

# Knuth Morris Pratt Algorithm

Dr. Mattox Beckman

UNIVERSITY OF ILLINOIS AT URBANA-CHAMPAIGN  
DEPARTMENT OF COMPUTER SCIENCE

# Naïve Matching

```
0 void naiveMatching() {  
1   for (int i = 0; i < n; i++) {  
2     bool found = true;  
3     for (int j = 0; j < m && found; j++)  
4       if (i + j >= n || P[j] != T[i + j])  
5         found = false; // mismatch!  
6     if (found) // if P[0..m-1] == T[i..i+m-1]  
7       printf("P is found at index %d in T\n", i);  
8   } }
```

# Example 1

```
i 0123456789012345678901234567890123456789
T This is a test
P is a
  ^
```

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i 0123456789012345678901234567890123456789
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i 0123456789012345678901234567890123456789
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i 0123456789012345678901234567890123456789
T This is a test
P   is a
    ^
```

## Example 1

```
i 0123456789012345678901234567890123456789
T This is a test
P   is a
    *
```



## Example 1

```
i 0123456789012345678901234567890123456789
T This is a test
P   is a
    ^
```

## Example 1

```
i 0123456789012345678901234567890123456789
T This is a test
P      is a
      ^
```

## Example 1

```
i 0123456789012345678901234567890123456789
T This is a test
P      is a
      ^
```

# Example 1

```
i 0123456789012345678901234567890123456789
T aaaaaaaaaaxaaaaaaaaaaaaaaaaaaaaaaaaaaaaab
P aaaaaaaaaab
```

# The KMP Algorithm

```
i 0123456789012345678901234567890123456789
T aaaaaaaaaaxaaaaaaaaaaaaaaaaaaaaaaaaaab
P aaaaaaaaaab
  *
```

# Example 1

```
i 0123456789012345678901234567890123456789
T aaaaaaaaaaxaaaaaaaaaaaaaaaaaaaaaaaaaaaaab
P          aaaaaaaaaab
  ^
```

# The idea

P    i s \_ a  
b   -1 0 0 0

P    a a a a b b b a a a a  
b   -1 0 1 2 0 0 0 0 1 2 3

P    a a b b a a b b c c c  
b   -1 0 0 0 0 1 2 3 0 0 0

# The Code

```
0 void kmpPreprocess() {  
1   int i = 0, j = -1; b[0] = -1;  
2   while (i < m) {  
3       while (j >= 0 && P[i] != P[j]) j = b[j];  
4       i++; j++;  
5       b[i] = j;  
6 } }
```



## Code, part 2

```
0 void kmpSearch() {  
1   int i = 0, j = 0;  
2   while (i < n) {  
3       while (j >= 0 && T[i] != P[j])  
4           j = b[j]; // different, reset j using b  
5       i++; j++;  
6       if (j == m) { // a match found when j == m  
7           printf("P is found at index %d in T\n", i - j);  
8           j = b[j];  
9   } } }
```