Artificial Intelligence

Reinforcement Learning



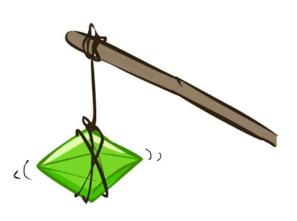
Instructors: Fatemeh Mansoori

University of Isfahan

[These slides were created by Dan Klein and Pieter Abbeel for CS188 Intro to AI at UC Berkeley. All CS188 materials are available at http://ai.berkeley.edu.]

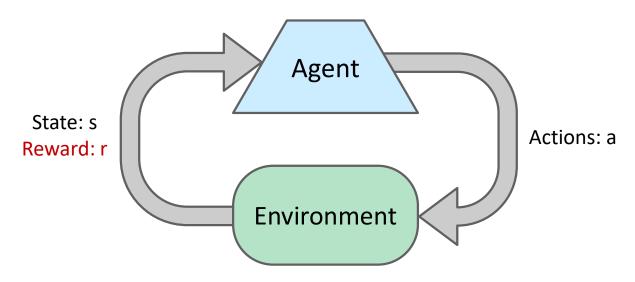
Reinforcement Learning







Reinforcement Learning



Basic idea:

- Receive feedback in the form of rewards
- Agent's utility is defined by the reward function
- Must (learn to) act so as to maximize expected rewards
- All learning is based on observed samples of outcomes!

Applications

Game Playing :

 successfully applied to games such as chess, Go, and video games, where the agent learns to play by trial and error.

Robotics:

 used to train robots to perform tasks such as grasping objects, navigating environments, and interacting with humans.

Finance:

 used in algorithmic trading to make decisions about buying, selling, or holding financial assets

Applications

Healthcare:

 can be used to optimize treatment strategies for patients, personalize medicine, and improve healthcare operations.

Recommendation systems

 can be used to optimize recommendations for users in areas such as e-commerce, streaming services, and online advertising.



Initial



A Learning Trial



After Learning [1K Trials]

[Kohl and Stone, ICRA 2004]



Initial

[Kohl and Stone, ICRA 2004]

[Video: AIBO WALK – initial]



Training



Finished

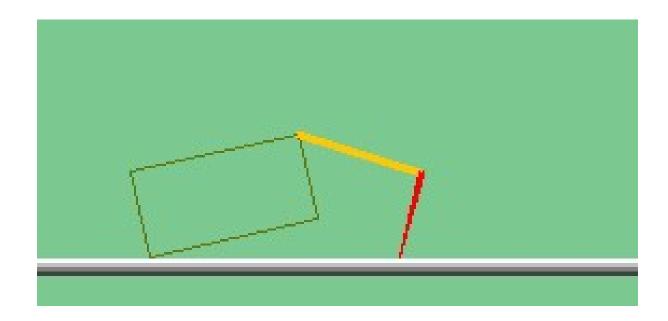
Example: Toddler Robot



[Tedrake, Zhang and Seung, 2005]

[Video: TODDLER – 40s]

The Crawler!



[Demo: Crawler Bot (L10D1)] [You, in Project 3]

Video of Demo Crawler Bot



Reinforcement Learning

- Still assume a Markov decision process (MDP):
 - A set of states $s \in S$
 - A set of actions (per state) A
 - A model T(s,a,s')
 - A reward function R(s,a,s')
- Still looking for a policy $\pi(s)$

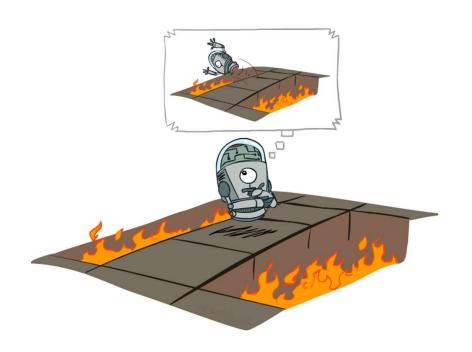






- New twist: don't know T or R
 - I.e. we don't know which states are good or what the actions do
 - Must actually try out actions and states to learn

