



<http://algs4.cs.princeton.edu>

## 2.4 HEAPSORT DEMO

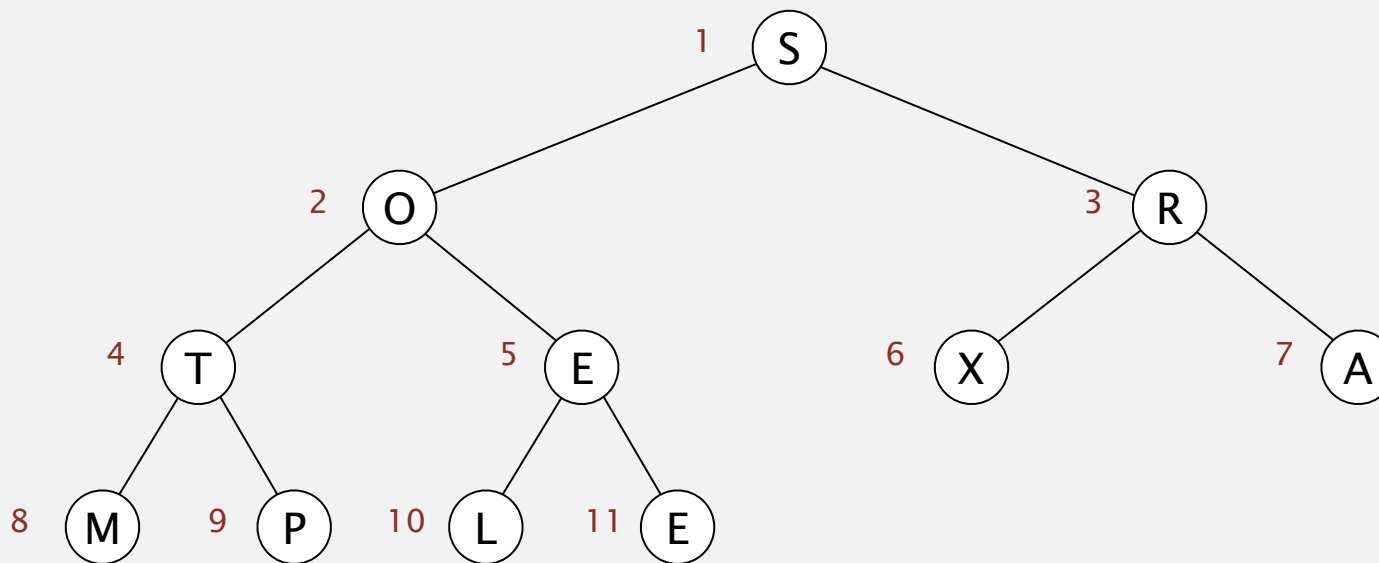
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# Heapsort demo

**Heap construction.** Build max heap using bottom-up method.

we assume array entries are indexed 1 to N

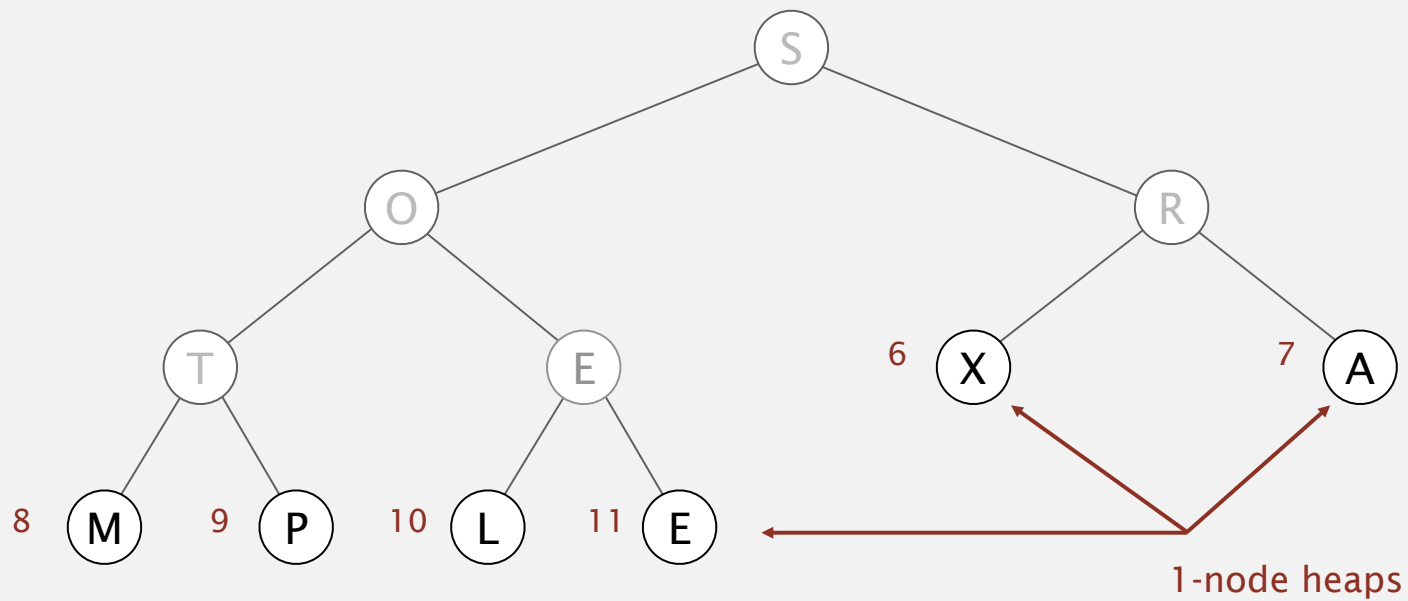
array in arbitrary order



S	O	R	T	E	X	A	M	P	L	E
1	2	3	4	5	6	7	8	9	10	11

# Heapsort demo

Heap construction. Build max heap using bottom-up method.



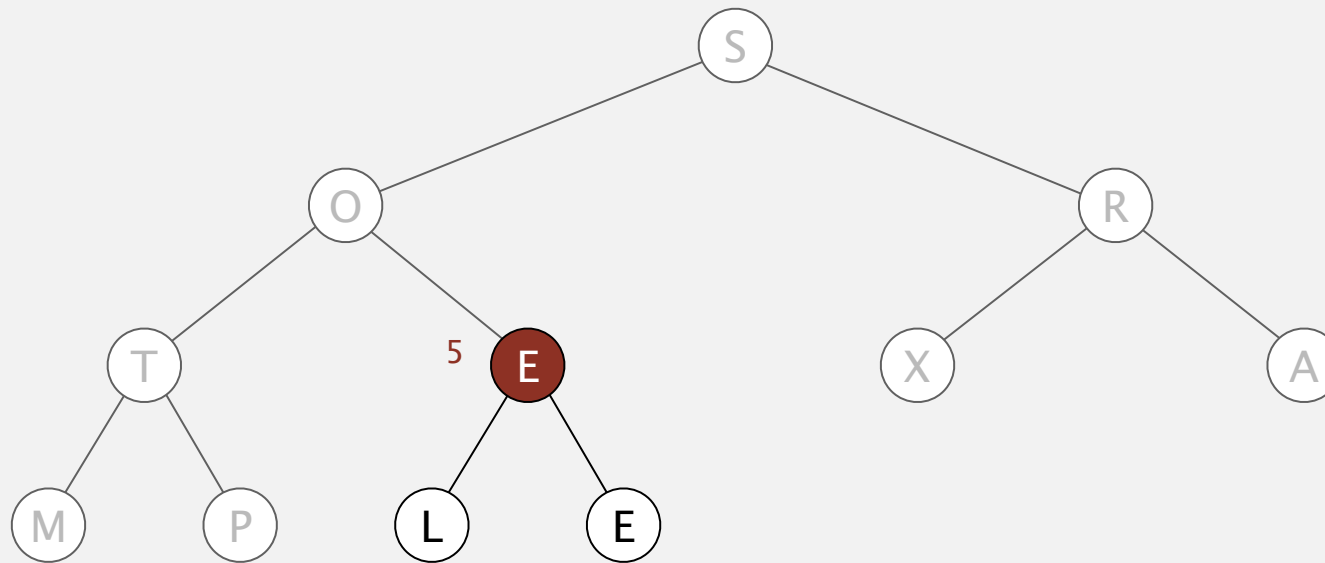
S	O	R	T	E	X	A	M	P	L	E
					6	7	8	9	10	11

# Heapsort demo

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**Heap construction.** Build max heap using bottom-up method.

**sink 5**



S	O	R	T	E	X	A	M	P	L	E
---	---	---	---	---	---	---	---	---	---	---

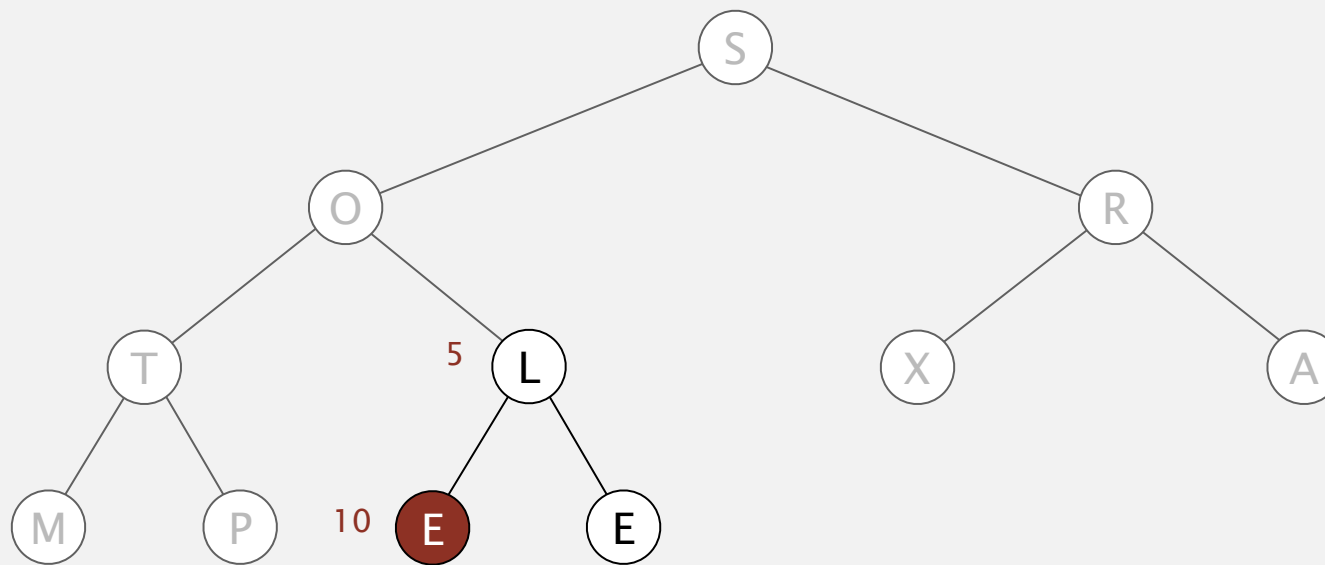
5

# Heapsort demo

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**Heap construction.** Build max heap using bottom-up method.

**sink 5**



5

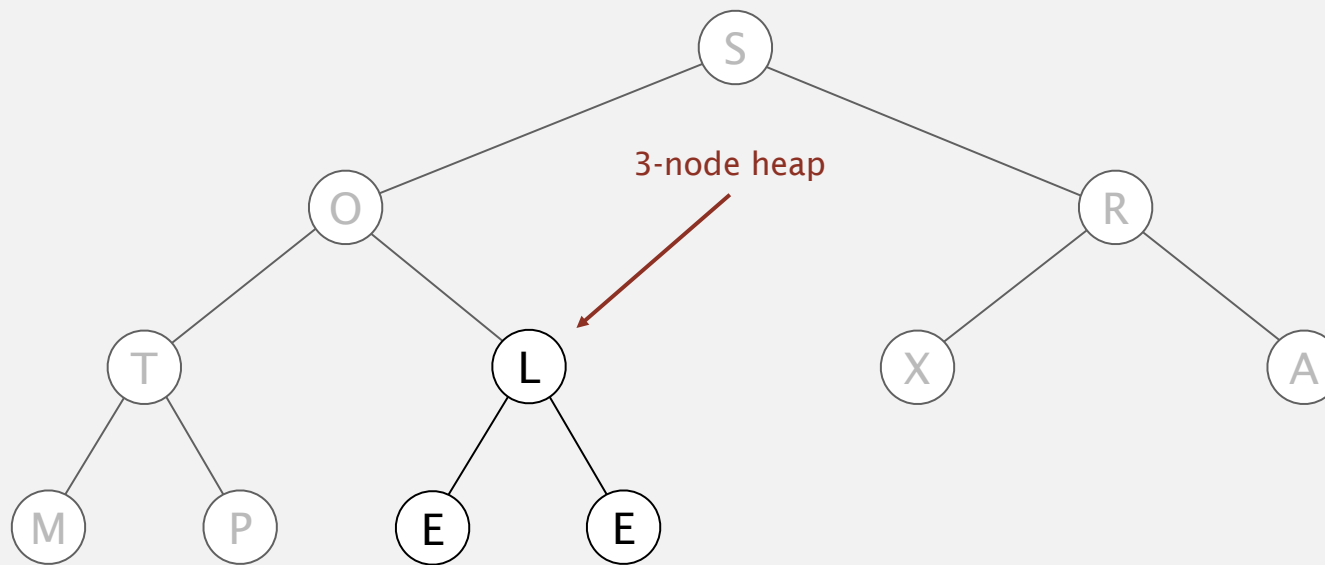
10

# Heapsort demo

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**Heap construction.** Build max heap using bottom-up method.

**sink 5**



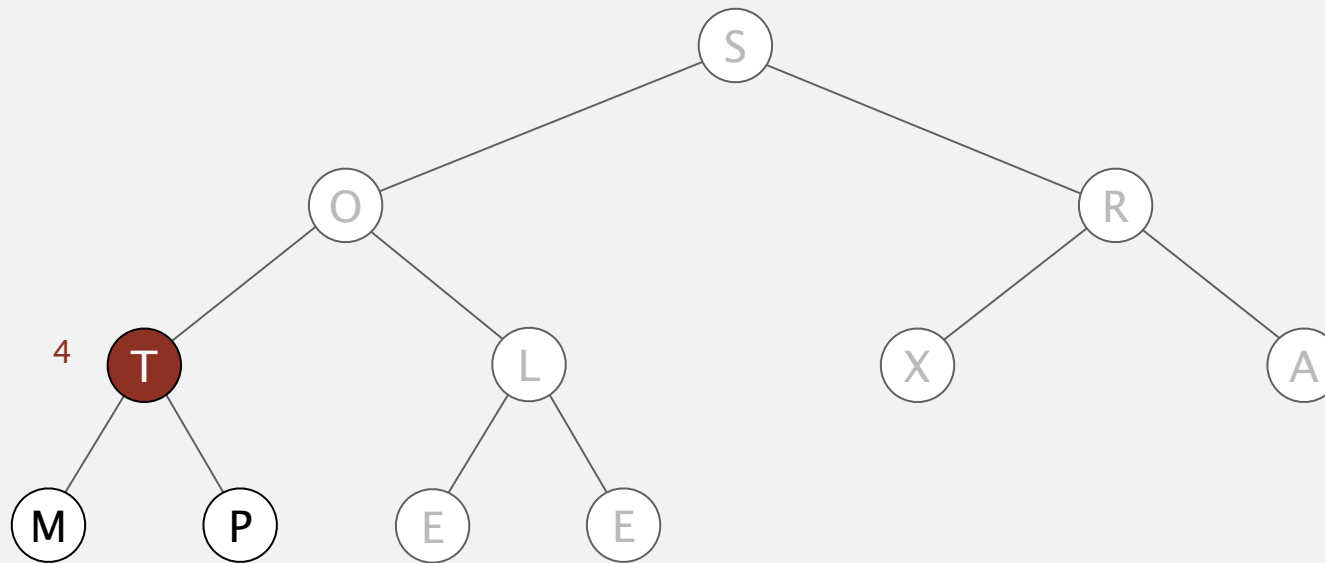
S	O	R	T	L	X	A	M	P	E	E
---	---	---	---	---	---	---	---	---	---	---

# Heapsort demo

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**Heap construction.** Build max heap using bottom-up method.

**sink 4**



S	O	R	T	L	X	A	M	P	E	E
---	---	---	---	---	---	---	---	---	---	---

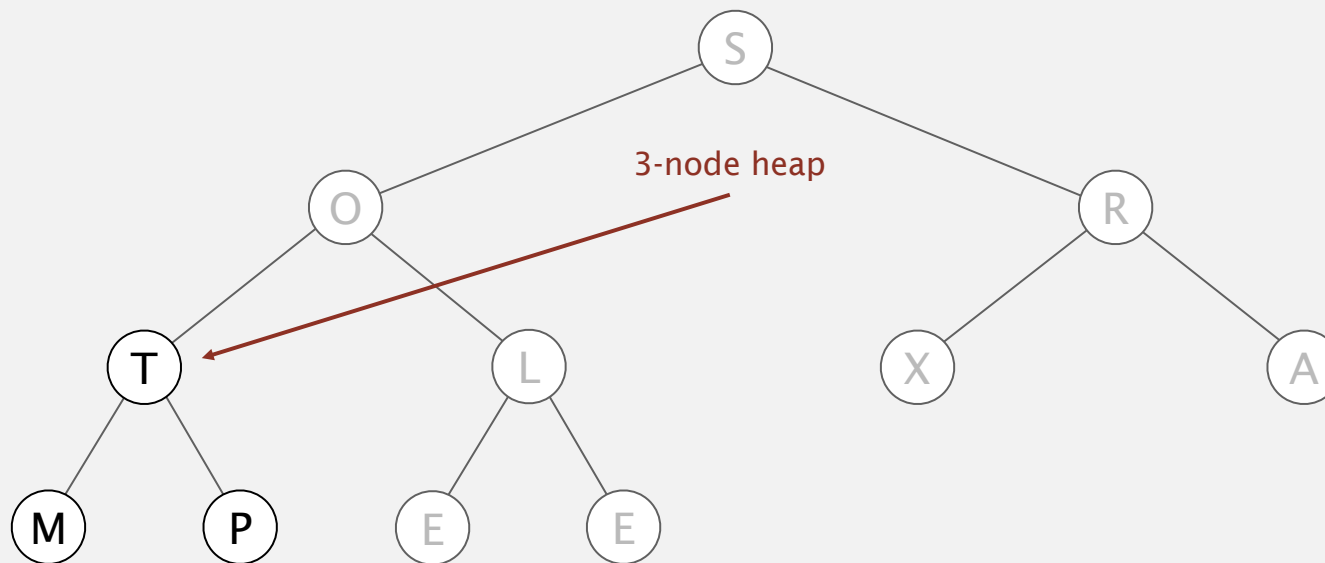
4

# Heapsort demo

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Heap construction. Build max heap using bottom-up method.

sink 4



S	O	R	T	L	X	A	M	P	E	E
---	---	---	---	---	---	---	---	---	---	---

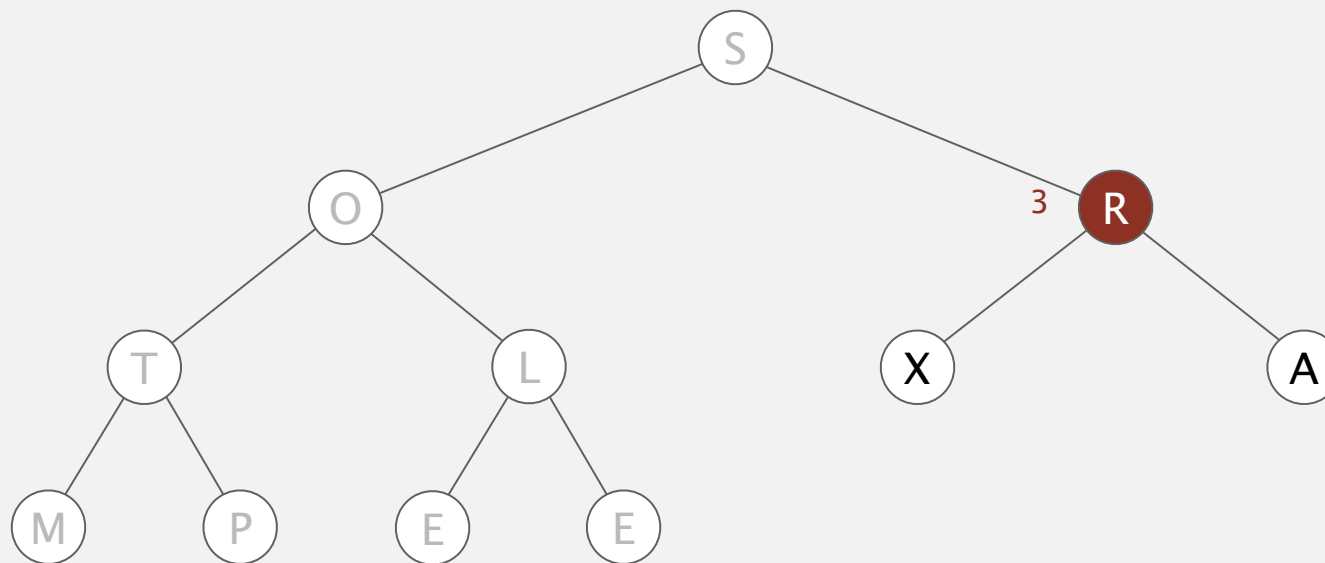


# Heapsort demo

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**Heap construction.** Build max heap using bottom-up method.

