);
45
46
        }
47
      if(rev==-1) {
48
49
        for(i=1; i< n/2; i++) swap(x[i],x[n-i]);
50
        w=Qpow(n,MOD-2,MOD);
51
        for(i=0; i<n; i++) x[i]=Mul(x[i],w);
      }
52
53
54
    int main() {
      Getwn();
55
      while(~scanf("%d%d",&n,&m)) {
56
        for(int i=0; i<n; i++)scanf("%lld",&a[i]);
57
58
        for(int i=0; i<m; i++)scanf("%lld",&b[i]);
59
        int len=1,s=n+m;
60
        while(len<s)len<<=1;</pre>
61
        for(int i=n; i<len; i++)a[i]=0;
        for(int i=m; i<len; i++)b[i]=0;
62
63
        NTT(a, len, 1);
64
        NTT(b, len, 1);
        for(int i=0; i<len; i++)a[i]=Mul(a[i],b[i]);
65
66
        NTT(a, len, -1);
67
        for(int i=0; i<=s; i++)printf("%lld<sub>\\\\\\</sub>",a[i]);
68
        puts("");
69
70
   }
71
72
   #include<cstdio>
73
   #include<iostream>
75
   |#include<cstring>
76
   #include<cmath>
77
   #include<complex>
78
   using namespace std;
79
   typedef long long LL;
80
   const LL MOD=998244353,g=3,gi=332748118;
81
   const LL N=1000005;
82
   LL n,m;
83
   LL a[N],b[N];
84
   LL pow (LL x,LL y) {
      if (y==1) return x;
85
86
      LL lalal=pow(x,y>>1)
87
      lalal=lalal*lalal%MOD;
```

```
88
       if (y&1) lalal=lalal*x%MOD;
 89
       return lalal;
 90
    }
 91
    void ntt (LL *a,LL n,LL o) {
 92
       if (n==1) return;
 93
       LL k=(n>>1);
 94
       LL w=1, wn=pow(o==1?q:qi, (MOD-1)/n), a0[k], a1[k];
 95
       for (LL u=0; u< k; u++) {
         LL i=u*2;
 96
 97
         a0[u]=a[i];
98
         a1[u]=a[i+1];
 99
100
       ntt(a0,k,o);
       ntt(a1,k,o);
101
102
       for (LL u=0; u< k; u++) {
103
         a[u]=a0[u]+w*a1[u]%MOD;
104
         a[u]=(a[u]%MOD+MOD)%MOD;
105
         a[u+k]=a0[u]-w*a1[u];
106
         a[u+k]=(a[u+k]%MOD+MOD)%MOD;
107
         w=w*wn%MOD;
108
       }
109
110
     void ntt(LL *a,LL n,LL op) {
111
       for (LL u=0; u<n; u++) bin[u]=(bin[u>>1]>>1)|((u&1)*(n>>1));
112
       for (LL u=0; u<n; u++) if (u<bin[u]) swap(a[u],a[bin[u]]);
113
       for (LL u=1; u<n; u<<=1) {
114
         LL wn=pow(op==1?g:gi,(MOD-1)/(u<<1)),w,t;
115
         for (LL i=0; i< n; i=i+(u<<1)) {
116
           w=1;
           for (LL k=0; k<u; k++) {
117
             t=w*a[u+i+k]%MOD;
118
119
             a[u+i+k]=(a[i+k]-t+MOD)%MOD;
120
             a[i+k]=(a[i+k]+t)%MOD;
121
             w=w*wn%MOD;
122
           }
123
         }
124
       if(op==-1) {
125
         LL Inv=pow(n,MOD-2);
126
127
         for(LL i=0; i<n; i++) a[i]=a[i]*Inv%MOD;
128
       }
129
    }
130
131
     int main() {
132
       scanf("%I64d%I64d",&n,&m);
       for (LL u=0; u<=n; u++) scanf("%I64d",&a[u]);
133
       for (LL u=0; u<=m; u++) scanf("%I64d",&b[u]);
134
135
       m=m+n;
136
       n=1;
137
       while (n \le m) n \le 1;
       ntt(a,n,1);
138
139
       ntt(b,n,1);
140
       for (LL u=0; u<=n; u++) a[u]*=b[u];
141
       ntt(a,n,-1);
       LL inv=pow(n,MOD-2);
142
143
       for (LL u=0; u<=m; u++)
                                  printf("%I64d<sub>\\_</sub>",a[u]*inv\%MOD);
144
       return 0;
145
```

# 5.8 Fast Walsh-Hadamard transform

异或

$$\mathcal{F}\{A\} = [\mathcal{F}\{A_0\} + \mathcal{F}\{A_1\}, \mathcal{F}\{A_0\} - \mathcal{F}\{A_1\}]$$

$$\mathcal{F}^{-1}\{A\} = \left[ \mathcal{F}^{-1}\{\frac{A_0 + A_1}{2}\}, \mathcal{F}^{-1}\{\frac{A_0 - A_1}{2}\} \right]$$

• 按位与

$$\mathcal{F}\{A\} = [\mathcal{F}\{A_0\} + \mathcal{F}\{A_1\}, \mathcal{F}\{A_1\}]$$
$$\mathcal{F}^{-1}\{A\} = [\mathcal{F}^{-1}\{A_0\} - \mathcal{F}^{-1}\{A_1\}, \mathcal{F}^{-1}\{A_1\}]$$

• 按位或

16

17

$$\mathcal{F}\{A\} = [\mathcal{F}\{A_0\}, \mathcal{F}\{A_1\} + \mathcal{F}\{A_0\}]$$
$$\mathcal{F}^{-1}\{A\} = [\mathcal{F}^{-1}\{A_0\}, \mathcal{F}^{-1}\{A_1\} - \mathcal{F}^{-1}\{A_0\}]$$

