

CH-8

Heteroskedasticity

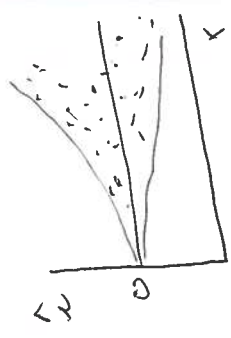
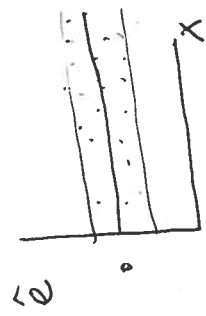
① what do we mean by heteroskedasticity or homoskedasticity?

In fact we mean heteroskedasticity of errors, i.e.,

$$Var(e_i | X) = \sigma^2 - \text{Constant}$$

→ if we plot the errors / residuals from a model,

If the case of homoskedastic error, we expect sth like:



clear pattern →
Here, as $X \uparrow$, there is a large variation in y or e .

In this context, homo - means the errors are the same / equal, while

hetero - means the errors are different.
what is the consequence of heteroskedasticity?
for the properties of least square estimators?

⇒ why do we care about heteroskedasticity? Of the well, homoskedasticity is one assumption of the Gauss-Markov assumptions. If violated, it means that our least square estimators are no longer BLUE

In particular, they are no longer best, → they are BLUE
There are other linear unbiased estimators, which have a lower sampling variance.

→ The SE for the least squares estimator are incorrect.
CI & hypothesis tests that use these SE may be misleading.

③ How do we detect the existence of heteroskedasticity?

informal theory → residual plots
formal (statistical) test

→ Goldfeld-Quandt test
→ B-P or LM test (The Lagrange multiplier)
→ white test → Breusch-Pagan test

④ What solutions do we have to fix heteroskedasticity

→ Quick & simple solution:
- use Robust standard errors (The White heteroskedasticity-consistent estimator (HCE)) → also called
→ Use better estimation techniques other than OLS
→ GLS / WLS