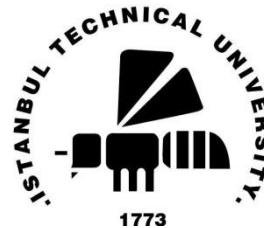


BLG435E

Artificial Intelligence



Lecture 7: Planning



- The Planning problem
- Planning with State-space search
- Partial-order planning

What is Planning

- Generate sequences of actions to perform tasks and achieve objectives.
 - States, actions and goals
- Search for solution over abstract space of plans.
- Classical planning environment: fully observable, deterministic, finite, static and discrete.
- Assists humans in practical applications
 - design and manufacturing
 - games
 - space exploration
 - military operations

Difficulty of real-world problems

- Assume a problem-solving agent using some search method ...
 - Which actions are relevant?
 - Exhaustive search vs. backward search
 - What is a good heuristic function?
 - Good estimate of the cost of the state?
 - Problem-dependent vs, -independent
 - How to decompose the problem?
 - Most real-world problems are ***nearly*** decomposable.

Planning language

- What is a good language?
 - **Expressive** enough to describe a wide variety of problems.
 - **Restrictive** enough to allow efficient algorithms to operate on it.
 - Planning algorithm should be able to take advantage of the logical structure of the problem.
- STRIPS and ADL

General language features

- Representation of states

- Decompose the world in logical conditions and represent a state as a *conjunction of positive literals*.
 - Propositional literals: $Poor \wedge Unknown$
 - FO-literals (ground and function-free): $At(Plane1, Melbourne) \wedge At(Plane2, Sydney)$
- Closed world assumption

- Representation of goals

- Partially specified state and represented as a *conjunction of positive ground literals*
 - $Poor \wedge Unknown \wedge At(P2, Tahiti)$
- A goal is *satisfied* if the state contains all literals in the goal.

General language features

- Representations of actions

- Action = PRECOND + EFFECT

- Action(Fly(p,from, to),*

- PRECOND: $At(p,from) \wedge Plane(p) \wedge Airport(from) \wedge Airport(to)$*

- EFFECT: $\neg AT(p,from) \wedge At(p,to)$*

- = action schema (p, from, to: need to be instantiated)

- Action name and parameter list
 - Precondition (conj. of function-free positive literals)
 - Effect (conj of function-free literals and P is True and not P is false)

- Add-list vs delete-list in Effect

Language semantics?

- How do actions affect states?

- An action is applicable in any state that satisfies the precondition.
- FO action schema applicability involves a substitution θ for the variables in the PRECOND.

$At(P1, JFK) \wedge At(P2, SFO) \wedge Plane(P1) \wedge Plane(P2) \wedge Airport(JFK) \wedge Airport(SFO)$

Satisfies : $At(p, from) \wedge Plane(p) \wedge Airport(from) \wedge Airport(to)$

With $\theta = \{p/P1, from/JFK, to/SFO\}$

Thus the action $Fly(P1, JFK, SFO)$ is applicable.

Language semantics?

- The result of executing action a in state s is the state s'

– s' is the same as s except

- Any positive literal P in the effect of a is added to s'
- Any negative literal $\neg P$ is removed from s'

EFFECT: $\neg AT(p, from) \wedge At(p, to)$:

*$At(P1, SFO) \wedge At(P2, SFO) \wedge Plane(P1) \wedge Plane(P2) \wedge$
 $Airport(JFK) \wedge Airport(SFO)$*

– STRIPS assumption: (avoids representational frame problem)

every literal NOT in the effect remains unchanged

Expressiveness and extensions

- STRIPS is simplified
 - Important limit: function-free literals
 - Allows for propositional representation
 - Function symbols lead to infinitely many states and actions
- Recent extension: Action Description language (ADL)

Action(Fly(p :Plane, from: Airport, to: Airport),

PRECOND: $At(p, from) \wedge (from \neq to)$

EFFECT: $\neg At(p, from) \wedge At(p, to)$

Standardization : *Planning domain definition language (PDDL)*

Example: air cargo transport

$Init(At(C1, SFO) \wedge At(C2, JFK) \wedge At(P1, SFO) \wedge At(P2, JFK) \wedge Cargo(C1) \wedge$
 $Cargo(C2) \wedge Plane(P1) \wedge Plane(P2) \wedge Airport(JFK) \wedge Airport(SFO))$
 $Goal(At(C1, JFK) \wedge At(C2, SFO))$

$Action(Load(c, p, a))$

PRECOND: $At(c, a) \wedge At(p, a) \wedge Cargo(c) \wedge Plane(p) \wedge Airport(a)$

EFFECT: $\neg At(c, a) \wedge In(c, p)$

$Action(Unload(c, p, a))$

PRECOND: $In(c, p) \wedge At(p, a) \wedge Cargo(c) \wedge Plane(p) \wedge Airport(a)$

EFFECT: $At(c, a) \wedge \neg In(c, p)$

$Action(Fly(p, from, to))$

PRECOND: $At(p, from) \wedge Plane(p) \wedge Airport(from) \wedge Airport(to)$

EFFECT: $\neg At(p, from) \wedge At(p, to)$

$[Load(C1, P1, SFO), Fly(P1, SFO, JFK), Load(C2, P2, JFK), Fly(P2, JFK, SFO)]$

Example: Spare tire problem

Init(*At*(Flat, Axle) \wedge *At*(Spare, trunk))

Goal(*At*(Spare, Axle))

Action(*Remove*(Spare, Trunk)

PRECOND: *At*(Spare, Trunk)

EFFECT: \neg *At*(Spare, Trunk) \wedge *At*(Spare, Ground))

Action(*Remove*(Flat, Axle)

PRECOND: *At*(Flat, Axle)

EFFECT: \neg *At*(Flat, Axle) \wedge *At*(Flat, Ground))

Action(*PutOn*(Spare, Axle)

PRECOND: *At*(Spare, Ground) \wedge \neg *At*(Flat, Axle)

EFFECT: *At*(Spare, Axle) \wedge \neg *At*(Spare, Ground))

Action(*LeaveOvernight*

PRECOND:

EFFECT: \neg *At*(Spare, Ground) \wedge \neg *At*(Spare, Axle) \wedge \neg *At*(Spare, trunk) \wedge \neg *At*(Flat, Ground) \wedge \neg *At*(Flat, Axle))



This example goes beyond STRIPS: negative literal in pre-condition (ADL description)

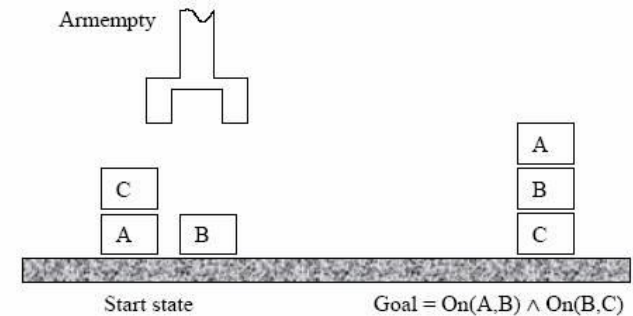
Example Spare tire problem - PDDL

Init(*Tire*(*Flat*) \wedge *Tire*(*Spare*) \wedge *At*(*Flat*, *Axle*) \wedge *At*(*Spare*, *Trunk*))
Goal(*At*(*Spare*, *Axle*))
Action(*Remove*(*obj*, *loc*),
 PRECOND: *At*(*obj*, *loc*)
 EFFECT: \neg *At*(*obj*, *loc*) \wedge *At*(*obj*, *Ground*))
Action(*PutOn*(*t*, *Axle*),
 PRECOND: *Tire*(*t*) \wedge *At*(*t*, *Ground*) \wedge \neg *At*(*Flat*, *Axle*)
 EFFECT: \neg *At*(*t*, *Ground*) \wedge *At*(*t*, *Axle*))
Action(*LeaveOvernight*,
 PRECOND:
 EFFECT: \neg *At*(*Spare*, *Ground*) \wedge \neg *At*(*Spare*, *Axle*) \wedge \neg *At*(*Spare*, *Trunk*)
 \wedge \neg *At*(*Flat*, *Ground*) \wedge \neg *At*(*Flat*, *Axle*) \wedge \neg *At*(*Flat*, *Trunk*))

Example: Blocks world

$Init(On(A, Table) \wedge On(B, Table) \wedge On(C, Table) \wedge Block(A) \wedge Block(B) \wedge Block(C) \wedge$
 $Clear(A) \wedge Clear(B) \wedge Clear(C))$

$Goal(On(A, B) \wedge On(B, C))$



$Action(Move(b, x, y))$

PRECOND: $On(b, x) \wedge Clear(b) \wedge Clear(y) \wedge Block(b) \wedge (b \neq x)$
 $\wedge (b \neq y) \wedge (x \neq y)$

