Vector Space Model and Term Weighting

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Introduction (1/2)

Now, you are able to segment a document into a set of tokens

 Perhaps with stopword removal, stemming, lemmatization, and other normalization techniques.

It is time to turn these tokens (in a document) into numbers.

And represent a document in a continuous space upon the numbers.

Here, we present **Vector Space Model** (VSM) which has been the mainstay **text representation** for text mining algorithms.

 Also term weighting schemes are introduced to help identify words important to a particular document.

Introduction (2/2)

Specifically, we look at the following ways to represent a document.

- Frequency-based vectors vector based word counts.
- Multi-hot vectors vectors based on word absence/presence.
- TF-IDF vectors vectors based on <u>term frequency and inverse</u> <u>document Frequency</u>.

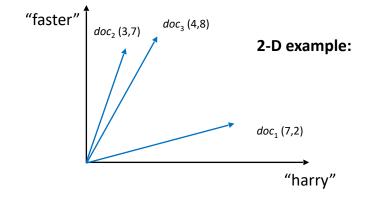
Last, vector operations are showed to measure **the similarity between documents**.

Vector Space Model (1/4)

The **dimensionality** of a vector space is <u>the</u> <u>count of the number of distinct words</u> that appear in the entire corpus.

- The number is just the **vocabulary size** |V|.
- Each dimension stands for a unique word.
- Always a high-dimensional vector space!!
 - For instance, the IMDB dataset consisting of 50K movie reviews could have more than 20K unique words!!

Each document is represented as a high-dimensional vector and the weights of words determine its location in a vector space.



Before talking about the weights and vector representation, let's review something we learned in the last chapter.

Vector Space Model (2/4)

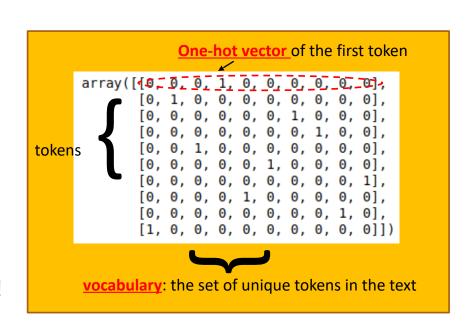
Remember the 'one-hot vectors' we created in the text-preprocessing chapter?

The one-hot vectors retain all the detail of the original document.

The document vector we are going to show compresses all detail into a single vector!!

Word order information is lost!!

Why should we do this?



Vector Space Model (3/4)

The storage require for one-hot vectors is so high!!

Say that you are going to process 3,000 documents; each of them contains 500 sentences and 15 words per sentence.

- Assuming the vocabulary size is 600,000 words, which is the word number in the Oxford English Dictionary.
- Then, each document needs 500*15=7,500 one-hot vectors.
- Or each document requires a matrix of 7,500 x 600,000 to store the one-hot information.
- That costs 4.2 GB per document (if each matrix element needs one bye) or
 536MB per document (one bit per matrix element)

Do not forget you are goinig to process 3,000 documents ...

Vector Space Model (4/4)

You certain would like to compress your document down to a single vector rather than a big table.

- That is, a high-dimensional vector in a vector space.
- Easier for text mining algorithms to work with.

Note that summarizing a document as a vector <u>loses the</u> <u>order information of tokens</u>.

• The document vector is just like a set (bag) of words; so sometimes we call vector space model the bag-of-word model.

Frequency-based Vectors (1/5)

A simple vector representation of documents is to <u>count the number of times a word in a given document</u>.

Which is also called term frequency (TF).

A document d is represented as a |V|-dimensional vector \underline{x}_d .

• A vector element $x_{t,d}$ is $tf_{t,d}$ which denotes the term frequency of t in d.

	'the'	ʻa'	'cake'	'tea'	 'dog'	'pay'	'bad'
doc_1	4	7	0	0	 5	1	3
doc_2	8	11	7	16	 1	4	0

Why term frequency?