```
void FWT(int a[],int n) {
 2
      for(int d=1; d<n; d<<=1)
 3
        for(int m=d<<1,i=0; i<n; i+=m)
          for(int j=0; j<d; j++) {
  int x=a[i+j],y=a[i+j+d];
 4
 5
 6
            a[i+j]=(x+y)\mod, a[i+j+d]=(x-y+mod)\mod;
 7
            //xor:a[i+j]=x+y,a[i+j+d]=(x-y+mod)%mod;
 8
            //and:a[i+j]=x+y;
 9
            //or:a[i+j+d]=x+y;
10
11
12
13
    void UFWT(int a□,int n) {
14
      for(int d=1; d<n; d<<=1)
15
        for(int m=d<<1,i=0; i<n; i+=m)
16
          for(int j=0; j<d; j++) {
17
            int x=a[i+j], y=a[i+j+d];
18
            a[i+j]=1LL*(x+y)*rev%mod, a[i+j+d]=(1LL*(x-y)*rev%mod+mod)%mod;
            //xor:a[i+j]=(x+y)/2,a[i+j+d]=(x-y)/2;
19
            //and:a[i+j]=x-y;
20
21
            //or:a[i+j+d]=y-x;
22
23
24
   void solve(int a□,int b□,int n) {
25
      FWT(a,n);
26
      FWT(b,n);
27
      for(int i=0; i<n; i++) a[i]=1LL*a[i]*b[i]%mod;
28
      UFWT(a,n);
29 }
    5.9 Lucas
 1
   /* Lucas, by Abreto<m@abreto.net>. */
 2
 3
    struct __lucas {
 4
      static const int maxp = 100000;
 5
      typedef long long int 11;
 6
 7
      int f[maxp]; // fiv[maxp], inv[maxp];
      inline int mul(const int a, const int b) {
 8
 9
        ll z = 1ll * a * b;
10
        z = z / p * p;
11
        return z;
12
      int qow(int a, int x) {
13
14
        int ret = 1;
15
        while (x) {
```

if (1 & x) ret = mul(ret, a);

a = mul(a, a);

```
18
         x >>= 1;
19
20
       return ret;
21
     }
22
     void init(int np) {
23
       p = np;
24
       // return; // uncomment this line if use binom()
25
       f[0] = f[1] = 1;
26
       // fiv[0] = fiv[1] = 1;
       // inv[1] = 1;
27
28
       for (int i = 2; i < p; i++) {
29
         f[i] = mul(f[i - 1], i);
30
         // inv[i] = mul(p - p / i, inv[p % i]);
         // fiv[i] = mul(fiv[i - 1], inv[i]);
31
       }
32
33
34
     int C(int n, int k) {
35
       if (n < k) return 0;
36
       return mul(f[n], qow(mul(f[k], f[n - k]), p - 2));
37
     /** use following if get TLE { */
38
39
     int binom(int n, int k) {
       if (n < k) return 0;
40
       if (k > n - k) k = n - k;
int a = 1, b = 1;
41
42
43
       while (k) {
44
         a = mul(a, n);
45
         b = mul(b, k);
46
         n--;
47
         k--;
48
49
       return mul(a, qow(b, p - 2));
50
51
     /** } ---- */
52
     int operator()(int n, int k) {
53
       if (0 == k) return 1;
54
       if (n  return <math>C(n, k);
55
       return mul(C(n \% p, k \% p), (*this)(n / p, k / p));
56
57 | } lucas;
         Linear Programming
   |/* 线性规划 */
 1
 2
   #include<bits/stdc++.h>
 3
 4
   using namespace std;
 5
   const int Maxn=110, Maxm=59;
 6
   class Simplex {
 7
 8
9
        接受有n个约束, m个基本变量的方程组a[0~n][0~m]
10
        a [0] [] 存放需要最大化的目标函数, a [] [0] 存放常数
11
        Base [] 存放基本变量的id,初始为1~m
12
        Rest □ 存 放 松 弛 变 量 的 id, 初 始 为 m+1~m+n
13
        返回此线性规划的最小值ans
14
        要 求 方 案 的 话, Base [] 中 的 变 量 值 为 0, Rest [] 中 的 变 量 值 为 相 应 行 的 [0]
15
        如果solve
16
        返回1,说明运行正常ans是它的最大值
        返回0,说明无可行解
17
18
        返回-1,说明解没有最大值
19
        测试:
20
        m=2, n=3
```

```
21
         double a[4][3]={
22
         {0,1,3},
23
         \{8,-1,1\},
24
         \{-3,1,1\},
25
         \{2,1,-4\}
26
         };
27
         solve=1, ans=64/3;
28
         注意ac不了可能是eps的问题
29
   public:
30
31
      static const double Inf;
32
      static const double eps;
33
      int n,m;
      double a[Maxn][Maxm];
34
35
      int Base[Maxm], Rest[Maxn];
36
      double val[Maxm];
37
      double ans;
38
      void pt() {
39
        for(int i=0; i<=n; i++) {
40
          for(int j=0; j<=m; j++)printf(^{\infty}.2f<sub>\(\tilde{1}\)</sub>,a[i][j]);
          puts("");
41
42
        }
43
44
      void pivot(int x, int y) { //将第x个非基本变量和第y个基本变量调换
45
        swap(Rest[x],Base[y]);
46
        double tmp=-1./a[x][y];
47
        a[x][y]=-1.;
48
        for(int j=0; j \leftarrow m; j++)a[x][j]*=tmp;
        for(int i=0; i<=n; i++) {
49
50
          if(i==x||fabs(a[i][y])<eps)continue;
51
          tmp=a[i][y];
52
          a[i][y]=0;
53
          for(int j=0; j<=m; j++)a[i][j]+=tmp*a[x][j];
54
        }
55
56
      bool opt() {
57
        while(1) {
58
          int csi=0;
59
          for(int i=1; i<=m; i++)if(a[0][i]>eps&&(!csi||Base[i]<Base[csi]))csi=i;
60
          if(!csi)break;
61
          int csj=0;
62
          double cur;
63
          for(int j=1; j<=n; j++) {
64
            if(a[j][csi]>-eps)continue;
65
            double tmp=-a[j][0]/a[j][csi];
66
            if(!csj||tmp+eps<cur||(fabs(tmp-cur)<eps&&Rest[j]<Rest[csj]))csj=j,cur=tmp;
67
68
          if(!csj)return 0;
69
          pivot(csj,csi);
70
71
        ans=a[0][0];
72
        return 1;
73
74
      bool init() {
        ans=0;
75
76
        for(int i=1; i<=m; i++)Base[i]=i;
77
        for(int i=1; i<=n; i++)Rest[i]=m+i;
78
        int cs=1;
79
        for(int i=2; i<=n; i++)if(a[i][0]<a[cs][0])cs=i;
80
        if(a[cs][0]>=-eps)return 1;
81
        static double tmp[Maxm];
82
        for(int i=0; i<=m; i++)tmp[i]=a[0][i],a[0][i]=0;
83
        for(int i=1; i<=n; i++)a[i][m+1]=1.;
84
        a[0][m+1]=-1.;
```

