

HOMEWORK

4.10 (20pts)

Compute the bits number 4, 17, 41, and 45 at the output of the first round of the DES decryption, assuming that the ciphertext block is composed of all ones and the external key is composed of all ones.

Main key $K = 11111111\ 11111111\ 11111111\ 11111111\ 11111111\ 11111111\ 11111111\ 11111111 \rightarrow 56$ bits

$K_1 = K_2 = \dots = K_{16} = 11111111\ 11111111\ 11111111\ 11111111\ 11111111\ 11111111\ 11111111\ 11111111$ (48 bits)

$C = 11111111\ 11111111\ 11111111\ 11111111\ 11111111\ 11111111\ 11111111\ 11111111$

$C_{\text{Left}} = 11111111\ 11111111\ 11111111\ 11111111$

$C_{\text{Right}} = 11111111\ 11111111\ 11111111\ 11111111$

32 bit to 48 bit

$E(\text{Right}) = 11111111\ 11111111\ 11111111\ 11111111\ 11111111\ 11111111$

Inside of the function F ,

$E(RD_0) + K_{16} = 00000000\ 00000000\ 00000000\ 00000000\ 00000000\ 00000000\ 00000000\ 00000000$

Permutation

$B = 11101111101001110010110001001101$

$P(B) = 11011000110110001101101110111100$

$R_1 = 00100111\ 00100111\ 00100100\ 01000011$

$L_1 = 11111111\ 11111111\ 11111111\ 11111111$

so $\rightarrow 11111111\ 11111111\ 11111111\ 11111111\ 00100111\ 00100111\ 00100100\ 01000011$

$4 \rightarrow 1$

$17 \rightarrow 1$

$41 \rightarrow 0$

$45 \rightarrow 0$

- 4.11 This problem provides a numerical example of encryption using a one-round version of DES. We start with the same bit pattern for the key K and the plaintext, namely:

Hexadecimal notation: 0 1 2 3 4 5 6 7 8 9 A B C D E F
Binary notation: 0000 0001 0010 0011 0100 0101 0110 0111
 1000 1001 1010 1011 1100 1101 1110 1111

- Derive K_1 , the first-round subkey.
- Derive L_0, R_0 .
- Expand R_0 to get $E[R_0]$, where $E[\cdot]$ is the expansion function of Table S.1.
- Calculate $A = E[R_0] \oplus K_1$.
- Group the 48-bit result of (d) into sets of 6 bits and evaluate the corresponding S-box substitutions.
- Concatenate the results of (e) to get a 32-bit result, B .

CHAPTER 4 / BLOCK CIPHERS AND THE DATA ENCRYPTION STANDARD

- Apply the permutation to get $P(B)$.
- Calculate $R_1 = P(B) \oplus L_0$.
- Write down the ciphertext.

$M = 0000\ 0001\ 0010\ 0011\ 0100\ 0101\ 0110\ 0111\ 1000\ 1001\ 1010\ 1011\ 1100\ 1101\ 1110\ 1111$

$K = 0000\ 0001\ 0010\ 0011\ 0100\ 0101\ 0110\ 0111\ 1000\ 1001\ 1010\ 1011\ 1100\ 1101\ 1110\ 1111$

From the original 64 bit key \rightarrow 56 bit key

$K^+ = 1111\ 0000\ 1100\ 1100\ 1010\ 1010\ 0000\ 1010\ 1010\ 1100\ 1100\ 1111\ 0000\ 0000$

$C_0 = 1111000011001100101010100000$

$D_0 = 1010101011001100111100000000$

| | |
|--|--|
| $C_1 = 1110\ 0001\ 1001\ 1001\ 0101\ 0100\ 0001$ $D_1 = 0101\ 0101\ 1001\ 1001\ 1110\ 0000\ 0001$ | We apply PC-2 to $K_n = C_n D_n$ $K_1 = 0000\ 1011\ 0000\ 0010\ 0110\ 0111\ 1001$ $1011\ 0100\ 1001\ 1010\ 0101$ |
|--|--|

