

Palindromes

Competitive Programming

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Objectives

- ▶ Use DP to find all palindromic substrings.
- ▶ Learn the word “aibohphobia”

The Problem

Given a string s , find all the palindromic sub-strings.

- ▶ babba has three non-trivial palindromic substrings:
 - ▶ bb, abba, and bab

The algorithm

- ▶ Create a DP array $dp[|s|][|s|]$.
 - ▶ $dp[i][j]$ indicates if substring $s[i..j]$ is a palindrome.
 - ▶ Initialize diagonal to 1
- ▶ For each pair i, j , if $s[i] = s[j]$ then check if $s[i + 1..j - 1]$ is also a palindrome.
- ▶ Must iterate over smaller gap sizes first.

Code

```
1  int numPalindromes(string s) {
2      int i,j,gap,count;
3      vvb dp(s.length(),vb(s.length()),false);
4
5      count = 0;
6      for(i=0; i<s.length(); ++i)
7          dp[i][i] = true; // one character palindroms
8
9      // base case: two character palindromes
10     for(i=1; i<s.length(); ++i)
11         if (s[i-1] == s[i]) {
12             dp[i-1][i] = true;
13             ++count;
14     }
```

Code, ctd

```
15     for(gap=2; gap<s.length()-1; ++gap)
16         for(j=gap, i=0; j<s.length(); ++i, ++j)
17             if (s[i] == s[j])
18                 if (dp[i+1][j-1]) {
19                     ++count;
20                     dp[i][j] = true;
21                 }
22     return count;
23 }
```

Example

- ▶ Example for babba

Matrix

	<i>b</i>	<i>a</i>	<i>b</i>	<i>b</i>	<i>a</i>
<i>b</i>					
<i>a</i>					
<i>b</i>					
<i>b</i>					
<i>a</i>					

Action

- ▶ Start with empty matrix

Example

- ▶ Example for babba

Matrix

	<i>b</i>	<i>a</i>	<i>b</i>	<i>b</i>	<i>a</i>
<i>b</i>	1				
<i>a</i>		1			
<i>b</i>			1		
<i>b</i>				1	
<i>a</i>					1

Action

- ▶ Start with empty matrix
- ▶ Initialize diagonal

Example

- ▶ Example for babba

Matrix

	b	a	b	b	a
b	1				
a		1			
b			1	1	
b				1	
a					1

Action

- ▶ Start with empty matrix
- ▶ Initialize diagonal
- ▶ Gap = 2, bb

Example

- ▶ Example for babba

Matrix

	b	a	b	b	a
b	1		1		
a		1			
b			1	1	
b				1	
a					1

Action

- ▶ Start with empty matrix
- ▶ Initialize diagonal
- ▶ Gap = 2, bb
- ▶ Gap = 3, bab

Example

- ▶ Example for babba

Matrix

	b	a	b	b	a
b	1		1		
a		1			1
b			1	1	
b				1	
a					1

Action

- ▶ Start with empty matrix
- ▶ Initialize diagonal
- ▶ Gap = 2, bb
- ▶ Gap = 3, bab
- ▶ Gap = 4, abba