```
85
         Base[m+1]=m+n+1;
 86
         pivot(cs,++m);
 87
         opt();
 88
         m--;
 89
         if(a[0][0] \leftarrow eps) return 0;
 90
         cs=-1;
 91
         for(int i=1; i<=n; i++) {
 92
           if(Rest[i]>m+n) {
 93
             cs=i;
 94
             break;
 95
           }
 96
 97
         if(cs>=1) {
 98
           int nxt=-1;
 99
           m++;
100
           for(int i=1; i<=m; i++)if(a[cs][i]>eps||a[cs][i]<-eps) {
101
               nxt=i;
102
               break;
103
104
           pivot(cs,nxt);
105
           m--;
106
107
         for(int i=1; i<=m; i++) {
108
           if(Base[i]>m+n) {
109
             swap(Base[i],Base[m+1]);
110
             for(int j=0; j<=n; j++)a[j][i]=a[j][m+1];
111
             break;
112
           }
113
114
         for(int i=1; i<=m; i++)a[0][i]=0;
115
         a[0][0]=tmp[0];
         for(int i=1; i<=m; i++)if(Base[i]<=m)a[0][i]=tmp[Base[i]];</pre>
116
117
         for(int i=1; i<=n; i++) {
118
           if(Rest[i]<=m) {
119
             for(int j=0; j<=m; j++)a[0][j]+=tmp[Rest[i]]*a[i][j];
120
121
         }
122
         return 1;
123
124
       void getval() {
125
         for(int i=1; i<=m; i++)val[i]=0;
126
         for(int i=1; i<=n; i++)if(Rest[i]<=m)val[Rest[i]]=a[i][0];
127
         //for(int i=1;i<=m;i++)printf("%.2f ",val[i]);puts("");</pre>
128
       }
129
       int solve() {
130
         if(!init())return 0;
         if(!opt())return -1;
131
132
         getval();
133
         return 1;
134
       }
135
     } solver;
136
     const double Simplex:: Inf=1e80;
137
     const double Simplex:: eps=1e-8;
138
     int main() {
139
       int m,n,type;
       scanf("%d%d%d",&m,&n,&type);
140
141
       solver.a[0][0]=0;
       for(int i=1; i<=m; i++)scanf("%lf",&solver.a[0][i]);</pre>
142
       for(int i=1; i<=n; i++) {
143
144
         for(int j=1; j<=m+1; j++) {
           if(j==m+1)scanf("%lf",&solver.a[i][0]);
145
146
             scanf("%lf",&solver.a[i][j]);
147
148
             solver.a[i][j]=-solver.a[i][j];
```

```
149
          }
        }
150
151
152
      solver.m=m, solver.n=n;
153
      int rep=solver.solve();
154
      if(rep==0)puts("Infeasible");
155
      else if(rep==-1)puts("Unbounded");
156
      else {
157
        printf("%.12f\n", solver.ans);
158
        if(type==1) {
159
          for(int i=1; i<=m; i++)printf("%.12f%c",solver.val[i],i==m?'\n':'u');
160
161
      }
    }
162
    5.11 Big Prime Test
   |#include <iostream>
    #include <cstdlib>
 3
    using namespace std;
    typedef long long LL;
 4
 5
    LL minfactor, p[11] = \{2, 3, 5, 7, 11, 13, 17, 19, 23, 29\};
    LL gcd(LL a, LL b) {
 6
      return b ? gcd(b, a % b) : a;
 7
 8
 9
    LL qmult(LL a, LL b, LL mod) { // 快速乘模
10
      LL sum = 0;
11
      while (b) {
        if (b & 1) {
 12
13
          sum += a;
14
          if (sum >= mod) sum -= mod; // 此处无需用%, %运算比减法慢很多
15
16
        b >>= 1, a <<= 1;
17
        if (a >= mod) a -= mod;
18
19
      return sum;
20
21
    LL qpow(LL a, LL b, LL mod) { // 快速幂模
22
      LL res = 1;
23
      while (b) {
24
        if (b \& 1) res = qmult(res, a, mod);
25
        b >>= 1;
26
        a = qmult(a, a, mod);
27
28
      return res;
29
30
    bool prime_test(LL n, LL a) { // 对整数n,底数a进行测试,返回true表示通过测试
31
      LL p = qpow(a, n - 1, n);
32
      if (p != 1) return false;
33
      else { // 二次探测
        LL s = n - 1;
34
 35
        while (!(s & 1) && p == 1) {
 36
          s >>= 1;
37
          p = qpow(a, s, n);
38
39
        if (p == 1 \mid | p == n - 1) return true;
40
        else return false;
41
      }
42
    bool Miller_Rabin(LL n) { // 对整数n进行Miller_Rabin素数测试,返回true表示通过测试
43
 44
                       // if这一块其实可以不用
      if (n <= 29) {
45
        for (int i = 0; i < 10; i++) {
          if (n == p[i]) return true;
46
```

