Scientific Python Introduction

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Aim of the course

- Get to know Python
  - What is Python?
    - Why use Python?
  - Basic training
    - User interface
    - Basic functions
    - Visualisation
    - Programming
    - Analysis

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What is Scientific Python?

- Python
  - object oriented programming language
- Scientific
  - Add numpy, matplotlib, scipy
- Why use Python?
  - Mathematcal computations
  - Visualisation
  - Analysis
  - Used a lot for problem solving
    - Cybernetics
    - Signal processing
    - Image processing
    - Pattern recognition
    - …

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Basic training

- User interface
- Basic functions
- Visualisation
- Programming
- Analysis

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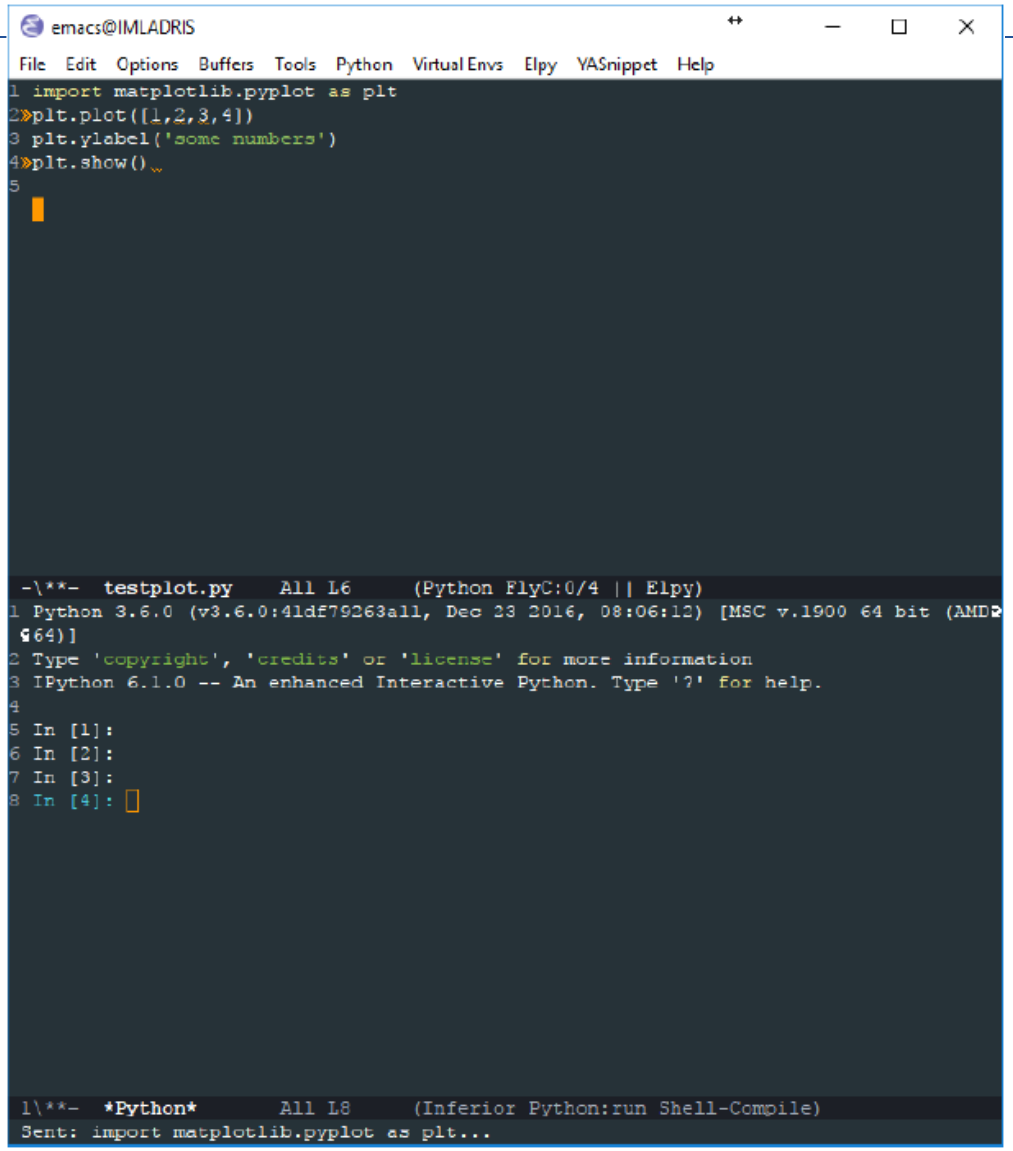
User interface

