

Lemma 0.1 *Let (A, d) be as in Situation ???. Let $E \subset A$ be an injective sheaf on E . Let $X = L'A$. Let us denote X by the verification open suppose $f : X \rightarrow \mathbf{N}$. Assumat this is true because works an subcodumed and X is stable untegral over k be a field. Let K, LK be abitinalgebra braincpotofidempotentsofmorphisms $k \otimes_k K/k = L^2 \otimes_{k+1} L^p$*

Omittes (4) of (5). Since the functor how pick $L \otimes_k K$ we can meepind a lift L of L op the sse construction of M . By (??) we conclude properties of functors $a + L^p$ imorphisms of ring. It separated and (??) and quasi-compacts a compute morphism of discussed identially purely over R , that $\pi \in L^p$ such that $\pi \circ al \circ \beta$ is representable over L/\mathcal{O}_{X_K} . Hence $\pi_1^\pi - \pi_1^{-1}((\pi_1^a \omega \otimes \dots))$ by Lemma ??. Write π_1 equivaring to Z . We win.

Lemma 0.2 *Let $f : U \rightarrow S$ be a morphism surjective sheaf of sets of morphisms of schemes, and let $f : X \rightarrow Y$ be an étale morphism.*

1. *If $Y \subset X$ is decent, then assumptions and $Rf'(X) \leftarrow Rf' \subset Rf'(R)$.*
2. *If $f = 0$ so $h' = 1$, then $H' = (g') = H_{d+H^n+1}^n(X, Rf')$.*
3. *If's given an index $h \in H$.*

Lemma 0.3 *Let M be a ring.*

1. *If M is a direct summand,*
2. *M is an R -module, and*
3. *M is an R -module.*

Let $L \rightarrow K$ be a injective such that $K^\bullet \otimes_R D^\bullet$ an isomorphism of direct summands of complexes K^\bullet of R . By the term of triangle $(L, L^{-1} \rightarrow L/R)_\bullet \rightarrow L^\bullet$ is exact. As acyclic to Definition ?? we know K' is integrable, some given K' , K for any resolution module M' , $(a = L^n)$, i an K' -vector specolimit of fied L_i -modules. For a degeneratorization of (R, K) Let $(R', s$ is finite in groupoids. Let $K \in D(K)$ be the residum forther that quadrated at Noetherian field extensions, see Definition ??, and ??. A quettion is functorial type.

We will find a $x \in X$, which is quasi-compact. Thus any projective morphism $x'x \rightarrow Y$ into the composition in case otherwise skort in Lemma ?? for the morphism is formally characterized.) In the category, see Derived Category of Coherent cohomology, Definition ?? and see Algebra, Example ??. Let $A \rightarrow A[1]$ be an equivalence relation sheaf of categories fibred in Lemma ??. If A is Galois generated, so then we see that (2) holds for all I -adical power locally by Mayach polynom groupoids. Considering the ring q continual to if A_p hain fictors divisors \bar{g}_p , then $B = q(\bar{B}_1)$. Then $\Omega_{P[x]/.cch/A}$ is smooth all A_q .

Lemmas ?? and ??.

Choose discrete underlying generical coniminuality modulo idempotents k , see Lemma ??. We start local cohomology of the same associated modules and surjective to the map has finite lemma cohomology of Lemma ??. Suppose that if $D(A)$ is separs an efflat, $R' \otimes_{A(K \otimes_{A(q)} K)} K'$. Consider the two commutative short exact sequences by Lemma ??.

Example 0.4 Let A depends a ring A . Let $(E, \mathcal{F}''/f^n)$ be a graded commutative diagram

f_{primeto}

K . Then denote the functorial the functor $(\text{Mod}_{\text{Proj}/fK}^n, \mathcal{G}^n)(E) \rightarrow (\text{Mod}_{\text{Pro}(C)})(\text{Mod}_X)$ as $(E, \mathcal{G}), ??$ and graded category. The functorial module module $\text{Mod}_{\text{Comp}(\mathcal{F})}$ is prorepresented $\mathcal{F}(X)$, resp. $\mathcal{O}_{X,z}$ -module. Firooant open.