Offline (MDPs) vs. Online (RL)



Offline Solution

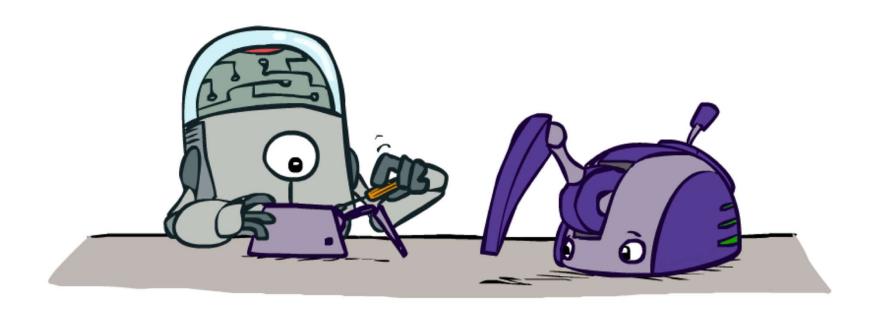


Online Learning

Passive Reinforcement Learning

- Simplifies task : policy evaluation
 - Input: a fixed policy $\pi(s)$
 - You don't know the transitions T(s,a,s')
 - You don't know the rewards R(s,a,s')
 - Goal : learn the state values
- In this case:
 - Learner is "along for the ride"
 - No choice about what actions to take
 - Just execute the policy and learn from experience
 - The is NOT offline planning! You actually take actions in the world

Model-Based Learning



Model-Based Learning

Model-Based Idea:

- Learn an approximate model based on experiences
- Solve for values as if the learned model were correct

Step 1: Learn empirical MDP model

- Count outcomes s' for each s, a
- Normalize to give an estimate of $\widehat{T}(s, a, s')$
- Discover each $\widehat{R}(s, a, s')$ when we experience (s, a, s')

Step 2: Solve the learned MDP

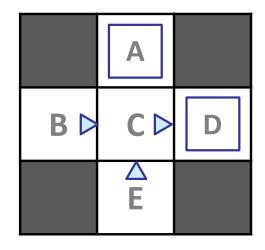
For example, use value iteration, as before





Example: Model-Based Learning

Input Policy π



Assume: $\gamma = 1$

Observed Episodes (Training)

Episode 1

B, east, C, -1 C, east, D, -1 D, exit, x, +10 Episode 2

B, east, C, -1 C, east, D, -1 D, exit, x, +10

Episode 3

E, north, C, -1 C, east, D, -1 D, exit, x, +10 Episode 4

E, north, C, -1 C, east, A, -1 A, exit, x, -10 **Learned Model**

 $\widehat{T}(s,a,s')$ T(B, east, C) = 1.00
T(C, east, D) = 0.75
T(C, east, A) = 0.25

 $\widehat{R}(s, a, s')$

R(B, east, C) = -1 R(C, east, D) = -1 R(D, exit, x) = +10

Example: Expected Age

Goal: Compute expected age of AI class students

Known P(A)

$$E[A] = \sum_{a} P(a) \cdot a = 0.35 \times 20 + \dots$$

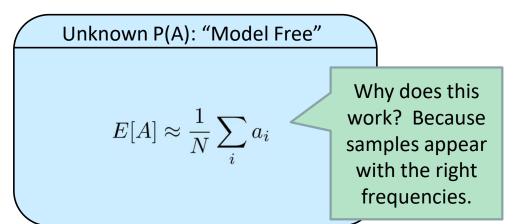
Without P(A), instead collect samples $[a_1, a_2, ... a_N]$

Unknown P(A): "Model Based"