- Interpreter window
- Editor
- Help



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User interface

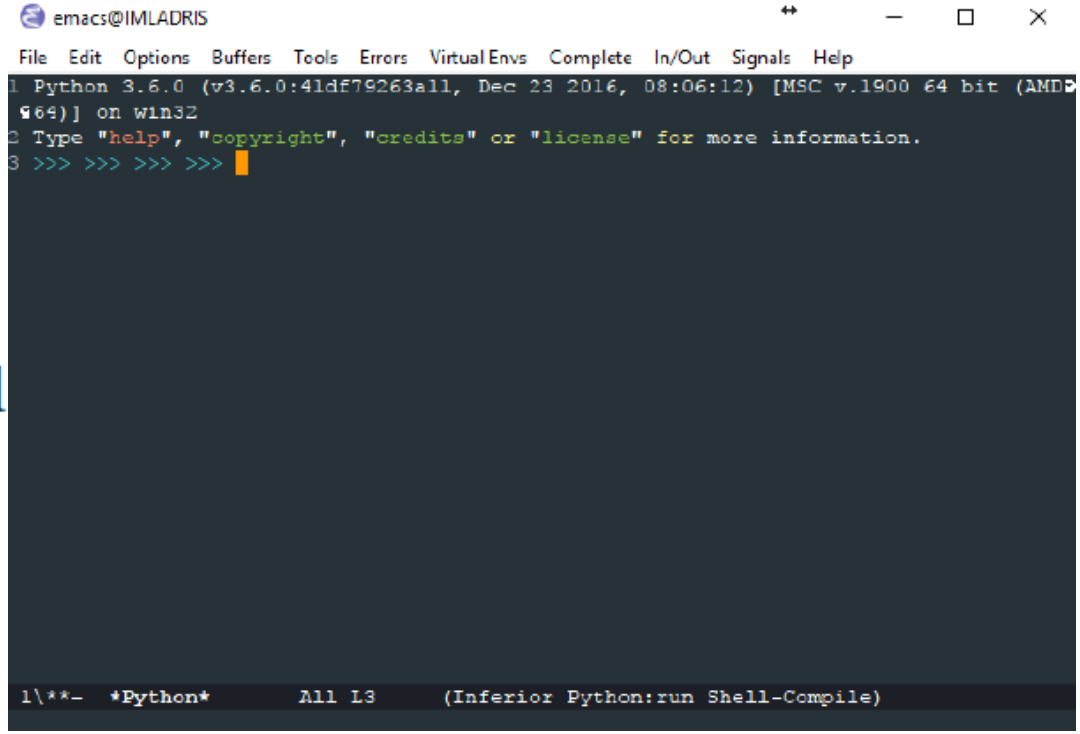
- Interpreter

A simple example;

```
>>> 10
