

1. For the following sequences, evaluate the limit, or determine the sequence diverges.

a) $\{\frac{2n}{5n-1}\}$

b) $a_n = \sqrt[n]{n}$

c) $\{0, 1, 0, 1, \dots\}$

d) $\{-3, 2, -\frac{4}{3}, \frac{8}{9}, -\frac{16}{27}, \dots\}$

e) $\{\frac{(n-1)!}{n!}\}$

f) $a_n = \frac{(\ln n)^2}{n}$

g) $a_n = \frac{1}{2}a_{n-1}, a_0 = 100$

2. For each series, write the first four terms of the sum. Then evaluate the series.

a)

$$\sum_{n=1}^{\infty} \frac{(-1)^n}{4^n}$$

b)

$$\sum_{n=0}^{\infty} \left(\frac{2^{n+1}}{5^n} \right)$$

c)

$$\sum_{n=2}^{\infty} \left(\frac{1}{\sqrt{n}} - \frac{1}{\sqrt{n+1}} \right)$$

d)

$$e^{-1} + e^{-2} + e^{-3} + \dots$$

3. Do the following series converge or diverge? Why or why not?

a)

$$\sum_{n=1}^{\infty} (\ln(n) - \ln(n+1))$$

b)

$$\sum_{n=1}^{\infty} \frac{2^n}{3^n}$$

c)

$$\sum_{n=1}^{\infty} \frac{5^n}{4^n + 3}$$

d)

$$\sum_{n=2}^{\infty} \frac{1}{3 + 2^{-n}}$$

e)

$$\sum_{n=1}^{\infty} (\sqrt{2})^n$$

f) A series whose n^{th} partial sum is $s_n = \frac{\ln(2n)}{\ln(n)}$

g)

$$\sum_{n=1}^{\infty} \left(1 - \frac{2}{n}\right)^n$$

4. Express the following decimals as a ratio of integers

a) $0.\overline{5} = 0.555\dots$

b) $0.\overline{31} = 0.313131\dots$

c) $0.\overline{9} = 0.999\dots$ (ask your LA to make sure this is right!)