EFFECT: $On(b, y) \wedge Clear(x) \wedge \neg On(b, x) \wedge \neg Clear(y)$

$Action(MoveToTable(b, x))$

PRECOND: $On(b, x) \wedge Clear(b) \wedge Block(b) \wedge (b \neq x)$

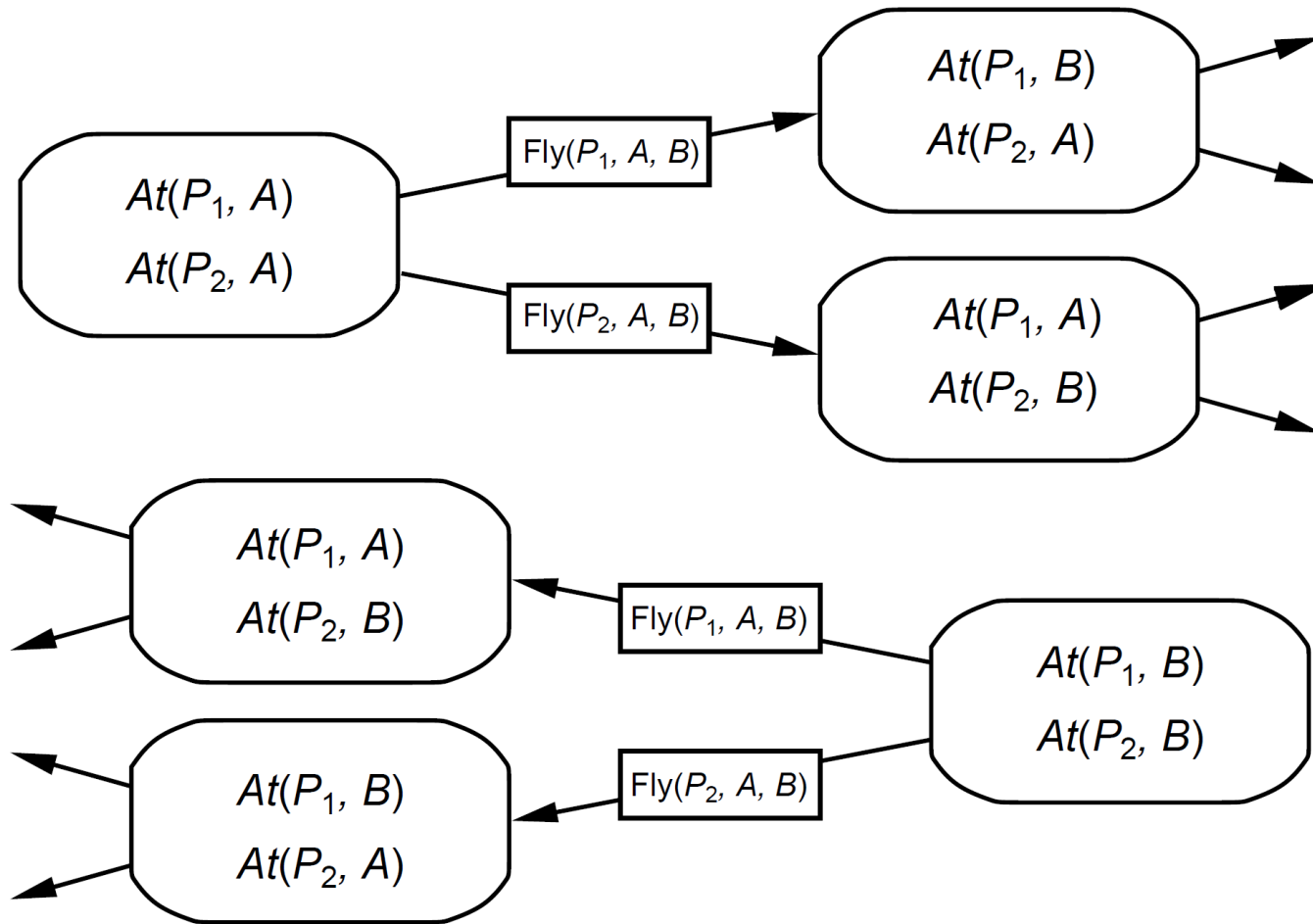
EFFECT: $On(b, Table) \wedge Clear(x) \wedge \neg On(b, x)$

Spurious actions are possible: $Move(B, C, C)$

Planning with state-space search

- Both forward and backward search possible
- Progression planners
 - forward state-space search
 - Consider the effects of all possible actions in a given state
- Regression planners
 - backward state-space search
 - To achieve a goal, what must have been true in the previous state.

Progression and regression



Progression algorithm

- Formulation as state-space search problem:
 - Initial state = initial state of the planning problem
 - Literals not appearing are false
 - Actions = those whose preconditions are satisfied
 - Add positive effects, delete negative
 - Goal test = does the state satisfy the goal
 - Step cost = each action costs 1
- No functions ... any graph search that is complete is a complete planning algorithm.
 - e.g. A*
- Inefficient:
 - (1) irrelevant action problem
 - (2) good heuristic is required for efficient search

Regression algorithm

- How to determine predecessors?
 - What are the states from which applying a given action leads to the goal?
Goal state = $At(C1, B) \wedge At(C2, B) \wedge \dots \wedge At(C20, B)$
Relevant action for the first conjunct: $Unload(C1, p, B)$
Works only if pre-conditions are satisfied.
Previous state = $In(C1, p) \wedge At(p, B) \wedge At(C2, B) \wedge \dots \wedge At(C20, B)$
Subgoal $At(C1, B)$ should not be present in this state.
- Actions must not undo desired literals (consistent)
- Main advantage: only relevant actions are considered.
 - Often much lower branching factor than forward search.

Regression algorithm

- General process for predecessor construction
 - Give a goal description G
 - Let A be an action that is relevant and consistent
 - The predecessors is as follows:
 - Any positive effects of A that appear in G are deleted.
 - Each precondition literal of A is added , unless it already appears.
- Any standard search algorithm can be used to perform the search.
- Termination when predecessor is satisfied by the initial state.
 - In FO case, satisfaction might require a substitution.

Heuristics for state-space search

- Neither progression nor regression are very efficient without a good heuristic.
 - How many actions are needed to achieve the goal?
 - Exact solution is NP hard, find a good estimate
- Two approaches to find admissible heuristic:
 - The optimal solution to the relaxed problem.
 - Remove all preconditions from actions
 - The subgoal independence assumption:

The cost of solving a conjunction of subgoals is approximated by the sum of the costs of solving the subproblems independently.

Partial-order planning

- Progression and regression planning are *totally ordered plan search* forms.
 - They cannot take advantage of problem decomposition.
 - Decisions must be made on how to sequence actions on all the subproblems
- Least commitment strategy:
 - Delay choice during search

Shoe example

Goal(RightShoeOn \wedge LeftShoeOn)

Init()

Action(RightShoe, PRECOND: RightSockOn

 EFFECT: RightShoeOn)

Action(RightSock, PRECOND:

 EFFECT: RightSockOn)

Action(LeftShoe, PRECOND: LeftSockOn

 EFFECT: LeftShoeOn)

Action(LeftSock, PRECOND:

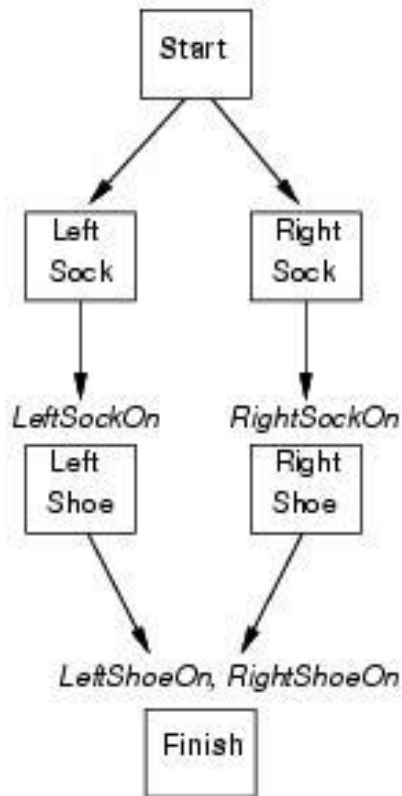
 EFFECT: LeftSockOn)

Planner: combine two action sequences (1)leftsock,
leftshoe (2)rightsock, rightshoe

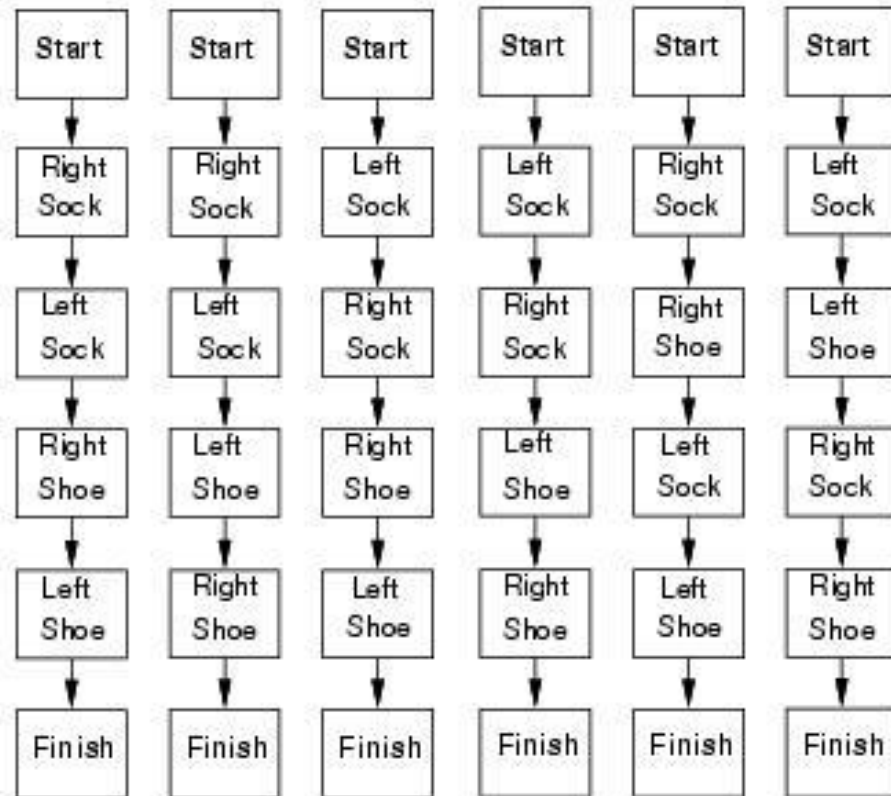
Partial-order planning (POP)

- Any planning algorithm that can place two actions into a plan without specifying the orders is a PO planner.