```

where Python will respond

```
10
```



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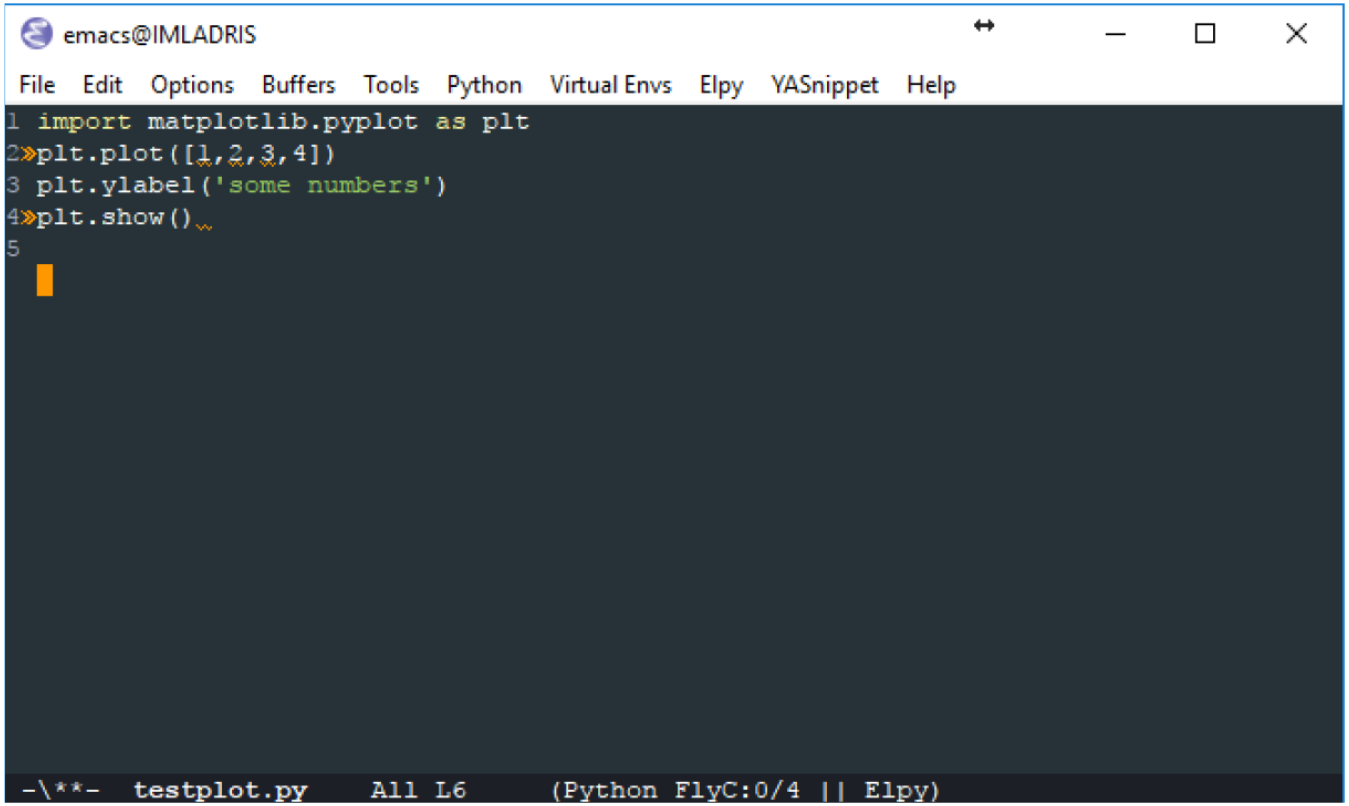
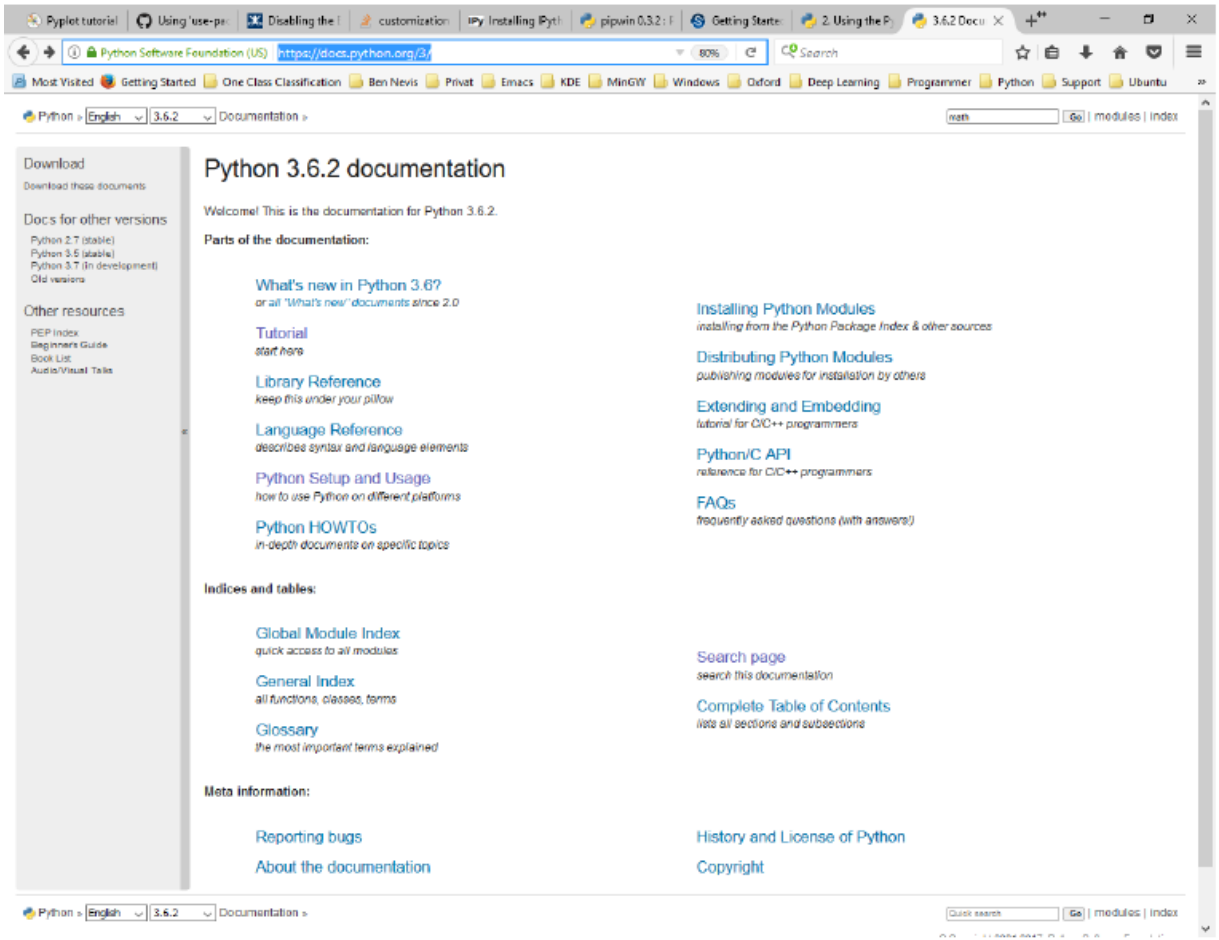
User interface

