

**Quiz 2 – 4 September 2019**

**Instructions.** You have 15 minutes to complete this quiz. You may use your calculator. You may not use any other materials (e.g., notes, homework, books).

Problem	Weight	Score
1	1	
2	1	
3	1	
4	1	
5	1	
Total		/ 50

For Problems 1 and 2, consider the following setting.

As an analyst at the Markov Company, you have been tasked with better understanding the performance of the company's high-speed computer network. There are only two types of messages sent on the network: 100-byte messages and 10000-byte messages.

Let  $X$  be the travel time of a message on the company's network in seconds, and let  $Y$  be the size of a message in bytes. Based on historical data, you have determined the joint pmf between  $X$  and  $Y$ :

		$Y$	
		100	10000
$X$	$p_{XY}$	15/36	0
	1/100	10/36	0
	1/10	5/36	3/36
	1	0	2/36
	10	0	1/36

**Problem 1.** What is the probability that a message has a travel time of 1 second?

- [All of you answered this problem correctly.](#)

**Problem 2.** What is the probability that the message is 10000 bytes long, given that its travel time is 1 second?

- [Be careful when applying the definition of conditional probability.](#)

For Problems 3, 4 and 5, consider the following setting.

Another analyst at the Markov Company has collected some other data on the company's network performance. According to her data,  $3/4$  of the messages sent on the network are 100 bytes long, and  $1/4$  are 10000 bytes long. In addition, she found that  $1/5$  of 100-byte messages have a travel time of 1 second, while  $2/5$  of 10000-byte messages have a travel time of 1 second.

Let  $X$  be the travel time of a message on the company's network in seconds, and let  $Y$  be the size of a message in bytes.

**Problem 3.** What is the probability that a message has a travel time of 1 second?

- Review the law of total probability from Lesson 3.

**Problem 4.** Are  $X$  and  $Y$  independent? Give a numerical argument for why or why not.

- You can use the definition of independence, or...
- You may find it easier to use one of the facts about independence and conditional probabilities at the bottom of page 3 of Lesson 3.

**Problem 5.** What is the expected size of a message in bytes?

- Review the definition of expected value. Remember that intuitively, the expected value is a weighted average. What is the (weighted) average message size?