Partial Order Plan:



Total Order Plans:



- linearization

POP as a search problem

- States are (mostly unfinished) plans.
 - The empty plan contains only start and finish actions.
- Each plan has 4 components:
 - A set of actions (steps of the plan)
 - A set of ordering constraints: $A < B$ (A before B)
 - Cycles represent contradictions.
 - A set of causal links
 - The plan may not be extended by adding a new action C that conflicts with the causal link. (if the effect of C is $\neg p$ and if C could come after A and before B)
 - A set of open preconditions.
 - If precondition is not achieved by actions in the plan.

Example of final plan

- Actions={Rightsock, Rightshoe, Leftsock, Leftshoe, Start, Finish}
- Orderings={Rightsock < Rightshoe; Leftsock < Leftshoe}
- Links={Rightsock->Rightsockon -> Rightshoe,
Leftsock->Leftsockon-> Leftshoe,
Rightshoe->Rightshoeon->Finish, ...}
- Open preconditions={}

POP as a search problem

- A plan is *consistent* iff there are no cycles in the ordering constraints and no conflicts with the causal links.
- A consistent plan with no open preconditions is a *solution*.
- A partial order plan is executed by repeatedly choosing *any* of the possible next actions.

- Assume propositional planning problems:
 - The initial plan contains *Start* and *Finish*, the ordering constraint $Start < Finish$, no causal links, all the preconditions in *Finish* are open.
 - Successor function :
 - picks one open precondition p on an action B and
 - generates a successor plan for every possible consistent way of choosing action A that achieves p .
 - Test goal

- When generating successor plan:
 - The causal link $A \xrightarrow{p} B$ and the ordering constraint $A < B$ is added to the plan.
 - If A is new, also add $\text{start} < A$ and $A < B$ to the plan
 - Resolve conflicts between new causal link and all existing actions
 - Resolve conflicts between action A (if new) and all existing causal links.
 - If a conflict between the casual link and action C
 - either add $C < A$ or $B < C$

- Operators on partial plans
 - Add link from existing plan to open precondition.
 - Add a step to fulfill an open condition.
 - Order one step w.r.t another to remove possible conflicts
- Gradually move from incomplete/vague plans to complete/correct plans
- Backtrack if an open condition is unachievable or if a conflict is irresolvable.

Example: Spare tire problem

Init(*At*(*Flat*, *Axle*) \wedge *At*(*Spare*, *trunk*))

Goal(*At*(*Spare*, *Axle*))

Action(*Remove*(*Spare*, *Trunk*))

PRECOND: *At*(*Spare*, *Trunk*)

EFFECT: \neg *At*(*Spare*, *Trunk*) \wedge *At*(*Spare*, *Ground*))

Action(*Remove*(*Flat*, *Axle*))

PRECOND: *At*(*Flat*, *Axle*)

EFFECT: \neg *At*(*Flat*, *Axle*) \wedge *At*(*Flat*, *Ground*))

Action(*PutOn*(*Spare*, *Axle*))

PRECOND: *At*(*Spare*, *Ground*) \wedge \neg *At*(*Flat*, *Axle*)

EFFECT: *At*(*Spare*, *Axle*) \wedge \neg *At*(*Spare*, *Ground*))

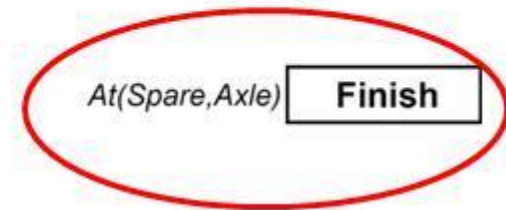
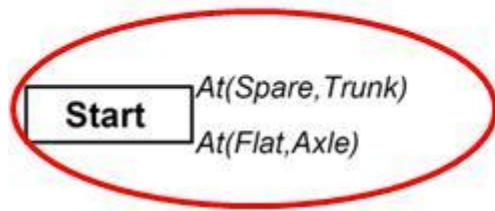
Action(*LeaveOvernight*)

PRECOND:

EFFECT: \neg *At*(*Spare*, *Ground*) \wedge \neg *At*(*Spare*, *Axle*) \wedge \neg *At*(*Spare*, *trunk*) \wedge \neg *At*(*Flat*, *Ground*) \wedge \neg *At*(*Flat*, *Axle*))

Solving the problem

- Initial plan: Start with EFFECTS and Finish with PRECOND.



Solving the problem

- Initial plan: Start with EFFECTS and Finish with PRECOND.
- Pick an open precondition: *At(Spare, Axle)*

Start *At(Spare, Trunk)*
At(Flat, Axle)

At(Spare, Axle) **Finish**

Example: Spare tire problem

Init(*At*(*Flat*, *Axle*) \wedge *At*(*Spare*, *trunk*))

Goal(*At*(*Spare*, *Axle*))

Action(*Remove*(*Spare*, *Trunk*))

PRECOND: *At*(*Spare*, *Trunk*)

EFFECT: \neg *At*(*Spare*, *Trunk*) \wedge *At*(*Spare*, *Ground*))

Action(*Remove*(*Flat*, *Axle*))

PRECOND: *At*(*Flat*, *Axle*)

EFFECT: \neg *At*(*Flat*, *Axle*) \wedge *At*(*Flat*, *Ground*))

Action(*PutOn*(*Spare*, *Axle*))

PRECOND: *At*(*Spare*, *Ground*) \wedge \neg *At*(*Flat*, *Axle*)

EFFECT: *At*(*Spare*, *Axle*) \wedge \neg *At*(*Spare*, *Ground*))

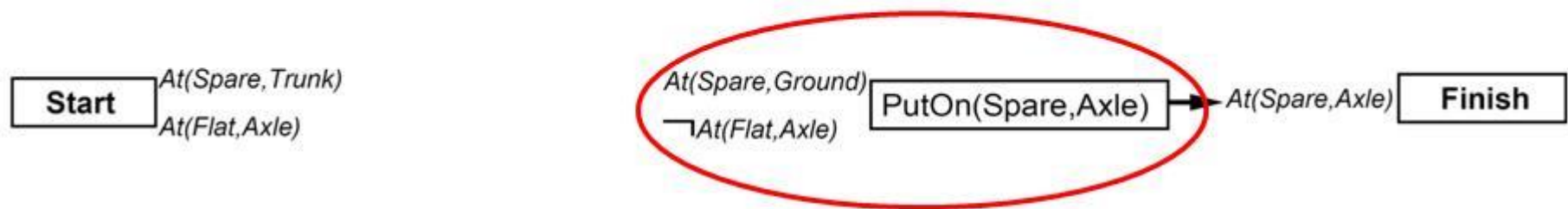
Action(*LeaveOvernight*)

PRECOND:

EFFECT: \neg *At*(*Spare*, *Ground*) \wedge \neg *At*(*Spare*, *Axle*) \wedge \neg *At*(*Spare*, *trunk*) \wedge \neg *At*(*Flat*, *Ground*) \wedge \neg *At*(*Flat*, *Axle*))

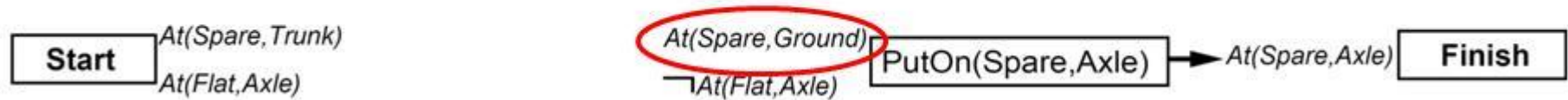
Solving the problem

- Pick an open precondition: $At(Spare, Axle)$
- Only $PutOn(Spare, Axle)$ is applicable
- Add constraint : $PutOn(Spare, Axle) < Finish$
- Add causal link: $PutOn(Spare, Axle) \xrightarrow{At(Spare, Axle)} Finish$