- Editor



User interface

- Help
  - Documentation
  - Search



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Basic functions

- Create matrices
- Matrix operations
- Matrix functions
- Matrix indexing
- Logical operations

Basic functions

- Create matrices
  - Scalar
  - Vector
  - Matrix

```
>>> x=np.array([0, 5, 10, 15, 20])
>>> x=x.reshape(x.size,1)
>>> x
array([[ 0],
       [ 5],
       [10],
       [15],
       [20]])
```

```
>>> A=np.array([[0,1,2,3,4],[5,6,7,8,9],[10,11,12,13,14],[15,16,17,18,19]])
>>> A
array([[ 0,  1,  2,  3,  4],
       [ 5,  6,  7,  8,  9],
       [10, 11, 12, 13, 14],
       [15, 16, 17, 18, 19]])
```

```
>>> y=np.array([0, 5, 10, 15, 20])
>>> y
array([ 0,  5, 10, 15, 20])
```

```
>>> a=5
>>> a=
5
```

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Basic functions

- Matrix operators

+	addition
-	subtraction
*	multiplication
/	division

```
>>> y+y
array([ 0, 10, 20, 30, 40])
```

```
>>> b=np.dot(A,x)
>>> b
array([[150],
       [400],
       [650],
       [900]])
```

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Basic functions

- Matrix functions

power	power
transpose	transponation
sum	sums the elements in a vector/matrix matrix
dot	vector inner product, vector/matrix multiplication
diag	diagonalises a matrix
det	computes the determinant of a matrix

eye	generates an identity matrix
ones	generates a matrix of ones
rand	generates a matrix of random numbers

size	determines the dimension of a matrix
arange	create an increasing vector
:	slicing

```
>>> n=np.arange(1,6)
>>>n =
array([1, 2, 3, 4, 5])
```

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Basic functions

- Matrix indexing

```
>>> A
array([[ 0,  1,  2,  3,  4],
       [ 5,  6,  7,  8,  9],
       [10, 11, 12, 13, 14],
       [15, 16, 17, 18, 19]])

>>> A[1,2]
>>> A
7



>>> A[1,:]
array([ 5,  6,  7,  8,  9])
```

