

Istanbul Technical University  
Faculty of Computer and Informatics  
Computer Engineering Department

BLG 435E  
AI  
Homework II

Uğur Uysal - 150140012

Dec 9<sup>th</sup>, 2018

# Contents

<b>1</b>	<b>Question I</b>	<b>1</b>
1.1	Model . . . . .	1
1.2	Implementation and Algorithm . . . . .	1
<b>2</b>	<b>Question II</b>	<b>3</b>
2.1	Part I . . . . .	3
2.2	Part II . . . . .	3
<b>3</b>	<b>Question III</b>	<b>6</b>
3.1	Part I . . . . .	6
3.2	Part II . . . . .	7

# 1 Question I

## 1.1 Model

I used blocks as variables and number of blocks as a domain. For example for the given first example the list of variables are these. The origin is top-left corner and it's coordinates increasing from left to right and from top to bottom.

Blocks represented as the direction and starting point. For vertical blocks, starting points is top, and for horizontal blocks, it is left.

- HORIZONTAL 0 3
- HORIZONTAL 1 1
- HORIZONTAL 1 4
- HORIZONTAL 2 2
- HORIZONTAL 2 5
- HORIZONTAL 5 0
- VERTICAL 2 1
- VERTICAL 3 3
- VERTICAL 3 6

Domain is values that can variables take. I used numbers from 0 to number of variables and I assigned the values as which order the block must be placed in grid.

This is the one of the solutions. My algorithms found that.

1. VERTICAL 3 6
2. VERTICAL 3 3
3. HORIZONTAL 5 0
4. VERTICAL 2 1
5. HORIZONTAL 2 5
6. HORIZONTAL 2 2
7. HORIZONTAL 1 4
8. HORIZONTAL 1 1
9. HORIZONTAL 0 3

The constraints are implemented as given in PDF. Also no blocks can be placed in same time, i.e their value can not be same.

## 1.2 Implementation and Algorithm

The algorithm does not stuck. Because if there is not any available assignment in domain space it just stops. Example output is given with visualization at the next page.

```
It is can be built
.....
.....
.....
.....X.
.....X.
.....X.
█
```

```
PROBLEMS OUTPUT DEBUG
It is can be built
.....
.....
.....
...X..X.
...X..X.
...X..X.
█
```

```
PROBLEMS OUTPUT
It is can be built
.....
.....
.....
...X..X.
...X..X.
...X..X.
000X..X.
█
```

```
PROBLEMS OUTPUT DEBUG CONSOLE
It is can be built
.....
.....
.X.....
.X.X..X.
.X.X..X.
000X..X.
█
```

```
PROBLEMS OUTPUT DEBUG CONSOLE
It is can be built
.....
.....
.X...000
.X.X..X.
.X.X..X.
000X..X.
█
```

```
PROBLEMS OUTPUT DEBUG CONSOLE
It is can be built
.....
.....
.X000000
.X.X..X.
.X.X..X.
000X..X.
█
```

```
PROBLEMS OUTPUT DEBUG CONSOLE
It is can be built
.....
...000.
.X000000
.X.X..X.
.X.X..X.
000X..X.
█
```