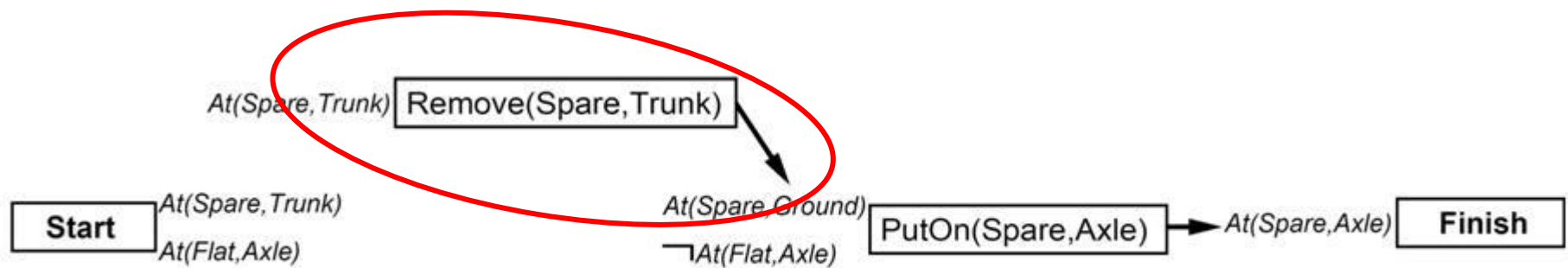
Solving the problem

- Pick an open precondition: *At(Spare, Ground)*



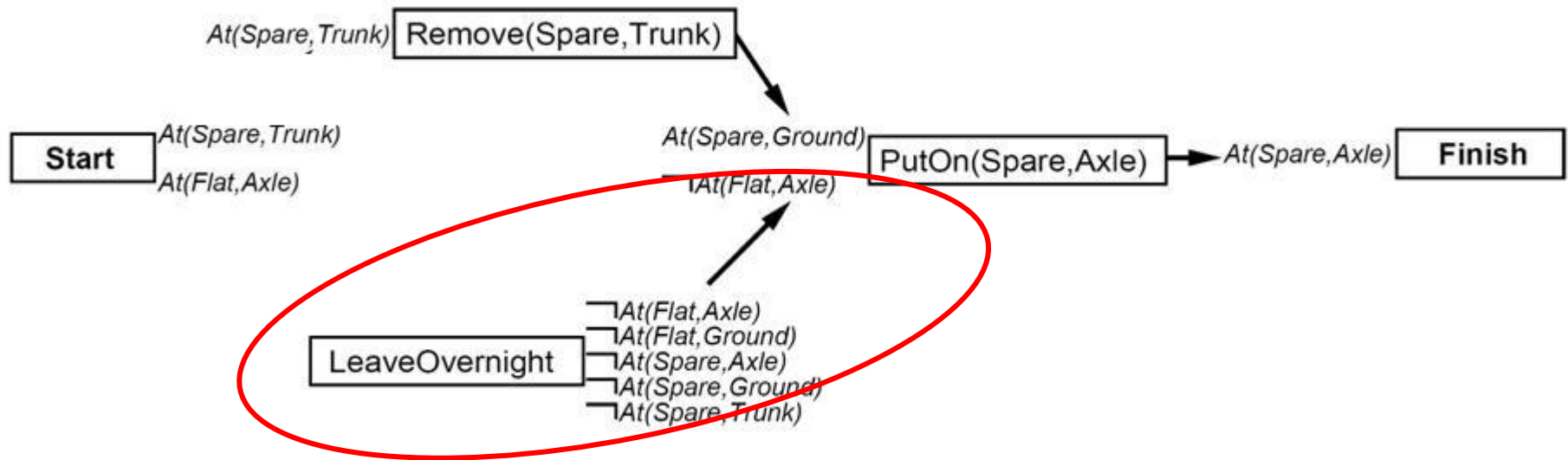
Solving the problem

- Pick an open precondition: $At(Spare, Ground)$
- Only $Remove(Spare, Trunk)$ is applicable
- Add causal link: $Remove(Spare, Trunk) \xrightarrow{At(Spare, Ground)} PutOn(Spare, Axle)$
- Add constraint : $Remove(Spare, Trunk) < PutOn(Spare, Axle)$



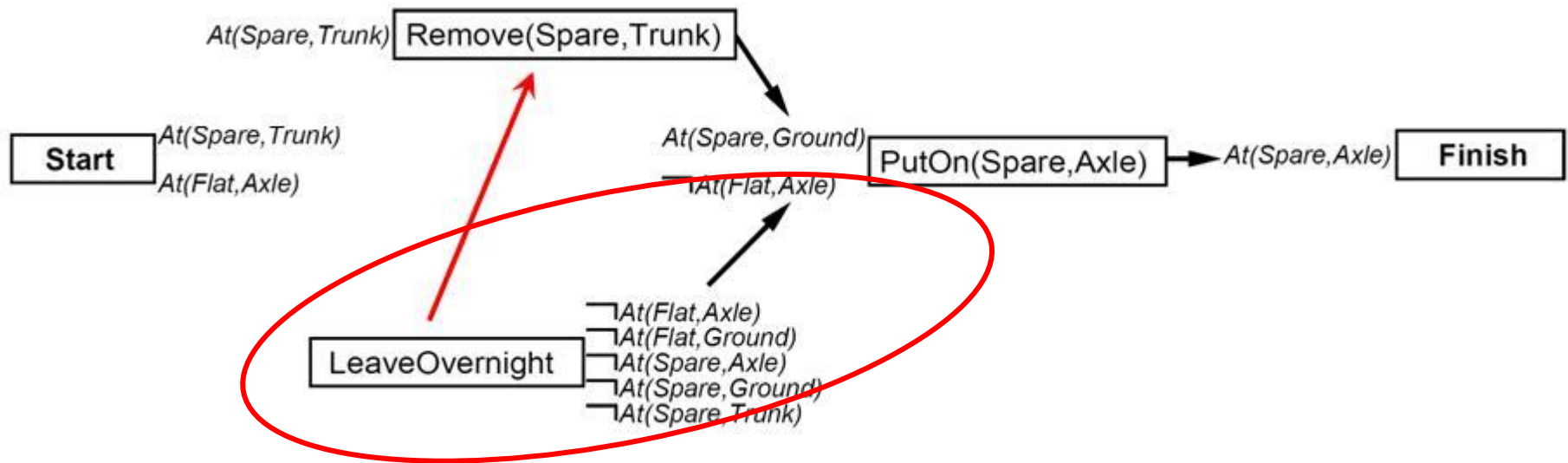
Solving the problem

- Pick an open precondition: $\neg At(Flat, Axle)$
- *LeaveOverNight* is applicable
- Add causal link: $LeaveOverNight \xrightarrow{\neg At(Flat, Axle)} PutOn(Spare, Axle)$
- Is there any conflict?



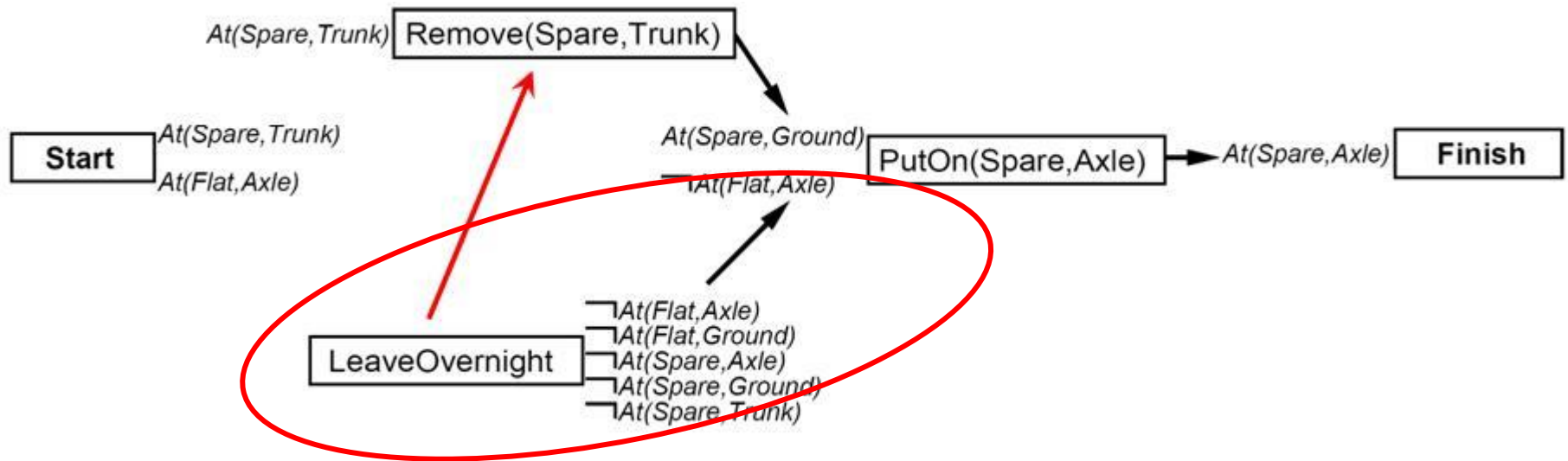
Solving the problem

- *LeaveOverNight* is applicable
- conflict: *LeaveOverNight* also has the effect $\neg \text{At}(\text{Spare}, \text{Ground})$
- To resolve, add constraint : *LeaveOverNight* < *Remove(Spare, Trunk)*