```
47
48
       return false;
49
50
     for (int i = 0; i < 10; i++) { // 利用前10个素数作为底数测试的正确率已经非常高
51
       if (gcd(n, p[i]) == 1 && !prime_test(n, p[i])) return false;
52
53
     return true;
54
   LL randf(LL x, LL n, LL c) { // 满足要求的产生伪随机数函数
55
56
     return (qmult(x, x, n) + c) \% n;
57
58
   LL pollard_rho(LL n, LL c) { // 查找n的因数, c为上面函数要用的随机数, c也可自己指定
       (但要有变化)
59
     LL x = rand() % n, y = x, i = 1, k = 2, p; // 随机生成随机数的初始值,也可自己指定
     while (true) {
60
61
       i++;
       x = randf(x, n, c);
62
63
       p = gcd(y - x + n, n);
       if (p > 1 \&\& p < n) return p;
64
65
       if (y == x) return n;
                             // 判 圈, 返 回 n 表 示 查 找 失 败, 要 更 新 随 机 种 子 重 新 查 找
       if (i == k) {
66
67
         y = x; // 更新范围和记录的数
68
         k <<= 1;
69
       }
70
71
72
   void find_factor(LL n) { // 查找所有因数
73
     if (Miller_Rabin(n)) {
74
       minfactor = min(minfactor, n);
75
       return ;
76
77
     LL p = n;
     while (p == n) p = pollard_rho(n, rand() % (n - 1) + 1); // 查找失败则更新随机种子
78
        重新查找,直到找到因子
                        // 递归查找更小因子
79
     find_factor(p);
80
     find_factor(n / p);
81
82
83
   int main() {
84
     int t;
85
     cin >> t;
86
     while (t--) {
87
       LL N;
88
       cin >> N;
89
       if (Miller_Rabin(N)) cout << "Prime" << endl;</pre>
90
       else {
91
         minfactor = N;
92
         find_factor(N);
93
         cout << minfactor << endl;</pre>
94
       }
95
96
     return 0;
97
   5.11.1 Miller Rabin
  /* Miller-Rabin Prime Test, by Abreto<m@abreto.net>. */
2
3
   |namespace miller_rabin {
4
5
   typedef long long int ll;
 6
   inline ll add(const ll a, const ll b, const ll mod) {
```

```
8
     ll z = a + b;
9
     if (z \ge mod) z = mod;
10
     return z;
11
   inline ll mul(ll a, ll b, const ll mod) {
12
13
     11 z = 0;
     if (a >= mod) a %= mod;
14
15
     if (b \ge mod) b mod;
16
     while (b) {
17
        if (1 \& b) z = add(z, a, mod);
18
        a = add(a, a, mod);
        b >>= 1;
19
20
     }
21
     return z;
22
23
24
   ll qow(ll a, ll x, ll mod) {
25
     ll ret = 1ll;
26
     while (x) {
27
        if (1 \& x) ret = mul(ret, a, mod);
28
        a = mul(a, a, mod);
29
        x >>= 1;
30
31
     return ret;
32
33
34
   const int K = 5;
35
   const int p[] = {
     2, 3, 7, 61, 24251
36
37
38
   const ll strong = 4685624825598111;
39
   /* 46 856 248 255 981 in (0, 1e16) */
40
41
   bool mr(ll n, int k) {
     ll d = n - 1;
42
43
     int s = 0;
44
     while (d > 1 \&\& 0 == (d \& 1)) {
45
        S++;
46
        d >>= 1;
47
48
     for (int i = 0; i < k; i++) {
49
        ll a = (i < K) ? p[i] : (1 + rand() % (n - 1));
50
        11 x = qow(a, d, n);
        for (int j = 0; j < s; j++) {
51
          ll xp = mul(x, x, n);
52
53
          if (1 == xp \&\& x != 1 \&\& x != n-1) return false;
54
55
56
        if (x != 1) return false;
57
58
     return true;
59
60
   /* 2,3,5,7,11,13 */
61
62
   const int pre[] = \{3, 5, 7, 11, 13\};
   bool test(ll n, int k = 5) {
63
64
     if (2 == n) return true;
65
     if (0 == (n \& 1)) return false;
66
     if (strong == n) return false;
67
     for (int i = 0; i < 5; i++) {
        if (n == pre[i]) return true;
68
69
        if (n == n / pre[i] * pre[i])
70
          return false;
71
     }
```

```
72
     return mr(n, k);
73
   }
74
75 |}
   5.11.2 Pollard's rho
   /* Pollard's rho, by Abreto<m@abreto.net>. */
 1
 3
   namespace pollards_rho {
 4
 5
   typedef long long int ll;
 6
 7
   inline ll add(const ll a, const ll b, ll mod) {
 8
     11 z = a + b;
9
     if (z >= mod) z -= mod;
10
     return z;
11
12
   inline ll mul(ll a, ll b, ll mod) {
     ll z = 0ll;
13
14
     if (a >= mod) a -= a / mod * mod;
     if (b \ge mod) b = b / mod * mod;
15
     while (b) {
16
17
        if (1 \& b) z = add(z, a, mod);
18
        a = add(a, a, mod);
19
        b >>= 1;
20
     }
21
     return z;
22
23
24
   ll gcd(ll m, ll n) {
25
     return (0 == n)? m : gcd(n, m % n);
26
27
   ll find(ll n, int c = -1) {
28
29
     ll x = rand() % n;
30
     11 y = x, k = 2;
31
     for (int i = 2; i++) {
32
        x = add(mul(x, x, n), (n + c) % n, n);
33
        ll d = gcd(y - x + n, n); // change to abs(y - x) if get WA
34
        if (1 != d && n != d) return d;
35
        if (y == x) return n;
        if (i == k) {
36
37
          y = x;
38
          k <<= 1;
39
        }
40
     }
41
   }
42
43
   /** usage:
44
     * void find(ll n, int c = 107)
45
    * {
         if (1 == n) return;
46
     *
47
         if ( miller-rabin(n) )
     *
48
         {
     *
49
           n is a prime;
     *
50
     *
           return;
51
     *
52
         ll p = n, k = c;
53
         while (p \ge n) p = pollards_rho(p, k--);
54
         find(p, c);
     *
55
         find(n/p, c);
     *
56
    * }
```