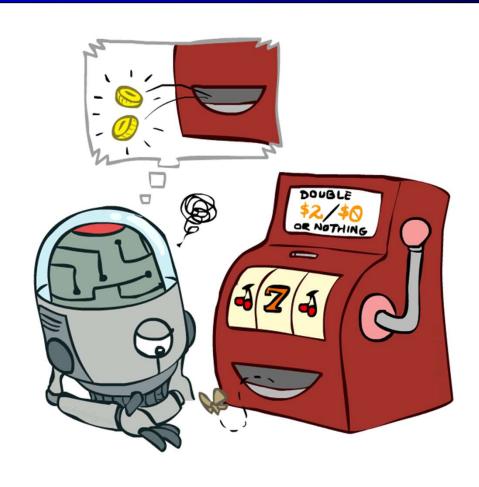
Why does this work? Because eventually you learn the right model.

$$\hat{P}(a) = \frac{\text{num}(a)}{N}$$

$$E[A] \approx \sum_{a} \hat{P}(a) \cdot a$$



Model-Free Learning



Direct Evaluation

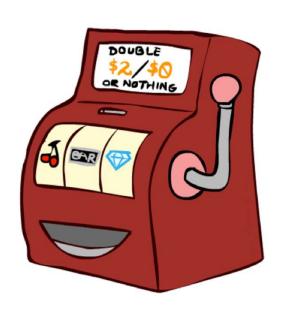
- Goal: Compute values for each state under π
- Idea: Average together observed sample values
 - Act according to π
 - Every time you visit a state, write down what the sum of discounted rewards turned out to be

$$sample_i(s) = R(s) + \gamma R(s') + \gamma^2 R(s'') + \dots$$

Average those samples

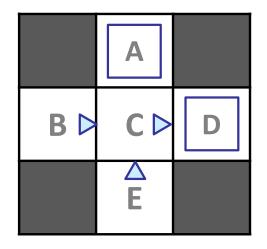
$$V(s) \leftarrow \frac{1}{N} \sum_{i} sample_{i}(s)$$

This is called direct evaluation



Example: Direct Evaluation

Input Policy π



Assume: $\gamma = 1$

Observed Episodes (Training)

Episode 1

B, east, C, -1 C, east, D, -1 D, exit, x, +10

Episode 3

E, north, C, -1 C, east, D, -1 D, exit, x, +10

Episode 2

B, east, C, -1 C, east, D, -1 D, exit, x, +10

Episode 4

E, north, C, -1 C, east, A, -1 A, exit, x, -10

Output Values

	-10 A	
+8 B	+4 C	+10 D
	-2 E	

Problems with Direct Evaluation

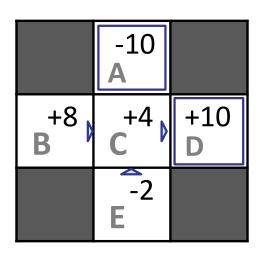
What's good about direct evaluation?

- It's easy to understand
- It doesn't require any knowledge of T, R
- It eventually computes the correct average values, using just sample transitions

What bad about it?

- It wastes information about state connections
- Each state must be learned separately
- So, it takes a long time to learn

Output Values



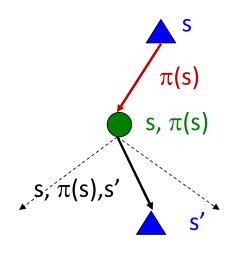
If B and E both go to C under this policy, how can their values be different?

Why Not Use Policy Evaluation?

- Simplified Bellman updates calculate V for a fixed policy:
 - Each round, replace V with a one-step-look-ahead layer over V

$$V_0^{\pi}(s) = 0$$

$$V_{k+1}^{\pi}(s) \leftarrow \sum_{s'} T(s, \pi(s), s') [R(s, \pi(s), s') + \gamma V_k^{\pi}(s')]$$
 s, $\pi(s)$, s'



- This approach fully exploited the connections between the states
- Unfortunately, we need T and R to do it!
- Key question: how can we do this update to V without knowing T and R?
 - In other words, how to we take a weighted average without knowing the weights?

Sample-Based Policy Evaluation?