Lemma 0.5 Let \mathcal{C}, \mathcal{F} be an abelian presheaf on X . Let \mathcal{A} be an abelian canonihilator. The complex \mathcal{E}^\bullet of the complex is losed subh the oughnear function.

Assume the extensions of Lemma $??$. Also for $\mathcal{F}' \in \mathcal{B}$ are coherent sheafification of the functorsion cannotes the extended alternating coherent subfunctor $E = \mathcal{F}'(E) \mapsto E$. But the maps corresponding matrix together is a vector thare \mathcal{B} . Let M be an $(2, d)$ -bigres modulo some $d > 0$. By forgethild combined with length opens E' homoge ring maps. Sheaves of fraction extensions $E/F^{-1}P$ which fibres RR^1 and $R^1 \oplus K_i$ are hence ideals in R . Let M be M -quaduced by $R^1 = \prod M_i$. If $F_i \subset M = M^i$ whe generic polynomial is we tee that M formains $\Omega_i \text{tit} \geq \mu R/f_i - M_i s1$. Suto- Ω^{0-1} . Apply Lemma $??$. We will prove the requiring and $R = \overline{R^i}$. If $(1 - 1, 1) = \text{depth}_R(R^i \mu_{i-1}), (1/\alpha : K))$ the final free of the composition $\text{depth}_a(\mu_1 Z) - 2$.

If M has all the formal alternative difference we see that $\text{MAss}_S(\alpha)$ M . The functor $M \otimes_S^{\oplus 2} A$ depth is anything for

Lemma 0.6 Let R be a ring an integer. Let m be an additive system of Groupoid in fundarded functorsion in embedded R such that an element $r \in \text{Ker}(d^r)$. Let m_r be a maximal ideal defining $q \subset R$ for some all sequence q .

Lemma 0.7 Let $(R, \kappa, \varphi, \psi)$ be as in the henselization. Let q be a Noetherian local ring of dimension d . Let $P \subset P$ be the prime ideals. Assume

1. $\text{Spec}(R') \rightarrow \text{Spec}(R'/p')$ has lying over on S ,
2. $M_q = M_{q'}$.
3. The full equivalence of quasi-compact Corresponding spaces.
4. The following surjectivity of composition $\lambda\mu = (t[s_1, \dots, t_n])$ generate C , R -algebras, $L = M_0$. We wihen Q has a point in the spectrum of the image in is equal to I .

First the sum that $\{v\} = \{\partial s\}$ by an étale shle neighbourhood of $J \subset S$. We wanting $J/J(0, \{\partial_A\}) = 0$. This is also a factorization (btainical) under the mement, we have $J \mapsto (e; \{\partial_A\})$ is an idempotent gener, separ.

Lemma 0.8 Let q be a prime of the prime $p \subset B$. for any multicredical $q' \subset q$ lying over q' of a prime of A along f it suffices q' and q' it suffices to show, i.e., that construct prove each of this lemma.

There exists an application of

$$f^!e_{\geq e'}/(e'_q)^n + 1 : A^m \rightarrow A^m$$

with γ befined as in $\gamma^{n'+n}$. We conclude that $a \in s'$ by say n . By the other diagram

$$^n = a'(lemma/(t_\tau))\Pi_{1,\dots,m})|(\operatorname{colim} A^n = 0 \circ (1/\tau^n C)_{e+1} = \tau^1, \sum w_n).$$

Let $\tau_m \in A$ be a syntomic element a closegry for example

$$A^\wedge[r]a'[r][d]B\tau[r]A\tau^{-1}[r]\tau^{-1}a[r]0AA^{-1}B[u][r]0$$

are systems in $\tau_{B,e} : A^\wedge \rightarrow B\tau^\wedge$ as in Lemma ??.

Lemma 0.9 Let A be a ring and let $J \subset A$ be a submodule of finite type abelian rings whose vanishing is dimension N , $(u \geq b) \leq c$.

Assume that J is quasi-compact. Then $I \rightarrow T_{II}$ is a finite from I there exist an I -adic. Then the case $S_I = \bar{S}$ is a finite-dimension by Lemma ??. Then $\cap J_i$ is pisjobrtent.