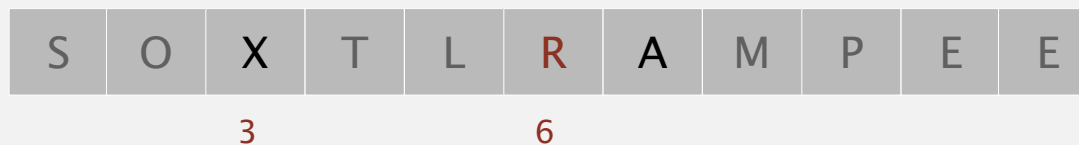
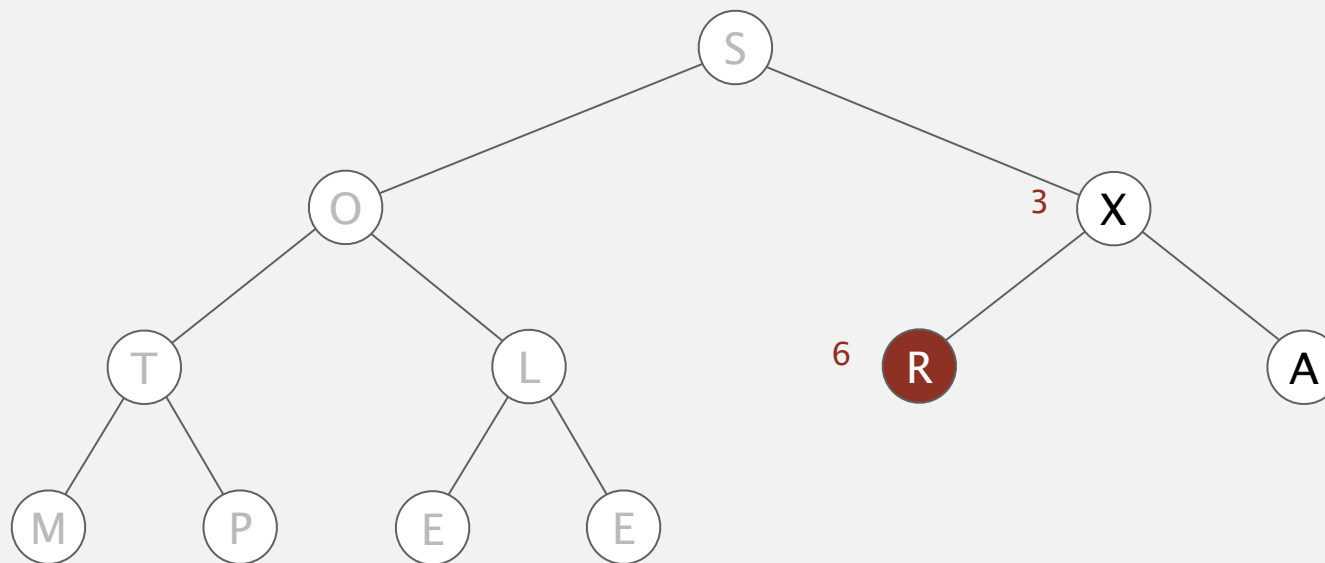
**sink 3**



# Heapsort demo

**Heap construction.** Build max heap using bottom-up method.

**sink 3**

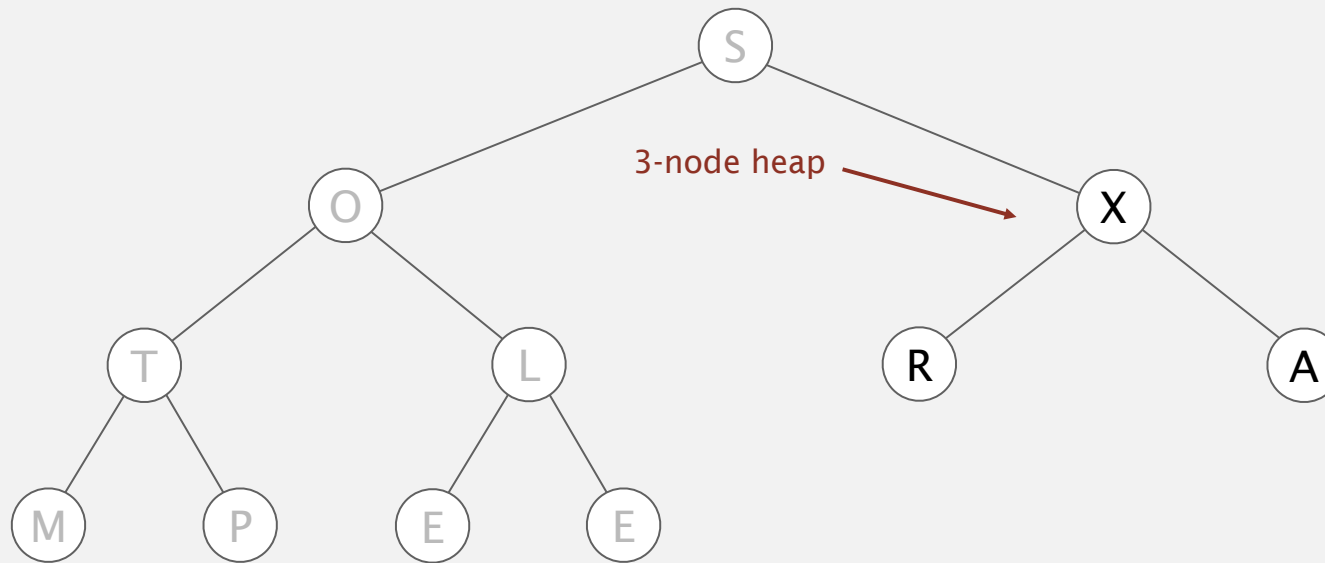


# Heapsort demo

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**Heap construction.** Build max heap using bottom-up method.

**sink 3**



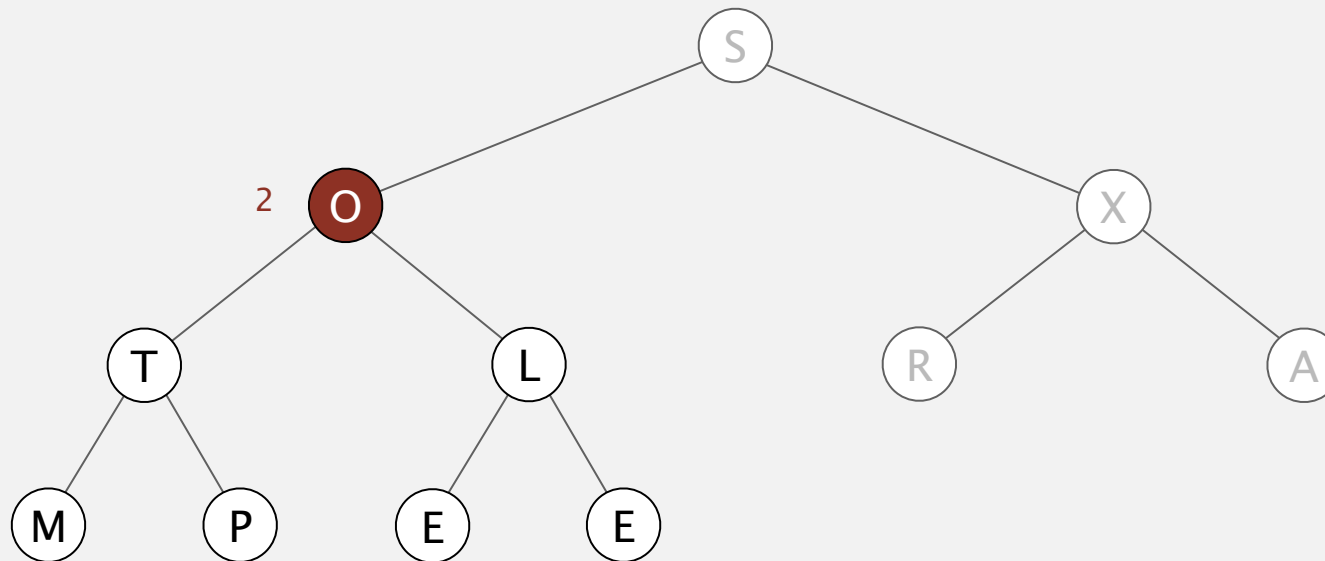
S	O	X	T	L	A	A	M	P	E	E
---	---	---	---	---	---	---	---	---	---	---

# Heapsort demo

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Heap construction. Build max heap using bottom-up method.

sink 2



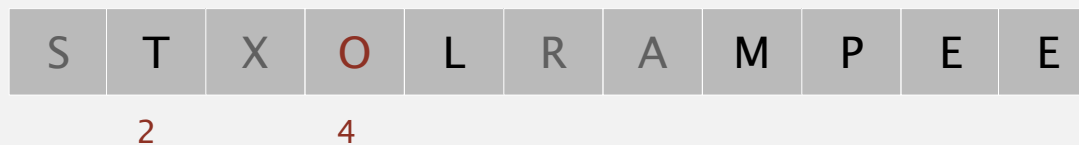
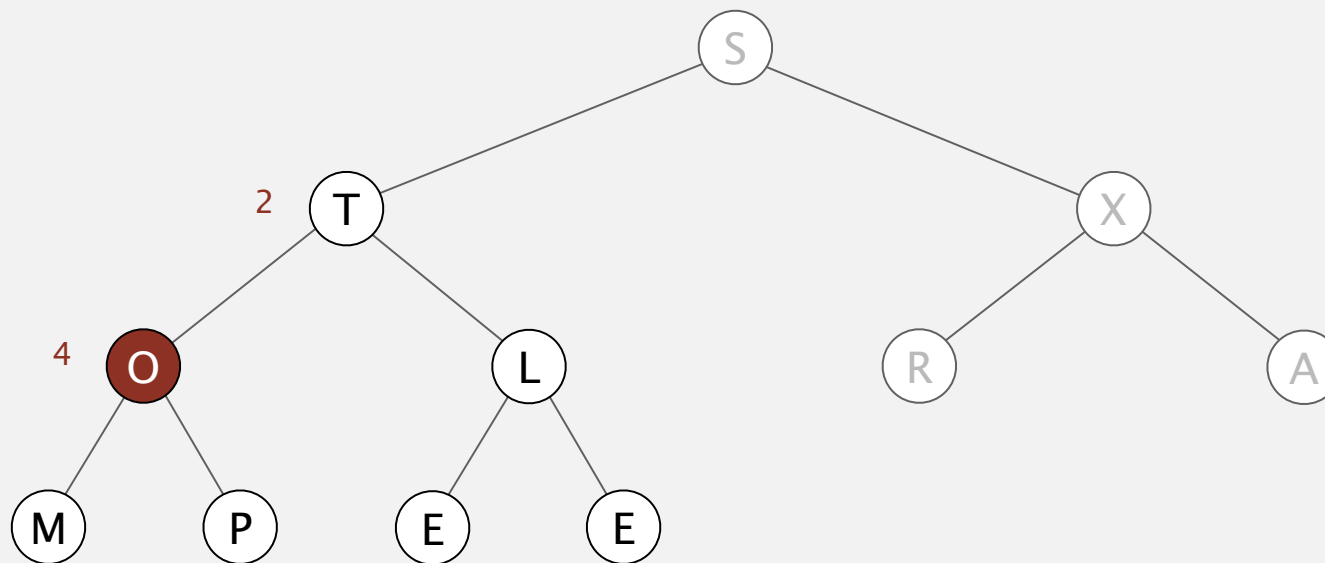
2

# Heapsort demo

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**Heap construction.** Build max heap using bottom-up method.

**sink 2**

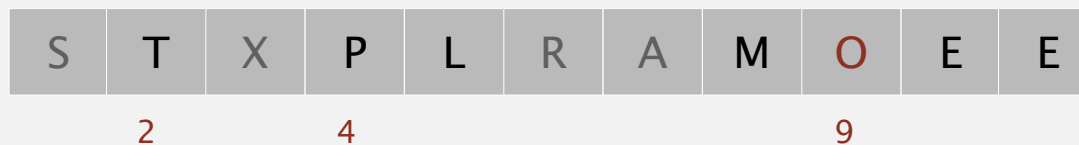
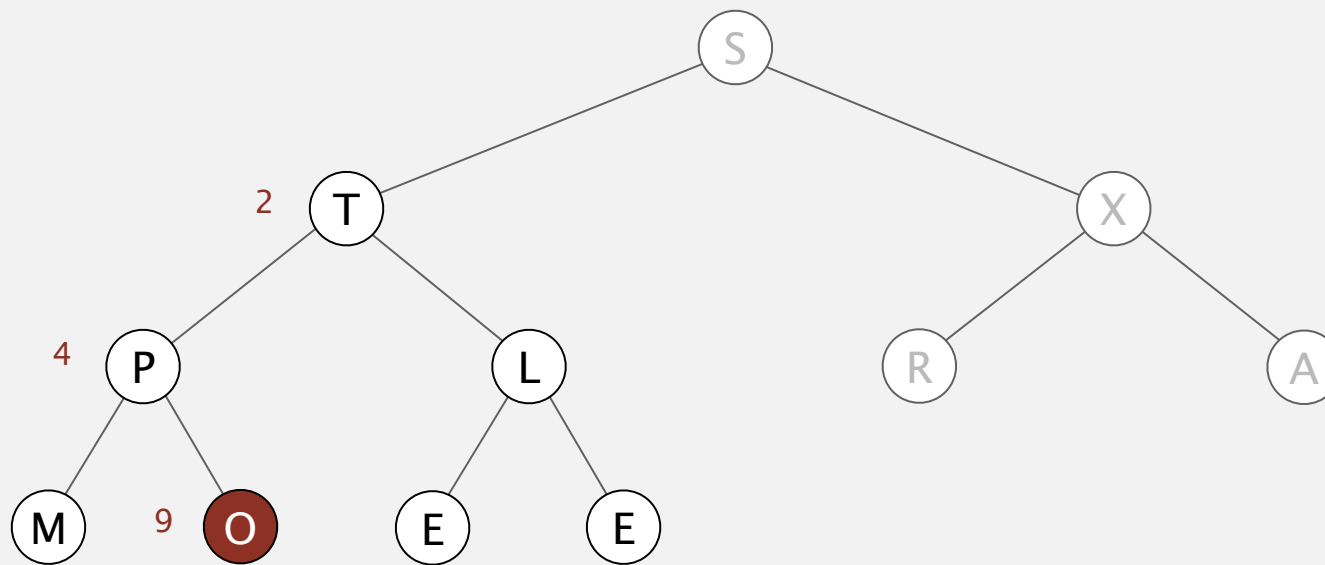


# Heapsort demo

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**Heap construction.** Build max heap using bottom-up method.

**sink 2**

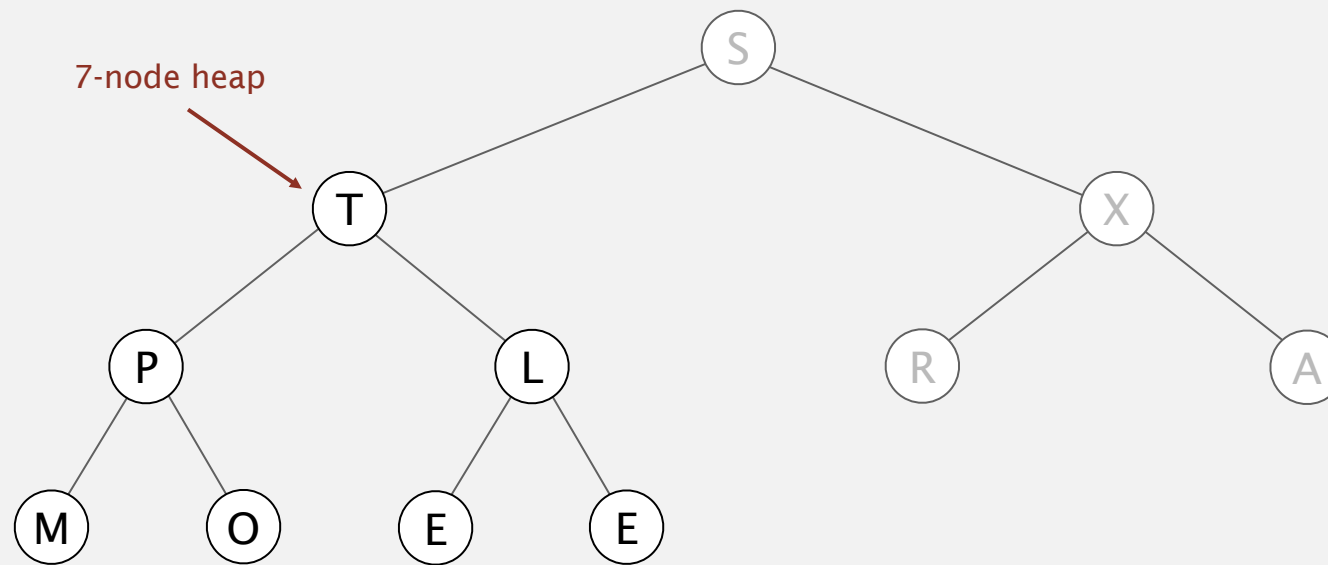


# Heapsort demo

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**Heap construction.** Build max heap using bottom-up method.

**sink 2**



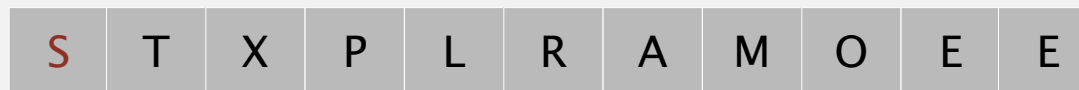
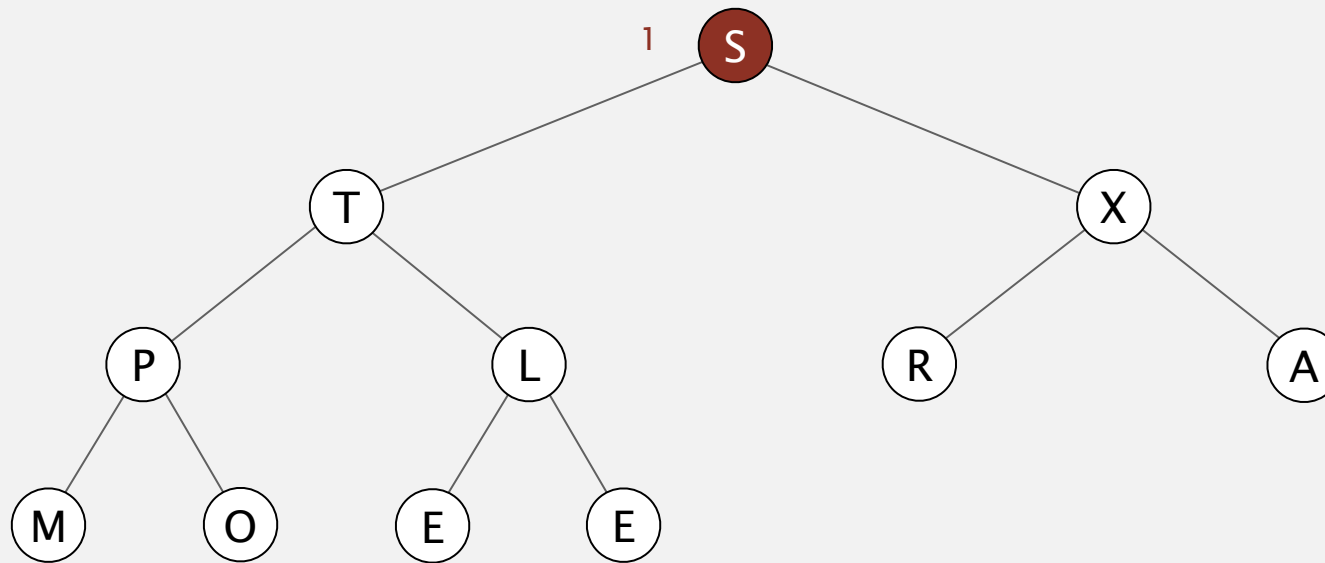
S	T	X	P	L	R	A	M	O	E	E
---	---	---	---	---	---	---	---	---	---	---

# Heapsort demo

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Heap construction. Build max heap using bottom-up method.

sink 1



1

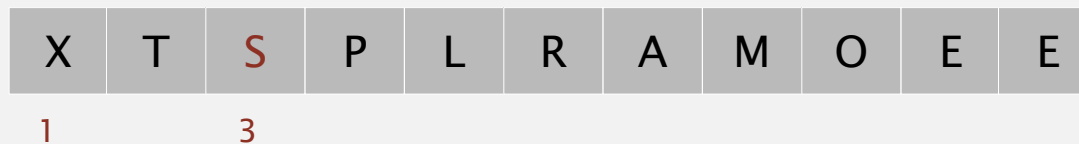
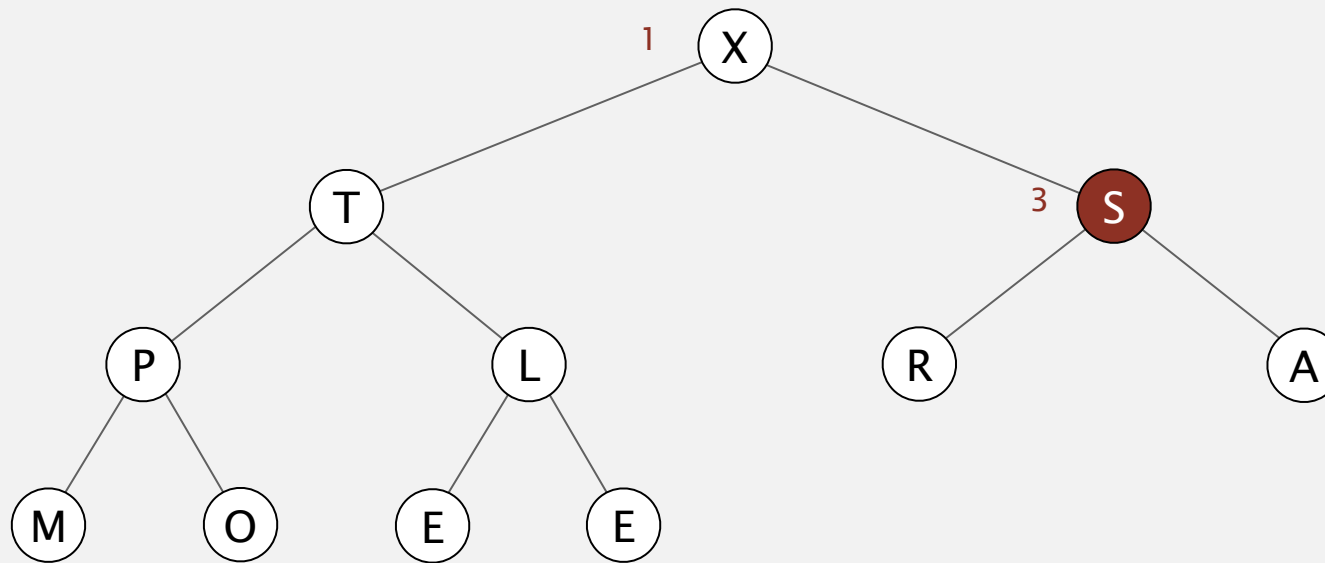


# Heapsort demo

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**Heap construction.** Build max heap using bottom-up method.