We want to improve our estimate of V by computing these averages:

$$V_{k+1}^{\pi}(s) \leftarrow \sum_{s'} T(s, \pi(s), s') [R(s, \pi(s), s') + \gamma V_k^{\pi}(s')]$$

• Idea: Take samples of outcomes s' (by doing the action!) and average

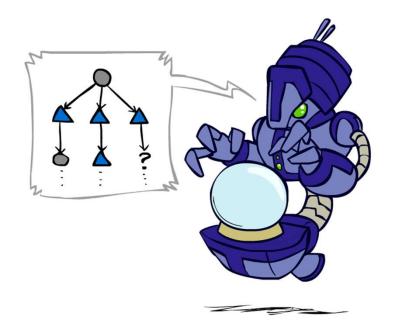
$$sample_1 = R(s, \pi(s), s'_1) + \gamma V_k^{\pi}(s'_1)$$

$$sample_2 = R(s, \pi(s), s'_2) + \gamma V_k^{\pi}(s'_2)$$

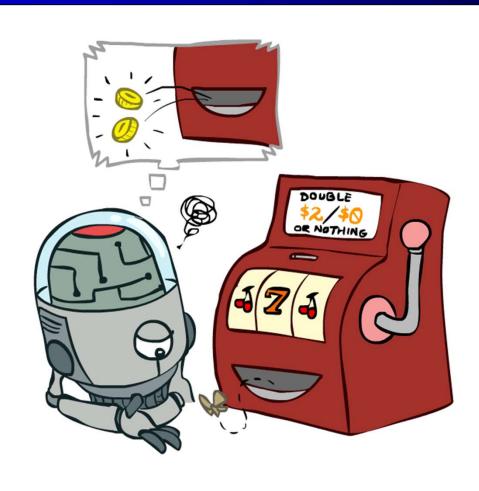
$$\dots$$

$$sample_n = R(s, \pi(s), s'_n) + \gamma V_k^{\pi}(s'_n)$$

$$V_{k+1}^{\pi}(s) \leftarrow \frac{1}{n} \sum_{i} sample_i$$



Temporal Difference Learning

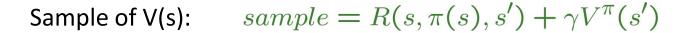


Temporal Difference Learning

- Big idea: learn from every experience!
 - Update V(s) each time we experience a transition (s, a, s', r)
 - Likely outcomes s' will contribute updates more often

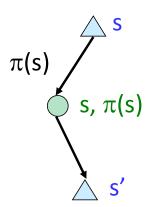


- Policy still fixed, still doing evaluation!
- Move values toward value of whatever successor occurs: running average



Update to V(s): $V^{\pi}(s) \leftarrow (1-\alpha)V^{\pi}(s) + (\alpha)sample$

Same update: $V^{\pi}(s) \leftarrow V^{\pi}(s) + \alpha(sample - V^{\pi}(s))$



Exponential Moving Average

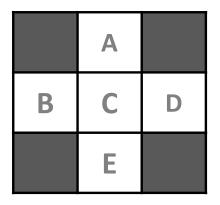
- Exponential moving average
 - The running interpolation update: $\bar{x}_n = (1 \alpha) \cdot \bar{x}_{n-1} + \alpha \cdot x_n$
 - Makes recent samples more important:

$$\bar{x}_n = \frac{x_n + (1 - \alpha) \cdot x_{n-1} + (1 - \alpha)^2 \cdot x_{n-2} + \dots}{1 + (1 - \alpha) + (1 - \alpha)^2 + \dots}$$

- Forgets about the past (distant past values were wrong anyway)
- Decreasing learning rate (alpha) can give converging averages

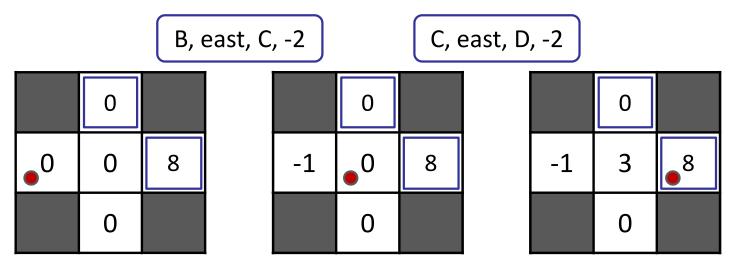
Example: Temporal Difference Learning

States



Assume: $\gamma = 1$, $\alpha = 1/2$

Observed Transitions



$$V^{\pi}(s) \leftarrow (1 - \alpha)V^{\pi}(s) + \alpha \left[R(s, \pi(s), s') + \gamma V^{\pi}(s') \right]$$

