Shapley Sneakers

The Shapley Sneaker Company is opening a new factory in Simplexville. One of its major purchases will be a leather cutting machine. The cost of maintaining a machine depends on its age as follows:

The cost of purchasing a machine at the beginning of each year is:

There is no trade-in value when a machine is replaced. The company's goal is to minimize the total cost (purchase plus maintenance) of having a machine for five years. Formulate this problem as a shortest path problem.