**sink 1**



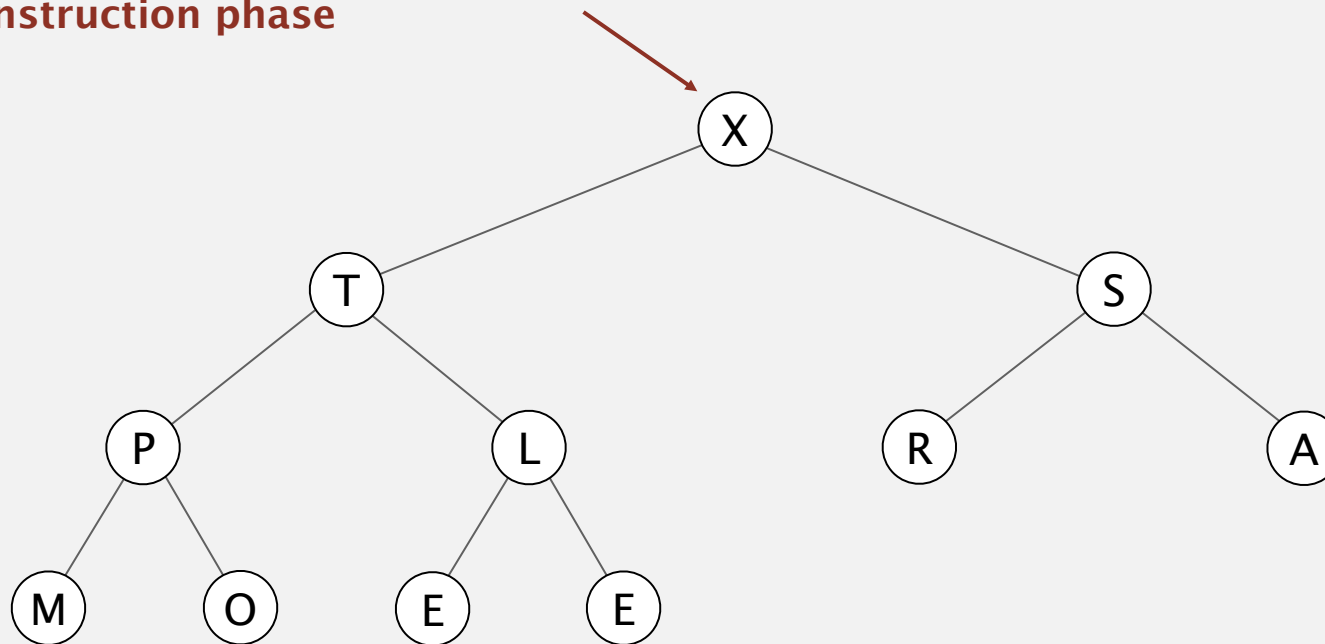
# Heapsort demo

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**Heap construction.** Build max heap using bottom-up method.

**end of construction phase**

11-node heap

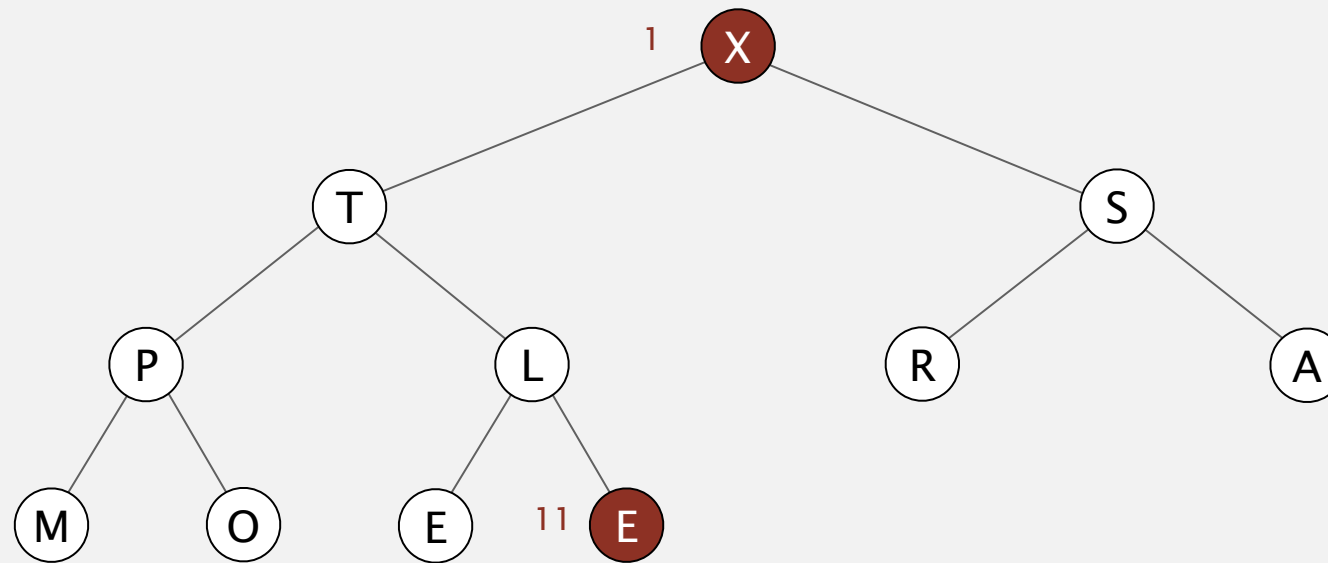


X	T	S	P	L	R	A	M	O	E	E
---	---	---	---	---	---	---	---	---	---	---

# Heapsort demo

**Sortdown.** Repeatedly delete the largest remaining item.

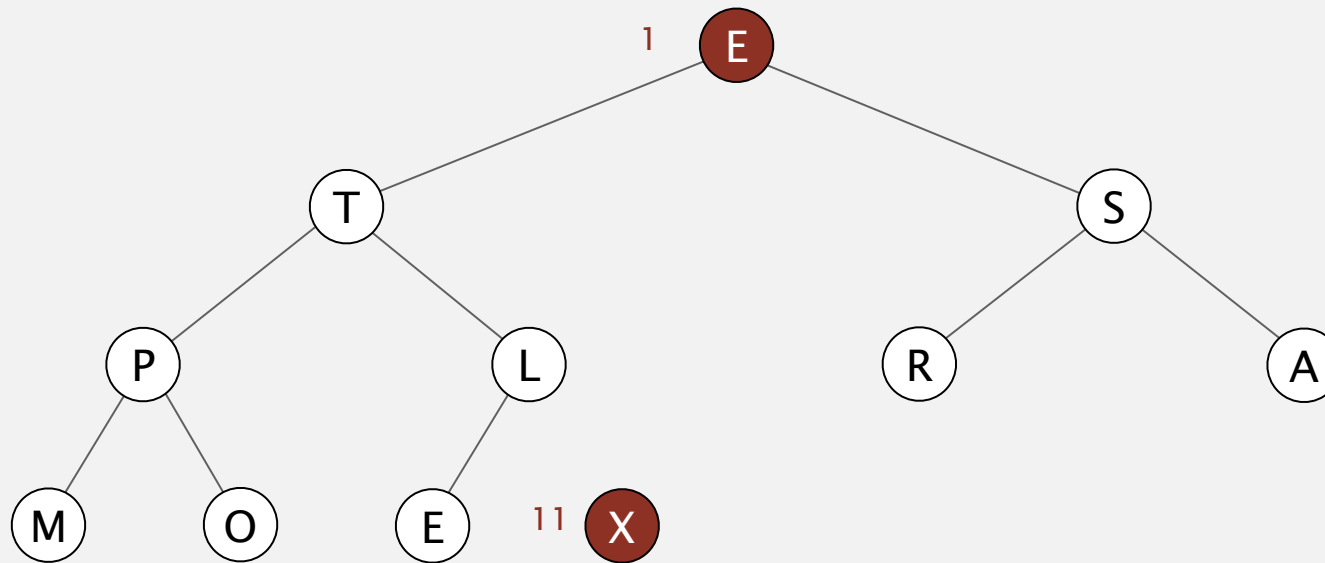
## exchange 1 and 11



# Heapsort demo

**Sortdown.** Repeatedly delete the largest remaining item.

## exchange 1 and 11

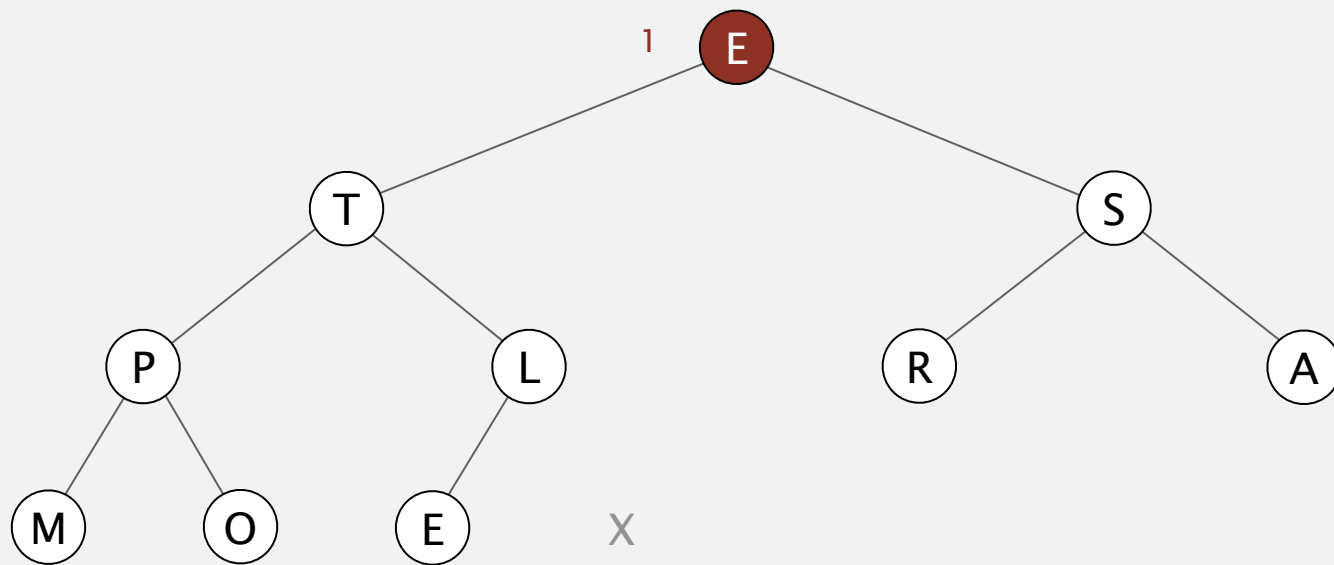


# Heapsort demo

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**Sortdown.** Repeatedly delete the largest remaining item.

**sink 1**



1

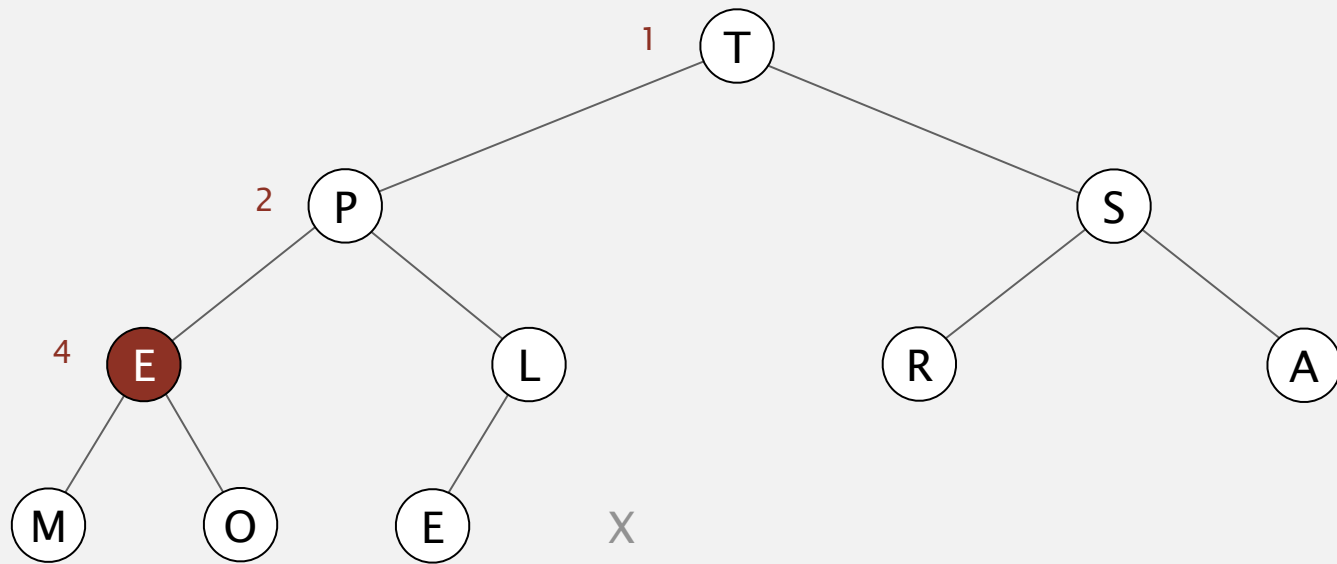


# Heapsort demo

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**Sortdown.** Repeatedly delete the largest remaining item.

**sink 1**

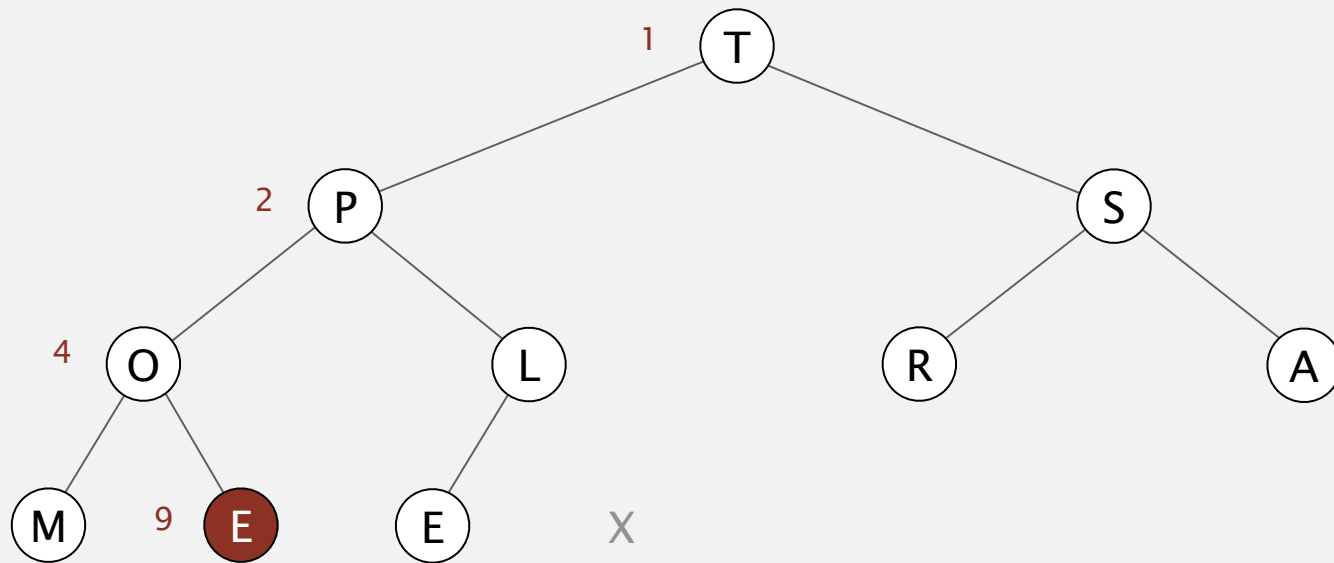


T	P	S	E	L	R	A	M	O	E	X
1	2		4							

# Heapsort demo

**Sortdown.** Repeatedly delete the largest remaining item.

**sink 1**



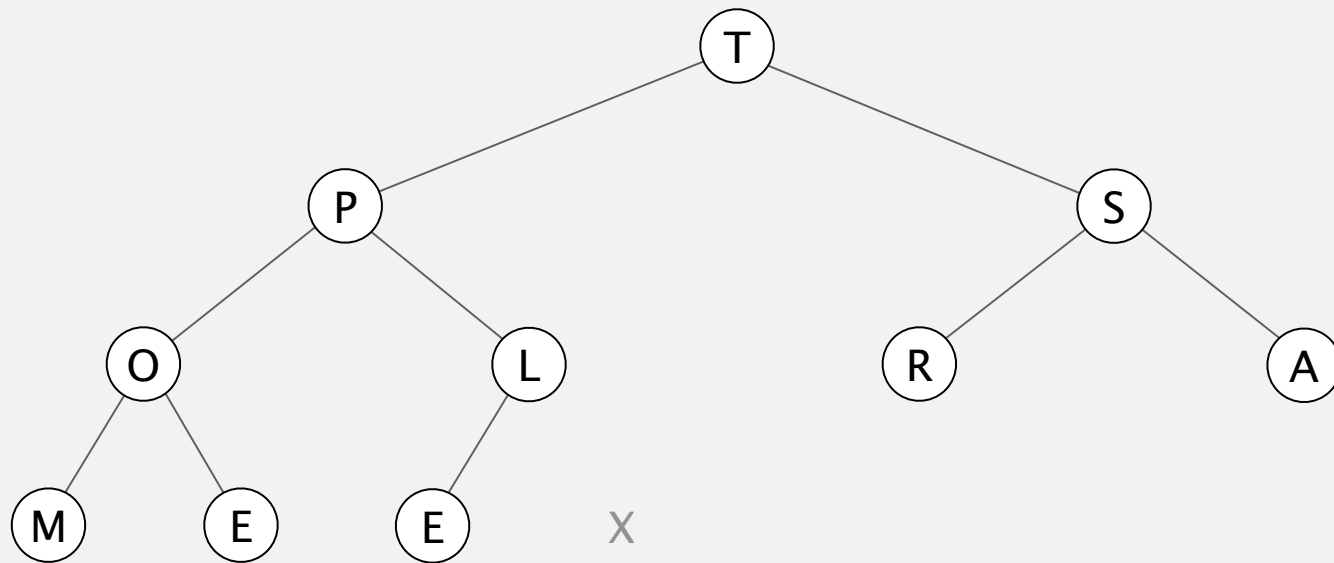
T	P	S	O	L	R	A	M	E	E	X
1	2		4					9		



# Heapsort demo

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**Sortdown.** Repeatedly delete the largest remaining item.

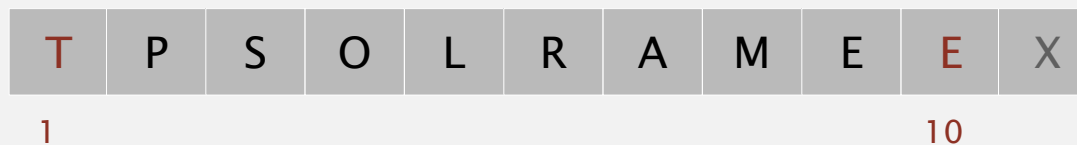
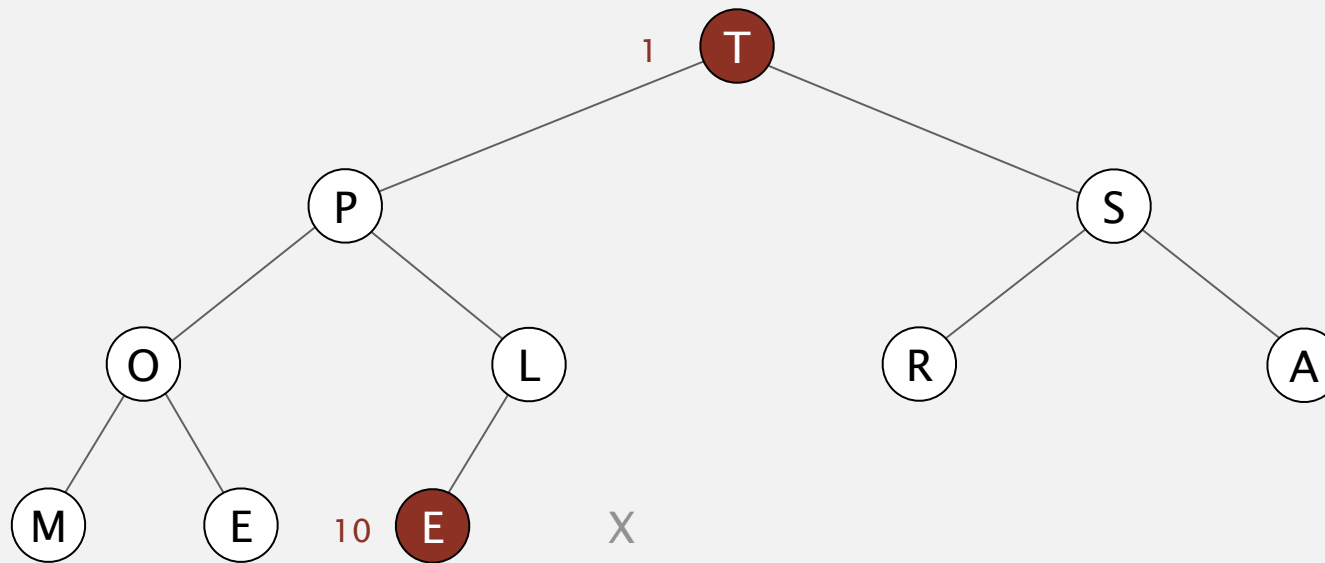


