4.0-Unit Vectors

January 2, 2024

```
[1]:
    import seaborn as sns
[2]: df=sns.load_dataset('iris')
     df.head()
[2]:
        sepal_length sepal_width petal_length petal_width species
     0
                 5.1
                              3.5
                                            1.4
                                                         0.2 setosa
                 4.9
                              3.0
     1
                                            1.4
                                                         0.2 setosa
                                                         0.2 setosa
     2
                 4.7
                              3.2
                                            1.3
                 4.6
                                            1.5
     3
                              3.1
                                                         0.2 setosa
     4
                 5.0
                              3.6
                                            1.4
                                                         0.2 setosa
[3]: from sklearn.preprocessing import normalize
[5]:
    df.columns
[5]: Index(['sepal_length', 'sepal_width', 'petal_length', 'petal_width',
            'species'],
           dtype='object')
[6]: normalize(df[['sepal_length', 'sepal_width', 'petal_length', 'petal_width']])
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[7]: import pandas as pd
     pd.DataFrame(normalize(df[['sepal_length', 'sepal_width', 'petal_length', u

¬'petal_width']]),
                  columns=['sepal_length', 'sepal_width', 'petal_length', u

¬'petal_width'])
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[7]:	sepal_length	${\tt sepal_width}$	petal_length	petal_width
0	0.803773	0.551609	0.220644	0.031521
1	0.828133	0.507020	0.236609	0.033801
2	0.805333	0.548312	0.222752	0.034269
3	0.800030	0.539151	0.260879	0.034784
4	0.790965	0.569495	0.221470	0.031639
	•••	•••	•••	•••
14	5 0.721557	0.323085	0.560015	0.247699
14	6 0.729654	0.289545	0.579090	0.220054
14	7 0.716539	0.330710	0.573231	0.220474
148	8 0.674671	0.369981	0.587616	0.250281
149	9 0.690259	0.350979	0.596665	0.210588

[150 rows x 4 columns]

[]:	
[]:	
[]:	