$M = 0000\ 0001\ 0010\ 0011\ 0100\ 0101\ 0110\ 0111\ 1000\ 1001\ 1010\ 1011\ 1100\ 1101\ 1110\ 1111$

$IP = 1100\ 1100\ 0000\ 0000\ 1100\ 1100\ 1111\ 1111\ 1111\ 0000\ 1010\ 1010\ 1111\ 0000\ 1010\ 1010$

$L_0 = 1100\ 1100\ 0000\ 0000\ 1100\ 1100\ 1111\ 1111$

$R_0 = 1111\ 0000\ 1010\ 1010\ 1111\ 0000\ 1010\ 1010$

$$L_n = R_{n-1}$$

$$R_n = L_{n-1} + f(R_{n-1}, K_n)$$

$$K_1 = 0000\ 1011\ 0000\ 0010\ 0110\ 0111\ 1001\ 1011\ 0100\ 1001\ 1010\ 0101$$

$$L_1 = R_0 = 1111\ 0000\ 1010\ 1010\ 1111\ 0000\ 1010\ 1010$$

$$R_1 = L_0 + f(R_0, K_1) = 1100\ 1100\ 0000\ 0000\ 1100\ 1100\ 1111\ 1111 \text{ xor } f(R_0, K_1)$$

$$E(R_0) = 0111\ 1010\ 0001\ 0101\ 0101\ 0101\ 0111\ 1010\ 0001\ 0101\ 0101\ 0101$$

$$K_1 + E(R_0) = 011100\ 010001\ 011100\ 110010\ 111000\ 010101\ 110011\ 110000$$

$$B_1 = 0\ 1110\ 0 \rightarrow \text{row is } 00 = 0, \text{ rest is } 1110 = \text{column number } 14 \rightarrow 0000$$

$$B_2 = 0\ 1000\ 1 \rightarrow \text{row is } 01 = 1, \text{ rest is } 1000 = \text{column number } 8 \rightarrow 1100$$

$$B_3 = 0\ 1110\ 0 \rightarrow \text{row is } 00 = 0, \text{ rest is } 1110 = \text{column number } 14 \rightarrow 0010$$

$$B_4 = 1\ 1001\ 0 \rightarrow \text{row is } 10 = 2, \text{ rest is } 1001 = \text{column number } 9 \rightarrow 0001$$

$$B_5 = 1\ 1100\ 0 \rightarrow \text{row is } 10 = 2, \text{ rest is } 1100 = \text{column number } 12 \rightarrow 0110$$

$$B_6 = 0\ 1010\ 1 \rightarrow \text{row is } 01 = 1, \text{ rest is } 1010 = \text{column number } 10 \rightarrow 1101$$

$$B_7 = 1\ 1001\ 1 \rightarrow \text{row is } 11 = 3, \text{ rest is } 1001 = \text{column number } 9 \rightarrow 0101$$

$$B_8 = 1\ 1000\ 0 \rightarrow \text{row is } 10 = 2, \text{ rest is } 1000 = \text{column number } 8 \rightarrow 0000$$