T	P	S	O	L	R	A	M	E	E	X
---	---	---	---	---	---	---	---	---	---	---

# Heapsort demo

**Sortdown.** Repeatedly delete the largest remaining item.

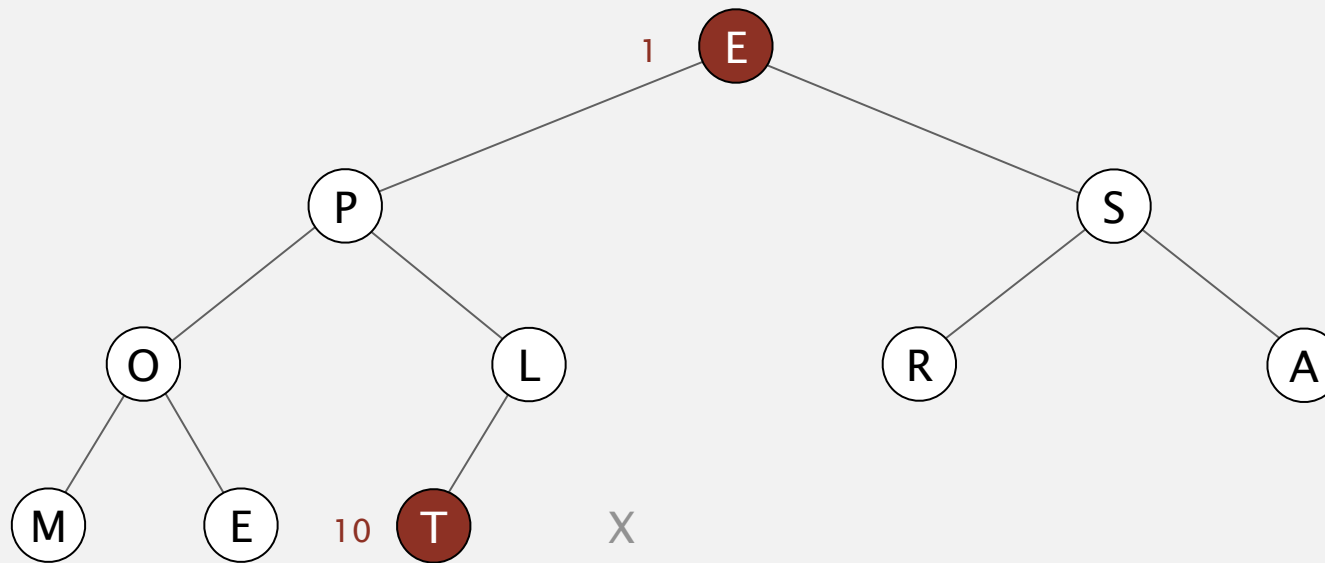
## exchange 1 and 10



# Heapsort demo

**Sortdown.** Repeatedly delete the largest remaining item.

## exchange 1 and 10

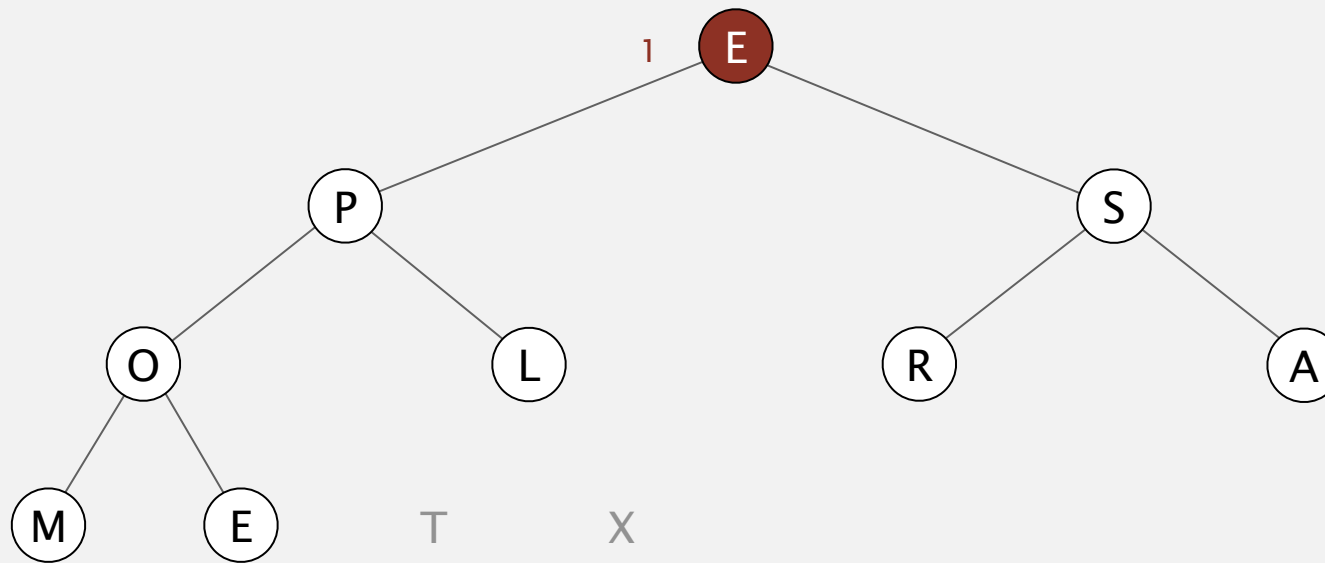


# Heapsort demo

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**Sortdown.** Repeatedly delete the largest remaining item.

**sink 1**

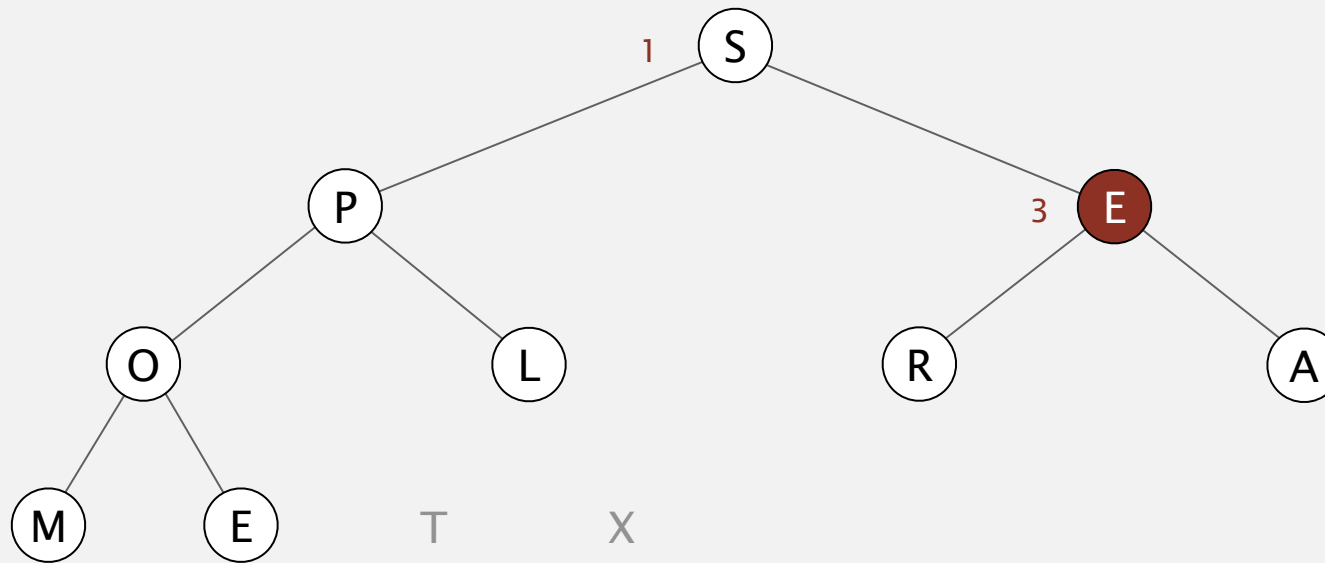


# Heapsort demo

---

**Sortdown.** Repeatedly delete the largest remaining item.

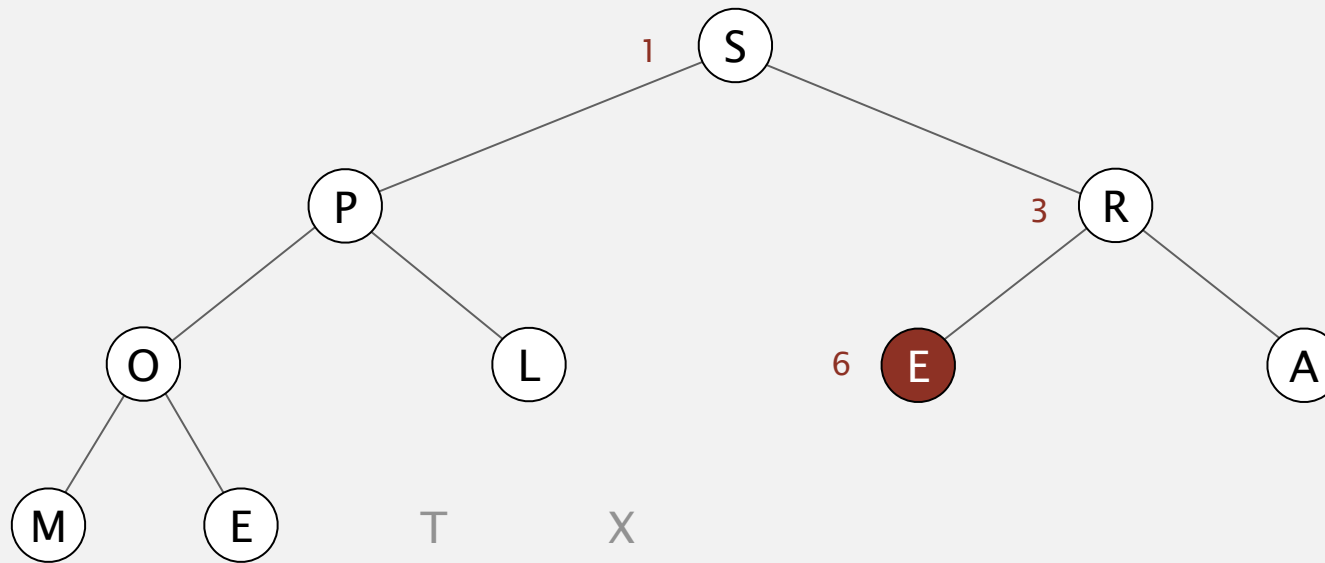
**sink 1**



# Heapsort demo

**Sortdown.** Repeatedly delete the largest remaining item.

**sink 1**

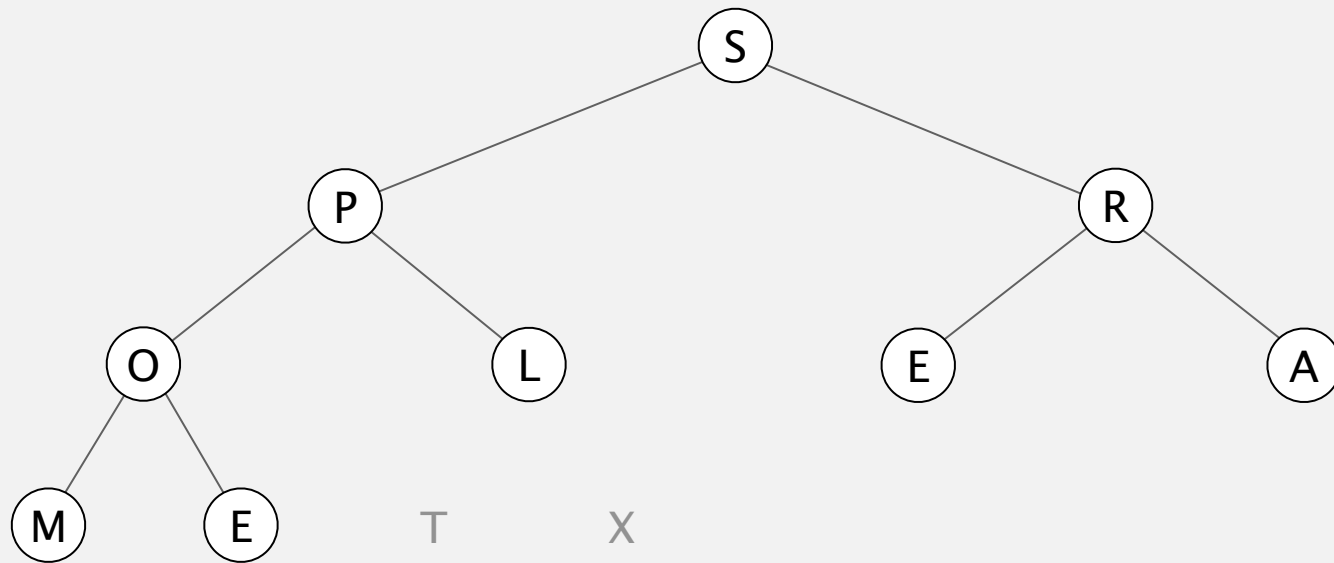


S	P	R	O	L	E	A	M	E	T	X
1	3				6					

# Heapsort demo

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**Sortdown.** Repeatedly delete the largest remaining item.



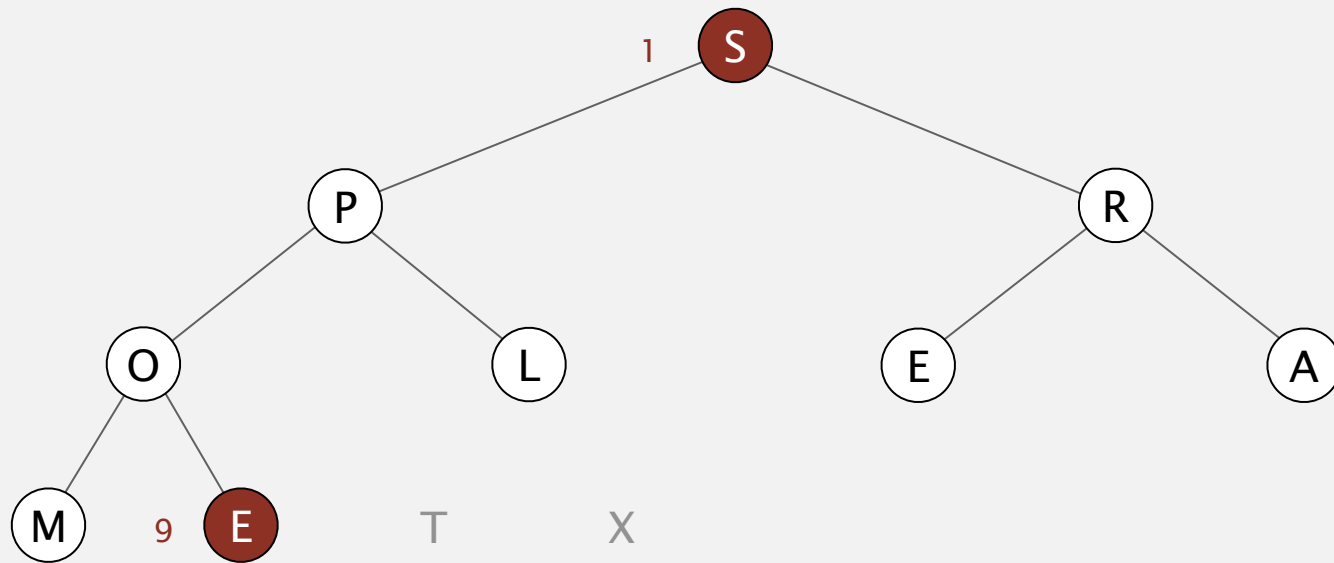
S	P	R	O	L	E	A	M	E	T	X
---	---	---	---	---	---	---	---	---	---	---

# Heapsort demo

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**Sortdown.** Repeatedly delete the largest remaining item.

exchange 1 and 9

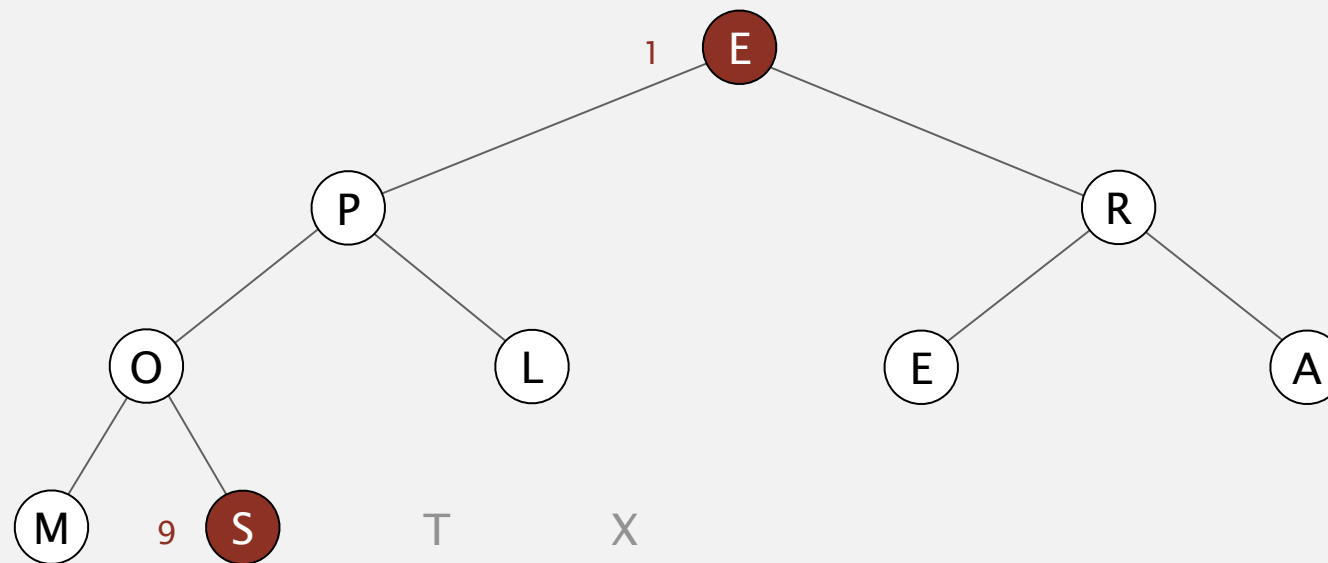




# Heapsort demo

**Sortdown.** Repeatedly delete the largest remaining item.

exchange 1 and 9

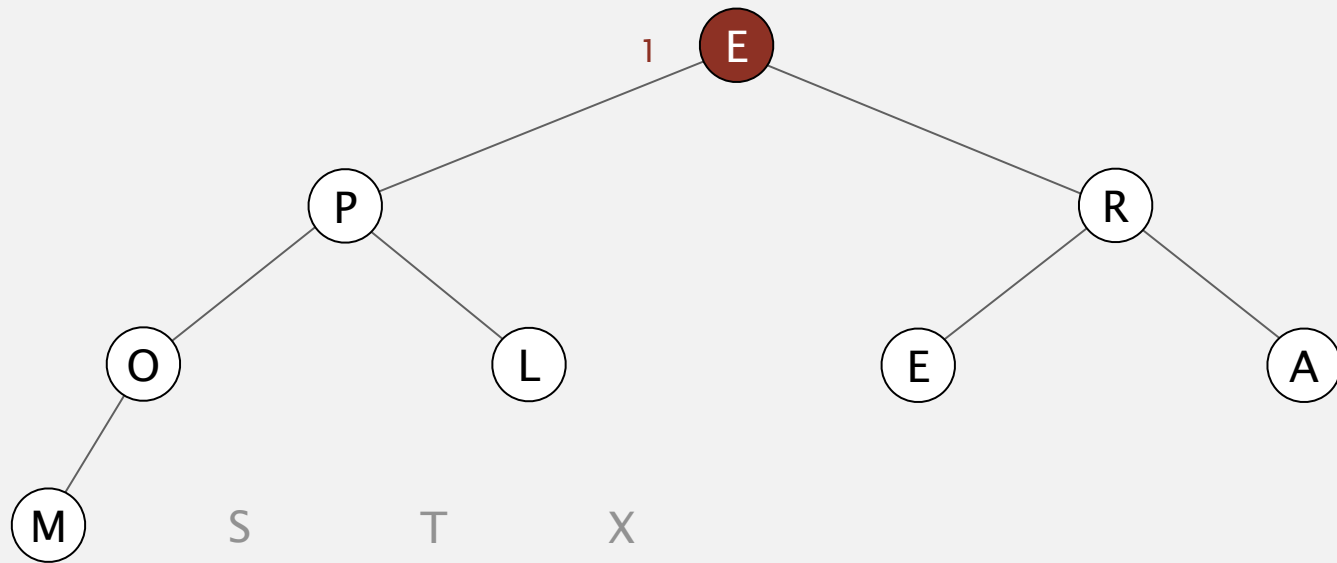


# Heapsort demo

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**Sortdown.** Repeatedly delete the largest remaining item.