```
57 | **/
58 |
59 |}
```

## 5.12 Montgomery modular multiplication

```
1
 2
    /* -- Montgomery modular algorithm { -- */
 3
   struct Mod64 {
 4
      typedef long long ll;
 5
      typedef unsigned long long u64;
      typedef __int128_t i128;
 6
     typedef __uint128_t u128;
Mod64() :n_(0) {}
 7
 8
 9
      Mod64(u64 n) :n_(init(n)) {}
10
      static u64 init(u64 w) {
11
        return reduce(u128(w) * r2);
12
      static void set_mod(u64 m) {
13
14
        mod = m;
15
        assert(mod & 1);
16
        inv = m;
17
        for (int i = 0; i < 5; ++i) inv *= 2 - inv * m;
18
        r2 = -u128(m) \% m;
19
      }
20
      static u64 reduce(u128 x) {
21
        u64 y = u64(x >> 64) - u64((u128(u64(x)*inv)*mod) >> 64);
22
        return ll(y)<0 ? y + mod : y;
23
24
      Mod64& operator += (Mod64 rhs) {
25
        n_+ = rhs.n_- mod;
        if (ll(n_)<0) n_+=mod;
26
27
        return *this;
28
29
      Mod64 operator + (Mod64 rhs) const {
30
        return Mod64(*this) += rhs;
31
32
      Mod64& operator -= (Mod64 rhs) {
33
        n_ -= rhs.n_;
34
        if (ll(n_)<0) n_+=mod;
35
        return *this;
36
37
      Mod64 operator - (Mod64 rhs) const {
38
        return Mod64(*this) -= rhs;
39
40
      Mod64& operator *= (Mod64 rhs) {
41
        n_{-} = reduce(u128(n_{-})*rhs.n_{-});
42
        return *this;
43
44
      Mod64 operator * (Mod64 rhs) const {
45
        return Mod64(*this) *= rhs;
46
47
      u64 get() const {
48
        return reduce(n_);
49
50
      static u64 mod, inv, r2;
51
      u64 n_;
52
   };
53
   Mod64::u64 Mod64::mod, Mod64::inv, Mod64::r2;
54
55
   /* -- } Montgomery modular algorithm -- */
56
57
   /**
```

```
58
    * usage:
59
     * First, Mod64::set_mod();
60
    * Mod64 a, b, c(init_val);
61
    * a = b * c;
62
    * printf("%llu\n", a.get());
63
          Berlekamp Massey
   /* Berlekamp Massey by HoldZhu. */
   #include <cstdio>
 3
   #include <vector>
 4
 5
   using namespace std;
 6
7
   namespace BerlekampMassey {
 8
   const int mod = 1e9 + 7;
   int L, m, b, n;
9
10
   vector<int> s, C, B;
   void init() {
11
12
     s.clear();
13
     C.clear();
14
     B.clear();
15
     C.push_back(1);
16
     B.push_back(1);
17
     L = n = 0;
     m = b = 1;
18
19
20
   int pow_mod(int a, int k) {
21
     int s = 1;
22
     while (k) {
23
        if (k & 1)
24
          s = 111 * s * a % mod;
25
        a = 111 * a * a % mod;
26
        k >>= 1;
27
28
     return s;
29
30
   void update(int d) {
31
      s.push_back(d);
     for (int i = 1; i \le L; ++i)
32
33
        d = (d + 111 * C[i] * s[n - i] % mod) % mod;
     if (d == 0)
34
35
        ++m;
36
     else if (2 * L <= n) {
37
        vector<int> T = C;
38
        C.resize(n + 1 - L + 1);
39
        for (int i = L + 1; i \le n + 1 - L; ++i)
40
          C[i] = 0;
        for (int i = 0; i < B.size(); ++i)
41
          C[i + m] = (C[i + m] + mod - 111 * d * pow_mod(b, mod - 2) % mod * B[i] % mod)
42
             % mod;
43
        L = n + 1 - L;
44
        B = T;
45
        b = d;
46
        m = 1;
47
     } else {
48
        for (int i = 0; i < B.size(); ++i)
49
          C[i + m] = (C[i + m] + mod - 111 * d * pow_mod(b, mod - 2) % mod * B[i] % mod)
             % mod;
50
        ++m;
     }
51
52
     ++n;
```