- Intuitively, the more times a word occurs, the more meaning it contributes to that document.
- A document about airplanes should frequently refer "wings" and "flight"

Frequency-based Vectors (2/5)

```
In [1]: doc = 'The faster Harry got to the store, the faster Harry, the fater, would get home.'
 In [2]: from nltk.tokenize import word tokenize
 In [3]: tokens = word tokenize(doc)
 In [5]: stop punc = [',',';','.']
 In [6]: final tokens = [x for x in tokens if x not in stop punc]
 In [7]: final tokens
 Out[7]: ['The',
          'faster',
          'Harry',
          'got',
          'to'.
          'the',
          'store'.
          'the',
          'faster',
          'Harry',
          'the',
          'fater'
          'would',
                                                   Collections.Counter is
          'get',
          'home']
                                                   a collection, not a vector...
 In [8]: from collections import Counter
             bag of words = Counter(final tokens)
In [10]: bag of words.most common(3)
Out[10]: [('the', 3), ('faster', 2), ('Harry', 2)]
```

In this document, the most frequent (important) word is 'the' (a)

- Your can remove it by using a stopword list.
- Or, later, inverse document frequency helps reduce its impact (weight).

Generally, term frequencies need to be **normalized**.

- For two documents A and B, say the word 'dog' occur 3 times in A and 100 times in B.
- You would say 'dog' is more important to B.
- But what if A is a 30-word email and B is a 580,000-word novel?
- By normalizing, you get the relative importance to the document of that term.
 - $TF_{A,dog} = 3/30 = 0.1$ $TF_{B,dog} = 100/580000 = 0.001$

Frequency-based Vectors (3/5)

```
In [2]: print(docs)
        print(len(docs))
        ['The faster Harry got to the store, the faster and faster Harry would get home.', 'Harry is hairy and faster than
        Jill.', 'Jill is not as hairy as Harry.'
In [3]: from nltk.tokenize import word tokenize
In [4]: stop punc = [',',';','.']
In [5]: docs tokens = []
        for doc in docs:
             tokens = word tokenize(doc)
            final tokens = [x \text{ for } x \text{ in tokens if } x \text{ not in stop punc}]
             docs tokens += [final tokens]
In [6]: print(docs tokens)
        [['The', 'faster', 'Harry', 'got', 'to', 'the', 'store', 'the', 'faster', 'and', 'faster', 'Harry', 'would', 'ge
        t', 'home'], ['Harry', 'is', 'hairy', 'and', 'faster', 'than', 'Jill'], ['Jill', 'is', 'not', 'as', 'hairy', 'as',
         'Harry']]
In [7]: docs tokens[2]
Out[7]: ['Jill', 'is', 'not', 'as', 'hairy', 'as', 'Harry']
In [8]: len(docs tokens[2])
Out[8]: 7
```

Frequency-based Vectors (4/5)

```
In [9]: all docs tokens = []
In [10]: for each doc tokens in docs tokens:
              all docs tokens.extend(each doc tokens)
In [11]: all docs tokens
Out[11]: ['The',
           'faster',
           'Harry',
           'got',
           'to',
           'the',
           'store',
           'the',
           'faster',
           'and',
           'faster',
           'Harry',
           'would',
           'get',
           'home',
           'Harry',
           'is',
           'hairy',
           'and',
           'faster',
           'than'.
           'Jill',
           'Jill',
           'is',
           'not',
           'as',
           'hairy',
           'as',
           'Harry']
```

Build the vocabulary

```
In [12]: vocab = sorted(set(all_docs_tokens))
In [13]: print(vocab)
    ['Harry', 'Jill', 'The', 'and', 'as', 'fastee', 'to', 'would']
```