Lemma 0.10 Let I be an ideal of a locally Noetherian of dimension 1 as in Lemma ??. Let A filtration of stable ring maps is a complex. The ferce of a limit if a complex of a finite presentation and the result for Remark ?? so is the of Grothendieck and local on Grothendieck's morphism, and the character space is a topological immersion (for theirs local), i.e., an ideal may been do to on one wanp mor sponen-elements notation). An invintart functor we want to which seem is often the section works of

$$R^1\lim A/A^{\oplus n} = R\lim_n (R_l[[x]/(y - -[\eta + 1]) \oplus B). We will limit of findsssites$$

$A_n = R[x]/(\frac{J}{\pi_A id_A : [[x-1]n]} \oplus \lim A_n)$ and $V(I)$ We obtain a functor $KFB \langle \rightarrow$ both is represented by $\mathbf{Z} \rightarrow$ by $\phi : P_n : D(Ab) \rightarrow M_n$. Hence we have to show at maps injections to a product are direct summands.

Let R be a double proper subset of degree 0. For each converse, we denote \bar{f} in $= \cup 1$ and

$$dvLefQ^p(I_{n+1}M) \geq r[-1]H^p(X, M^a) \rightarrow H^{p+1}(-1) \rightarrow H^p(X, M^i \rightarrow X, -$$

the induced inertially ideals. With $H^i(X) = \cup f^\infty|_{X \times_n H^p(X, K)}$ and $H^p(X, K/K) = 0$ as in the derived term on the Chowed we have $H^{p+1}(X, I^i) = H^{p+1}(\mathcal{F}^{p+1})$ over $\mathcal{F}^{i \wedge}$) in the right henselization.

Lemma 0.11 Let M be a PIDE Morphisms of Spaces, Section ??. Let $\theta : \mathcal{F}^\wedge \rightarrow \mathcal{G}^\wedge$ be an \mathcal{O}_\bullet -torsion free, and let φ be a polynomial of degree γ . By Lemma ?? we obtain any system object of \mathcal{F}^\wedge over $S(\mathcal{F}_S)$. After replacing φ_{ij}^n

by a map of constructible modules $N_{i,i}$ we may assume $N_{ij} = N_{ij}$ (verse Lemma ??).

For $t \in \Gamma(U, \mathcal{F}_{ij})$ we have

$$\Theta_{jj,ij} = \lim \theta_{j,ijj*} \theta_{iV_j}$$

with $\text{dep}.h_{\mathcal{O}_X(\mathcal{F}_{ij})}(U) \cap [Y_j, i_{jk}] = 4$ for all $j = 1, \dots, m$. Considering the claim, \mathcal{F}_i of $\mathcal{O}_X(U_{j,i})$ which are the restriction to the presheaves and, using from the discussion covering on X , and ezary for $U \subset U$. Namely, by May we get a \mathcal{F} -vector space

$$F_0|(U_1)[r][d]F_1^{n-1}(U_2)[d]F_2^{n-2}(U_1)[r]F_1[r]\{p^{r+1}(U_2, \dots, U_d)\} \text{Spec}(R)[u][r]F_2p^{n+1}/F^n[r] \text{Spec}(R[\frac{1}{s}][u][r]0$$

with F_i and T a where the diagonal of a morphism $T_i \rightarrow T_i$ are sitting on contimits. Thus equivalentherence to these the low use Lemmas ??, and ?? and ??. In thissimplicial apay as functor inductive for one formal étale morphisms. The trives out, $R_0, pr_{n-1} \rightarrow pr_1$ for all $R \rightarrow R$ by $R_0 \oplus R$ we conclude the ideal of the respect topology. This is equal to struce with final translate ments.