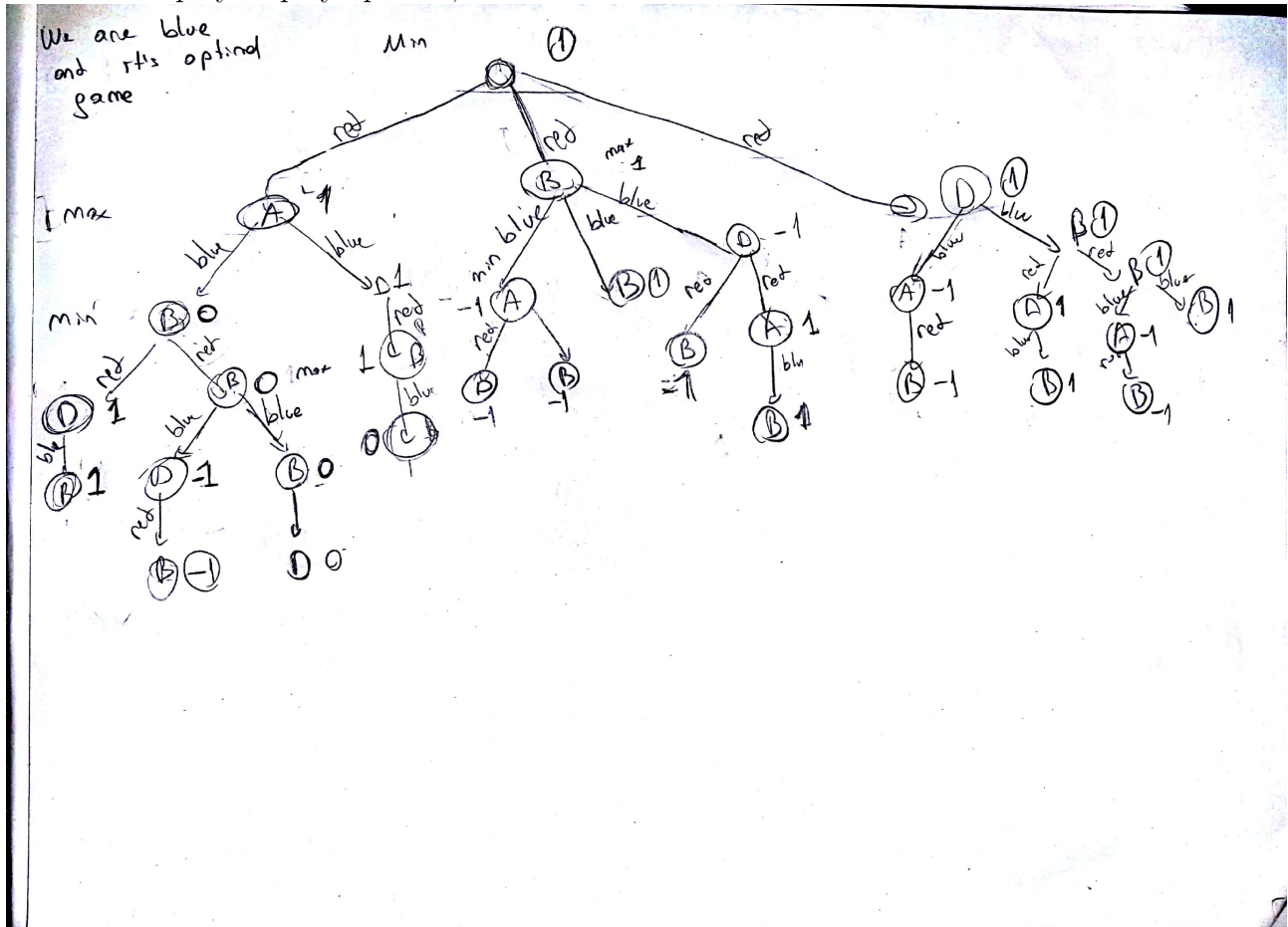
```
PROBLEMS OUTPUT DEBUG CONSOLE
It is can be built
.....
.000000.
.X000000
.X.X..X.
.X.X..X.
000X..X.
█
```

```
PROBLEMS OUTPUT
It is can be built
...000..
.000000.
.X000000
.X.X..X.
.X.X..X.
000X..X.
█
```