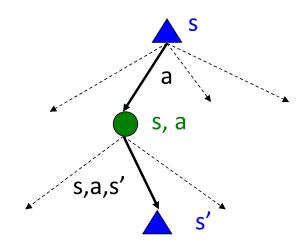
Problems with TD Value Learning

- TD value leaning is a model-free way to do policy evaluation, mimicking Bellman updates with running sample averages
- However, if we want to turn values into a (new) policy, we're sunk:

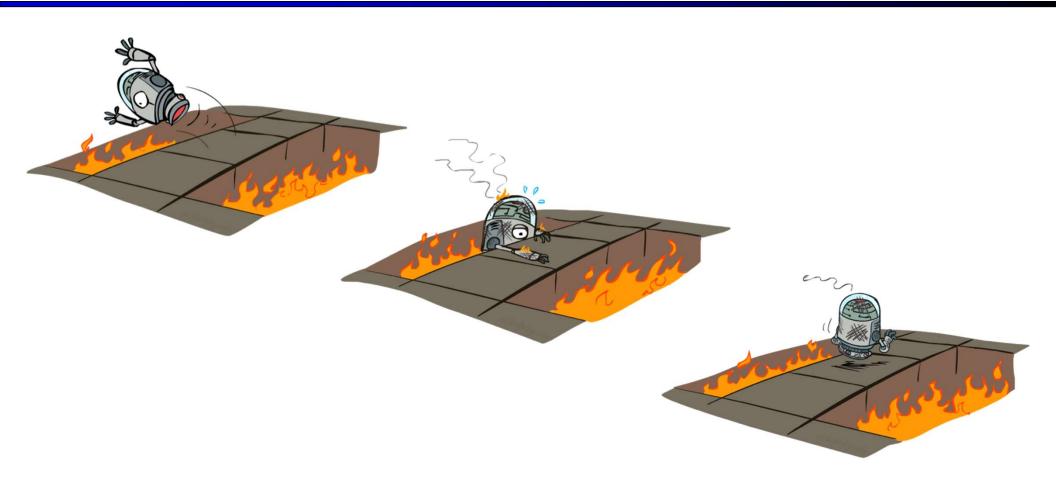
$$\pi(s) = \arg\max_{a} Q(s, a)$$

$$Q(s, a) = \sum_{s'} T(s, a, s') \left[R(s, a, s') + \gamma V(s') \right]$$

- Idea: learn Q-values, not values
- Makes action selection model-free too!



Active Reinforcement Learning



Active Reinforcement Learning

- Full reinforcement learning: optimal policies (like value iteration)
 - You don't know the transitions T(s,a,s')
 - You don't know the rewards R(s,a,s')
 - You choose the actions now
 - Goal: learn the optimal policy / values



In this case:

- Learner makes choices!
- Fundamental tradeoff: exploration vs. exploitation
- This is NOT offline planning! You actually take actions in the world and find out what happens...

Q-Value Iteration

- Value iteration: find successive (depth-limited) values
 - Start with $V_0(s) = 0$, which we know is right
 - Given V_k, calculate the depth k+1 values for all states:

$$V_{k+1}(s) \leftarrow \max_{a} \sum_{s'} T(s, a, s') \left[R(s, a, s') + \gamma V_k(s') \right]$$

- But Q-values are more useful, so compute them instead
 - Start with $Q_0(s,a) = 0$, which we know is right
 - Given Q_k, calculate the depth k+1 q-values for all q-states:

$$Q_{k+1}(s, a) \leftarrow \sum_{s'} T(s, a, s') \left[R(s, a, s') + \gamma \max_{a'} Q_k(s', a') \right]$$