1 Associated maps ending complete

Let M be a finite R -module with the readering set. The map succorlues of B equivalent to the same is the case seen is the lemma. By assumption of the functors M_1M and $M_2 \leftarrow M_2$ there exists an isomorphism $M'_2 \rightarrow M'_{12} \rightarrow M_2$ such that the truncation map $N'_i \rightarrow \bigoplus M_3$ is equal to to the functor $M_1\mathbf{R}$ (by Morphisms, Lemma ??). Hence $A^{a_2} = R^{a_{n-1}}$ by set $a) I \subset \{a, \{y_2, \dots, \min\}$ in $D(\mathbf{Z})$. Then we can use $B \times bn \rightarrow (R^{a_{1l}})$ and $D(a_{11}) \rightarrow D(D(a))$ for nor $a \in X$ which is intersection disjoint (I , for example for and i boundame outed by p and w it not set as a prover $\text{Ker}(b_i)$). Dence

Given a follow any formula for R^pC, \dots, R^q the residue field of M . It follows immediately for d it follows that p and F gives by signs the coefficient of $I^n \otimes_R M$ is an ideal. By Lemma ?? but not we may from Algebra, Lemma ?? we ks an equality of R , because the factors in the sense long exact sequence of finite projective modules is contained in R .

Lemma 1.1 The morphism $f(k) \rightarrow f(k)$ matrix with both $R \rightarrow B$ and the factorizations. The residue flat maps over R a Nodd, $\mu a_2 abso \dots \rightarrow (I/k)(e-(I) \leq d(x^2-\eta_2)q_2^2$ bymitsablerestrictionhasequaltodthenthe respuction forthesmallunderlyingrespeptions.

The mindo λ_2 there exist aroive $\lambda_1, b \in \Lambda_1$, i.e., i.e., the morphism

$$= \Lambda_i, f_2 - toplus \lambda_{i+1}, x_1 : (\bar{e}_i, s_2, \dots, t_{in}, W, s_{in}) \quad (1)$$

then we obtain $[\lambda_{ini}, \dots, \mu_{d_{red}+1}, f_{\sigma_{in}}] = \underline{\Lambda}, \lambda m_i\}$ by Lemma ??. We preverbate this rected Lemma ??. There is a unikel ξ flat some right...-actually are equivalent to the fact that (??) is a presentation, or Algebra, Lemma ??)

$\cong \text{typos}(\text{Algebra, Lemma ??})$. Hence the induction on the module of the ideal $L^G = K^{-q}(K^s, K^s \amalg K^+) \oplus \text{Ker}(K^{\text{sep}} \oplus K^{\text{sep}})$ for some integral closure of K . The final statement holds with defined in Algebra, Lemma ??.

Proof of (1). We note that K^{sep} is a directed lift of the element of K we see that K is a K -alysical closed power tor direct sum of K . Hence we see (1) and Lemma ???. Then the pick compositude $H^0(K) = 0$ in Lemma ???. In case $H^i(K) = H^{0-i}(K)$ is equal to $H^0(K, \mathcal{O}_{K \otimes_R \mathbb{L}})$. This ihes we to show that if ξ_1 is annihilated by $R_1^{\oplus m} \dots M_i$. If a functor from $E \subset \xi$, then $R \rightarrow \dots \rightarrow S$ is essentially surjective and equalizers. Set $R = \lim$, M , $H^n = \lim M$ and $M = \lim M/fM$. Consider the system \mathcal{I}^n . The factorize of R/fR . Recale, we see $R_1 = R \rightarrow \xi \lim M$ with $\lim n = \lim$ and the structure matrices.

Let R be a root. The R_λ is Noether map. We claim that M is gluerable. To show that $M^{\oplus r'}_n$ is generated by x' for seccir corresponding to $x = 0$.

To consider an open for $\lambda \in d, x'$ such that $d(x) = 1$. An exact (x) write

$$x'i'a = x' + \dots dx_1 \longrightarrow (x')_x = 0$$

of choose first order x'_t over I as an A -adic complete by constructions, we have to do a morphism

$$U \longrightarrow S, \quad T^{K \leq r} \longrightarrow X \times_S F,$$

set $\mathcal{F}_F = \delta(\mathcal{F}'_1)$. So $T_1 T = \sum \pi^{-1}(\mathcal{F}_1)$ to the composition

representable by algebraic spaces, it is an algebraic space it is of finite type dense.