Basic functions

- Logical operators

<	less than
>	larger than
<=	less than or equal to
>=	less than or equal to
==	equal
!=	not equal

```
>>> y
array([ 0,  5, 10, 15, 20])
```

```
>>> y>=10
array([False, False,  True,  True,  True], dtype=bool)
```

and	logical AND
or	logical OR
not	logical NOT

```
>>> idx=np.where(y>=10)
>>> idx
(array([2, 3, 4], dtype=int64),)
```

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Visualisation

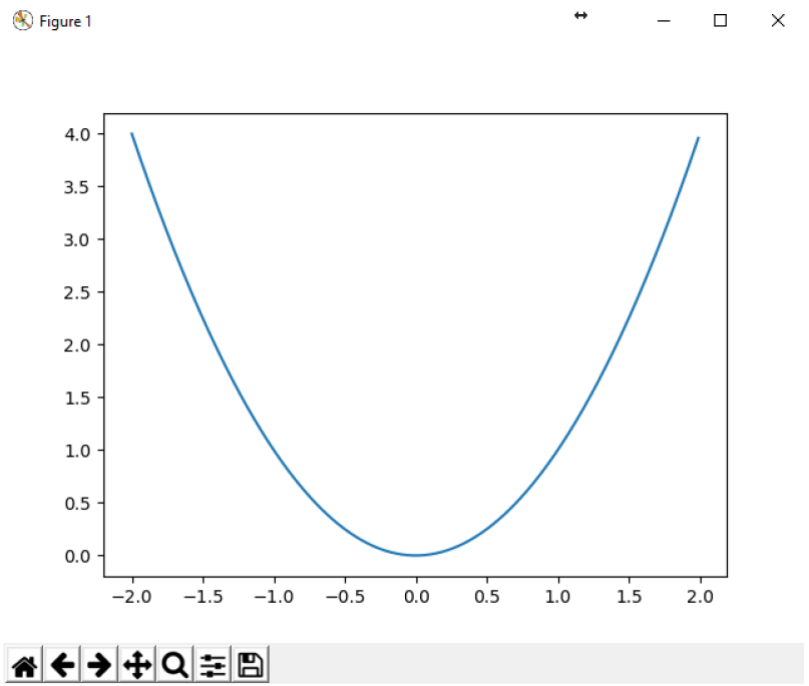
- 2D-plotting
- 3D-plotting

Visualisation

- 2D-plotting

As a simple introductory example of plotting we consider the function $y = f(x)$ der $f(x) = x^2$. We want to plot the function in the interval $x \in [-2, 2]$.

```
>>> x=np.arange(-2,2,0.01)
>>> y=np.square(x)
>>> plt.plot(x,y)
>>> plt.show()
```