**sink 1**

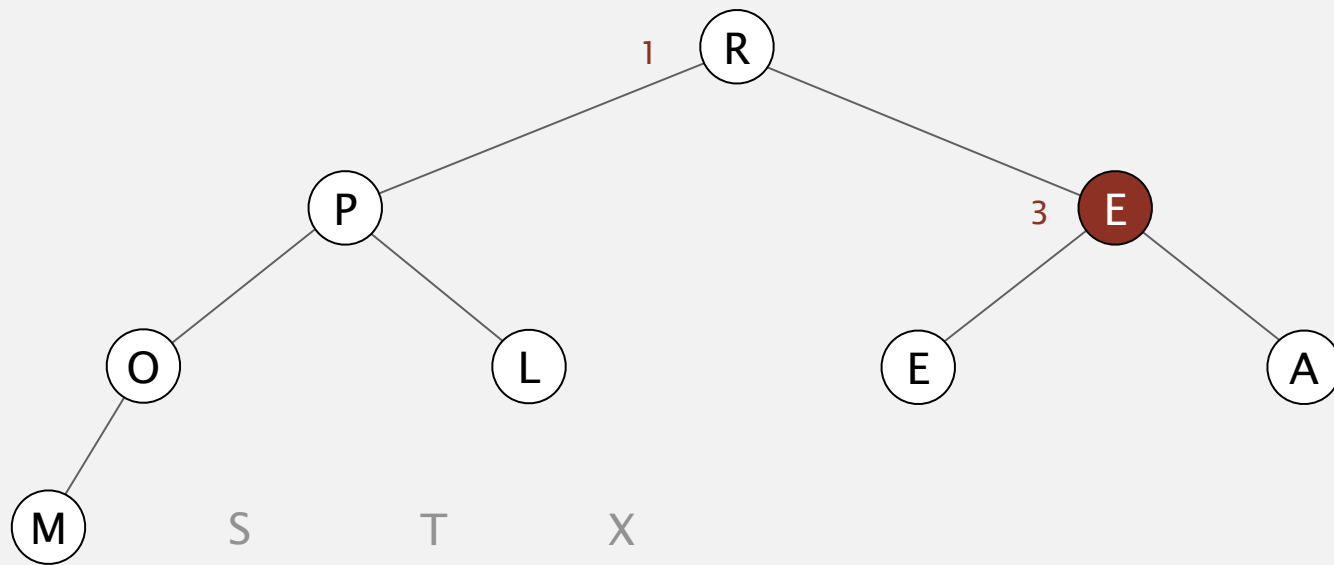


# Heapsort demo

---

**Sortdown.** Repeatedly delete the largest remaining item.

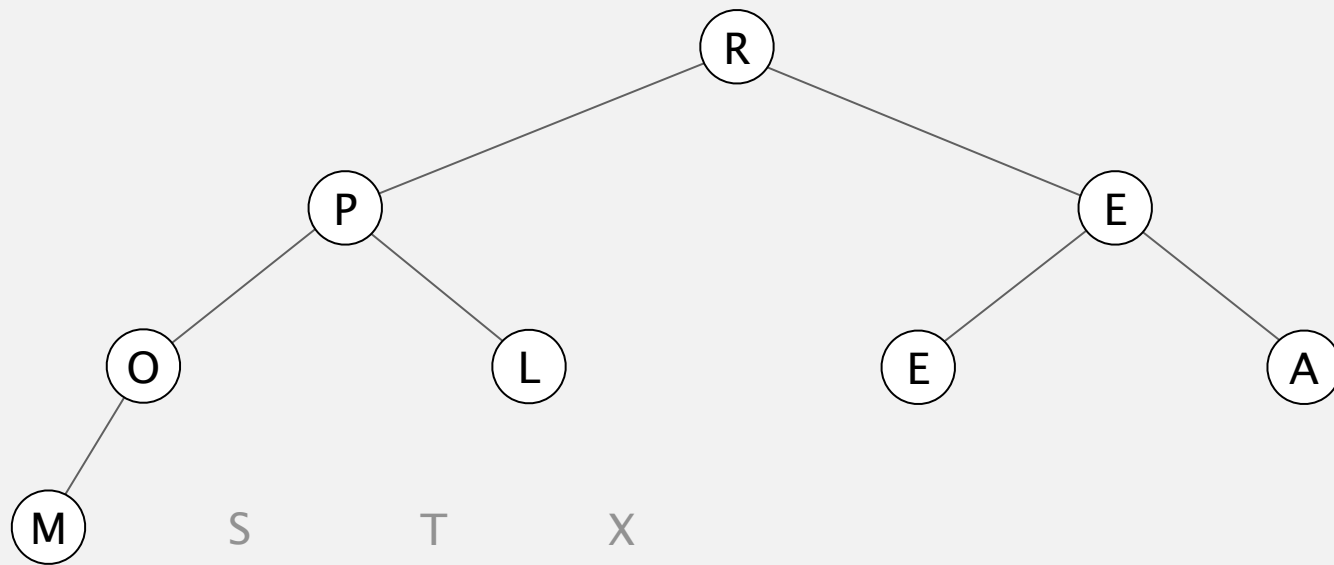
**sink 1**



# Heapsort demo

---

**Sortdown.** Repeatedly delete the largest remaining item.



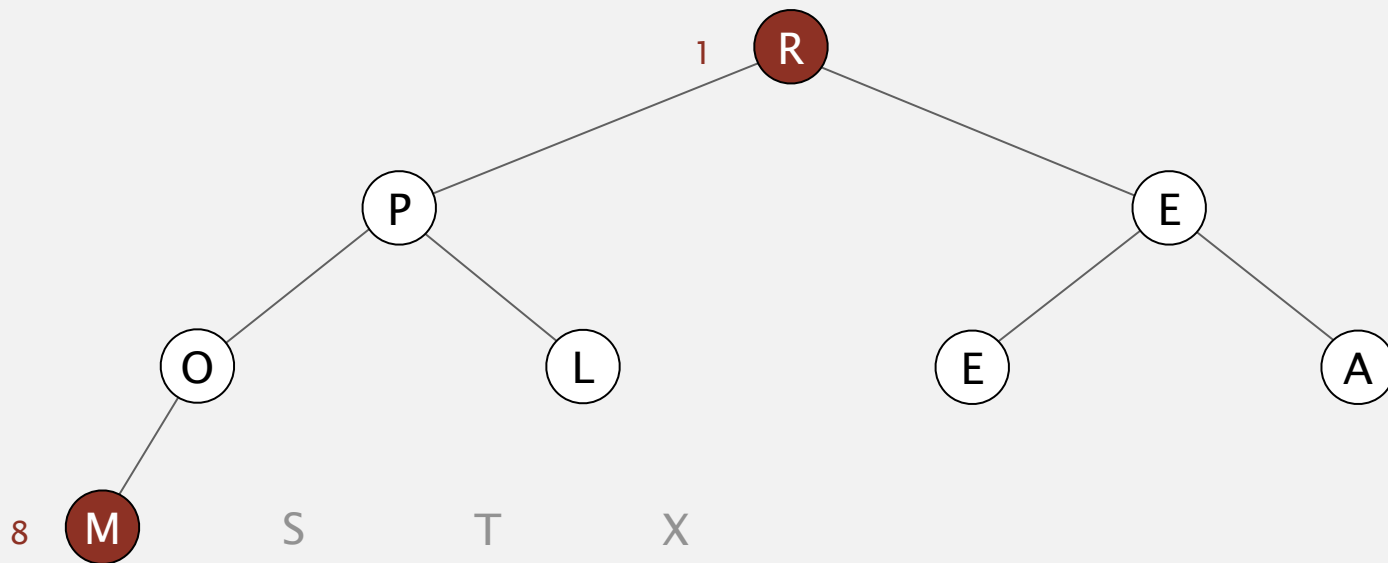
R	P	E	O	L	E	A	M	S	T	X
---	---	---	---	---	---	---	---	---	---	---

# Heapsort demo

---

**Sortdown.** Repeatedly delete the largest remaining item.

exchange 1 and 8

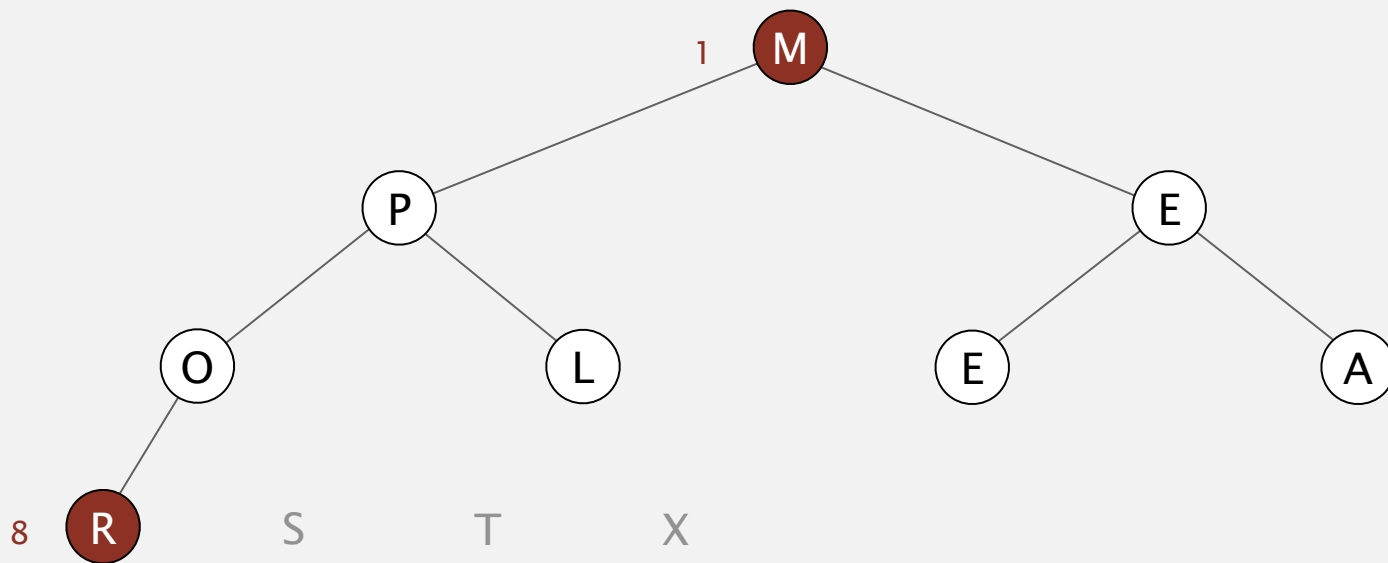


# Heapsort demo

---

**Sortdown.** Repeatedly delete the largest remaining item.

exchange 1 and 8

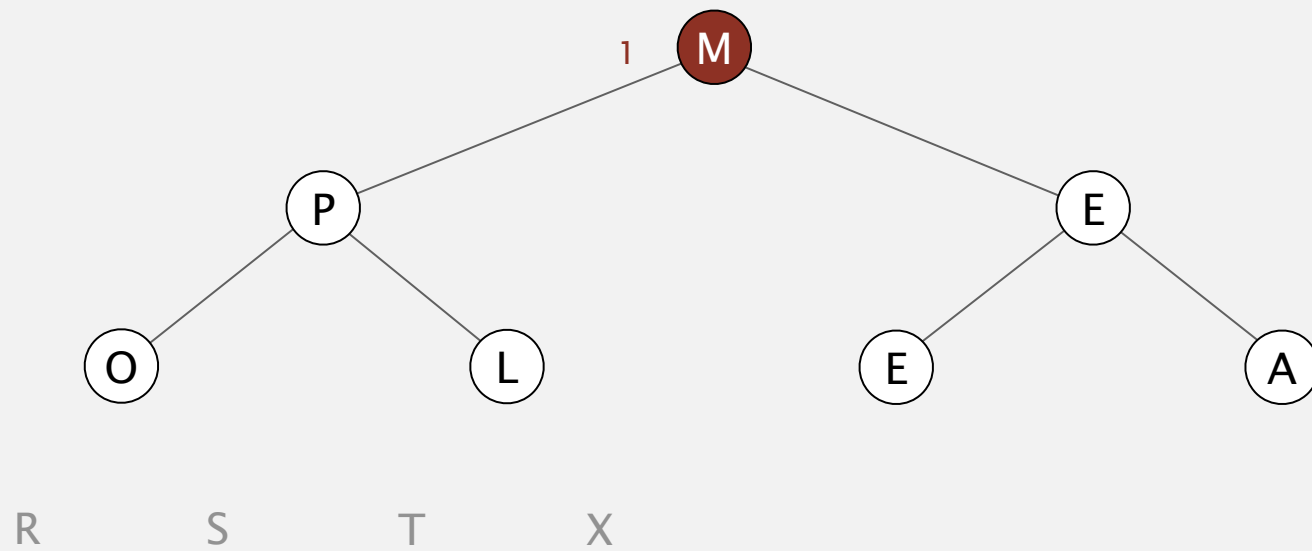


# Heapsort demo

---

**Sortdown.** Repeatedly delete the largest remaining item.

**sink 1**



1



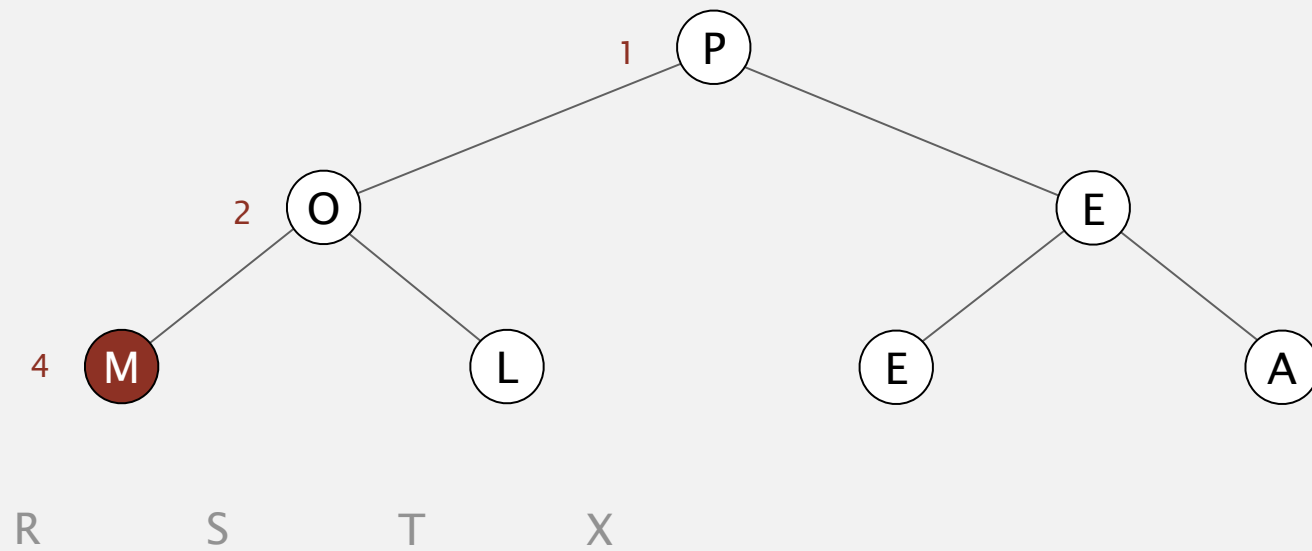


# Heapsort demo

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**Sortdown.** Repeatedly delete the largest remaining item.

**sink 1**

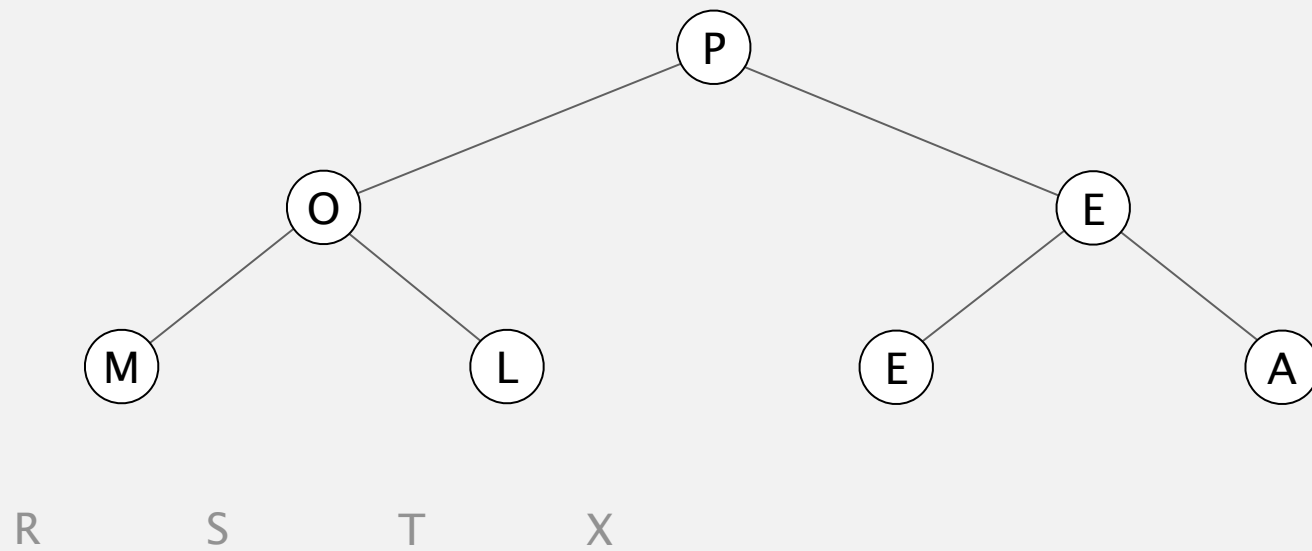


P	O	E	M	L	E	A	R	S	T	X
1	2		4							

# Heapsort demo

---

**Sortdown.** Repeatedly delete the largest remaining item.



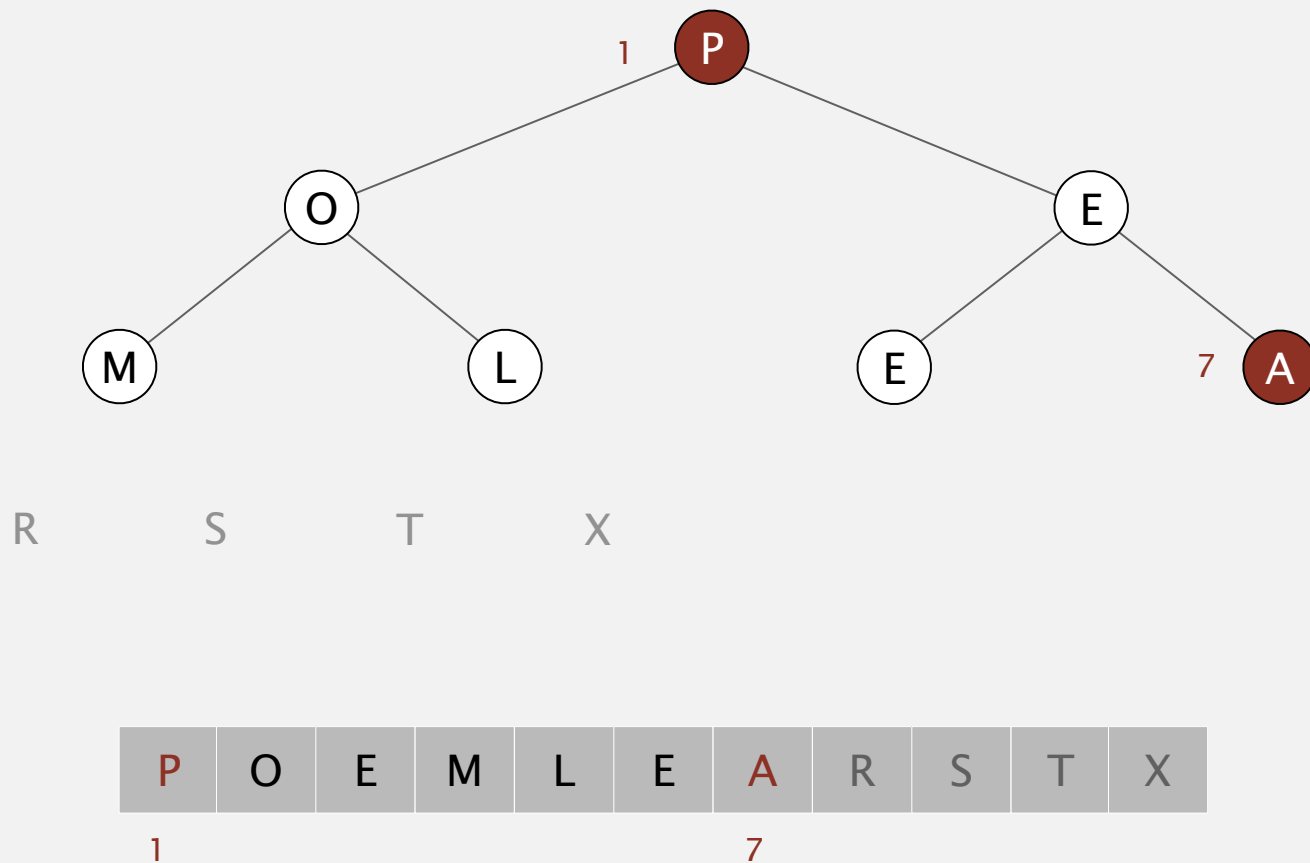
P	O	E	M	L	E	A	R	S	T	X
---	---	---	---	---	---	---	---	---	---	---

# Heapsort demo

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**Sortdown.** Repeatedly delete the largest remaining item.

exchange 1 and 7

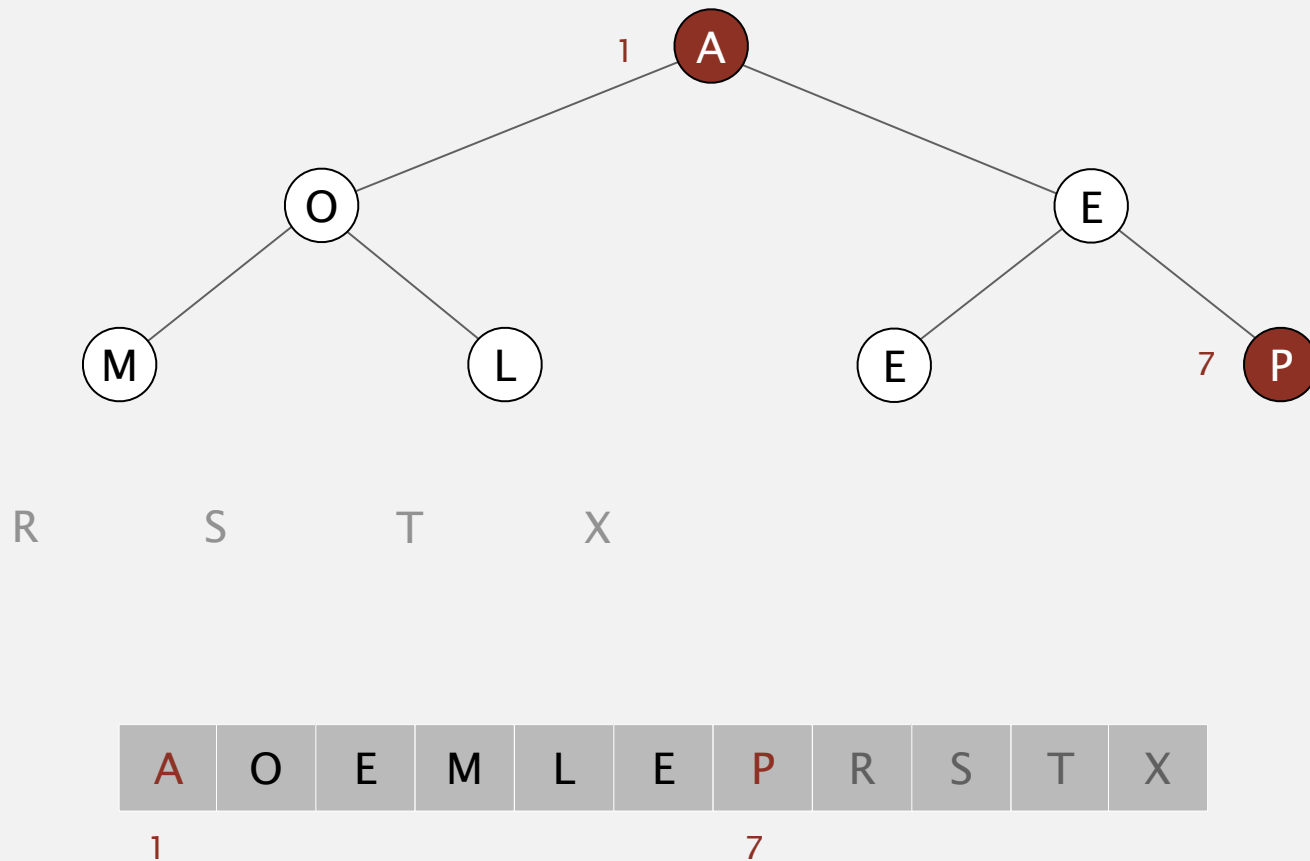


# Heapsort demo

---

**Sortdown.** Repeatedly delete the largest remaining item.

exchange 1 and 7

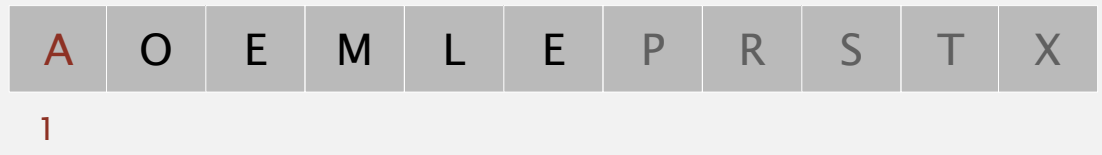
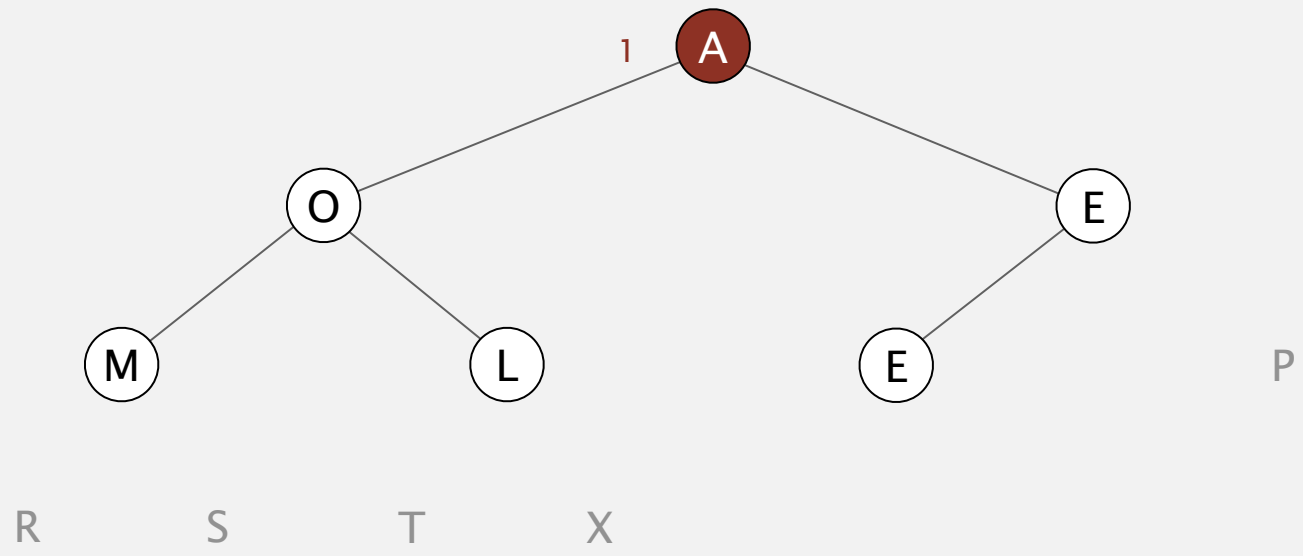


# Heapsort demo

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**Sortdown.** Repeatedly delete the largest remaining item.