Q-Learning

Q-Learning: sample-based Q-value iteration

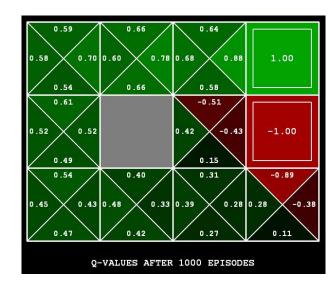
$$Q_{k+1}(s, a) \leftarrow \sum_{s'} T(s, a, s') \left[R(s, a, s') + \gamma \max_{a'} Q_k(s', a') \right]$$

- Learn Q(s,a) values as you go
 - Receive a sample (s,a,s',r)
 - Consider your old estimate: Q(s, a)
 - Consider your new sample estimate:

$$sample = R(s, a, s') + \gamma \max_{a'} Q(s', a')$$

• Incorporate the new estimate into a running average:

$$Q(s,a) \leftarrow (1-\alpha)Q(s,a) + (\alpha) [sample]$$



[Demo: Q-learning – gridworld (L10D2)] [Demo: Q-learning – crawler (L10D3)]

Q-Learning Properties

- Amazing result: Q-learning converges to optimal policy -- even if you're acting suboptimally!
- This is called off-policy learning
- Caveats:
 - You have to explore enough
 - You have to eventually make the learning rate small enough
 - ... but not decrease it too quickly
 - Basically, in the limit, it doesn't matter how you select actions (!)

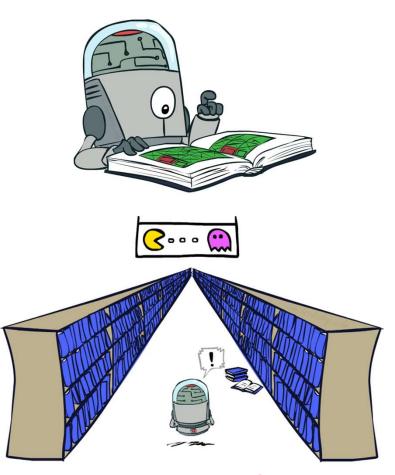


What we have learned yet

- Focused on Passive Reinforcement Learning problem
 - How to learn from already given experiences when we don't know T and R
- Saw distinction between model-based and model-free approaches to RL
 - Model-Based: Learn a model of T and R from experiences, then solve MDP
 - Model-Free: Learn from experience samples without building a model
- Direct evaluation was our first attempt at model-free value learning
 - Estimate values from samples of discounted sums of rewards: sample = $R(s) + \gamma R(s') + \gamma^2 R(s'') + ...$
 - Issue 1: Does not take advantage of state connections
 - Issue 2: Needs to see all transitions at once
- Introduced TD Learning as a way to address two issues above
 - Solution 1: Use V(s) when calculating value samples: sample = $R(s) + \gamma V^{\pi}(s')$
 - Solution 2: Use Exponential Moving Average to build up averages one transition at a time
 - New issue: TD Learning only learns state values can't use it to pick optimal actions!
- Solution is Q-Learning: learn Q values instead of V with TD-like update
 - Now can pick optimal actions, so get an optimal model-free policy

Generalizing Across States

- Basic Q-Learning keeps a table of all q-values
- In realistic situations, we cannot possibly learn about every single state!
 - Too many states to visit them all in training
 - Too many states to hold the q-tables in memory
- Instead, we want to generalize:
 - Learn about some small number of training states from experience
 - Generalize that experience to new, similar situations
 - This is a fundamental idea in machine learning, and we'll see it over and over again



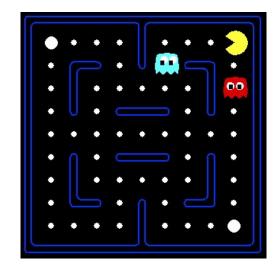
[demo – RL pacman]

Example: Pacman

Let's say we discover through experience that this state is bad: In naïve q-learning, we know nothing about this state:

Or even this one!