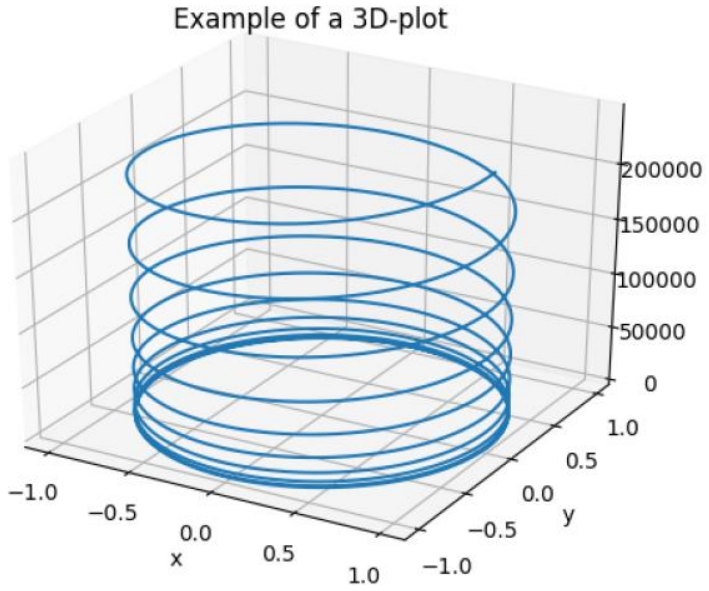


Visualisation

- 3D-plotting

3D line plot We can plot a line through (x, y, z) points defined parametrically using the following instructions:

```
>>> import matplotlib as mpl
>>> from mpl_toolkits.mplot3d import Axes3D
>>> fig = plt.figure()
>>> ax = fig.gca(projection='3d')
>>> t=np.arange(0,20*np.pi,0.01)
>>> x=np.cos(t)
>>> y=np.sin(t)
>>> z=np.power(t,3)
>>> ax.plot(x, y, z)
>>> plt.xticks(np.arange(-1,1.1,0.5))
>>> plt.yticks(np.arange(-1,1.1,0.5))
>>> plt.xlabel('x')
>>> title('Example of a 3D plot');
```

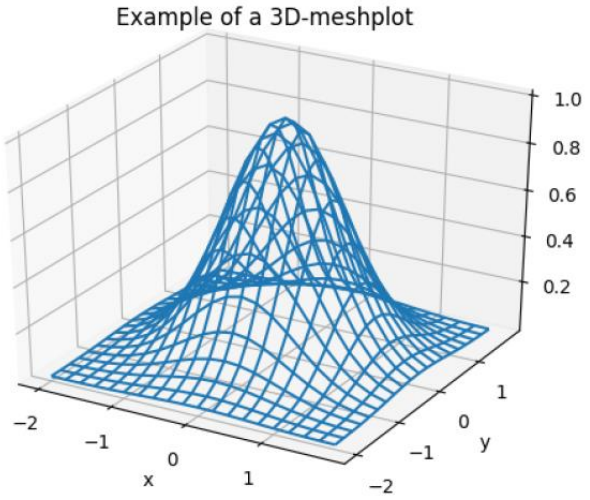


Visualisation

- 3D-plotting

3D surface plot We can plot surface functions as for example the surface given as $z = e^{-x^2-y^2}$. We want to plot this function over the square $[-2, 2] \times [-2, 2]$. To do this we have to generate a grid of point of compu-

```
>>> x=np.arange(-2,2,.2)
>>> y=np.arange(-2,2,.2)
>>> X, Y = np.meshgrid(x,y)
>>> Z=np.exp(-np.square(X)-np.square(Y))
>>> fig = plt.figure()
>>> ax = fig.add_subplot(111, projection='3d')
>>> ax.plot_wireframe(X,Y,Z)
>>> plt.xlabel('x')
>>> plt.ylabel('y')
>>> plt.title('Example of a 3D mesh plot')
```



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Programming

- Function files
- Control structures
  - if
  - while
  - for

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Programming

- Function files

As a simple example we will make a function for computing the normal probability density function,

$$p(x) = \frac{1}{\sqrt{2\pi}\sigma} \cdot e^{\frac{-(x-\mu)^2}{2\sigma^2}}. \quad (1)$$

Here we will use the variable x and the function parameters μ and σ as input parameters. p will be the output parameter. We will call the function *pdens.m*. The contents of the file might look like følger:

```
import numpy as np

def pdens(x, m, s):
    # PDENS Computes the probaaility density values
    # P=PDENS(X,M,S) computes the density value P for
    # X for a gaussian density function with
    # mean value M og standard deviation S.
    p = 1/(np.sqrt(2*np.pi)*s)* \
        np.exp(-1/2*np.square((x-m))/(2*np.square(s)))
    return p
```

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Programming

- Condition control using *if*

For example if one needs to make a procedure, *absolute*, that computes the absolute value $y = |x|$ of a number, x, so that $y = x$ when x is positive and $y = -x$ otherwise.

```
def absolute(x)

    # ABSOLUTE Computes the absolute value
    # Y=ABSOLUTE(X) computes the absolute value, Y, of X

    if x < 0:
        y=-x
    else:
        y=x
    return y
```

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Programming

- Iterations using *while*

As an example one might want to make a function, *divideby2*, which divides an integer n with 2 as many times as possible. The commands `fix` and `rem` are used to compute the integer quotient and the remainder respectively.

```
def divideby2(n)

    # DIVIDEBY2 Divide by 2 as long as the remainder is zero
    # Q=DIVIDEBY2(N) computes the quotient, Q,
    # the maximum number of divisions by 2

    q=n
    while np.remainder(q,2) == 0:
        q=np.fix(q/2)
    return q
```