## 2 Question II

### 2.1 Part I

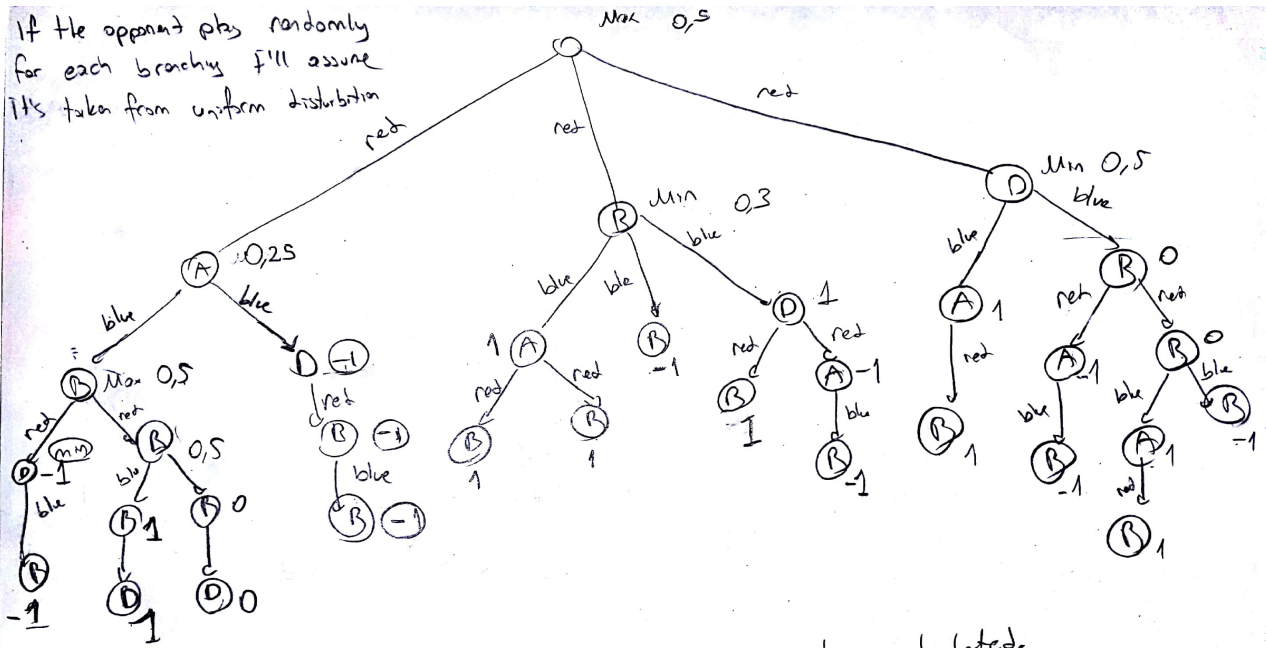
This is the mini-max tree. The given state of the board Red moves first and we can observe that if both players play optimal, Blue win.



### 2.2 Part II

This is the mini-max tree. The given state of the board Red moves first. Calculations are made based on expected value since blue plays randomly.

If the opponent plays randomly for each branching I'll assume it's taken from uniform distribution.



For each branching of blue player expected value calculated.



### 3 Question III

#### 3.1 Part I

Knowledge Base

$$\forall x, \exists y [Student(x) \wedge StudentClub(y)] \Rightarrow Attends(x, y)$$

$$\forall x [Student(x) \wedge Attends(x, LIT CLUB)] \Rightarrow \neg Like(x, COLA)$$

$$\forall x [Student(x) \wedge Attends(x, CINEMA CLUB)] \Rightarrow Like(x, POPCORN)$$

- $Like(Ayşe, COLA) \wedge \neg Like(Ayşe, POPCORN)$
- $Like(BARİŞ, COLA) \wedge Like(BARİŞ, COLA)$
- $\forall x [\neg Likes(Ayşe, x)] \Rightarrow Like(Cem, x).$

$Student(x) \rightarrow$  true if  $x$  is student

$StudentClub(x) \rightarrow$  true if  $x$  is studentClub

$Attends(x, y) \rightarrow$  true if  $x$  attends to club  $y$

$Like(x, y) \rightarrow$  true if  $x$  likes  $y$ .

(Part II).