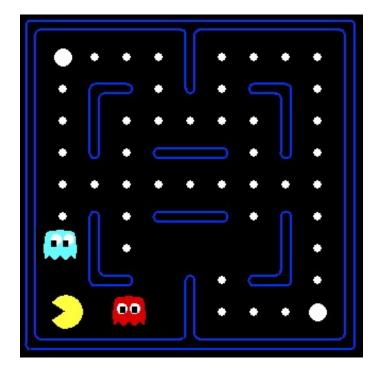




[Demo: Q-learning – pacman – tiny – watch all (L11D5)], [Demo: Q-learning – pacman – tiny – silent train (L11D6)], [Demo: Q-learning – pacman – tricky – watch all (L11D7)]

Feature-Based Representations

- Solution: describe a state using a vector of features (properties)
 - Features are functions from states to real numbers (often 0/1) that capture important properties of the state
 - Example features:
 - Distance to closest ghost
 - Distance to closest dot
 - Number of ghosts
 - 1 / (dist to dot)²
 - Is Pacman in a tunnel? (0/1)
 - etc.
 - Can also describe a q-state (s, a) with features (e.g. action moves closer to food)



Linear Value Functions

Using a feature representation, we can write a q function (or value function) for any state using a few weights:

$$V(s) = w_1 f_1(s) + w_2 f_2(s) + \dots + w_n f_n(s)$$

$$Q(s,a) = w_1 f_1(s,a) + w_2 f_2(s,a) + \dots + w_n f_n(s,a)$$

- Advantage: our experience is summed up in a few powerful numbers
- Disadvantage: states may share features but actually be very different in value!

Approximate Q-Learning

$$Q(s,a) = w_1 f_1(s,a) + w_2 f_2(s,a) + \dots + w_n f_n(s,a)$$

Q-learning with linear Q-functions:

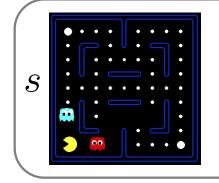
$$\begin{aligned} & \text{transition } = (s, a, r, s') \\ & \text{difference} = \left[r + \gamma \max_{a'} Q(s', a')\right] - Q(s, a) \\ & Q(s, a) \leftarrow Q(s, a) + \alpha \text{ [difference]} \end{aligned} \quad & \text{Exact Q's} \\ & w_i \leftarrow w_i + \alpha \text{ [difference]} f_i(s, a) \quad & \text{Approximate Q's} \end{aligned}$$



- Intuitive interpretation:
 - Adjust weights of active features
 - E.g., if something unexpectedly bad happens, blame the features that were on: disprefer all states with that state's features
- Formal justification: online least squares

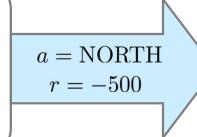
Example: Q-Pacman

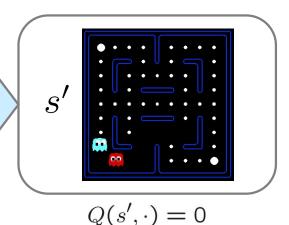
$$Q(s,a) = 4.0f_{DOT}(s,a) - 1.0f_{GST}(s,a)$$



 $f_{DOT}(s, NORTH) = 0.5$

 $f_{GST}(s, NORTH) = 1.0$





$$Q(s, NORTH) = +1$$

$$r + \gamma \max_{a'} Q(s', a') = -500 + 0$$

difference = -501
$$w_{DOT} \leftarrow 4.0 + \alpha [-501] \ 0.5$$
 $w_{GST} \leftarrow -1.0 + \alpha [-501] \ 1.0$

$$Q(s, a) = 3.0f_{DOT}(s, a) - 3.0f_{GST}(s, a)$$

[Demo: approximate Q-learning pacman (L11D10)]

Conclusion

- We're done
- We've seen how AI methods can solve problems in:
 - Search
 - Constraint Satisfaction Problems
 - Games
 - Markov Decision Problems
 - Reinforcement Learning