**sink 1**



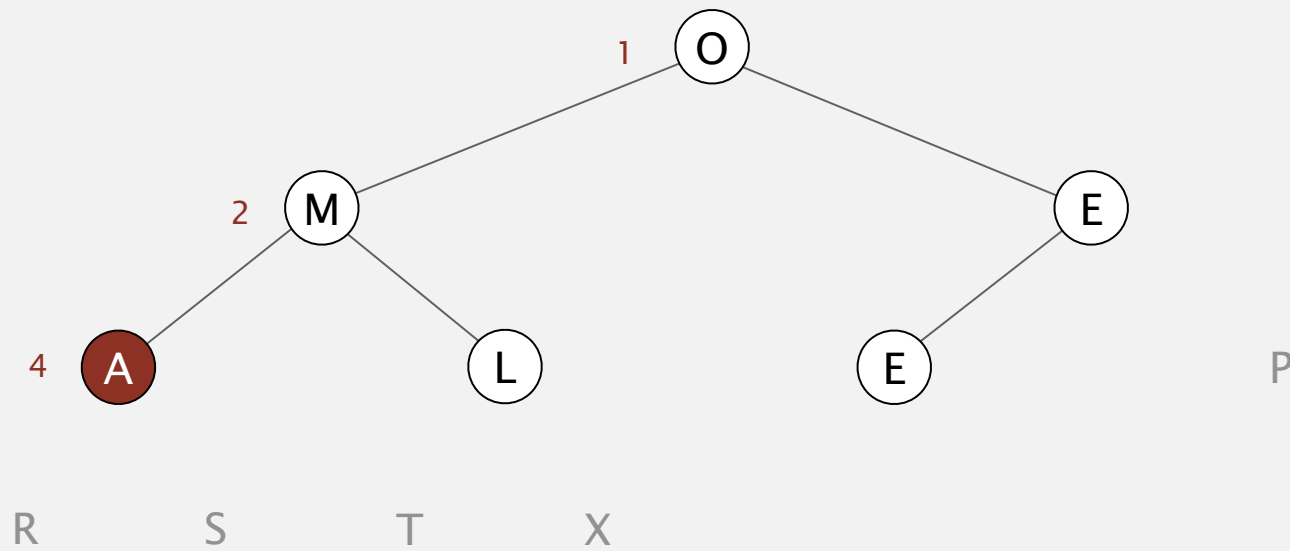


# Heapsort demo

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**Sortdown.** Repeatedly delete the largest remaining item.

**sink 1**



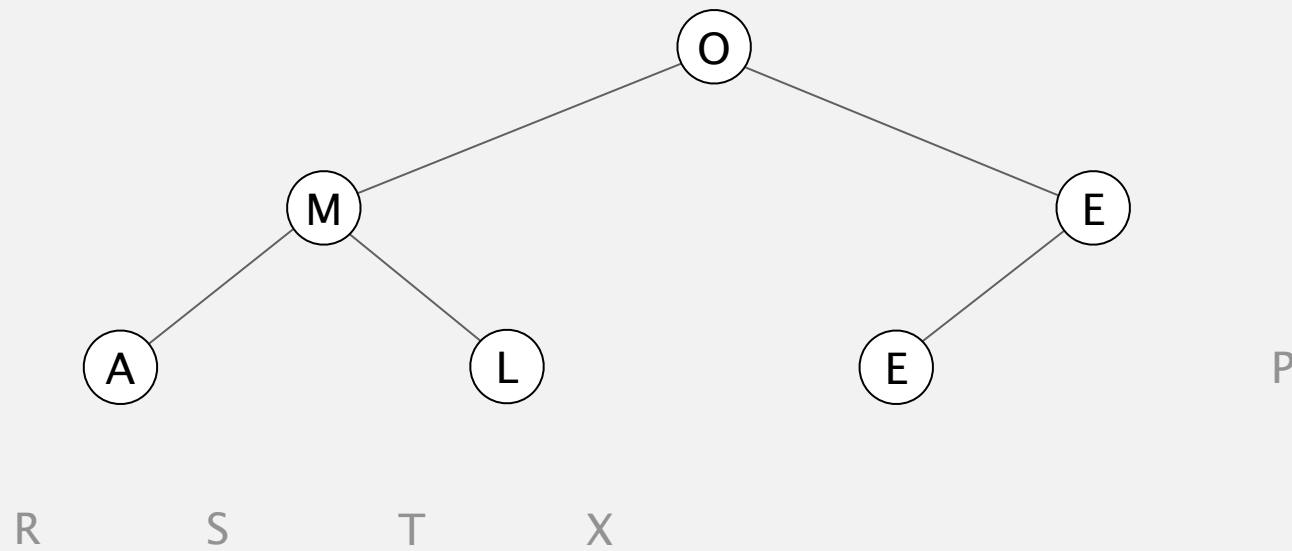
O	M	E	A	L	E	P	R	S	T	X
1	2		4							

# Heapsort demo

---

**Sortdown.** Repeatedly delete the largest remaining item.

**sink 1**



O	M	E	A	L	E	P	R	S	T	X
---	---	---	---	---	---	---	---	---	---	---

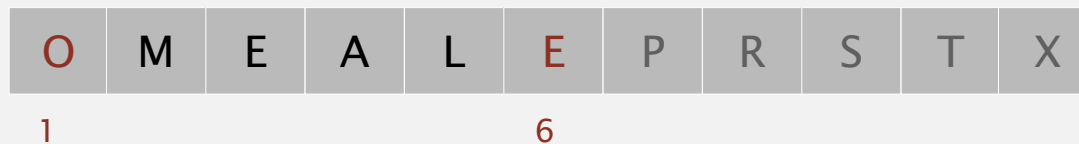
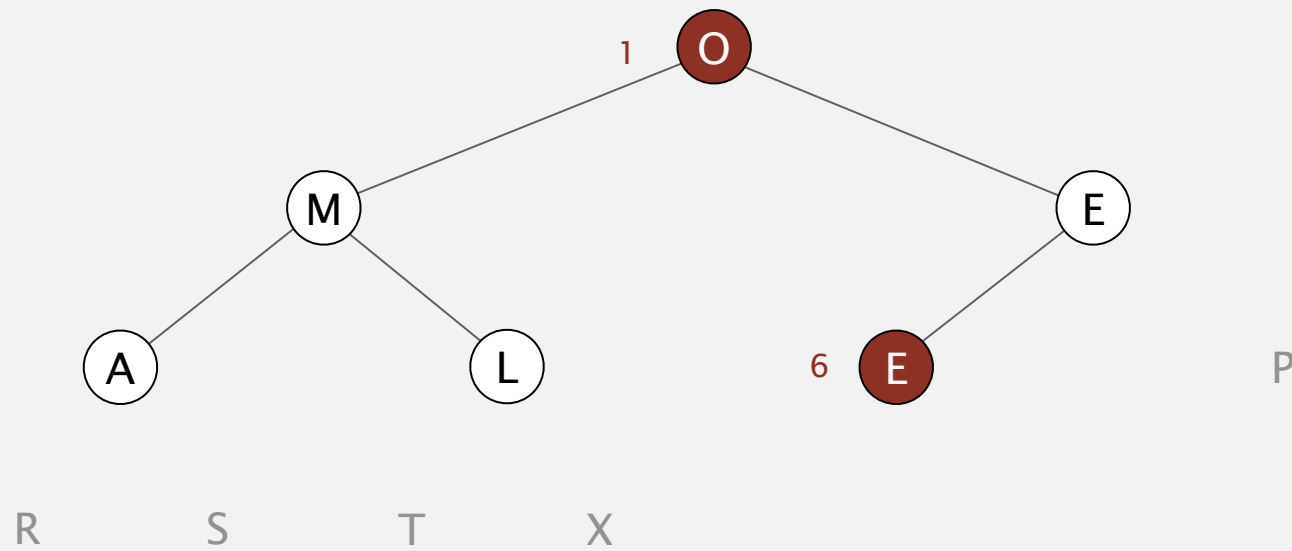


# Heapsort demo

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**Sortdown.** Repeatedly delete the largest remaining item.

exchange 1 and 6

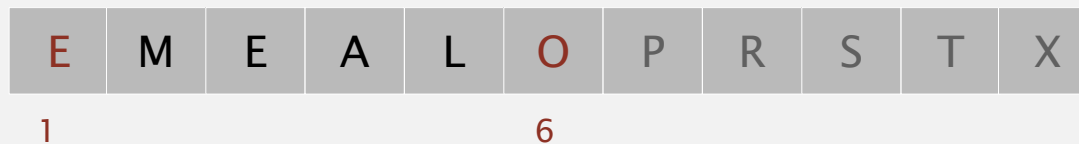
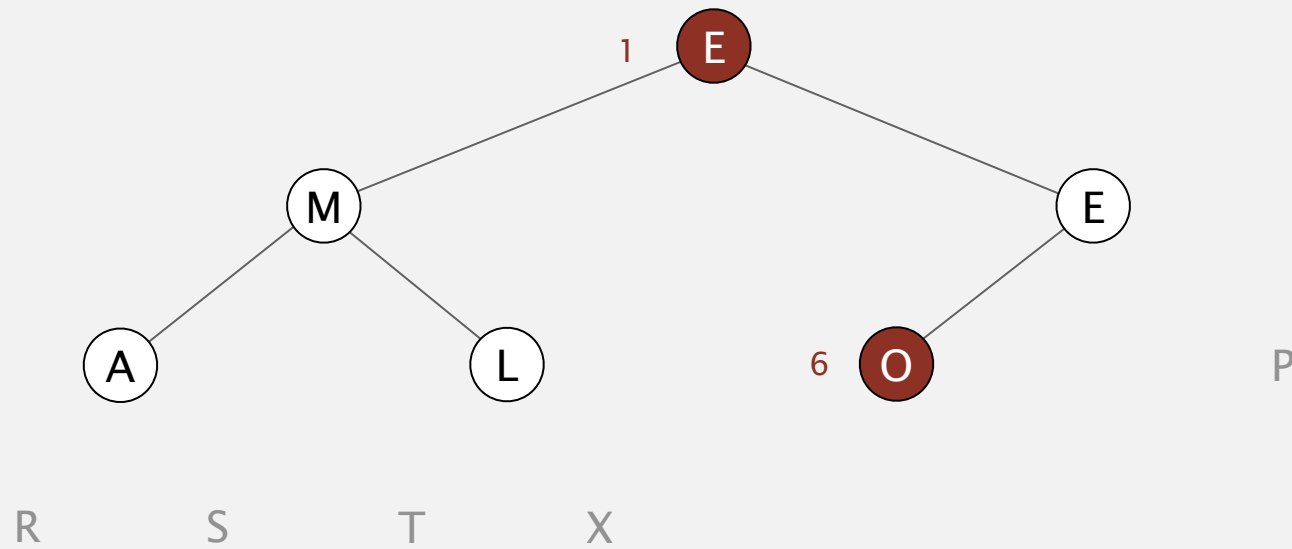


# Heapsort demo

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**Sortdown.** Repeatedly delete the largest remaining item.

exchange 1 and 6

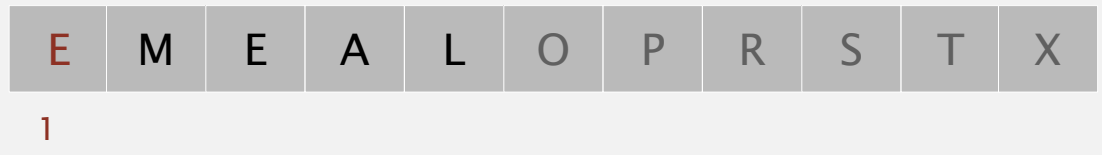
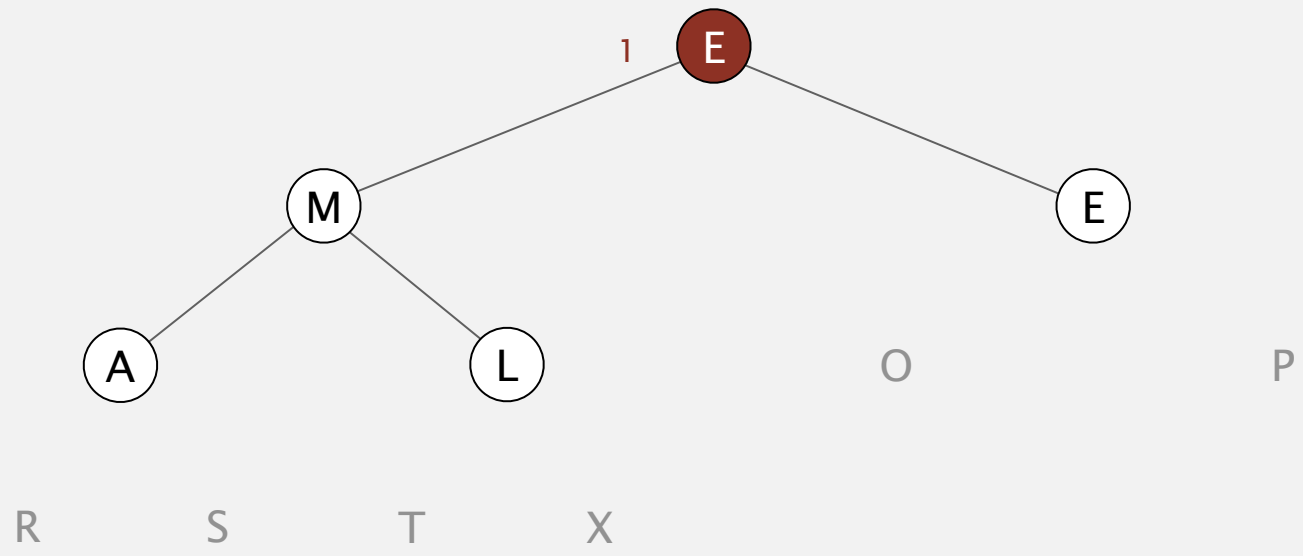


# Heapsort demo

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**Sortdown.** Repeatedly delete the largest remaining item.

**sink 1**



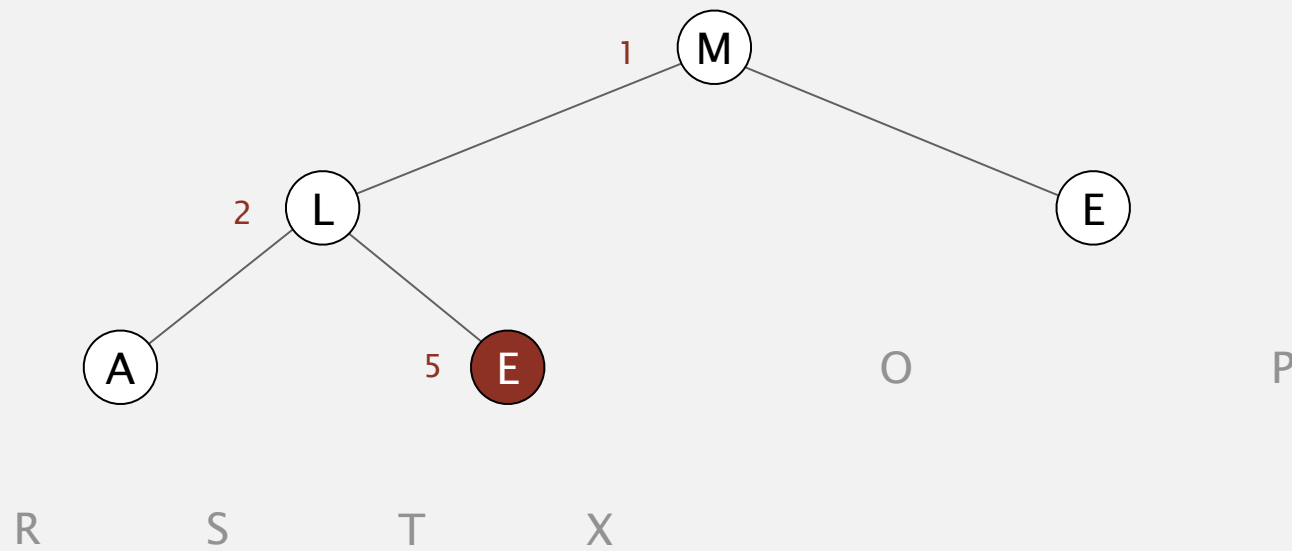


# Heapsort demo

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**Sortdown.** Repeatedly delete the largest remaining item.