Construct TF vectors

Frequency-based Vectors (5/5)

```
In [17]: for i, token list in enumerate(docs tokens):
             doc len = len(token list)
             print(doc len)
             token counts = Counter(token list)
             print(token counts)
             for key, value in token counts.items():
                 TF vectors[i][vocab.index(key)] = value / doc len
         Counter({'faster': 3, 'Harry': 2, 'the': 2, 'The': 1, 'got': 1, 'to': 1, 'store': 1, 'and': 1, 'would': 1, 'get':
         1, 'home': 1})
         Counter({'Harry': 1, 'is': 1, 'hairy': 1, 'and': 1, 'faster': 1, 'than': 1, 'Jill': 1})
         Counter({'as': 2, 'Jill': 1, 'is': 1, 'not': 1, 'hairy': 1, 'Harry': 1})
In [18]: print(TF vectors.round(3))
                                          0.2
                                                0.067 0.067 0.
                                                                  0.067 0.
         [[0.133 0.
                       0.067 0.067 0.
                                                                                           Each vector needs to have 17
                       0.133 0.067 0.0671
           0.067 0.
                                                                                           values, even if the document for
          [0.143 0.143 0.
                             0.143 0.
                                          0.143 0.
                                                            0.143 0.
                                                                        0.143 0.
```

0.143 0.

[0.143 0.143 0.

0.

0.]

0.286 0.

11

So complicated ... later, we show you an easy way to construct frequency vectors

0.143 0. 0.143 0.143

that vector does not contain all

words in the vocabulary

Multi-Hot Vectors

You can generalize term frequency vectors into multi-hot vectors.

- Also called binary incidence vectors.
- Is the input of many machine learning or deep learning models (e.g., Bernoullibased Naïve Bayes Classification)

Again, each document d is represented as a |V|-dimensional vector \underline{X}_d .

• A vector element $x_{t,d}$ is 1 if term t is present in the document, otherwise, it is 0.

	'the'	ʻa'	'cake'	'tea'		'dog'	'pay'	'bad'
doc_1	1	1	0	0	•••	1	1	1
doc_2	1	1	1	1		1	1	0

Self-practice: Modify the last term frequency vector program to convert a set of documents into multi-hot vectors!!

TF-IDF Vectors (1/3)

Frequency-based vectors obviously are more informative than multi-hot vectors.

However, pure term frequency may not be able to tell you how important a word is.

Recall Zipf's Law – sparse phenomenon the word usage.



TF-IDF Vectors (2/3)

Inverse Document Frequency (IDF): measure <u>how rare a</u> word in a corpus.

$$idf_t = \log \frac{N}{df_t}$$
 the number of documents in a collection that contain term t

If a word occur many times in every document, it actually does not provide any information.

• E.g., 'term' in a set of text-mining-related documents.

Words that are not prevent across the entire corpus, but for the ones where they frequently occurred, are helpful to learn the documents.

• E.g., 'Dirichlet' often appears in documents about topic mining.

TF-IDF Vectors (3/3)

Finally, the TF-IDF weight of a term t in a document d is:

• tf- $idf_{t,d} = tf_{t,d} \times idf_t$

The weight of term *t* in document *d* is **high**, when *t* occurs many times in *d* and appears within a small number of documents.

What about **stop words** that occurs in every document?

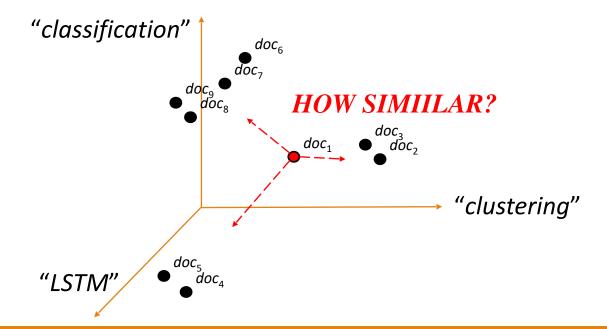
- The TF-IDF weights of them in the document would be ... (almost) zero.
- This helps identify the core (keywords) of a document.



Comparing Document Vectors (1/3)

You have represented documents as vectors sharing a common vector space.

It is time to compare them!!



Comparing Document Vectors (2/3)

Two popular measures for calculating the similarity/distance between vectors:

Euclidean distance between document d_i and d_j :

$$\left| \underline{x}_i - \underline{x}_j \right| = \sqrt{\sum_{t=1}^{M} (x_{t,i} - x_{t,j})^2}$$

- Note the distance is <u>sensitive to document length!!</u>
 - Normalize vectors if you want to lessen the effect of document length.
 - Using normalized TF, or normalize vectors to their unit vectors.