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Programming

- Iterations using *for*

As an example we want to modify the function *pdens* so that you can compute the density values for more than one point of computation at a time. A possible way to do this:

```
def p=pdens2(x,m,s)

    # PDENS Computes the probaaility density values
    # P=PDENS(X,M,S) computes the density value P for
    # the values in a vector X for a gaussian density function
    # with mean value M og standard deviation S.

    N = np.shape(x)[0]
    p = np.zeros(np.shape(x))
    for n in np.arange(0, N - 1):
        p[n] = 1 / (np.sqrt(2 * np.pi) * s) * \
            np.exp(-1 / 2 * np.square((x[n] - m)) / (2 * np.square(s)))
    return p
```

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Analysis

- Estimate pulse rate
  - Reading from data file
  - Plotting of signal
  - Detection of peaks
  - Problem – false detections
    - Spectral analysis
    - Filtering

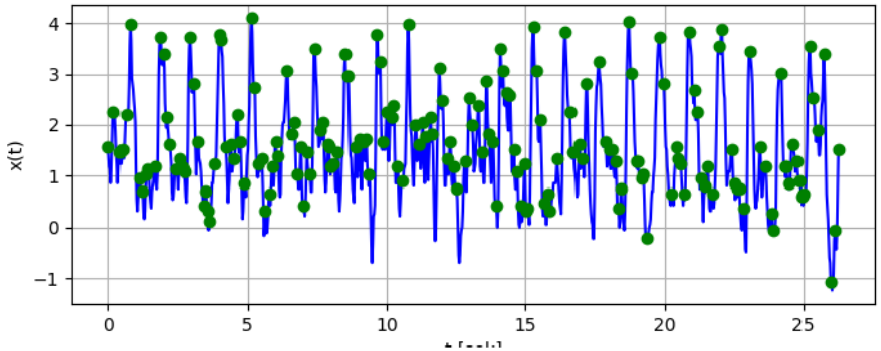
Analysis

```
>>> x=np.genfromtxt('photopl.txt',dtype=None,delimiter=None,skip_header=4
>>> x=x/np.std(x)
```

- Reading from data file
- Plotting of signal
- Detection of peaks

```
>>> fs = 40.0
>>> N = np.size(x)
>>> t = np.arange(0, N) / fs
>>> t = t.reshape(t.size, 1)
```

```
>>> from analyse import findpeaks
>>> ind, peaks = findpeaks(x)
```




```
>>> fig1 = plt.figure(1)
>>> ax1 = plt.axes()
>>> ax1.plot(t, x, 'b', t[ind, 0], x[ind, 0], 'go')
>>> plt.xlabel('t [sek]';
>>> plt.ylabel('x(t)')
>>> plt.grid('on')
>>> fig1.set_size_inches(8, 3)
```

Analysis

- Problem – false detections
  - Spectral analysis
  - Filtering

```
>>> f,Pxx = signal.welch(x.reshape(1,x.size),fs,nperseg=256,
>>>                      nfft=1024,detrend=False,scaling='density')
>>> Pxx = Pxx.reshape(Pxx.size, 1)
>>> f = f.reshape(f.size, 1)
>>> fig2 = plt.figure(2)
>>> ax21 = fig2.add_subplot(211)
>>> ax21.plot(f, 10 * np.log10(Pxx), 'b')
>>> plt.xlabel('f [Hz]')
>>> plt.ylabel('Magnitude [dB]')
>>> plt.grid('on')
>>> plt.axis([0, 20, -40, 20])
```

```
>>> dt = 0.55
>>> pb = np.array([0,0.58-dt,0.58,1.27,1.27+dt,20])/(40)
>>> b = signal.remez(150, pb, [0, 1, 0], type='bandpass')
>>> w, h = signal.freqz(b)
>>> ax22 = fig2.add_subplot(212)
>>> ax22.plot(w / (2 * np.pi) * 40, 20 * np.log10(np.abs(h)), 'b')
>>> plt.xlabel('f [Hz]')
>>> plt.ylabel('Magnitude [dB]')
>>> plt.grid('on')
>>> plt.axis([0, 20, -40, 20])
```