$$S_1(B_1)S_2(B_2)S_3(B_3)S_4(B_4)S_5(B_5)S_6(B_6)S_7(B_7)S_8(B_8) = 00001100001000010110110101010000$$

After P

$$f = 1001\ 0010\ 0001\ 1100\ 0010\ 0000\ 1001\ 1100$$

$$R_1 = L_0 + f(R_0, K_1)$$

$$R_1 = 1100\ 1100\ 0000\ 0000\ 1100\ 1100\ 1111\ 1111 + 1001\ 0010\ 0001\ 1100\ 0010\ 0000\ 1001\ 1100$$

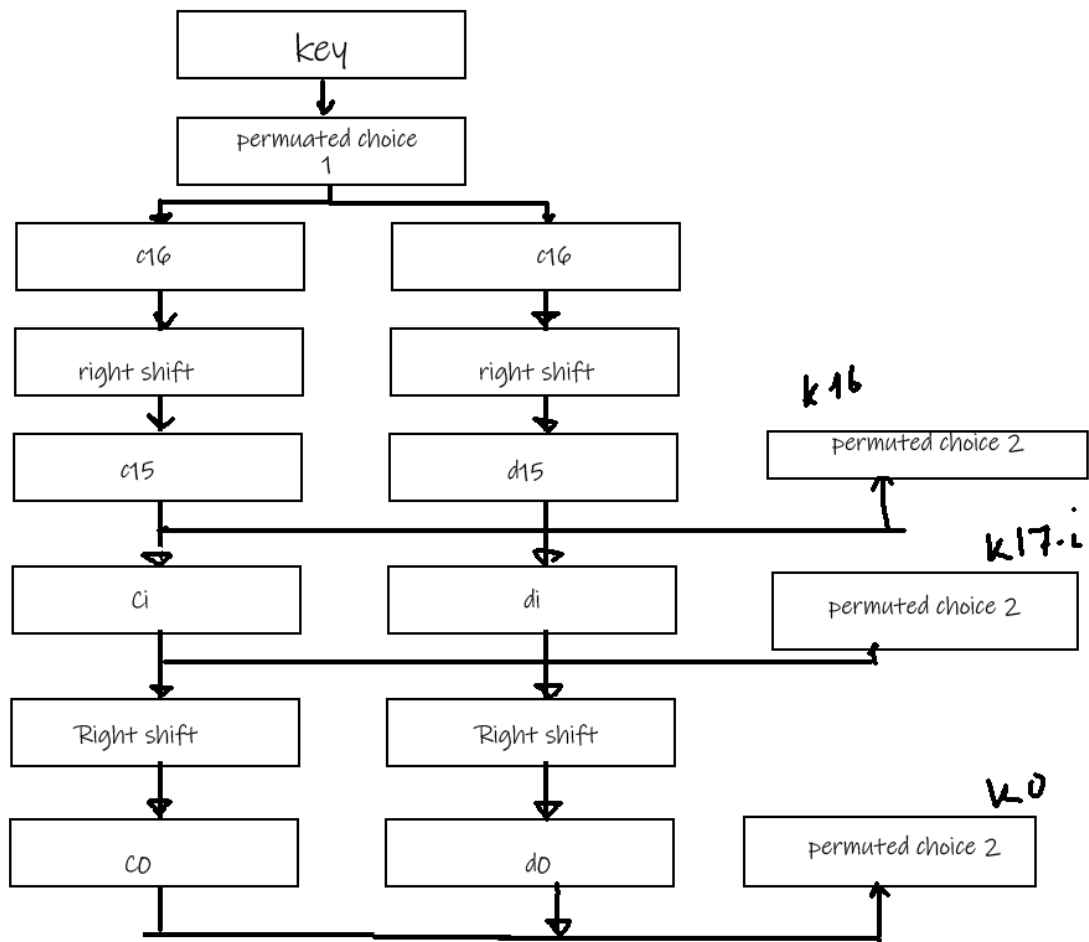
$$= 0101\ 1110\ 0001\ 1100\ 1110\ 1100\ 0110\ 0011$$

$$R_1L_1 = 0101111000011100111011000110001111110000101010101111000010101010$$

$$IP^{-1} = 0000\ 0001\ 0110\ 0011\ 0101\ 0100\ 0111\ 0110\ 1101\ 1000\ 1010\ 1111\ 1100\ 1101\ 1010\ 1110$$

$$1635476D8AFCDAE$$

4.13 When using the DES algorithm for decryption, the 16 keys (K_1, K_2, \dots, K_{16}) are used in reverse order. Therefore, the right-hand side of Figure S.1 is not valid for decryption. Design a key-generation scheme with the appropriate shift schedule (analogous to Table S.3d) for the decryption process.



| | | | | | | | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|----|----|----|----|----|----|----|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 |
| 0 | 1 | 2 | 2 | 2 | 2 | 2 | 2 | 1 | 2 | 2 | 2 | 2 | 2 | 2 | 1 |

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$$M = 01000110$$

$$K = 1010000010$$

Subkeys

After P10 $K = 1000001100$

$$L_0 = 10000 \quad R_0 = 01100$$

Left shift 1

$$L_0 = 00001 \quad R_0 = 11000$$

After P8 we get $K_1 = 10100100$

Left shift 2 of Left shift 1

$$L_0 = 00100 \quad R_0 = 00011$$

After P8 we get $K_2 = 01000011$

We get our keys.

Message

Initial permutation of $M = 11000001 = IP$

Round 1

$$L = 1100 \quad R = 0001$$

• Expansion permutation $10000010 = EP$

$$• EP \oplus K_2 = \underbrace{1100}_{L} \underbrace{0001}_{R}$$

$\underbrace{1}_{S\text{-box } 0} \underbrace{0}_{01} \quad \underbrace{0}_{S\text{-box } 1} \underbrace{1}_{10} \Rightarrow \text{After P4 } 1010 \Rightarrow \text{XOR} \Rightarrow 0100$

$$fk_1 = 01100001 \quad \text{switch func} = 00010110$$

Round 2

- Let's split switch into 2

$$L = 0001 \quad R = 0110$$

- Apply expansion $EP_2 = 00111100$

$$\bullet EP_2 \oplus K_2 = \underbrace{1001}_L \underbrace{1000}_R$$

$$\bullet \begin{array}{r} S_{box0} \\ 11 \end{array} \quad \begin{array}{r} S_{box1} \\ 11 \end{array} \Rightarrow \text{After } P_4 = 1111 \Rightarrow \text{XOR} \Rightarrow 1110$$

$$fK_2 \text{ is } 11100110$$

$$IP^{-1} = \text{Result} = 01101101$$