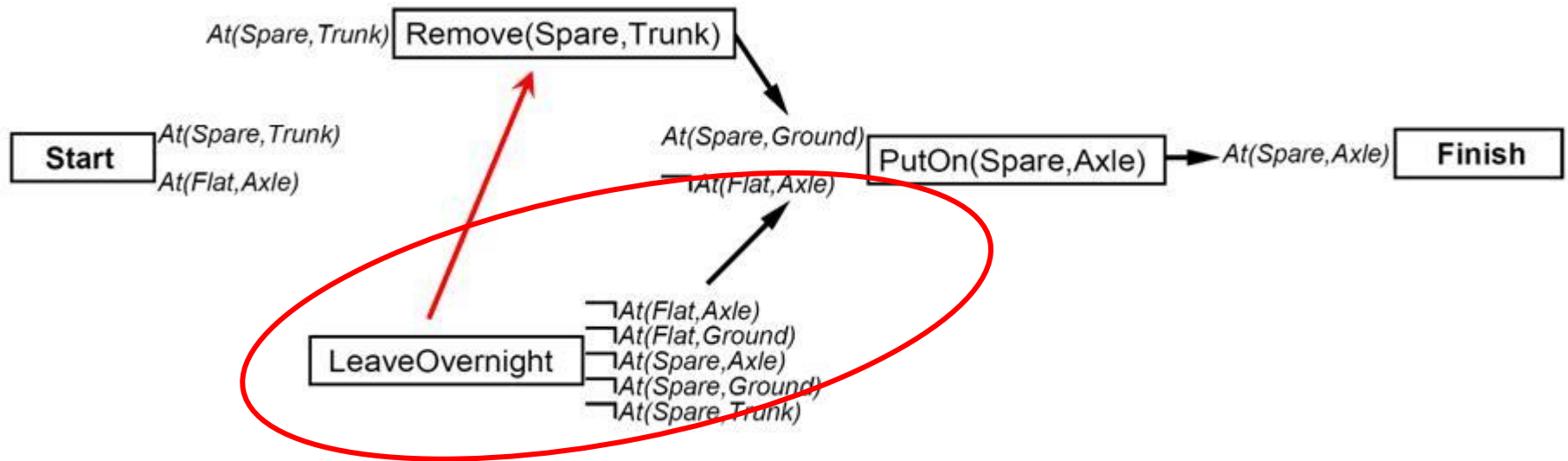
Solving the problem

- To resolve, add constraint : $LeaveOverNight < Remove(Spare, Trunk)$
- Add causal link: $LeaveOverNight \xrightarrow{\neg At(Spare, Ground)} Remove(Spare, Trunk)$



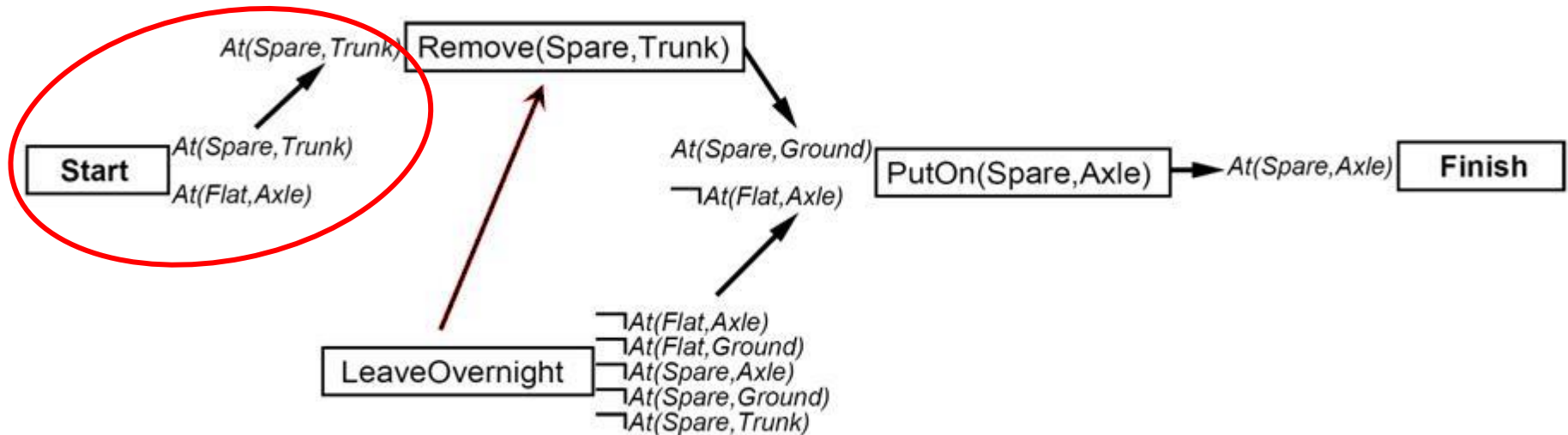
Solving the problem

- Pick an open precondition: *At(Spare, Trunk)*



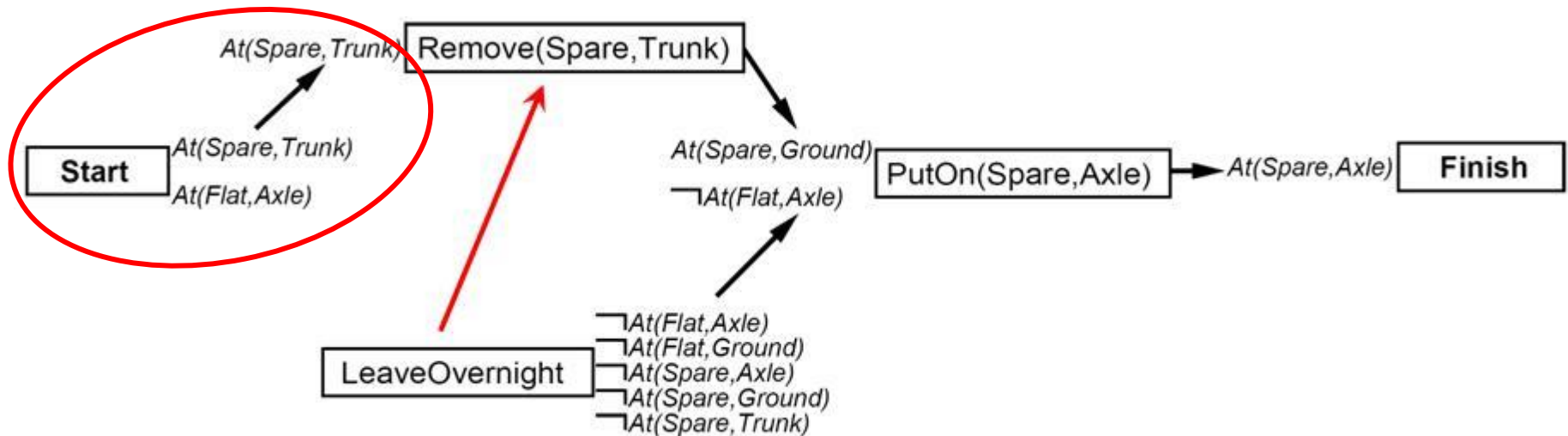
Solving the problem

- Only Start is applicable
- Add causal link: $Start \xrightarrow{At(Spare, Trunk)} Remove(Spare, Trunk)$
- Is there any conflict?



Solving the problem

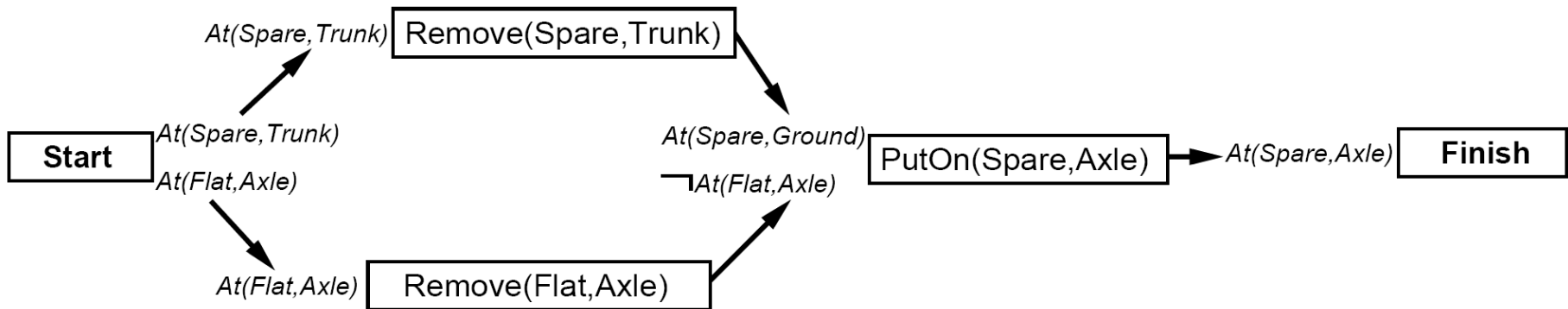
- Only Start is applicable
- Add causal link: $Start \xrightarrow{At(Spare, Trunk)} Remove(Spare, Trunk)$
- Conflict of causal link with effect $\neg At(Spare, Trunk)$ in LeaveOverNight



- No re-ordering solution possible, backtrack

Solving the problem

- Remove *LeaveOverNight*, *Remove(Spare, Trunk)* and causal links
- Repeat step with *Remove(Spare,Trunk)*
- Add also *Remove(Flat,Axle)* and finish



Some details ...