```
53
54
    void output() {
55
      printf("F(n)=");
56
       for (int i = 1; i < C.size(); ++i) {
         int output = (mod - C[i]) \% mod;
57
58
         if (output > mod / 2)
 59
           output = mod;
         printf("%s%d*F(n-%d)", (output < 0 \mid i == 1)? "" : "+", output, i);
60
61
62
      puts("");
63
64
    void output_code_for() {
      static const char *name = "dp";
65
       static const char *index = "i";
66
       static const char *upperbound = "maxn";
67
68
      puts("//_Generated_by_Berlekamp—Massey_algorithm");
69
      for (int i = 1; i < C.size(); ++i) {
 70
         printf("%s[%d]=%d;\n", name, i - 1, s[i - 1]);
 71
      printf("for(int<sub>\(\)</sub>i=\(\)d;i<\(\)s;++i)\\n", (int)C.size() - 1, upperbound);</pre>
 72
 73
      printf("_{\sqcup \sqcup}%s[%s]=((", name, index);
      for (int i = 1; i < C.size(); ++i) {
 74
 75
         int output = (mod - C[i]) % mod;
 76
         if (output > mod / 2)
 77
           output -= mod;
         printf("%s%d*%s[%s-%d]%mod", (output < 0 | | i == 1) ? "" : "+", output, name,
 78
            index, i);
79
80
      puts(")%mod+mod)%mod;");
81
82
    void output_code_matrix() {
83
      // TODO
84
85
    };
86
87
    /** usage */
88
    int usage() {
      // int arr[12] = {2, 24, 96, 416, 1536, 5504, 18944, 64000, 212992, 702464,
89
          2301952, 7512064};
90
      int arr[] = \{3, 20, 119, 696, 4059, 23660, 137903, 803760, 4684659\};
91
      BerlekampMassey::init();
92
       for (auto ai : arr) {
93
         BerlekampMassey::update(ai);
94
95
      printf("Formule:□");
96
      BerlekampMassey::output();
97
      printf("Code: \n");
98
      BerlekampMassey::output_code_for();
99
       return 0;
100 | }
         String
    6
    6.1
         Hash
    /* Common hash for any substrings. */
  1
  3
    typedef unsigned long long int llu;
    #define MAXN 1000000
  5
    int n;
```

char s[MAXN];

|llu H[MAXN], xP[MAXN], P = 9999111;

```
8
   void init(void) {
9
     int i = 0;
10
     xP[0] = 111;
11
     for(i = 1; i < MAXN; ++i) xP[i] = xP[i-1] * P;
12
     H[n] = 0;
13
     for(i = n-1; i \ge 0; --i) H[i] = H[i+1]*P + s[i];
14
15 |\#define HASH(i,l) (H[i] - H[i+l]*xP[l])
   6.2 KMP
   /* KMP, by Abreto<m@abreto.net>. */
 1
 2
   #include <string.h>
 3
 4
   /* !!NEED IMPROVING!! */
 5
 6
   #define MAXL (1000010)
   char W[MAXL], T[MAXL];
 8
9
   int f[MAXL];
10
   int lW, lT;
11
12
   int count(void) {
13
     int cnt = 0;
14
     int i, j;
15
      lW = strlen(W);
     lT = strlen(T);
16
17
     // -- self-matching
     f[0] = j = -1;
18
     for(i = 1; i < lW; i++) {
19
20
        while( j \ge 0 \& W[j+1] != W[i] )
21
          j = f[j];
        if( W[j+1] == W[i] ) j++;
22
23
        f[i] = j;
24
     // ___
25
26
      i = -1;
     for(i = 0; i < lT; i++) {
27
28
        while(j \ge 0 \&\& W[j+1] != T[i])
          j = f[j];
29
        if(W[j+1] == T[i]) j++;
30
31
        if( j == lW-1 ) {
32
          cnt++;
33
          j = f[j];
        }
34
35
36
      return cnt;
37
   6.3 \text{ exKMP}
 1
   #include <bits/stdc++.h>
 2
   using namespace std;
 3
   namespace exkmp {
 6
   const int maxn = 1000100, maxm = 1000100;
 8
   int n, m;
 9
   char S[maxn], T[maxm];
10
```

```
|/* the length of longest prefix between T[i..m-1] and T[0..m-1] */
11
   int nxt[maxm];
12
   /* the length of longest prefix between S[i...n-1] and T[0...m-1] */
13
   int ex[maxn];
15
16
   void getsize() {
17
      n = strlen(S);
18
     m = strlen(T);
19
20
21
   void self(void) {
22
      int q = 1, p = 0;
23
      nxt[0] = m;
24
      while (1 + p < m \& T[1 + p] == T[p]) p++;
25
      nxt[1] = p;
      for (int i = 2; i < m; i++) {
26
27
        int l = nxt[i - q];
28
        if (i + l - 1 < p) {
29
          nxt[i] = 1;
        } else {
30
          int j = max(0, p - i + 1);
31
          while (i + j < m \&\& T[i + j] == T[j]) j++;
32
33
          nxt[i] = j;
34
          p = i + j - 1;
35
          q = i;
36
        }
37
      }
38
   }
39
40
   void run(void) {
41
      int q = 0, p = 0;
42
      self();
43
      while (p < n \&\& p < m \&\& S[p] == T[p]) p++;
44
      ex[0] = p;
45
46
      for (int i = 1; i < n; i++) {
47
        int l = nxt[i - q];
48
        if (i + l - 1 < p) {
          ex[i] = l;
49
50
        } else {
51
          int j = max(0, p - i + 1);
52
          while (i + j < n \&\& S[i + j] == T[j]) j++;
53
          ex[i] = j;
54
          p = i + j - 1;
55
          q = i;
56
        }
57
      }
58
59
   void inspect(void) {
60
61
      printf("S:□");
62
      for (int i = 0; i < n; i++) putchar(S[i]);
      puts("")
63
     printf("T:⊔");
64
65
      for (int i = 0; i < m; i++) putchar(T[i]);
      puts("");
66
67
      printf("next:");
      for (int i = 0; i < m; i++) printf("_{\square}%d", nxt[i]);
68
      puts("");
69
70
      printf("extend:");
      for (int i = 0; i < n; i++) printf("_{\square}%d", ex[i]);
71
      puts("");
72
73
   }
74
```

## 6.4 Suffix Array