Comparing Document Vectors (3/3)

Cosine similarity between document d_i and d_i :

$$cosine\left(\frac{x_{i}, x_{j}}{x_{i}}\right) = \frac{\frac{x_{i} z_{i}}{|x_{i}|} \frac{x_{i}}{|x_{j}|}$$

$$= \frac{\sum_{t=1}^{M} (x_{t,i} * x_{t,j})}{\sqrt{\sum_{t=1}^{M} (x_{t,i} * x_{t,i})^{2}} \sqrt{\sum_{t=1}^{M} (x_{t,j} * x_{t,j})^{2}}$$

- Cosine automatically normalize document vectors to their unit vectors, then do dot product of the normalized vectors.
- The range of cosine similarity is [-1, 1]
 - But ... if your are using frequency-based term weights, the range would always be [0, 1].
 - ° Close to 1 when two documents are using similar words in similar proportion.
 - ∘ 0 also called orthogonal, if two documents share no words in common; <u>but is possible that they have similar meaning</u>.

Ease Your Life with Packages

Many packages are readily available to help us turn documents into vectors.

Also, functions of cosine similarity and Euclidean distance are provided to compare the resulting vectors!!

Do it with sklearn ©



CountVectorizer TF/Multi-Hot Vectors

```
In [2]: docs
Out[2]: ['The faster Harry got to the store, the faster and faster Harry would get home.',
        'Harry is hairy and faster than Jill.',
        'Jill is not as hairy as Harry.']
In [3]: from sklearn.feature extraction.text import CountVectorizer
In [4]: TF vectorizer = CountVectorizer()
In [5]: TF vectors = TF vectorizer.fit transform(docs)
In [6]: TF vectorizer.get feature names()
Out[6]: ['and',
        'as',
        'faster',
        'get',
        'got',
                                                      In [13]: binary vectorizer = CountVectorizer(binary=True)
        'hairy',
        'harry',
        'home',
                                                      In [14]: binary vectors = binary vectorizer.fit transform(docs)
        'is',
        'jill',
        'not',
                                                      In [15]: print(binary vectors.toarray())
        'store',
        'than',
        'the',
                                                                 [[1011101100010111]
        'to'.
                                                                  [1010011011001000]
        'would']
                                                                  [0 1 0 0 0 1 1 0 1 1 1 0 0 0 0 0]]
In [7]: print(TF vectors.toarray())
       [[1031102100010311]
        [1010011011001000]
        [0 2 0 0 0 1 1 0 1 1 1 0 0 0 0 0]]
```

TfidfVectorizer TF-IDF Vectors

```
In [17]: from sklearn.feature extraction.text import TfidfVectorizer
In [18]: TFIDF vectorizer = TfidfVectorizer()
In [19]: TFIDF vectors = TFIDF vectorizer.fit transform(docs)
In [20]: print(TFIDF vectors.toarray())
         [[0.1614879 0.
                               0.48446369 0.21233718 0.21233718 0.
           0.25081952 0.21233718 0.
                                                               0.21233718
                     0.63701154 0.21233718 0.21233718]
          [0.36930805 0.
                               0.36930805 0.
                                                               0.36930805
           0.28680065 0.
                               0.36930805 0.36930805 0.
          0.48559571 0.
                                          0.
                                Θ.
          [0.
                     0.75143242 0.
                                                               0.28574186
           0.22190405 0.
                               0.28574186 0.28574186 0.37571621 0.
           0.
                     0.
                               Θ.
                                          Θ.
```

Cosine Similarity & Euclidean Distance

Parameters When Creating Vectorizer

Useful parameters when creating CountVectorizer **and** TfidfVectorizer

- lowcase: Convert all characters to lowercase before tokenizing, default is true
- o stop_words: default = None, or stop_words = 'English'
- max_df: remove terms whose document frequencies are higher than the given threshold
- min_df: remove terms whose document frequencies are lower than the given threshold