- What happens when a first-order representation that includes variables is used?
 - Complicates the process of detecting and resolving conflicts.
 - Can be resolved by introducing inequality constraints.
- CSP's most-constrained-variable constraint can be used for planning algorithms to select a PRECOND.

Planning graphs

- Used to achieve better heuristic estimates.
 - A solution can also be directly extracted using GRAPHPLAN.
- Consists of a sequence of levels that correspond to time steps in the plan.
 - Level 0 is the initial state.
 - Each level consists of a set of literals and a set of actions.
 - *Literals* = all those that **could** be true at that time step, depending upon the actions executed at the preceding time step.
 - *Actions* = all those actions that **could** have their preconditions satisfied at that time step, depending on which of the literals actually hold.

Planning graphs

- They work only for propositional problems.
- Example:

Init(Have(Cake))

Goal(Have(Cake) \wedge Eaten(Cake))

Action(Eat(Cake), PRECOND: Have(Cake)

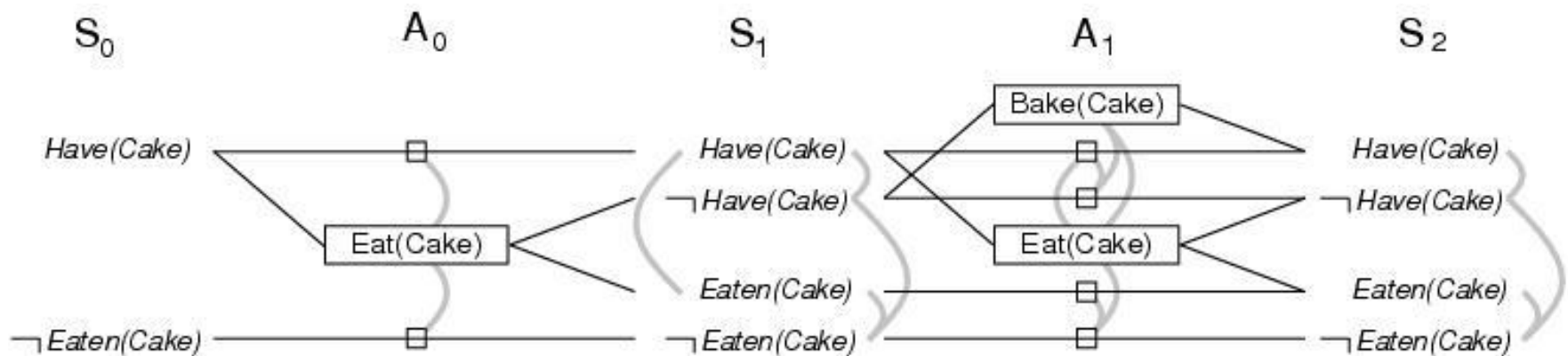
EFFECT: \neg Have(Cake) \wedge Eaten(Cake))

Action(Bake(Cake), PRECOND: \neg Have(Cake)

EFFECT: Have(Cake))

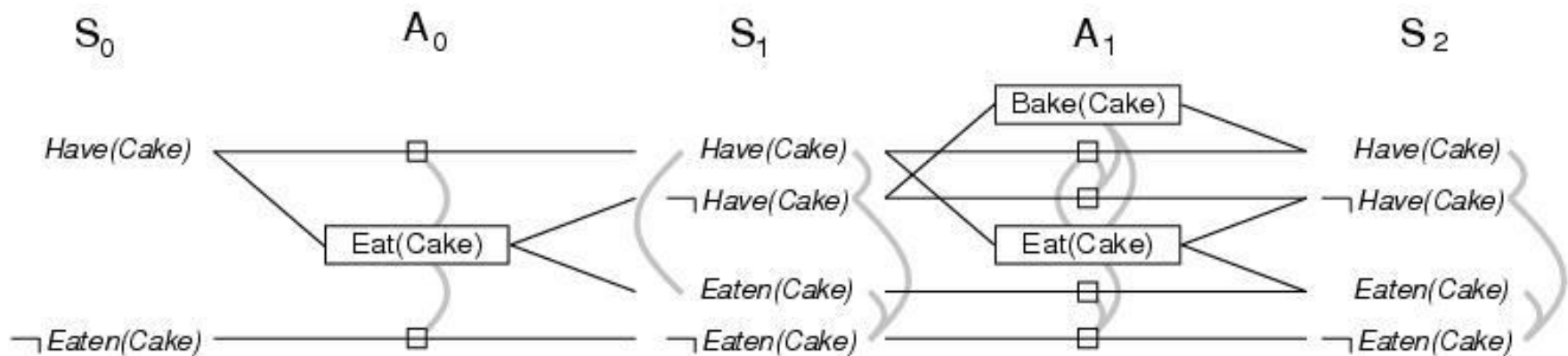
Cake example

- Start at level S_0 and determine action level A_0 and next level S_1 .
 - $A_0 \gg$ all actions whose preconditions are satisfied in the previous level.
 - Connect preconditions and effects of actions $S_0 \rightarrow S_1$
 - Inaction is represented by *persistence actions*.
- Level A_0 contains the actions that could occur
 - Conflicts between actions are represented by *mutex links*



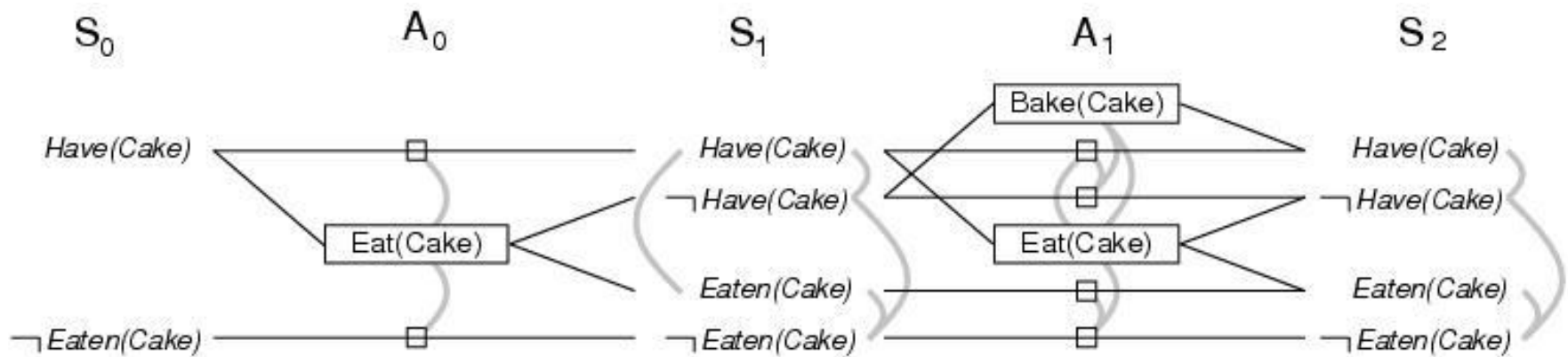
Cake example

- Level S_1 contains all literals that could result from picking any subset of actions in A_0
 - Conflicts between literals that can not occur together (as a consequence of the selection of the action) are represented by mutex links.
 - S_1 defines multiple states and the mutex links are the constraints that define this set of states.
- Continue until two consecutive levels are identical: *leveled off*
 - Or contain the same number of literals



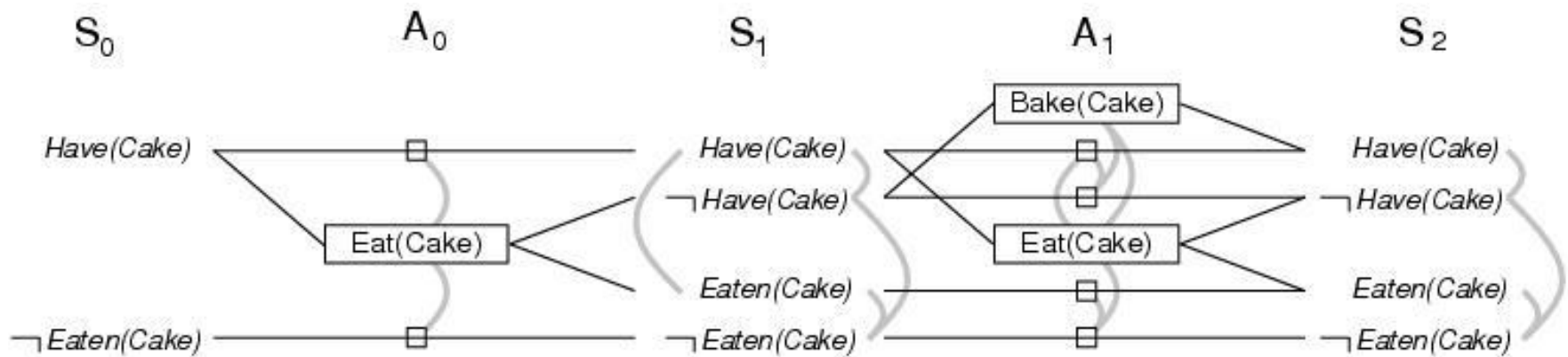
Cake example

- A mutex relation holds between **two actions** when:
 - Inconsistent effects: one action negates the effect of another.
 - Interference: one of the effects of one action is the negation of a precondition of the other.
 - Competing needs: one of the preconditions of one action is mutually exclusive with the precondition of the other.