```
/* Suffix Array, copied. */
 2
 3
   #define MAXN
                    (200010)
 4
   namespace mzry_sa {
 5
   int wx[MAXN],wy[MAXN],*x,*y,wss[MAXN],wv[MAXN];
 7
   bool dacmp(int *r,int n,int a,int b,int l) {
 8
      return a+1< n & b+1< n & r[a]==r[b]&&r[a+1]==r[b+1];
 9
10
   void da(int str[],int sa[],int rank[],int height[],int n,int m) {
11
     int *s = str;
12
     int *x=wx,*y=wy,*t,p;
13
     int i,j;
14
      for(i=0; i<m; i++)wss[i]=0;
15
     for(i=0; i<n; i++)wss[x[i]=s[i]]++;
16
     for(i=1; i<m; i++)wss[i]+=wss[i-1];
17
      for(i=n-1; i>=0; i--)sa[--wss[x[i]]]=i;
18
      for(j=1,p=1; p<n \&\& j<n; j*=2,m=p) {
19
        for(i=n-j,p=0; i<n; i++)y[p++]=i;
20
        for(i=0; i<n; i++)if(sa[i]-j>=0)y[p++]=sa[i]-j;
21
        for(i=0; i<n; i++)wv[i]=x[y[i]];
22
        for(i=0; i<m; i++)wss[i]=0;
23
        for(i=0; i<n; i++)wss[wv[i]]++;
        for(i=1; i<m; i++)wss[i]+=wss[i-1];
24
25
        for(i=n-1; i>=0; i--)sa[--wss[wv[i]]]=y[i];
26
       for(t=x,x=y,y=t,p=1,i=1,x[sa[0]]=0; i<n; i++)
27
          x[sa[i]]=dacmp(y,n,sa[i-1],sa[i],j)?p-1:p++;
28
29
     for(int i=0; i<n; i++) rank[sa[i]]=i;
30
     for(int i=0,j=0,k=0; i<n; height[rank[i++]]=k)
31
        if(rank[i]>0)
          for(k?k-:0, j=sa[rank[i]-1];
32
33
              i+k < n && j+k < n && str[i+k]==str[j+k];
34
              k++);
35
36
   }
37
38
39
   Suffix array 0(n lg^2 n)
40
   LCP table O(n)
41
   */
42
   #include <cstdio>
43
   #include <algorithm>
44
   #include <cstring>
45
46
   using namespace std;
47
48
   #define REP(i, n) for (int i = 0; i < (int)(n); ++i)
49
50
   namespace SuffixArray {
51
   const int MAXN = 1 \ll 21;
52
   char * S;
53
   int N, gap;
54
   int sa[MAXN], pos[MAXN], tmp[MAXN], lcp[MAXN];
55
   bool sufCmp(int i, int j) {
56
     if (pos[i] != pos[j])
57
58
        return pos[i] < pos[j];
59
     i += gap;
```

```
60
 61
       return (i < N && j < N) ? pos[i] < pos[j] : i > j;
 62
    }
 63
 64
    void buildSA() {
 65
      N = strlen(S);
      REP(i, N) sa[i] = i, pos[i] = S[i];
 66
 67
      for (gap = 1;; gap <<= 1) {
 68
         sort(sa, sa + N, sufCmp);
 69
         REP(i, N-1) tmp[i+1] = tmp[i] + sufCmp(sa[i], sa[i+1]);
         REP(i, N) pos[sa[i]] = tmp[i];
 70
 71
         if (tmp[N-1] == N-1) break;
 72
      }
 73
 74
 75
    void buildLCP() {
 76
      for (int i = 0, k = 0; i < N; ++i) if (pos[i] != N - 1) {
 77
           for (int j = sa[pos[i] + 1]; S[i + k] == S[j + k];)
 78
 79
           lcp[pos[i]] = k;
 80
           if (k)—k;
 81
         }
 82
    } // end namespace SuffixArray
 83
 84
 85
    namespace HashSuffixArray {
 86
    const int
 87
    MAXN = 1 << 21;
 88
 89
    typedef unsigned long long hash;
 90
 91
    const hash BASE = 137;
 92
 93
    int N;
    char * S;
 94
 95
    int sa[MAXN];
 96
    hash h[MAXN], hPow[MAXN];
 97
 98
    #define getHash(lo, size) (h[lo] - h[(lo) + (size)] * hPow[size])
 99
100
    inline bool sufCmp(int i, int j) {
101
      int lo = 1, hi = min(N - i, N - j);
102
      while (lo <= hi) {
103
         int mid = (lo + hi) >> 1;
         if (getHash(i, mid) == getHash(j, mid))
104
105
           lo = mid + 1;
106
         else
107
           hi = mid - 1;
108
109
      return S[i + hi] < S[j + hi];</pre>
110
111
112
    void buildSA() {
113
      N = strlen(S);
      hPow[0] = 1;
114
115
      for (int i = 1; i <= N; ++i)
116
         hPow[i] = hPow[i - 1] * BASE;
117
      h[N] = 0;
118
      for (int i = N - 1; i >= 0; —i)
119
         h[i] = h[i + 1] * BASE + S[i], sa[i] = i;
120
121
       stable_sort(sa, sa + N, sufCmp);
122
    }
123
```