For Ayşe: Prof by Contradiction

$$\textcircled{1} KB \wedge \neg Attends(Ayşe, Goro Club).$$

$$\forall x, \exists y [Student(x) \wedge StudentClub(y)] \Rightarrow Attends(x, y) \Rightarrow \begin{cases} Attends(Ayşe, LIT CLUB) \vee \\ Attends(Ayşe, Goro Club) \vee \\ Attends(Ayşe, Cinema Club) \end{cases} \rightarrow Q$$

$$\neg [Student(x) \wedge StudentClub(y)] \Rightarrow Attends(x, y) \vee Q$$

$$\neg [\neg (Student(x) \wedge StudentClub(y)) \vee Attends(x, y)] \vee Q$$

$$((Student(x) \wedge StudentClub(y)) \wedge \neg Attends(x, y)) \vee Q$$

$\rightarrow$  In KB

$$\neg Attends(Ayşe, Goro Club)$$

$$Attends(Ayşe, LIT CLUB) \vee Attends(Ayşe, Cinema Club)$$

$$\rightarrow Student(Ayşe) \wedge Attends(Ayşe, LIT CLUB) \Rightarrow \neg Like(Ayşe, COLA) \quad \left( \begin{array}{l} Like(Ayşe, COLA) \\ \text{in KB} \\ \text{if } \neg \text{opposite is false} \end{array} \right)$$

we infer  $\neg Attends(Ayşe, LIT CLUB)$ ,

$$Student(Ayşe) \wedge Attends(Ayşe, Cinema Club) \Rightarrow Like(Ayşe, POPCORN) \quad \left( \begin{array}{l} \neg Like(Ayşe, COLA) \\ \text{in KB} \\ \vee \text{ least false} \end{array} \right)$$

we infer  $\neg Attends(Ayşe, Cinema Club)$



### 3.2 Part II

Now we have contradiction in ①.

so  $\neg \text{Attends}(\text{Ayse}, \text{Game Club})$  is unsatisfiable.

Ayse Attends to Game Club.

For Boris:

$\neg \text{Attends}(\text{Boris}, \text{Game Club})$

$\text{Student}(\text{Boris}) \Rightarrow \text{Attends}(\text{Boris}, \text{Game Club}) \vee \text{Attends}(\text{Boris}, \text{LIT}) \vee \text{Attends}(\text{Boris}, \text{CINEMA})$

$\text{Attends}(\text{Boris}, \text{LIT CLUB}) \Rightarrow \neg \text{Like}(\text{Boris}, \text{COLA})$

$\neg \text{Attends}(\text{Boris}, \text{LIT CLUB}) \vee \neg \text{Like}(\text{Boris}, \text{COLA}) \vee \text{Like}(\text{Boris}, \text{COLA})$  so Boris does not like

$\text{Attends}(\text{Boris}, \text{CINEMA CLUB}) \Rightarrow \text{Like}(\text{Boris}, \text{POPCORN})$

$\neg \text{Attends}(\text{Boris}, \text{CINEMA CLUB}) \vee \text{Like}(\text{Boris}, \text{POPCORN}) \vee \neg \text{Like}(\text{Boris}, \text{POPCORN})$

We cannot infer whether Boris attends CINEMA CLUB or Game CLUB,

For Cem:

$\neg \text{Attends}(\text{Cem}, \text{Game Club})$

$\text{Student}(\text{Cem}) \Rightarrow \text{Attends}(\text{Cem}, \text{LIT}) \vee \text{Attends}(\text{Cem}, \text{Cinema}) \vee \text{Attends}(\text{Cem}, \text{Game})$

$\neg \text{Like}(\text{Ayse}, \text{POPCORN}) \Rightarrow \text{Like}(\text{Cem}, \text{POPCORN})$

$\text{Attends}(\text{Cem}, \text{Cinema}) \Rightarrow \text{Like}(\text{Cem}, \text{POPCORN})$

So we cannot infer which Club Cem attends. it could be any club.