Cake example

- A mutex relation holds between **two literals** when (inconsistent support):
 - If one is the negation of the other
 - if **each** possible action pair that could achieve the literals is mutex.



PG and heuristic estimation

- PGs provide information about the problem
 - A literal that does not appear in the final level of the graph cannot be achieved by any plan.
 - Useful for backward search (cost = inf).
 - Level of appearance can be used as cost estimate of achieving any goal literals = *level cost*.
 - Small problem: several actions can occur
 - Restrict to one action using serial PG (add mutex links between every pair of actions, except persistence actions).
 - Can be used to construct heuristics
 - Cost of a conjunction of goals? Max-level, sum-level and set-level heuristics.
- PG is a relaxed problem.

The GRAPHPLAN Algorithm

- How to extract a solution directly from the PG

function GRAPHPLAN(*problem*) **returns** solution or failure

graph \leftarrow INITIAL-PLANNING-GRAPH(*problem*)

goals \leftarrow CONJUNCTS(*problem*.GOAL)

nogoods \leftarrow an empty hash table

for *tl* = 0 **to** ∞ **do**

if *goals* all non-mutex in S_t of *graph* **then**

solution \leftarrow EXTRACT-SOLUTION(*graph*, *goals*, NUMLEVELS(*graph*), *nogoods*)

if *solution* \neq failure **then return** *solution*

if *graph* and *nogoods* have both leveled off **then return** failure

graph \leftarrow EXPAND-GRAPH(*graph*, *problem*)

Example: Spare tire problem

Init(*At*(*Flat*, *Axle*) \wedge *At*(*Spare*, *trunk*))

Goal(*At*(*Spare*, *Axle*))

Action(*Remove*(*Spare*, *Trunk*))

PRECOND: *At*(*Spare*, *Trunk*)

EFFECT: \neg *At*(*Spare*, *Trunk*) \wedge *At*(*Spare*, *Ground*)

Action(*Remove*(*Flat*, *Axle*))

PRECOND: *At*(*Flat*, *Axle*)

EFFECT: \neg *At*(*Flat*, *Axle*) \wedge *At*(*Flat*, *Ground*)

Action(*PutOn*(*Spare*, *Axle*))

PRECOND: *At*(*Spare*, *Ground*) \wedge \neg *At*(*Flat*, *Axle*)

EFFECT: *At*(*Spare*, *Axle*) \wedge \neg *Ar*(*Spare*, *Ground*)

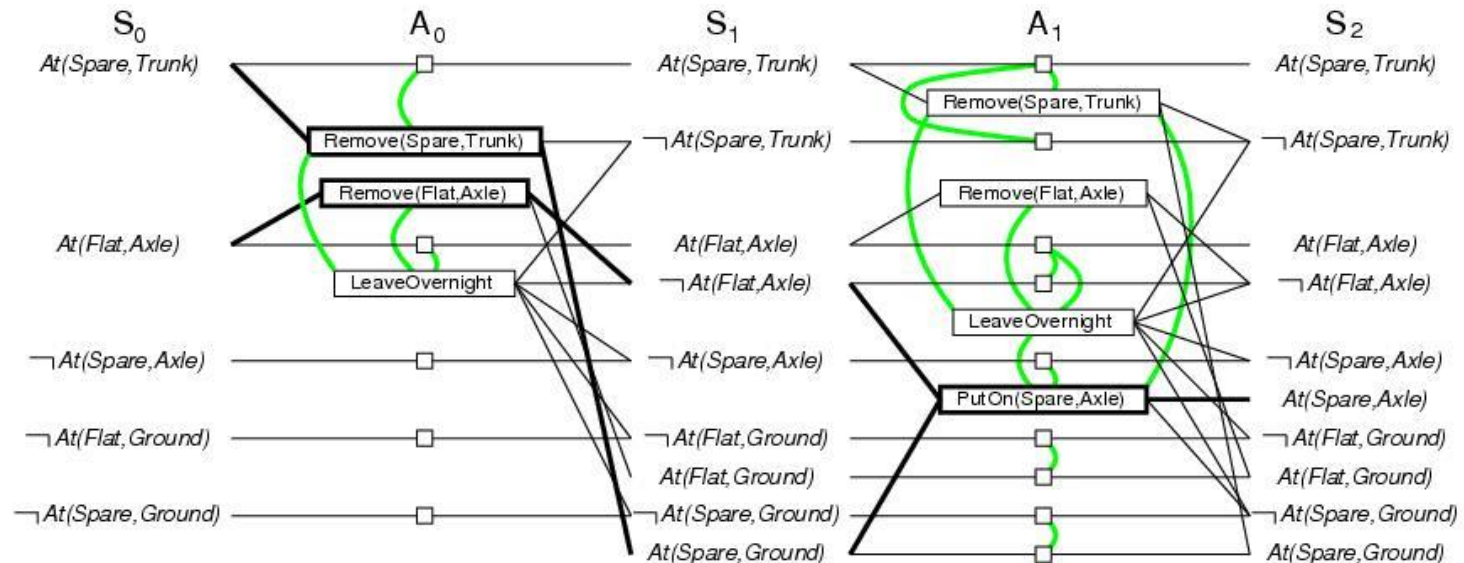
Action(*LeaveOvernight*)

PRECOND:

EFFECT: \neg *At*(*Spare*, *Ground*) \wedge \neg *At*(*Spare*, *Axle*) \wedge \neg *At*(*Spare*, *trunk*) \wedge \neg *At*(*Flat*, *Ground*) \wedge \neg *At*(*Flat*, *Axle*)

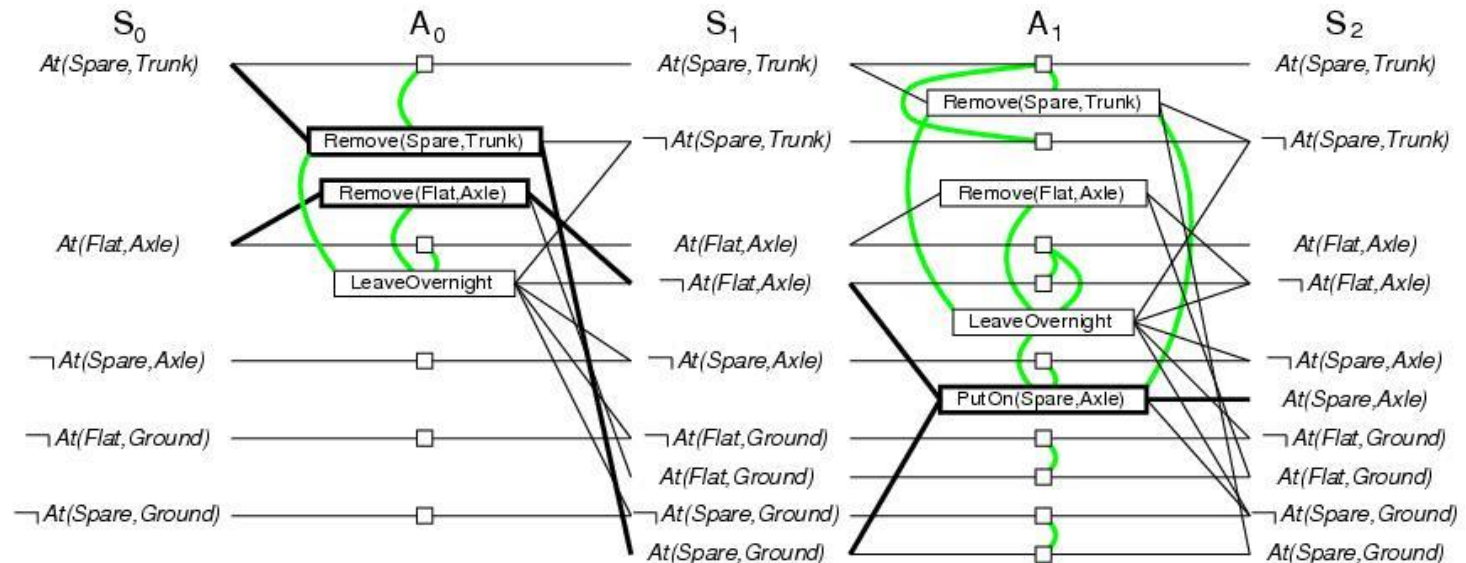
GRAPHPLAN example

- Initially the plan consist of 5 literals from the initial state and the CWA literals (S_0).
- Add actions whose preconditions are satisfied by EXPAND-GRAPH (A_0)
- Also add persistence actions and mutex relations.
- Add the effects at level S_1
- Repeat until goal is in level S_i



