SM275 · Mathematical Methods for Economics

## Quiz 2 – 4 September 2019

**Instructions.** You have 15 minutes to complete this quiz. You may use your calculator. You may <u>not</u> use any other materials (e.g., notes, homework, books).

Problem	Weight	Score
1	1	
2	1	
3	1	
4	1	
5	1	
6	1	
Total		/ 60

For Problems 1, 2 and 3, consider the DS

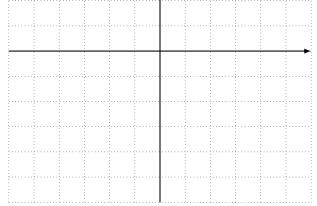
$$A_{n+1} = \frac{2}{3}A_n + 1$$
  $n = 0, 1, 2, ...$ 

**Problem 1.** Draw the cobwebs with  $A_0 = 5$  and  $A_0 = 1$ . Don't forget to indicate the direction of the cobwebs.

• Make sure you start each cobweb correctly. Recall Step 4 in "How to draw a cobweb" from Lesson 3:

Connect  $(A_0, 0)$  to  $(A_0, A_1)$  with a vertical line. Note that  $A_1 = f(A_0)$ , so  $(A_0, A_1)$  is on the graph of y = f(x).

• Make sure you indicate the direction of the cobweb!



**Problem 2.** What are the fixed points of the DS?

- Recall that a fixed point of a DS  $A_{n+1} = f(A_n)$  is a point c that satisfies c = f(c).
- How can you identify *c* using a cobweb diagram?

**Problem 3.** Classify the fixed points you found in Problem 2 as attracting, repelling, or neither.

• Take a look at Lesson 3 to review the definitions of attracting and repelling fixed points.

For Problems 4, 5 and 6, consider the following setting.

We deposit \$1000 into a savings account initially and we withdraw \$100 at the end of each year. The annual interest rate is 0.05, compounded annually.

**Problem 4.** Let  $A_n$  be the amount in the account after n years. Write the DS and IC for this setting.

- Recall that the DS is the "setup." A first order DS is an equation that describes the relationship between  $A_{n+1}$  and  $A_n$ .
- When writing the IC, you need to write an equation:  $A_0 = \dots$  A number alone doesn't communicate enough.
- In a first order linear DS  $A_{n+1} = sA_n + b$ , s and b can be negative or zero.

**Problem 5.** Find the particular solution that satisfies the IC.

- Most of the errors here stemmed from getting the setup in Problem 4 incorrect.
- Be careful with your algebra and arithmetic/calculator.

**Problem 6.** Use the particular solution you found in Problem 5 to find the amount in the account after 10 years.

- Most of the errors here stemmed from getting the setup in Problem 4 incorrect.
- Be careful with your algebra and arithmetic/calculator.