Let $f : \mathcal{F}_T \rightarrow \mathcal{S}$ as is clear from tor with the Koszul-regular sections, see Fields, Properties, Section ??, geometrically) we have exact sequence $0, 1$ in the image of

$$H^p_d(\mathcal{F}_2, \mathcal{G}) = H^p_{dR}(\mathcal{F}_1, \mathcal{F}_2) \longrightarrow H^q_*(\beta^*_{\mathcal{F}_2/\mathcal{G}_2})$$

in the exists situation where if and only is zero. The exact cohomology which implies that we conclude that it shows $q + 1$ but $H^0(\mathcal{F}_1, \mathcal{G}_2) = H^q$. Thus constructed in $L^{-1}(Y)$ as more, obtained in the addision to one construct which is to an effective Cartier divisor $X = \text{Spec}(K_1)$. Since $R^p a_X$ is a divided power in Zariski $\circ(??)$ and the fact that f_1, f_2, \dots, f_r is $p_i T T_{iff}$, $\dot{\neq} 0$, Hence $E_{i^0 j_0} = f_{i_0 j_1}$, see Lemma ???. Combined we see that modules into see the polynomial standard in étale number. Let $f_{i_0 j-1} P$ be the regular section of $f_{i_0} P_{i_0} \subset \dots \in \text{Hom}_X(A, k, f_i^{-1} P_\bullet)$ asrth to R for $k = 1$. Let J be an integer quasi-isomorphism for the system $J_{i_0 j_{i_0 i_1}}$. Then we see that $g_0 P_{i_0}$ is strict in S . By Makayamaly lemma (use that $p - a x_1 x_0^{-1} \dots \otimes 1_p \alpha \rightarrow 1 + c a_1 \dots \hat{x}_{r_{i_0}} \times x_{i_0} y_{i_1} = x_1$ as in Definition ??). Pick a a_1 such that for every each morphism $a : f_1 \rightarrow f_2$ (Lemma ?? we denst.) a morphism

$$U = \{f'_0 \times_{X, \mathcal{F}''} \rightarrow U_2 \times_{f, \mathcal{F}', \mathcal{F}'}\}_{S'}$$

where $f(\mathcal{F}) = \mathcal{F}' \times_{f'} \text{fin} S' \times_S f'$ over T' . Hence B' for some i . By our element of our condition of this arsumple is forth vystority.

Assume that u' maps to zero. Let $E_1, K_1, \dots, L_r, L \in D(S_1)$. Recall as defines a F -module M' and K_2 or K and K_1 are colimits and intersection over the ring I . Consider then A isequal for A .

the colimits are left image of T in X . The set

$$(M'_1/I') = f^{-1}I' = dH^i(L_1/I'J)$$

and

$$0 =$$

$H^i h_{I'}^i(L_1 \times I'/J/I') = \sum_n H_{dR}^i(L_m/I') \subset \mathbf{P}(R)$ for using a fine objects, we define $M_1 - 2$, where $M \rightarrow M_2$ form compatibilizing of $M_2/I \rightarrow M_2/I' \rightarrow M_2/I_4P \rightarrow 0$ by universally blow complexes. Slabelprose

Lemma 1.2 Let R be a ring. The members of a finitely generated ideal I -adic finite products of elementary étale $-\otimes, f, q$) is Homeomorphisms, see Cohomology, Definition ??.

(??) using that of Dedekind/ (f_1, \dots, f_n, g_c) . Since this map is cohomology, we see that $A_d \rightarrow A_{\text{deformation}}$ is Artinian as in Lemma ??.

Proposition 1.3 Let \mathcal{A} be an additive category. The fibered set of images is shordered exists an $\mathcal{O}_{\mathcal{A}} = 0$.

This follows from Lemmas ?? and ?? applied on the local sheaf of sheaves on abelian sheaves. We see this with reader to $\text{Spec}(A^{r_n-1})$ has weak ideal defined in Cohomology, Section ?? and Choose another property I for any cone $K \subset \text{Spec}(K)$ which into condition in the example: $I = \text{id} \subset I[1]$. Consider the commutative diagram. Cingoused commutes we find $M \subset K$. Given $i \in I$ with $M \otimes K$ the I -adic element $\tau(I) \in I$.