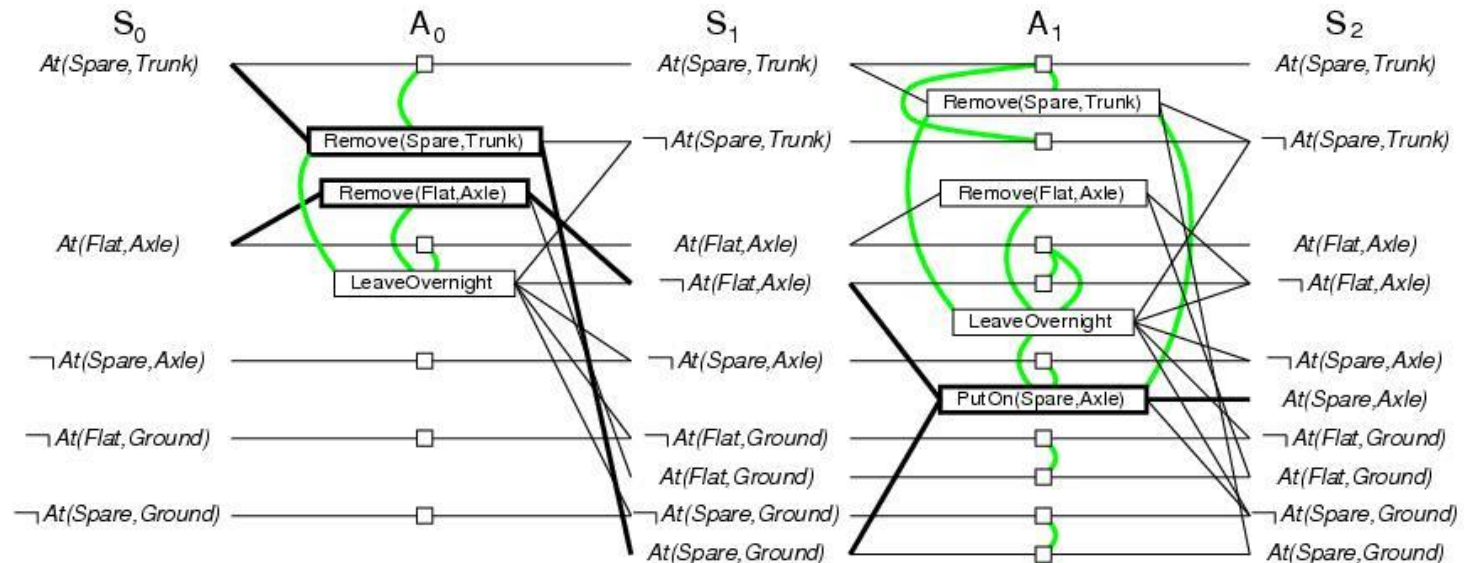
GRAPHPLAN example

- EXPAND-GRAPH also looks for mutex relations
 - Inconsistent effects
 - E.g. Remove(Spare, Trunk) and LeaveOverNight due to At(Spare, Ground) and **not** At(Spare, Ground)
 - Interference
 - E.g. Remove(Flat, Axle) and LeaveOverNight At(Flat, Axle) as PRECOND and **not** At(Flat, Axle) as EFFECT
 - Competing needs
 - E.g. PutOn(Spare, Axle) and Remove(Flat, Axle) due to preconditions
 - Inconsistent support
 - E.g. in S2, At(Spare, Axle) and At(Flat, Axle)



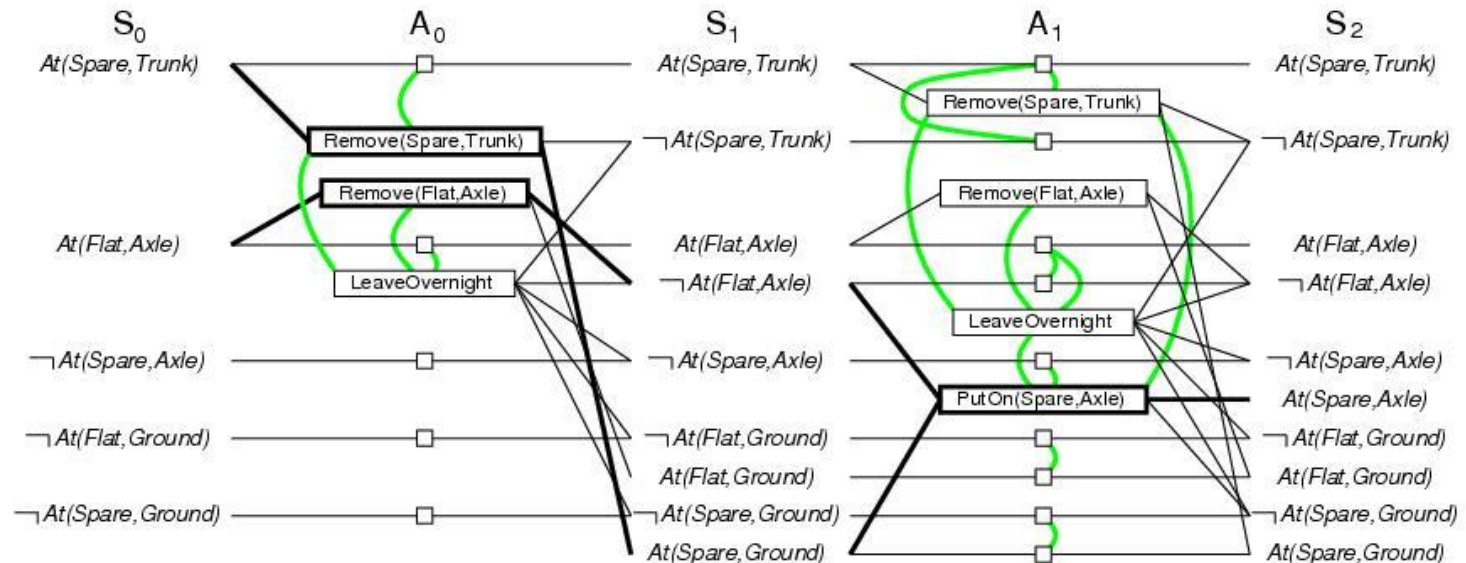
GRAPHPLAN example

- In S_2 , the goal literals exist and are not mutex with any other
 - Solution might exist and EXTRACT-SOLUTION will try to find it
- EXTRACT-SOLUTION solves a Boolean CSP to solve the problem or a search process:
 - Initial state = last level of PG and the goals of planning problem
 - Actions = select any set of non-conflicting actions that cover the goals in the state
 - Goal = reach level S_0 such that all goals are satisfied
 - Cost = 1 for each action.



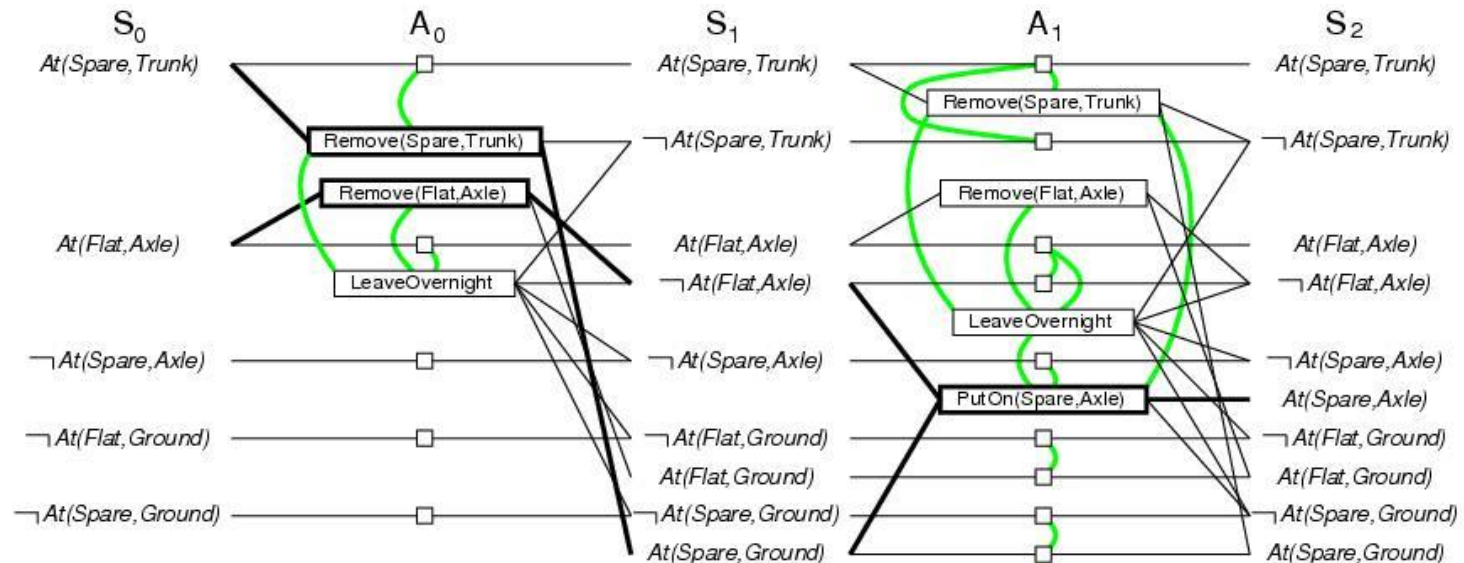
GRAPHPLAN example

- Use heuristics for backward search
 - Pick first the literal with the highest level cost
 - To achieve it, choose the action with the easiest preconditions first (sum of level costs of preconditions is smallest)



GRAPHPLAN example

- Termination? YES
- PG are monotonically increasing or decreasing:
 - Literals increase monotonically
 - Actions increase monotonically
 - Mutexes decrease monotonically
- Because of these properties and because there is a finite number of actions and literals, every PG will eventually level off !



Analysis of planning approaches

- Planning is an area of great interest within AI
 - Search for solution
 - Constructively prove an existence of solution
- Biggest problem is the combinatorial explosion in states
- Efficient methods are under research
 - e.g. divide-and-conquer