```
124
    |} // end namespace HashSuffixArray
125
126
    namespace lrj_sa {
127
    const int MAXN = 1000;
    char s[MAXN]; /* 原始字符数组 (最后一个字符应必须是0,而前面的字符必须非0) */
128
129
    int sa[MAXN], t[MAXN], t2[MAXN], c[MAXN], n; /* n seems to be the length of s. */
130
    /* every charactor is in [0,m-1] */
    void build_sa(int m) {
131
132
      int i, *x = t, *y = t2;
133
      for(i = 0; i < m; ++i) c[i] = 0;
134
      for(i = 0; i < n; i++) c[x[i]=s[i]]++;
135
      for(i = 1; i < m; ++i) c[i] += c[i-1];
136
      for(i = n-1; i >= 0; --i) sa[--c[x[i]]] = i;
      for(int k = 1; k <= n; k <<= 1) {
137
138
        int p = 0;
        for(i = n-k; i < n; ++i) y[p++] = i;
139
140
        for(i = 0; i < n; ++i) if(sa[i] >= k) y[p++] = sa[i]-k;
141
        for(i = 0; i < m; i++) c[i] = 0;
142
        for(i = 0; i < n; i++) c[x[y[i]]]++;
143
        for(i = 0; i < m; ++i) c[i]+=c[i-1];
        for(i = n-1; i >= 0; --i) sa[--c[x[y[i]]]] = y[i];
144
145
        swap(x,y);
146
        p = 1;
147
        x[sa[0]] = 0;
148
        for(i = 1; i < n; ++i)
149
          x[sa[i]] = y[sa[i-1]] = y[sa[i]] & y[sa[i-1]+k] = y[sa[i]+k] ? p-1:p++;
150
        if(p >= n) break;
151
        m = p;
152
      }
153
154
    int rank[MAXN], height[MAXN];
155
    void get_height(void) {
156
      int i,j,k = 0;
      for(i = 0; i < n; ++i) rank[sa[i]] = i;
157
158
      for(i = 0; i < n; ++i) {
159
        if(k) k = ;
160
         j = sa[rank[i]-1];
161
        while(s[i+k]==s[j+k]) k++;
        height[rank[i]] = k;
162
163
164
165 |} // end namespace lrj_sa
         Aho-Corasick Automata
    //* Aho-Corasick automaton algorithm, by Abreto<m@abreto.net>. */
  1
  2
  3
    #define MAXN 500500
    #define NALPHA
  5
    #define FIRSTA
                    'a'
  6
  7
    /* pointer version => { */
    struct vtx {
  8
 9
      vtx *nxt[NALPHA];
 10
      vtx *fail;
 11
      int end;
 12
    } vtxs[MAXN];
 13
    int nvtxs;
    void myclr(void) {
 14
 15
      nvtxs = 0;
 16
```

17

vtx \*new\_vtx(void) {

vtx \*ret = vtxs+(nvtxs++);

```
19
      for(int i = 0; i < NALPHA; i++)
20
        ret->nxt[i] = NULL;
21
      ret->fail = NULL;
22
      ret->end = 0;
23
      return ret;
24
25
    void myins(vtx *root, char const *s) {
26
      for(; *s; s++) {
27
        int of = (*s) - FIRSTA;
28
        if ( NULL == root->nxt[of] ) {
29
          root->nxt[of] = new_vtx();
30
        }
31
        root = root->nxt[of];
      }
32
33
      root->end++;
34
35
   void build_ac(vtx *root) {
36
      queue<vtx *> q;
37
      q.push(root);
38
      while(!q.empty()) {
39
        vtx *p = q.front();
40
        q.pop();
        for(int i = 0; i < NALPHA; i++) {
41
42
          if( NULL == p->nxt[i] ) continue;
43
          if( root == p ) p->nxt[i]->fail = root;
44
          else {
45
            vtx *t = p \rightarrow fail;
46
            while ( t && NULL == t->nxt[i] ) {
47
              t = t \rightarrow fail;
48
            if (t) p\rightarrow xt[i]\rightarrow fail = t\rightarrow xt[i];
49
50
            else p->nxt[i]->fail = root;
51
52
          /* version[1] { */
53
          p->nxt[i]->end += p->nxt[i]->fail->end; /* update this sum, add its existing
              prefix to this. */
54
          /* } */
55
          q.push(p->nxt[i]);
56
57
58
59
    int qry(vtx *root, char const *s) {
60
      vtx *p = root;
      int cnt = 0;
61
      for(; *s; s++) {
62
63
        int of = (*s) – FIRSTA;
        while( p != root \&\& NULL == p->nxt[of] ) {
64
65
          p = p \rightarrow fail;
66
        if (p->nxt[of]) p = p->nxt[of];
67
        cnt += p->end; // correct when version[1] exists.
68
69
        // if version[1] not exists, you need to add all ends from this vertex up.
70
        //for( vtx *t = p ; t ; t = t->fail )
71
        // cnt += t->end;
72
73
      return cnt;
74
75
   /* } */
76
77
    /* -- usage (of pointer version) -- */
78
   #include <bits/stdc++.h>
79
   using namespace std;
80
81 | char S[1000100];
```

```
82
    char pat[64];
 83
 84
     int main(void) {
 85
       int T, N;
 86
       vtx *root = NULL;
       scanf("%d", &T);
87
       while(T—) {
 88
 89
         myclr();
 90
         root = new_vtx();
         scanf("%s", S);
 91
         scanf("%d", &N);
 92
 93
         while(N---) {
           scanf("%s", pat);
 94
 95
           myins(root, pat);
96
 97
         build_ac(root);
 98
         printf("%d\n", qry(root, S));
 99
100
       return 0;
101 | }
     6.6 Manacher
    |char t[MAXL<<1];</pre>
  1
  2
     int p[MAXL<<1];</pre>
  3
     int manacher(char *s) {
  4
       int i;
  5
       int sl = strlen(s);
  6
       int pos = 0, mxr = 0;
  7
       int ret = 0;
       t[0] = '^';
  8
       for(i = 0; i < sl; ++i) {
  9
         t[i*2+1] = '#';
 10
 11
         t[i*2+2] = s[i];
 12
       t[sl*2+1] = '#';
 13
       t[sl*2+2] = '$';
 14
 15
       sl = sl*2+2;
       for(i = 1; i < sl; ++i) {
 16
         if(i <= mxr) {
 17
           p[i] = min(p[2*pos - i], mxr-i+1);
 18
 19
         } else {
 20
           p[i] = 1;
 21
 22
         while( t[i-p[i]] == t[i+p[i]] ) p[i]++;
 23
         if(i + p[i] - 1 > mxr) {
           mxr = i+p[i]-1;
 24
 25
           pos = i;
 26
 27
         ret = max(ret, p[i]-1);
 28
 29
       return ret;
 30 |}
```