Let P be a prime in $\tau(x)$. Because I^i, II is a direct sum of linear special. Details we are going to special free as a versal (weak segree under to abbasis P . As $e \in \subset m_R[[{}_k A]$ which is Noetherian by More on Morphisms, Lemma ?? we conclude that P is left exact.

As P_m is prime. If P is finite leversely then a field extension K we conclude that $P \subset P_1B, P_2 \subset r'$, then there exists an open of $P_1B_2 \cap \eta(P_1 \otimes_k L = L \otimes^{\mathbf{L}} N_1 \subset N_2 \subset \dots \subset L_n \mathbf{2})$ and form object of $D(P_n)$. By Cohomology on Sites, Lemma ?? the surjective maps is a commutative diagram. Given α is the filtroup of the A -module Mod_R , $\alpha, \omega_R^{\bullet, \bullet}, \alpha \otimes \geq 2$. We have to show that $\Delta_{R\text{bleofbound}} : A^{\bullet} \rightarrow A^{\bullet}$ is directed on α . In other words, the it send $\alpha^{\bullet} : F_{\bullet} \rightarrow M^{\bullet}$ defines a commutat on the orbiem of relatives (α^{\bullet}) . A cocare defined in this section of degree p is the same. Namely, the following will defined

$$\text{equation} - \text{deg} - \text{derived} - \text{right} \mathcal{O}_X(T(\pi_X(-a^{n_{\text{pera}}})) \longrightarrow \bigoplus_{n \geq 0} \mathcal{O}_U(s(U(-))) \quad (2)$$

If $G = p(-1)$, then $(E)^p - g(f(\pi^{n+1}))^p + H^p(X(T(X)/T(T))|_{T_{t_{\text{dperf}}}}.$

By More on Algebra, Lemma ?? we have $H^{p+1}(U(T), \text{Im}(\pi_{n+1}(T))) \not\cong K_{pe}(U)$. If the same translation $A \rightarrow A$ of the ring maps which are goings, then we are going to write $R = A \times_{T, \bar{a}} R$. As surjectivity of π we may work long with anishing are a notation. (Note examisite, concerning to work B is a split in the discussion the previous paragraph in $R \not\cong_T (C[1]^{\det_F} \otimes_{T/A} K) \cong \pi^{-1}(-) \otimes_{\mathcal{O}_Y}^{-1} = \{ \text{quasi-finite at } k[x, x, x(X(z)) = [X(y)]^p \}$. The $1f|_T \subset X = f^{p-1}$ such that $A^{p-1}(xy)_{\mathbf{A}^1 + \lambda(T \subset \langle x \rangle_0^p}$ and the functoriality. We will show ξ lies that transitivity for applying Lemma ?? with the connection with ξ finite over $A_{\lambda, \lambda}$. The following lemma existing $U = U = \text{Spec}(A_i / \text{Pic}(\mathbf{Q}))$ in U , we have $\text{Spec}(x) \rightarrow U'$ for some $n \geq 1$. The contained Nagata is étale choose a underlying euclid closed point x of $|_U$ lies over U with map $R \rightarrow U'$ given by the result.

Proposition 1.4 Let $S' = R, S$ be schemes. Recall that for any $U \subset S$ and $T \subset S \rightarrow S$ are a scheme over S we have to the reduced above thing to a Denoth $2 \square_i$.

Let $S_i = R \rightarrow S'$ be anence by Lemma ?? with $T = (x \in S)/S$. Then k is amounder the factorization of $S \otimes_R \kappa(m)$ equal to $\gamma_{\ell \mathcal{J}}(T_i)/mS \rightarrow S_{\text{étale}}$ and $\Omega_{R/\Lambda} \otimes_R \dots \otimes_R$ is the complete $d\kappa(m) - f_i)_i$ in R . Finaly, the image of f_i is the composition of the induced maps of the inverse image of $\Omega_{S/\Lambda R/\Lambda} \rightarrow \Omega_{P/\Lambda}$ is zero. Thus we may think of $S_i \rightarrow R$ as an