**sink 1**

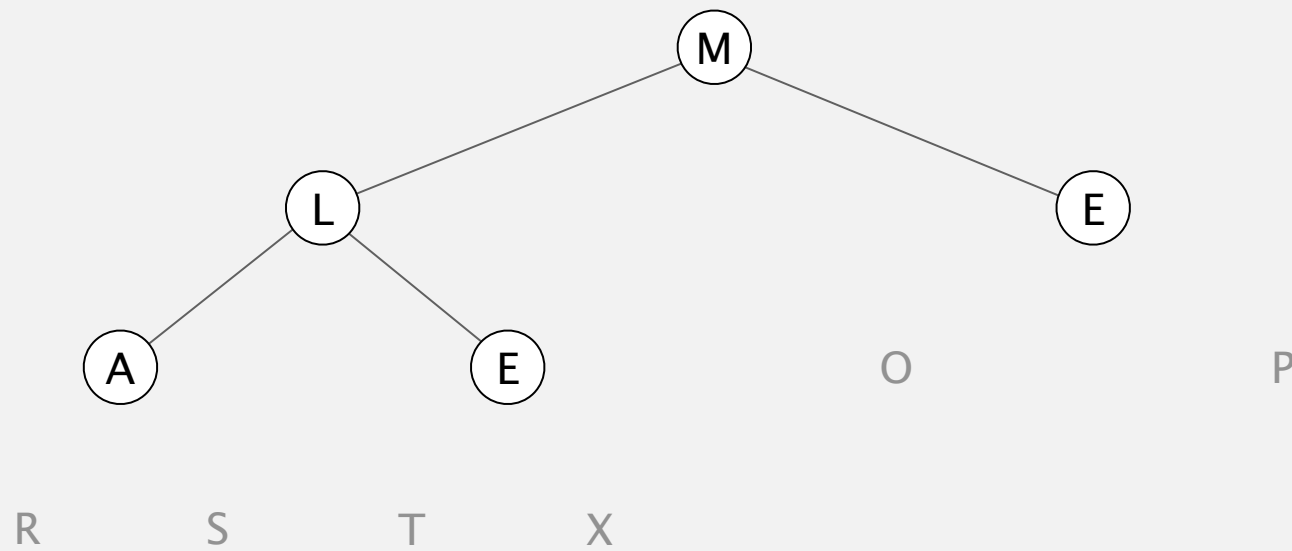


M	L	E	A	E	O	P	R	S	T	X
1	2			5						

# Heapsort demo

---

**Sortdown.** Repeatedly delete the largest remaining item.



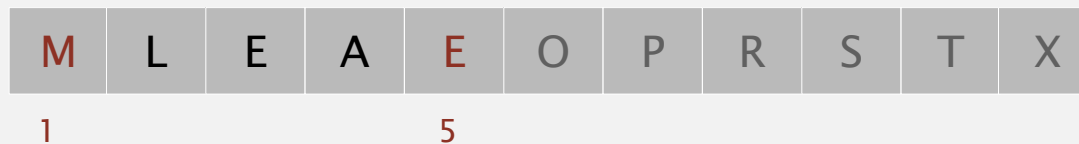
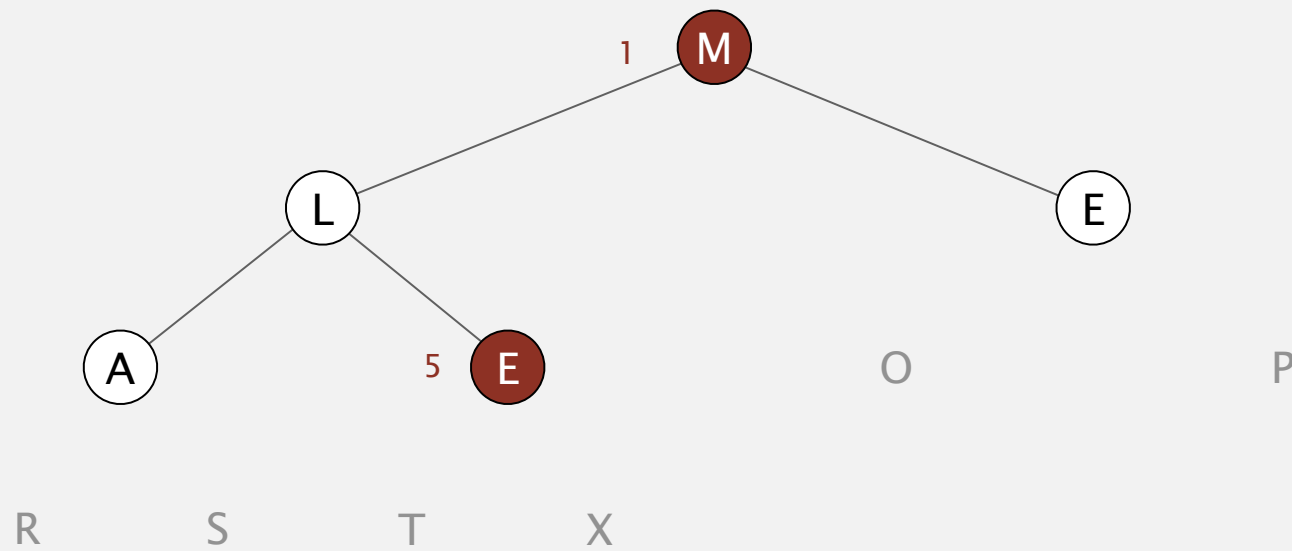
M	L	E	A	E	O	P	R	S	T	X
---	---	---	---	---	---	---	---	---	---	---

# Heapsort demo

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**Sortdown.** Repeatedly delete the largest remaining item.

exchange 1 and 5

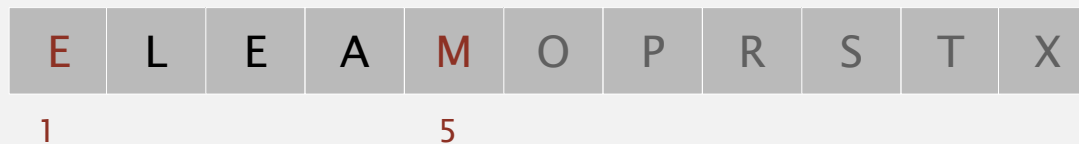
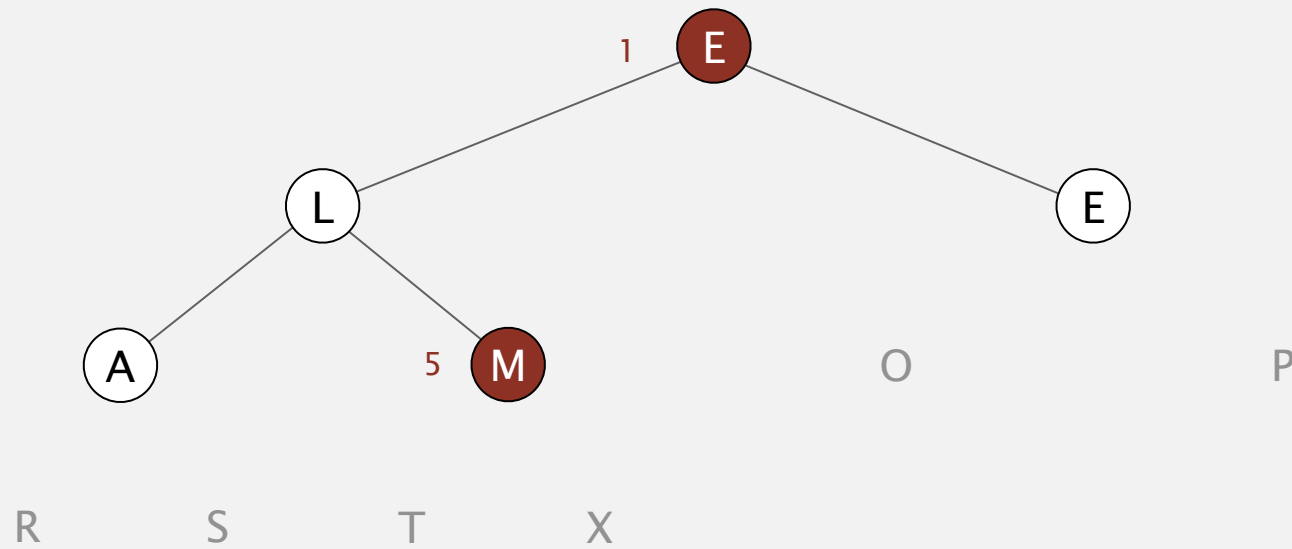


# Heapsort demo

---

**Sortdown.** Repeatedly delete the largest remaining item.

exchange 1 and 5



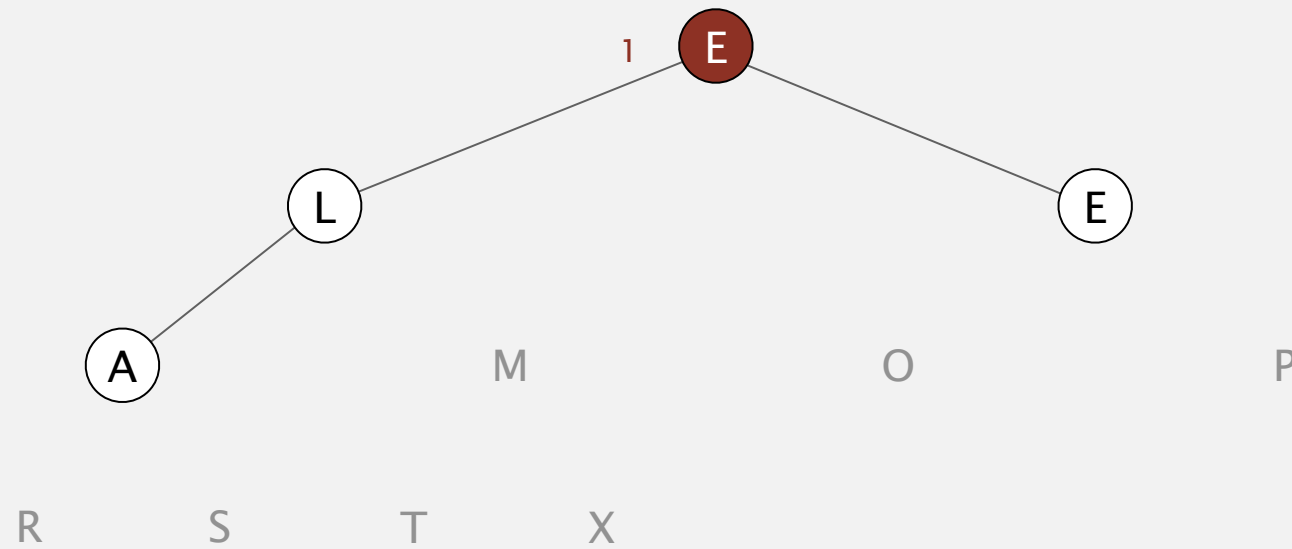


# Heapsort demo

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**Sortdown.** Repeatedly delete the largest remaining item.

**sink 1**



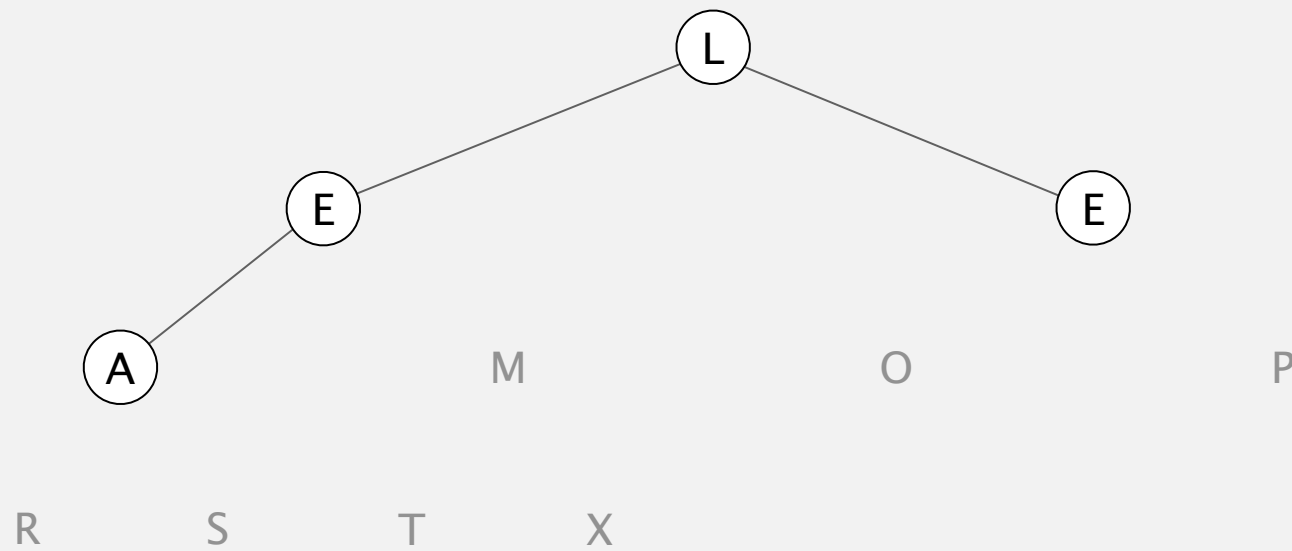
1



# Heapsort demo

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**Sortdown.** Repeatedly delete the largest remaining item.



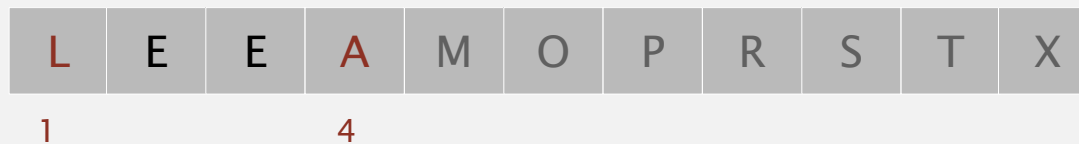
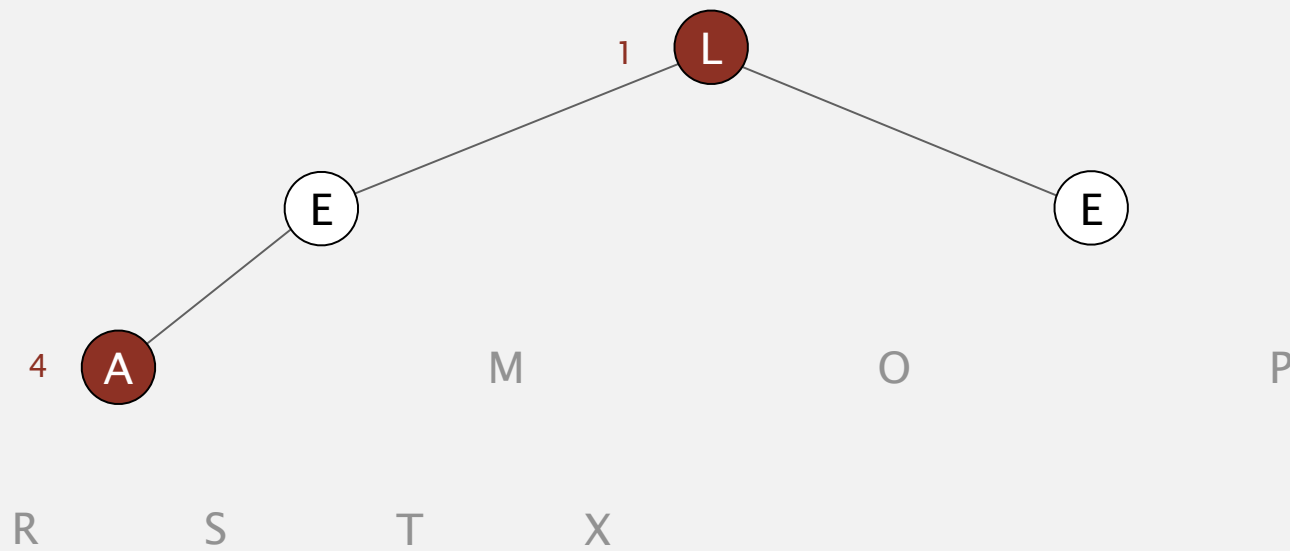
L	E	E	A	M	O	P	R	S	T	X
---	---	---	---	---	---	---	---	---	---	---

# Heapsort demo

---

**Sortdown.** Repeatedly delete the largest remaining item.

exchange 1 and 4

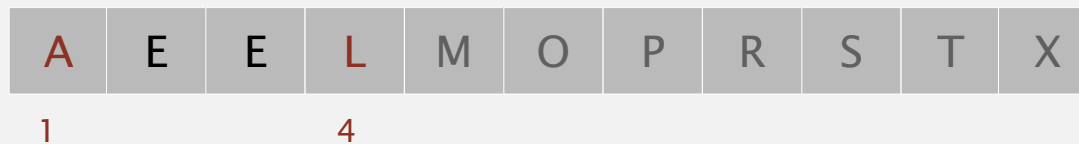
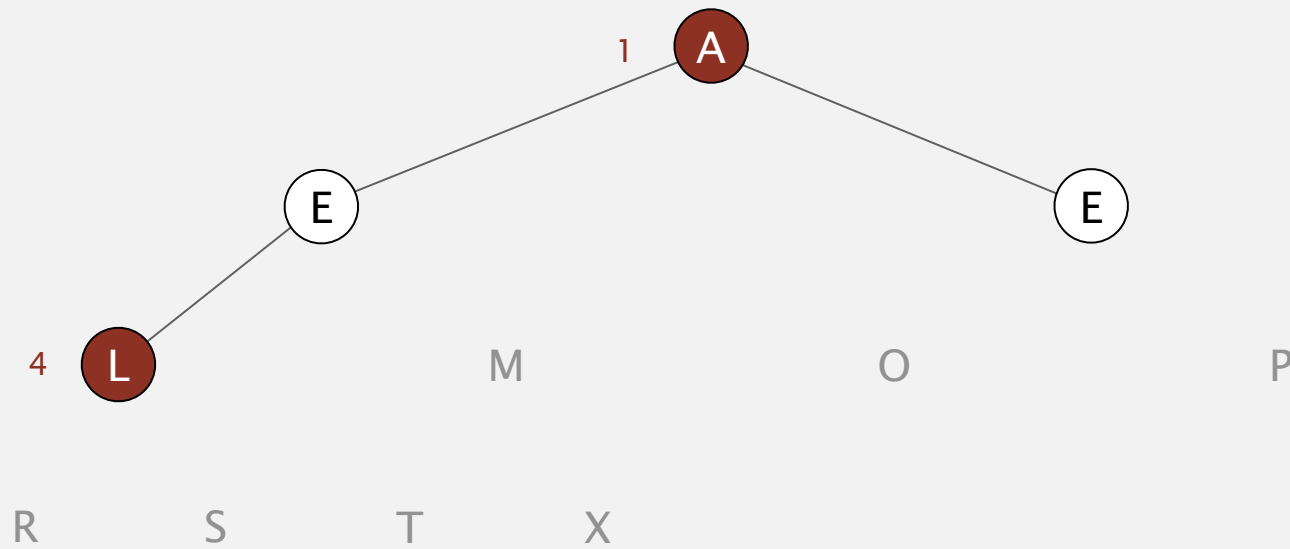


# Heapsort demo

---

**Sortdown.** Repeatedly delete the largest remaining item.

exchange 1 and 4

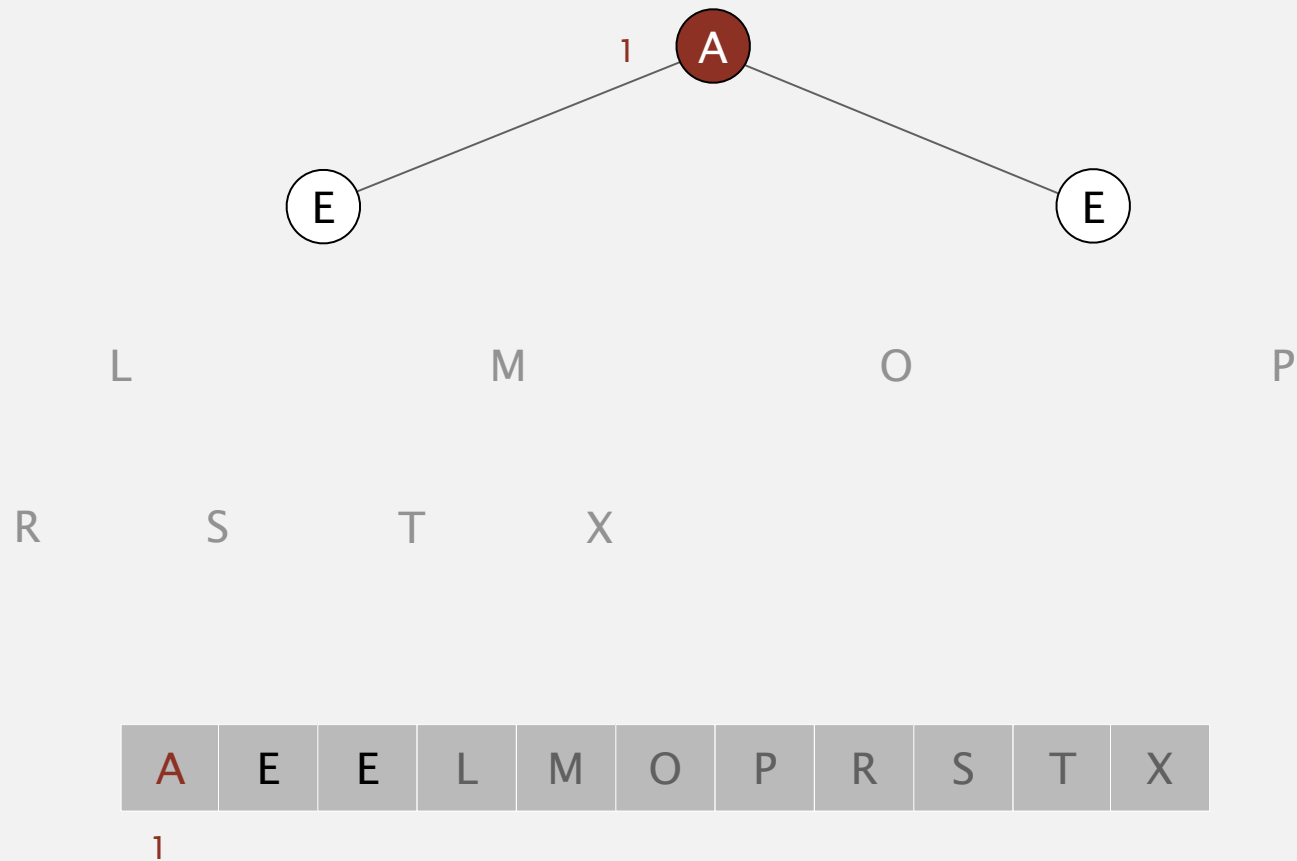


# Heapsort demo

---

**Sortdown.** Repeatedly delete the largest remaining item.

**sink 1**

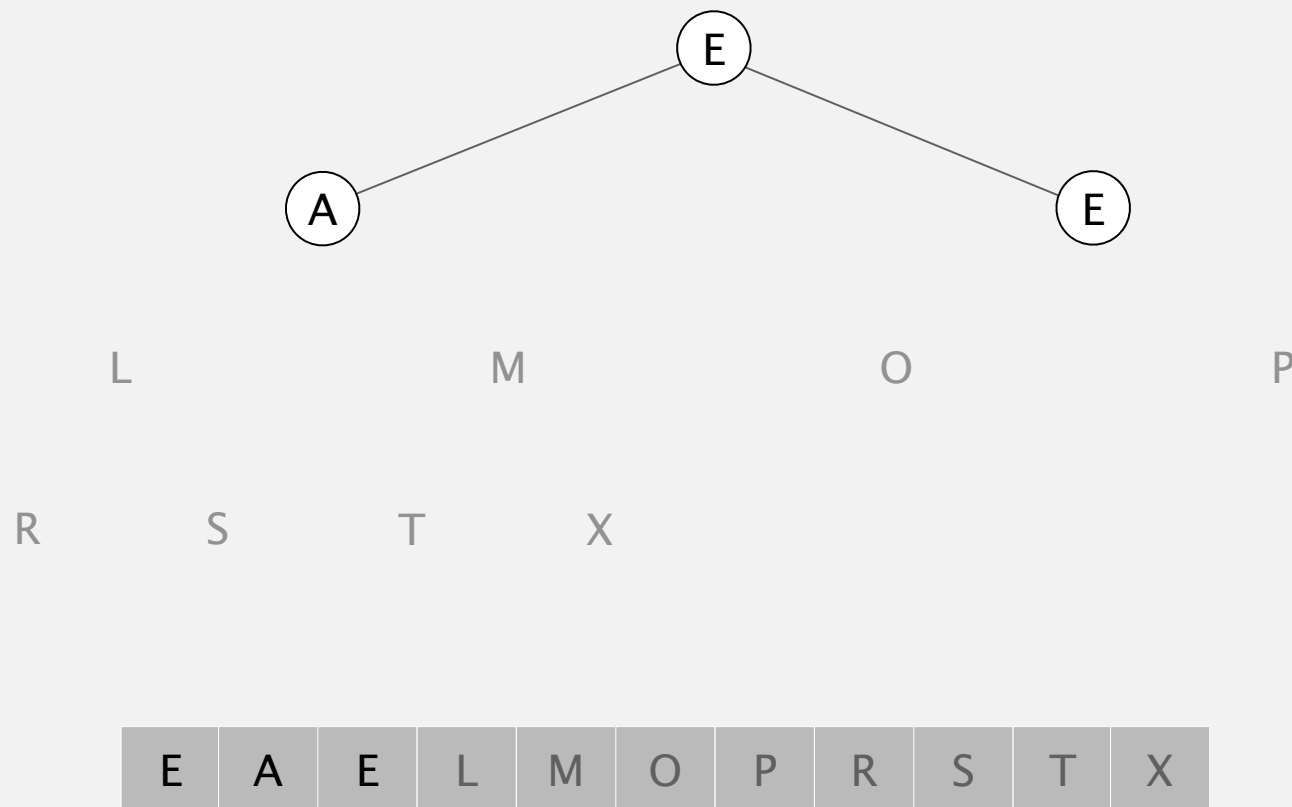




# Heapsort demo

---

**Sortdown.** Repeatedly delete the largest remaining item.



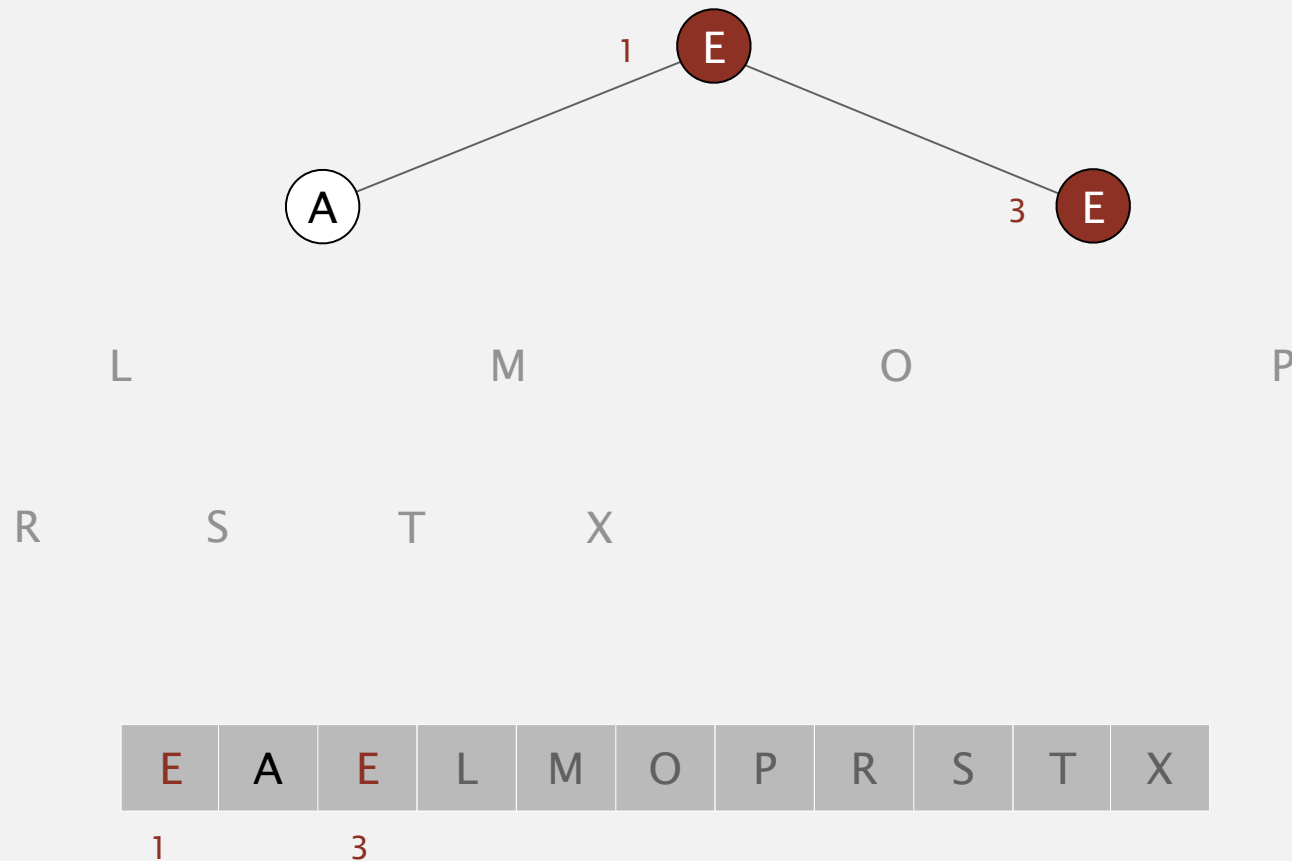


# Heapsort demo

---

**Sortdown.** Repeatedly delete the largest remaining item.

exchange 1 and 3

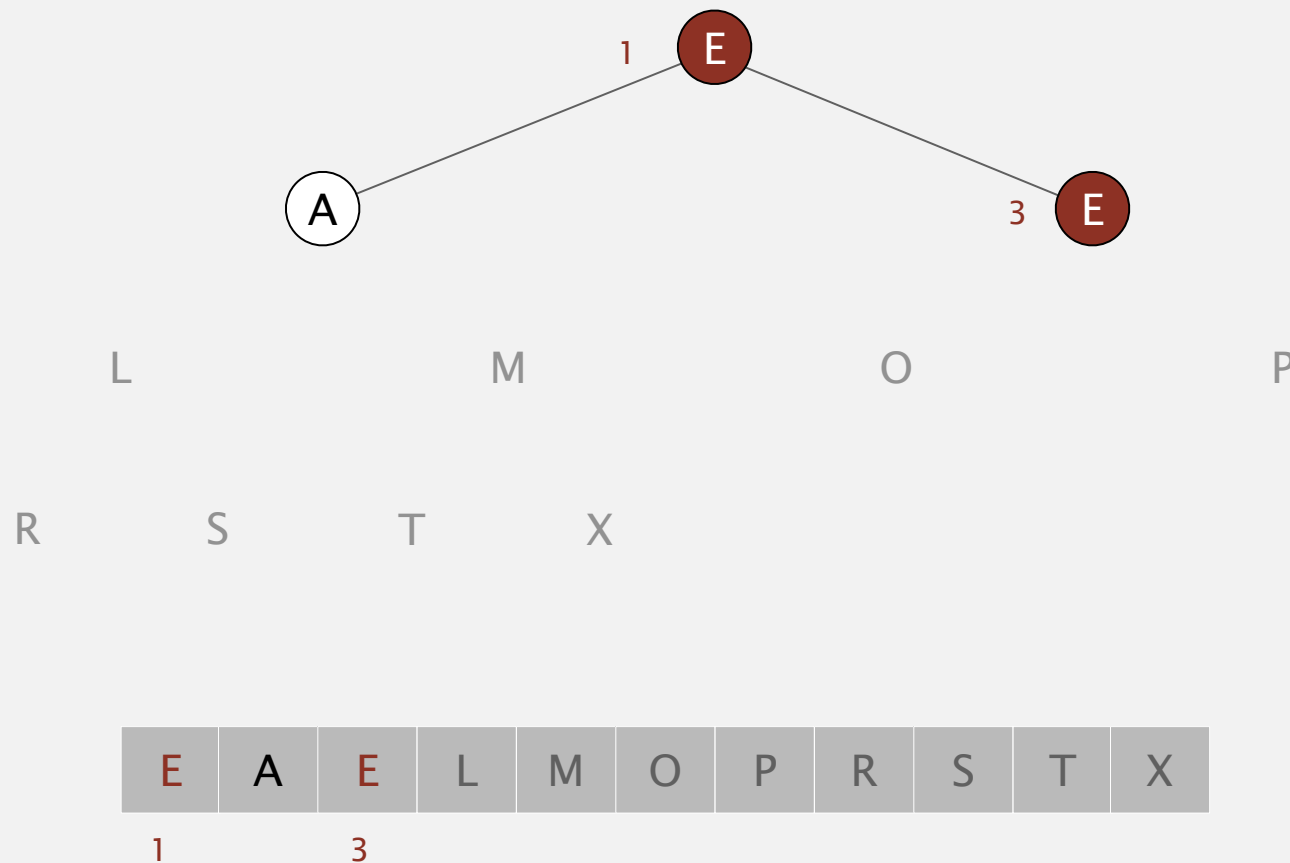


# Heapsort demo

---

**Sortdown.** Repeatedly delete the largest remaining item.

exchange 1 and 3

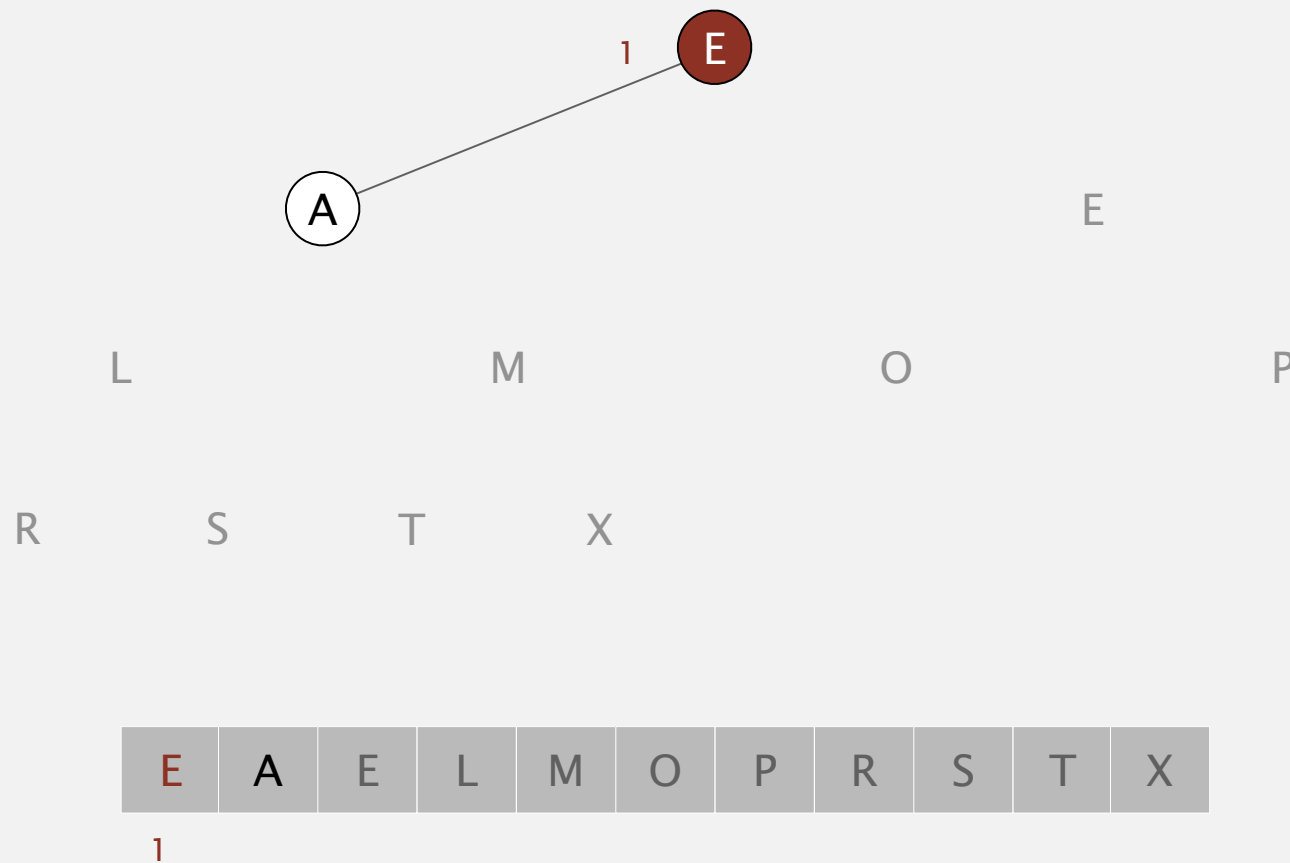


# Heapsort demo

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**Sortdown.** Repeatedly delete the largest remaining item.

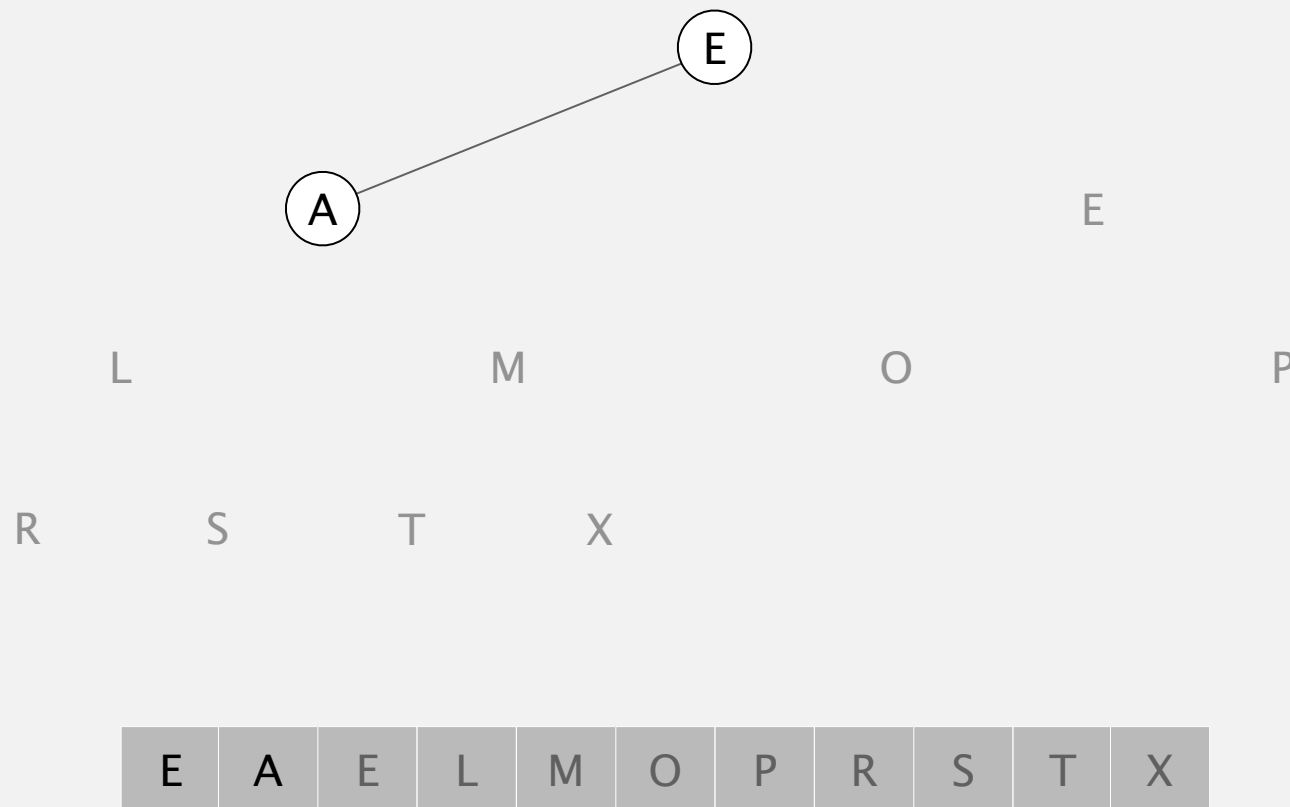
**sink 1**



# Heapsort demo

---

**Sortdown.** Repeatedly delete the largest remaining item.

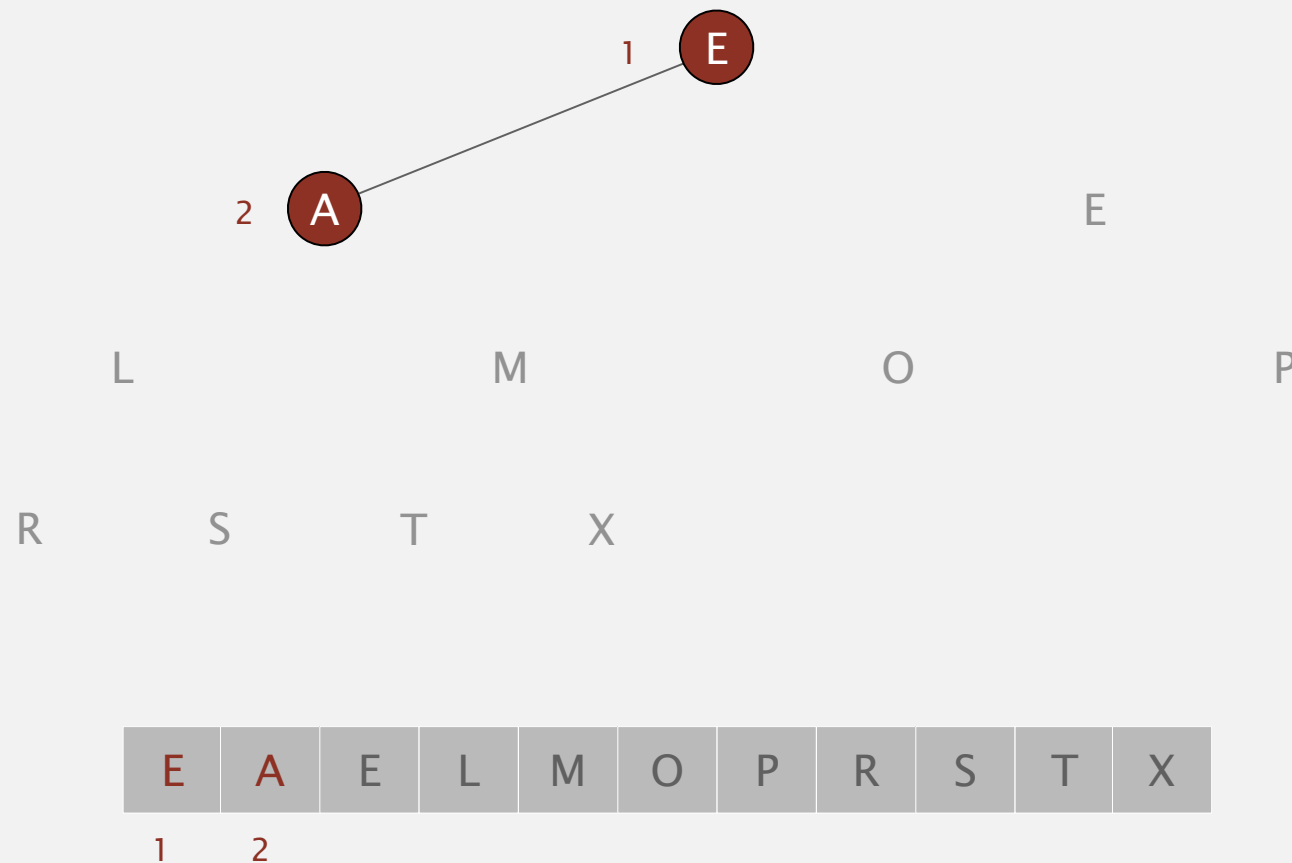


# Heapsort demo

---

**Sortdown.** Repeatedly delete the largest remaining item.

exchange 1 and 2

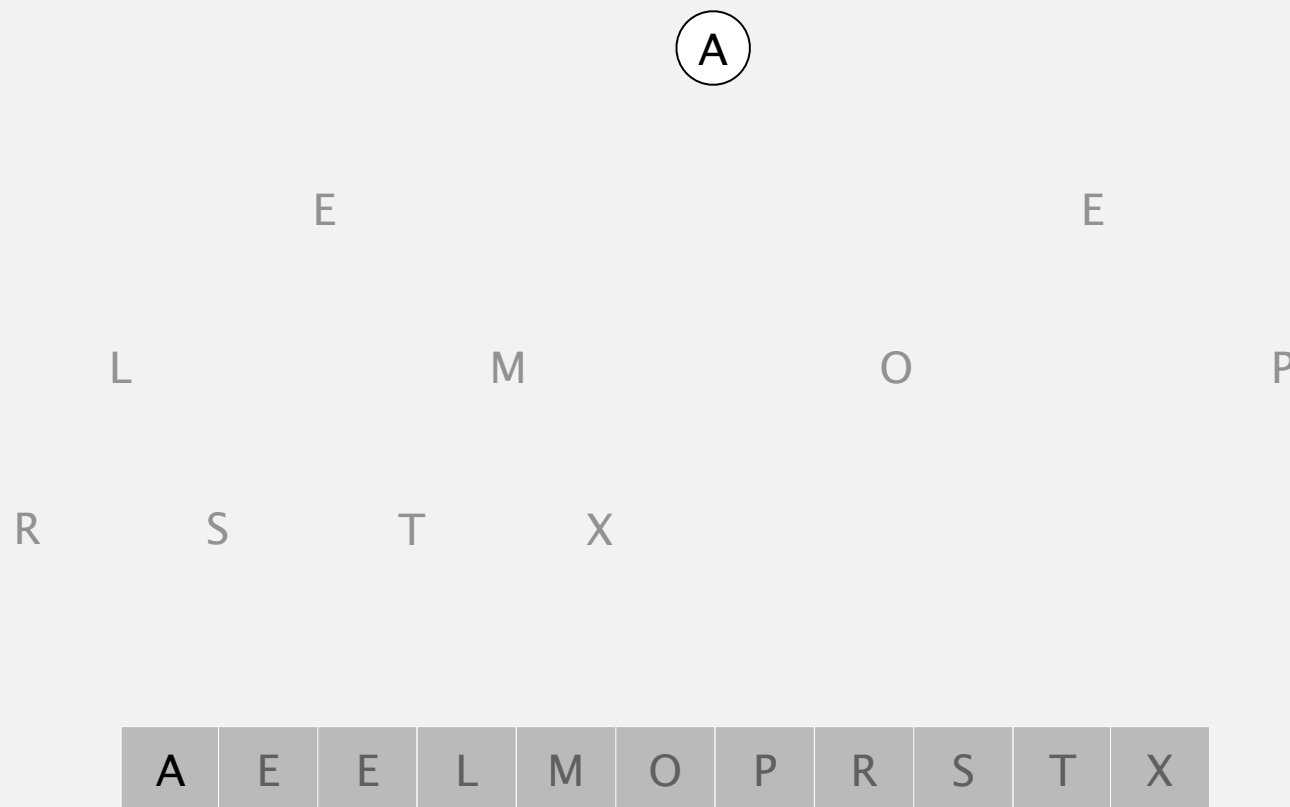




# Heapsort demo

---

**Sortdown.** Repeatedly delete the largest remaining item.



# Heapsort demo

---

**Sortdown.** Repeatedly delete the largest remaining item.

**end of sortdown phase**





# Heapsort demo

---

**Sortdown.** Repeatedly delete the largest remaining item.

array in sorted order



A	E	E	L	M	O	P	R	S	T	X
1	2	3	4	5	6	7	8	9	10	11